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A Physically Based Subgrid Parameterization for the Production and Maintenance of Mixed-Phase Clouds in a General Circulation Model

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ABSTRACT

A physically based method for parameterizing the role of subgrid-scale turbulence in the production and maintenance of supercooled liquid water and mixed-phase clouds is presented. The approach used is to simplify the dynamics of supersaturation fluctuations to a stochastic differential equation that can be solved analytically, giving increments to the prognostic liquid cloud fraction and liquid water content fields in a general circulation model (GCM). Elsewhere, it has been demonstrated that the approach captures the properties of decameter-resolution large-eddy simulations of a turbulent mixed-phase environment. In this paper, it is shown that it can be implemented in a GCM, and the effects that this has on Southern Ocean biases and on Arctic stratus are investigated.

1. Introduction

Mixed-phase and supercooled liquid water clouds are known to be difficult to represent in numerical weather prediction (NWP) and climate models. This has been implicated as a potential cause of serious model biases. For example, many of the IPCC models exhibit large sea surface temperature biases over the Southern Ocean. This adversely affects the global circulation and leads to difficulties in simulations of the cryosphere, such as underestimation of the extent of Antarctic sea ice. Given the critical role of the Southern Ocean for energy and carbon uptake, deep-water mass formation, and climate sensitivity, alleviation of these biases is seen as a priority for climate prediction (Rintoul 2011). Southern Ocean surface temperature biases are accompanied by a bias in the shortwave (SW) radiation reflected to space by clouds (Bodas-Salcedo et al. 2014), the most likely cause of which is insufficient amounts of model supercooled liquid water.

Similar problems have been identified in the simulation of Arctic climates. In a study of Arctic stratus clouds, Klein et al. (2009) showed that many models have significant surface radiation biases that are linked to the determination of the phase of the condensate.

Hypotheses exist for why models struggle to represent mixed-phase clouds [see Klein et al. (2009) for a review]. For example, Forbes and Ahlgrimm (2014) incorporated the subgrid vertical structure of mixed-phase clouds into a general circulation model (GCM) by making microphysical process rates depend directly on the distance from cloud top. Another suggestion (e.g., Korolev and Field 2008) is that small-scale turbulence plays a role by driving fluctuations in relative humidity that lead to the condensation of liquid water. In competition with this effect is the depositional sink of water vapor to the ice phase, which acts to damp out humidity fluctuations. If real-world mixed-phase clouds owe their longevity to the interplay of these processes, then their accurate parameterization in numerical models becomes important because, as a result of computational constraints, GCMs cannot resolve small-scale variability. Indeed, at climate model resolutions, subgrid humidity variability (due to unresolved eddy motions) must ultimately account for the majority of liquid water formation, and it is the long-recognized goal of GCM cloud schemes to parameterize this condensation pathway in terms of the resolved model variables.

In this paper, we will consider how turbulence forms and maintains mixed-phase clouds and propose a method for including these effects in numerical models. Our approach originates in the study by Field et al. (2014, hereafter F14), who proposed an analytically soluble model of mixed-phase cloud dynamics based on a stochastic differential equation for supersaturation fluctuations. Their

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model gave the liquid cloud properties in terms of the local turbulence and the properties of any preexisting ice cloud and agreed well with the results of decameter-scale large-eddy simulations.

Broadly speaking, F14 sought to address the following question: given the turbulent and ice microphysical state of a preexisting ice cloud, can the liquid phase properties be determined analytically from the underlying dynamical equations? Although their approach was initially used to analyze mixed-phase environments, it naturally contains the ice-free limit as a special case and can therefore be applied to predict liquid condensation from clear-sky conditions at any temperature.

To describe the turbulence, F14 used the turbulent kinetic energy (TKE) and dissipation rate. They also accounted for mixing of environmental air into cloudy regions, modeled via the mixing length over which turbulent transport occurred. Ice effects were included via the phase-relaxation time scale, characterizing the rate at which the conditions in a fluid parcel attain ice saturation. It was shown that the above parameters completely specify the steady-state probability density function (PDF) of supersaturation fluctuations inside an air volume. This PDF can then be inspected to obtain the liquid cloud properties, which appear naturally as truncated PDF moments.

In this paper, we will use the F14 method to develop a parameterization of subgrid liquid water cloud production for use in a GCM. In each model grid box, the analytical solution of F14 will be applied to diagnose the liquid cloud properties from the gridbox-mean variables. Closure relations will be introduced to obtain the turbulence information needed to determine the subgrid statistics. The effect of the parameterization on Southern Ocean radiative biases and simulations of Arctic stratus clouds will then be considered.

2. Model description and implementation

The starting point for the study by F14 is a modified form of the linearized Squires equation for the supersaturation S_i with respect to ice:

$$\frac{dS_i}{dt} = -\frac{S_i}{\tau_p} - \frac{S_i - S_E}{\tau_E} + a_i w, \quad (1)$$

where d/dt is the Lagrangian time derivative, w is the turbulent vertical velocity, τ_p is the phase-relaxation time scale, S_E is the environmental supersaturation with respect to ice, τ_E is a mixing time scale, and a_i is a function of temperature (see the appendix).

The standard version of Squires equation is obtained from Eq. (1) by omitting the term $(S_E - S_i)/\tau_E$. F14 added this term to model the exchange of air parcels

between a turbulent zone of depth ℓ_E and its surroundings. The time needed for homogenization by turbulent diffusion over this length scale is given by

$$\tau_E = \left(\frac{\ell_E^2}{\epsilon} \right)^{1/3}, \quad (2)$$

where ϵ is the turbulent dissipation rate.

To include the effects of turbulence, F14 modeled w as Gaussian white noise with variance σ_w^2 and autocorrelation

$$\langle w(t_1)w(t_2) \rangle = \sigma_w^2 \tau_d \delta(t_1 - t_2), \quad (3)$$

where δ is the Dirac distribution, and τ_d is the Lagrangian decorrelation time scale, characterizing vertical velocity correlations along fluid parcel trajectories. Throughout this paper, we will use angle brackets to denote ensemble averages over realizations of w .

For homogeneous, isotropic, stationary turbulence, it is known that

$$\tau_d = \frac{2\sigma_w^2}{\epsilon C_0}, \quad (4)$$

where C_0 is an empirical constant (Rodean 1997).

The effects of ice enter via the phase relaxation time scale, which is defined by

$$\tau_p = \frac{1}{b_i B_0 \mathcal{M}_1}, \quad (5)$$

where \mathcal{M}_1 is the first moment of the ice particle size distribution, and b_i and B_0 are functions of temperature given in the appendix.

Equation (1) can be solved analytically for the statistics of S_i . In particular, it can be shown that the steady-state PDF $F(S_i)$ of S_i is Gaussian with variance σ_S^2 and mean $\langle S_i \rangle$, given by

$$\sigma_S^2 = \frac{(1/2)a_i^2 \sigma_w^2 \tau_d}{1/\tau_p + 1/\tau_E} \quad \text{and} \quad (6)$$

$$\langle S_i \rangle = S_E \frac{1/\tau_E}{1/\tau_p + 1/\tau_E}. \quad (7)$$

The liquid cloud fraction ϕ and mean liquid water mass mixing ratio $\langle q_l \rangle$ are given by the following truncated moments of the S_i PDF:

$$\phi = \int_{S_{iw}}^{\infty} ds F(s) \quad \text{and} \quad (8)$$

$$\langle q_l \rangle = \int_{S_{iw}}^{\infty} ds q_{sl}(s - S_{iw}) F(s), \quad (9)$$

where S_{iw} is the value of the ice supersaturation in water-saturated conditions, and q_{si} is the saturated mass mixing ratio of water vapor in air with respect to ice. We note that the integrals in Eqs. (8) and (9) can be performed analytically.

a. Underlying assumptions

In this section, we revisit the derivation of the F14 model to highlight the assumptions on which it is based. The premise of the model is that the cloud liquid water content can be deduced by inspecting the PDF of ice supersaturation in the absence of liquid condensate. However, we propose that it can also be used to represent the supersaturation dynamics once an air parcel becomes mixed phase.

Diagnosing liquid cloud properties from the PDF of S_i is possible because of the dynamical equivalence between the water vapor mixing ratio q_v in a system without liquid water and $q_v + q_l$ in a system that includes a mass q_l of liquid water per unit mass of dry air. To make this more precise, let us define the liquid water supersaturation with respect to ice η_i to be

$$\eta_i = \frac{q_v + q_l}{q_{si}(p, T_l)} - 1, \tag{10}$$

where $T_l = T - L_v q_l / c_p$ is the liquid water temperature of the system, and T and p are the air temperature and pressure.

It can be shown that, for temperatures below 0°C, the dynamical equation for η_i can be obtained from Eq. (1) by substituting η_i in place of S_i . In other words, η_i evolves according to the same equation as does S_i in the absence of liquid water. Hence, the results of F14 can be interpreted as giving analytical expressions for the PDF of η_i .

Note that for $T > 0^\circ\text{C}$, we can modify the definition of η_i by replacing q_{si} with its liquid water counterpart q_{sw} . Dynamically, the resultant quantity is still equivalent to S_i if L_v is substituted for L_s in the definitions of a_i , b_i , and B_0 .

F14 compared S_i with S_{iw} to determine the threshold for liquid water condensation. However, the exact criterion for condensation of liquid water is

$$\eta_i > \frac{q_{sw}(p, T)}{q_{si}(p, T_l)} - 1, \tag{11}$$

which necessarily involves q_l via the liquid water temperature. This induces an inconvenient circularity: one cannot diagnose the presence of liquid water without already knowing the value of q_l .

However, the right-hand side of inequality (11) is approximately $S_{iw}(p, T)$ if q_l is sufficiently small. This suggests that the model of F14 applies only in situations

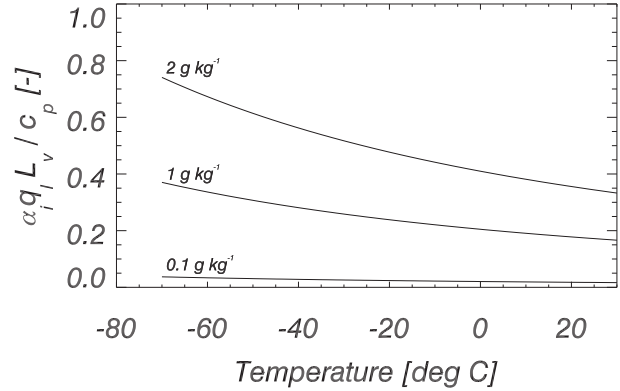


FIG. 1. An evaluation of the range of validity of the small q_l approximation, whereby the effects of latent heating on q_{si} can be neglected. The curves show the quantity $\alpha_i L_v q_l / c_p$ as a function of temperature for a range of q_l values.

where latent heating due to liquid condensation can be neglected. This is equivalent to introducing the following approximation:

$$\alpha_i \frac{L_v}{c_p} q_l = \frac{L_v L_s q_l}{c_p R_v T^2} \ll 1, \tag{12}$$

where $\alpha_i = \partial \ln q_{si} / \partial T$ (see the appendix for a complete nomenclature of symbols); that is, the fractional change in q_{si} due to latent heating is small. We will call condition (12) the small q_l approximation. Figure 1 gives an indication as to its range of validity. The parameterization implemented here is most active for temperatures warmer than -15°C and typically gives condensation increments in the range 0.1–0.5 g kg^{-1} . From Fig. 1, this corresponds to errors of around 10%; however, this is lower (e.g., 5%) for cold clouds.

We can then identify the subset of phase space that corresponds to nonzero q_l as approximately those points for which

$$\eta_i > S_{iw}(p, \langle T \rangle), \tag{13}$$

where we have made the further assumption that T can be replaced with its mean value $\langle T \rangle$. [Note that, for temperature fluctuations on the order of $L_v \langle q_l \rangle / c_p$, this follows from Eq. (12).]

Furthermore, the amount of liquid water present at any one of these phase points is

$$q_l = q_{si}(p, \langle T \rangle) [\eta_i - S_{iw}(p, \langle T \rangle)]. \tag{14}$$

Condition (13) and Eq. (14) correspond to the model of F14 for temperature below 0°C. For temperatures above 0°C, Eqs. (13) and (14) continue to hold, provided one substitutes q_{sw} for q_{si} , thereby setting $S_{iw} = 0$.

In this paper, we interpret the F14 model as giving PDFs of the humidity variable η_i . The above small q_l approximation can then be used to predict mean liquid water mass mixing ratio $\langle q_l \rangle$ and cloud fraction ϕ . As inputs, the model requires the parameters needed to specify the η_i PDF, along with the values p and $\langle T \rangle$.

b. Closure relations

To implement the model in a GCM, closure relations are required for the parameters that determine the supersaturation distribution in each model grid box. We recall that the following variables are required: the vertical velocity variance σ_w^2 , the eddy dissipation rate ϵ , the turbulent mixing length ℓ_E , the turbulent decorrelation time scale τ_d , and the supersaturation S_E of the air entrained from the surroundings. In addition, we must specify the mean values of p and T for the state of the subgrid model. These latter two quantities we will take to be equal to the resolved values in the grid box: $\langle T \rangle = \bar{T}$ and $p = \bar{p}$. We use an overbar for gridbox-mean quantities.

Consistency between the closure relations requires that Eq. (4) hold for τ_d . In addition, we choose to impose the constraint that

$$\ell_E = \tau_d \sigma_w. \quad (15)$$

This equation states that the turbulent mixing length is the typical decorrelation length scale of the unresolved eddies.

In the Met Office Unified Model, σ_w^2 is a diagnostic from the boundary layer scheme, although it is available at all altitudes. In regions where σ_w^2 is small, the subgrid PDF is very narrow, and no liquid water is produced. The scheme is therefore able to produce liquid cloud at any altitude where sufficient turbulence is diagnosed, although in practice its effects are largest in the boundary layer where σ_w^2 is large. By construction, the TKE diagnostic is zero in regions of deep convection.

We impose the constraint that the unresolved motions are similar in vertical extent to the gridbox depth Δ_z . Hence, the mixing length $\ell_E = \beta_1 \Delta_z$, where β_1 is a proportionality constant. We will take β_1 to be an adjustable tuning parameter, subject to the constraint that it should be of order 1. In physical terms, we therefore have in mind an ensemble of subgrid-scale motions (eddies), each driven by an independent random realization of the subgrid noise w and making excursions that are on the order of gridbox depth. In this paper, we choose $\beta_1 = 2$.

Using Eqs. (2) and (4) and the eddy size constraint equation [Eq. (15)], we obtain closed expressions for τ_d and τ_E :

$$\tau_d = \frac{\beta_1 \Delta_z}{\sigma_w} = \beta_2 \tau_E, \quad (16)$$

where $\beta_2 = (2/C_0)^{1/3}$. Following F14, we will set $C_0 = 10$ [Rodean (1997) states that estimates are in the range 0.6–10; see F14 for a detailed discussion]. Using Eq. (16), we can diagnose the dissipation rate ϵ from Eq. (4).

The phase-relaxation time scale τ_p is calculated using Eq. (5) with the gridbox-mean values \bar{T} and \bar{p} and first moment of ice particle size distribution \mathcal{M}_1 from the cloud microphysics scheme. The environmental supersaturation S_E is assumed to be the gridbox-mean supersaturation \bar{S}_i . We note that the turbulent cloud production scheme does not change the amount of ice in a grid box: rather, it uses information about pre-existing ice to determine how much liquid water condensation occurs. The growth of ice from vapor occurs only in a cloud microphysics scheme. Hence, although this condensation mechanism and the cloud microphysics scheme both deplete q_v , this depletion represents different processes in the two schemes.

Using these closures in Eqs. (6) and (7) gives the following expressions for σ_S^2 and $\langle S_i \rangle$:

$$\sigma_S^2 = \frac{(1/2)a_i^2 \beta_1 \sigma_w \Delta_z}{b_i B_0 \mathcal{M}_1 + \gamma \sigma_w / \Delta_z} \quad \text{and} \quad (17)$$

$$\langle S_i \rangle = \frac{\gamma \sigma_w \bar{S}_i / \Delta_z}{b_i B_0 \mathcal{M}_1 + \gamma \sigma_w / \Delta_z}. \quad (18)$$

where it is convenient to define a constant $\gamma = \beta_2 / \beta_1$.

Two limiting cases are of interest:

- (i) *Microphysics dominated*: $\tau_p \ll \tau_E$. In this case, σ_S and $\langle S_i \rangle$ tend to zero. In the presence of large amounts of ice, the supersaturation distribution becomes very sharply peaked around ice saturation.
- (ii) *Entrainment dominated*: $\tau_E \ll \tau_p$. In this case,

$$\sigma_S \sim a_i \Delta_z, \quad \langle S_i \rangle \sim \bar{S}_i. \quad (19)$$

In the presence of rapid entrainment from the environment, the cloud layer quickly homogenizes to the humidity of the environment, and the supersaturation fluctuations are determined by the vertical extent of the turbulent excursions.

c. Incrementing model prognostics

The most prosaic way of implementing the scheme is to use the values calculated from Eqs. (8) and (9) to increment the GCM prognostics for \bar{q}_i , \bar{q}_v , \bar{T} , and ϕ . For example, if the turbulent cloud production parameterization diagnoses a liquid water content $\langle q_l \rangle$ in a grid box that already contains an amount of liquid

\bar{q}_l , then the resultant increment to the gridbox-mean value is

$$\Delta\bar{q}_l = \langle q_l \rangle - \bar{q}_l, \quad (20)$$

together with a compensating change in the water vapor prognostic and an amount of latent heating $L_v\Delta\bar{q}_l/c_p$. However, applying the same recipe to cloud fraction increments leads to the following inconsistency with the GCM macroscale cloud scheme.

Underlying the Unified Model macroscale cloud scheme [prognostic cloud fraction and prognostic condensate (PC2) scheme; Wilson et al. 2008] is an implicit PDF for subgrid moisture variability. To initialize the liquid cloud fields away from states with zero cloud fraction, the PC2 scheme uses a diagnosed PDF width based on the vertical profile of an adjustable parameter: the critical relative humidity (RH_c). This diagnosed profile represents the PDF widths at the onset of cloud formation. An equivalent approach is used to initialize the liquid cloud fields away from totally overcast states by breaking up overcast skies when the gridbox-mean total relative humidity falls below $2 - RH_c$.

Care must therefore be taken with any parameterization that can add significant amounts of cloud fraction to the model. Suppose a parameterization elevates the cloud fraction to $\phi = 1$ in a grid box that is then diagnosed by the PC2 scheme to meet the criteria for initialization away from overcast skies. The PC2 initialization parameterization will then remove some of the additional cloud fraction, almost immediately counteracting the desired tendency toward greater cloudiness.

This situation essentially arises because the turbulent production parameterization and the PC2 initialization scheme have conflicting definitions of the critical relative humidity. We must therefore adopt a method that calculates ϕ increments that are consistent with both the turbulence-based scheme and the underlying PC2 cloud scheme.

One such method is the following. The increments to \bar{q}_l are determined by the turbulent production mechanism [i.e., from Eq. (9)] using the recipe given above. The cloud fraction increment, however, is not found from Eq. (8). Instead, we use available resolved-scale information to determine a ϕ increment that is consistent with the current state of moisture PDF from the PC2 cloud scheme. To do this, we use the fact that, as shown in Morcrette (2012), changes in ϕ and \bar{q}_l can be related by

$$\Delta\phi = \frac{Q_c G(-Q_c)}{\phi Q_c - \bar{q}_l} \Delta\bar{q}_l, \quad (21)$$

where G is the subgrid moisture PDF in the macroscale cloud scheme, and Q_c is the boundary between

the saturated and unsaturated parts of the moisture PDF.

The ϕ increments determined in this way will be consistent with the underlying subgrid variability that is implicit in the PC2 cloud scheme [via the parameterization of $G(-Q_c)$]. As a consequence, the RH_c -based, PC2 initiation scheme is inhibited from counteracting the turbulence-driven scheme. In addition, we note that the structure of the PC2 code prevents PC2 initiation from initializing more cloud in grid boxes that already contain liquid water. Hence, in the regions with significant TKE, the turbulent production scheme overrides PC2 initiation as the main condensation pathway.

Figure 2a shows a typical global σ_w^2 field from a low-resolution global model a couple of hours into the simulation at a height of 1 km. Figures 2b and 2c show the associated increments of \bar{q}_l and ϕ . It can be seen that the liquid cloud increments are located in the turbulent regions. More intense turbulence tends to imply larger cloud increments. However regions of high σ_w^2 with little liquid cloud produced can also be identified. This occurs when the gridbox-mean state is too dry for the parameterized subgrid motions to produce liquid water (e.g., over Australia).

Note that, in Figs. 2b and 2c, orange is used to denote grid boxes where the cloud increments are below the lower limit of the color scale. Hence, in Fig. 2b, orange regions show the (relatively infrequent) occurrence of negative \bar{q}_l increments. This happens where the scheme diagnoses less liquid condensate than is already present in the model grid box. Similarly, in Fig. 2c, orange denotes regions where the cloud fraction decreases as a result of the scheme. This occurs because, as noted in Wilson et al. (2008), Eq. (21) does not constrain $\Delta\phi$ to be positive for positive $\Delta\bar{q}_l$ if the grid box is moist enough. Typically, however, we have found $\Delta\phi$ to be small (greater than -0.05) when negative.

3. NWP simulations

a. Comparison to AMSR

We compare the results of global NWP simulations to satellite observations of liquid condensate path from the Advanced Microwave Scanning Radiometer (AMSR). The AMSR-E (version 7) 3-day composite global scenes from the 6-day period ending at 0000 UTC 24 September 2011 were compared to 6-h-mean model output over the same period (Wentz et al. 2014). The NWP model used is the Met Office Unified Model at N512 horizontal resolution (25-km midlatitude grid spacing) with 70 vertical levels (L70). The control is a development configuration of the Unified Model similar to the Met Office Global Atmosphere 6.1 (GA6) configuration

At 02Z on 1/9/1988, from 00Z on 1/9/1988

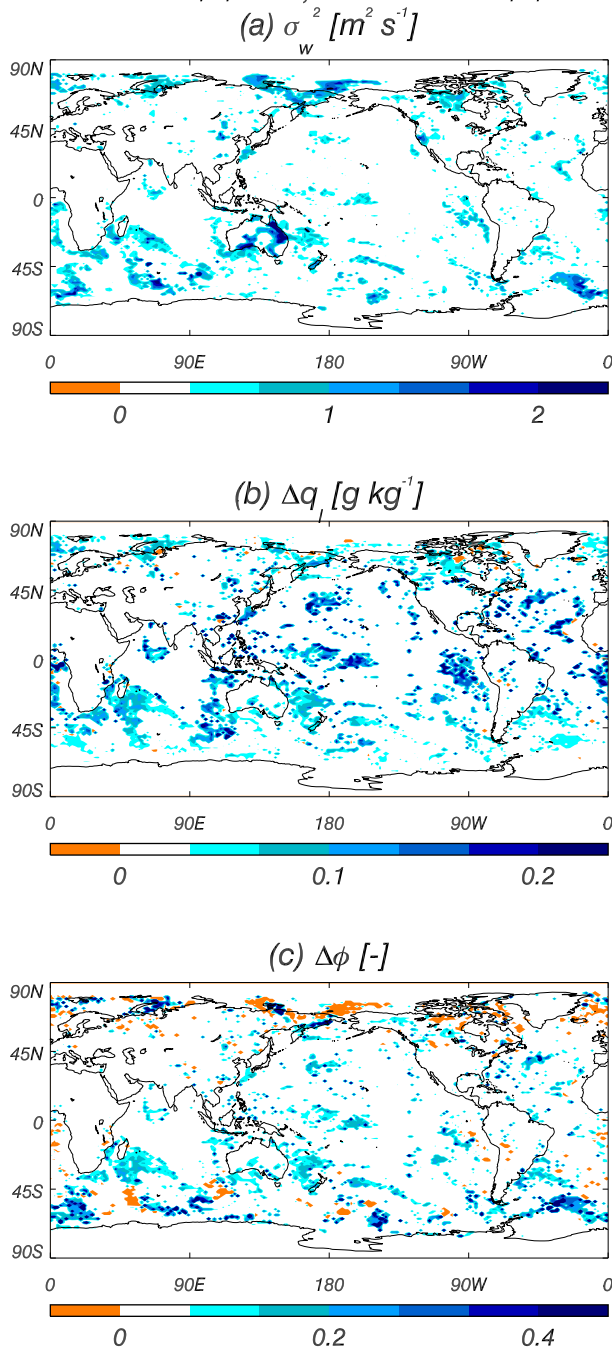


FIG. 2. Instantaneous global fields at a height of 1120 m above the surface, 2 h into an N96L70 (130-km horizontal grid spacing, 70 vertical levels) global simulation. (a) The variance of the turbulent vertical velocity, diagnosed by the boundary layer scheme; (b) liquid water mass mixing ratio increment produced by the scheme; and (c) liquid cloud fraction increment produced by the scheme.

described by D. N. Walters et al. (2015, unpublished manuscript). We test the effect of adding the turbulent cloud production parameterization to this model. To determine the model liquid water paths, we sum contributions from the model large-scale (stratiform) cloud and convection schemes.¹

AMSRE provides cloud water path and surface rain rate products that are interrelated by the algorithm described in Hilburn and Wentz (2008). If a drop size distribution and fall speed–size relation are assumed for rain, then the algorithm can be inverted to obtain an estimate of the total liquid water path (LWP). Here, we have assumed the fall speed relation according to Sachidananda and Zrnić (1986) and the particle size distribution from Abel and Boutle (2012).

Figure 3a compares the zonal- and time-averaged AMSR-E liquid water path (red line) to the model predictions. The line-filled regions show the envelopes of zonally averaged model LWP. AMSR observations are not available over land or sea ice, and the model has therefore been filtered to correspond with the AMSR data mask.

South of 50°S and in the Arctic, the control model (black-lined region) underpredicts the LWP. Including the turbulent production parameterization (green-lined region) increases the LWPs and goes some way to addressing this bias. Note that the latitudinal coverage of the comparison is limited by the extent of the polar sea ice. In the tropics and subtropics, however, the experiment overpredicts the LWP. In fact, away from the polar regions, the control model agrees reasonably well with the observations.

Only the model large-scale cloud-scheme LWP is directly affected by the turbulent production mechanism. Figure 3b shows that the parameterization increases the model large-scale LWP by approximately 50%.

Increasing the stratiform cloud LWP will cause more SW radiation to be reflected back to space. Over the Southern Ocean, this effect is beneficial because the Unified Model has a large negative bias in outgoing SW radiation in that region (Bodas-Salcedo et al. 2014). Similarly, the increase in Arctic LWP will enhance the surface downwelling longwave (LW) flux, which is also negatively biased in the control model.

The extra stratiform tropical and subtropical LWP is not beneficial and leads to a positive bias in reflected SW over the tropics. There are several possible reasons for

¹ The convective cloud water content is derived as a product of the convective cloud condensate amount and a convective cloud fraction diagnostic. The convective rain contribution has to be calculated from the convective rain rate by assuming a size distribution and fall speed. For this, the same modeling assumptions were made as for the AMSR-E data.

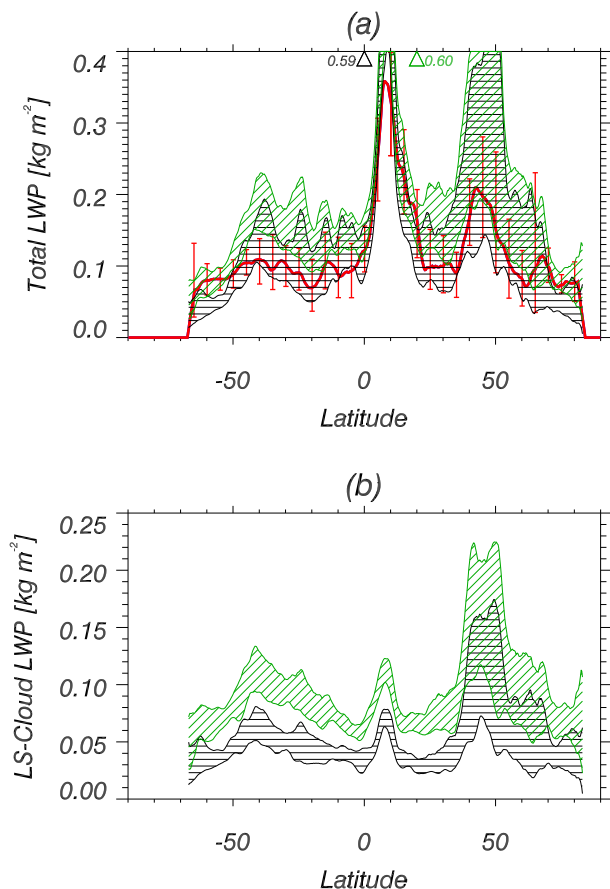


FIG. 3. Comparison of model LWPs to AMSR-E. (a) Total LWP, all cloud types. (b) Model large-scale (stratiform) cloud LWP (excluding large-scale rain and convective condensate). In (a), the red line shows the zonal and time average of the AMSR-E observations for the 6-day period ending 24 Sep 2011. The line-filled envelopes show model LWP ranges for the same period for the control (black) and experiment (green) configurations. The vertical red bars show the range of AMSR-E observations.

this. First, there may be flaws in the parameterization, either because of simplifications in the F14 model itself, or because of the closure relations used in this implementation. Second, there are uncertainties in the way in which liquid water paths are estimated from the model convection scheme and the AMSR surface rain rates. In addition, other sources of model error may be complicating the comparisons. For example, the model may contain too much rainwater.

Third, it is known that the control model possesses a good representation of subtropical/tropical cloud compared with other models (Wyant et al. 2010). Parameterizing a previously unrepresented pathway to cloud formation, as has been done here, may therefore be likely to degrade the model for warm clouds simply because the model is already in a relatively acceptable state. This would suggest that

weaknesses in warm clouds could be remedied by tuning parameterizations as part of a much broader model development activity.

By contrast, for cold clouds, the control model is sub-optimal with respect to cloud phase, as evidenced by Fig. 3 and the large Southern Ocean radiative biases. This is because existing PC2 processes are not providing a significant source of liquid water within cold clouds. We argue that this is precisely because they do not represent the main pathway to cold-cloud formation: namely, inhomogeneous condensation in response to small-scale turbulent fluctuations.² Hence, by adding this process, there is considerable scope to improve the representation of cold clouds.

Finally, perhaps the scheme leads to processes being overparameterized, in the sense of their being handled by two separate parameterizations. This, however, should not be the case. The method described in section 2c prevents any inconsistency with the PC2 initiation parameterization (which does not act if the turbulence-based scheme has done so). In addition, there should be no overlap of physical processes between the current scheme and other PC2 source terms, since the latter either are homogeneous forcings in response to spatially uniform cooling or humidification, without change to the underlying PDF shape (e.g., boundary layer scheme increments) or are caused by manifestly different physics (e.g., convective detrainment).

In summary, we are left with a need for a pragmatic way of retaining the benefit of more LWP at high latitudes, but without the detrimental effects in the subtropics. To this end, we choose to implement the turbulent cloud production mechanism only in grid boxes where the temperature is below 0°C. We revisit this issue in the context of climate simulation in section 4.

b. M-PACE simulations

We consider the effect of the turbulent cloud production parameterization on NWP simulations of the Mixed-Phase Arctic Cloud Experiment (M-PACE) flying period (Klein et al. 2009). M-PACE was an aircraft campaign with coincident ground-based measurements, which took place over Barrow in northern Alaska in October 2004. The observations show a stratiform mixed-phase cloud deck underlying a weak inversion at a height of around 1.5 km and descending to 0.5 km from the surface. In situ measurements showed the vertical profile of liquid water content increasing toward the cloud top, which had a typical temperature of -15°C. Below the mixed-phase layer, snowfall was recorded that extended down to the surface.

²The only PC2 process that does try to represent this process is PC cloud initiation, but it appears that this alone is not currently sufficient.

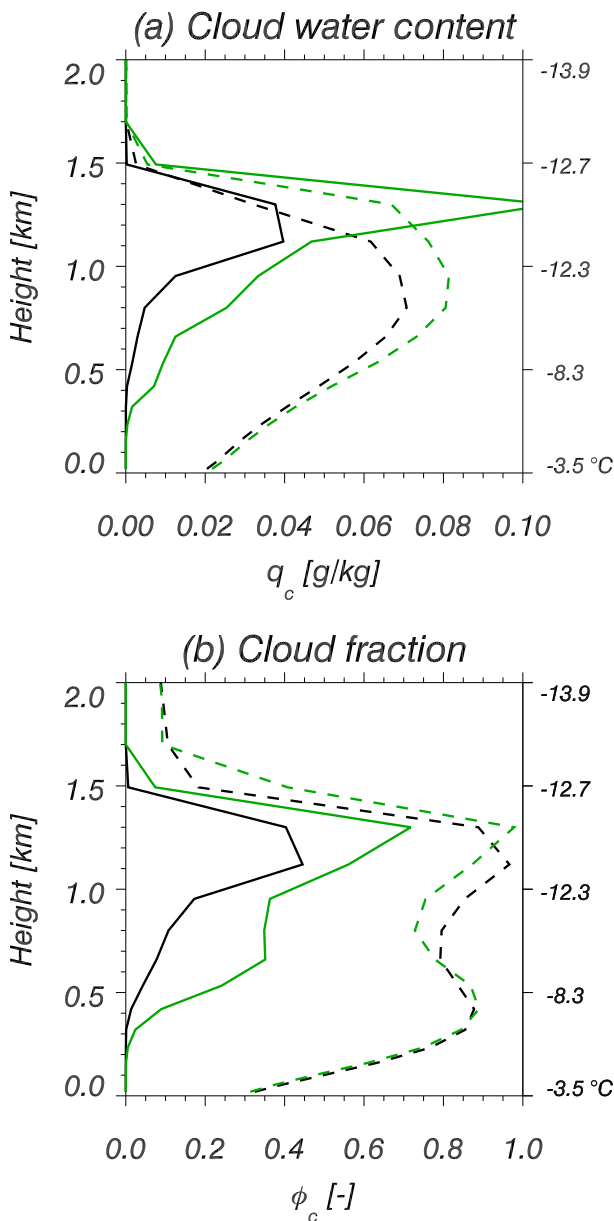


FIG. 4. Vertical profiles of (a) gridbox-mean condensed water content for liquid (solid lines) and ice (dashed lines), and (b) cloud fraction ϕ_c of liquid (solid lines) and ice (dashed lines) along a cross section through the target region, around Barrow on the North Slope of Alaska, for the two N512 global model forecasts. The fields are averaged along a transect joining 70.51°N, 149°W and 71.3°N, 157°W for a 12-h time interval. The black lines are for the control model, and the green lines are for the experiment.

Figure 4 shows the changes in the mean vertical liquid cloud profiles along a cross section through the target area. The transect chosen for the cross section joins the Barrow Atmospheric Radiation Measurement (ARM) Program site in the northwest to Oliktok Point, approximately 300 km to the southeast, and corresponds

closely to the flight path of the aircraft during the experiment. The left-hand-side vertical axes in Fig. 4 show height above the surface. The profiles are means constructed from hourly model outputs over a 12-h period beginning at 1700 UTC 9 October 2004. The model used is the N512 global model described in section 3a. Initial conditions were prescribed at 0000 UTC 9 October, using an ECMWF analysis.

Profiles from two model runs are plotted in Fig. 4. The control model, shown by the black lines, is compared to an experiment that includes the turbulent cloud production parameterization. The solid lines show liquid water contents and cloud fractions; the dashed lines are for ice cloud.

The experiment shows significantly more liquid cloud throughout the depth of the profile. The profile of q_l becomes more adiabatic in character, with the biggest increases in liquid water content occurring near cloud top, where enhanced TKE due to cloud-top instability drives the production of extra liquid water.

The cloud-top liquid water contents attained are still much lower than those observed: 0.1 g kg^{-1} in the experiment model compared with 0.3 g kg^{-1} in the observations. In addition, the model ice water contents are larger than observed and typically exceed the liquid water contents. This problem is exacerbated in the experiment because of riming of the increased liquid water.

The improvements made to the subgrid cloud fraction fields are relatively modest. The observed stratus had mixed-phase cloud fractions of close to 1 throughout its depth (Klein et al. 2009). Figure 4b shows that the liquid cloud fractions have increased in the experiment but remain significantly lower than were recorded in reality.

Figure 5 shows the mean thermodynamic structure of the boundary layer in the two models. Also shown are the mean vertical extents of the cloud layers.³

The cloud base in the control model is typically too high, compared to the observed value of 500 m. The experiment shows more frequent occurrence of low cloud bases, and this improves the mean cloud-base forecast. The temperature range of cloud (also shown in Fig. 4) is similar to that inferred from the observations [cf. Fig. 2 of Klein et al. (2009)]. However, the coldest temperatures attained at the inversion are around a degree warmer than the reported cloud top of -15°C . This is potentially due to underresolution of the inversion structure because of vertical grid spacing.

³ Following Klein et al. (2009), we define cloud base as the height beneath which the liquid water content is below a threshold of $10^{-3} \text{ g kg}^{-1}$.

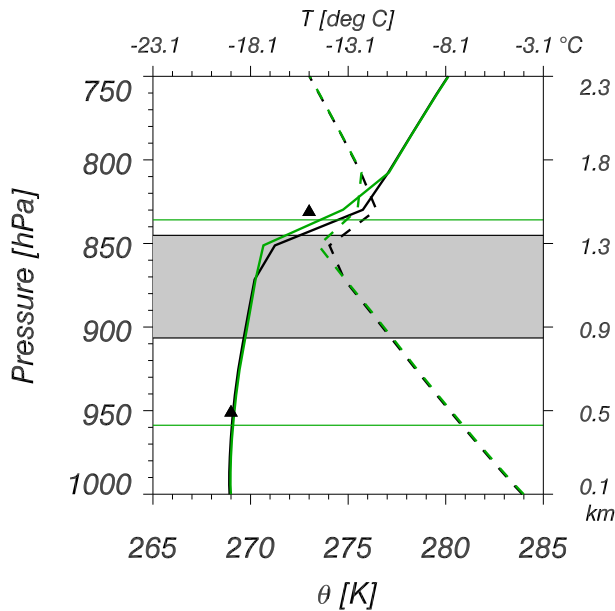


FIG. 5. Vertical profiles of potential temperature (solid lines; bottom axis) and temperature (dashed lines; top axis), averaged along the cross section through the target region. The gray rectangle shows the mean vertical extent of the cloud layer in the control run. The green horizontal lines show the mean cloud-base and cloud-top heights for the experiment model. The black triangles show the observed cloud-top and cloud-base heights and potential temperatures.

For the Arctic climate, it is interesting to consider the effects of the additional liquid cloud on the surface radiation budget. Figure 6 shows the joint PDF of surface downwelling LW flux and liquid water path. The statistics were obtained for a $1.2^\circ \times 8.8^\circ$ rectangle centered on 70.5°N , 153°W , which includes the two ARM sites. The black contours show the joint PDF for the control model; the green contours show those for the experiment. The green and black symbols correspond to Barrow and Oliktok Point, at both of which the liquid water paths more than doubled. The increase in LWP has a radiative impact at the surface, leading to an average increase in surface downwelling LW of approximately 10 W m^{-2} and bringing the forecast closer to the observations (shown by the gray rectangle). The variability of the model fields is also improved: the control model gives a longer tail of low LWPs and LW fluxes, which is shifted to higher values in the experiment. However, it is clear that deficiencies remain in the way the model represents Arctic stratus cloud.

4. Climate simulations

In this section, we consider the effects of the turbulent cloud production parameterization on 20-yr climate

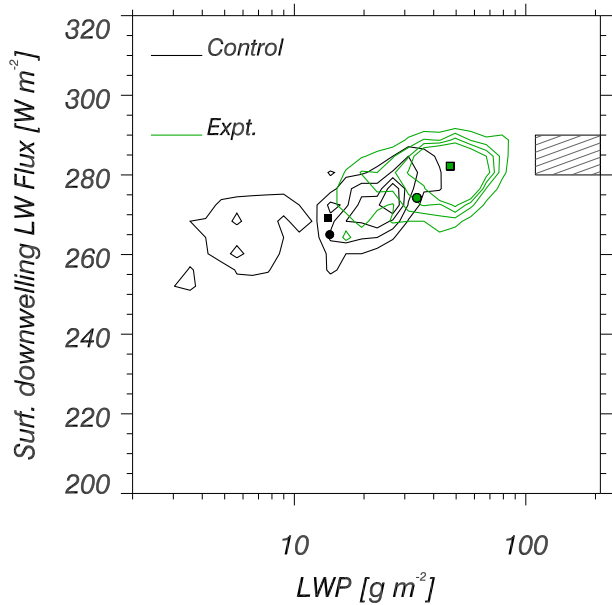


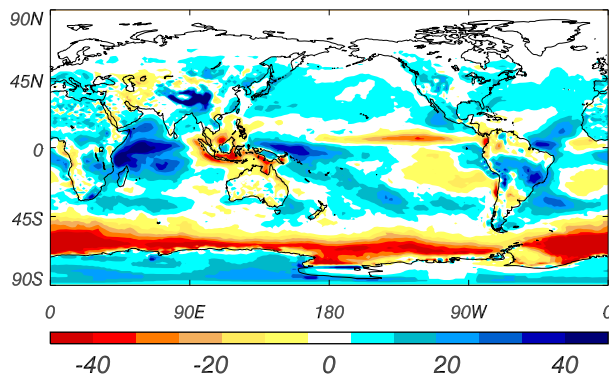
FIG. 6. Joint histogram of surface downwelling longwave flux and LWP for the North Slope of Alaska region. The line-filled box shows the M-PACE observations. The small colored symbols show the means at Barrow (circles) and Oliktok Point (squares).

simulations. In particular, we quantify the impact of the additional liquid cloud on the model top-of-atmosphere (TOA) and surface radiation biases. The control model used is similar to the GA6 configuration of the Met Office Unified Model at N96L70 resolution (approximate horizontal grid spacing is 130 km).

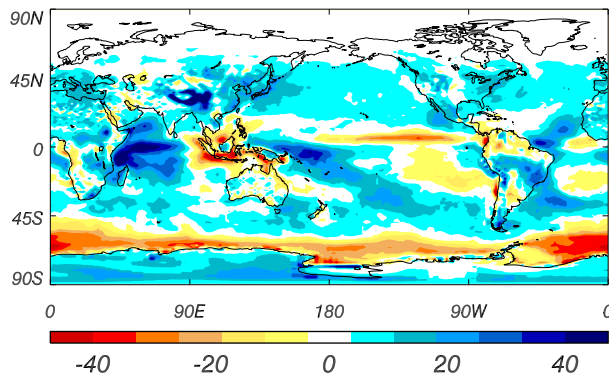
As shown in section 3a, applying the turbulent cloud production scheme for all temperatures results in a significant increase in large-scale cloud LWP globally. At high latitudes, this increase addresses an existing LWP deficit in the control model. However, the significant increase in tropical large-scale cloud due to the scheme leads to a very large increase in outgoing SW radiation over the tropics. Consequently, for the climate simulations presented here, we constrain the scheme to operate only for temperatures below 0°C . This effectively restricts the production of additional liquid cloud to the poles and midlatitudes. In future work, it may be possible to relax this temperature restriction by making alterations to the model cloud and radiation schemes.

Figures 7a and 7b show the 20-yr mean bias in TOA outgoing SW flux for the control and experiment, relative to CERES-EBAF (Loeb et al. 2009) in the Southern Hemisphere summer. There is a very large negative shortwave bias over the Southern Ocean for the control model that is significantly reduced for the experiment. The extent of the bias reduction is apparent from Fig. 7c,

From 1/12/1988 to 1/3/2008
(a) TOA $\delta[\text{SW}]$ (Control-CERES)



(b) TOA $\delta[\text{SW}]$ (Expt.-CERES)



(c) TOA $\delta[\text{SW}]$ (Expt.-Control)

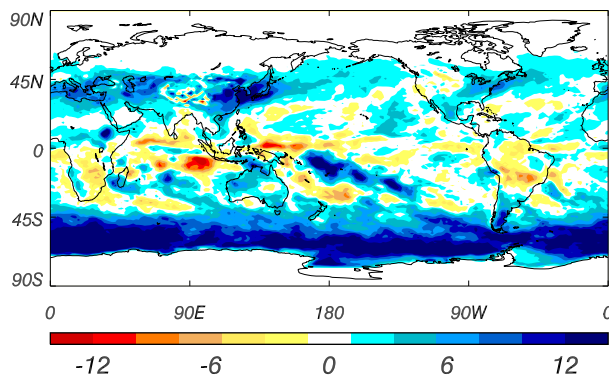


FIG. 7. The 20-yr seasonal TOA outgoing SW flux means (W m^{-2}) for December–February from the low-resolution (N96L70) climate simulations. (a) Difference between the control model and CERES-EBAF. (b) Difference between the experiment model and CERES-EBAF. (c) Difference between the experiment and control models.

which shows the differences in the outgoing TOA shortwave flux between the two models.

Figure 8a shows the zonally averaged, 20-yr TOA flux differences. The additional liquid water produced at

midlatitudes in both hemispheres results in an increase in the reflected SW of up to 6 W m^{-2} and a decrease in outgoing LW of 2 W m^{-2} .

The effect on model TOA fluxes is similar in both hemispheres. This can also be seen from Fig. 7, where brightening of clouds is visible, for example, over the North Pacific and the Sea of Japan. Because Northern Hemisphere SW biases are smaller than those over the Southern Ocean, and typically positive in sign, brightening of Northern Hemisphere clouds is detrimental to the SW. This is most pronounced in the Arctic during the summer (not shown). However, given severity of the Southern Ocean biases and their importance for climate prediction, improvement there might be valued over degradation elsewhere.

Figure 8b shows the zonally averaged differences in the surface fluxes. The total surface flux is a sum of the net surface LW and SW fluxes, sensible heat flux, and latent heat flux. The black line shows how the total surface flux differs between the control and experiment. The effect of the increased liquid cloud in the experiment is to reduce the total energy flux into the surface over most of the regions that show increased cloudiness. Over the Southern Ocean, for example, the total energy flux is reduced in the experiment by up to 4 W m^{-2} .

Also shown in Fig. 8c are the various contributions to the surface energy balance. The net flux of SW radiation into the surface (red line) is reduced in the experiment as a result of increased cloud optical depth. There is a corresponding increase in net surface LW flux (blue line) as a result of thermal emission from the extra liquid mass. The green line shows the increase in the sum of the latent and sensible heat fluxes out of the surface (i.e., into the atmosphere) in response to the changes in cloudiness.

In the subtropics and midlatitudes, the total surface flux is dominated by the decrease in downwelling SW. At polar latitudes, the total flux is a sensitive balance of radiative and turbulent heat fluxes. For example, north of 70°N , the change in the total radiative flux into the surface (i.e., the sum of LW and SW contributions) is positive, because of the low solar irradiance in the winter months. This is offset by an increase in turbulent transport out of the surface, and the total flux is approximately the same in both models.

5. Sensitivity to model parameters

The parameterization has a strong, nonlinear sensitivity to the choice of the entrainment length scale parameter β_1 . For example, in sensitivity tests, we found that halving β_1 ($\ell_E = \Delta_z$) more than halved the liquid water produced. This occurs because the cloud ice water

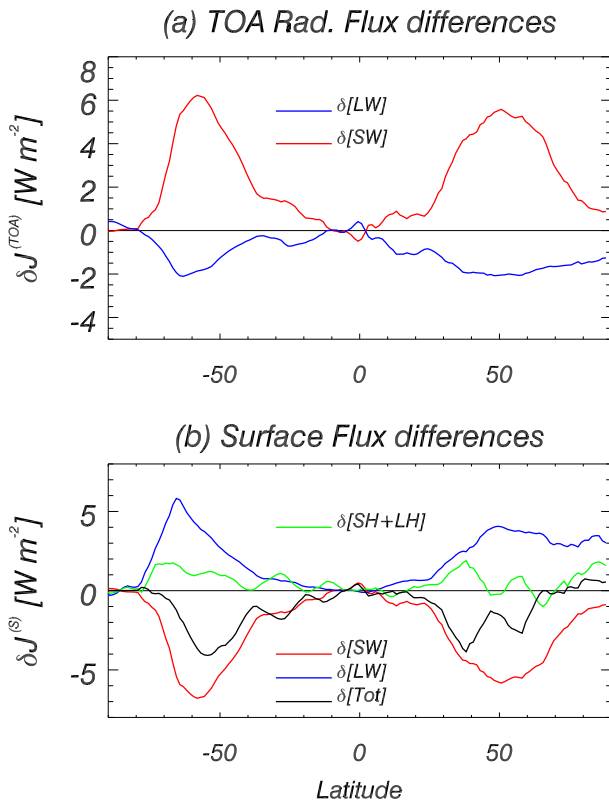


FIG. 8. The 20-yr annual radiative flux differences for the low-resolution (N96L70) climate simulations. (a) Zonal-mean outgoing TOA flux differences: SW (red) and LW (blue). (b) Zonal-mean surface flux differences: SW (red), LW (blue), turbulent heat flux out of the surface (green), and total flux into the surface (black). Note that the LW, SW, and total surface fluxes are positive into the surface. The latent and sensible heat fluxes are positive into the atmosphere.

contents are such that the entrainment time scale τ_E is comparable to the ice phase-relaxation time scale τ_p , so the width of subgrid PDF of S_i is strongly influenced by the entrainment terms in Eq. (6).

For the NWP simulations of the M-PACE case study, using a reduced entrainment tuning of $\beta_1 = 1$ gives a much more modest impact on LW fluxes and LWCs (increases of a few watts per square meter in LW flux and 0.02 g kg^{-1} in cloud-top q_t , compared to those shown in Figs. 4 and 6).

Similarly, for the climate simulations in section 4, the amount of liquid cloud produced can be reduced by decreasing the value of β_1 . Decreasing the liquid water paths leads to less intense cloud brightening and reduces the LW flux reaching the surface. For example, in sensitivity tests, we found that setting $\beta_1 = 1$ approximately halved the increase in outgoing SW flux at midlatitudes but retained the geographical distribution of changes shown in Fig. 7. Indeed, the associated map of mean SW

flux bias (not shown) is similar to that shown in Fig. 7b, but with a change of color scale.

In addition to sensitivity to closure parameters, there is uncertainty in the choice of the closure relations themselves. For example, the constraint that l_E scales like the gridbox depth is a structural assumption in the scheme that could be replaced with a different closure. There is also sensitivity to the TKE diagnostic used to drive the cloud production mechanism. Since it modulates the liquid cloud increments, changes to the formulation of the boundary layer TKE would affect the distribution and amount of cloud produced.

The most appropriate settings for use in a climate model or NWP model depends on the exact nature of the cloud and radiation biases in that model. For example, the Met Office Unified Model shows large outgoing SW biases (on the order of 30 W m^{-2}) but relatively small surface LW flux biases over the Southern Ocean. In this region, improvements to the SW flux need to be traded off against the desire to reduce the downward heat flux across the sea surface. To address these issues, in situ observations are needed to determine the optimal closure relations for the model.

6. Conclusions

We have implemented a parameterization of subgrid-scale liquid cloud formation due to unresolved turbulent processes. The parameterization is based on an analytical model of moisture variability that predicts the PDF of total relative humidity, from which the liquid cloud in each model grid box can be diagnosed. The PDF shape depends on small-scale turbulence and ice microphysics. We have developed closure relations that allow the model to be implemented in a GCM. Turbulence information is obtained from the boundary layer scheme and properties of any preexisting cloud from the cloud microphysics scheme. The liquid cloud properties diagnosed from the parameterization are used to increment the GCM prognostic cloud variables in a way that is consistent with the GCM's preexisting, macroscopic large-scale cloud scheme (PC2).

The model improves liquid water paths at polar latitudes compared with satellite retrievals from the AMSR instrument. This leads to an increase in reflected SW radiation at TOA over the Southern Ocean and in the Arctic, with associated changes in the surface radiation budget in these regions. For a case study focusing on Arctic stratus in Alaska, the enhanced liquid water paths were shown to bring the GCM closer to the observations of Klein et al. (2009). Over the Southern Ocean, the SW bias was reduced in magnitude and spatial extent but not eliminated. Many factors are implicated in the

remaining bias: for example, continuing cloud biases, wind and storm-track errors, and aerosol physics.

If the parameterization is active at all temperatures, then an increase in tropical and subtropical liquid water path occurs that leads to a positive bias with respect to the AMSR retrievals. This has a detrimental effect on the overall tropical radiative balance. To avoid this issue, we have restricted the scheme to work only for temperatures below 0°C and therefore produce only cold clouds. This retains the beneficial effects at high latitudes while avoiding detrimental effects associated with too much tropical and subtropical midlevel liquid cloud.

The improvements over the Southern Ocean are at the expense of increased radiation biases in the Northern Hemisphere, particularly the Arctic. This is despite the parameterization improving the structure and phase of Arctic clouds, perhaps suggesting that the Northern Hemisphere SW biases are due to a combination of other model errors. In future work, we aim to remove the temperature restriction and offset the Northern Hemisphere radiative impacts by making other changes to the model cloud and radiation schemes.

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APPENDIX

Definitions

For reference, we collate some of the state-dependent functions used in this paper:

$$b_i = \frac{1}{q_v} + \frac{L_s^2}{c_p R_v T^2}, \quad (\text{A1})$$

$$B_0 = 4\pi C \left(\frac{L_s^2}{K_a R_v T^2} + \frac{R_v T}{e_{si} \psi} \right)^{-1}, \quad \text{and} \quad (\text{A2})$$

$$a_i = \frac{g}{R_d T} \left(\frac{R_d L_s}{c_p R_v T^2} - 1 \right), \quad (\text{A3})$$

where K_a is thermal conductivity of air, ψ is the molecular diffusivity of air, L_v is the latent heat of vaporization

of water, L_s is the latent heat of sublimation of water, c_p is the specific heat capacity of water at constant pressure, R_d is the gas constant of dry air, R_v is the gas constant of water vapor, and the constant C is the capacitance of the ice crystal population. The following values have been assumed: $L_v = 2.501 \times 10^6$, $L_s = 2.835 \times 10^6$, $c_p = 1005$, $R_d = 287.05$, $R_v = 461.51$, and $C = 1$.

The solution to the stochastic Squires equation [Eq. (1)] is given by

$$S_i(t) = \exp[-(B + C)t] \times \left(S_0 + S_E \frac{C}{B + C} \{ \exp[(B + C)t] - 1 \} \right) + a_i \int_0^t dr w(r) \exp[-(B + C)(t - r)], \quad (\text{A4})$$

where $B = 1/\tau_p$, $C = 1/\tau_E$, and $S_0 = S_i(0)$ is the initial supersaturation of the air parcel. The steady-state statistics of S_i can be derived from Eq. (A4) using the method described in F14.

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