



UNIVERSITY OF LEEDS

This is a repository copy of *Assessment of hydro-morphodynamic modelling and geomorphological impacts of a sediment-charged jökulhlaup, at Sólheimajökull, Iceland.*

White Rose Research Online URL for this paper:
<http://eprints.whiterose.ac.uk/90930/>

Version: Accepted Version

Article:

Guan, M, Wright, NG, Sleight, PA et al. (1 more author) (2015) Assessment of hydro-morphodynamic modelling and geomorphological impacts of a sediment-charged jökulhlaup, at Sólheimajökull, Iceland. *Journal of Hydrology*, 530. 336 - 349. ISSN 0022-1694

<https://doi.org/10.1016/j.jhydrol.2015.09.062>

© 2015, Elsevier. Licensed under the Creative Commons Attribution-NonCommercial-NoDerivatives 4.0 International
<http://creativecommons.org/licenses/by-nc-nd/4.0/>

Reuse

Unless indicated otherwise, fulltext items are protected by copyright with all rights reserved. The copyright exception in section 29 of the Copyright, Designs and Patents Act 1988 allows the making of a single copy solely for the purpose of non-commercial research or private study within the limits of fair dealing. The publisher or other rights-holder may allow further reproduction and re-use of this version - refer to the White Rose Research Online record for this item. Where records identify the publisher as the copyright holder, users can verify any specific terms of use on the publisher's website.

Takedown

If you consider content in White Rose Research Online to be in breach of UK law, please notify us by emailing eprints@whiterose.ac.uk including the URL of the record and the reason for the withdrawal request.



eprints@whiterose.ac.uk
<https://eprints.whiterose.ac.uk/>

1 **Assessment of hydro-morphodynamic modelling and geomorphological impacts** 2 **of a sediment-charged jökulhlaup, at Sólheimajökull, Iceland**

3 Mingfu Guan ^{a*}, Nigel G. Wright ^a, P. Andy Sleight ^a, Jonathan L. Carrivick ^b

4 ^a Water@Leeds and School of Civil Engineering, University of Leeds, Leeds, LS2 9JT, UK

5 ^b Water@Leeds and School of Geography, University of Leeds, Leeds, LS2 9JT, UK

6 **Abstract:** Understanding of complex flood-riverbed interaction processes in large-scale (field) outburst
7 floods remains incomplete, not least due to a lack of well-constrained field data on hydraulics and sediment
8 transport, but also because consensus on an appropriate model framework has yet to be agreed. This study
9 presents a novel full 2D hydro-morphodynamic model containing both bedload and suspended load
10 capability. Firstly, the model design is presented with an emphasis on its design to simulate rapidly-varied
11 sediment-laden outburst floods and also the associated geomorphological impacts. Secondly, the model is
12 applied to a large-scale (field) glacier outburst flood or ‘jökulhlaup’ at Sólheimajökull, Iceland. For this real-
13 world event, model scenarios with only water and with inclusion of sediment with different parameter setups
14 were performed. Results indicated that grain size specifications affected resultant geomorphological changes,
15 but that the sensitivity of the simulated riverbed changes to the empirical bedload transport formulae were
16 insignificant. Notably, a positive feedback occurred whereby the jökulhlaup led to significant net erosion of
17 the riverbed, producing an increase in flow conveyance capacity of the river channel. Furthermore, bulking
18 effects of sediment entrainment raised the peak discharge progressively downstream, as well as the flood
19 volume. Effects of geomorphological changes on flood water level and flow velocity were significant.
20 Overall, despite the increased computational effort required with inclusion of sediment transport processes,
21 this study shows that river morphological changes cannot be ignored for events with significant in-channel
22 erosion and deposition, such as during outburst floods.

23 **Keywords:** morphodynamic model; outburst floods; sediment transport; river morphology

* Corresponding author. Dr. Mingfu Guan
Email address: mingfu.guan@hotmail.com;

24 1. Introduction

25 Outburst floods or dam break type floods are amongst the most catastrophic natural hazards for human
26 society and infrastructure. Part of the hazard of outburst floods is due to sediment transport. Glacial outburst
27 floods or 'jökulhlaups' are a sudden onset flood from glaciers and ice sheets, either due to an ice or moraine
28 dam failure, or due to volcanic or geothermal activity (Alho et al., 2005; Carrivick et al., 2010; Carrivick and
29 Rushmer, 2006; Dai et al., 2005; Huggel et al., 2002; Manville et al., 1999). Field evidence demonstrates
30 jökulhlaups often entrain a large amount of sediment and cause severe in-channel erosion and deposition,
31 owing to high flow energy (Alho et al., 2005; Russell et al., 2010; Staines et al., 2014). In contrast to
32 perennial river flows, a jökulhlaup is usually orders of magnitude larger in discharge, which implies that
33 within a jökulhlaup the flood-riverbed interaction is more intense. In proglacial areas, the riverbed generally
34 comprises of poorly sorted sediment materials from coarse particles (nominally greater than 250 mm) to fine
35 (sand) particles (Alho et al., 2005; Russell et al., 2010), hence both bedload-dominant sheet flows and
36 suspended load govern the sediment movement within a jökulhlaup. The entrained sediments will admittedly
37 affect floodwater dynamics and rheology and riverbed adjustment (Berzi and Jenkins, 2008; Carrivick et al.,
38 2011). However, the complex sediment - bed interactions within jökulhlaups are poorly understood, because
39 of the difficulty of field measurements and the unpredictability of such sudden onset floods.

40 Partly as a reaction to the problem of field measurements, small-scale laboratory experiments (e.g.
41 (Carrivick et al., 2011; Zech et al., 2008)) have been conducted and provide fundamental insights into the
42 hydraulics and flow-bed interactions within dam break outburst floods. The studies have shown that gravel
43 particles in outburst floods are generally transported in bedload dominant mode in a specific layer called a
44 'sheet flow layer'; while the finer particles are transported in a suspension layer. These experiments were
45 performed in small-scale flumes with specific definition of flow conditions or grain-size distribution. The
46 laboratory work therefore is only a crude model of geomorphological processes within large-scale outburst
47 floods, because of the complexity of the real-world topography and flow conditions, spatially varying grain-
48 size distribution, as well as the difficulty in ensuring physical similarity. In recent decades, attention has
49 increasingly been paid to numerical modelling of such flood events (Carling et al., 2010; Carrivick et al.,
50 2010); because it can give greater details of the phenomena during an event that cannot be captured by field

51 and flume measurements. Although the exact quantification of bed change is unattainable through numerical
52 modelling, the modelling technique can enhance and improve our insights into rapid sediment-laden floods
53 (e.g. Carrivick et al., (2013).

54 In terms of numerical models, which should be informed by field data or experimental data, to date a
55 large number of one-dimensional (1D) and two-dimensional (2D) morphodynamic models have been
56 developed to represent erosion and deposition by dam-break outburst floods (Cao et al., 2004; Fraccarollo
57 and Capart, 2002; Guan et al., 2015; Zech et al., 2008). However, these numerical models have been limited
58 to theoretical investigations or to simulating small-scale laboratory flume experiments. Numerical modelling
59 of a large-scale real-world flood with river morphology changes includes Carrivick et al. (2010) and Huang
60 et al. (2014), but is still rare despite its being crucial to improving understanding of geomorphological
61 processes with outburst floods and their complex interactions. Some fully three-dimensional (3D)
62 morphodynamic models based on Navier-Stokes equations have also been reported in recent decades
63 (Khosronejad et al., 2007; Shimizu et al., 1990; Wu et al., 2000). A 3D model can give more detailed
64 computation of the water flow field, such as inclusion of secondary flows. However, a disadvantage in using
65 a fully 3D model is that the computational time is at least an order of magnitude longer than a 2D model. The
66 majority of the fully 3D models were developed focusing on meandering channel flows or flows near
67 structures where complex 3D features are exhibited. Although there are studies to investigate the possibility
68 of modelling the bed changes in a natural river using a fully 3D model (Fischer-Antze et al., 2008), these are
69 still quite rare (Westoby et al., 2014). For engineering applications, a 2D hydro-morphodynamic model is
70 usually adequate. The capabilities of 2D models include the ability to simulate multi-directional and multi-
71 channel flows, super-elevation of flow around channel bends and turbulent eddying. These are dynamic
72 characteristics intrinsic to a jökulhlaup and all types of outburst floods.

73 A 2D layer-based morphodynamic model has been developed and validated against a series of
74 experimental tests for a noncohesive dyke breach (Guan et al., 2014). However, this model only accounted
75 for uniform bedload, which is only applicable to cases of bedload-dominant sheet flows. Field evidence
76 demonstrates that suspended load plays an equally important role for jökulhlaups (Carling, 2013; Staines,
77 2012). Therefore, building on the bedload dominant sheet flow model (Guan et al., 2014), an improved layer-

78 based model is developed in this study by the inclusion of a suspended load model, and by including non-
79 uniform sediment characteristics. Furthermore, this study applies the hydro-morphodynamic model to the
80 well documented 1999 jökulhlaup in Iceland, to explore geomorphological impacts within the jökulhlaup.
81 Therefore, the aims of this study are: (1) to develop a numerical model capable of modelling field-scale
82 outburst floods with bedload and suspended load, and geomorphological changes, (2) to explore the effects
83 of the morphological changes within a jökulhlaup on flood dynamics, and (3) to improve understanding of
84 rapidly-varied and unsteady hydraulics and flow-bed interactions in large-scale jökulhlaups.

85 **2. Study area and data collection**

86 2.1. The 1999 jökulhlaup

87 Jökulhlaups induced by volcanic activity have frequently occurred in Iceland and one of them, the July
88 1999 jökulhlaup burst from Sólheimajökull southern Iceland. The 1999 jökulhlaup has been well recorded
89 through field investigations (Russell et al., 2000; Russell et al., 2010; Sigurdsson et al., 2000; Staines, 2012;
90 Staines et al., 2014), which provides a good opportunity to develop greater understanding of
91 geomorphological impacts of a sediment-charged jökulhlaup through detailed numerical modelling.
92 Sólheimajökull is an approximately 8 km long temperate, non-surgingly outlet glacier draining the
93 Mýrdalsjökull ice cap belonging to the southern volcanic zone in Iceland (Fig. 1a). The glacier surface area
94 is 78 km² with a snout 1 km wide, and it is slightly over-deepened. A river channel called Jökulsá á
95 Sólheimasandi drains Sólheimajökull which has three main flow sources: (1) Jökulsárgilsjökull, an outlet
96 glacier 3 km to the north of Sólheimajökull; (2) the glacial meltwater from Sólheimajökull itself via a 1km
97 long subglacial tunnel; and (3) the river Fjallgilsá, flowing into the Jökulsá approximately 2 km downstream
98 of the glacier snout.

99 The flooding process was sudden, short-lived and had high discharge, lasting approximately 6 h. The
100 flood burst initially from the western margin of Sólheimajökull and drained into a former ice-dammed lake
101 basin, approximately 3.7 km from the glacier snout thereby filling it (Fig. 1b location a). Then the meltwater
102 overspill from this lake basin flowed into a lower tributary valley, Jökulsárgil (Fig. 1b location b). Additional
103 floodwater increased the discharge into Jökulsárgil along the western margin of the glacier between the

104 upper basin and Jökulsárgil, and meanwhile shattered glacial ice entered into Jökulsárgil with meltwater
105 caused by ice fracturing. Additionally, the supra-glacial fracture outlets about 3km from the glacier snout
106 also carried quantities of sediment-laden floodwater (Roberts et al., 2003). The Western Conduit and the
107 Central Conduit were the two major floodwater sources in the river channel. The Western Conduit with 150
108 m in width was the biggest floodwater source, and the Central Conduit opened up in the centre of the snout
109 draining the majority of waning stage and post-outburst flooding flow. The floodwater in the two conduits
110 ran together into the river channel, Jökulsá á Sólheimasandi. Some smaller flows exited the eastern margin of
111 the snout from a small, newly-cut, steep-sided channel and from a series of minor outlets flowing across
112 vegetated hillslopes.

113 2.2. Data collection and general considerations

114 The data used in this study are summarised in Table 1. The bed terrains before and after the 1999
115 jökulhlaup were surveyed in 1996 and 2001 using photogrammetry (Staines et al., 2014). These datasets are
116 a very unusual asset for this kind of modelling study. Although there are some slight changes within the river
117 channel between the survey year and the jökulhlaup time, it was considered preferable to use the bed before
118 the jökulhlaup rather than a post-flood bed as is often the case in jökulhlaup reconstructions (Staines, 2012).
119 Thus, the 1996 digital elevation model (DEM) was used as the initial input domain for simulation, and the
120 2001 DEM was compared to the simulated bed. DEMs errors and uncertainty were assessed by comparing
121 grid values with the differential Global Positioning System (dGPS) and with a DEM constructed from a 2010
122 summer LiDAR survey, which is assumed had no errors. More details about the surveyed dataset were given
123 by Staines et al. (2014). In this study, the DEMs with two different resolutions ($8\text{ m} \times 8\text{ m}$ and $4\text{ m} \times 4\text{ m}$)
124 were applied in order to elucidate the appropriate balance of computational efficiency and accuracy of the
125 model.

126 Field observations indicate that the western conduit and the central conduit are two major sources from
127 which floodwater flowed to the river channel. The observations with a peak discharge of $1700\text{ m}^3/\text{s}$ were
128 made at the bridge after ~ 1 hour initiation of the 1999 jökulhlaup by Sigurdsson et al. (2000). The peak
129 discharge was reconstructed to be $4000\text{ m}^3/\text{s}$ by Russell et al. (2010). Staines (2012) pointed out that the peak
130 value $4000\text{ m}^3/\text{s}$ was rather high and defined a hydrograph with 40% of the discharge from the central

131 conduit and 60% from the western conduit (Fig. 2) which was a good-fit to the observations. Thus, this study
132 used the input hydrograph provided by Staines (2012) as the model input hydrograph.

133 Based on the field observations, the sediment material in the channel is constituted of various grain-sizes
134 from fine granule to coarse boulder (Russell et al., 2010; Staines et al., 2014). The size fractions are
135 summarised in Table 2 and include boulders, cobbles and granules. The median diameters for the three
136 fractions differ significantly, and the distribution in reality is generally spatially varying. Grain-size is
137 considered to be an uncertainty factor for morphodynamic modelling due to the difficulty in estimating the
138 grain-size in a full-scale channel, and there are no proposed sediment transport equations for the transport of
139 such coarse boulders. Also, the proportion of coarse boulders is small. Consequently, an appropriate
140 simplification is made that only the sediment fractions of granules and cobbles were considered in the
141 morphodynamic modelling. The proportion of both fractions was initially given as 50%. The updating of the
142 proportion of each grain-size at each grid cell was calculated using the method described in section 2.5. To
143 explore and emphasize the importance of grain-size on modelling results, we also used a single size fraction
144 ($d = 40$ mm and $d = 80$ mm) for two runs.

145 Many studies have reported that Manning's roughness has significant effects on the modelled bed
146 morphology, flow discharge and timing (Huang et al., 2014; Nicholas, 2003; Staines and Carrivick, 2015).
147 Some studies used a constant Manning's value varying from 0.04 to 0.06 in proglacial areas comprising sand
148 to cobble sized materials (Alho et al., 2005; Staines and Carrivick, 2015). To estimate the Manning's value,
149 this study used the Manning-Strickler equation $n = 0.038d_{90}^{1/6}$ which is used to reconstruct the hydrograph
150 of the 1999 jökulhlaup in the study area by Russell et al. (2010).

151 **3. Hydro-morphodynamic model**

152 **3.1. Conceptual model structure**

153 This study uses a layer-based conceptual model. The model which includes bedload has been developed
154 and validated by Guan et al. (2014). As field evidence shows, the riverbed in the study site is composed of
155 grains with a wide range from fine granules to coarse boulder. The jökulhlaup can not only induce the coarse
156 particles in motion (bedload), but also entrains plenty of fine sediment particles in suspension because of the

157 high bed shear stress. Therefore, the bedload dominant sheet flow model might be limited in simulating the
 158 whole range of geomorphological processes within the jökulhlaup. A suspended load model is crucial to
 159 reconstruct the physical processes more appropriately. In this regard, the model used in this study extended
 160 the layer-based bedload dominant sheet flow model by including an additional suspension layer. The model
 161 is a two-dimensional numerical model based on full shallow water equations for unsteady incompressible
 162 flow conditions. The main advantages of the model are that it calculates the natural velocity difference
 163 between the sheet flow layer and the mixed flow, and simulates the bank erosion as well. The depth-averaged
 164 2D model was preferred because it has a higher computational efficiency over 3D modelling, and horizontal
 165 flow conditions were expected to predominate over vertical flows.

166 3.2. Hydrodynamic model

167 The 2D shallow water equations are solved using a Godunov-based finite volume method as in many
 168 existing flood models (Begnudelli and Sanders, 2006; Guan et al., 2013; Villanueva and Wright, 2006). The
 169 governing equations are extended with the incorporation of sediment transport and also considering the mass
 170 and momentum exchange of flow and bed. Based on the morphodynamic model proposed in previous work
 171 (Guan et al., 2014), the mass and momentum equations with sediment effects are written in vector form as
 172 follows:

$$\frac{\partial \mathbf{U}}{\partial t} + \nabla \cdot \mathbf{F} = \mathbf{S} \quad (1)$$

173 where \mathbf{U} is the vector of conserved variables, \mathbf{F} is the flux vector function and \mathbf{S} is the vector of source terms,
 174 and $\nabla = \vec{i}(\partial/\partial x) + \vec{j}(\partial/\partial y)$ is the gradient operator. \mathbf{U} , \mathbf{F} and \mathbf{S} are

$$\mathbf{U} = \begin{bmatrix} \eta \\ hu \\ hv \end{bmatrix}, \quad \mathbf{F} = \begin{bmatrix} h\mathbf{V} \\ hu\mathbf{V} + \frac{1}{2}gh^2\vec{i} \\ hv\mathbf{V} + \frac{1}{2}gh^2\vec{j} \end{bmatrix} \quad (2)$$

$$\mathbf{S} = \begin{bmatrix} 0 \\ gh \left(-\frac{\partial z_b}{\partial x} - S_{fx} \right) + \frac{\Delta\rho u}{\rho} \frac{\partial z_b}{\partial t} (\alpha(1-p) - C) - \frac{\Delta\rho gh^2}{2\rho} \frac{\partial C}{\partial x} - \mathbf{S}_{ad} \\ gh \left(-\frac{\partial z_b}{\partial y} - S_{fy} \right) + \frac{\Delta\rho v}{\rho} \frac{\partial z_b}{\partial t} (\alpha(1-p) - C) - \frac{\Delta\rho gh^2}{2\rho} \frac{\partial C}{\partial y} - \mathbf{S}_{ad} \end{bmatrix} \quad (3)$$

177 where h = flow depth (m); z_b = bed elevation (m); η = water surface (m); u, v = the x and y components of
 178 flow velocity respectively (m/s); \mathbf{V} is the velocity vector defined by $\mathbf{V} = u\vec{i} + v\vec{j}$; p = sediment porosity
 179 (dimensionless); C = total volumetric concentration (dimensionless); ρ_s, ρ_w = densities of sediment and water
 180 respectively (m^3/s); $\Delta\rho = \rho_s - \rho_w$; ρ = density of flow-sediment mixture (m^3/s); S_{fx}, S_{fy} are frictional slopes
 181 based on Manning's coefficient in x and y direction (dimensionless); $\alpha = u_s/u$ = sediment-to-flow velocity
 182 ratio (dimensionless) which represents the velocity difference of lower bedload transport and the mixed flow,
 183 the relationship defined by Greimann et al. (2008) was used as shown in Eq.(4); \mathbf{S}_{ad} is the additional term
 184 vector related to the velocity ratio α defined by Eq.(5).

$$185 \quad \alpha = \frac{u_*}{u} \frac{1.1(\theta/\theta_{cr})^{0.17}[1-\exp(-5\theta/\theta_{cr})]}{\sqrt{\theta_{cr}}} \quad (4)$$

$$186 \quad \mathbf{S}_{ad} = S_A\vec{i} + S_B\vec{j} = \frac{\Delta\rho\mathbf{V}}{\rho}(1 - \alpha)[C\nabla \cdot (h\mathbf{V}) - (h\mathbf{V})\nabla \cdot \mathbf{C}] \quad (5)$$

187 where θ, θ_{cr} represent the real dimensionless bed shear stress, and the critical Shields parameter; \mathbf{C} is the
 188 sediment concentration vector defined by $\mathbf{C} = C(\vec{i} + \vec{j})$.

189 3.3. Sediment transport model

190 3.3.1. Sheet flow load

191 Sheet flow is conventionally referred to as bed-load transport occurring at high bottom shear stress.
 192 Sheet flow load generally has highly concentrated sediment in a layer near the bed with a thickness of
 193 several times the sediment grain size. The velocity in this layer is usually lower than the main water velocity
 194 (Pugh and Wilson, 1999; Sumer et al., 1996). To account this, a velocity difference coefficient α is included
 195 in this study. The mass conservation equation of the i th size class in sheet flow layer is written considering
 196 the velocity ratio α by the following equation (Guan et al., 2014).

$$\frac{\partial hS_{bi}}{\partial t} + \alpha \frac{\partial huS_{bi}}{\partial x} + \alpha \frac{\partial hvS_{bi}}{\partial y} = - \frac{\alpha(q_{bi} - F_i q_{b*i})}{L_i} \quad (6)$$

197 where S_{bi} =volumetric bedload concentration of the i th size class; q_{bi} = real sediment transport rate of the i th
 198 fraction; q_{b*i} = sediment transport capacity of the i th fraction; L_i = non-equilibrium adaptation length of

199 sediment transport of the i th fraction, F_i represents the proportion of i th grain-size fraction in the total
 200 moving sediment.

201 Although there are a number of bedload transport formulae which were empirically proposed based on
 202 laboratory or fieldwork datasets, none can be universally applied to complex natural rivers due to the range
 203 and varying distribution of grain sizes. As suggested by Guan et al. (2014), this study chooses the
 204 combination of the modified Meyer-Peter & Müller formula (MPM) (Meyer-Peter and Müller, 1948) and the
 205 Smart & Jäggi formula (SJ) (Smart and Jäggi, 1983) based on the bed slopes. As the accuracy of the
 206 formulae has been considered to be poor, several other commonly-used formulae in the literature were also
 207 selected to conduct a sensitivity test. The bedload transport rate is written by:

$$q_{b*i} = \varphi \sqrt{g(\rho_s/\rho_w - 1)d_i^3} \quad (7)$$

208 where φ is determined by the following five selected formulae:

- 209 • A combination of MPM and SJ:

$$210 \quad \varphi = \begin{cases} \psi 8(\theta_i - \theta_{cr,i})^{1.5} & 0 \leq S_o < 0.03 \\ 4 \left(\frac{d_{90}}{d_{30}}\right)^{0.2} \frac{h^{1/6}}{n\sqrt{g}} \min(S_o, 0.2) \theta_i^{0.5} (\theta_i - \theta_{cr,i}) & S_o \geq 0.03 \end{cases}$$

- 211 • $\varphi = 8(\theta_i - \theta_{cr,i})^{1.5}$ for MPM
- 212 • $\varphi = 12\theta_i^{1.5} \exp(-4.5\theta_{cr,i}/\theta_i)$ for C&L (Camenen and Larson, 2005)
- 213 • $\varphi = 13\theta_i^{1.5} \exp(-0.05/\theta_i^{1.5})$ for C (Cheng, 2002) :
- 214 • $\varphi = 12\theta_i^{0.5}(\theta_i - \theta_{cr,i})$ for N (Nielsen, 1992):

215 where S_o is bed slope; $\theta_{cr,i}$ is critical dimensionless bed shear stress of i th fraction; θ_i is the dimensionless bed
 216 shear stress of i th fraction. The non-equilibrium adaptation length is calculated by

$$L_i = \frac{h\sqrt{u^2 + v^2}}{\gamma\omega_{fi}} \text{ with } \gamma = \min\left(\alpha \frac{h}{h_b}, \frac{1-p}{C}\right) \quad (8)$$

217 in which, h_b is the thickness of sheet flow layer; ω_f is the effective settling velocity of sediment particle which
 218 is estimated using the formulation with hindered settling effect proposed by Soulsby (1997).

219 3.3.2. Suspended load transport

220 The advection-diffusion equation has been widely used for suspended load models (Carrivick et al.,
 221 2010; Wu, 2004; Yang et al., 2015) because of its accuracy in calculating the propagation of sediment
 222 concentration in a water body. This study utilised the depth-averaged 2D advection-diffusion equation for
 223 suspended transport as:

$$\frac{\partial hS_i}{\partial t} + \frac{\partial huS_i}{\partial x} + \frac{\partial hvS_i}{\partial y} = \frac{\partial}{\partial x} \left(\varepsilon_x h \frac{\partial S_i}{\partial x} \right) + \frac{\partial}{\partial y} \left(\varepsilon_y h \frac{\partial S_i}{\partial y} \right) + S_{E,i} - S_{D,i} \quad (9)$$

224 where S_i = volumetric suspended load concentration of the i th size class; $S_{E,i}$ = entrainment flux of sediment
 225 of the i th size class; $S_{D,i}$ = deposition flux of sediment of the i th size class; $\varepsilon_x, \varepsilon_y$ = turbulent diffusion
 226 coefficients of sediment in the x and y direction. The first and second terms on the right hand side of Eq.(9)
 227 represent diffusion terms. Bohorquez and Ancy (2015) reported that sediment diffusion can induce bed
 228 instabilities and thereby provoke bed formation.

229 In Eq.(9), the entrainment flux and deposition flux for sediments are two vital parameters for updating
 230 the bed elevation, because both factors directly determine how much sediment is entrained and how much is
 231 deposited. However, a complete theoretical expression does not exist for the fluxes. In this study, a widely
 232 used approach is adopted (Wu et al., 2004).

$$S_{D,i} = \omega_{f,i} S_{a,i}, S_{E,i} = F_i \omega_{f,i} S_{ae,i} \quad (10)$$

234 where $S_{a,i} = \delta S_i$ is the near-bed concentration at the reference level a which refers to the depth of the sheet
 235 flow layer; the definition of the coefficient δ by Cao et al. (2004) is used as $\delta = \min\{2.0, (1 - p)/C\}$; $S_{ae,i}$ is
 236 the near bed equilibrium concentration at the reference level determined by the empirical equation of van
 237 Rijn (1984); the fraction coefficient F_i is defined in section 3.5. The deposition flux is represented as a
 238 product of the effective sediment settling velocity and the near-bed concentration at the reference level. The
 239 near bed equilibrium concentration is given as:

$$S_{ae,i} = 0.015 \frac{d_i T_i^{1.5}}{a d_{*i}^{0.3}} \quad (11)$$

$$T_i = \frac{(u_{*i}^2 - u_{*i,cr}^2)}{u_{*i,cr}^2}; a = \min[\max(\mu \theta_i d_{50}; 2d_{50}; 0.01h), 0.2h]$$

242 where T_i is the transport stage parameter; $u_{*i} = (g^{0.5}/C')u$ is bed-shear velocity related to grains; C' is the
243 Chézy-coefficient related to grain; $u_{*i,cr}$ is the critical bed-shear velocity.

244 3.4. Morphological evolution model

245 Erosion and deposition is calculated per grid cell at each time step to update the new bed elevation on the
246 basis of the results from the hydrodynamic model and sediment transport model described above. The
247 morphological evolution for non-uniform sediment material is calculated by:

$$\frac{\partial z_b}{\partial t} = \frac{1}{1-p} \sum_{i=1}^N \left[\frac{(q_{bi} - F_i q_{b*i})}{L_i} + S_{D,i} - S_{E,i} \right] \quad (12)$$

248 where the parameters on the right side are calculated according to the equations in previous sections.

249 3.5. Model consideration

250 The above coefficient F_i represents the proportion of i th grain-size fraction in the total sediment in
251 motion. It varies with time so F_i is updated at each time step. The updating of bed material composition is an
252 essential process for non-uniform bed aggradation and degradation. Among the three classified layers in the
253 model, it is the active layer that participates in the exchange with moving sediment. There are several bed
254 material sorting models available in the literature; the approach presented by Wu (2004) is adopted in this
255 study. The method divides the bed material above the non-erodible bed into several layers. The top layer is
256 the mixed layer where the exchange with the moving sediment occurs. The variation of bed material
257 gradation in the mixed layer is then updated at each time step.

258 Since the grain-size in the study domain varies greatly, the hiding/exposure effects between particles
259 and particles are important for the incipient motion and settling of sediments. Thus, this study accounts for
260 such effects in the estimation of the threshold for sediment incipient motion. Flood-induced erosion within
261 the main channel can cause further bank erosion. Also, the simulated morphological evolution can generate
262 an over-steep bed which is naturally unstable. To address this, this study utilised a bank failure model
263 developed by Guan et al. (2014) to update the unstable newly deformed bed. The model uses different
264 critical bed angles and re-formation bed angles above and below the water. Both the calculation of sediment

265 incipient motion and the bank failure model are given in details by Guan et al. (2014) and so for brevity are
266 not repeated here.

267 The 2D hydro-morphodynamic model system consists of Eq.(1), Eq.(6), Eq.(9) and Eq.(12). In this
268 study, a second-order Godunov-type finite volume method (Guan et al., 2014) is used to solve the improved
269 hydro-morphodynamic model considering both bedload and suspended load. A variable time step Δt , adapted
270 to local flow conditions, is calculated at each time step by the following equation.

$$271 \quad \Delta t = CFL \min \left(\min \frac{dx_i}{|u_i| + \sqrt{gh_i}}, \min \frac{dy_j}{|v_j| + \sqrt{gh_j}} \right) \quad (13)$$

272 As the numerical scheme is explicit, the restriction of Courant number $0 < CFL < 1.0$ is implemented for
273 the calculation of flow sediment transport, and bed change. The inclusion of sediment transport model
274 requires the reduction of the CFL number to maintain the model stability, which increases the computational
275 time.

276 4. Results and discussion

277 4.1. Sensitivity of grain size

278 Table 3 shows the simulated extent of bed erosion and deposition for the three scenarios with different
279 grain-size inputs. It indicates that the total bed change area is 2.51 km² for the mixed grain-size (the mixture
280 of granules and cobbles shown in Table 2) which is larger than the bed change area of 2.08 km² for $d = 40$
281 mm whilst the extent of bed change for $d = 80$ mm is the smallest for the three cases, at only 1.60 km². Fig. 3
282 demonstrates the spatial distribution of the simulated bed erosion and deposition in the river channel. It is
283 clearly shown that the extent of bed change for $d = 80$ mm is much smaller than that for the other two. The
284 extent of bed change for the mixed grain-size input is the broadest in the three cases. Although the maximum
285 depth of erosion and deposition do not differ from each other greatly, the simulation with mixed grain-size
286 predicts more erosion and deposition within the channel than other scenarios. For example, in the highlighted
287 circular area of Fig. 4, erosion and deposition hardly occur for the scenario with $d = 80$ mm, yet, we found
288 significant erosion and deposition with the input of mixed grain-size. There are a couple of reasons causing
289 these differences. First, a different grain-size estimates a different Manning's roughness which affects the

290 calculation of bed shear stress. A more important reason is that finer sediment particles have a smaller
291 settling velocity, and higher dimensionless bed shear stress induces the finer particles into motion more
292 easily, even with relative weak flows. The results imply that for a real flood over non-uniform bed, the use of
293 a single grain-size might cause over-/under-prediction of morphological changes. It is necessary to adopt the
294 appropriate representative fractions of grain-size which can reflect the natural conditions as realistically as
295 possible.

296 4.2. Sensitivity of sediment transport functions

297 Fig. 4 plots the simulated temporal change of bed erosion and deposition volumes during the flood as
298 modelled with different transport formulae. Fig. 4a indicates that the overall trends for the five runs are
299 similar, with all increasing rapidly before the peak stage of $t = 2$ hours and then reaching an approximately
300 constant value. However, the deposition volumes differ from each other. The difference of $0.67 \times 10^5 \text{ m}^3$ is
301 12.1%. The plot of the erosion volumes shows more significant differences with a maximum of $1.61 \times 10^5 \text{ m}^3$,
302 i.e. about 21%. The bed changes simulated by the formulas of MPM and C&L differ slightly from each other.
303 The formulas of C, N and MPM&SJ led to more severe erosion and deposition than MPM and C. Fig. 4b
304 shows the total area of simulated net sediment erosion and aggradation. It is noted in Fig. 4b that both
305 erosion area and deposition area are influenced only slightly by the sediment transport formulae. The areal
306 extents of the total bed changes for the five runs are also found to be similar with a difference smaller than
307 1%. The sensitivity test in this section reveals that the empirical transport functions can affect the magnitude
308 of net bed erosion and deposition, but qualitatively, the sensitivity of bed change features to these functions
309 is slight. It should be noted that the sensitivity test is to explore the effects of different existing empirical
310 bedload functions on simulated results, it does not account for the uncertainty factors such as the critical
311 Shields number, the probability of sediment entrainment as bedload and suspended load, and particle
312 diffusivity etc. The slight sensitivity verified here does not imply that the simulation results by the model is
313 as accurate as the real field observation, but means that the model is significantly affected by the choice of
314 empirical transport functions.

315 4.3. Implications of DEM resolution

316 Higher resolution topographic data can represent geomorphology more accurately, but at the expense of
317 increasing simulation time. To examine the appropriate balance between these two factors, bed topography at
318 two resolutions (Run 1: 8 m×8 m and Run 2: 4 m×4 m) was tested in this study. Table 4 indicates that the
319 simulated total erosion and deposition volumes are $7.8\times 10^5 \text{ m}^3$ and $5.9\times 10^5 \text{ m}^3$ respectively for Run 2, while
320 for Run 1, the total erosion and deposition are $7.4\times 10^5 \text{ m}^3$ and $5.5\times 10^5 \text{ m}^3$, respectively. The differences for
321 erosion and deposition are $0.4\times 10^5 \text{ m}^3$ (4.4%) and $0.4\times 10^5 \text{ m}^3$ (5.8%), respectively. At the cross section $x =$
322 332908.86 m close to a bridge which is located in the middle of the channel, it is found that the difference of
323 the maximum water level is just 0.08 m. Furthermore, the simulated temporal evolution of both erosion and
324 deposition volumes have a similar trend of increase and then tend to a constant value. Both total erosion and
325 deposition volumes are very close before 1.5 hours; but at later times, both are slightly larger for Run 2 than
326 those for the Run 1. Fig. 5 (a, b) demonstrates that the spatial pattern and extent of the erosion and deposition
327 for the two runs are in general similar, and both runs predict the maximum erosion and deposition depths
328 with a slight difference. Fig. 5(c) shows that the difference of Run 2 and Run 1 occurs across the whole
329 channel. However, we found both mean +/- differences are smaller than 0.2 m. The results indicate that the
330 DEM resolution slightly affects the simulated spatial distribution of bed changes. This is because the finer
331 resolution DEM represents the bed terrain with more detail, thus the simulated flow conditions (velocity and
332 water depth) will be slightly different. However, the computational time for the finer resolution is higher by a
333 factor of over four than that for the coarser one.

334 In summary, whilst topography is very important for defining the transient nature of outburst flood
335 hydraulics and geomorphological change (e.g.(Carrivick et al., 2013b)), the implications of varying input
336 topography resolutions in this study shows that: (1) the simulated net bed erosion and deposition for the finer
337 4 m × 4 m resolution is slightly more severe than those for the coarser 8 m×8 m DEM; (2) both the simulated
338 bed change have a similar pattern and extent; however, (3) the computational time for the finer 4 m×4 m
339 DEM is four times more expensive than that for the coarser 8 m × 8 m resolution; (4) so the coarse resolution
340 of 8 m×8 m is sufficient for the geomorphological analysis herein.

341 4.4. Multiple effects of sediment transport

342 Sediment transport entrained by outburst floods has the potential to affect the flow hydraulics by
343 modifying the flow density, the flow viscosity and the turbulence regime. Hence, the frontal wave speed, the
344 flow velocity as well as the flow depth will be altered considerably due to the incorporation of sediment
345 transport in flood propagation (Carrivick et al., 2011; Fraccarollo and Capart, 2002; Zech et al., 2008). In this
346 section, the effects of sediment transport on flood propagation are discussed and analysed from the numerical
347 modelling of a large-scale (field) event. In order to achieve this, two scenarios are modelled, namely: a clear
348 water flood without sediment transport (denoted Run 1); and a water-sediment mixed flood with sediment
349 transport (denoted Run 2). The two scenarios are compared via flow discharge at the cross section
350 ($x=332908.86$) near the bridge and the water surface at a gauge ($332908.86, 480099.78$), as shown in Fig. 6.
351 It reveals the following key points.

- 352 • The peak flow discharge at the cross section $x = 332908.86$ m increases slightly by $22 \text{ m}^3/\text{s}$ (1%)
353 from $2111.5 \text{ m}^3/\text{s}$ to $2133.5 \text{ m}^3/\text{s}$. Also during the flood period, the volume of the sediment-laden
354 flow through the cross section is about $2.09 \times 10^7 \text{ m}^3$, while the fluid volume is approximately
355 $2.02 \times 10^7 \text{ m}^3$. The incorporation of sediment transport leads the flow volume to increase by 7.0×10^5
356 m^3 . This manifests the bulk effects of sediment entrainment within sediment-laden floods. During
357 the outburst flood, the total erosion volume is about $7.4 \times 10^5 \text{ m}^3$, and the deposition volume is
358 $5.5 \times 10^5 \text{ m}^3$, i.e. a net riverbed change with a volume of $1.9 \times 10^5 \text{ m}^3$ occurs during the whole flood
359 period. The modelled net loss clarifies the source of the increased flow volume within the sediment-
360 laden flood.
- 361 • The water level with sediment at the point ($332908.86, 480099.78$) is smaller than that without
362 sediment throughout the flood period apart from a short initial stage, because the sediment-laden
363 flow arrives at the location earlier than the clear water flood. The decrease of water level in the
364 falling period is particularly significant.
- 365 • The water depth against time at the gauge point is also changed greatly due to the inclusion of in-
366 channel erosion and deposition. Specifically, the maximum water depth with consideration of
367 sediment transport is approximately 3.45 m , 0.47 m larger than that without sediment transport of

368 2.98 m. The water depth becomes smaller after the peak flow discharge as a result of the bed
369 deformation caused by the flood;

370 • As expected, the arrival time of the peak discharge at the cross section for Run 2 is considerably
371 shorter than that for Run 1 (Table 5), the time difference is 7.2 minutes. The arrival time of the water
372 front is also decreased by about 2.6 minutes due to the incorporation of sediment transport. The
373 faster propagation of waterfront and peak flows of the flood has also been found by Staines and
374 Carrivick (2015), who conclude that a morphodynamic model advanced flood arrival and peak
375 discharge times by 100% and 19% over hydrodynamic model. The simulated arrival time of peak
376 flow to the bridge is about 1 hour 13 minutes, which overall agrees with the recorded time by
377 Sigurdsson et al. (2000) and with the investigation by (Staines, 2012).

378 In summary, the outburst flood changes the bed terrain, which alters the flood dynamics, such as the water
379 level, the water depth and the flow velocity field etc. Fig. 7 shows that: the differences of the minimum bed
380 elevation have positive values and negative values (63.3% and 36.7% respectively) because of the erosion
381 and deposition caused by the jökulhlaup; the maximum water surface and maximum water depth for Run 2
382 are significantly smaller than those for Run 1 at most cross sections (89.8% and 86.1% respectively). Table 6
383 shows the statistics of the simulated results for the two runs. The water levels are reduced due to inclusion of
384 sediment transport in an area of approximately 3.03 km², whilst the water levels are raised in an area of only
385 0.76 km². The water depths decrease and increase in an area of approximately 2.68 km² and 1.11 km²,
386 respectively. In addition, the flood submerged area simulated by Run 1 is about 0.34 km² larger than the
387 submerged area for Run 2.

388 Fig. 8 illustrates the flow velocity fields of the two runs at the peak stage of t=2 hours. In overview both
389 flow fields show similar patterns in terms of the regions of high velocity and low value, yet the absolute
390 magnitudes appear to be different. Specifically, the surface of flow velocity field shows a smooth contour
391 distribution for the sediment-laden flood, whereas some fluctuations occur in the surface of the contour
392 distribution for the clear water flood. This characteristic is also shown in the spatial distribution of the water
393 depth in the river channel. Clearly, the changes in flood dynamics are caused by in-channel erosion and
394 deposition due to the rapid flood. It is inferred that the flood water induces sediment transport, creating a

395 smoother topography and thereby improves the flow conveyance capacity of the river channel, which in
396 return enables the flood to propagate faster. Incorporation of sediment transport promotes a faster (shorter)
397 arrival time of the water front and the peak flow discharge.

398 4.5. Erosion and deposition

399 The 1999 jökulhlaup eroded and carried a considerable amount of sediment, causing rapid bed change
400 (e.g. Russell et al. 2013). However, it is quite challenging to quantify the volume and the rate of bed erosion
401 and deposition at both temporal-scale and spatial-scale by physical measurements in the field (Russell et al.
402 2013). Therefore this study presents further understanding of these processes that can be derived from the
403 applications of a morphodynamic model. To verify the capability of the model in predicting
404 geomorphological changes, the difference of DEMs (DoD) before (1996 DEM) and after (2001 DEM) the
405 1999 jökulhlaup was used to compare to the simulated riverbed changes, which is demonstrated in Fig.9. It
406 indicates that the simulated spatial pattern of bed erosion and deposition is in general agreement with the
407 difference of DEMs before and after the flood. For example, in the highlighted circle zones of Fig.9 (a,b), the
408 location and magnitude of bed changes are properly simulated, which agrees with the measurement fairly
409 well and is not just limited to the circular areas but in other regions of the channel, where and how river
410 morphology changes are reasonably predicted. Inevitably, there are some discrepancies between the
411 measured and the modelled in terms of the depth in erosion and deposition. The measurements show that the
412 riverbed is changed in a wider area. The difference between the DoD and the modelled results is
413 demonstrated in Fig.9 (c). The mean difference between the two is in the range of (-0.78m – 0.92m), which
414 means only two-boulder diameters (diameter of a boulder is 0.4 m). The difference in the volume and depth
415 of bed changes is attributed to several uncertainty factors as investigated by Staines (2012). First, the time
416 scale between the measurement and the simulation is different; the time interval between the two DEMs
417 before and after the flood is ~ 5 years, yet the simulation time is only 6 hours for the flooding period. There
418 must be geomorphological activity during the 5 years which is one of the uncertainties in this study. Second,
419 the jökulhlaup can carry a large amount of sediment materials from upstream glacial areas, but it is difficult
420 to quantify the accurate volume. Furthermore, the empirical parameterisation for model input may influence
421 the simulated results, such as the Manning's value, the empirical transport rates, entrainment and deposition

422 fluxes. Fig. 10 plots the comparison at four cross sections to further demonstrate the agreement and
423 difference between the measurement and the simulation. It can be seen that the modelled bed agrees with the
424 surveyed bed after the flood very well at CS1 and CS3, while significant differences are found at some parts
425 of CS2 and CS4. As discussed before, the difference is caused by the uncertainties in the model and its
426 parameters. Overall, the present model is capable of predicting reasonably where and how the river
427 geomorphology changes during the 1999 jökulhlaup, which gives confidence for further assessment of the
428 geomorphological behaviours within the flooding.

429 From the final spatial pattern of net bed change, it is seen that the modelled outburst flood causes erosion
430 and deposition to occur in the main channel, and both are more severe in the narrower reach of the river,
431 because the water depth and flow velocity are higher in the narrower channel, increasing the bed shear stress,
432 which induces more sediments into motion. To further demonstrate flood-induced scour, Fig. 11 plots the
433 bed topography of a reach near the bridge before the flood, at the peak stage and after the flood. The changes
434 during the three stages clearly demonstrate that the main channel is expanded due to erosion. The temporal
435 evolution of the total erosion and deposition volume, as well as the net erosion are shown in Fig. 12. Points
436 of note, are that:

437 (1) the total erosion volume accumulates and increases rapidly in the rising phase of the flow discharge
438 as a result of the more intense bed shear stress, and the entrained sediment load in the water body then re-
439 deposits within a certain transport distance;

440 (2) during the peak flow stage, the total erosion and deposition volumes increase continually, and after
441 2.5 hours, both tend to reach an approximate constant value;

442 (3) the volume of net change (erosion minus deposition) steadily increases with the inundation time, i.e.
443 increasingly more sediment is entrained into the water body, which must increase the total fluid volume; this
444 outcome implies the bulk effects of sediment entrainment as shown in Section 4.4 above; (4) in the flood
445 recession limb, bed changes are weakened with slightly bedform development.

446 In this jökulhlaup, the final deposition volume is modelled to be approximately $5.5 \times 10^5 \text{ m}^3$ and the total
447 erosion volume to be about $7.4 \times 10^5 \text{ m}^3$. The net riverbed change is $1.9 \times 10^5 \text{ m}^3$, which indicates how much

448 sediment was transported into the downstream sea along with the jökulhlaup. The majority of the bed erosion
449 and deposition occurs within approximately 2-3 hours of the flood initiation; conversely, bed scour rarely
450 takes place in the recession limb of the flood. To demonstrate the sediment-laden flood inundation process,
451 Fig. 13 illustrates the water depth and the resulting spatial pattern of bed changes at several indicative time
452 steps. In summary, this sub-set of results indicates that:

- 453 • the outburst flood causes rapid geomorphological change; the bed degradation and aggradation
454 mostly occur in the initial 2-3 hours when the flood is increasing,
- 455 • net erosion occurs within the flood, and erosion increases progressively with inundation time, and
- 456 • the narrower the initial channel is, the more severe the flood-induced bed erosion and deposition.

457 In order to show the changes of flow conveyance capacity due to bed erosion and deposition, Manning's
458 equation is used to estimate the discharge capacity of an open channel following Pepper and Rickard (2009).

$$Q_c = \frac{AR^{2/3}\sqrt{i}}{n}$$

459 where: Q_c = discharge capacity (m^3/s); A = area of cross section of flow (m^2); $R = A/P$ = the hydraulic radius,
460 (m); P = wetted perimeter of the channel cross section (m); i = hydraulic gradient (usually approximated by
461 the longitudinal slope of the channel). The term, \sqrt{i}/n , could be approximately considered to be unchanged
462 before and after the flood. Thus, the changes of the flow conveyance capacity can be approximately taken as
463 A and P . At a single cross section, net erosion can lead to a significant increase of A , but the wetted perimeter
464 P is only slightly affected, resulting in an increase in $AR^{2/3}$. Net erosion increases with the inundation time
465 (Fig. 11). The final net eroded volume reaches $1.9 \times 10^5 \text{ m}^3$. This outcome implies that the flow conveyance
466 capacity of the river channel will be raised with the net increase of erosion in the channel, which also gives a
467 reason why the flood propagation is accelerated by the inclusion of sediment transport during the outburst
468 flood.

469 4.6. Wider discussion

470 Here we suggest that whilst the exact prediction of bed change is still unattainable, the application of
471 numerical models can enhance and improve insights into real-world outburst floods via both quantitative

472 analysis and qualitative assessment of the model outputs. Additionally, since any model output admittedly
473 has uncertainties, this study has sought to determine the sensitivity of a model to representations of the major
474 morphodynamic processes.

475 The previous theoretical, small-scale numerical and experimental studies (Bohorquez and Ancy, 2015;
476 Cao et al., 2004; Carrivick et al., 2011) have provided fundamental insight on the complex interaction
477 between outburst flows and a movable bed. However, these studies have unknown representation of
478 geomorphological processes within large-scale (field) outburst floods, because amongst other properties the
479 real-world topography is generally complex, the real-world grain size distribution is spatial varying, and the
480 real-world erosion and deposition in outburst floods occurs vertically and laterally. From a spatial-scale
481 application, this study found that the effects of sediment transport on flood dynamics were significant and
482 must be treated within outburst flood modelling (Fig. 6-Fig. 8). These findings agree with recent studies that
483 have also investigated the effects of morphological change on flood dynamics at large-scale, e.g. (Bohorquez
484 and Darby, 2008; Li et al., 2014; Wong et al., 2014). Wong et al. (2014) reported that the inclusion of bed
485 elevation changes appeared to alter flood dynamics locally, but that it was not significant for flood
486 inundation, so hydraulic models do not need to account for morphodynamic changes within events.
487 However, their study only considered bed erosion, and neglected deposition, which according to the findings
488 of this study cause effects on flood hydraulics that are far greater than for erosion. Furthermore, this study
489 has indicated that flow bulking effects due to sediment entrainment can influence flood propagation, and this
490 is a property of outburst floods that is not explicitly considered in the study of Wong et al.(2014). Li et al.
491 (2014) showed that very strong bed erosion and the decrease of bed friction due to bed change led to an
492 increase of peak flow discharge within hyperconcentrated floods in the Yellow River. Yet, in the study by Li
493 et al. (2014), the flood dynamics and geomorphological processes within floods were not identified. The
494 results presented in this study demonstrate that both water surface and water depth at the peak stage were
495 reduced in most areas of the river channel with consideration of morphological changes, the flood
496 propagation was accelerated notably, peak flows in particular, and the water volume was increased because
497 of sediment entrainment. The inundation extent was slightly affected by morphological changes for the
498 specific case (Table 6) in general agreement with the finding by Wong et al. (2014). We also found that

499 morphological changes caused river channel adjustment conducive to flood propagation (Fig. 12), which
500 reflected the effects of sediment transport on flood dynamics. The fundamental reasons that sediment
501 transport affects flood dynamics can be summarized as: (1) sediment entrainment into the floodwater and the
502 rheology of sediments increase the density of the fluid flows, thereby increasing the flow mass and
503 accelerating flood propagation; (2) the flood-induced net erosion enhanced the flow conveyance capacity of
504 the river channel, which is elucidated above in Section 4.5. All these results greatly improved the
505 understanding of the importance of geomorphological changes within inundation modelling.

506 In this study, the morphodynamic model has quantified the spatio-temporal bed degradation and
507 aggradation, including spatial patterns, volumes and rates, caused by the 1999 jökulhlaup. Although there is
508 a discrepancy between the modelled landscape changes and the DoD because of the uncertain sediment
509 activity during the long-time interval (5 years) for measurements before and after the flood (Staines, 2012),
510 the morphodynamic model predicted the landscape change pattern in general agreement with the measured
511 pattern. This gives confidence in the assessment of geomorphological impacts during the 1999 jökulhlaup
512 quantitatively and qualitatively via the morphodynamic model. Future studies can use the model presented
513 herein to assess flood-induced geomorphological changes in the context of annual and seasonal intra-
514 catchment sediment fluxes and geomorphological activity (e.g.(Carrivick et al., 2013a)). In the modelled
515 jökulhlaup, the geomorphological changes were more severe when the flood was at the rising and peak stage.
516 The temporal change of total erosion and deposition volume within the outburst flood increased rapidly on
517 the rising limb and was slowed down in the flood recession. This relative timing of geomorphological work
518 was also reported in the study of (Carrivick et al., 2010). Additionally, we found in this study that
519 geomorphological adjustments by an outburst flood can modify bed friction which with the new topography
520 can further alter the dynamics of subsequent floods in flood sequences. This has revealed the importance and
521 necessity for river flood modelling to consider the associated geomorphological impacts. In summation, the
522 prediction of both hydrodynamic and morphodynamic aspects of outburst floods can provide valuable
523 information for flood risk assessment that hydrodynamic models run over a fixed bed cannot.

524 5. Conclusions

525 This study presented a 2D hydro-morphodynamic model designed for outburst floods which consider a
526 bedload and suspended load, non-uniform sediment grain-size distribution effects, bed slope effects and
527 different velocities for each vertical layer. A large-scale volcano-induced jökulhlaup has been reproduced by
528 this model. Comparison with the surveyed landscape change has indicated that the model is capable of
529 predicting geomorphological changes due to a jökulhlaup reasonably well. Based on the results and
530 discussion presented above, the study improved understanding of geomorphological processes within the
531 1999 jökulhlaup and the effects of river channel changes on flood dynamics.

532 In this study of the Sólheimajökull flood, it has been calculated that a large amount of sediments of the
533 order of 10^5 m^3 transport occurred during the jökulhlaup. The net change (minus) occurred during the whole
534 flood period, and the net volume increased along with the flood (Fig. 12). It was also found that bed changes
535 were more active in the rising limb during which over 75% bed changes were finished. The peak erosion rate
536 and deposition rate occurred at the peak stage. In the falling limb, there was only slight bedform
537 development, but both total erosion and deposition volume did not increase greatly (Fig. 12).

538 More widely, it has firstly been confirmed that grain-size significantly affects the geomorphological
539 changes because of the resulting effects on Manning's roughness and bed shear stress. This suggests that a
540 representative parameterisation of spatially varying grain-size is vital for morphodynamic modelling of real-
541 life floods with geomorphological changes. For numerical modelling, although the accuracy of sediment
542 transport formula is generally considered poor, the features of riverbed changes are not greatly influenced by
543 the choice of formulae. The influence of DEM resolution is also insignificant in quantifying outburst flood
544 dynamics and geomorphological changes.

545 Secondly, the analysis has verified that the net change (minus) during an outburst flood can lead to an
546 increase of the flow conveyance capacity of the river channel, and the in-channel scour can reduce the
547 Manning's value. This implies that flood propagation becomes 'smoother' or 'easier' due to rapid river
548 channel adjustment. This is why the inclusion of sediment transport and geomorphological changes
549 accelerate the inundation over the hydrodynamic modelling over fixed bed. Effects of geomorphological
550 changes on flood dynamics are also apparent in water levels and water depths within the river channel that

551 are mostly reduced for an event where net erosion occurs. Furthermore, the bulking effects of intense and
552 voluminous sediment entrainment increase not only the flow volume, but also the downstream peak
553 discharge, and the increase rate is dependent on how much sediment is entrained to floods. This effect of
554 morphodynamics is very important because water levels, peak flow, and the time of flood are the generally
555 preferred important indicators for flood risk assessment. Therefore, a major implication of this study is the
556 verification of the significant impacts of geomorphological changes on hydraulics required for flood risk
557 assessment during an event where erosion and deposition is severe.

558 **References**

- 559 Alho, P., Russell, A.J., Carrivick, J.L., Käyhkö, J., 2005. Reconstruction of the largest Holocene jökulhlaup within
560 Jökulsá á Fjöllum, NE Iceland. *Quaternary Science Reviews*, 24(22): 2319-2334.
561 DOI:10.1016/j.quascirev.2004.11.021
- 562 Begnudelli, L., Sanders, B.F., 2006. Unstructured grid finite-volume algorithm for shallow-water flow and scalar
563 transport with wetting and drying. *Journal of Hydraulic Engineering-ASCE*, 132(4): 371-384.
564 DOI:10.1061/(asce)0733-9429(2006)132:4(371)
- 565 Berzi, D., Jenkins, J.T., 2008. A theoretical analysis of free-surface flows of saturated granular-liquid mixtures. *Journal*
566 *of Fluid Mechanics*, 608: 393-410. DOI:doi:10.1017/S0022112008002401
- 567 Bohorquez, P., Ancey, C., 2015. Stochastic-deterministic modeling of bed load transport in shallow water flow over
568 erodible slope: Linear stability analysis and numerical simulation. *Advances in Water Resources*, 83(0): 36-54.
569 DOI:<http://dx.doi.org/10.1016/j.advwatres.2015.05.016>
- 570 Bohorquez, P., Darby, S.E., 2008. The use of one- and two-dimensional hydraulic modelling to reconstruct a glacial
571 outburst flood in a steep Alpine valley. *Journal of Hydrology*, 361(3-4): 240-261.
572 DOI:<http://dx.doi.org/10.1016/j.jhydrol.2008.07.043>
- 573 Camenen, B., Larson, M., 2005. A general formula for non-cohesive bed load sediment transport. *Estuarine, Coastal*
574 *and Shelf Science*, 63(1-2): 249-260. DOI:<http://dx.doi.org/10.1016/j.ecss.2004.10.019>
- 575 Cao, Z., Pender, G., Wallis, S., Carling, P., 2004. Computational dam-break hydraulics over erodible sediment bed.
576 *Journal of Hydraulic Engineering-ASCE*, 130(7): 689-703. DOI:10.1061/(asce)0733-9429(2004)130:7(689)
- 577 Carling, P. et al., 2010. Unsteady 1D and 2D hydraulic models with ice dam break for Quaternary megaflood, Altai
578 Mountains, southern Siberia. *Global and Planetary Change*, 70(1-4): 24-34. DOI:10.1016/j.gloplacha.2009.11.005

579 Carling, P.A., 2013. Freshwater megaflood sedimentation: What can we learn about generic processes? *Earth-Science*
580 *Reviews*, 125(0): 87-113. DOI:<http://dx.doi.org/10.1016/j.earscirev.2013.06.002>

581 Carrivick, J.L. et al., 2013a. Contemporary geomorphological activity throughout the proglacial area of an alpine
582 catchment. *Geomorphology*, 188(0): 83-95. DOI:<http://dx.doi.org/10.1016/j.geomorph.2012.03.029>

583 Carrivick, J.L., Jones, R., Keevil, G., 2011. Experimental insights on geomorphological processes within dam break
584 outburst floods. *Journal of Hydrology*, 408(1–2): 153-163. DOI:10.1016/j.jhydrol.2011.07.037

585 Carrivick, J.L., Manville, V., Graettinger, A., Cronin, S.J., 2010. Coupled fluid dynamics-sediment transport modelling
586 of a Crater Lake break-out lahar: Mt. Ruapehu, New Zealand. *Journal of Hydrology*, 388(3-4): 399-413.
587 DOI:10.1016/j.jhydrol.2010.05.023

588 Carrivick, J.L., Rushmer, E.L., 2006. Understanding high-magnitude outburst floods. *Geology Today*, 22(2): 60-65.
589 DOI:10.1111/j.1365-2451.2006.00554.x

590 Carrivick, J.L., Turner, A.G.D., Russell, A.J., Ingeman-Nielsen, T., Yde, J.C., 2013b. Outburst flood evolution at
591 Russell Glacier, western Greenland: effects of a bedrock channel cascade with intermediary lakes. *Quaternary*
592 *Science Reviews*, 67(0): 39-58. DOI:<http://dx.doi.org/10.1016/j.quascirev.2013.01.023>

593 Cheng, N., 2002. Exponential Formula for Bedload Transport. *Journal of Hydraulic Engineering*, 128(10): 942-946.
594 DOI:doi:10.1061/(ASCE)0733-9429(2002)128:10(942)

595 Dai, F.C., Lee, C.F., Deng, J.H., Tham, L.G., 2005. The 1786 earthquake-triggered landslide dam and subsequent dam-
596 break flood on the Dadu River, southwestern China. *Geomorphology*, 65(3-4): 205-221.
597 DOI:10.1016/j.geomorph.2004.08.011

598 Fischer-Antze, T., Olsen, N.R.B., Gutknecht, D., 2008. Three-dimensional CFD modeling of morphological bed
599 changes in the Danube River. *Water Resources Research*, 44(9): W09422. DOI:10.1029/2007WR006402

600 Fraccarollo, L., Capart, H., 2002. Riemann wave description of erosional dam-break flows. *Journal of Fluid Mechanics*,
601 461: 183-228. DOI:<http://dx.doi.org/10.1017/S0022112002008455>

602 Greimann, B., Lai, Y., Huang, J.C., 2008. Two-dimensional total sediment load model equations. *Journal of Hydraulic*
603 *Engineering-ASCE*, 134(8): 1142-1146. DOI: [http://dx.doi.org/10.1061/\(ASCE\)0733-9429\(2008\)134:8\(1142\)](http://dx.doi.org/10.1061/(ASCE)0733-9429(2008)134:8(1142))

604 Guan, M., Wright, N., Sleigh, P., 2013. A robust 2D shallow water model for solving flow over complex topography
605 using homogenous flux method. *International Journal for Numerical Methods in Fluids*, 73(3): 225-249.
606 DOI:10.1002/flid.3795

607 Guan, M., Wright, N., Sleigh, P., 2014. 2D Process based morphodynamic model for flooding by noncohesive dyke
608 breach. *Journal of Hydraulic Engineering*, 140(7). DOI:10.1061/(ASCE)HY.1943-7900.0000861

609 Guan, M., Wright, N., Sleigh, P., 2015. Multimode morphodynamic model for sediment-laden flows and geomorphic
610 impacts. *Journal of Hydraulic Engineering*. DOI:doi:10.1061/(ASCE)HY.1943-7900.0000997

611 Huang, W., Cao, Z.-x., Carling, P., Pender, G., 2014. Coupled 2D hydrodynamic and sediment transport modeling of
612 megaflood due to glacier dam-break in Altai Mountains, Southern Siberia. *J. Mt. Sci.*, 11(6): 1442-1453.
613 DOI:10.1007/s11629-014-3032-2

614 Huggel, C., Kaab, A., Haerberli, W., Teyssere, P., Paul, F., 2002. Remote sensing based assessment of hazards from
615 glacier lake outbursts: a case study in the Swiss Alps. *Canadian Geotechnical Journal*, 39(2): 316-330.
616 DOI:10.1139/t01-099

617 Khosronejad, A., Rennie, C., Salehi Neyshabouri, S., Townsend, R., 2007. 3D Numerical modeling of flow and
618 sediment transport in laboratory channel bends. *Journal of Hydraulic Engineering*, 133(10): 1123-1134.
619 DOI:doi:10.1061/(ASCE)0733-9429(2007)133:10(1123)

620 Li, W., van Maren, D.S., Wang, Z.B., de Vriend, H.J., Wu, B., 2014. Peak discharge increase in hyperconcentrated
621 floods. *Advances in Water Resources*, 67(0): 65-77. DOI:<http://dx.doi.org/10.1016/j.advwatres.2014.02.007>

622 Manville, V., White, J.D.L., Houghton, B.F., Wilson, C.J.N., 1999. Paleohydrology and sedimentology of a post-1.8 ka
623 breakout flood from intracaldera Lake Taupo, North Island, New Zealand. *Geological Society of America Bulletin*,
624 111(10): 1435-1447. DOI:10.1130/0016-7606(1999)111<1435:pasoa>2.3.co;2

625 Meyer-Peter, E., Müller, R., 1948. *Formulas for bed load transport*, Stockholm, Sweden.

626 Nicholas, A.P., 2003. Investigation of spatially distributed braided river flows using a two-dimensional hydraulic
627 model. *Earth Surface Processes and Landforms*, 28(6): 655-674. DOI:10.1002/esp.491

628 Nielsen, P., 1992. *Coastal bottom boundary layers and sediment transport*. Advanced Series on Ocean Engineering, 4.
629 World Scientific, 324 pp.

630 Pepper, A., Rickard, C., 2009. Works in the river channel. In: Ackers, J.C., Rickard, C.E., Gill, D.S. (Eds.), *Fluvial*
631 *Design Guide*. Environment Agency, pp. 8.1-8.36.

632 Pugh, F.J., Wilson, K.C., 1999. Velocity and concentration distributions in sheet flow above plane beds. *Journal of*
633 *Hydraulic Engineering-ASCE*, 125(2): 117-125. DOI:10.1061/(asce)0733-9429(1999)125:2(117)

634 Roberts, M.J., Tweed, F.S., Russell, A.J., Knudsen, Ó., Harris, T.D., 2003. Hydrologic and geomorphic effects of
635 temporary ice-dammed lake formation during jökulhlaups. *Earth Surface Processes and Landforms*, 28(7): 723-737.
636 DOI:10.1002/esp.476

637 Russell, A.J., Tweed, F.S., Knudsen, Ó., 2000. Flash flood at Sólheimajökull heralds the reawakening of an Icelandic
638 subglacial volcano. *Geology Today*, 16(3): 102-106. DOI:10.1046/j.1365-2451.2000.00005.x

639 Russell, A.J. et al., 2010. An unusual jökulhlaup resulting from subglacial volcanism, Sólheimajökull, Iceland.
640 Quaternary Science Reviews, 29(11–12): 1363-1381. DOI:<http://dx.doi.org/10.1016/j.quascirev.2010.02.023>

641 Shimizu, Y., Yamaguchi, H., Itakura, T., 1990. Three-dimensional computation of flow and bed deformation. Journal of
642 Hydraulic Engineering, 116(9): 1090-1108. DOI:doi:10.1061/(ASCE)0733-9429(1990)116:9(1090)

643 Sigurdsson, O., Zóphóníasson, S., Ísleifsson, E., 2000. Jökulhlaup úr Sólheimajökull 18. júlí 1999. , 49. , Jökull, 49: 75-
644 81.

645 Smart, G., Jäggi, M., 1983. Sediment transport on steep slopes. Mitteilung. 64. Versuchsanstalt für Wasserbau,
646 Hydrologie und Glaziologie, ETH Zurich, Zurich.

647 Soulsby, R., 1997. Dynamics of marine sands: a manual for practical applications. Thomas Telford, London, UK, 249
648 pp.

649 Staines, K.E.H., 2012. Quantifying Landscape Change in a Jökulhlaup-prone Proglacial System Sólheimajökull,
650 Southern Iceland, University of Leeds, Leeds, UK, 224 pp.

651 Staines, K.E.H., Carrivick, J.L., 2015. Geomorphological impact and morphodynamic effects on flow conveyance of
652 the 1999 jökulhlaup at sólheimajökull, Iceland. Earth Surface Processes and Landforms: n/a-n/a.
653 DOI:10.1002/esp.3750

654 Staines, K.E.H. et al., 2014. A multi-dimensional analysis of pro-glacial landscape change at Sólheimajökull, southern
655 Iceland. Earth Surface Processes and Landforms: n/a-n/a. DOI:10.1002/esp.3662

656 Sumer, B.M., Kozakiewicz, A., Fredsoe, J., Deigaard, R., 1996. Velocity and concentration profiles in sheet-flow layer
657 of movable bed. Journal of Hydraulic Engineering-ASCE, 122(10): 549-558.
658 DOI:[http://dx.doi.org/10.1061/\(ASCE\)0733-9429\(1996\)122:10\(549\)](http://dx.doi.org/10.1061/(ASCE)0733-9429(1996)122:10(549))

659 van Rijn, L.C., 1984. Sediment transport part II, suspended load transport. Journal of Hydraulic Engineering-ASCE,
660 110 (11): 1613–1641. DOI:[http://dx.doi.org/10.1061/\(ASCE\)0733-9429\(1984\)110:11\(1613\)](http://dx.doi.org/10.1061/(ASCE)0733-9429(1984)110:11(1613))

661 Villanueva, I., Wright, N.G., 2006. Linking Riemann and storage cell models for flood prediction. Proceedings of the
662 ICE - Water Management, 159(1): 27-33. DOI:10.1680/wama.2006.159.1.27

663 Westoby, M.J. et al., 2014. Modelling outburst floods from moraine-dammed glacial lakes. Earth-Science Reviews,
664 134(0): 137-159. DOI:<http://dx.doi.org/10.1016/j.earscirev.2014.03.009>

665 Wong, J.S., Freer, J.E., Bates, P.D., Sear, D.A., Stephens, E.M., 2014. Sensitivity of a hydraulic model to channel
666 erosion uncertainty during extreme flooding. Hydrological Processes. DOI:10.1002/hyp.10148

667 Wu, W., 2004. Depth-averaged two-dimensional numerical modeling of unsteady flow and nonuniform sediment
668 transport in open channels. *Journal of Hydraulic Engineering-ASCE*, 130(10): 1013-1024.
669 DOI:[http://dx.doi.org/10.1061/\(ASCE\)0733-9429\(2004\)130:10\(1013\)](http://dx.doi.org/10.1061/(ASCE)0733-9429(2004)130:10(1013))

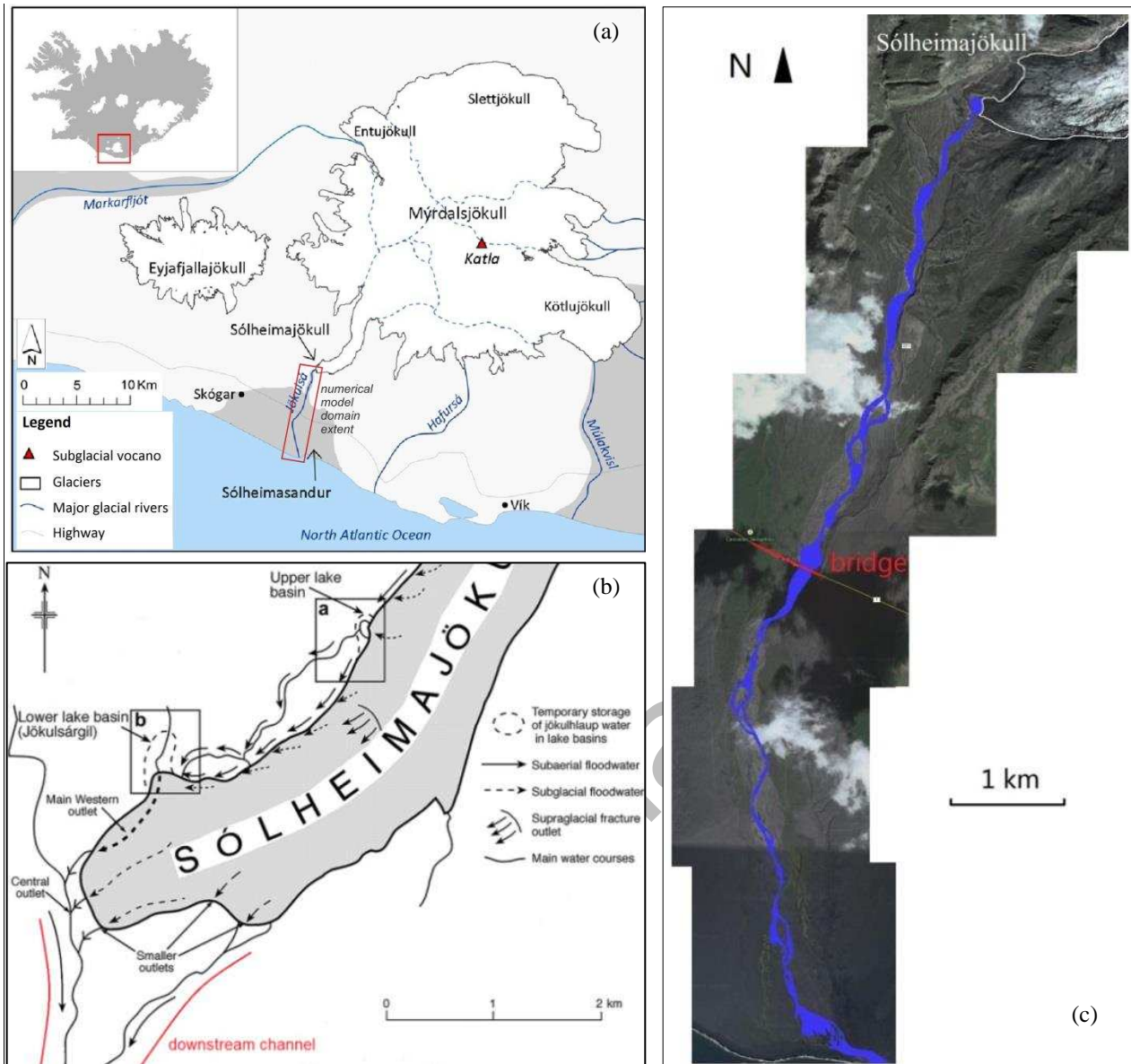
670 Wu, W., Rodi, W., Wenka, T., 2000. 3D numerical modeling of flow and sediment transport in open channels. *Journal*
671 *of Hydraulic Engineering*, 126(1): 4-15.

672 Yang, H., Lin, B., Zhou, J., 2015. Physics-based numerical modelling of large braided rivers dominated by suspended
673 sediment. *Hydrological Processes*, 29(8): 1925-1941. DOI:10.1002/hyp.10314

674 Zech, Y., Soares-Frazao, S., Spinewine, B., Grelle, N.L., 2008. Dam-break induced sediment movement: Experimental
675 approaches and numerical modelling. *Journal of Hydraulic Research*, 46(2): 176-190.
676 DOI:10.1080/00221686.2008.9521854

677
678

Accepted Manuscript



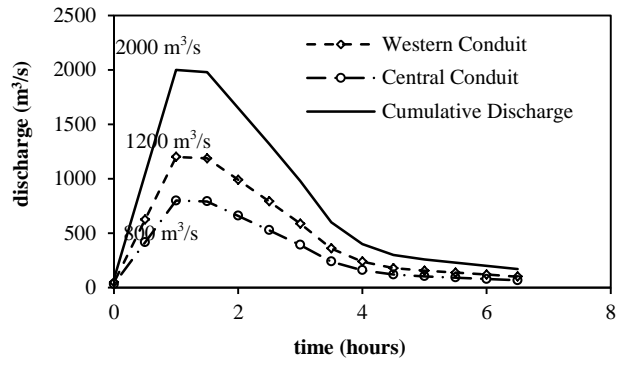
679

680 Fig. 1. (a) The location of the glacier, (b) the July 1999 flood route ways and temporary floodwater storage locations

681 (Russell et al., 2010), (c) the studied river channel for numerical modelling

682

683



684

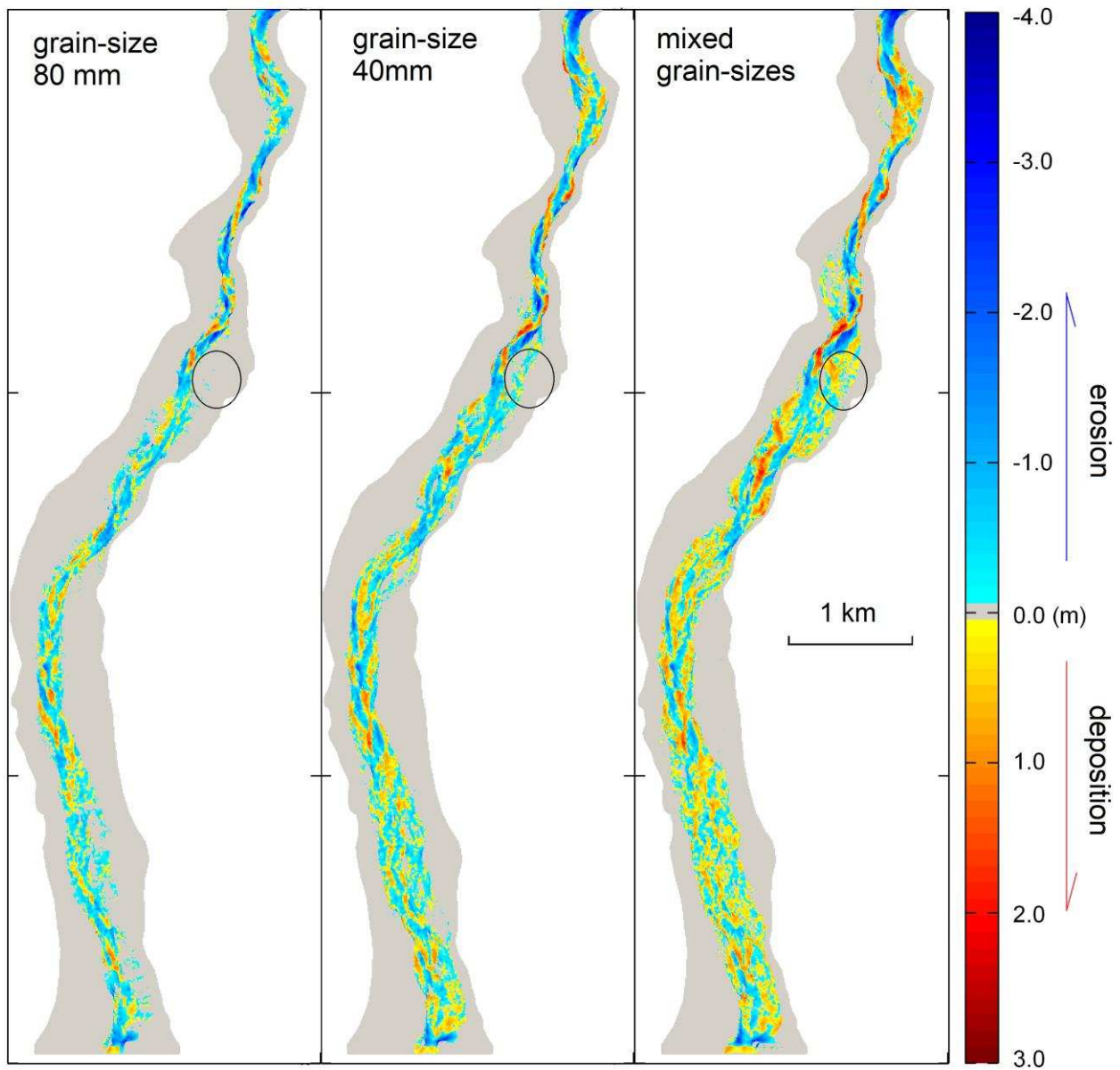
685

686

687

Fig. 2 The hydrograph from Western Conduit, Central Conduit and cumulative inflow discharge

Accepted Manuscript

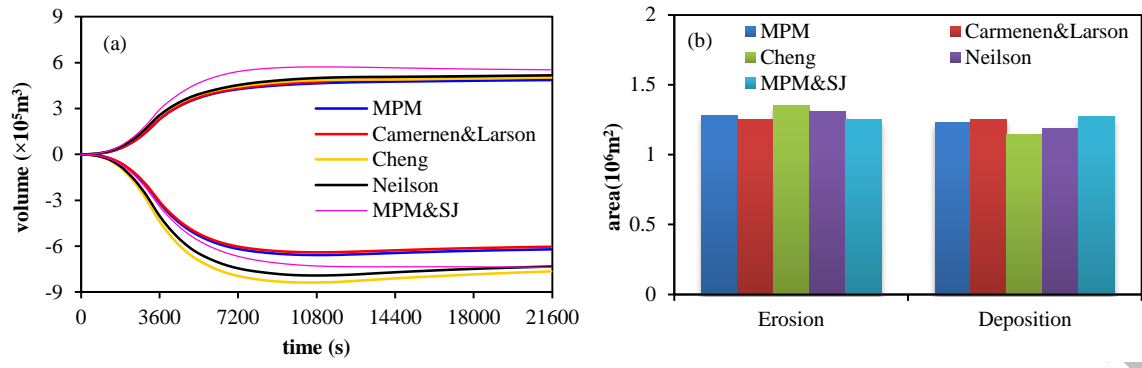


688

689 Fig. 3. The simulated spatial distribution of net bed erosion and deposition for the three parameterisations of grain-size

690

Accepted



691

692 Fig. 4. (a) Temporal changes of modelled erosion and deposition volumes, note: negative values denotes erosion

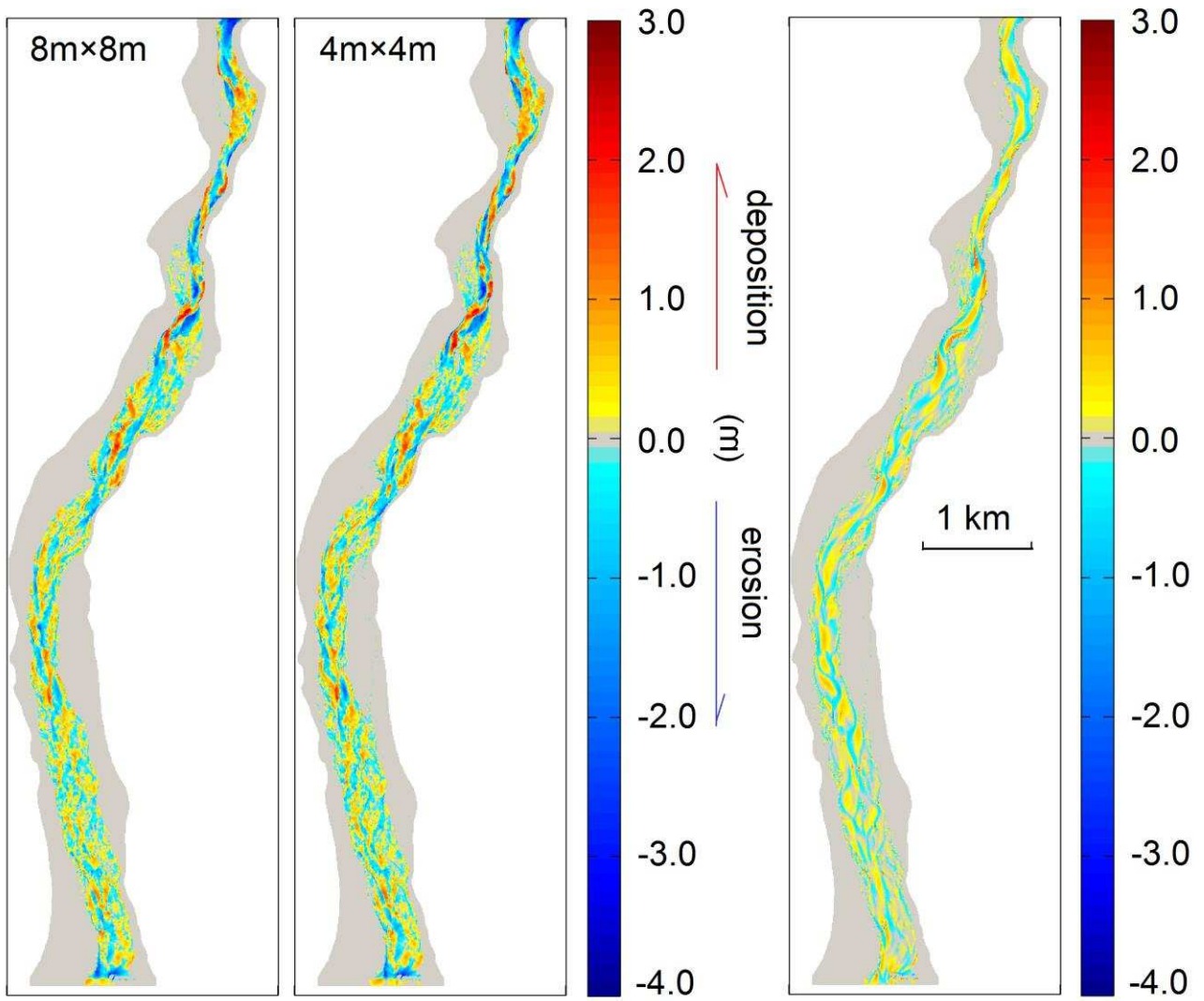
693 volume, positive value represents deposition volume, and (b) the final erosion area and deposition area in the

694 river channel

695

696

Accepted Manuscript



697

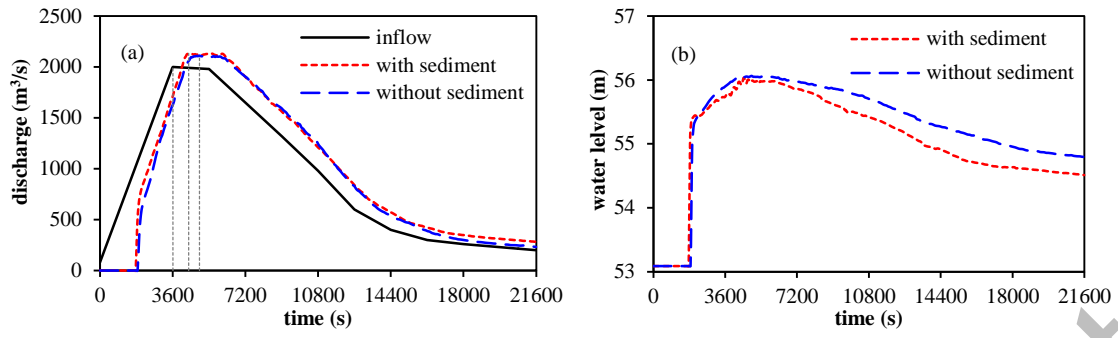
698 Fig. 5. Spatial pattern of modelled erosion and deposition for the simulations with DEMs of 4m×4m and 8m×8m, and

699 the difference between the two runs (DEM with 4m×4m minus DEM with 8m×8m)

700

701

Accepted



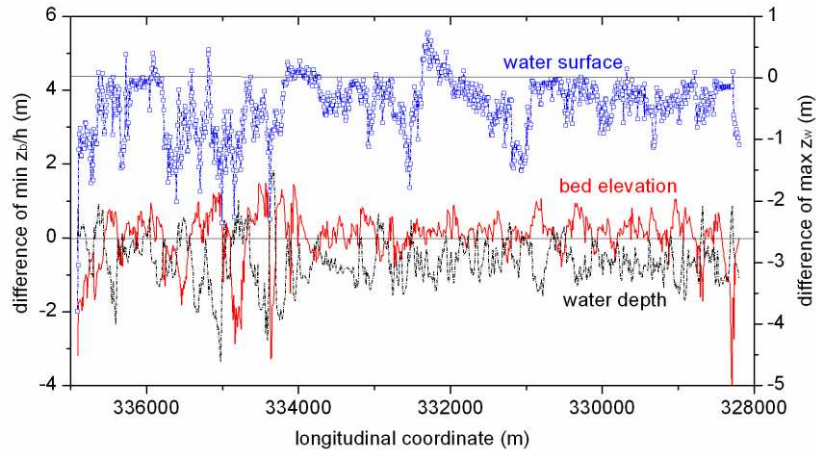
702

703 Fig. 6. (a) The temporal change of flow discharge at the cross section $x=332908.86$; and (b) the temporal change of
 704 water depth at the gauge (332908.86, 480099.78)

705

706

Accepted Manuscript



707

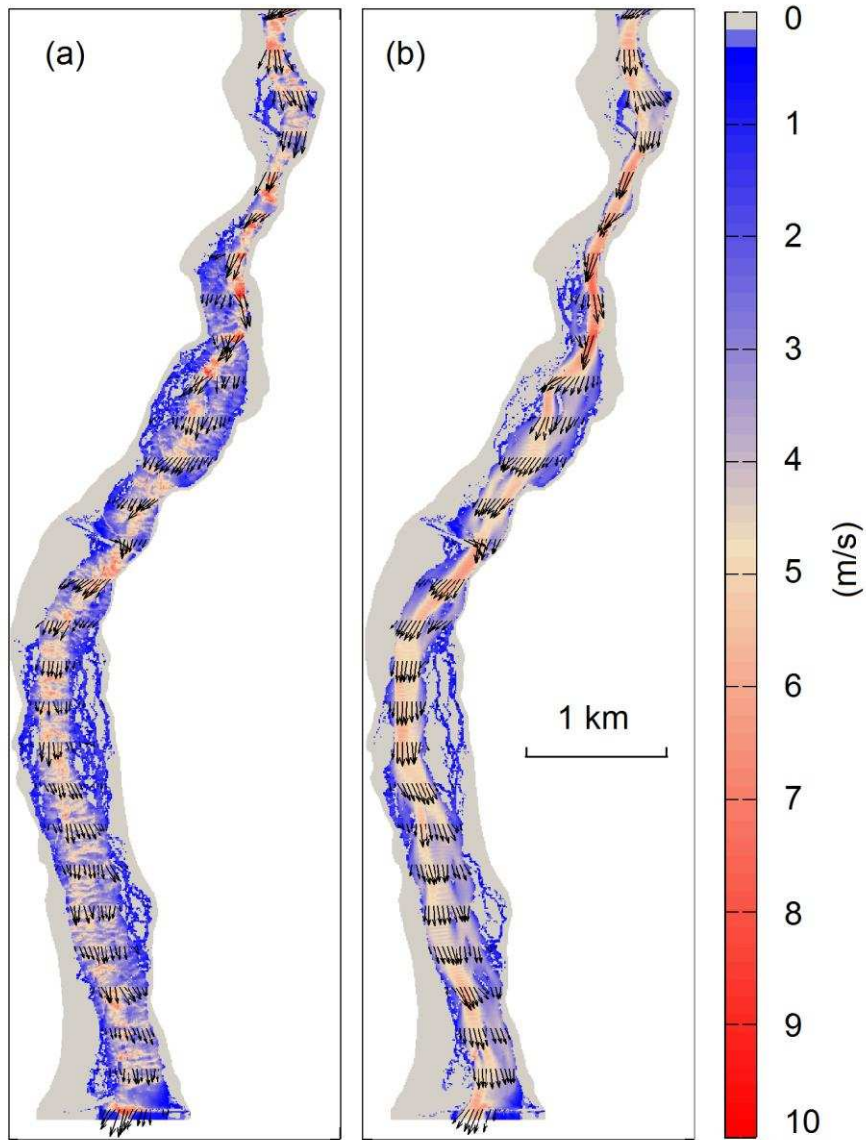
708 Fig. 7. The differences of the modelled results with and without the inclusion of sediment transport, including the

709 minimum water level, the minimum water depth, and the minimum bed elevation; herein $\Delta\eta = \eta_{sed} -$

710 $\eta_{no\ sed}, \Delta h = h_{sed} - h_{no\ sed}, \Delta z = z_{sed} - z_{no\ sed}$

711

Accepted Manuscript



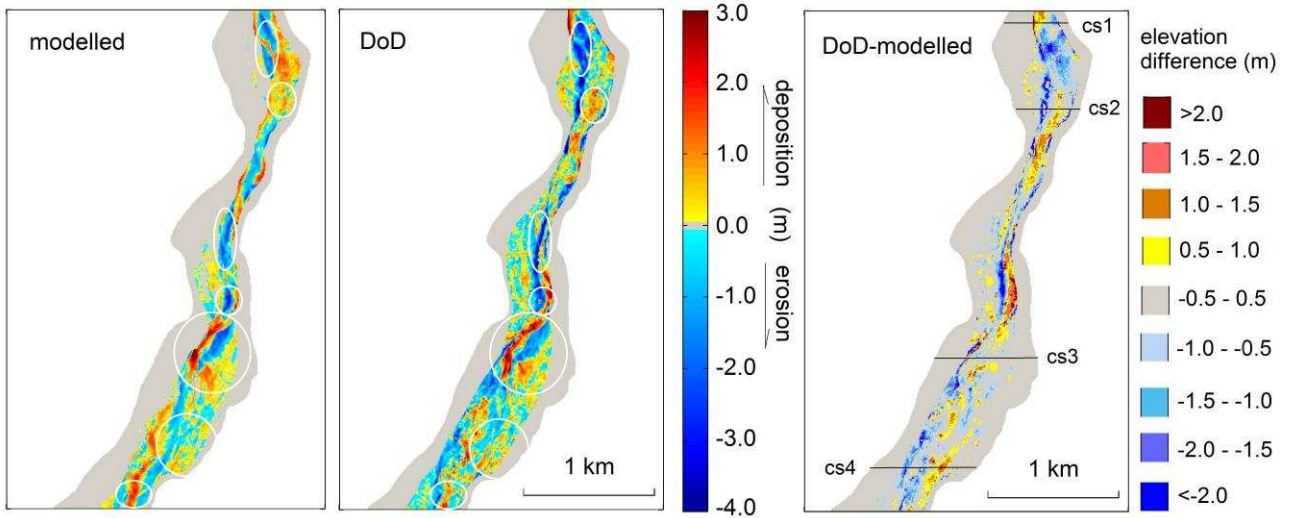
712

713 Fig. 8. The spatial pattern of the modelled velocity field, and the velocity vectors at some cross-sections with and

714 without the consideration of geomorphological changes at the peak stage $t = 2$ hours; (a) the modelled result

715 without morphological changes, (b) the modelled results with morphological changes

716



717

718 Fig. 9. Comparison of the modelled bed changes (a) and the measured differenced DEM between the pre-flood DEM

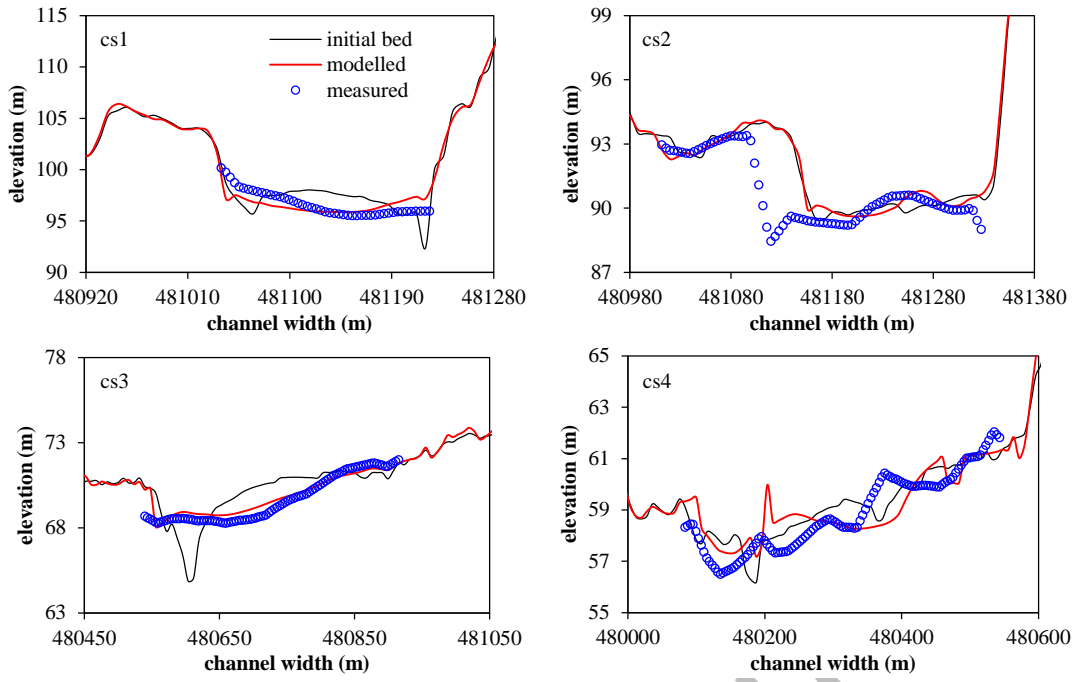
719 and the post-flood DEM (b), and (c) the elevation difference between the modelled and the measured bed

720 changes (measured bed minus modelled bed); the while circles represent several highlight zones.

721

722

Accepted Manuscript



723

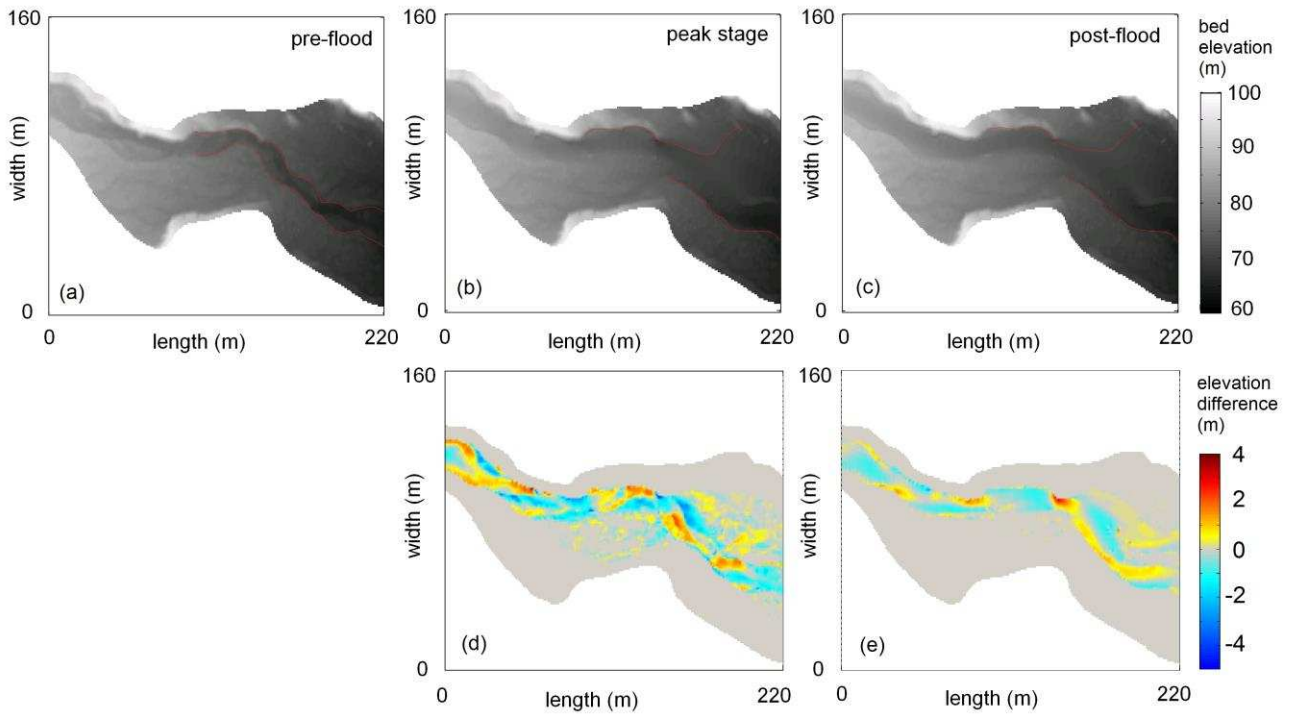
724

725

Fig. 10. Comparison of the modelled bed profiles and the measured ones at the four cross-sections shown in Fig. 9(c).

726

727



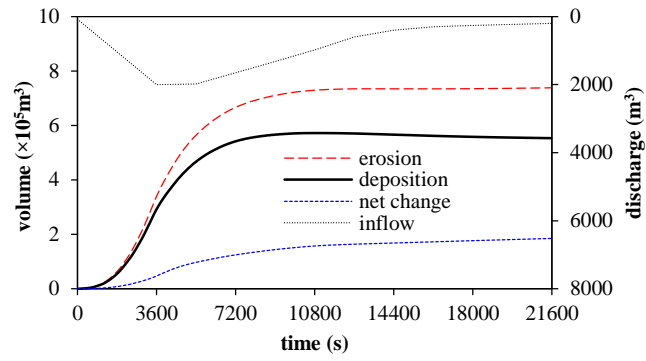
728

729 Fig. 11. Bed elevation of a short reach near the bridge (a) before flood; (b) at peak stage; (c) after flood; as well as the

730 difference of bed elevation between each other, (d) = (b) - (a), (e) = (c) - (b)

731

732



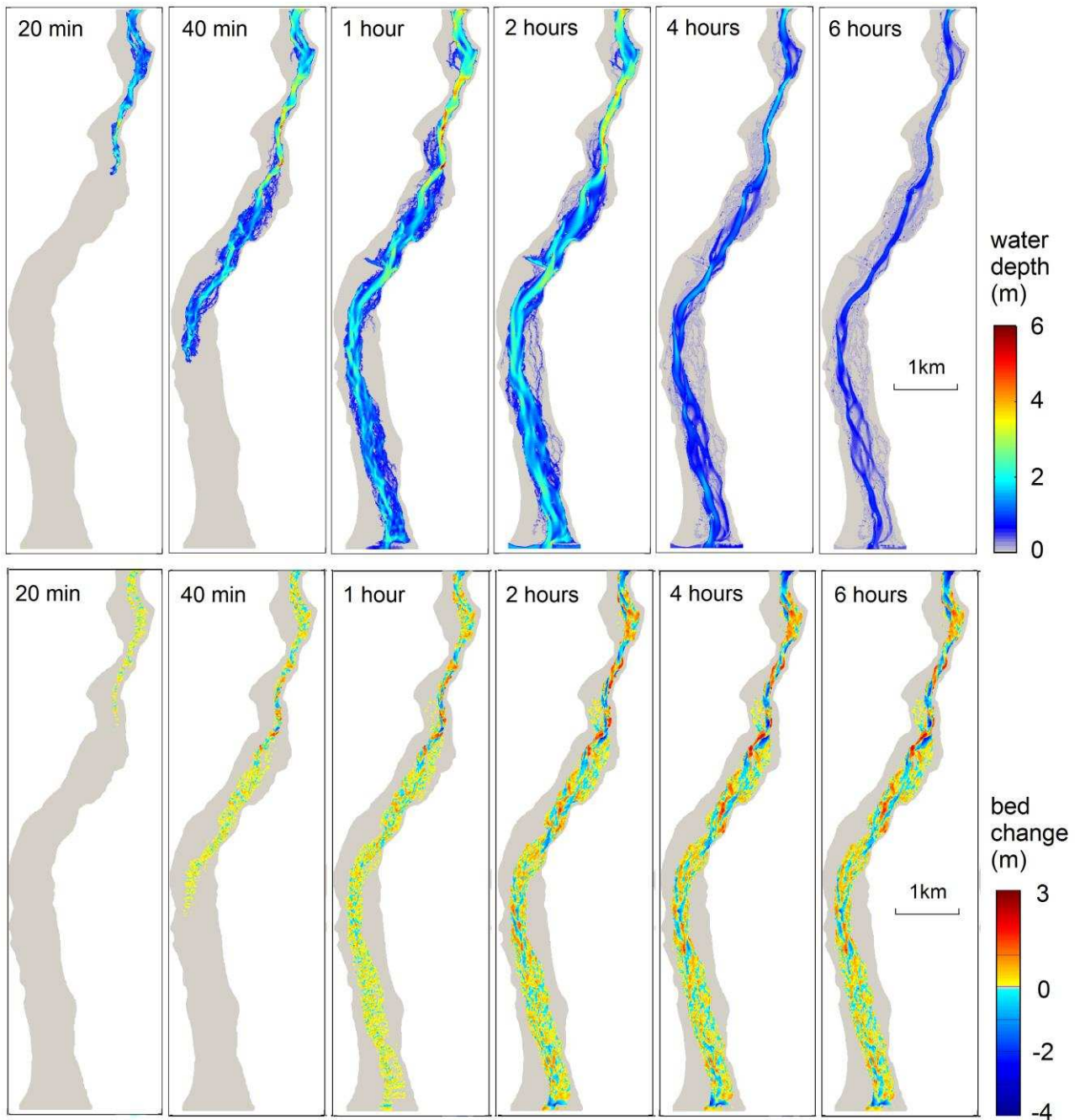
733
734

Fig. 12. Temporal volume evolution for total erosion, deposition, and net riverbed change (erosion minus deposition)

735

736

Accepted Manuscript



737

738 Fig. 13. Spatial pattern of the modelled water depth (the upper row) and bed changes (the lower row),

739 1 hour, 2 hours, 4 hours and 6 hours after the flood initiation; note: for the bed changes, negative value denotes

740 erosion depth, and positive value represents deposition depth

741