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Abstract: Crystal nucleation in food colloids is considered in the light of recent developments in classical nucleation theory (CNT); it is shown that CNT remains a sound basis upon which to understand nucleation in colloids and in particular nucleation in lipids such as triacylglycerols. Computation of the energy barrier to nucleation for a studied triacylglycerol system (Cocoa butter oil-in-water emulsion) indicates that whilst homogeneous nucleation is unlikely at higher surface energies the addition of surfactant, lowering the interfacial energy may have a dramatic impact on surface nucleation rates. Data is included supporting this contention. The impact of reducing the size of colloidal particles to the point where the interfacial region occupies a significant proportion of the total volume of the dispersed phase is discussed and it is suggested that in these circumstances undercooling may fall significantly in comparison with the undercooling measured in micrometer emulsions.

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Dear Professor Phillips,

Festschrift for Professor Eric Dickinson

I am pleased to submit my revised version of my manuscript.

Best wishes,

Malcolm Povey

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*Detailed Response to Reviewers

All the reviewers comments have been accepted and responded to.

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For Food Hydrocolloids: Crystallization in colloids

1 **Crystal nucleation in food colloids**

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5

6 *Abstract*

7 Abstract

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9 classical nucleation theory (CNT); it is shown that CNT remains a sound basis upon which to
10 understand nucleation in colloids and in particular nucleation in lipids such as
11 triacylglycerols. Computation of the energy barrier to nucleation for a studied triacylglycerol
12 system (Cocoa butter oil-in-water emulsion) indicates that whilst homogeneous nucleation is
13 unlikely at higher surface energies the addition of surfactant, lowering the interfacial energy
14 may have a dramatic impact on surface nucleation rates. Data is included supporting this
15 contention. The impact of reducing the size of colloidal particles to the point where the
16 interfacial region occupies a significant proportion of the total volume of the dispersed phase
17 is discussed and it is suggested that in these circumstances undercooling may fall
18 significantly in comparison with the undercooling measured in micrometer emulsions.

19 Keywords: Crystal, nanoparticle, colloid, emulsion, ultrasound, sound speed

20 **1 Introduction**

21 It was Eric Dickinson who showed me that it was possible to carry out scientifically rigorous
22 and repeatable measurements on systems which gave insight into the behaviour and structure
23 of food. I had begun my scientific career in Food Science by studying ultrasound propagation
24 in whole eggs with a view to developing a practical method for the automated testing of eggs.
25 I was immediately confronted with the problem that no two eggs were the same acoustically
26 and there began my transformation from physicist to physicist and food scientist. Eric's
27 method was a form of reductionism in which a food system like milk was modelled by
28 producing a much simpler but reproducible system such as n-alkane oil in water emulsion. At
29 the time he was criticised for studying these model systems on the basis that they were not
30 real foods and were usually comprised of materials you would not dream of eating. Looking
31 back now of course, it is possible to see that this method helped establish the science of food
32 colloids as a scientific discipline, a discipline which has underpinned a whole variety of
33 innovations in practical food production involving foods as diverse as cream liqueurs through
34 fatty spreads to dairy products.

35 From my point of view as a physicist, collaboration with a chemical physicist such as Eric
36 gave me access to a laboratory containing a wide variety of colloid characterisation
37 techniques which allowed me to test my new ultrasound techniques using well characterised
38 and reproducible systems. We collaborated in the development of techniques for the study of
39 colloid stability and also crystallisation in emulsions, part of the subject of this paper.

40 **2 Nucleation Theory**

41 **2.1 Introduction**

42 In this work we consider crystal nucleation and growth in the dispersed phase of a colloidal
43 system. By a colloidal system is meant any substance dispersed through another with particle
44 diameters between 2 nm and 2000 nm, although the suspending phase considered will always
45 be water. Micro emulsions are excluded from this discussion in order to keep it short. There
46 is no discussion here of the impact of van der Waals forces although it is common knowledge
47 that these dominate the interactions between small colloidal particles and are responsible for
48 the well-known phenomenon of nano-particle aggregation.

49 We adopt the approach that there are three phases in crystallization: induction, nucleation and
50 growth. Firstly we consider the relevance of classical nucleation theory and briefly explain
51 what it is, then consider its application to bulk fluids and finally to colloidal fluids. This work
52 will not consider the growth phase in any detail, primarily because nucleation is the rate
53 limiting step for crystallization in colloids.

54 Crystallization in emulsions is an increasingly important area both technically and
55 scientifically. Agrochemicals, pharmaceuticals (Espitalier, Biscans, Authelin, & Laguerie,
56 1997), ceramic manufacture, food, cosmetics (Wang & Lee, 1997), speciality chemicals,
57 photographic emulsions are examples of processes where emulsion crystallization is employed
58 or in development. In ceramics manufacture emulsion crystallization offers more uniform
59 stoichiometry, smaller ceramic particle size and a superior fired ceramic (Hirai, Hariguchi,
60 Komasaawa, & Davey, 1997; Hirai, Okamoto, & Komasaawa, 1998) and is one example of
61 materials processing based on emulsions (Bibette, 1991; Davey, Garside, Hilton, Mcewan, &
62 Morrison, 1995, 1996; Davey, Hilton, & Garside, 1997; Davey, Hilton, et al., 1996;

63 Dinsmore, Crocker, & Yodh, 1998; Espitalier, et al., 1997; Pileni, 1997). In foods, emulsion
64 crystallization was discovered accidentally as part of the butter churning process (Fredrick, et
65 al., 2011; Walstra & Vanberesteyn, 1975). In the case of margarine manufacture (Haighton,
66 1976) nucleation is initiated in the dispersed oil phase of an oil-in-water emulsion, the
67 emulsion is inverted under shear during the crystallization process so that crystallization
68 completes when the oil forms the continuous phase. The result is a kinetically stable water-in-
69 oil emulsion, which would otherwise be a kinetically stable oil-in-water emulsion. This has
70 the interesting property of inverting back to a water continuous emulsion when the crystal
71 network melts in the mouth. In ice cream, the role of crystallization in stabilizing and
72 structuring the product is even more complex (Goff, 1997a, 1997b). In foods, fat crystals
73 formed from a colloidal oil dispersion play an important role in structuring emulsions (Garti,
74 Aserin, Tiunova, & Binyamin, 1999; Garti, Binyamin, & Aserin, 1998; Walstra, Van Vliet,
75 and Kloek, 1995).

76

77 **2.2 Classical nucleation theory**

78 A number of authors have cast doubt on the applicability of classical nucleation theory
79 (CNT), for example (Sanz, Valeriani, Frenkel, & Dijkstra, 2007; Prestipino, Laio, & Tosatti,
80 2012; Kashchiev, 2008; Cabriolu, Kashchiev, & Auer, 2012). However, it has been our
81 experience that it explains very well nucleation in colloidal systems and recent work
82 (Lechner, Dellago, & Bolhuis, 2011, Kashchiev, Borissova, Hammond, & Roberts, 2010) has
83 placed classical nucleation theory (albeit in a modified form) on a firm theoretical footing in
84 both colloidal and bulk fluids. In particular, the underpinning idea that there is a critical
85 nucleus size at which crystal growth may begin and that size is determined through an energy

86 balance between surface (proportional to diameter squared) and volume terms (proportional
87 to diameter cubed) has been vindicated. This idea is not challenged by some critics of CNT
88 (Prestipino et al., 2012) and interestingly their modifications to the surface energy term
89 account for the relatively large thermal surface fluctuations which occur in nano-scale
90 particles (of which see Section 2.3 below).

91 **2.3 Nucleation in bulk fluids**

92 **2.3.1 Homogeneous Nucleation**

93 Detailed accounts of crystallization in bulk materials can be found in (Kashchiev, 2000;
94 Kashchiev, Borissova, Hammond, & Roberts, 2010; Kashchiev & van Rosmalen, 2003;
95 McClements, 2012).

96 We adopt a model (Ozilgen, Simoneau, German, Mccarthy, & Reid, 1993; Sear, 2007;
97 Volmer, 1939) whereby the initial stage of crystallization involves nucleation. In crystal
98 nucleation ordered domains are formed from the melt. In energy terms these domains possess
99 a reduced energy and entropy throughout their volume but an increased energy by virtue of
100 the creation of an interface between the ordered domain and the disordered liquid. Thus a
101 critical size is inherent in the energy balance which underlies their formation. Below this
102 critical size the surface energy expenditure required to create the domain boundary exceeds
103 the volume energy gain arising from condensation of the liquid into the ordered material
104 constituting the nucleus. The volume energy gain will relate to the undercooling or
105 supercooling relative to the bulk melting point of the ordered material. Hence the critical size
106 of the crystal nucleus will reduce as the undercooling increases. If only pure material exists
107 and extraneous surface and material is absent, then the formation of an ordered domain
108 capable of growth will be a purely stochastic process, involving the diffusion of the liquid

109 molecules, their encounter in a specific, lower entropy conformation and the critical size of
110 the nucleus. This is homogeneous nucleation.

111 According to (Fisher, Hollomon, & Turnbull, 1948) “Particles of a new phase that exceed the
112 critical size required for continuous growth are commonly called nuclei. Particles of
113 subcritical size will be called embryos in order to differentiate them from nuclei. Turnbull has
114 discussed the way in which the sizes of embryos change by statistical fluctuations. Nuclei do
115 not leap into existence with a single fluctuation; rather, they arise from embryos that change
116 their sizes continuously at finite rates by losing or gaining atoms one at a time from the
117 surrounding matrix. An important consequence of this idea is that the transient concentration
118 of embryos of every size can differ greatly from the equilibrium or steady state concentration
119 whenever insufficient time has been allowed for steady-state conditions to be realized.”

120 More recent versions of CNT allow more than one atom or molecule to join and leave the
121 nucleus at a time (e.g. Prestipino et al., 2012). The phase prior to nucleation where embryos
122 in an undercooled system come into existence and then disappear is related to the induction
123 period referred to above but is not considered further in this discussion.

124 Turnbull and co-workers (Fisher, Hollomon, & Turnbull, 1949; Turnbull, 1950a, 1950b,
125 1950c, 1952; Turnbull & Cormia, 1961; Turnbull & Fisher, 1949; Turnbull & Vonnegut,
126 1952) provide comprehensive details on the crystallization kinetics of liquid metals and
127 alkane liquids. Nucleation rates in emulsified fats can be determined by measuring the
128 volume fraction of solid fat (φ) as a function of time (t). The crystallization rate will be
129 proportional to the volume fraction of droplets that contain no crystals ($1-\varphi$) and therefore
130 decreases with time:

131
$$\frac{d\varphi}{dt} = k(1 - \varphi) \tag{1}$$

132 The reaction rate constant k can be expressed as a function of J , the nucleation rate. For
133 homogeneous volume nucleation, the rate constant k_v is proportional to the droplet volume v_d ,

$$134 \quad k_v = Jv_d \quad (2)$$

135 If homogeneous nucleation proceeds at the droplet surface, the rate constant k_s is proportional
136 to the droplet surface a_d ,

$$137 \quad k_s = Ja_d \quad (3)$$

138 Solving the differential Equation 1 gives

$$139 \quad \varphi = 1 - e^{-kt} \quad (4)$$

140 Taking into account the droplet size distribution, (4) has to be summed over all the droplet
141 sizes:

$$142 \quad \varphi = 1 - \int_0^\infty \varphi_d^0 e^{-kt} \delta d \quad (5)$$

143 where φ_d^0 is the differential volume fraction of droplets with sizes between d and $d + \delta d$.

144 Whether homogeneous volume nucleation or nucleation catalyzed by the homogeneous
145 droplet boundary, the isothermal crystallization rate can be modelled by one nucleation rate
146 independent of particle diameter if it is assumed that the droplet composition and the
147 composition of the droplet surface do not change.

148 The Gibbs energy change $\Delta G_{\text{nucleus}}$ for formation of a nucleus is the result of a balance
149 between a positive energy term ΔG_s due to surface tension and a negative volume term ΔG_v
150 due to enthalpy of fusion. The nucleus is assumed to be either a sphere in which case
151 nucleation is isotropic or a cube with a surface energy γ_i on the i^{th} face. The surface area of

152 each face is A_i . V is the volume of the nucleus and $\Delta G_{\bar{v}}$ is the change in Gibbs energy per
 153 unit volume arising from the phase transition.

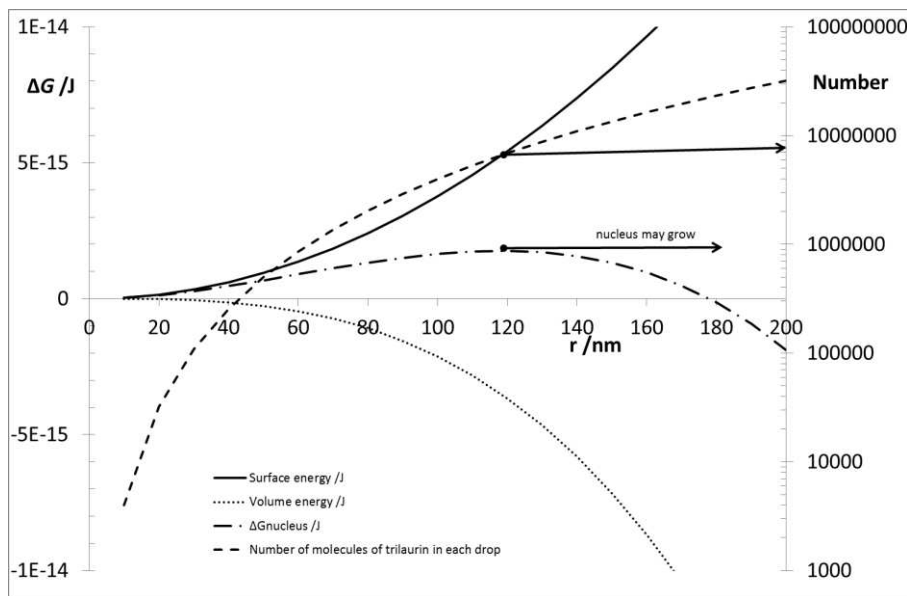
$$154 \quad \Delta G_{\text{nucleus}} = \Delta G_s + \Delta G_v = \sum_i A_i \gamma_i + V \Delta G_{\bar{v}} \quad (6)$$

155 For a spherical nucleus this becomes

$$156 \quad \Delta G_{\text{nucleus}} = 4\pi r^2 \gamma + \frac{4}{3}\pi r^3 \Delta G_{\bar{v}} \quad (7)$$

157 Surface energies for triacylglycerols in water have been measured by (Lucassenreynnders &
 158 Kuijpers, 1992) and in their Figure 4 values tend to 30 mN/m at zero surfactant concentration
 159 to around 1 mN/m for concentrations above 1% w/w of an unsaturated monoacylglycerol
 160 (Dimodan LS, Danisco), for the sunflower oil-water interface. Volume energies can be
 161 estimated from the latent heat of fusion (Charbonnet & Singleton, 1947) who quote around
 162 40 cal/gm (167 J/kg) for the alpha form of pure triacylglycerols. The calculations in Figure 1
 163 have been carried out for trilaurin using a value of 30 mN/m for the surface tension and 167
 164 J/kg for the enthalpy change on crystallization into the alpha form.

165



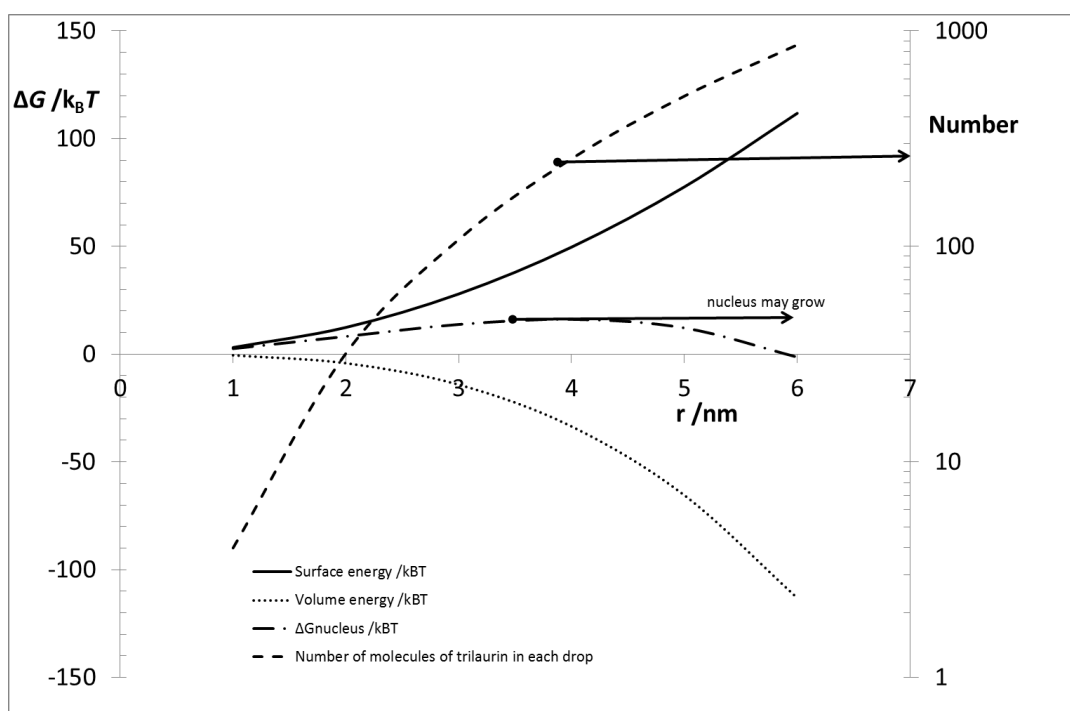
166

167 **Figure 1** Plot of surface and volume energy as a function of particle radius for a trilaurin droplet,
 168 together with the number of molecules per droplet and the energy of formation of the nucleus. The
 169 surface tension in this plot is 30 mN/m and the enthalpy change of the trilaurin into the alpha form is
 170 taken as 167 J/kg.

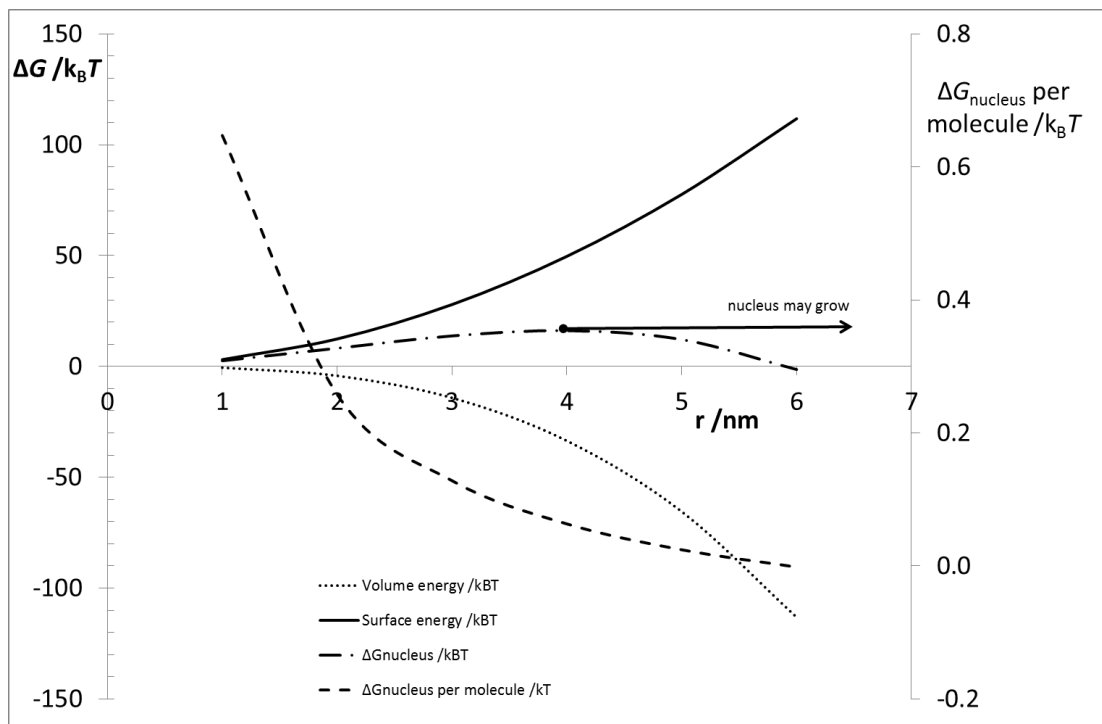
171 It may be noted from Figure 1 first of all that initially the surface term (increasing energy)
 172 grows more quickly than the volume term (decreasing energy) and that this forms an energy
 173 barrier to the formation of a stable nucleus. For trilaurin a nucleus needs to exceed around
 174 120-nm in order for it to grow and this corresponds to nearly 10 million molecules, a highly
 175 unlikely event.

176 However, if the surface energy may be reduced then the situation is transformed. For
 177 example, in anticipation of the colloid section (Section 2.4) of this discussion, if the surface
 178 energy term is greatly reduced to 1 mN/m which may be achieved through the addition of 1%
 179 w/w of an unsaturated mono-acylglycerol (Dimodan LS, Danisco), for a sunflower oil-water
 180 interface (Lucassenreynnders, et al., 1992); only a few hundred molecules are needed to
 181 achieve the point where growth is favourable (Figure 2). In this figure the energy is
 182 calculated in units of $k_B T$ and it can be seen that energies of only a few $k_B T$ are sufficient for

183 crystal nucleation which then becomes a much more likely event. This becomes even clearer
 184 in Figure 3 where the energy per molecule added to the nucleus is shown to have a value
 185 below $1 k_B T$ indicating that nucleation is highly probable. This suggests that, contrary to the
 186 views of some authors, for example (Sear, 2007), there are circumstances where
 187 homogeneous nucleation may become highly likely and this will be examined in the next
 188 section (Section 2.4).



189
 190 **Figure 2 Plot of surface and volume energy in units of $k_B T$ as a function of particle radius for a trilaurin**
 191 **droplet, together with the number of molecules per droplet and the energy of formation of the nucleus.**
 192 **The surface tension in this plot is 1 mN/m and the enthalpy change of the trilaurin into the alpha form is**
 193 **taken as 167 J/kg.**



194

195 **Figure 3 Plot of surface and volume energy in units of $k_B T$ as a function of particle radius for a trilaurin**
 196 **droplet, together with the estimated attachment energy per molecule in units of $k_B T$. The surface tension**
 197 **in this plot is 1 mN/m and the enthalpy change of the trilaurin into the alpha form is taken as 167 J/kg.**

198 Differentiation of Equation 7 with respect to r and equating to zero gives a critical size r^* for
 199 a cubic nucleus and for a sphere of:

200
$$r_{\text{cube}}^* = \frac{-4\bar{\gamma}}{\Delta G_{\bar{V}}};$$

201
$$r_{\text{sphere}}^* = \frac{-2\gamma}{\Delta G_{\bar{V}}};$$

202
$$\bar{\gamma} = (\gamma_{ab}\gamma_{ac}\gamma_{bc})^{1/3}$$

203 where ab , ac and bc refer to the different nucleus faces.

204 Here it is assumed that the cubic nucleus adopts an orthogonal co-ordinate system described
 205 by the axes a , b and c and $\bar{\gamma}$ is the corresponding average Gibbs surface energy.

206 The activation Gibbs energy for the formation of a spherical nucleus can be expressed as a
 207 function of supersaturation. Substitute r^* and $\Delta G = \Delta\mu/\bar{V}$ into Equation 7, where \bar{V} is the
 208 molar volume in a crystal lattice and $\Delta\mu$ the chemical potential difference between the
 209 supersaturated and the saturated solution or melt.

$$210 \quad \Delta G_{\text{nucleus}}^* = \frac{16\pi\bar{V}^* \gamma^3 N_0^2}{3\Delta\mu_i^2}$$

211 where

$$212 \quad \Delta\mu_{\text{solution}} = RT \ln(\beta)$$

$$213 \quad \Delta\mu_{\text{melt},i} = \Delta H_i \frac{T_{m,i} - T}{T_{m,i}}$$

214 Here β is the supersaturation ratio which is the ratio between the solubilities of the
 215 crystallizing component at saturated and unsaturated conditions; R is the gas constant; T the
 216 crystallization temperature; N, Avogadro's number; \bar{V}^* the molecular volume of a crystal;
 217 $T_{m,i}$ the melting temperature of polymorph i and ΔH_i , the enthalpy of fusion of polymorph i.

218 The nucleation rate for crystallization, J, is given by the following semi-phenomenological
 219 equation for the case of homogeneous nucleation. It is based on the product of the collision
 220 frequency in a system of N crystallizable molecules, together with a kinetic barrier factor that
 221 delays crystallization and the entropy loss associated with the formation of a nucleus:

$$222 \quad J = N \frac{k_B T}{h} \exp\left(\frac{-\alpha \Delta S_i}{R}\right) \exp\left(\frac{-\Delta G_{\text{nucleus}}^*}{k_B T}\right) \quad (8)$$

223 where $\exp(-\alpha \Delta S_i / R)$ is the probability that a fraction α of the molecule is in the right
224 conformation to crystallize and the loss of entropy ΔS on incorporation of material in a
225 nucleus is given by:

$$226 \quad \Delta S_i = \frac{\Delta H_i}{T_{m,i}}$$

227 Here k_B is Boltzman's constant; R is the gas constant; T the crystallization temperature in $^{\circ}\text{K}$;
228 $T_{m,i}$ the melting temperature of polymorph i . $\Delta G^*_{\text{nucleus}}$, activation Gibbs energy for the
229 formation of a spherical nucleus and ΔH_i , the enthalpy of fusion of polymorph i .

230 **2.3.2 Impact of thermal diffusion**

231 Thermal diffusion is often neglected when considering crystal nucleation and growth. It is
232 worth noting that very large enthalpy changes occur during the transformation from a liquid
233 oil to a solid (Charbonnet, et al., 1947; Wesdorp, 1990). This is a significant factor during
234 nucleation since the energy released during the transformation from solid to liquid heats the
235 surrounding liquid, reducing the supercooling and the probability of growth. The likelihood
236 that this will occur can be estimated from the thermal wave length ($2\pi\mu$ where μ =thermal
237 diffusion length, $\mu=\sqrt{2\alpha/\omega}$, α =thermal diffusivity, ω is radial frequency). If for the sake of
238 argument we require that a nucleus must persist in order to grow for at least 50 ns (R. P. Sear,
239 2007) ($\omega = 2\pi f = \frac{2\pi}{50 \times 10^{-9}} = 12.6 \times 10^6$) then the thermal diffusion length will be
240 approximately 300 nm (thermal diffusivity of water is $0.143 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$ at 25 C). It would
241 be reasonable to assume therefore that no other nucleus could begin to form within this
242 distance of an existing nucleation event.

243

244

TAG-name	ΔH_f kJ/mol			ΔS_f J/mol K		
	α	β'	β	α	β'	β
MMM	84	107	145	275	334	440
PPP	98	132	169	309	399	501
StStSt	113	156	193	343	464	561
n-C19	45	60	-	147	197	-
n-C21	48	63	-	153	203	-

245 **Table 1** Entropy and enthalpy of fusion for some triacylglycerols and n-alkanes (Wesdorp, 1990). MMM
 246 – trimyristin, PPP – tripalmitin; StStSt – tristearin.

247

TAG	Percentage %	$T_{m,\alpha}$ °C	$\Delta H_{f,\alpha}$ kJ mol ⁻¹	$T_{m,\beta'}$ °C	$\Delta H_{f,\beta'}$ kJ mol ⁻¹	$T_{m,\beta}$ °C	$\Delta H_{f,\beta}$ kJ mol ⁻¹
PPP	4.0	44.7	95.8	55.7	126.5	65.9	171.3
PStP	26.1	47.2	112.2	67.7	165.5	65.3	173.6
PStSt	39.0	50.1	106.0	61.8	-	64.4	172.9
StStSt	14.5	54.7	108.5	64.3	156.5	72.5	194.2
PPSt	6.0	46.4	100.0	58.7	124.0	62.6	166.3
StPSt	2.2	50.7	103.0	-	-	68.0	170.3

248

249 **Table 2** Melting temperature and enthalpies of fusion of pure triacylglycerols in polymorph i, together
 250 with the composition of fully hydrogenated palm oil (Wesdorp, 1990)

251

252 **2.3.3 Heterogeneous nucleation**

253 In the case of heterogeneous nucleation the process cannot be modelled by a single nucleation
 254 rate, as the number of impurities in each droplet will vary with diameter. Initially, the
 255 droplets containing the greatest number of catalytic impurities will crystallize. The maximum
 256 nucleation rate can probably be related to the nucleation of bulk fats. As solidification
 257 continues, smaller droplets will crystallize because they contain fewer impurities. At the end
 258 of the crystallization process, the volume fraction of solidified droplets will reach a plateau
 259 value φ_m because some droplets do not contain impurities and thus will not nucleate
 260 heterogeneously. If it is assumed that the catalytic impurities are distributed randomly, the
 261 maximal achievable volume fraction of solid droplets can be related to the number of
 262 impurities per volume by

$$263 \quad \varphi_m = 1 - e^{-v_d N_{imp}} \quad (9)$$

264 where N_{imp} is the number density of catalytic impurities (strongly dependent on temperature).

265 Combining Equations 1 and 9 with observations by Walstra and van Berestyn (Walstra, et al.,
 266 1975) the volume fraction of droplets containing crystals during heterogeneous nucleation as
 267 a function of time can be expressed as

$$268 \quad \varphi = \varphi_m \frac{J_0 v_d t}{1 + J_0 v_d t} \quad (10)$$

269 where J_0 is the maximum nucleation rate. Fitting crystallization curves of emulsified
 270 triglycerides to a heterogeneous nucleation model requires the fit parameters J_0 and N_{imp} ,
 271 while homogeneous nucleation requires only the nucleation rate as a fit parameter (Kloek,
 272 1998). To take particle size distributions into account, (Wu, Sirota, Sinha, Ocko, & Deutsch,

273 1993). Equation 10 has to be summed over all the droplet sizes as in (Turnbull, et al., 1961).
274 Similarly, when surface fits are to be expressed, v_d becomes a_d .

275 **2.3.4 Secondary nucleation**

276 Once the first nucleus has formed and a crystal has begun to grow, other types of nucleation
277 may come into play. Of course primary nucleation may occur independently in many
278 different places throughout the volume of liquid. However, the growing crystal may itself
279 nucleate new centres of crystal growth by a variety of processes (Herhold, Ertas, Levine, &
280 King, 1999; Walstra, 1998; Walstra, Van Vliet and Kloek, 1995; Walstra, et al., 1975). In the
281 case of emulsions for example, solid droplets can nucleate crystallization in liquid droplets
282 through collision (Dickinson, Kruizenga, Povey, & Vandermolen, 1993; Dickinson,
283 McClements 1995; McClements, 2012; McClements, Dickinson, et al., 1993; McClements,
284 Dickinson, & Povey, 1990; McClements & Dungan, 1993, 1997; McClements, Dungan,
285 German, & Kinsella, 1992, 1993a, 1993b; McClements, Dungan, German, Simoneau, &
286 Kinsella, 1993; McClements, Han, & Dungan, 1994; Ostwald, 1897).

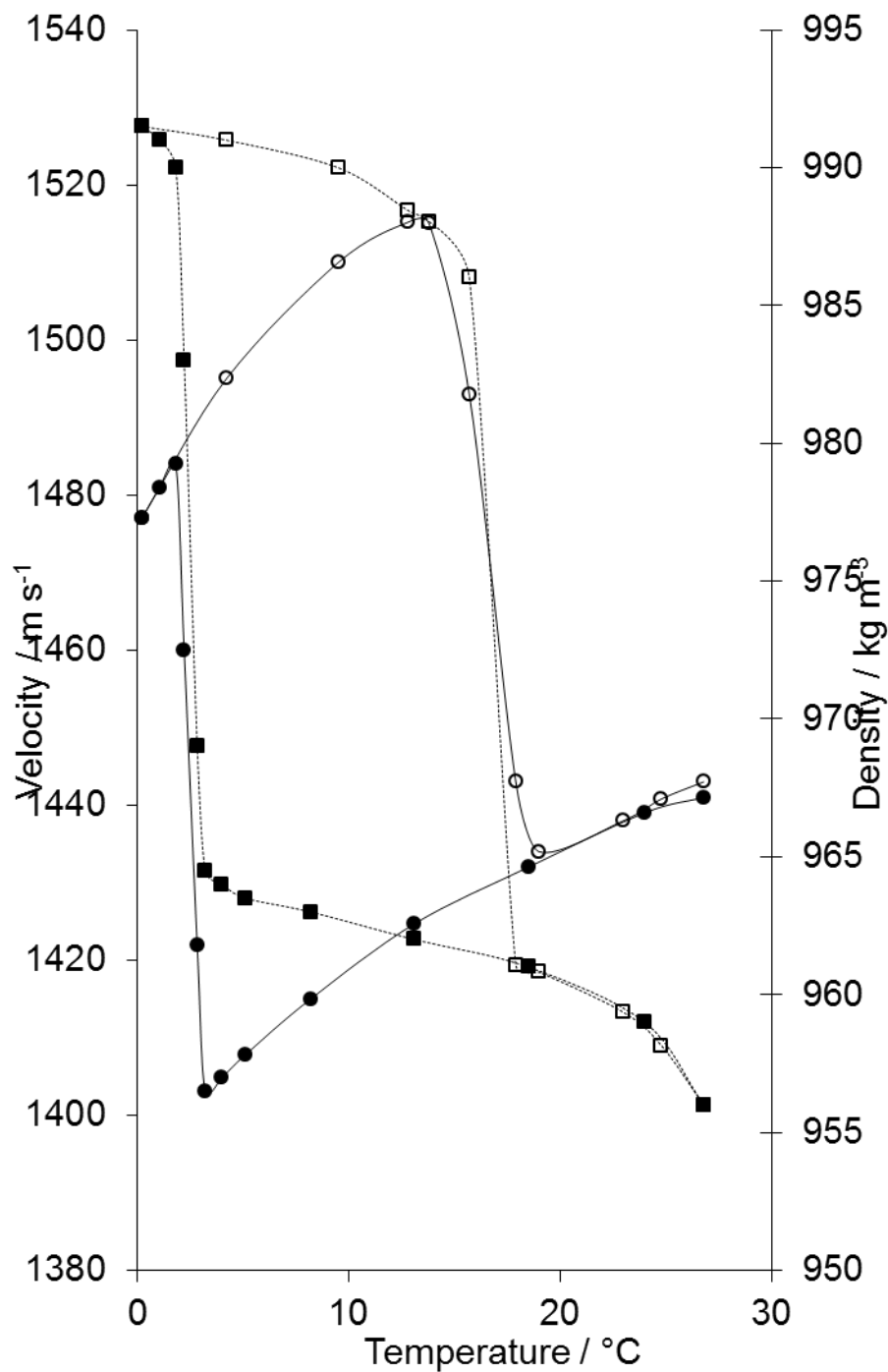
287

288 **2.4 Nucleation in dispersed fluids**

289 In this Section we will assume that once nucleation occurs within an emulsion droplet its
290 growth embracing the whole droplet is effectively instantaneous. This is a convenient
291 simplification that glosses over the details of the crystallization process, particularly within
292 larger droplets.

293 In bulk liquids guest molecules and foreign surface may catalyse crystal nucleation. This
294 process is called heterogeneous nucleation. Once such a liquid is subdivided into very many
295 particles, subdivision of the bulk liquid into a large number of smaller ones also partitions

296 those nuclei that may catalyse heterogeneous nucleation amongst the droplets (Gibout, Jamil,
297 Kousksou, Zéraouli, & Castaing-Lasvignottes, 2007). As a result the number of catalytic
298 impurities per droplet may vary, depending on particle size, between many per droplet to
299 approximately zero. This is generally observed as a greatly increased supercooling, also
300 called undercooling (Figure 4).



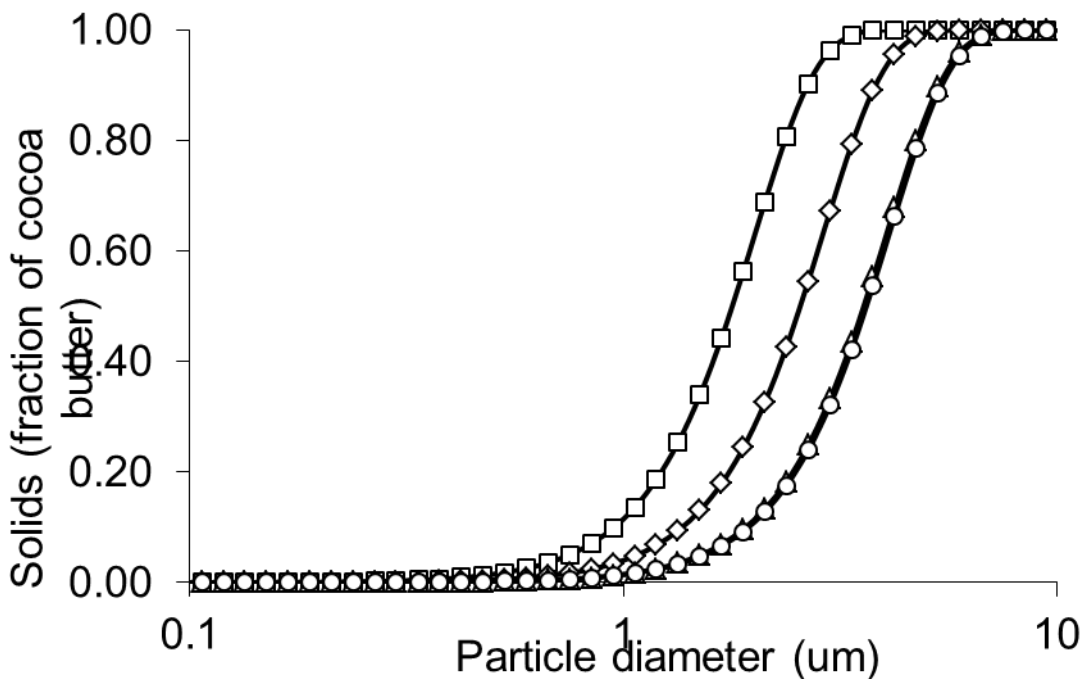
301

302 **Figure 4** Velocity of sound and density plotted against temperature for a 20 vol. % n-hexadecane oil-in-
 303 water emulsions containing 2 wt % Tween 20. Closed circles, velocity on cooling; open circles, velocity on
 304 heating; closed squares, density on cooling; open squares, density on heating. Average volume-surface
 305 diameter of 800 nm. taken from (E. Dickinson, et al., 1993)

306 In Figure 4 the bulk melting point of n-hexadecane is around 18.2 °C. However, the
307 emulsion droplets do not freeze until the temperature reaches 3.5 °C. When the emulsion is
308 heated it does not melt at its freezing temperature; instead it melts close to the melting point
309 of the bulk liquid. When the number of catalytic impurities is less than one per droplet, the
310 kinetics will initially be proportional to the volume of each drop and hence to the cube of
311 droplet diameter.

312 The dramatic impact on crystallization rate due to reduction in emulsion droplet size is
313 illustrated in Figure 5 where nucleation in droplets sized around 100-nm is almost completely
314 absent. This plot of solids fraction against particle diameter is based on the knowledge of the
315 number of crystal nuclei per unit volume in the sodium caseinate-stabilized Cocoa Butter
316 (CB) emulsions. Thus, below a certain droplet size the probability of one of these droplets
317 containing a catalytic impurity (i.e., CB seed crystal) able to initiate nucleation is negligibly
318 small. Figure 5 also illustrates the temperature sensitivity of CB seed crystals. For example,
319 at a 1- μm oil droplet size the calculated solids fraction at 15.5 and 15.8°C (based on the
320 number of catalytic impurities determined per unit volume, N_{imp} , values of $2.86 \times 10^{16} \text{ m}^{-3}$
321 and $2.74 \times 10^{16} \text{ m}^{-3}$, respectively) is around 0.02, whereas at 14.2°C ($N_{\text{imp}} = 2.33 \times 10^{17} \text{ m}^{-3}$)
322 this value approaches 0.14.

323 It can be concluded therefore that at 15.5 and 15.8°C very few active seed nuclei would likely
324 be found in emulsion droplets of less than 1 μm diameter. In the case of CB seed crystals, the
325 proportion of seed crystals is itself temperature dependent.

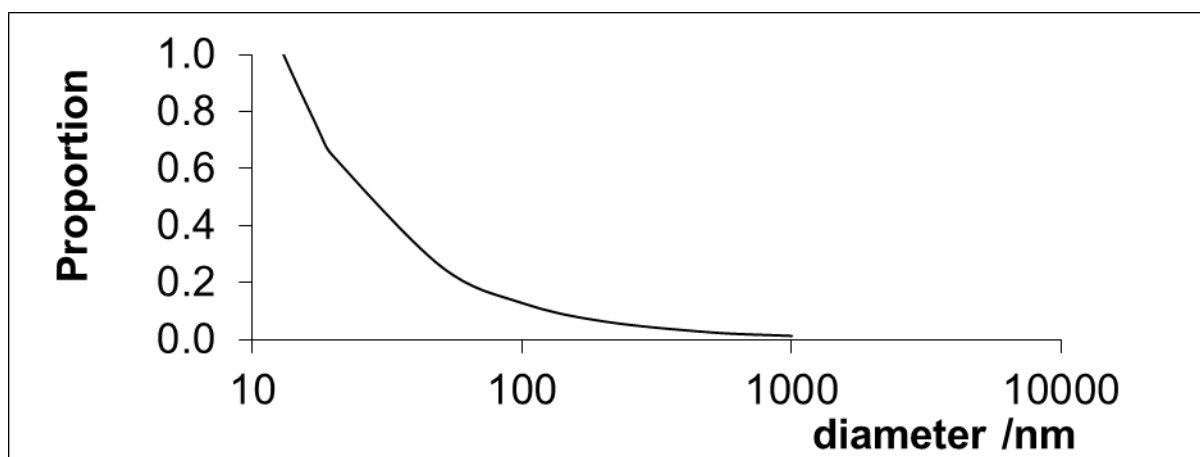


326

327 **Figure 5** Cocoa butter solids content plotted as a function of particle diameter crystallized at 14.2 °C
 328 (open squares), 15.0 °C (open diamonds), 15.5 °C (open triangles) and 15.8 °C (open circles). (S. Hindle, et
 329 al., 2000)

330 A big impact on crystal nucleation in emulsions arises as a result of the creation of an
 331 enormous interfacial surface area. In the example of Table 3, 1 litre of 20% v/v trilaurin oil-
 332 in-water emulsion contains 1.2 m² of surface area when the drops have a diameter of 1-mm
 333 and this increases to 1.2 x 10⁵ m² when the diameter falls to 10-nm. Under these
 334 circumstances nucleation at the interface between the crystallizable, dispersed material and
 335 the non-crystallizable continuous phase becomes more probable. For example surfactant
 336 molecules such as Tween 20 contain a hydrophobic tail of lauric acid. If the droplets
 337 comprise trilaurin, then the surfactant may catalyse crystal growth from the surface (Smith,
 338 Cebula, & Povey, 1994; Smith & Povey, 1997; Smith, 1995). Thus the probability of
 339 nucleation will be related to the surface interfacial area and hence to the square of droplet
 340 diameter. The impact of reducing surface energy has already been examined in Section 2.3

341 where it is shown that nucleation may become a certainty if the surface energy is lowered
342 sufficiently. In order to obtain a monolayer coverage of Tween 20 (estimated head-group size
343 of 1.3-nm, for a 1227 gm mol wt and a density of 1100 kg m⁻³ assuming the head group is
344 spherical and tightly packed in a monolayer at the surface of a spherical droplet) in a 20% v/v
345 trilaurin oil-in-water emulsion around 0.16% v/v Tween 20 is required for a 1- μ m emulsions,
346 1.6% for a 0.1- μ m emulsion and 16% for a 10-nm emulsion. Not only is the total volume of
347 potential nucleator material increasing as particle size decreases but the volume occupied by
348 the lauric acid moiety which forms the hydrophobic tail of Tween 20 within the trilaurin is
349 also increasing (Figure 6).



350

351 **Figure 6 Proportion of total volume of a trilaurin droplet occupied by a surface layer 6 –nm deep. This**
352 **choice of surface layer depth is based on the assumption that the lauric acid moiety of Tween 20 organises**
353 **a trilaurin layer one unit cell deep.**

354

355 In such cases (Kaneko, et al., 1999; Katsuragi, Kaneko, & Sato, 2001), we would expect the
356 likelihood of nucleation to increase as particle size decreases, contrary to what is observed for
357 the sodium caseinate stabilized CB emulsions (Figure 5).

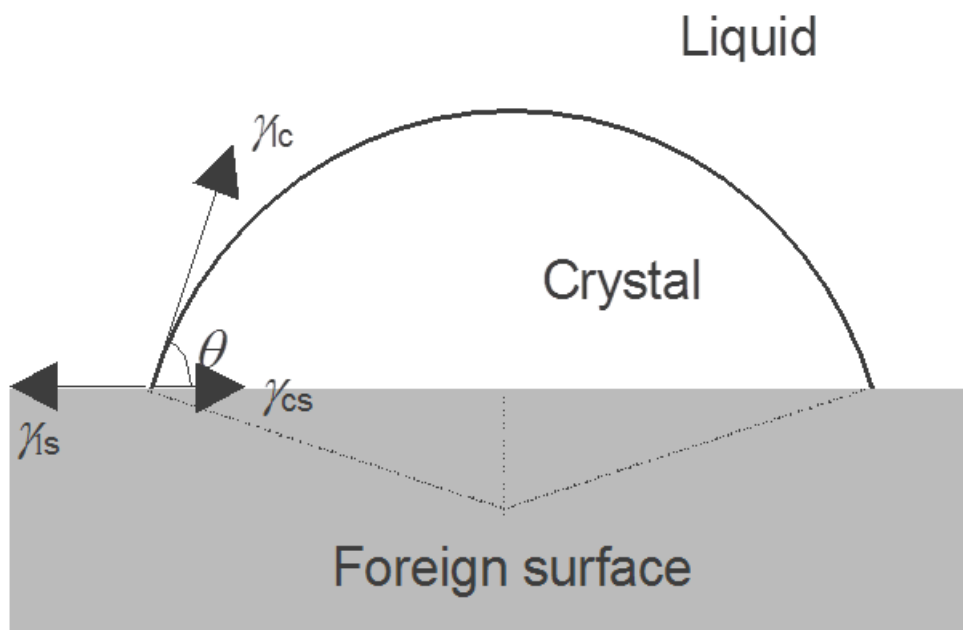
358 **Table 3 Particle volume, area and number together with estimates for single molecular layer**
 359 **coverage of emulsion particle with Tween 20, for 1 litre of 20 % v/v trilaurin oil-in-water emulsion. The**
 360 **choice of surface layer depth is based on the assumption that the lauric acid moiety of Tween 20 organises**
 361 **a trilaurin layer one unit cell deep.**

Particle diameter	Particle diameter	Particle diameter	Volume per particle	Volume per particle	Area per particle	Area per particle	Total surface area	Total surface area	Number of particles	Number of molecules of trilaurin per droplet	Volume of Tween 20 for monolayer coverage	Volume fraction of Tween 20 for monolayer coverage
	m	µm	m ³	µm ³	m ²	µm ²	m ²	µm ²			m ³	
1mm	0.001	1000	5.24E-10	5.24E+08	3.14E-06	3.14E+06	1.2	1.20E+12	3.82E+05	4.44E+17	1.56E-09	0.0002%
100 µm	0.0001	100	5.24E-13	5.24E+05	3.14E-08	3.14E+04	12	1.20E+13	3.82E+08	4.44E+14	1.56E-08	0.0016%
10 µm	0.00001	10	5.24E-16	5.24E+02	3.14E-10	3.14E+02	120	1.20E+14	3.82E+11	4.44E+11	1.56E-07	0.0156%
1 µm	1E-06	1	5.24E-19	5.24E-01	3.14E-12	3.14E+00	1200	1.20E+15	3.82E+14	4.44E+08	1.56E-06	0.1560%
100 nm	1E-07	0.1	5.24E-22	5.24E-04	3.14E-14	3.14E-02	12000	1.20E+16	3.82E+17	4.44E+05	1.56E-05	1.5600%
10 nm	1E-08	0.01	5.24E-25	5.24E-07	3.14E-16	3.14E-04	120000	1.20E+17	3.82E+20	4.44E+02	1.56E-04	15.6000%

362
 363 Another consequence of the dissolution of the methylene chain into the oil is that the melting
 364 point of any solid phase formed is depressed since the surface layer is actually a solution of
 365 the methylene chains in the oil (Povey, Hindle, Aarflot, & Hoiland, 2006).

366 Droplets with sizes smaller than a few µm in water undergo Brownian diffusion. As a result,
 367 collisions between droplets that have crystallized with ones that have not may catalyse
 368 crystallization (Hindle, Povey, & Smith, 2000). Alternatively the growth of needle crystals
 369 out of a droplet and the collision of this crystalline material with other droplets and
 370 subsequent nucleation may lead to a process called partial coalescence in which the
 371 crystallized droplets are connected together through needle crystals reaching through the
 372 aqueous phase (Boode, Bisperink, & Walstra, 1991; Boode & Walstra, 1993a, 1993b; Boode,
 373 Walstra, & Degrootmostert, 1993; Brooker, Krog, Dickinson, & Boode, 1993; Hindle, et al.,
 374 2000). This is a secondary nucleation process since it cannot occur until primary nucleation,
 375 either homogeneous or heterogeneous, has occurred somewhere in the system. This type of
 376 crystal growth through an emulsion will be critically dependent on the surface energy of the
 377 triple contact (Figure 7). For example, if θ is small the oil phase (liquid in Figure 7) will

378 spread into the water and feed the growth of the crystal; on the other hand if $\theta \gg 90^\circ$, the
 379 liquid oil will not spread into the water at the water/crystal interface and crystal growth will
 380 be confined to the oil phase. The contact angle will be affected by surfactant which will
 381 therefore influence the crystal morphology in the emulsion.



382
 383 **Figure 7** In the case of an emulsion the foreign surface will be water, the crystal will be
 384 the solid lipid and the liquid the oil from which the fat is crystallizing. γ_{ls} is the interfacial tension between
 385 the liquid and the foreign surface, γ_{cs} the interfacial tension between the crystal and the foreign surface and
 386 γ_{lc} the interfacial tension between the liquid and the crystal. This produces Young's relation $\cos\theta = \frac{\gamma_{ls} - \gamma_{cs}}{\gamma_{lc}}$.

387 Many workers have discussed the complex issues that arise with regard to crystal wetting in
 388 emulsions (Bergenshtahl & Alander, 1997; Boode, et al., 1991; Boode & Walstra, 1993b;
 389 Boode, Walstra, et al., 1993; Johansson & Bergenshtahl, 1995a, 1995b; Johansson,
 390 Bergenshtahl, & Lundgren, 1995; Ogden & Rosenthal, 1994, 1997, 1998). It is worth
 391 remarking that the surface energy concept itself may fail when the entities involved (nuclei,
 392 surfactant molecules and micelles and oil molecules) are all of comparable sizes in a system
 393 which may be kinetically stable but is not in thermodynamic equilibrium.

394 Surfactant causes a level of solubilisation of the dispersed liquid phase in the continuous
395 phase, enabling transport of the otherwise insoluble liquid between droplets. In the presence
396 of a wide range of particle sizes, a driving force exists which causes the large particles to
397 grow at the expense of the smaller ones. This is called Ostwald ripening (Ostwald, 1897) and
398 may have an impact on crystallization. For example, it can increase the likelihood of
399 coalescence between two droplets, once crystallized and the other not, if they have very
400 different sizes. This same transport mechanism may permit mixing of different oils between
401 droplets of the same size but different composition (Dickinson, Goller, McClements, &
402 Povey, 1991). This may impact on crystallization by alteration of the composition of each
403 droplet. It has also been suggested that guest molecules and other catalytic impurities may be
404 transported between droplets (Herhold, Ertas, Levine, & King, 1999).

405 The adsorbed layer at the oil-water interface may itself undergo crystallization (Fillery-
406 Travis, 1995; Hianik, 1999) and finally, heat transfer processes between the crystallizing
407 dispersed phase and the continuous phase may greatly alter the polymorphic form and crystal
408 habit (Bedecarrats, Strub, Falcon, & Dumas, 1996; Dumas, Krichi, Strub, & Zeraouli, 1994;
409 Dumas, Strub, & Broto, 1990; Dumas, Strub, & Krichi, 1990; Dumas, Zeraouli, & Strub,
410 1994; Dumas, Zeraouli, Strub, & Krichi, 1993, 1994; Gibout, et al., 2007); see also Section
411 2.3.

412 Room temperature thermal fluctuations generate surface displacements (Wang, Kim, Mir, &
413 Popescu, 2013) of up to 50-nm with frequencies between 1 Hz and 1kHz and these surface
414 fluctuations may have a big influence on nucleation in emulsion droplets with diameters
415 below 100-nm (See Figure 1, Figure 2 and Figure 3).

416 Emulsions form a very convenient framework within which to study crystallization itself. The
417 earliest example of this is the work of Vonnegut (Vonnegut, 1948). Turnbull and co-workers

418 formed dispersions of molten metal particles in order to study crystallization in bulk metals
419 (Turnbull, 1950a) and employed normal alkane oils as relatively simple model systems
420 (Turnbull, et al., 1961). As indicated above, by subdividing a bulk fluid into smaller and
421 smaller particles, it is possible to control the probability that a nucleus will be found in a
422 given particle of fluid. A careful study of nucleation kinetics in emulsions can tell us a great
423 deal about the nature of the crystal nucleation. For example, it is possible to distinguish
424 between homogeneous and heterogeneous nucleation and between nucleation at the droplet
425 surface and nucleation which is volume dependent. In the case of heterogeneous nucleation it
426 is possible to determine the nature of the nucleus, its Gibbs free energy for nucleation, the
427 concentration of nuclei and even to get some idea of the size of nuclei and this will be
428 illustrated in the next section.

429 ***2.5 Characterizing nucleation by the oil-in-water emulsion*** 430 ***crystallization method***

431 **2.5.1 Surface and volume nucleation**

432 Nucleation rates in emulsified fats can be determined by measuring the volume fraction of
433 solid fat (ϕ) as a function of time (t). Solid contents in the work quoted in this paper have all
434 been determined by the speed of sound method. (Povey, 1997) and also see (Dickinson,
435 Goller, McClements, Peasgood and Povey, 1990; Dickinson, McClements and Povey, 1991;
436 Dickinson et al., 1991; Coupland, Dickinson, McClements, Povey and de Mimmerand, 1993;
437 Dickinson et al., 1993; Dickinson et al. 1996; Hindle et al., 2000; Hindle et al., 2002;
438 McClements et al., 1990; McClements et al., 1991; McClements, Povey and Dickinson, 1993;
439 Povey, 2001; Povey, Hindle and Smith, 2001; Povey et al., 2006; Povey et al., 2007; Povey
440 et al., 2009). A crystal nucleation event at the droplet surface will have the same effect as an

441 event in the bulk because following the onset of nucleation complete crystallization of
442 colloidal particles is effectively instantaneous; hence, the crystallization rate is determined by
443 the nucleation rate (Turnbull, 1952; Turnbull, et al., 1961; Turnbull, et al., 1949).

444 In the case of homogeneous nucleation, in the bulk volume or at the droplet boundary, the
445 isothermal crystallization rate is determined by only one fit parameter, i.e., J, the nucleation
446 rate. Taking into account droplet size distribution, the volume fraction of solid fat is

$$447 \quad \varphi = 1 - \int_0^{\infty} \varphi_d^0 e^{-kt} \delta d \quad (11)$$

448

449 where k is the reaction rate constant and φ_d^0 is the differential volume fraction of droplets
450 with sizes between d and d + δd . k is expressed as a function of J such that

$$451 \quad k = Jv_d$$

452 v_d being the droplet volume or

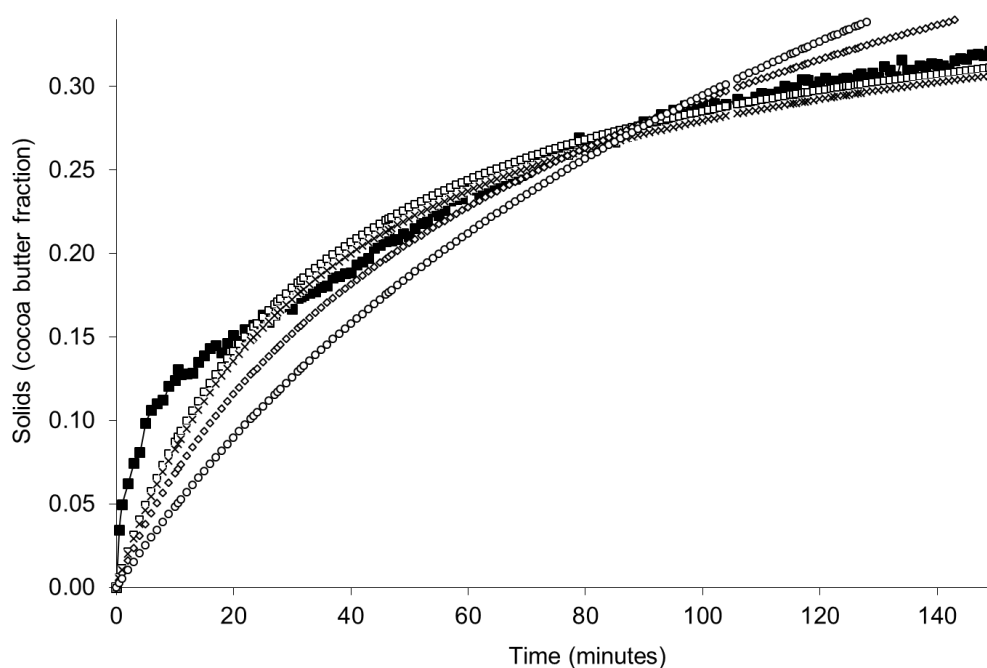
$$453 \quad k = Ja_d$$

454 a_d being the droplet area.

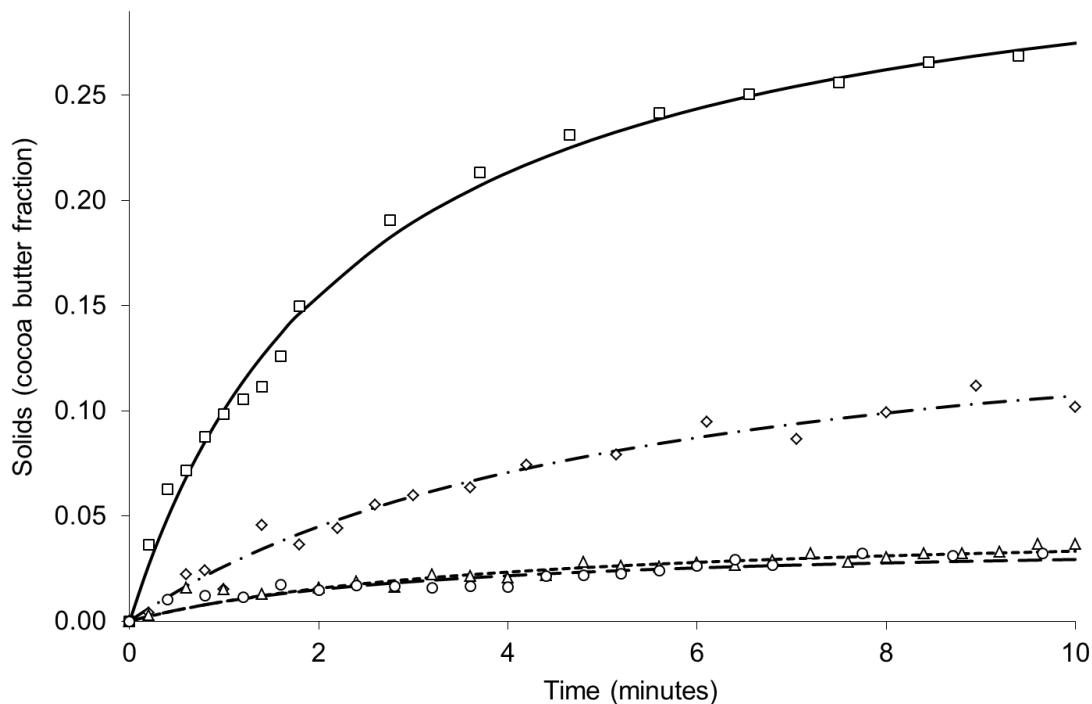
455 Finally, the surface Gibbs free energy of the nucleating surface can be determined by taking
456 the gradient of a plot of $\ln J_0$ against $1/T\Delta T^2$, and ΔT^2 is the difference between the
457 crystallization temperature and the melting temperature of the α polymorph of the nucleating
458 surface.

459 In Figure 8 an attempt is made to fit volume and surface homogeneous and heterogeneous
460 nucleation models to the measured solid content in a cocoa butter emulsion without success,
461 even when the droplet size distribution is accounted for properly (Hindle, Povey, & Smith,
462 2002). In circumstances like this it might be concluded that a nucleation rate does not exist

463 and empirical modelling is required. (Sear, 2012; Sear, 2013). However, what the data of
 464 Figure 8 shows is that nucleation has occurred rapidly in a proportion of droplets and then in
 465 the remaining uncrystallised droplets a proportion of collisions with crystallized droplets
 466 induces nucleation. In Figure 9, heterogeneous volume particle size distribution models fit the
 467 experimental data well, indicating that a proportion of droplets contain catalytic impurities, in
 468 this case cocoa butter seed crystals.



469
 470 **Figure 8 Plot of solids against time for a 20.75% vol/vol West African cocoa butter (WACB) oil- in-water**
 471 **emulsion (1.00 wt% sodium caseinate) crystallized isothermally at 15.0°C (■ experimental data). The**
 472 **following nucleation models are fitted based on particle size distribution; □ volume heterogeneous, ×**
 473 **surface heterogeneous, ◇ volume homogeneous and Δ surface homogeneous. (Hindle, et al., 2002)**



474

475 **Figure 9 Plot of solids against time for 20.75% vol/vol WACB oil-in-water emulsions (1.00 wt% sodium**
 476 **caseinate) crystallized at □ 14.2, ◇ 15.0, Δ 15.5, and ○ 15.8°C. Heterogeneous volume particle size**
 477 **distribution nucleation models are fitted to experimental data (shown as solid lines) (Hindle, et al., 2002).**
 478 **For abbreviations see Figure 8.**

479 In inter-droplet heterogeneous nucleation, it is assumed that a collision occurs between a
 480 single liquid and a single solid droplet, and, as a reactive pair, that crystallization occurs
 481 spontaneously. It is also assumed that both the newly formed and the original solid droplet
 482 have equal reactivity. Thus, the change in the fraction of liquid oil ($1 - \varphi$) remaining after
 483 time t is given by:

484
$$\frac{d(1-\varphi)}{dt} = -k_{ls}\varphi(1 - \varphi) \tag{12}$$

485 where φ is the volume fraction of solidified oil and k_{ls} is the second-order rate constant
 486 giving degree of reactivity. Integration of Equation 12 gives:

$$487 \quad \ln\left(\frac{1-\varphi}{\varphi}\right) = \ln\left(\frac{1-\varphi_0}{\varphi_0}\right) - k_{ls}t \quad (13)$$

488 where φ_0 is the initial volume fraction of solidified droplets. The rate constant, k_{ls} , can be
 489 calculated from the slope of a plot of $\ln[(1 - \varphi)/\varphi]$ against time (Dalglish & Leaver, 1991;
 490 Dickinson, et al., 1993; McClements, Dickinson, et al., 1993; McClements, et al., 1990) and
 491 is dependent upon the collision frequency of the droplets and the effectiveness of the
 492 collisions that (von Smoluchowski, 1917) promote secondary heterogeneous nucleation

$$493 \quad n_c = \frac{8k_B T n_0^2}{3\eta} \quad (14)$$

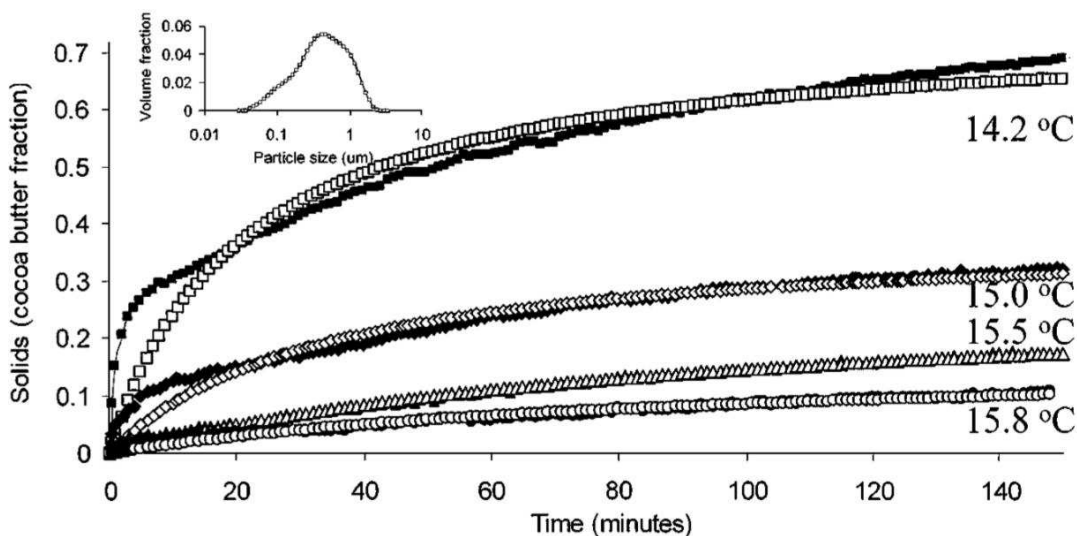
494 Where n_c is the number of collisions per second, n_0 is the total number of droplets per unit
 495 volume of emulsion and η is the viscosity of the continuous phase. The fraction of collisions
 496 that produce nucleation is then

$$497 \quad \frac{1}{W} = \frac{k_{ls}}{n_c/n_0} \quad (15)$$

498 And the potential barrier E to inter-droplet nucleation is

$$499 \quad E = k_B T \ln W \quad (16)$$

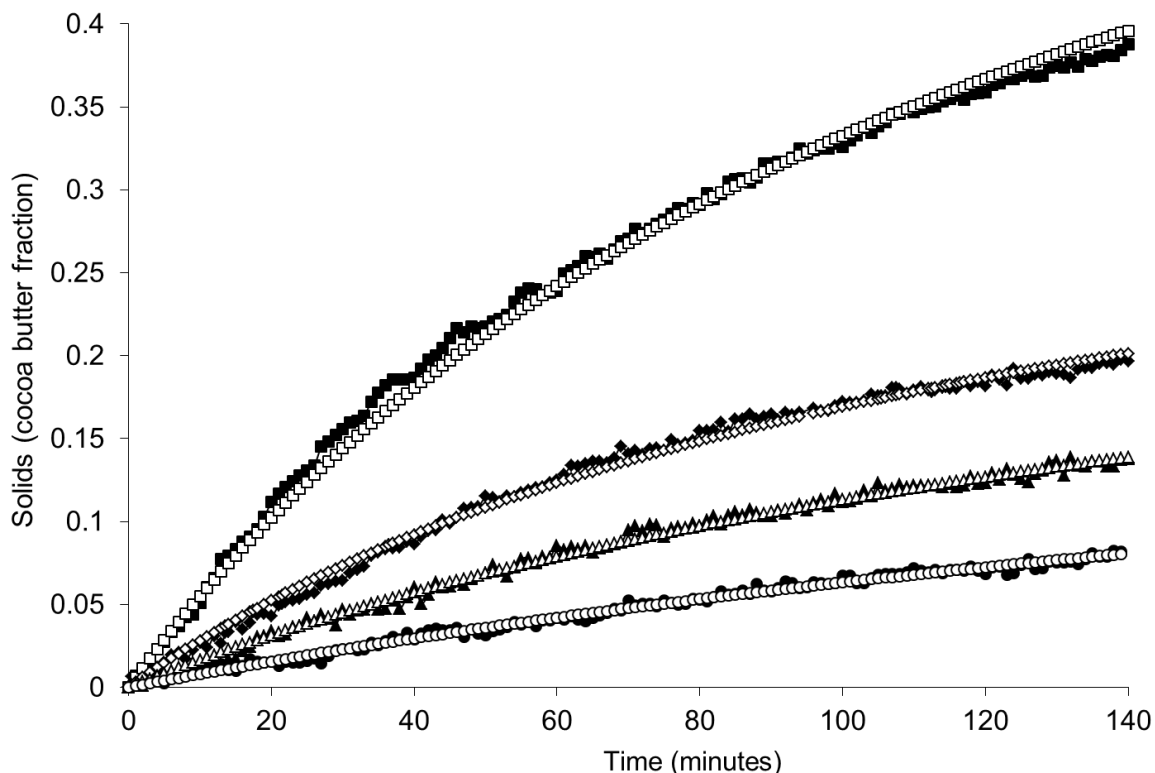
500 The data presented in Figure 8 can be analysed in terms of an initial heterogeneous nucleation
 501 event in a minority of droplets (Figure 9) followed by collision induced nucleation using
 502 Equations 12, 13 and 14 (Figure 10).



503

504 **Figure 10** Plot of solids against time for 20.75% v/v WACB oil-in-water emulsions (0.8% v/v Tween 20)
 505 crystallized isothermally at \circ , 14.2°C; Δ , 15.0°C; \diamond , 15.5°C; and \square , 15.8°C. Closed symbols are
 506 experimental data and open symbols are heterogeneous volume particle size distribution models fitted
 507 over the time period 0–150 min. Insert: Corresponding particle size distribution (Hindle, Povey, &
 508 Smith, 2000)

509 Given the ability to measure nucleation rate in a minority of droplets it is possible to study in
 510 detail the catalytic impurities responsible for nucleation and this can be done simply by
 511 reducing the size of the droplets until the probability that a catalytic impurity will be found in
 512 the droplet is vanishingly small. This has been done for cocoa butter seed crystals (Hindle, et
 513 al., 2002) and in many instances in fats the properties of the catalytic impurities are
 514 temperature dependent (Kloek, 1998). Alternatively, if every drop contains a catalytic
 515 impurity then a heterogeneous model can be fitted to the data

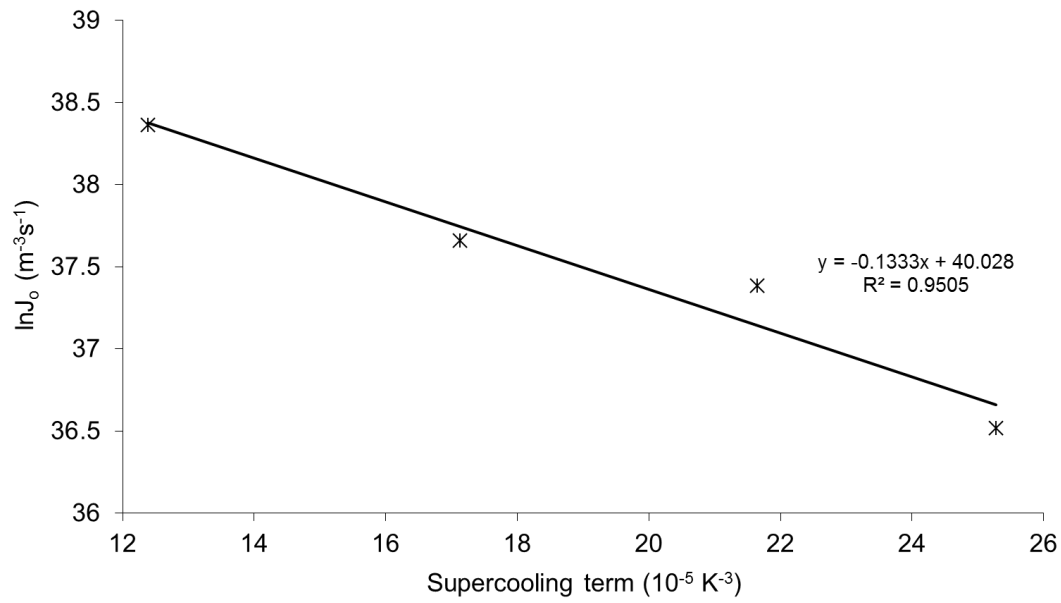


516

517 **Figure 11. Plot of solids against time in which the first 10 minutes of the data in Figure 10 is ignored A**
 518 **heterogeneous nucleation model now fits the data very well. (20.75% v/v WACB oil-in-water emulsions**
 519 **(0.8% v/v Tween 20) crystallized isothermally at ○, 14.2°C; △, 15.0°C;◇ , 15.5°C; and□, 15.8°C. Closed**
 520 **symbols are experimental data.) (S Hindle, et al., 2000)**

521 Solid content data such as that shown in Figure 11 can be plotted on a log-log plot using
 522 Equation 13 (Figure 12) from which the surface Gibbs free energy of the nucleating surface.

523 A plot of $1/T\Delta^2T$, a supercooling term, yields a straight line with whose gradient is the sur-
 524 face Gibbs energy and the intercept a pre-exponential term (Zettlemoyer, 1969). This is
 525 exemplified in Figure 13 where the rate constant for nucleation is determined for a range of
 526 oil/surfactant combinations. Data such as this has been used to assemble the data presented in
 527 Table 4 (Discussed in the next section).

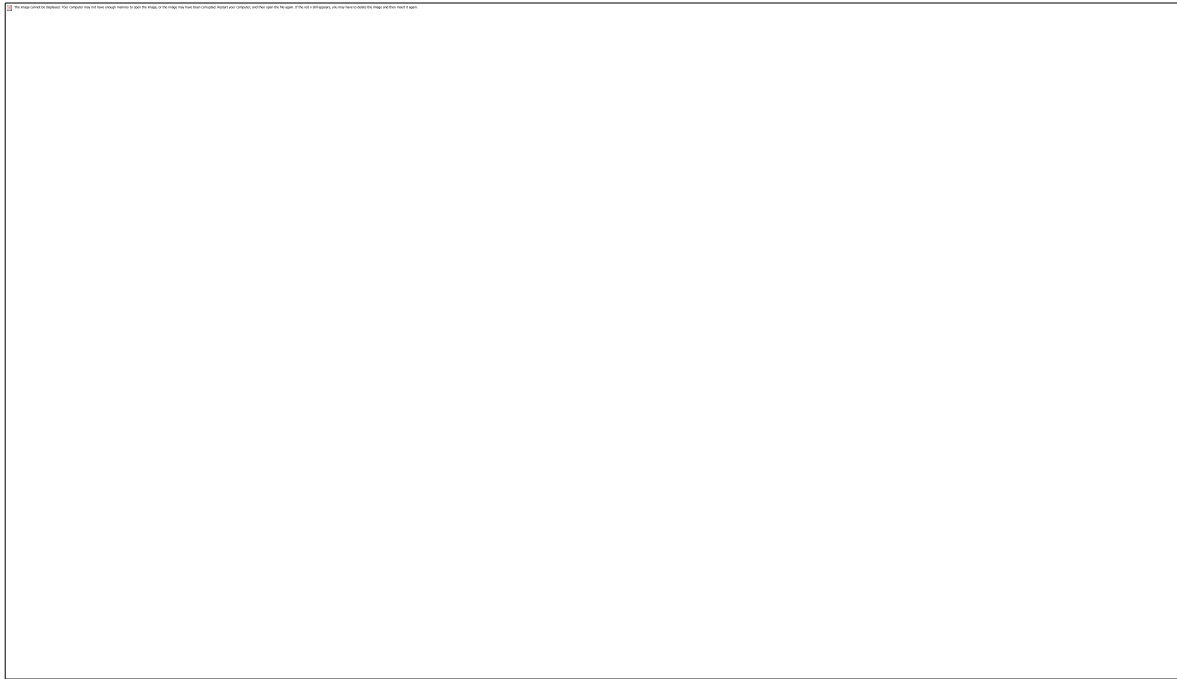


528

529 **Figure 12 Data in Figure 11 plotted against the undercooling term $\frac{1}{T\Delta^2 T}$**

530

531

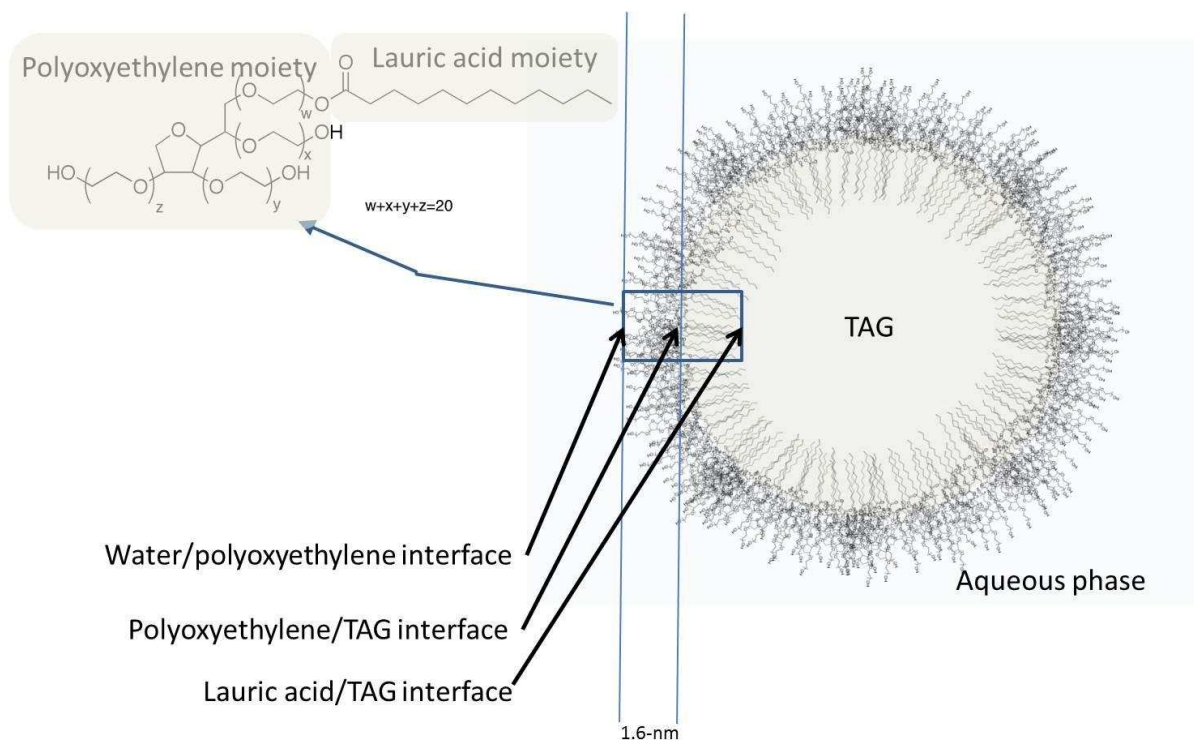


532

533 **Figure 13 Analysis of a range of solid content vs time data using Equation 13 for a range of crystallizing**
534 **oils and surfactants. The rate constant k_{1s} is shown on the Figure for each combination of oil and**
535 **surfactant (Povey, Awad, Huo, & Ding, 2009)**

536

537 **2.5.2 Role of surfactant**



538

539 **Figure 14 Drawing of a triacylglycerol (TAG) liquid droplet with Tween 20 (polyoxyethylene 20**
 540 **monolaurate) adsorbed at the oil/water interface.**

541 The presence of surfactant may have a number of important consequences for crystallization.
 542 As the droplet gets smaller the role of the surface becomes more important and the
 543 complexity of the surface will dominate nucleation. Examination of Figure 14 indicates that
 544 the surfactant introduces two new interfaces into the droplet, separating the oil phase to a
 545 great extent from the aqueous phase. Thermal fluctuations will give rise to large surface
 546 displacements (Wang, et al., 2013). The surfactant itself may crystallize (Fillery-Travis,
 547 1995; Hianik, 1999) for example. It is shown above that changes in surface energy may have
 548 a profound impact on nucleation (Figure 1, Figure 2, Figure 3) and modification of interfacial
 549 energy is discussed in Sections 2.3 and 2.4 above. The hydrophobic moiety may itself
 550 catalyse nucleation through chain length matching (Povey, 2001). The melting point of the

551 interfacial layer will be depressed through the formation of a solid solution of the
552 hydrophobic moiety and the oil.

553 **Table 4 List of the kinetic barrier properties of emulsions containing different surfactants, in units of**
 554 **$k_B T$, $E/k_B T$, and the probability that a collision event will lead to nucleation (w^{-1}) for a variety of oils,**
 555 **surfactants and particle sizes. The kinetic data were obtained through measurement of collision mediated**
 556 **nucleation. Crystallisation temperature is defined as the temperature at which the solids fraction is noted**
 557 **to rise above zero, at a given cooling rate. Undercooling is the difference between the bulk melting point**
 558 **and the crystallisation temperature. The cooling rate is 1 °C/min in all experiments apart from the cocoa**
 559 **butter, in which case the experiments were carried out isothermally, and the 123-nm Caflon-stabilised**
 560 **emulsion, which was cycled first at 1 °C/min then at 12 °C/min. The cocoa butter data (WACB) is also**
 561 **shown in Figure 13 and the longer time data represents collision mediated nucleation whilst the short**
 562 **time data is a result of seed crystal nucleation.**

563 § - data unavailable because nucleation was too fast.

564 ± Data from a microemulsion.

565 † These data are consistent with dissolution of the surfactant (PGE) in the bulk of the oil.

566 \$ The nucleation in this sample occurred too quickly to measure.

Oil in dispersed phase	Surfactant	Particle size d_p [nm]	Crystallisation temperature T_c [°C]	Reference	Rate constant for transformation from liquid to solid [$l^{-1} s^{-1}$]	Collisions per second per droplet $\frac{d_p^3}{6} \frac{v}{w}$ [s^{-1}]	The fraction of collisions leading to nucleation $\frac{1}{w} = \frac{k_n}{k_d} \frac{v}{w}$	Energy barrier to nucleation $E = k_B T \ln(w)$ [eV]	
m-hexadecane	Tween 20	2440	1.5/16.7	Povey et al, 2009	§				
		800	2.5/14.7	Povey et al, 2009	§				
		360		McClements et al, 1993	2.22	12	0.18	15.20	
		370		Dickinson et al, 1993	1.70	7	0.23	15.21	
		370		Dickinson et al, 1993	3.10	7	0.45	14.61	
		370		Dickinson et al, 1993	5.20	7	0.76	14.09	
		360		Dickinson et al, 1993	7.40	7	0.99	13.82	
		370		Dickinson et al, 1993	8.10	7	1.18	13.65	
		370		Dickinson et al, 1993	9.20	7	1.34	13.52	
		160	2.9/14.3	Povey et al, 2009					
	130	3.1/14.1	Povey et al, 2009	3.00	252	3.30	12.60		
	Tween 20 + 0.3 wt. % xanthan	370		Dickinson et al, 1996	1.80	1	2.32	12.97	
	Tween 20	130		Povey et al, 2009	3.00	252	3.28	12.63	
	Sodium dodecyl sulfate (SDS)	360		McClements et al, 1994	1.30	12	0.11	16.04	
	beta-lactoglobulin	360		McClements et al, 1993	0.66	12	0.05	16.72	
	beta-casein	400		McClements et al, 1996	0.18	9	0.02	17.70	
	PGO	PGE	130		Povey et al, 2009	300.00	63	1312.90	6.64
417			3/14.2	Povey et al, 2009	4.00	8	144.44	8.84	
330			2.8/14.4	Povey et al, 2009					
139			1/16.2	Povey et al, 2009					
123				Povey et al, 2009	40.00	75	148.27	8.82	
123			Povey et al, 2009	900.00	74	3336.08	5.70		
50		9.6/18.6	Povey et al, 2009						
Caflon ph060		148		Povey et al, 2009	300.00	44	1937.23	6.23	
m-undecane		Tween 20	3450	13/16.3	Guilstein and Coupland, 2007				
			420	12.5/17	Guilstein and Coupland, 2007				
	130		12/17.5	Guilstein and Coupland, 2007					
	Sodium caseinate	3450	14/15.3	Guilstein and Coupland, 2007					
	420	13.5/16	Guilstein and Coupland, 2007						
Cocoa butter	Tween 20	2400	14/13.3	Hindie et al, 2002					
		160		Hindie et al, 1999	100.00	34	843.63	7.08	
	Sodium caseinate	2400	14.2/18	Hindie et al, 2002					
	423		Hindie et al, 2002	0.40	8	15.08	11.10		
423		Hindie et al, 2002	30.00	8	1130.74	6.78			

567

568 As colloid sizes reduce whilst keeping the dispersed phase volume constant a point is reached
569 at which nucleation rates begin to rise again, having fallen from the bulk value due to
570 emulsification and the reduction in the numbers of catalytic impurities per droplet. This rise
571 is due (a) to increased surfactant and lower surface tension; (b) rapidly increasing inter-
572 droplet collision rates; (c) van der Waals attraction between small droplets and larger
573 surfaces, encouraging aggregation and an increased likelihood of inter-droplet nucleation.
574 The details of these processes have still to be demonstrated experimentally. Nevertheless, a
575 great deal of quantitative information regarding surfactants and the kinetic barriers that they
576 present can be elicited (Table 4). A number of interesting features of the data may be
577 highlighted. Firstly in the case of the different nucleation rates for West African Cocoa Butter
578 (WACB – Figure 13 and Table 4), at short times (seconds) the rate is controlled by the
579 presence of seed crystals in a minority of the droplets and at later times (hours) by collision
580 mediated nucleation between those dropolyplets that do not contain seed crystals and those
581 that do and crystallised quickly. Secondly, Povey et al, 2009 suggest that the polyglycol ester
582 L-7D (PGE) actually dissolves into the n-hexadecane oil phase, causing extensive surface
583 melting during the heating phase arising from melting point depression in the mixture of oil
584 and surfactant. Finally, the crystallisation temperature of the micro-emulsion is much higher
585 than that of the emulsions and correspondingly, the undercooling is much lower. This
586 suggests that nucleation is occurring at a higher rate in the micro-emulsion.

587 **3 Conclusion**

588 Crystal nucleation in food colloids is a complex subject, however here it is shown that
589 classical nucleation theory provides a sound theoretical basis with which to understand the
590 important phenomena. Emulsion crystallization and the measurement of solid content

591 provides a methodology whereby very many characteristics of crystal nucleation may be
592 quantified – surface Gibbs energy for nucleation, determination of the nature of the
593 nucleation (volume or surface homogeneous or volume or surface heterogeneous, interdroplet
594 collision, partial coalescence, energy barrier to coalescence (Table 4) and combinations
595 thereof). As colloidal particles get smaller many new physical phenomena appear which have
596 an impact on nucleation, these phenomena are only partially understood and a great deal of
597 careful and detailed scientific work will be needed to realise the full potential of emulsion
598 crystallization in food colloids.

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601 **5 References**

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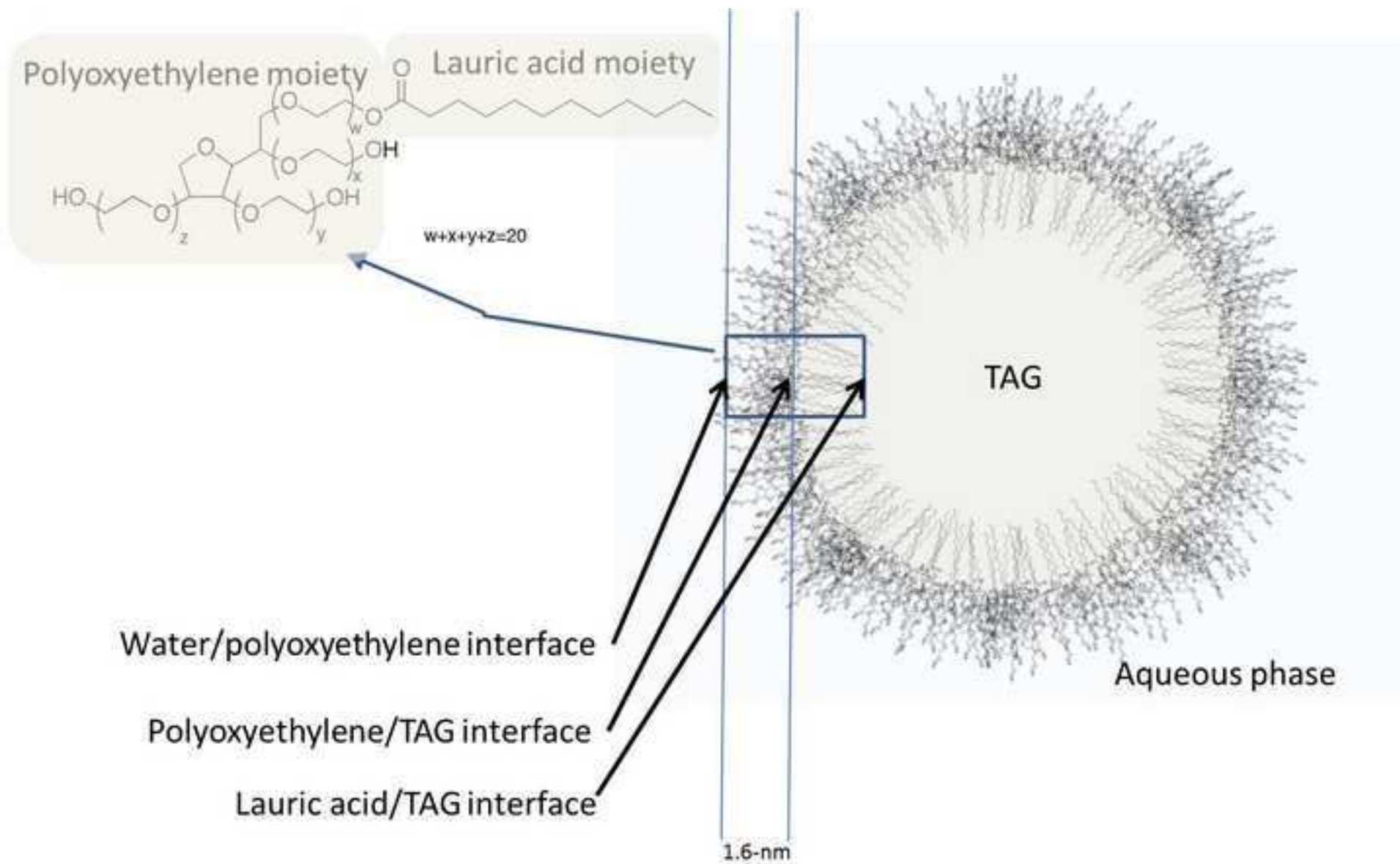
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Research highlights

- Speed of sound measurement is very sensitive to crystal nucleation.
- Isothermal nucleation rates are measured in a range of oil-in-water emulsions.
- Classical nucleation theory explains well all the measured data.
- Lowering interfacial energies may dramatically raise surface nucleation rates.

Figure 1
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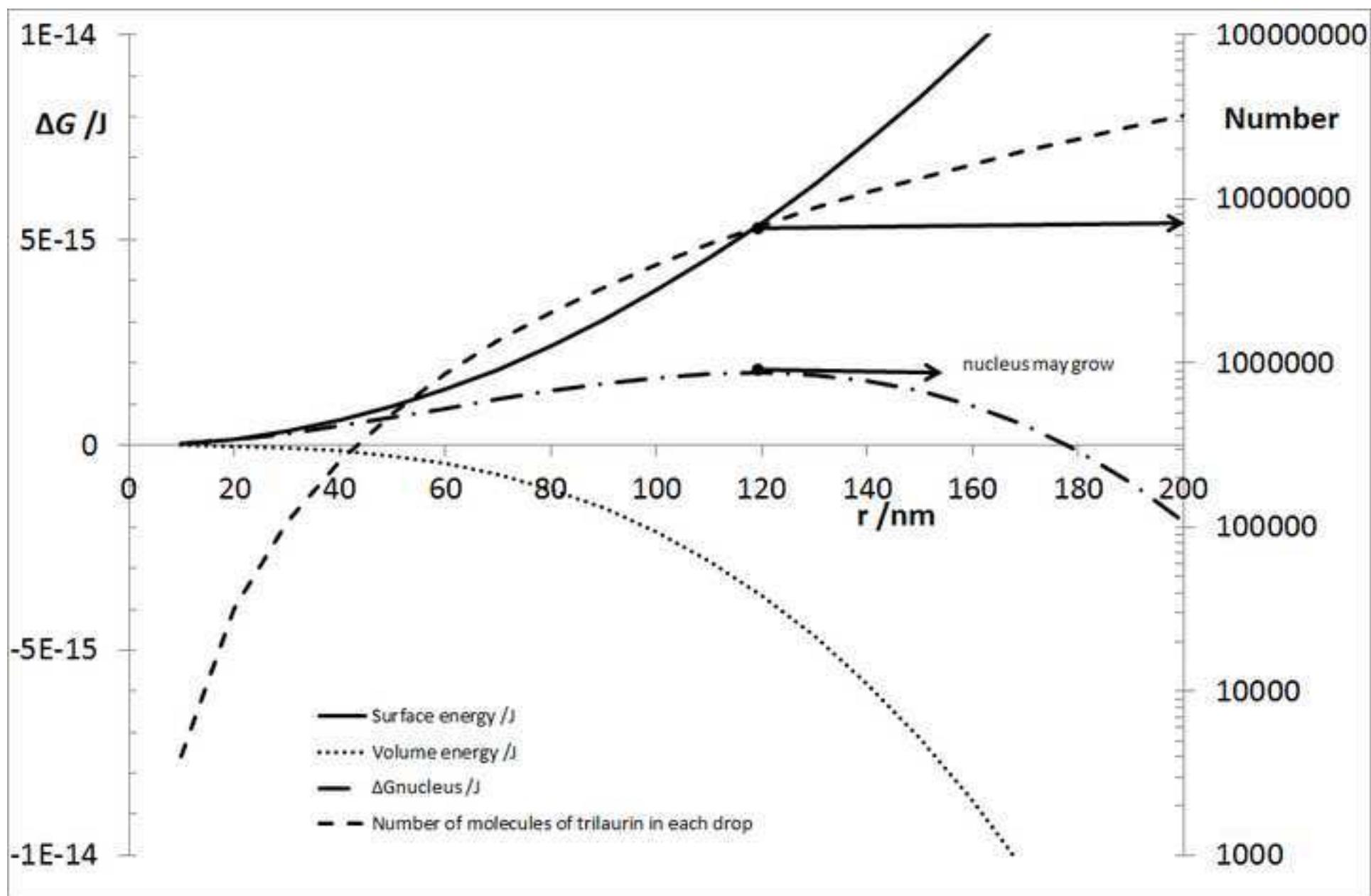


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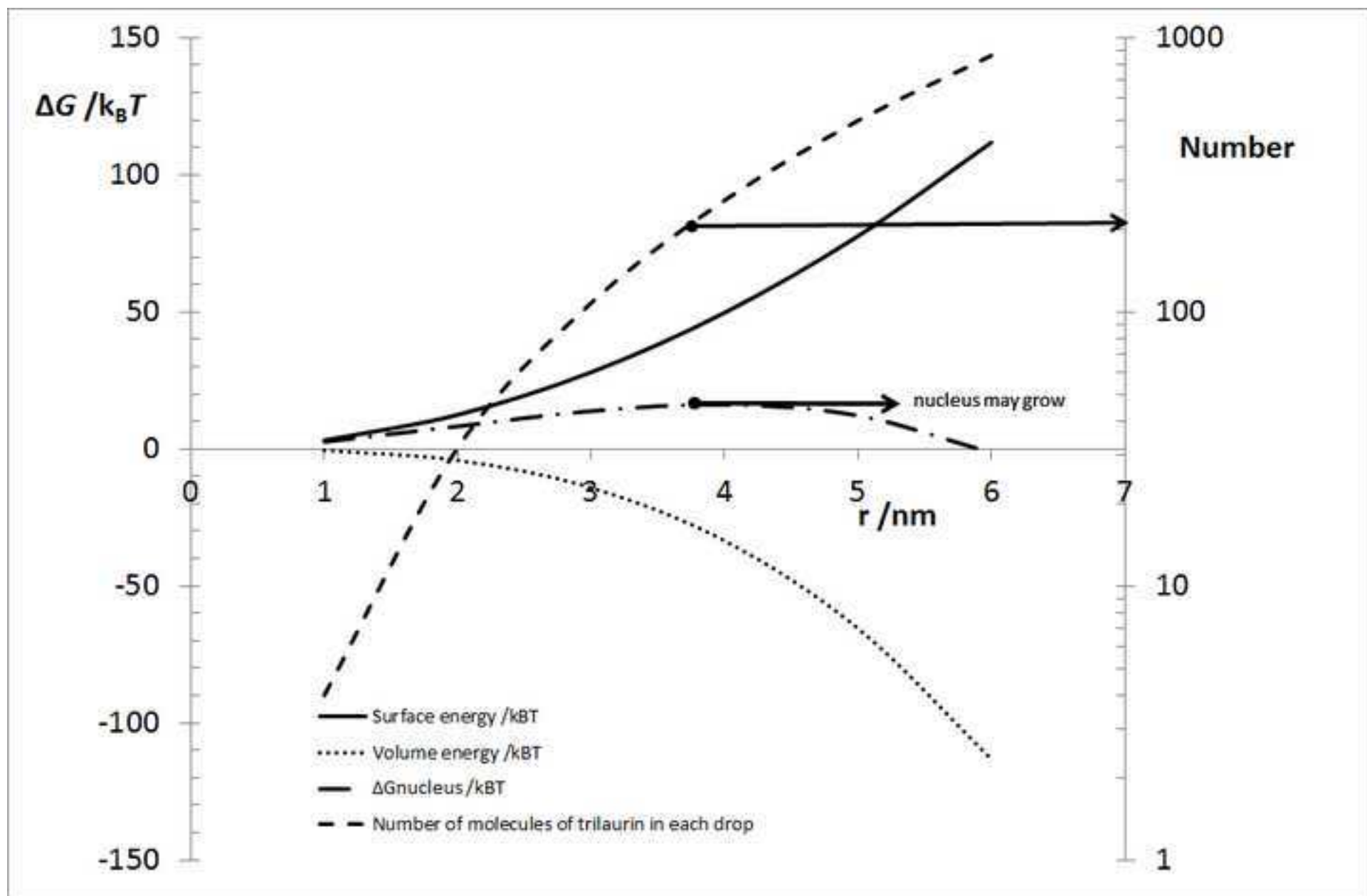


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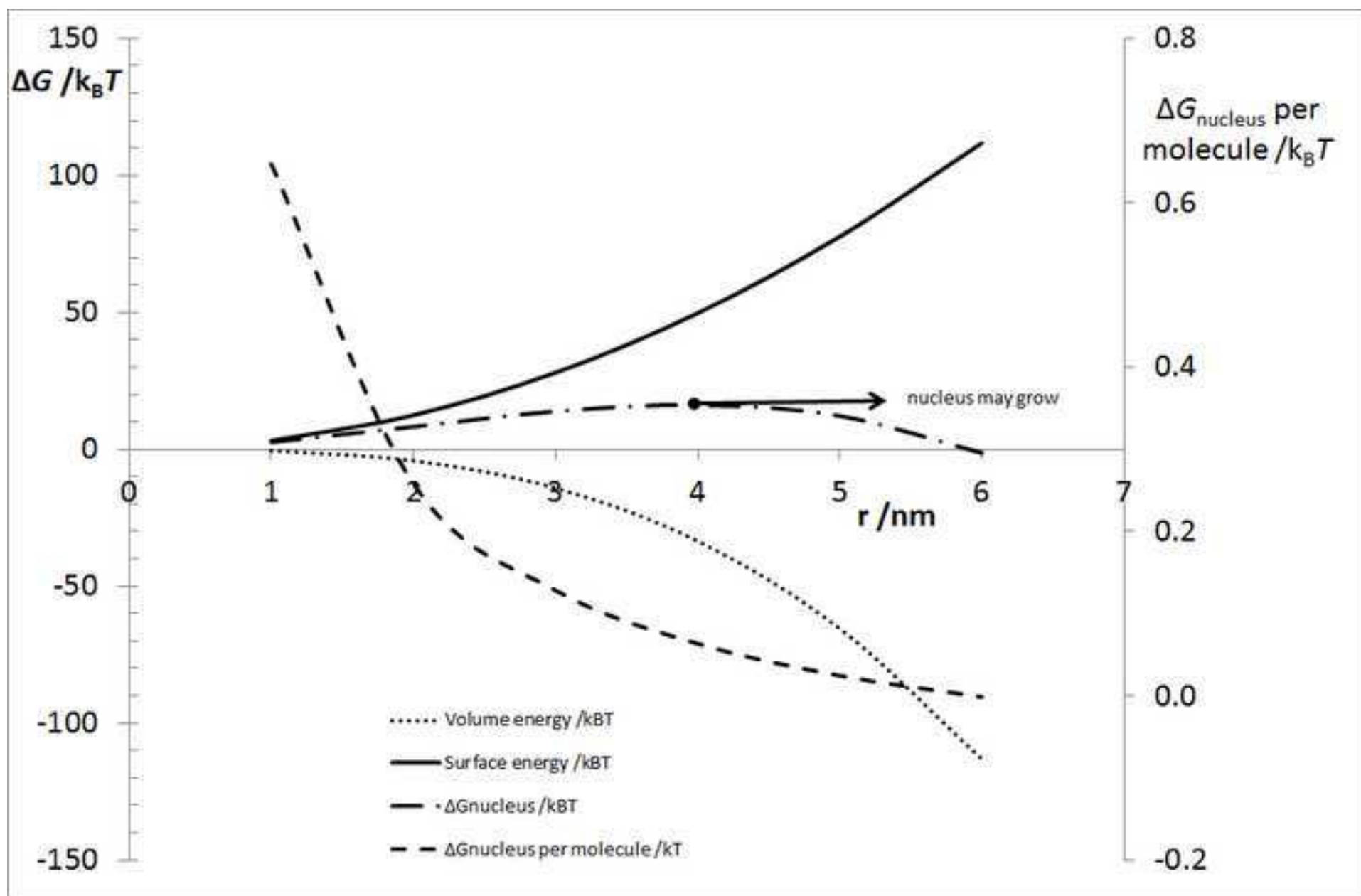


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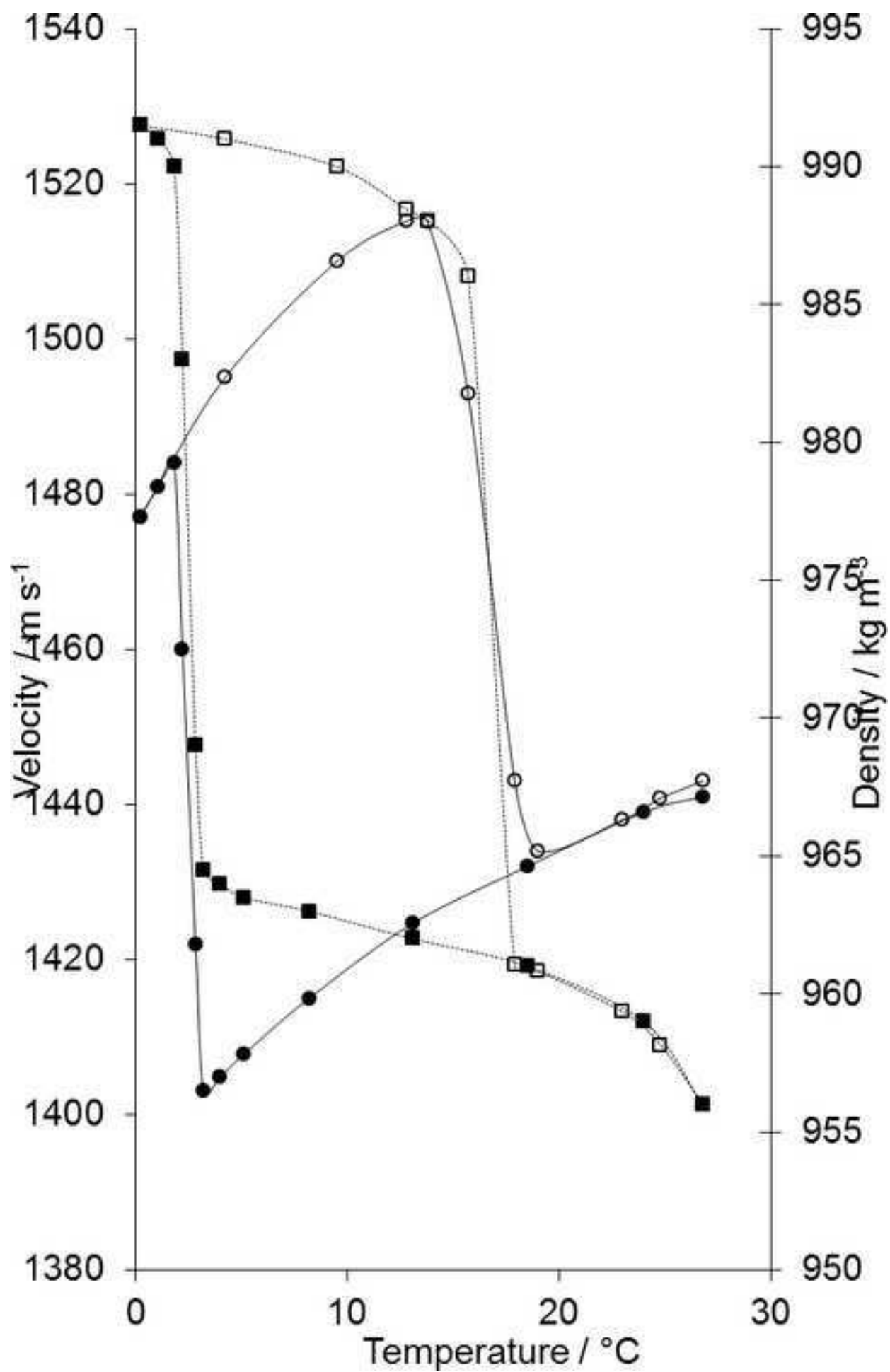


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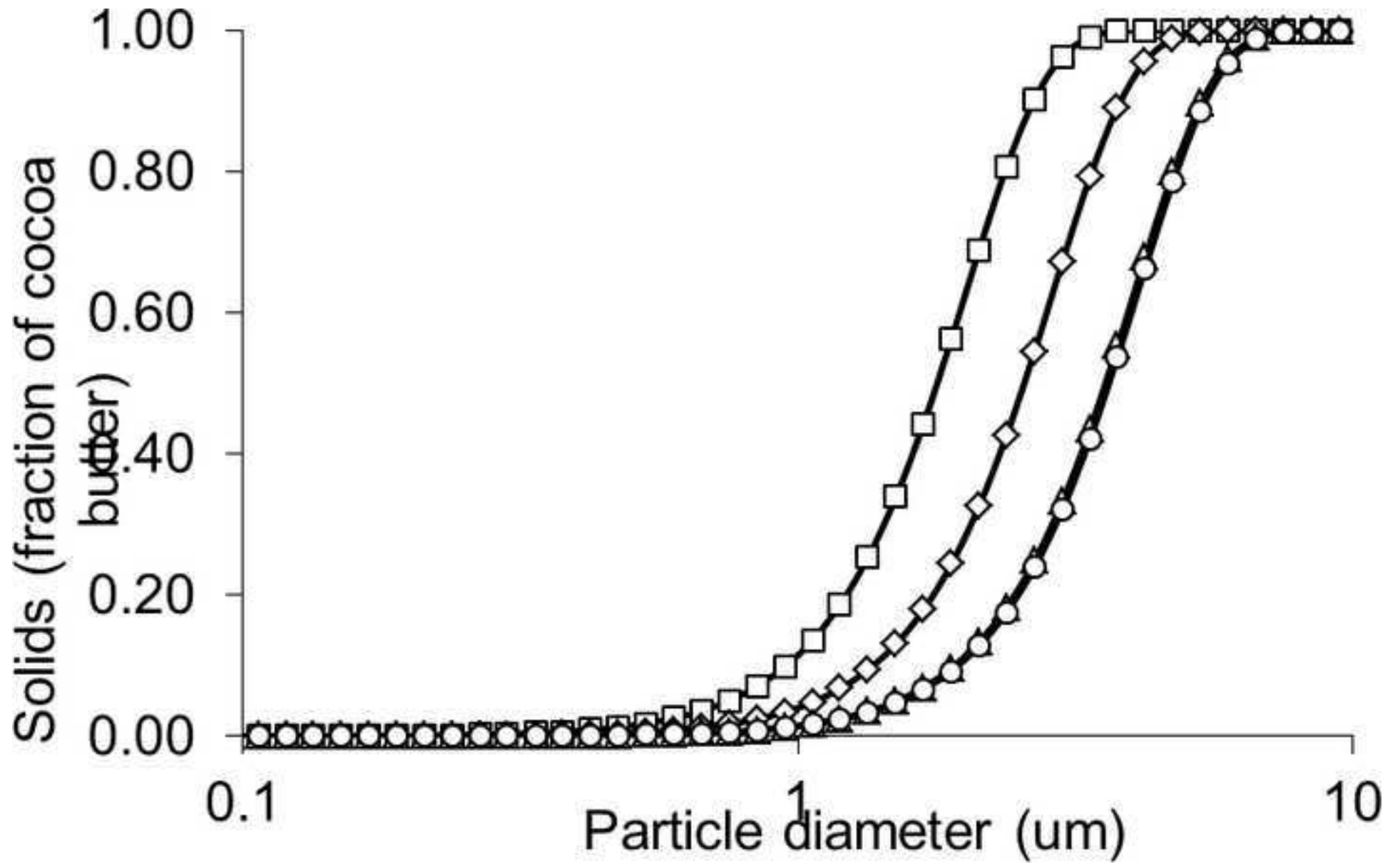


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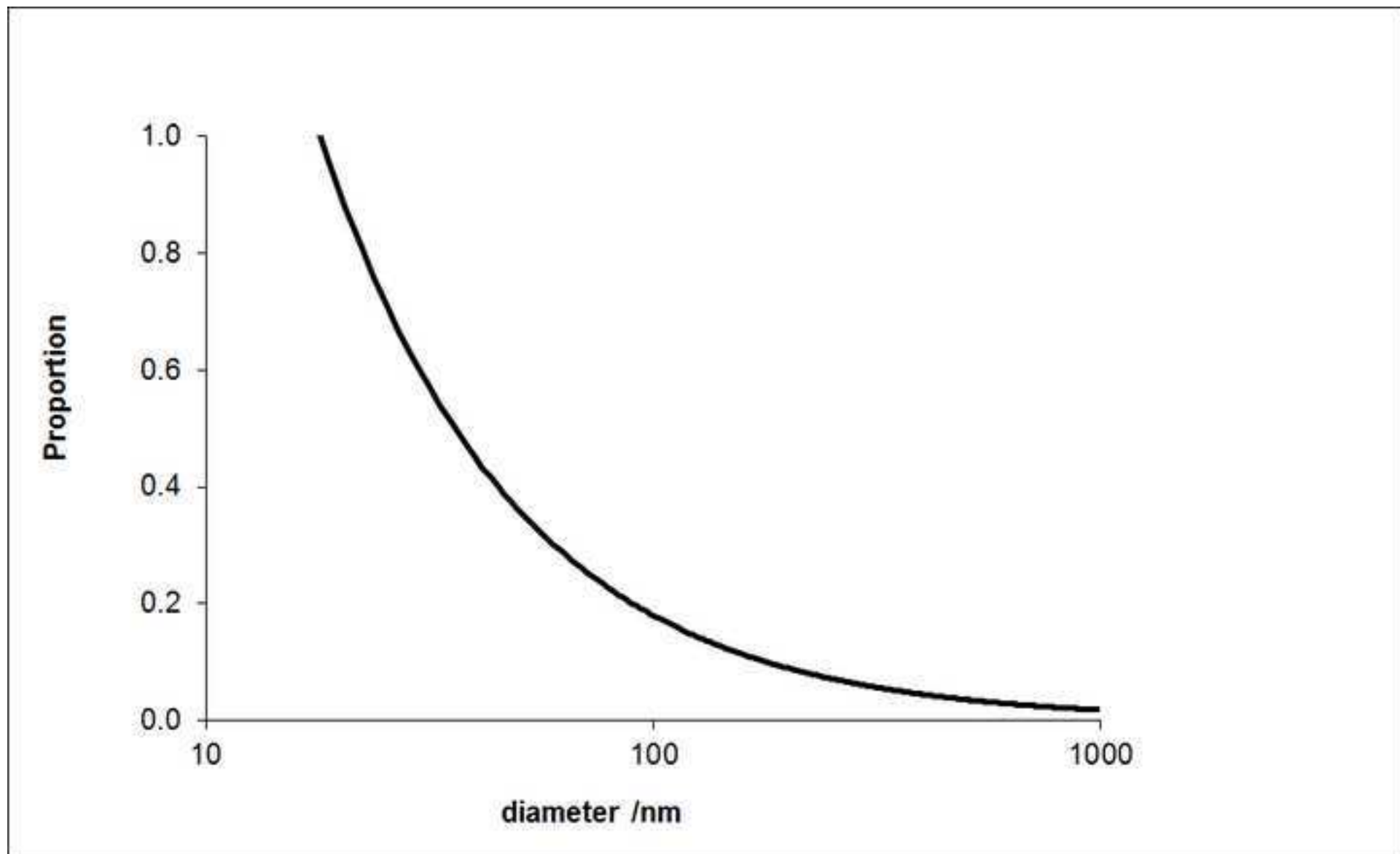


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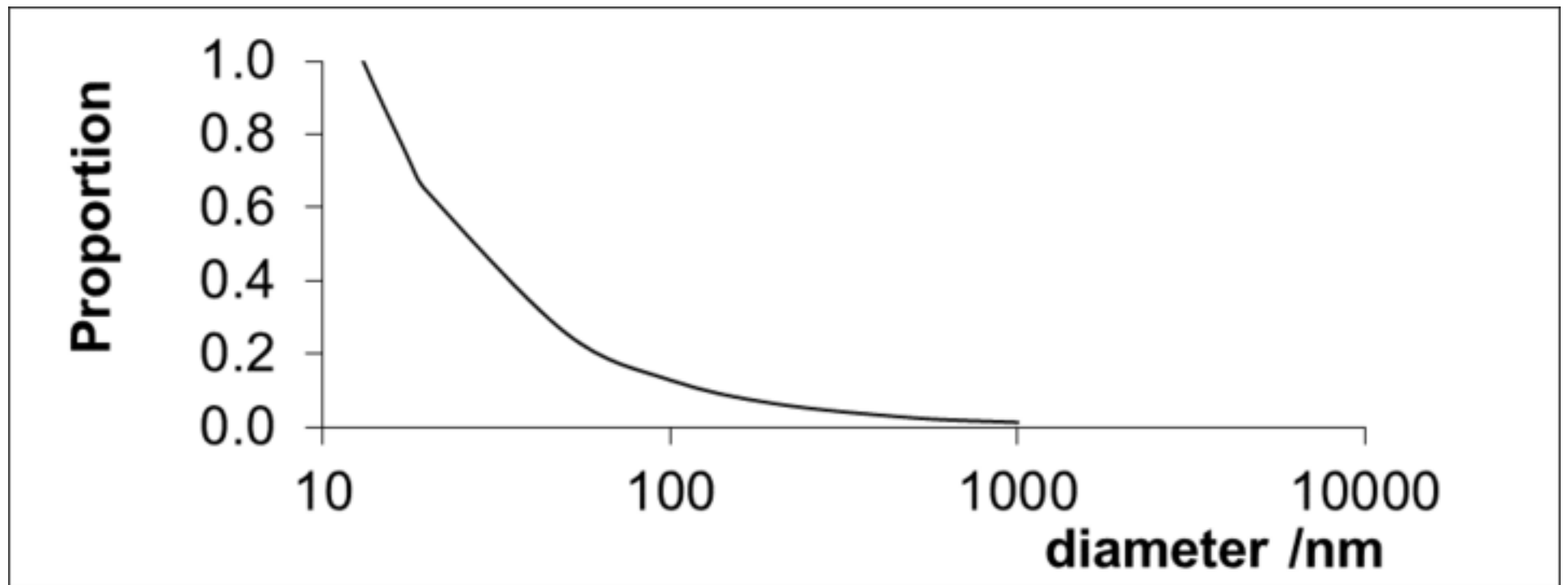


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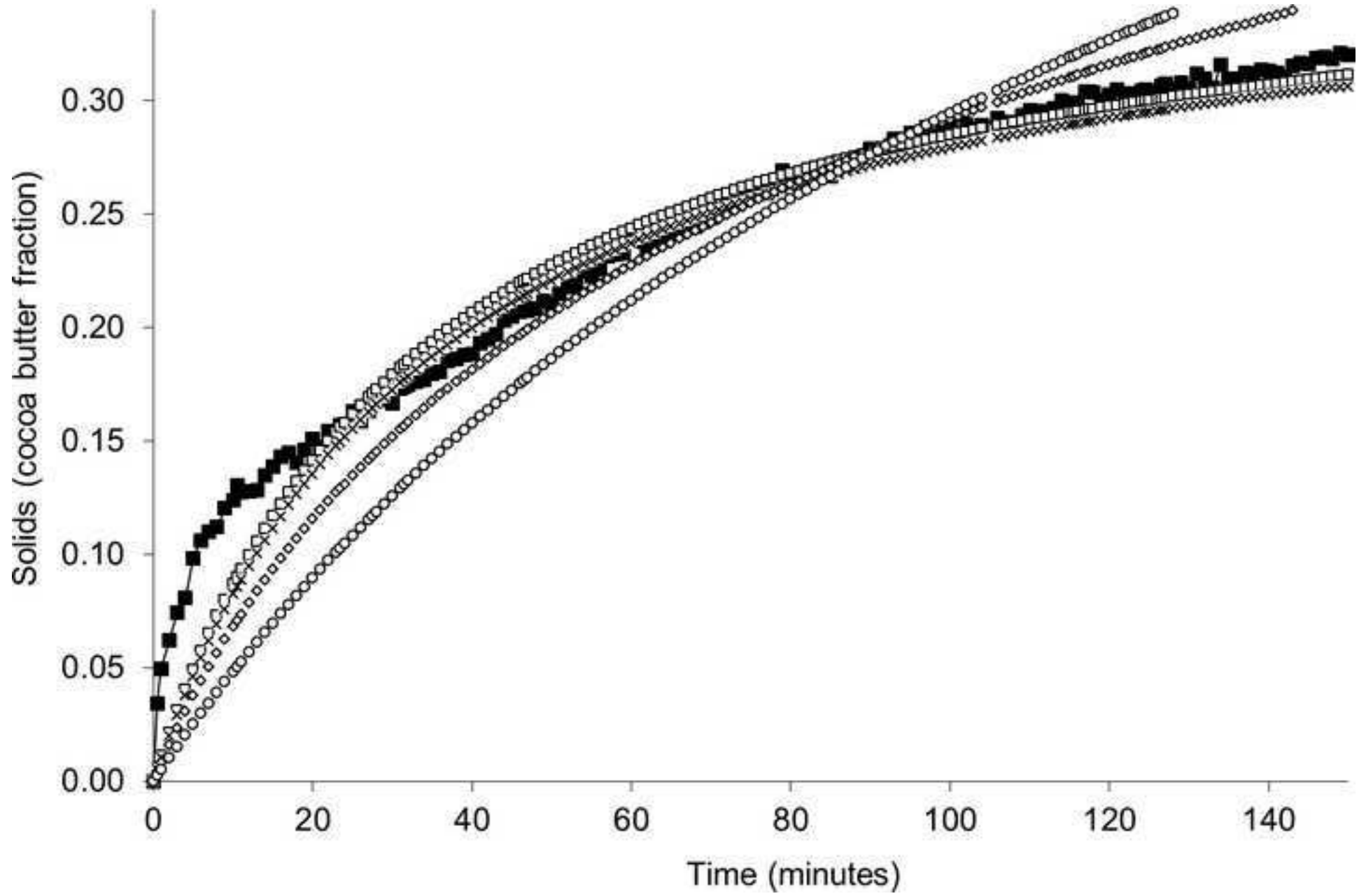


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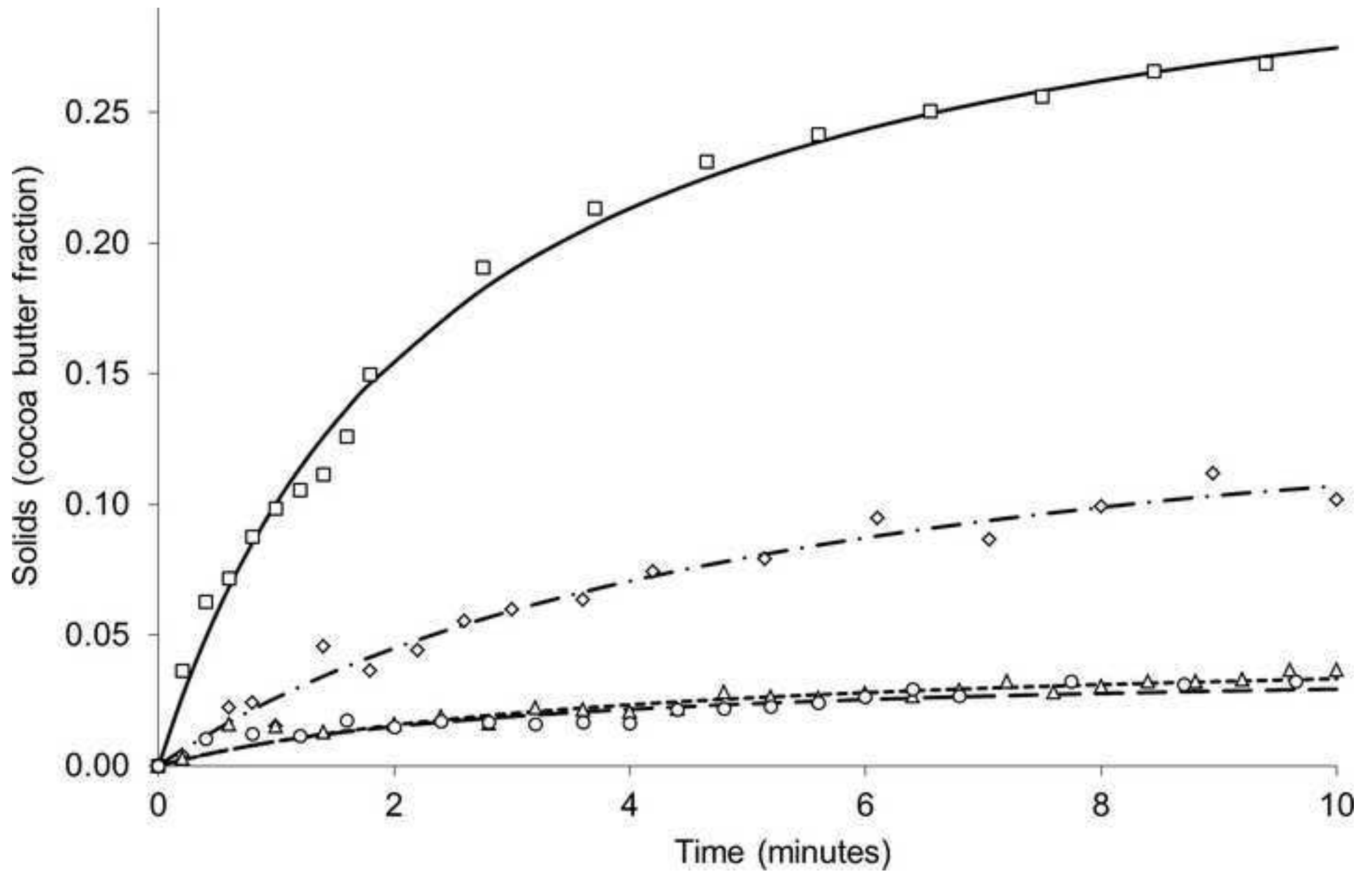


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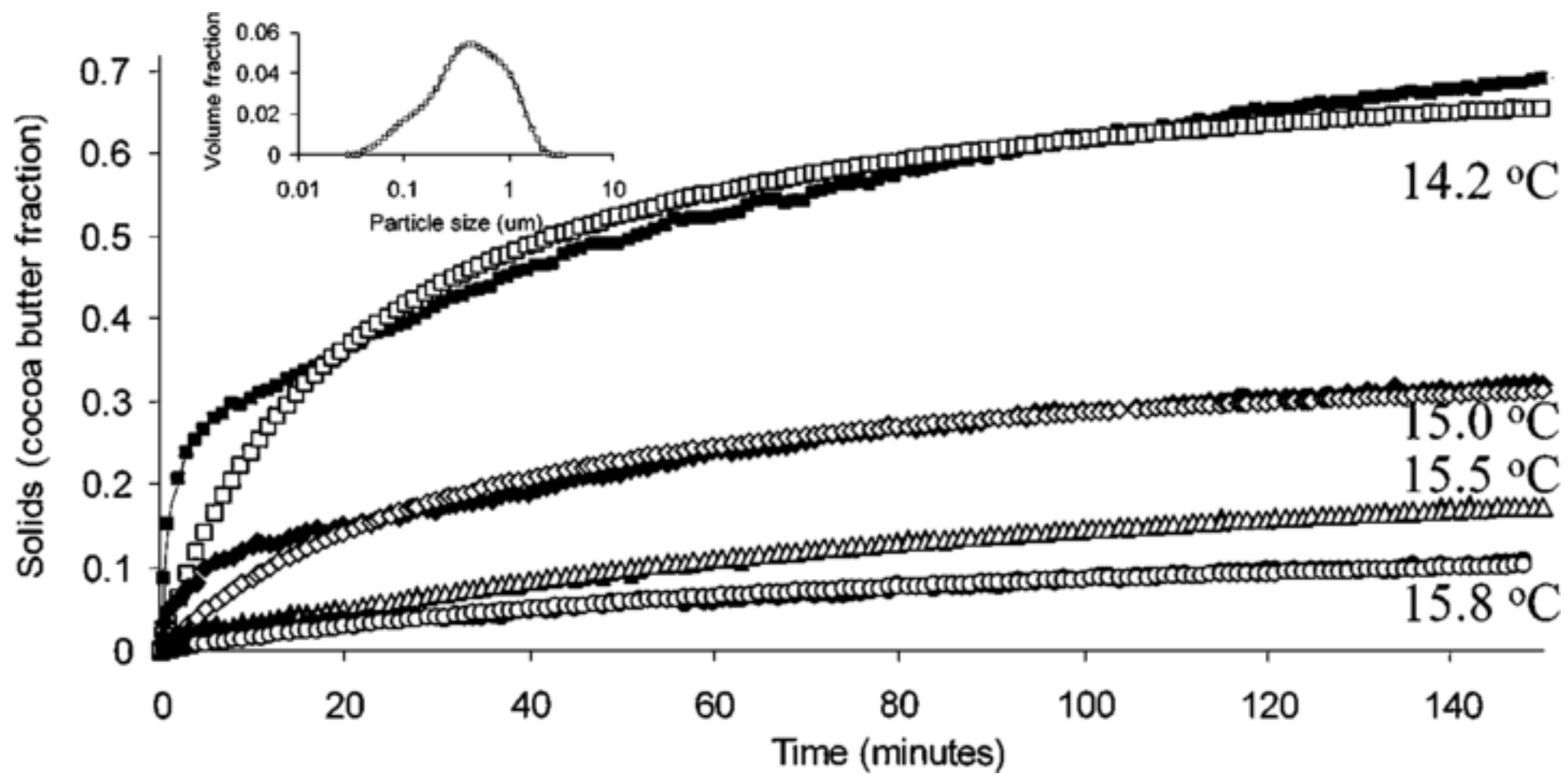


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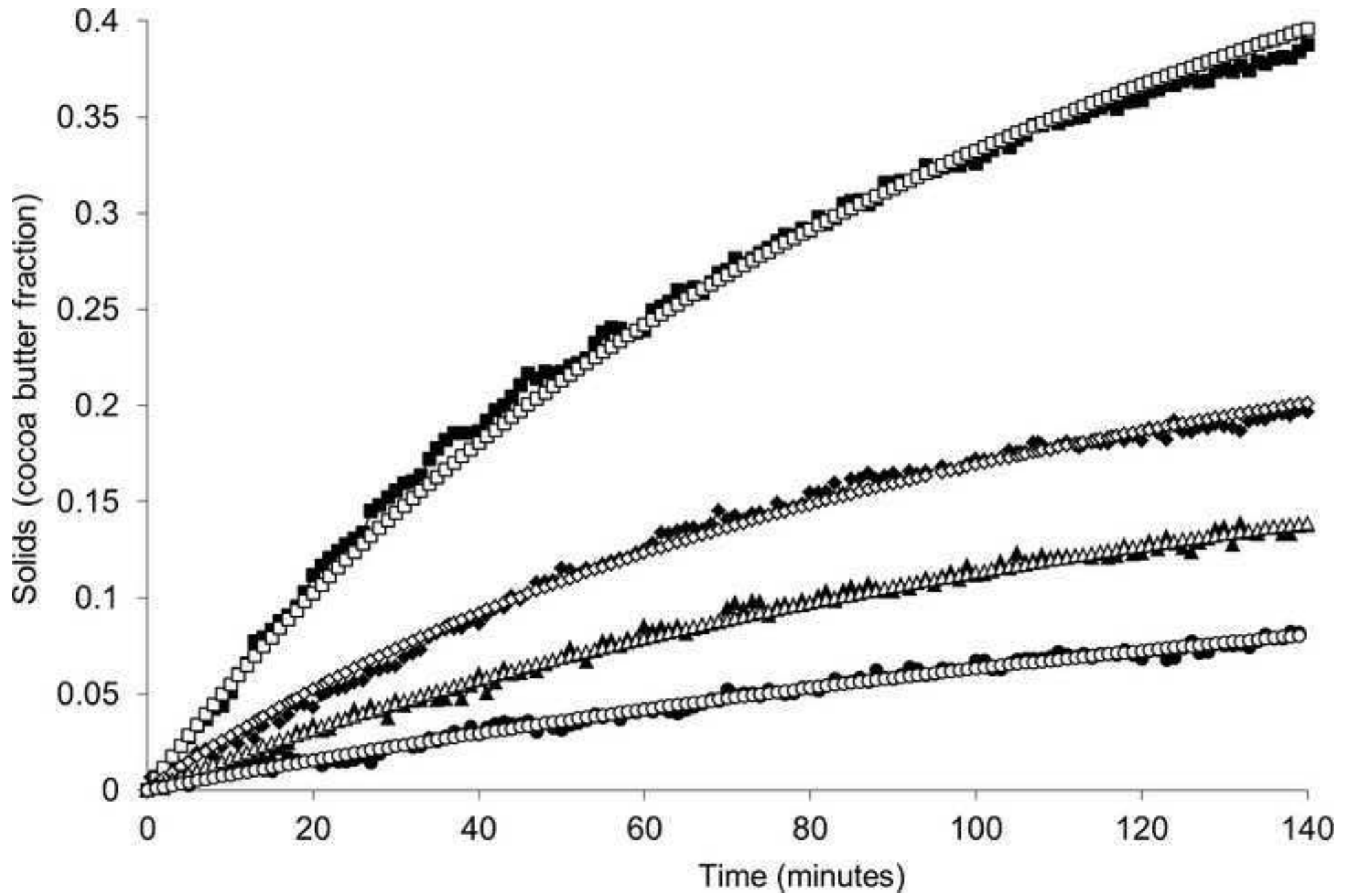


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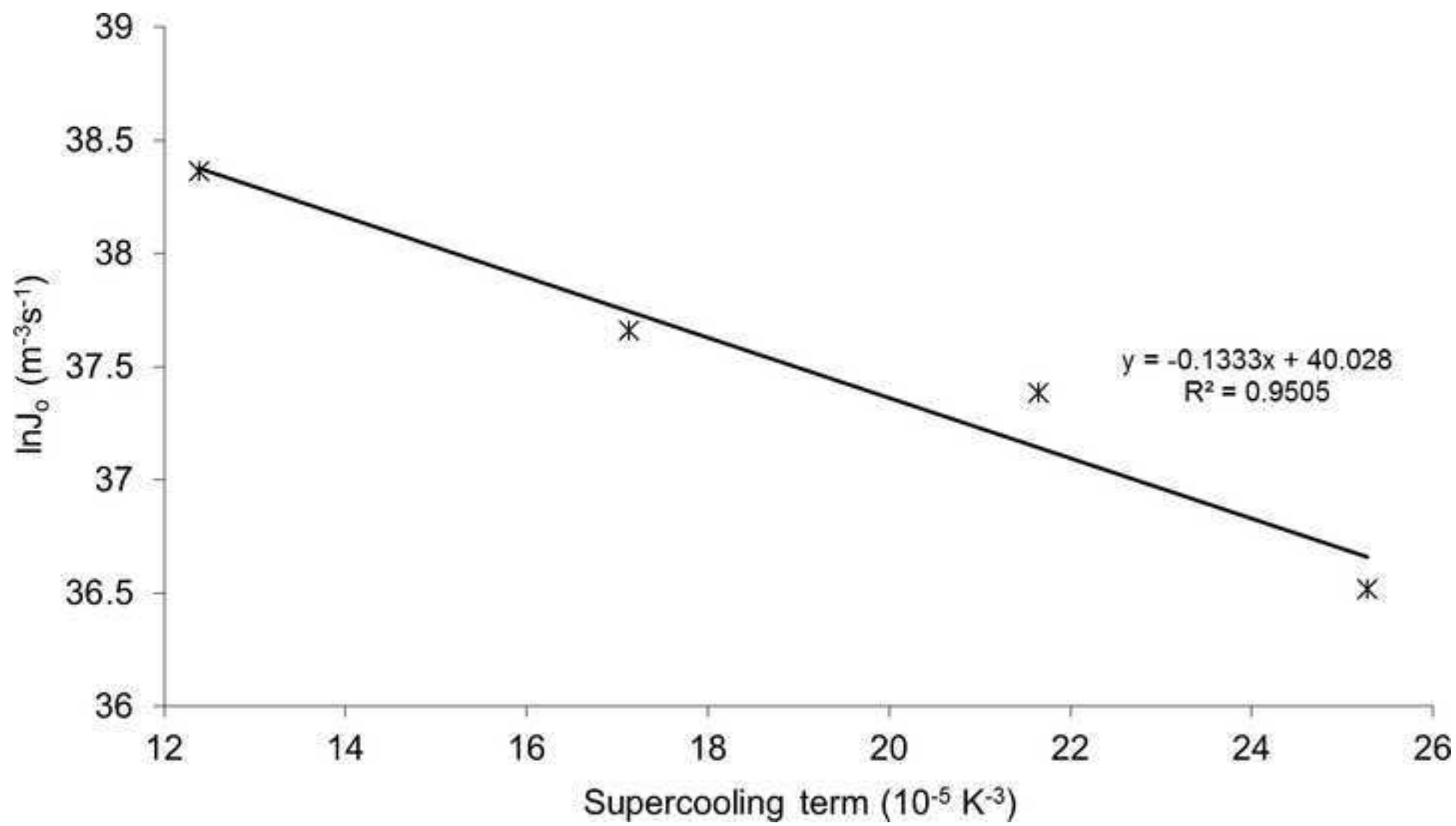


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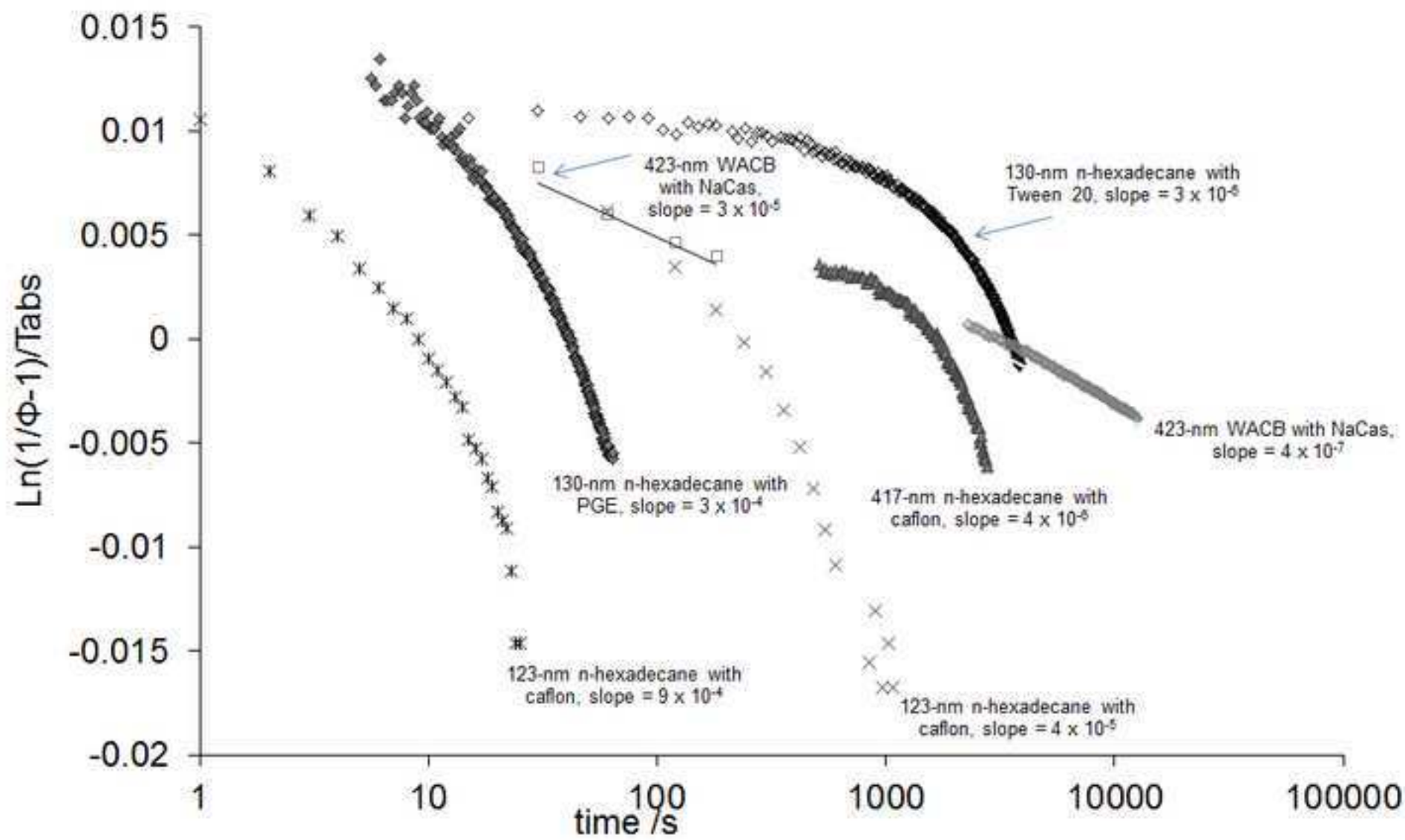


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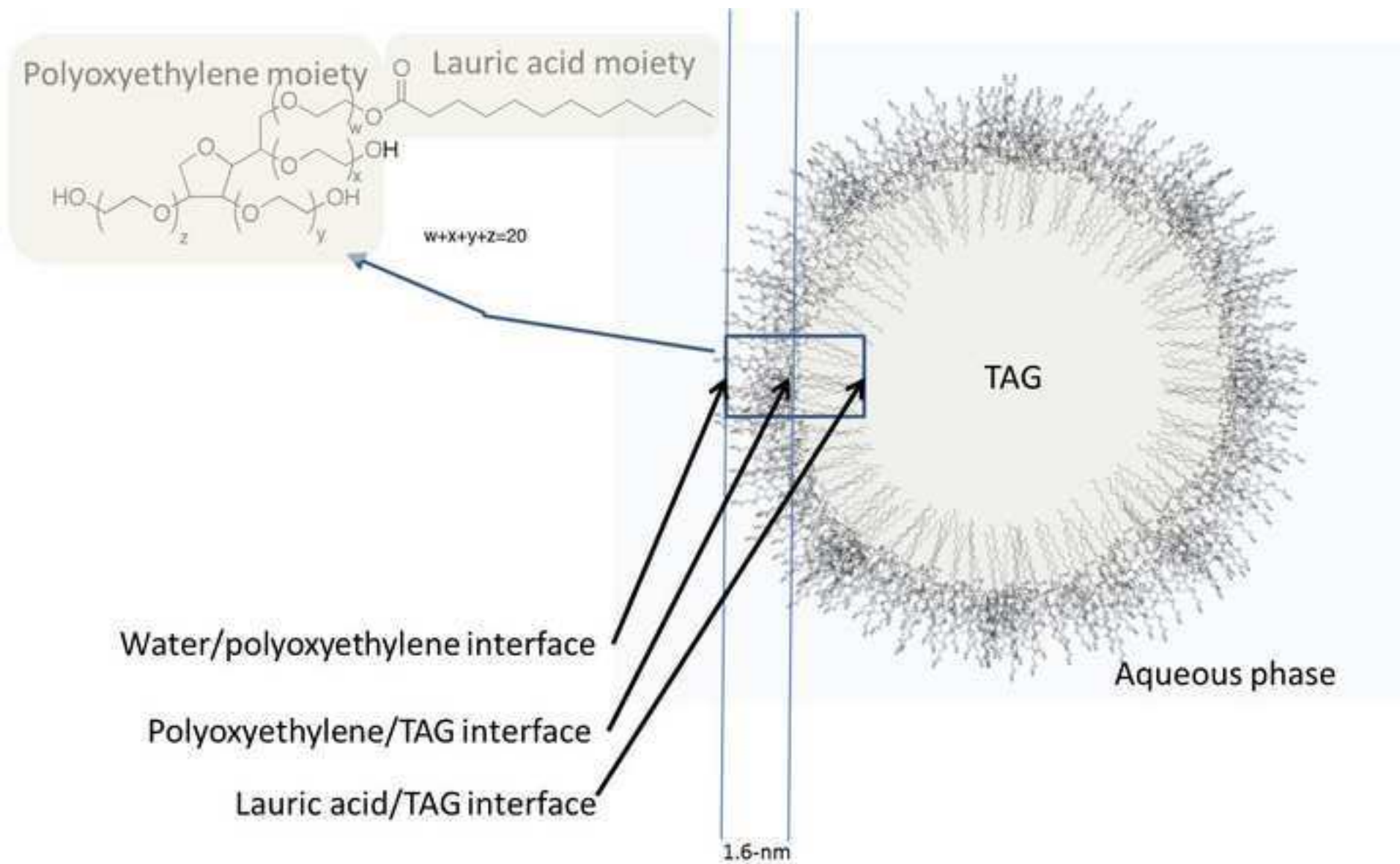


Table 1

TAG-name	ΔH_f kJ/mol			ΔS_f J/mol K		
	α	β'	β	α	β'	β
MMM	84	107	145	275	334	440
PPP	98	132	169	309	399	501
StStSt	113	156	193	343	464	561
n-C19	45	60	-	147	197	-
n-C21	48	63	-	153	203	-

Table 2

TAG	Percentage %	T_{m,α} °C	ΔH_{f,α} kJ mol ⁻¹	T_{m,β'} °C	ΔH_{f,β'} kJ mol ⁻¹	T_{m,β} °C	ΔH_{f,β} kJ mol ⁻¹
PPP	4.0	44.7	95.8	55.7	126.5	65.9	171.3
PStP	26.1	47.2	112.2	67.7	165.5	65.3	173.6
PStSt	39.0	50.1	106.0	61.8	-	64.4	172.9
StStSt	14.5	54.7	108.5	64.3	156.5	72.5	194.2
PPSt	6.0	46.4	100.0	58.7	124.0	62.6	166.3
StPSt	2.2	50.7	103.0	-	-	68.0	170.3

Table 3

Particle diameter	Particle diameter	Particle diameter	Volume per particle	Volume per particle	Area per particle	Area per particle	Total surface area	Total surface area	Number of particles	Number of molecules of trilaurin per droplet	Volume of Tween 20 for monolayer coverage	Volume fraction of Tween 20 for monolayer coverage
	m	μm	m^3	μm^3	m^2	μm^2	m^2	μm^2			m^3	
1mm	0.001	1000	5.24E-10	5.24E+08	3.14E-06	3.14E+06	1.2	1.20E+12	3.82E+05	4.44E+17	1.56E-09	0.0002%
100 μm	0.0001	100	5.24E-13	5.24E+05	3.14E-08	3.14E+04	12	1.20E+13	3.82E+08	4.44E+14	1.56E-08	0.0016%
10 μm	0.00001	10	5.24E-16	5.24E+02	3.14E-10	3.14E+02	120	1.20E+14	3.82E+11	4.44E+11	1.56E-07	0.0156%
1 μm	1E-06	1	5.24E-19	5.24E-01	3.14E-12	3.14E+00	1200	1.20E+15	3.82E+14	4.44E+08	1.56E-06	0.1560%
100 nm	1E-07	0.1	5.24E-22	5.24E-04	3.14E-14	3.14E-02	12000	1.20E+16	3.82E+17	4.44E+05	1.56E-05	1.5600%
10 nm	1E-08	0.01	5.24E-25	5.24E-07	3.14E-16	3.14E-04	120000	1.20E+17	3.82E+20	4.44E+02	1.56E-04	15.6000%

Table 4

Oil in dispersed phase	Surfactant	Particle size d_{32} [nm]	Crystallisation temperature/undercooling [°C]	Reference	Rate constant for transformation from liquid to solid [K ⁻¹ 10 ⁻⁶ s ⁻¹]	Collisions per second per droplet n_d/n_0 [s ⁻¹]	The fraction of collisions leading to nucleation x $1/w = k_{is} * n_d/n_c$	Energy barrier to nucleation $E = k_B T \ln(w)$ [k _B T]
<i>n-hexadecane</i>	Tween 20	2440	1.5/16.7	Povey et al, 2009	§			
		800	2.5/14.7	Povey et al, 2009	§			
		360		McClements et al, 1993	2.22	12	0.18	15.50
		370		Dickinson et al, 1993	1.70	7	0.25	15.21
		370		Dickinson et al, 1993	3.10	7	0.45	14.61
		370		Dickinson et al, 1993	5.20	7	0.76	14.09
		360		Dickinson et al, 1993	7.40	7	0.99	13.82
		370		Dickinson et al, 1993	8.10	7	1.18	13.65
		370		Dickinson et al, 1993	9.20	7	1.34	13.52
		160	2.9/14.3	Povey et al, 2009				
	130	3.1/14.1	Povey et al, 2009	3.00	252	3.30	12.60	
	Tween 20 +0.3 wt % xanthan	370		Dickinson et al, 1996	1.80	1	2.32	12.97
	Tween 20	130		Povey et al, 2009	3.00	252	3.28	12.63
	Sodium dodecyl sulfate (SDS)	360		McClements et al, 1994	1.30	12	0.11	16.04
	beta lactoglobulin	360		McClements et al, 1995	0.66	12	0.05	16.72
beta casein	400		McClements et al, 1996	0.18	9	0.02	17.70	

	PGE	130		Povey et al, 2009†	300.00	63	1312.90	6.64
	Caflon phc060	417	3/14.2	Povey et al, 2009	4.00	8	144.44	8.84
		330	2.8/14.4	Povey et al, 2009				
		139	1/16.2	Povey et al, 2009				
		123		Povey et al, 2009	40.00	75	148.27	8.82
		123		Povey et al, 2009	900.00	74	3336.08	5.70
		50	9.6//8.6	Povey et al, 2009±				
n-octadecane	Caflon phc060	148		Povey et al, 2009	300.00	44	1937.25	6.25
	Tween 20	3450	13/16.5	Gulseren and Coupland,, 2007				
		450	12.5/17	Gulseren and Coupland,, 2007				
		150	12/17.5	Gulseren and Coupland,, 2007				
	Sodium caseinate	3450	14/15.5	Gulseren and Coupland,, 2007				
		450	13.5/16	Gulseren and Coupland,, 2007				
Cocoa butter	Tween 20	2400	14/15.5	Hindle et al, 2002				
		260		Hindle et al 1999	100.00	34	843.63	7.08
	Sodium caseinate	2400	14.2/18	Hindle et al, 2002				
		423		Hindle et al, 2002	0.40	8	15.08	11.10
		423		Hindle et al, 2002	30.00	8	1130.74	6.78

1 Tables

Table 1 Entropy and enthalpy of fusion for some triacylglycerols and n-alkanes (Wesdorp, 1990). MMM – trimyristin, PPP – tripalmitin; StStSt – tristearin..... 14

Table 2 Melting temperature and enthalpies of fusion of pure triacylglycerols in polymorph i, together with the composition of fully hydrogenated palm oil (Wesdorp, 1990)..... 14

Table 3 Particle volume, area and number together with estimates for single molecular layer coverage of emulsion particle with Tween 20, for 1 litre of 20 % v/v trilaurin oil-in-water emulsion. The choice of surface layer depth is based on the assumption that the lauric acid moiety of Tween 20 organises a trilaurin layer one unit cell deep.22

Table 4 List of the kinetic barrier properties of a range of emulsions containing different surfactants, in units of $k_B T$, $E/k_B T$, and the probability that a collision event will lead to nucleation (w^{-1}) for a variety of oils, surfactants and particle sizes. The kinetic data were obtained through measurement of collision mediated nucleation. Crystallisation temperature is defined as the temperature at which the solids fraction is noted to rise above zero, at a given cooling rate. The undercooling is the amount by which the crystallisation temperature is reduced below the bulk melting point. The cooling rate is 1 °C/min in all experiments apart from the cocoa butter, in which case the experiments were carried out isothermally, and the 123-nm Caflon-stabilised emulsion, which was cycled first at 1 °C/min then at 12 °C/min. The cocoa butter data is also shown in Figure 13 and the longer time data represents collision mediated nucleation whilst the short time data is a result of seed crystal nucleation.

§ - data unavailable because nucleation was too fast.

± Data from a microemulsion.

† These data are consistent with dissolution of the surfactant (PGE) in the bulk of the oil.

\$ The nucleation in this sample occurred too quickly to measure.

.....35

1 Figure Captions

- [Figure 1 Plot of surface and volume energy as a function of particle radius for a trilaurin droplet, together with the number of molecules per droplet and the energy of formation of the nucleus. The surface tension in this plot is 30 mN/m and the enthalpy change of the trilaurin into the alpha form is taken as 167 J/kg.....8](#)
- [Figure 2 Plot of surface and volume energy in units of \$k_B T\$ as a function of particle radius for a trilaurin droplet, together with the number of molecules per droplet and the energy of formation of the nucleus. The surface tension in this plot is 1 mN/m and the enthalpy change of the trilaurin into the alpha form is taken as 167 J/kg..... 10](#)
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- [Figure 4 Velocity of sound and density plotted against temperature for a 20 vol. % n-hexadecane oil-in-water emulsions containing 2 wt % Tween 20. Closed circles, velocity on cooling; open circles, velocity on heating; closed squares, density on cooling; open squares, density on heating. Average volume-surface diameter of 800 nm. taken from \(E. Dickinson, et al., 1993\) 18](#)
- [Figure 5 Cocoa butter solids content plotted as a function of particle diameter crystallized at 14.2 °C \(open squares\), 15.0 °C \(open diamonds\), 15.5 °C \(open triangles\) and 15.8 °C \(open circles\). \(S. Hindle, et al., 2000\)20](#)

Figure 6 Proportion of total volume of a trilaurin droplet occupied by a surface layer 6 –nm deep. This choice of surface layer depth is based on the assumption that the lauric acid moiety of Tween 20 organises a trilaurin layer one unit cell deep.21

Figure 7 In the case of an emulsion the foreign surface will be water, the crystal will be the solid lipid and the liquid the oil from which the fat is crystallizing. γ_{ls} is the interfacial tension between the liquid and the foreign surface, γ_{cs} the interfacial tension between the crystal and the foreign surface and γ_{lc} the interfacial tension between the liquid and the crystal. This produces Young’s relation $\cos\theta = \gamma_{ls} - \gamma_{cs}/\gamma_{lc}$23

Figure 8 Plot of solids against time for a 20.75% vol/vol West African cocoa butter (WACB) oil- in-water emulsion (1.00 wt% sodium caseinate) crystallized isothermally at 15.0°C (■ experimental data). The following nucleation models are fitted based on particle size distribution: □ volume heterogeneous, × surface heterogeneous, ◇ volume homogeneous, and Δ surface homogeneous. (Hindle, et al., 2002)27

Figure 9 Plot of solids against time for 20.75% vol/vol WACB oil-in-water emulsions (1.00 wt% sodium caseinate) crystallized at □ 14.2, ◇ 15.0, Δ 15.5, and ○ 15.8°C. Heterogeneous volume particle size distribution nucleation models are fitted to experimental data (shown as solid lines) (Hindle, et al., 2002). For abbreviation see Figure 8.28

Figure 10 Plot of solids against time for 20.75% v/v WACB oil-in-water emulsions (0.8% v/v Tween 20) crystallized isothermally at ○, 14.2°C; Δ, 15.0°C;◇ , 15.5°C; and□, 15.8°C. Closed symbols are experimental data and open symbols are heterogeneous volume particle size distribution models fitted over the time period 0–150 min. Insert: Corresponding particle size distribution (S. Hindle, M. Povey, & K. Smith, 2000)30

Figure 11. Plot of solids against time in which the first 10 minutes of the data in Figure 10 is ignored A heterogeneous nucleation model now fits the data very well. (20.75% v/v WACB

oil-in-water emulsions (0.8% v/v Tween 20) crystallized isothermally at \circ , 14.2°C; Δ , 15.0°C; \diamond , 15.5°C; and \square , 15.8°C. Closed symbols are experimental data.) (S Hindle, et al., 2000)31

Figure 12 Data in Figure 11 plotted against the undercooling term $1T\Delta 2T$ 32

Figure 13 Analysis of a range of solid content vs time data using (13, for a range of crystallizing oils and surfactants. The rate constant k_s is shown on the Figure for each combination of oil and surfactant (Povey, Awad, Huo, & Ding, 2009)33

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