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# A Comparative Analysis of Particle Tracking in a Mixer by Discrete Element Method and Positron Emission Particle Tracking

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## Abstract.

Characterisation of particle flow using Positron Emission Particle Tracking (PEPT) is based on tracking the position of a single particle in a dynamic system. Recent developments in PEPT have facilitated tracking multiple particles aiming at improvements in data representation. Nevertheless for systems with a wide residence time distribution and/or dead zone, the conditions for getting representative data which could reflect the bulk behaviour of the powders need to be analysed and specified. In the present work, an attempt is made to simulate PEPT experiments for a paddle mixer using Discrete Element Method (DEM), with a view to investigate the effect of increasing the number of tracers on their time-averaged velocity distribution and whether it can represent the data on whole population of particles. The time averaged velocity distribution of the individual tracer particles (resembling simulated PEPT) is obtained and compared with the time averaged data on entire particle population. The DEM results indicate that for the investigated paddle mixer, it takes 251 seconds for one tracer to travel adequately in all the active space of the system. The instantaneous tracer velocity fluctuates around the average value obtained for all the particles, suggesting the average tracer velocity is adequately representative of the average particle velocity in the system. The data of PEPT experiment with one tracer with those of DEM with one tracer are in good agreement, however DEM

34 simulation suggests that increasing the number of tracers in the paddle mixer system does not  
35 influence the average velocity distribution. Furthermore, the velocity for all particles in the DEM  
36 shows a smooth distribution with a peak frequency of the velocity distribution that is lower than PEPT  
37 and DEM tracer. When tracking a single tracer in DEM or PEPT, it may not be detected to have zero  
38 velocity at any instant of time, while the data for all particles show that about 0.3% of particles are  
39 stagnant.

40

41 **Keywords:** Discrete Element Method (DEM), Positron Emission Particle Tracking (PEPT), Paddle  
42 mixer, Number of Tracers

43

#### 44 **1. Introduction**

45 In industries such as detergent, cosmetic, food and pharmaceutical manufacturing, powder mixing is a  
46 common process. Optimisation and control of mixing are critically important but very challenging. A  
47 key step in optimising the mixing process is to understand the powder kinematic behaviour (flow  
48 fields, mixing patterns, etc.) to enable efficient process design and control [1]. However it is difficult  
49 to obtain an insight into the internal flow field during mixing processes and to address the kinematic  
50 behaviour of powders using experimental approaches, particularly at large scales. Advances in  
51 experimental measurements of internal flow based on Positron Emission Particle Tracking (PEPT)  
52 have made it possible to get detailed information on the rate of mixing, but are limited to small scales  
53 [2, 3]. In PEPT, the motion of an irradiated tracer particle is tracked using appropriate sensors, from  
54 which the temporal and spatial information about the particle is deduced [4]. A natural question which  
55 emerges is to what extent the data from a single particle are representative and how such information  
56 could be applicable to larger scales. For this purpose Hassanpour et al. [5] simulated a paddle mixer  
57 using the Distinct Element Method (DEM) and compared the results to those of PEPT. A qualitative  
58 comparison between the time-averaged velocity profiles of a representative case from PEPT  
59 measurements and corresponding DEM simulations showed a good qualitative agreement on the  
60 internal flow patterns. In order to make quantitative comparisons, the particle dynamics were analysed  
61 in terms of normalised velocity distributions (i.e. magnitude of particle velocity normalised to paddle

62 tip speed). Due to the computational limitations, DEM simulations were carried out for a maximum of  
63 10 s of real time only. Within this short period, the data were insufficient for one single particle  
64 relating to comparison with PEPT measurements; therefore the data from all particles in the DEM  
65 simulations were used in the calculations. The time-averaged normalised velocity distribution  
66 obtained from DEM analysis was compared with that from PEPT measurements for representative  
67 process conditions. It was found that the DEM model predicted a smooth distribution of particle  
68 velocities while the PEPT data showed more scatter or fluctuation in the frequency plot. This  
69 difference was attributed to the fact that the PEPT analysis was based on data from only one particle,  
70 i.e. the tracer, while the DEM results were from the velocity profiles of the whole population of  
71 particles. Overall there was a reasonable agreement in the velocity distribution, but the comparison  
72 was not rigorous.

73

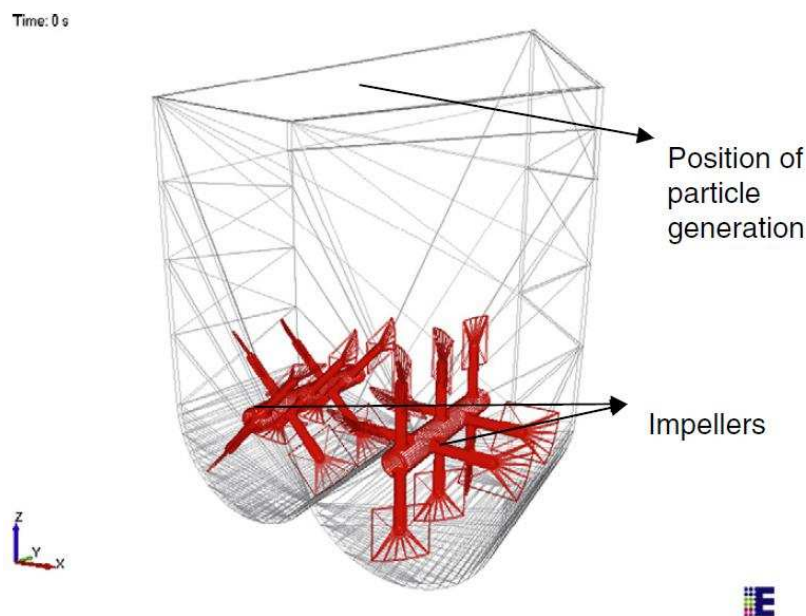
74 In PEPT the tracking process is carried out for a few minutes to generate sufficiently accurate time-  
75 averaged data. However, the total length of experiment for reliable and statistically representative  
76 data is based on trial and error and there is no solid evidence confirming the tracer could represent the  
77 data for all particles. It has recently been shown [6] that using manipulated algorithms, multiple  
78 tracers can be used in PEPT, however its effect on providing better representative data for all the  
79 particles has yet to be critically evaluated. In the present work, an attempt is made to simulate PEPT  
80 experiments for a paddle mixer using DEM, with a view to investigate the effect of increasing the  
81 number of tracers on the time-averaged velocity distribution. The velocity information is available for  
82 all individual particles in DEM; therefore, the average particle velocity and velocity distribution of the  
83 whole population of particles could be compared with those of individual tracers in the simulation.  
84 The results of DEM are also compared to those of PEPT experiment using a single tracer.

85

## 86 **2. DEM simulation of the paddle mixer**

87 DEM simulations provide dynamic information of transient forces acting on individual particles  
88 throughout the simulations, which is otherwise difficult to obtain. The interactions between the  
89 constituent particles are based on theories of contact mechanics. More details on the methodology of

90 the DEM and its applications are presented elsewhere [7, 8]. The simulations were conducted using  
91 EDEM<sup>®</sup> software provided by DEM Solutions, Edinburgh, UK. The calculation of the contact forces  
92 of the particles is based on the Hertz-Mindlin model [9]. The experimental work using PEPT was  
93 carried out on dry, free-flowing particles; hence the contact model did not include adhesive term. Due  
94 to the limitation of computer power, it is not possible at this stage to simulate the actual number of  
95 particles (around 50 millions) within a reasonable time. Therefore, the simulation was carried out with  
96 a smaller number but larger particles. In this case particle density is adjusted to maintain a similar  
97 momentum exchange between particles as of the real case [10]. In the previous work by Hassanpour  
98 et al. [5] it was shown that the steady state average velocity magnitude slightly decreased as the  
99 particle size was reduced in the same paddle mixer system. This shows that the average particle  
100 velocity is slightly sensitive to the particle size, but the effect is not very significant. Here, the same  
101 particle size similar to that used by Hassanpour et al. [5] is used. The geometry of the simulated  
102 paddle mixer is the same as the previous work, for which a CAD drawing was imported into the  
103 EDEM computer code (Figure 1).



104

105 Figure 1: The imported geometry of the paddle mixer simulated by the DEM.

106

107 As it can be seen, the mixer consists of two intersected semi-cylinders of the same span and two  
108 counter-rotating impellers, each with 10 paddles positioned pair-wise along 5 axial positions.

109 Properties of the particles are also the same as the previous work [5], which can be seen in Table 1  
110 and 2. Particles were generated randomly at spatial locations above the impellers (the position shown  
111 in Figure 1).

112

113 Table 1: The properties of particles and walls used in DEM simulation

Property	Particles	Equipment wall
Particle diameter (mm)	4.52	-
Shear modulus (GPa)	0.1	70
Density (kg/m <sup>3</sup> )	1000	7800
Poisson's ratio (-)	0.2	0.3

114

115

116 Table 2: The contact properties used in DEM simulation

Property	Particle-particle	Particle-wall
Coefficient of sliding friction	0.3	0.3
Coefficient of rolling friction	0.01	0.01
Coefficient of restitution	0.4	0.4

117

118 The filling of 60000 particles was carried out while the mixer impellers were stationary similar to  
119 previous work [5]. The particles were subjected to gravitational acceleration and gradually settled  
120 toward the bottom of the mixer. The simulations were carried out under a constant rotational speed of  
121 impellers for 10 minutes of real time which took three months to complete. For confidentiality reasons  
122 it is not possible to disclose the impeller rotational speeds.

123

### 124 3. PEPT experiments

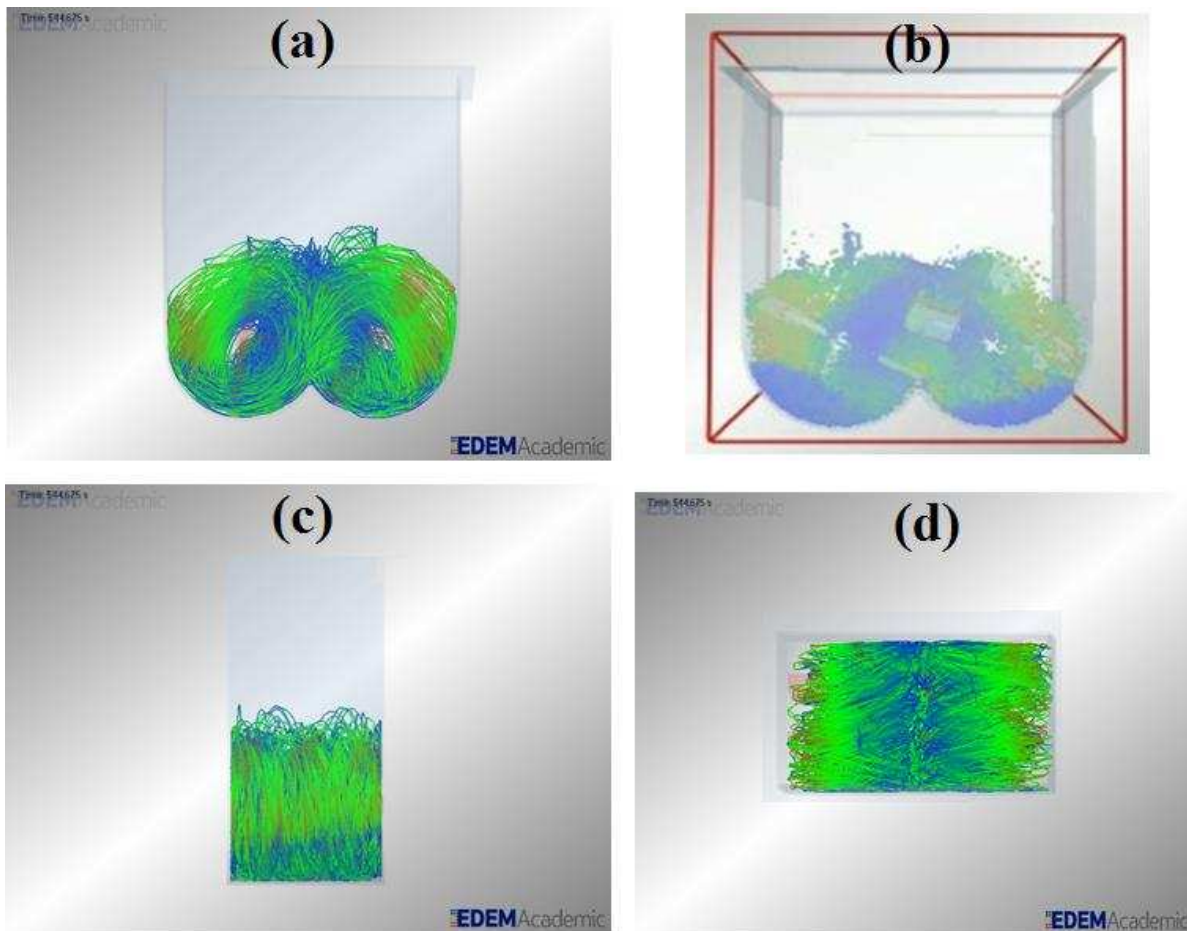
125 The experimental results of PEPT are taken from the previous work of Hassanpour et al [5]. In their  
126 work, the Positron Emission Particle Tracking (PEPT) facility of the University of Birmingham  
127 (Birmingham, UK) was used to track particle motion. In a typical experiment, particles were loaded  
128 into the mixer which was then started and run for a couple of minutes to ensure that the steady state  
129 was reached before starting the data requisition process. Radioactive particles (0.7 mm in diameter  
130 with 1200 kg/m<sup>3</sup> density) were used as tracers, which were activated by an ion exchange method with  
131 radioactive water produced in a cyclotron [4]. For each experiment one tracer was used and the data

132 acquisition was performed for at least 15 min for each run which gave at least 20,000 data points in  
133 the form of spatial locations in the Cartesian coordinate as a function of time.

134

#### 135 4. Results and discussion

136 Figure 2 shows the streamlines of the tracer from three different viewing angles as well as a view of  
137 all the particles in the system, all coloured based on the normalised speed (i.e. ratio of tracer particle  
138 speed to paddle tip speed): red being the maximum (i.e. 1) and blue being the minimum (i.e. 0).



139

140 Figure 2: The tracer streamlines and particles view: (a) front view streamlines (b) front view of the  
141 particles (c) right view streamlines and (d) top view streamlines in the system. The colour scheme is  
142 based on the normalised speed of the tracer/particles.

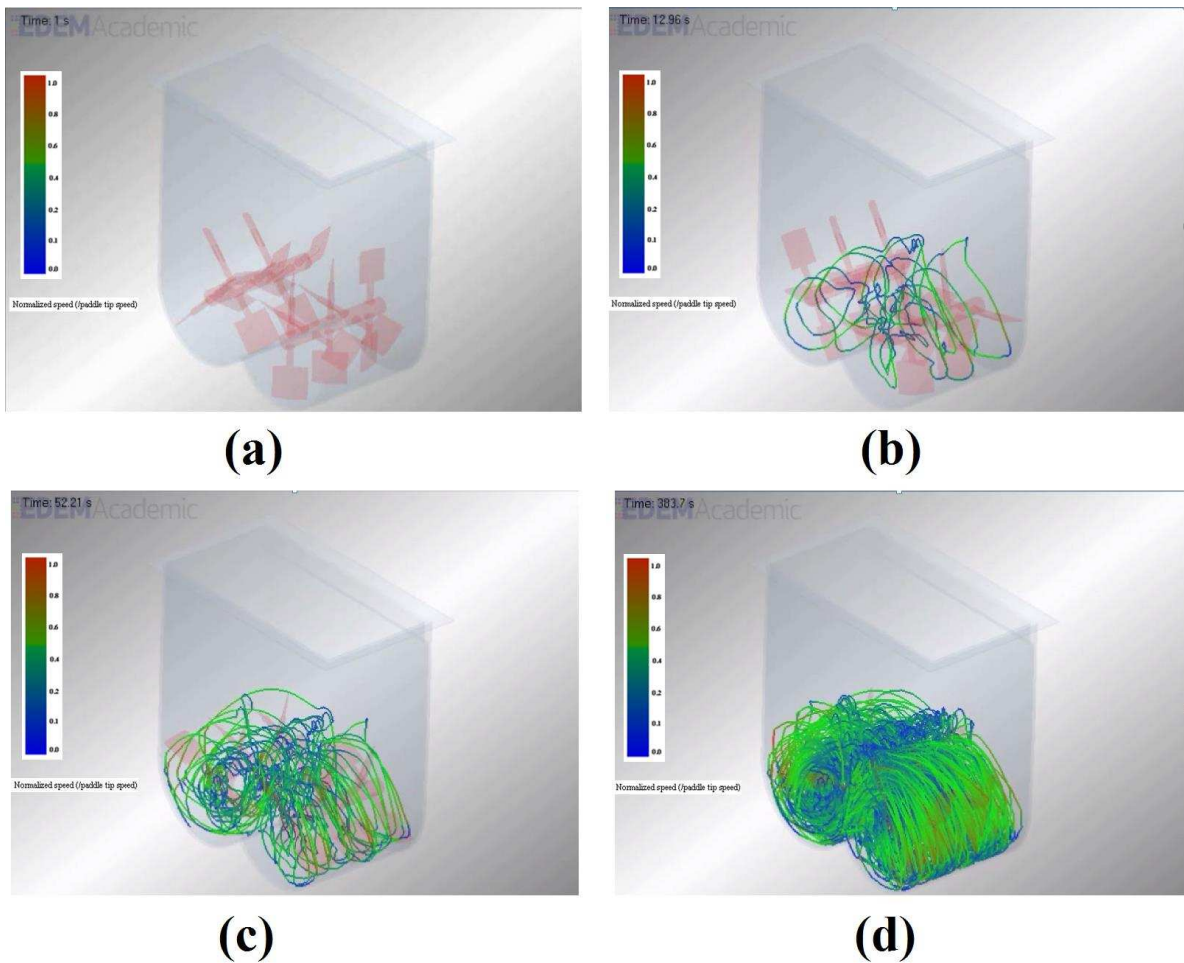
143

144 Figure 2 qualitatively shows that the tracer particle has been present almost in all active locations of  
145 the mixer space, which was occupied by the particles. The velocity distribution, which can be

146 qualitatively seen by the colour scheme used in the figure, matches with that of the whole population  
147 of particles in the simulation. This has been analysed quantitatively and will be shown in the next  
148 section.

149

150 Figure 3 shows the development of tracer streamlines at four different simulation times: 1, 13, 52 and  
151 384 s. The trace is coloured based on the normalised speed of the tracer particle: red being the  
152 maximum (i.e. 1) and blue being the minimum (0).



153

154 Figure 3: Tracer streamlines development at four different simulation times: (a) 1, (b) 13, (c) 52 and  
155 (d) 384 s. The trace is coloured based on the normalised speed of the tracer particle.

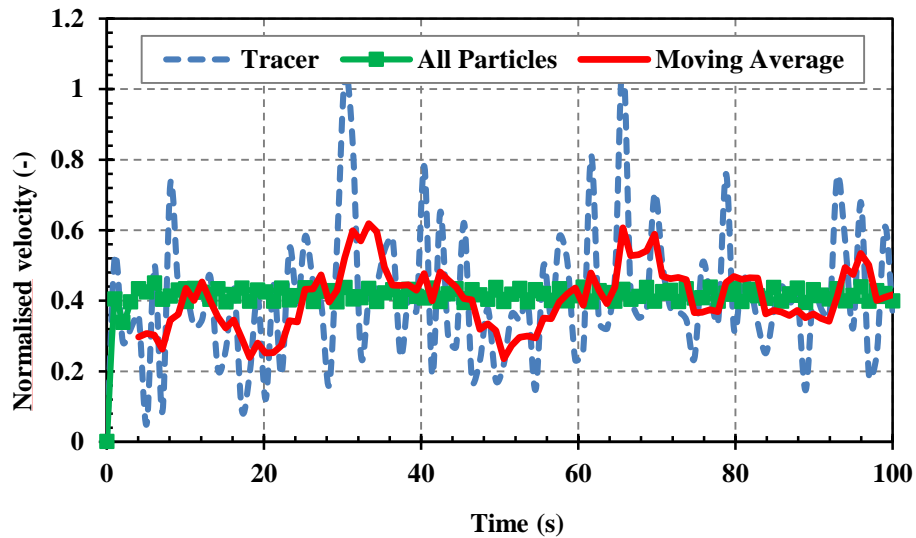
156

157 Figure 3 qualitatively shows the streamlines gradually develop and after about 384 seconds of  
158 simulation time shows presence in almost all the dynamic space of the geometry.

159



160 Figure 4 shows the average velocity (magnitude of velocity) of the whole particle population as  
161 compared to the tracer velocity for the first 100 seconds of the simulation.



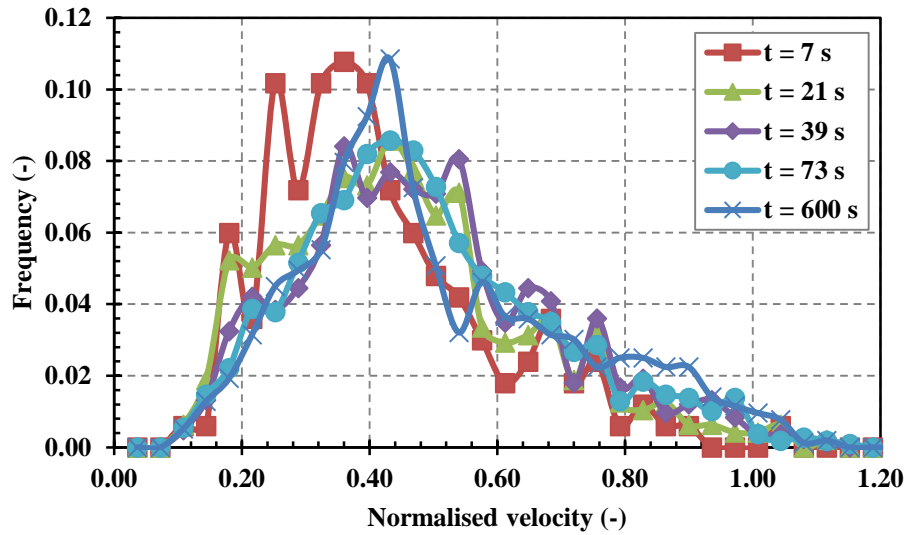
162  
163 Figure 4: Average velocity of the whole particle population, tracer velocity and its moving average for  
164 the first 100 seconds of the simulation.

165  
166 The figure shows the tracer velocity fluctuates over the average value obtained for all the particles in  
167 the system. In order to better compare the tracer velocity with the average velocity of all particles, the  
168 fluctuations of tracer particle were reduced by arithmetically averaging the tracer velocity for every 5  
169 data points (i.e. every 0.05 seconds instead of every 0.01 seconds) which is also plotted as a function  
170 of time. The moving average trend of the tracer velocity demonstrates fewer fluctuations, suggesting  
171 that the average tracer velocity could be representative of the average particle velocity in the system.

172  
173 In order to quantitatively investigate the time needed for the tracer to develop its streamlines, the  
174 normalised tracer velocity distribution is evaluated at different simulations times and is plotted in  
175 Figures 5 and 6. To do so, the active region of the geometry was divided into cuboid bins each of  
176 which had dimensions of 0.0205, 0.02 and 0.02 m in x, y and z direction, respectively. In each  
177 recorded time-step, based on the position of the tracer, the bin in which the tracer existed was  
178 determined. This spatial discretisation is similar to PEPT analysis. The normalised tracer velocity in  
179 each bin which was then evaluated and its distribution among bins is plotted (as seen in Figures 5 and

180 6). Throughout the present paper, the velocity distributions for DEM tracer(s) are obtained based on  
181 recording sample rates of 0.01 seconds.

182



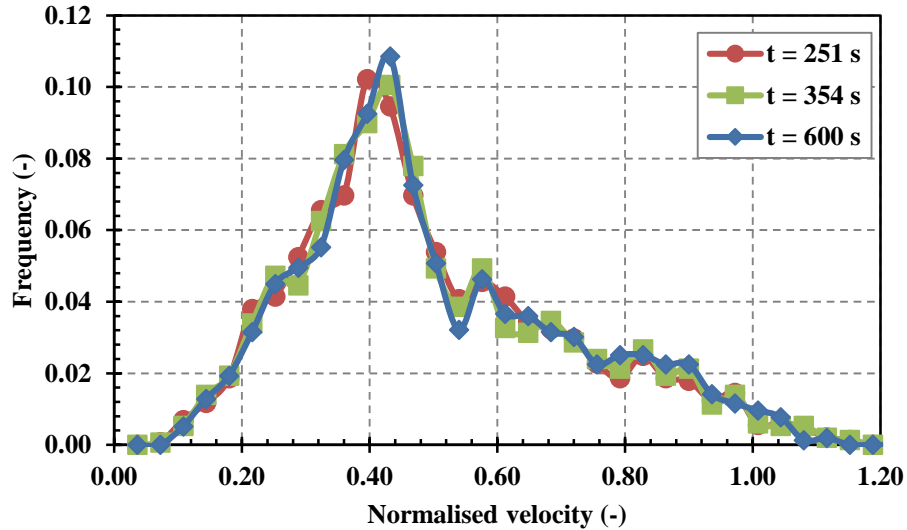
183

184 Figure 5: Tracer normalised velocity distribution at different simulations time: 7, 21, 39, 73 and 600 s

185

186 As it can be seen in Figure 5, the normalised tracer velocity distribution develops with time. If the  
187 velocity distribution does not change after some simulation time, it can be concluded that at that time  
188 the velocity distribution is developed and therefore there is no need to carry on the simulations (or in  
189 experiments carrying out the PEPT experiments). This can be seen in Figure 6, where the normalised  
190 velocity distribution of the tracer does not change much after about 251 seconds of simulation time.

191



192

193 Figure 6: Tracer normalised velocity distribution at different simulation time: 251, 354 and 600 s

194

195 In order to investigate the effects of multiple tracers in the velocity distribution, five particles were  
 196 tracked in the simulations. These five particles were selected randomly at different positions inside the  
 197 mixer at the end of the simulation (i.e. at  $t = 600$  s), then post processing started from initial time (0 s)  
 198 for these particles. Figure 7 shows the normalised tracer velocity distribution using 1-5 tracers at the  
 199 end of simulation (i.e.  $t = 600$  s). For the multiple tracer cases, the normalised velocity is calculated  
 200 by taking the average value of the normalised velocity of the tracers in each bin. It must be noted that  
 201 the sampling rate can affect the distributions however since all the distribution are based on the same  
 202 sampling rate (every 0.01 seconds), the comparative conclusions are valid.

203

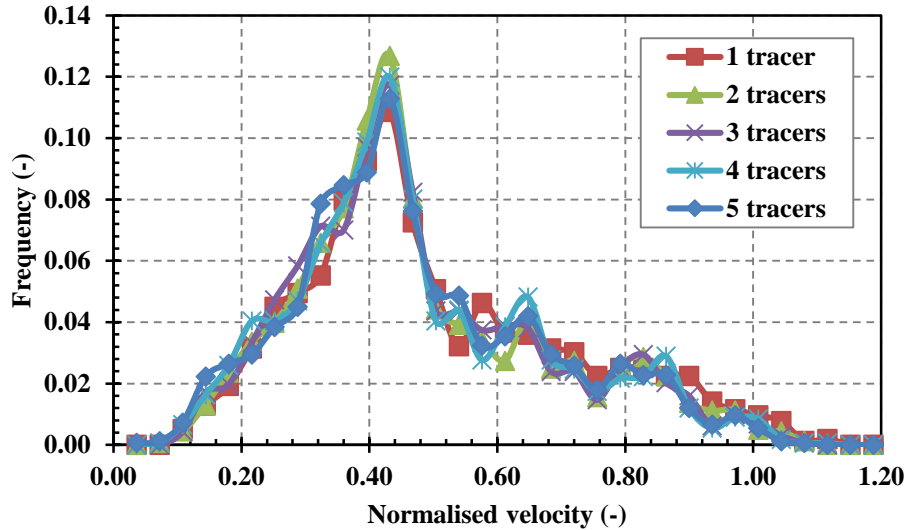


Figure 7: Normalised tracer velocity distribution using 1-5 tracers at  $t = 600$  s

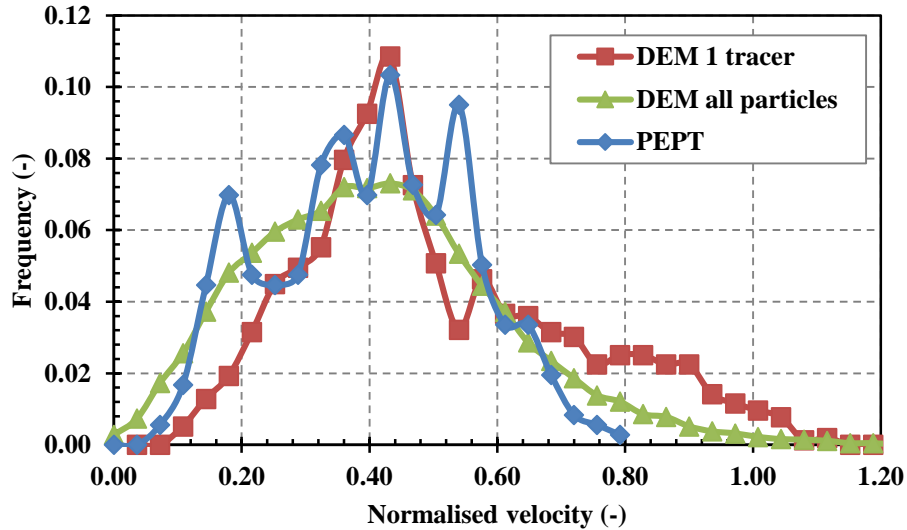
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205

206

207 As it can be seen, increasing the number of tracers in this paddle mixer system does not influence the  
 208 velocity distribution. In addition, for the system studied in this work it has been observed that  
 209 increasing the number of tracers does not significantly shorten the time required to achieve a  
 210 representative and time independent data. Furthermore for experimental PEPT the data acquisition  
 211 and analysis could be more complex and time consuming. Therefore, one conclude that the use of  
 212 multiple tracers in PEPT measurements does not provide improvements in the velocity distribution  
 213 results and hence little benefit in this respect could be achieved. Figure 8 compares the normalised  
 214 velocity distributions obtained from the experimental PEPT, one tracer particle in DEM and all the  
 215 population of particles in DEM. The data on all particles has not been analysed in bins and rather data  
 216 on each particle was time averaged and their distribution was plotted. The aim was to compare if  
 217 PEPT results are representative of entire system in terms of entire particle population velocity  
 218 distribution.

219



220

221 Figure 8: Comparison of normalised velocity distributions obtained from the experimental PEPT, 1  
 222 tracer particle in DEM and all the population of particles in DEM.

223

224 The figure shows although the peak frequencies of the velocity distribution for PEPT and DEM with  
 225 one tracer are very similar, there are discrepancies over the width of the distribution and the  
 226 frequencies of tracer with higher velocities. DEM tracer predicts a wider velocity distribution  
 227 compared to PEPT. For normalised velocity of 0.7 and higher, the frequency distribution of DEM  
 228 tracer is significantly higher than PEPT. One reason for this observation could be the differences in  
 229 particle shape and size distribution for DEM and the experiment. Furthermore, the velocity for all  
 230 particles in DEM shows a smooth distribution with a peak frequency of the velocity distribution lower  
 231 than PEPT and DEM tracer. The velocity distribution data for the population of particles in DEM are  
 232 based on a large number of particles (60,000 in this case), while for PEPT and DEM tracers it is based  
 233 on time-averaged velocity distribution of a single tracer. Therefore the scatter and fluctuations in  
 234 PEPT and DEM one tracer data, relative to DEM population, is expected. Potential explanations for  
 235 the difference in the peak of the distribution could be attributed to the aforementioned particle size  
 236 discrepancies and/or the sampling method: PEPT and DEM tracer analyses are based on data from  
 237 only one particle within a discretised domain, i.e. the bins, while the DEM results consider the  
 238 velocity profiles of the whole population of particles. Furthermore, in contrast to the DEM with one  
 239 tracer data and PEPT, it can be seen that the data for all particles show that about 0.3% of particles are

240 stagnant at any instance. When tracking a single tracer in DEM or PEPT, it may not be possible to  
241 detect zero velocity at any time. This could have implications for diagnosing stagnant regions where  
242 some particles in the mixer have no motion. This is a short coming of single tracer data which could  
243 not be representing all particles, particularly those which are stagnant. This requires further attention  
244 in future work.

245

## 246 **5. Conclusions**

247 The DEM results indicate that for the investigated paddle mixer, it takes 251 seconds for one tracer to  
248 travel adequately in all the dynamic space of the system. The tracer velocity fluctuates around the  
249 average value obtained for all the particles in the system suggesting the average tracer velocity could  
250 be representative of the average particle velocity in the system. Increasing the number of tracers in the  
251 paddle mixer system does not influence the average velocity distribution. The data of PEPT with one  
252 tracer with those of DEM with one tracer provide a good agreement; however for normalised velocity  
253 of 0.7 and higher, the frequency distribution of DEM tracer was found to be higher than PEPT. One  
254 reason for this observation could be the differences in particle shape and size distribution for DEM  
255 and the experiment. The velocity for all particles in DEM shows a smooth distribution with a peak  
256 frequency of the velocity distribution lower than PEPT and DEM tracer. The velocity distribution data  
257 for the population of particles in DEM are based on a large number of particles which reduce the  
258 scatter and fluctuations. Potential explanations for the difference in the peak of the distribution could  
259 be attributed to the particle size differences and the sampling method: PEPT and DEM tracer analyses  
260 are based on data from only one particle within a discretised domain, while the DEM results consider  
261 the velocity profiles of the whole population of particles. When tracking a single tracer in DEM or  
262 PEPT, particle having zero velocity may not be detected, while the data for all particles shows that  
263 about 0.3% of particles are stationary.

264

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