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# Counterbalancing Needed to Avoid Bias in Side-By-Side Brightness Matching Tasks

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## Abstract

Spectral power distribution (SPD) is one of the variables that can be manipulated in lighting design. This article examines twenty previous studies which have investigated the effect of SPD on brightness using the side-by-side matching technique. Three sources of experimental bias are identified and are shown to be present in the majority of these studies, and hence must be considered to provide an unreliable estimate of the magnitude of the SPD effect on brightness. The first bias is associated with test participants' use of dimming control and two forms are apparent – a response contraction bias when the test is repeated at multiple reference illuminances and a conservative bias when the test is carried out at a single reference illuminance. The second bias is associated with the primary direction in which dimming must take place and the third bias is associated with the relative position of the stimuli within the apparatus.

## 1 Introduction

There is a renewed attempt to investigate SPD effects within the lighting community. IESNA has established committee RO17 to investigate effects of lamp spectral distribution and there were articles from five research groups at the 26th Session of the CIE in Beijing, 2007. This article presents evidence to aid in the identification of experimental procedures expected to produce reliable data.

This article presents a critical analysis of past research on the effect of spectral power distribution (SPD) on the perception on brightness. More specifically, our analysis focuses on studies that used side-by-side matching as the principal experimental methodology. In side-by-side matching, participants are presented with two adjacent stimuli and instructed to adjust the illuminance of one until both appear equal according to a prescribed criterion. At the point of subjective equality (PSE) the stimulus magnitudes are recorded, in units of either illuminance or luminance, and the ratio is used to quantify the visual effect. A variety of visual equality criteria have been used in previous matching studies, including equal brightness, equal appearance, and equal clarity, but there appears to be little effect on the PSE (Fotios & Gado 2005) and hence this article is phrased in terms of brightness.

At photopic levels twelve studies have used stimuli of large size, such as illuminated rooms or booths (Aston & Bellchambers 1969; Bellchambers & Godby 1972; Boyce 1977; Fotios & Levermore 1995, 1997; Hu, Houser & Tiller 2006<sup>†</sup>; Lemons & Robinson 1976; Levermore 1994; Thornton, Chen, Morton & Rachko 1980; Thornton & Chen 1978; Worthey 1985; Zheleznikova & Myasoedova 1995) and six studies have used stimuli of small size, such as light patches subtending a visual arc of up to ten degrees at the eye (Alman 1977; Alman, Breton & Barbour 1983; Booker 1978; Harrington 1954; Hashimoto & Nayatani 1994; Houser & Hu 2004). Two studies have been carried out at mesopic levels typical of street lighting at night time (Fotios & Cheal 2007a; Randhawa 1997). While the list is not assumed to be exhaustive, it does extend those presented in a recent review of the subject (Fotios 2001a). The authors in all 20 studies reported that light source SPD had significant affect upon the illuminance ratio at equal brightness, and thus this collection appears to be a strong body of evidence. However, as will be shown, it is prudent to filter this body of work by considering the quality of the experiments, and to re-evaluate the confidence that can be placed in the conclusions for each of these studies.

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<sup>†</sup> This study is described in greater detail, along with other methods for judging brightness, in Houser, Tiller & Hu, 2003.

The assessment of brightness is a psychophysical scaling task that requires the test participant to make sensory responses to stimuli. These assessment tasks can usually be allocated into one of three types [Gescheider 1988; Poulton 1989]:

- (i) *Discrimination*: the participant is required to make simple ordinal discrimination judgements of stimuli.
- (ii) *Adjustment*: the participant is required to adjust stimuli toward a given sensation. This group includes the side-by-side matching task.
- (iii) *Category Rating*: the participant is required to assign numbers to stimuli that represent the sensation magnitude.

Poulton places matching and discrimination tasks joint first in his order of preference because they suffer from fewer source of bias than does category rating (Poulton 1989). Although matching is preferable to other psychophysical methods, it is nonetheless imperfect. Brightness is a highly subjective perception that has unfamiliar units, and this can lead to bias (Poulton 1989).

Bias is a change in the value of a psychophysically defined entity such as a PSE that accompanies a change in task variables or in the set of test stimuli used: it can be due to either sensory variables such as light/dark, chromatic or contrast adaptation, to decision variables such as shifts in the subject's psychophysical criterion, or to a combination of both (Teller, Pereverzeva & Civan 2003). If bias changes the PSE then there will be a distortion in the magnitude of the effect under study. For example, if the methodology used to determine the illuminance ratio at equal brightness is biased, then the magnitude of lamp SPD effects will be misstated.

This article presents evidence for three biases within the side-by-side brightness matching task. The first is a response contraction bias associated with the application of dimming<sup>‡</sup> to the observed stimuli. The second bias is associated with the primary direction in which dimming must take place. The third bias is associated with the relative position of the stimuli within the apparatus. Hence three stages of counterbalancing are required to remove the effect of biases from the experimental results, these being application of dimming control to both stimuli in a pair, that the initial illuminance of the variable source starts at both higher and lower levels than the reference, and that the stimuli occupy the two available locations (e.g. left and

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<sup>‡</sup> The term *dimming* is used to describe the procedure of manually adjusting the amount of light. The direction of this adjustment may be to increase or decrease the amount of light.

right). Complete counterbalancing within subjects thus demands eight trials per pair of stimuli.

This article suggests that 10 of the 20 previous studies (Alman 1977; Alman, Breton & Barbour 1983; Aston & Bellchambers 1969; Bellchambers & Godby 1972; Booker 1978; Hashimoto & Nayatani 1994; Houser & Hu 2004; Randhawa 1997; Worthey 1985; Zheleznikova & Myasoedova 1995) contain bias which has not been countered and thus do not provide reliable evidence of the magnitude of the SPD effect on brightness; four studies present insufficient data to know whether bias has been countered (Harrington 1954; Lemons & Robinson 1976; Levermore 1994; Thornton Chen Morton & Rachko 1980). This is a critical finding because some of these studies (e.g. Alman 1977; Aston & Bellchambers 1969; Bellchambers & Godby 1972) are extensively referenced in the literature. Thus the 'strong body of evidence' is reduced to only six studies which provide reliable evidence of the magnitude (in illuminance units) of the SPD effect on brightness in the side-by-side matching task (Boyce 1977; Fotios & Levermore 1995, 1997; Fotios & Cheal 2007a; Hu Houser & Tiller 2006; Thornton & Chen 1978). Whilst this article is directed toward comparing lighting of different SPD, the findings are applicable to psychophysical tests employed to investigate other attributes of lighting.

## **2 Application of Dimming**

In the typical matching task, the observer is given dimming control over one of the two stimuli. Findings from previous studies demonstrate that if the dimming mechanism is not applied with equal frequencies to both of the stimuli then there will be bias in the results. Two different biases have been found, a response contraction bias if the task is carried out at a range of reference illuminances, and a conservative bias if the task is carried out at a single reference illuminance (Fotios & Cheal 2007b; Fotios 2001b).

### **2.1 Response contraction bias**

If the visual match is made at several different reference illuminances, a response contraction toward the center of the range of stimulus magnitudes is expected (Fotios & Cheal 2007b). Following Poulton (Poulton 1989) this is labeled a response contraction bias, as the range of responses tends to converge toward the center of the stimulus range, but it may alternatively be considered a sequential effect because previous stimuli apparently become an additional reference magnitude against which the next variable stimulus is judged.

A response contraction is commonly found in psychophysical magnitude estimation tasks – a natural tendency to shift the sensation in memory toward the middle of a scale of intensities; participants performing estimation tasks are not certain about the true values of the stimuli and therefore keep their estimates well within the boundaries (or ranges) of stimulus values (Jou et al 2004). It would be expected, for example, when estimating the brightness of a single stimulus presented at a range of luminances. The brightness of the low luminance stimuli will be overestimated whilst brightness of the high luminance stimuli will be underestimated. It was not expected in side-by-side comparisons where the reference and variable stimuli are simultaneously visible, for example it is not listed as an expected bias in Poulton (Poulton 1989, Table 3.4, p61). Consider a reference stimulus that is set to three illuminances for successive tests, e.g. 300, 400, and 500 lux. Matches made to the 300 lux reference will be biased upwards toward 400 lux, matches made to the 500 lux reference will be biased downwards toward 400 lux, and matches made at the middle reference illuminance will not be significantly biased.

Evidence for a response contraction bias in the side-by-side visual matching task was initially found in post-hoc analysis of null condition data and was then confirmed in the between-lamps data (Fotios & Cheal 2007b). The null condition tests used 18 color-normal participants, each making eight brightness matches between two side-by-side booths at each of three reference illuminances (2.0, 7.5, and 15.0 lux) . The eight trials were carried out in anticipation of bias to enable complete counterbalancing of stimulus position (left and right booth), dimming application (to both of the stimuli) and the direction of dimming (initial illuminance of variable source either higher or lower than illuminance of reference source). Identical lamps were used in each booth.

The null condition data (Table 1) is presented as the ratio of the illuminances of the variable and reference stimuli. A mean illuminance ratio of unity would suggest no significant bias, and this was found at the middle of the three reference illuminances. At the lower reference illuminance, the illuminance ratio is significantly greater than unity, indicating the variable source tended to be set to a higher illuminance than the reference – a bias toward the middle of the reference illuminance range. At the higher reference illuminance, the illuminance ratio is significantly smaller than unity, indicating the variable source tended to be set to a lower illuminance than the reference, again a bias toward the middle of the range of reference illuminances. If

this were an apparatus based bias, such as a positional bias (see below) the direction of this error would be the same at all three reference illuminances – that it isn't suggests it is caused by the range of reference illuminances. The direction of the error is toward the middle of the range of reference stimulus magnitudes, and hence was identified as a response contraction bias.

[Table 1]

The results of Fotios & Cheal's (Fotios & Cheal 2007a) between-lamps tests (Table 2) also suggested a response contraction bias. In these tests, three different light sources (CFL, MH1, MH2) were matched with a single reference source (HPS). This was carried out by 21 color-normal participants, each making four trials for each of three reference illuminances (2.0, 7.5, and 15.0 lux) and the three lamp pairs. The four trials were used to counterbalance dimming application and initial illuminance of the variable stimulus – stimulus position was balanced between subjects as the null condition tests suggested negligible bias between the left and right-hand sides. In Table 2 the results are broken down according to the application of dimming. It can be seen that at the lower reference illuminance, the illuminance of the variable stimulus is biased toward a higher level, whilst at the higher reference illuminance the illuminance of the variable stimulus is biased toward a lower level – a contraction of the response range. These differences are significant according to the t-test.

[Table 2]

The effect of a response contraction bias is small but statistically significant, and sufficient to affect whether a hypothesis of equality is accepted or rejected (Fotios & Cheal 2007b). Fotios & Cheal used their null condition data as a correction factor to the main results: that this correction did not significantly change the mean results suggests that applying the dimming control with equal frequency to the two stimuli was successful in countering the bias.

Fotios & Cheal suggested that where a number of different reference illuminances are used, the range appears to become apparent to the observer, as does the approximate center of the range of responses, and this becomes a secondary reference toward which responses are biased (Fotios & Cheal 2007b). This is confirmed by Jou et al (Jou et al 2004) who suggested that participants are able to

compute some summary statistic about the stimuli, such as a measure of central tendency, and this is used as a basis for modifying responses.

A response contraction bias can also be seen in the null condition data of Tiller & Veitch (Tiller & Veitch 1995). This study used side-by-side brightness matching to compare lighting of identical SPD but different spatial distribution (uniform and non-uniform) at three different reference illuminances, 300 lux, 500 lux and 700 lux. In the null condition trials, rooms of identical SPD and spatial distribution were matched. The results are shown in Table 3. Tiller & Veitch report the mean illuminance required to match the reference interior. At the lower reference illuminance (300 lux) the mean illuminance of the adjusted lighting is slightly higher than the reference, whereas at the higher reference illuminances (500 lux and 700 lux) the mean illuminances of the adjusted lighting are lower than the references.

To analyze whether the differences are significant requires variance data. The standard error of the mean ( $SE_M$ ) can be estimated at  $\pm 7$  lux from graphical illustration of the results (Figure 2 in Tiller & Veitch). Standard deviation ( $\sigma$ ) can then be found using  $\sigma = SE_M \cdot N^{1/2}$  (Field 2005). Each condition (luminance distribution and illuminance) has a sample of size  $n=120$  (30 test participants x 4 trials), which gives a standard deviation of  $\sigma=77$  lux. The  $t$ -test is applied to determine whether the mean illuminance of the comparison room is the same as the nominal illuminance of the reference room; the difference is significant at 500 and 700 lux ( $p<0.01$ ) but not at 300 lux.

[Table 3]

Whilst no additional studies have been found which can provide further clarification of response contraction bias in side-by-side matching tasks carried out at multiple stimulus magnitudes, the results from two previous studies (Teller, Pereverzeva & Civan 2003; Jou et al 2004) provide further demonstration that using multiple stimulus ranges will bias participant behavior.

Teller, Pereverzeva & Civan sought brightness judgments of red and blue targets (subtending two degrees visual arc) presented on a white monitor screen (Teller, Pereverzeva & Civan 2003). For each color, a range of targets varying in luminance were presented in random order, and observers reported whether the target was



brighter or dimmer than the surround. Three ranges of target luminance were used in successive trials – for the red target these ranges had mid-point values of -0.6, -0.3 and 0.1 log luminance relative to the white surround. Typically 11 target stimuli were used in each range, increasing in steps of 0.05 log units. Seven test participants were used, each making 20 judgments of relative brightness per condition. It was found that a stimulus judged *brighter* than the surround on 100% of trials with the target range of low mid-point luminance was judged *dimmer* than the surround on 100% of trials with a high mid-point range of luminances. Thus, the stimulus range affected the brightness judgment, despite their being no change in the reference stimulus. For the red target, a change in mid-point luminance of 0.7 log units (-0.6 to 0.1 log luminance relative to white surround) caused a mean PSE shift of 0.4 log units. For the blue target, a change in mid-point luminance of 0.8 log units (-0.9 to -0.1 log luminance relative to white surround) caused a mean PSE shift of 0.6 log units. These findings were subsequently repeated by Pereverzeva & Teller (Pereverzeva & Teller, 2005) who also adapted the test procedure in order to identify the underlying mechanisms.

In the study of Jou et al (Jou et al, 2004) participants estimated alphabetic interval distances between two letters for different levels of inter-letter distances. From all possible letter pairs in the alphabet there are 325 distinct pairs. These were used in three groups; *low*, having 1 to 13 inter-letter distances between letter pairs; *middle*, having 9 to 21 inter-letter distances; and *high*, having 14 to 25 inter-letter distances. In trials, letter pairs from within one of these groups were presented to observers whose task was to estimate the distance between the letters without counting. The results reveal a systematic distortion in the form of a centering bias within all three separate groups, with inter-letter distances at the lower end of the range being overestimated and inter-letter distances at the higher end of the range being underestimated.

The range of inter-letter distances caused a difference in estimates of inter-letter distance as can be seen by comparing inter-letter distances common to two ranges. Inter-letter distances of 9 to 13 were common to the low and middle range groups; in the low group these inter-letter distances are under-estimated and in the middle group they are over-estimated. Inter-letter distances of 14 and 15 were common to the middle and high range groups; in the middle group these inter-letter distances are under-estimated and in the high group they are over-estimated.

## **2.2 Conservative adjustment bias**

A second potential bias associated with the application of dimming occurs when side-by-side matching tests are carried out at only one reference illuminance. This was previously reported by Fotios (Fotios, 2001b) who found from analysis of null condition data that the stimulus over which participants have dimming control is set to an illuminance below that of the reference stimulus. The bias is also evident in more recent experimental data (Fotios & Gado, 2005; Houser & Hu, 2004). This may be considered to be a conservative bias, reflecting the general conservative tendency that is found in all quantitative judgments (Poulton, 1989). Although LaBoeuf & Shafir might argue against such an explanation because participants were able to adjust up and down, repeatedly, and with impunity (LaBoeuf & Shafir, 2006) the effect is clearly evident in experimental results. As with the response contraction bias the effect is small but statistically significant. A mean illuminance ratio (constant/variable) of 1.098 was determined from the results of 80 null condition trials (Fotios & Gado, 2005), similar to that reported previously (1.058) by Fotios (Fotios, 2001b).

Houser, Tiller & Hu (Houser, Tiller & Hu, 2003) carried out brightness matching using side-by-side rooms at one reference illuminance (300 lux) and their null condition data exhibits a bias with the application of dimming. Null condition trials using identical lamps in both rooms were carried out by 32 observers, each providing two responses under the same conditions. The mean illuminance ratio at equal brightness (fixed/variable) is 0.877 (std dev = 0.083, n=63) which shows that on average the variable stimulus was set to a higher illuminance than the fixed reference. This is a significant departure from unity ( $p < 0.01$ ,  $t$ -test). However, this effect is in the opposite direction to that reported by Fotios (Fotios, 2001b) and Fotios & Gado (Fotios & Gado, 2005). This difference may be because their null condition trials were confounded by simultaneous positional bias (the lamp to which dimming was applied was always in the left-hand room) and directional bias (the variable stimulus always demanded dimming up from the start level of 150 lux toward the comparison level of 300 lux). Results of the between-lamps tests carried out by Houser, Tiller & Hu suggest a similar trend, that on average the variable lamp was set to a slightly higher illuminance than the fixed lamp, but this is not a significant difference.

## **2.3 Dimming application - Summary**

There is evidence to suspect significant bias in the act of dimming the illuminance of a visual stimulus during a side-by-side matching task. If dimming is applied to only one of a pair of matched stimuli, this can significantly affect the PSE. The bias can be countered by applying dimming to both stimuli in the pair for an equal number of trials.

There are variants in the type of dimming and the method used to apply dimming. Fotios & Levermore (Fotios & Levermore, 1997) used electronic dimming applied to fluorescent lamps and this was operated directly by the test participants. Electronic dimming can affect lamp SPD and hence Fotios & Cheal (Fotios & Cheal, 2007a) used a mechanical dimming device, an iris in the light transport tube, to control light from high intensity discharge lamps, and this was controlled directly by the participants. Gescheider suggested a shortcoming of the adjustment method results from giving the observer control of the stimulus, as this makes it difficult to maintain constant conditions during threshold measurement (Gescheider, 1997). Hence Houser, Tiller & Hu (Houser, Tiller & Hu, 2003) used electronic dimming of fluorescent lamps, but this was done by the experimenter and test participants instructed the experimenter to adjust the lighting by saying “higher” or “lower” for the variable room (the other room being fixed). Further analysis is needed of the effects of different methods of dimming control.

### **3 Initial Illuminance of Variable Stimulus**

In the side-by-side matching task, the stimulus to which dimming is applied can be set by the experimenter to an initial illuminance either higher or lower than that of the reference stimulus. The observer’s task is thus either to primarily increase the brightness or primarily to decrease the brightness. This directional quality may have significant effect on the results of the brightness matching task.

Consider the method of limits for determining a difference threshold. Two stimuli are presented, the standard and comparison, and the comparison stimulus is set initially to a magnitude greater or smaller than the standard. The test participant reports whether the comparison stimulus is different to or equal to the standard, and if different the magnitude of the comparison is changed by a small amount in the direction of the standard. This method hence employs a series of ascending or descending stimuli, and the point at which the comparison is reported to be equal with the standard is different in each case, tending to be a higher magnitude with the descending series from a high initial magnitude and tending to be a lower magnitude

with the ascending series from a low initial magnitude. The difference between these two points of equality, the upper and lower limens, is the interval of uncertainty, and the point of subjective equality will be the mid-point of this range (Geschider, 1997). This effect may be related to the state of visual adaptation or to the general tendency to compare things against recent memory, with recent memory serving as a benchmark.

Therefore, when a single visual stimulus is set by test participants to an absolute illuminance, in the absence of a simultaneous reference, then it is expected that a higher level will be set when starting from an initially high illuminance than when starting from an initially low illuminance. This can be seen in the results of tests carried out by Ray who asked observers to adjust the illuminance of lighting to a level *clear and comfortable to read at* (Ray, 1989). This was carried out under two lamps, clear-glass tungsten filament (GLS) and blue-glass tungsten filament (BG), and 18 observers repeated this twice for each lamp, once each starting from a high illuminance and a low illuminance. The results are shown in Table 4. It can be seen that the lamps are set to a higher illuminance when the initial illuminance is high than when the initial illuminance is low – these differences are significant ( $p < 0.05$ ,  $t$ -test).

[Table 4]

It is expected that different starting points will yield different estimates, which are biased toward the initial values (Tversky & Kahneman 1974). This may be due to anchoring, with the initial illuminance of the variable stimulus modifying the perceived illuminance of the reference stimulus. For the side-by-side matching task, this would mean a trend for the variable stimulus to be set to a higher level at the matched condition when starting from a high initial illuminance than when starting from a low initial illuminance. Whilst this trend can be seen in the results from two studies (Fotios & Cheal, 2007a; Fotios & Levermore, 1997) it is frequently not a significant trend, and a significant effect in the opposite effect has been found (Houser, Tiller & Hu, 2003).

Table 5 shows the results of null condition tests carried out at three reference illuminances, broken down according to whether the initial illuminance was set by the experimenter to be either above or below that of the comparison (Fotios & Cheal, 2007a). There is a trend for the illuminance ratio to be higher when the variable lamp starts from the higher illuminance, but application of the two-sample  $t$ -test suggests

the difference is significant only at the lower of the three reference illuminances ( $p < 0.01$ , *t*-test).

[Table 5]

Table 6 shows the results of side-by-side matching tests which used separate warm white (WW) fluorescent lamps to illuminate each booth (Fotios & Levermore, 1997). Each booth had individual electric dimming control. Each of fifteen test participants repeated the matching task three times. The dimming control dials were set by the experimenter to one of three positions on their range prior to each trial, these being high-middle, low-middle and low-high for the left and right booths respectively. Observers were given the dimming controller for both booths, and had a free choice as to whether only one, or both, of the booths were adjusted. The trend is again for the booth initially set to the higher illuminance to end up at the slightly higher illuminance, although the differences in illuminance are not significant (Wilcoxon Signed Ranks; the results were not found to be normally distributed), although it is not known whether this is because the higher illuminance stimulus was insufficiently dimmed downwards or the lower illuminance stimulus was dimmed upwards too far.

[Table 6]

The results from a further study (Houser, Tiller & Hu, 2003) revealed the opposite conclusion, that in a side-by-side brightness matching task when the adjusted stimulus is initially set to a higher illuminance it is set, on average, to a lower illuminance at the matched condition than when it starts from an initial low illuminance. In the between-lamps trials (VT vs. CV lamps) the fixed stimulus was set to 300 lux whilst the variable stimulus was set to either 150 lux or 450 lux before dimming was applied. This was counterbalanced within trials. The results are shown in Table 7. The mean illuminance ratio at equal brightness is significantly affected by the direction of dimming ( $p < 0.01$ ). When the initial illuminance was higher (450 lux) it is set on average to a lower level than when the initial illuminance was lower (150 lux). A difference between this work and the two studies discussed above is that dimming was carried out by the experimenter, under orders from the test participant, rather than by the test participant directly, but this is not believed to explain the difference in results.

[Table 7]

Analysis of previous work suggests that the initial illuminance of the variable stimulus, being either greater than or less than the reference stimulus, can significantly affect the PSE in the matching task. Although the evidence is not conclusive, with trends found in both directions, it is sufficient to warrant the precaution of counterbalancing the initial illuminance of the variable stimulus.

#### **4 Positional Bias**

In the side-by-side matching task, the variable and reference stimuli will occupy the left-hand side (LHS) or right-hand side (RHS) of the visual field. Similarly, if a horizontal border is used, there are top and bottom fields. Poulton (Poulton, 1977) comments that a stimulus range effect can occur when the observer knows which stimulus of a pair is the standard, for example the one which is always presented on the left, and that when the observer knows which stimulus is the standard he/she tends to neglect it after a while, and instead judges each stimulus against the range of stimuli presented. Data from previous lighting studies demonstrates a potential bias caused by the position in which a stimulus is presented.

Thornton & Chen (Thornton & Chen, 1978) used side-by-side matching to compare the visual clarity of lamps of different SPD. Their lamp pairs included four null conditions, the same SPD being presented in both sides, for which an illuminance ratio (RHS/LHS) of unity would be expected at equal clarity if there were no bias. Subsequent analysis (Fotios, 2001a) of these null condition results suggested a mean illuminance ratio (RHS/LHS) of 1.145 at equal clarity, although there are insufficient data to determine whether this is a statistically significant departure from unity.

Houser, Tiller & Hu also employed side-by-side matching to compare the brightness of lighting from lamps of different SPD (Houser, Tiller & Hu, 2003). In null condition trials carried out using VT65 lamps in both rooms, the mean illuminance ratio (LHS/RHS) at equal brightness is 1.15 (std dev = 0.106, n=63) which is a significant departure from unity ( $p < 0.01$ ,  $t$ -test) and suggests a significant positional bias. These null condition tests are however confounded by a simultaneous bias in the application of dimming - dimming was only applied to the left-hand lamp, and always demanded dimming up from the initial level of 150 lux toward the comparison level of 300 lux. A positional bias can be found within their between-lamps trials although this was counterbalanced. On average, the LHS was set to a higher illuminance

(310.7 lux) than the RHS (298.4 lux). At equal brightness, the mean illuminance ratio (LHS/RHS) is 1.049 (std dev = 0.12, n=1024) which is a significant departure from unity ( $p < 0.01$ ,  $t$ -test).

These two studies (Houser, Tiller & Hu, 2003, Thornton & Chen, 1978) presented large interior spaces. No matter how hard one tries to make two rooms or booths identical there are always small differences. It is possible that the bias is caused by experimental effects such as dissimilarities in the spatial distribution of luminance or the location of the photometric measurement, variables which can be difficult to match precisely in large spaces. A positional bias has also been reported when using smaller fields; Kinney (Kinney, 1955) comments upon a subjective positional bias, although without numerical data. This was an observer who consistently reported the top half of a horizontally split field to be brighter than the bottom half, even when the top and bottom stimuli were reversed.

Some studies using side-by-side stimuli have tested for this bias but did not find a statistically significant effect (Fotios & Cheal, 2007a; Boyce 1977). Hence, although a significant positional bias must be suspected when using techniques where two side-by-side stimuli are compared, it is not a certainty, and this can be determined if there are either sufficient quantitative data or that the stimuli locations were counterbalanced. To generate reliable data the two lamps being compared should each be used to illuminate the left-hand and right-hand spaces (or top and bottom) for an equal number of trials.

## **5 Unreliable Data**

From the above discussions it is apparent that for the side-by-side matching task to generate reliable data the experimental design must consider effects of dimming application, dimming direction, and stimulus position.

In some previous studies within the lighting literature, the application of dimming and stimulus position were not counterbalanced, and in the absence of null condition data to quantify the effect, the results must be considered unreliable. For example, Table 8 shows the results from Bellchambers' two studies (Aston & Bellchambers, 1969; Bellchambers & Godby, 1972), which used side-by-side booths and rooms. In these, dimming was applied to only one lamp in the pair, this being the Kolor-rite lamp, and this was always in the left-hand side. The results show that the Kolor-rite lamp is set to a lower median illuminance than the comparison lamps. This could be re-written

as the *variable* lamp is set to a lower median illuminance, or the *left-hand* lamp is set to a lower median illuminance, and can hence be at least partially attributed to effects other than SPD.

[Table 8]

An estimate can be made of the cumulative effect of the three biases based on null condition data described above. For the bias associated with the application of dimming, the results from Tiller & Veitch at 700 lux suggest a bias magnitude of 1.09 (Tiller & Veitch, 1995). For the effect of dimming direction, the results of Fotios & Levermore suggest an effect of magnitude 1.08 can be expected (Fotios & Levermore, 1997). For the positional bias, analysis of data from Thornton & Chen suggested an effect of magnitude 1.145 (Thornton & Chen, 1978; Fotios, 2001a) and data from Houser, Tiller & Hu suggests a ratio of 1.15 (Houser, Tiller & Hu, 2003). The product of these is 1.35, the bias expected assuming the effects are accumulative. In a test with incomplete counterbalancing it is possible that some biases would cancel out others but that would be fortuitous. The ratio of illuminance of the Kolor-rite lamp to the median illuminance of the test lamps in Bellchamber's two studies ranges from 0.54 to 0.93. Hence, whilst bias is suspected, it does not explain all the results. An effect of SPD is demonstrated but it is not possible to determine what the size of this effect is because of the unknown amount attributed to bias.

Worthey (Worthey, 1985) used side-by-side booths to demonstrate that the visual clarity response is due to the distinctness of borders involving red-green contrasts. The booths were separately lit by different light sources, a cool white fluorescent (CW) in the left-hand booth and a prime-color cool white fluorescent (PCW) in the right-hand booth. Neither lamp position nor dimming application were counterbalanced in this study. Table 9 shows the seven experimental steps followed by test participants. Of these seven steps, the clarity matches with identical color papers in each booth (steps 3 and 6) were the focus of the experiment, the other steps being control conditions. In each step a particular combination of colored papers and visual equality criteria were used, and dimming was applied to one booth in order to match them for the given visual criteria. This dimming was, however, applied to just one interior, and hence to just one lamp, in each step. Worthey reports the mean illuminance ratio from ten observers each making four trials as



shown in Table 9. In each step it is the stimulus to which dimming has been applied that has been set to the lower illuminance.

[Table 9]

There are further matching studies which have not applied sufficient counterbalancing and these also tend to reveal systematic bias with dimming application and stimulus position. These studies demonstrate that the biases are widespread and apparent across a range of viewing conditions and visual tasks.

- **Alman, 1977:** This study employed brightness matching with a two-degree field, using a reference source that was always located on the right-hand side of the field and dimming was applied only to the reference source (Alman, 1977). Of 26 stimulus pairs, the mean luminance ratios are all in the same direction (greater than 1.0) except for only one (luminance ratio equal to 1.0) and there are no null condition data by which to evaluate the causes of bias.
- **Alman, Breton & Barbour, 1983:** This study used side-by-side matching with a two-degree bipartite field (Alman, Breton & Barbour, 1983). Dimming was applied only to the test stimulus which was placed continually in the right-hand side. In 35 of the 38 cases (filters of different color) the adjusted lamp is set to a lower luminance than the fixed reference and there are no null condition data.
- **Booker, 1978;** This study used side-by-side comparisons of alpha-numeric stimuli (the letter H) of approximate size one degree (Booker, 1978). The three test stimuli were always located on the right-hand side, the reference source was always on the left-hand side, and dimming was applied only to the reference source. All three results are in the same direction, having a luminance ratio (variable/fixed) of  $>1.0$  and there are no null condition data to check this.
- **Hashimoto & Nayatani, 1994:** This study used side-by-side booths to match the contrast of four-color samples under different sources of light using haploscopic presentation (Hashimoto & Nayatani, 1994). The reference source was always on the left-hand side and was maintained at 1000 lux. The eight test lamps were used to illuminate the right-hand booth, and dimming was applied only to these lamps. For seven of the eight test lamps, the booth was set to a lower mean illuminance than the reference, ranging from 445 lux to 994 lux, the other result being 1049 lux. Again, this is a trend for the adjusted lamp to be set to the lower illuminance and there are no null condition data.

- **Randhawa, 1997:** This study used side-by-side booths to compare different lamps (Randhawa, 1997). In all of the comparisons dimming was applied to only one of the two lamps and this was always the same lamp and always in the right-hand booth. In 17 of the 18 conditions (6 lamp combinations and 3 visual equality criteria) it is the booth to which dimming was applied that was set to the lower illuminance.
- **Zheleznikova & Myasoedova, 1995:** This study used sequential matching rather than side-by-side, in which the illuminance of the second room was dimmed to match the brightness of the preceding room, identical other than type of light source (Zheleznikova & Myasoedova, 1995). Two different lamps were compared, and these were always observed in the same order. Dimming was applied to lighting in only one room and hence only to one of the lamps, the fluorescent. They found that the room lit by the fluorescent lighting required approximately 15% less illuminance than the room lit by the sodium lighting for equal brightness. It is again seen that the source to which dimming has been applied is that which was set to the lower illuminance and there are no null condition data.

Houser & Hu used a matching task but this was the Maxwell method of color-matching rather than a brightness match (Houser & Hu, 2004). This study used a ten degree horizontally bisected bipartite field with the lower half lit by 'daylight' fluorescent lamplight and the upper half lit by one of two tri-band primary sets – a positional bias. Each of the three components of the primary sets was created using incandescent lamps and narrow-band filters and these were individually adjustable. The method of dimming was different in the upper and lower fields. In the upper field subjects had independent control of the tri-band components, which were adjusted individually using rotary dimmers. The subject adjusted the lower field with a toggle switch that moved the daylight fluorescent lamps in and out of an integrating chamber. This method allowed the subjects to make complete visual matches such that the upper and lower fields were visually identical in both color and brightness, despite having different spectral power distributions. *Visually* this is a simpler task than brightness matching because the subject is not expected to ignore color differences whilst making the match, but it is a more difficult task *physically* because there are four separate "lights" that the subject can adjust. For both of the tri-band primary sets, the mean luminance ratio (daylight/triband) at equal brightness was greater than unity, although a significant departure in only one case, showing a tendency for the upper field to be set to a lower luminance than the lower field. This

result could be attributed to the differences in spectral power distribution, which was the main effect under study, but this is confounded with the positional bias. There are no null condition data.

Fotios & Levermore used side-by-side booths to match lighting from standard tungsten filament lamps (GLS) and similar lamps in which the glass envelope has a blue coating, so-called daylight simulating lamps (Fotios & Levermore, 1995). Lamp position and dimming direction were counterbalanced but dimming was applied only to the GLS lamps, hence a potential bias – this was however corrected in later work using null condition data (Fotios & Levermore, 1997).

An objective of this article is to highlight the need for null condition trials and for counterbalancing. The benefits can be seen in the results from Houser, Tiller & Hu (Houser, Tiller & Hu, 2003). In their null condition trials they did not apply counterbalancing - the lamp to which dimming was applied was always in the left-hand room and the variable stimulus always demanded dimming upwards from the initial illuminance of 150 lux toward the comparison illuminance of 300 lux. The mean illuminance ratio at equal brightness (fixed/variable) was 0.877 - on average the variable stimulus (or, alternatively, the left-hand stimulus) was set to a higher illuminance than the fixed (or right-hand) stimulus, and this is a significant effect ( $p < 0.01$ ,  $t$ -test). The bias could have been due to some combination of position, and/or direction, and/or the application of dimming. In their between-lamps tests they did counterbalance lamp position, dimming direction and dimming application. Whilst this did not eliminate the biases it made it possible to disengage them from the SPD effects, hence to estimate their magnitude.

The counterbalancing discussed in this article is not the only consideration to be made when using side-by-side matching. The results may be affected by contrast adaptation and by the method of dimming employed – whether it affects the spectral and spatial distribution of light and whether the control device provides the participant with unintentional cues. The side-by-side presentation means that participants' vision will be chromatically adapted to the mixed SPD of the two stimuli rather than to the SPD of one particular light source: this is not a dilemma, but rather awareness is needed when considering analysis and application of the results.

## **6 Conclusions**

This article has highlighted three causes for potential bias in side-by-side visual matching tasks - a positional bias, a bias associated with the application of dimming, and a bias with the direction of dimming. These biases can be counterbalanced, demanding that in a test comparing two stimuli dimming is applied to both stimuli, the stimuli are located in both positions, and the variable stimulus starts at an illuminance higher and lower than the reference stimulus. The implication for experimental design is that to examine one stimulus pair requires that participants carry out eight trials, extending the duration of testing.

The existence of these biases means that several previous studies using the matching task to identify the effect of lamp SPD on visual perception must be considered unreliable because they did not carry out sufficient counterbalancing. This conclusion is drawn with the caveat that it is important to consider the magnitude of the between-lamps effect with respect to the magnitude of the expected bias – it may be that the work does demonstrate an effect of SPD but the size of this effect cannot be reliably quantified.

This work highlights the benefit of carrying out null condition trials. Unfortunately, this means of validating experimental apparatus is absent from many studies in the lighting literature. Null condition data can be used to correct non-null condition data which did not employ sufficient counterbalancing, but this should be considered a last resort: the preferred approach is to employ counterbalancing and use null condition data as a back-up validation.

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Reference illuminance (lux)	<b>2.0</b>	<b>7.5</b>	<b>15.0</b>
Mean illuminance ratio (variable/reference)	1.05	0.99	0.97
Std dev	0.13	0.10	0.08
n	144	144	144
Departure from unity (student's t-test)	<b>p&lt;0.01</b>	n.s.	<b>p&lt;0.01</b>

**Table 1**

Results of null condition tests using a side-by-side brightness matching task to compare lamps of identical SPD (Fotios & Cheal, 2007b). The illuminance ratios suggest the illuminance to which the variable stimulus is set is biased toward the middle of the range of reference illuminances.

Test Lamp	<b>CFL</b>			<b>MH1</b>			<b>MH2</b>			
	Reference illuminance (lux)	2.0	7.5	15.0	2.0	7.5	15.0	2.0	7.5	15.0
<b>Test lamp is dimmed</b>										
Mean illum. ratio (test/HPS)	0.737	0.699	0.657	0.793	0.723	0.685	0.718	0.697	0.645	
Std dev	0.154	0.129	0.124	0.184	0.141	0.148	0.199	0.147	0.173	
n	42	42	42	42	42	42	42	42	42	
<b>HPS lamp is dimmed</b>										
Mean illum. ratio (test /HPS)	0.654	0.737	0.810	0.669	0.744	0.763	0.642	0.752	0.837	
Std dev	0.152	0.105	0.179	0.142	0.179	0.164	0.188	0.180	0.184	
n	42	42	42	42	42	42	42	42	42	
Illuminance of adjusted booth relative to overall average.*	H	L	L	H	L	L	H	L	L	
Difference between mean illuminance ratios	<b>p&lt;0.05</b>	n.s.	<b>p&lt;0.01</b>	<b>p&lt;0.01</b>	n.s.	<b>p&lt;0.05</b>	<b>**p&lt;0.05</b>	n.s.	<b>p&lt;0.01</b>	

**Table 2**

Results of between-lamp tests using a side-by-side brightness matching task (Fotios & Cheal, 2007b). The results are broken down according to the application of dimming to either the reference lamp (HPS) or the Test lamp (CFL, MH1, MH2). Comparison of the illuminance ratios demonstrates that the illuminance of the variable stimulus is biased toward a higher level at the lower reference illuminance, and to a lower level at the higher reference illuminance.

\* H = Illuminance of adjusted booth is **higher** than overall average  
L = Illuminance of adjusted booth is **lower** than overall average lower

\*\* This significance level is found using the one-tailed t-test: it is not significant if the two-tailed test is applied.

Illuminance (lux) in reference room	Mean illuminance (lux) for equivalent brightness in the comparison room	Analysis of difference	
		<i>student's t</i>	Difference
<b>Uniform-Uniform comparison</b>			
300	310	-1.42	ns
500	475	3.56	p<0.01
700	642	8.25	p<0.01
<b>Nonuniform-Nonuniform comparison</b>			
300	302	-0.28	ns
500	471	4.13	p<0.01
700	642	8.25	p<0.01

**Table 3**

Results of null condition tests using a side-by-side brightness matching task to compare lamps of identical SPD and spatial distribution (Tiller & Veitch, 1995). The mean illuminance of the variable stimulus is biased toward the middle of the stimulus range. In each case, standard deviation estimated at  $\sigma=77$  lux and the sample size is  $n=120$ .

Lamp	<b>Standard GLS lamp</b>		<b>GLS lamp with blue glass bulb</b>	
	high	low	high	low
Initial illuminance of variable stimulus	high	low	high	low
Mean illuminance (lux) set " <i>clear and comfortable to read at</i> ".	1123	645	806	419
Std dev	482	505	513	375

**Table 4**

Mean illuminances of lamps set to a level "*clear and comfortable to read at*" (Ray, 1989). Note: unpublished undergraduate thesis, raw data analyzed by Fotios (Fotios 2001a).



Initial illuminance of adjusted lamp	Illuminance ratio (variable/fixed)	Reference illuminance (lux)		
		<b>2.0</b>	<b>7.5</b>	<b>15.0</b>
<b>Higher</b>	Mean	1.08	1.00	0.98
	Std dev	0.12	0.10	0.08
<b>Lower</b>	Mean	1.02	0.99	0.97
	Std dev	0.13	0.10	0.08
Difference between <i>higher</i> and <i>lower</i> mean illuminance ratios ( <i>t</i> -test)		<b>p&lt;0.01</b>	n.s.	n.s

**Table 5**

Results of brightness matching null condition tests, broken down according to the initial illuminance of the adjusted stimulus, an illuminance higher or lower than the illuminance of the reference stimulus (Fotios & Cheal, 2007a). In all cases, sample size  $n = 72$ .

Initial position of dimming control dial for the Left-Right booths	<b>high-mid</b>	<b>low-mid</b>	<b>low-high</b>
Mean illuminance ratio at equal brightness (LHS/RHS)	1.08	0.99	0.99
Standard deviation	0.161	0.083	0.066
Number of observations	15	15	15
Difference in illuminance between left and right booths (Wilcoxon Signed ranks)	ns ( $p=0.10$ )	ns ( $p=0.50$ )	ns ( $p=0.92$ )

**Table 6**

Results of null condition matching tests in which the dimming control dials applied to two stimuli were set to either a high, middle or low position prior to each trial (Fotios & Levermore, 1997). The stimulus set to the higher initial illuminance is, on average, maintained at the higher illuminance at equal brightness in all three cases, although the difference is not statistically significant.

Lamp to which dimming applied	Initial illuminance of variable lamp (lux)	Mean illuminance ratio (VT/CV)	std dev	Effect of initial illuminance (two sample t-test)
VT	150	1.084	0.126	p<0.01
	450	0.980	0.095	
CV	150	0.989	0.115	p<0.01
	450	1.056	0.127	

**Table 7**

Results of brightness matching tests broken down according to the initial illuminance of the variable stimulus (Houser, Tiller & Hu, 2003). In all cases n=256.

Study	Aston & Bellchambers (1969)			Bellchambers & Godby (1972)			
Test lamp	Daylight	Warm White	White	Daylight	Warm White	White	'D' Lamp
<b>Ref illum.</b>	<b><i>Median illuminance (lux) of Kolor-rite lamp</i></b>						
200 lux	170	130	145	155	170	160	185
400 lux	270	230	270	330	320	340	345
600 lux				465	475	480	500
800 lux	560	460	435				
<b>conclusion</b>	<b>Dimmed lamp in LHS has been set to lower illuminance</b>			<b>Dimmed lamp in LHS has been set to lower illuminance</b>			

**Table 8**

Results of Bellchambers' side-by-side matching studies (Aston & Bellchambers, 1969; Bellchambers & Godby, 1972). These data suggest presence of the positional bias and dimming application bias.

Step N°	Lamp in LHS	Lamp in RHS	Criteria for visual equality	Lamp to which dimming was applied	Mean illuminance ratio (PCW/CW) at the visual match	Booth at lowest illuminance
1	CW	PCW	brightness	PCW	0.9	PCW
2	CW	PCW	overall brightness	PCW	0.8	PCW
3	CW	PCW	clarity of red-green border	PCW	0.085	PCW
4	CW	PCW	clarity of border	CW	20.0	CW
5	CW	PCW	overall brightness	PCW	0.9	PCW
6	CW	PCW	clarity of blue-yellow border	CW	3.2	CW
7	CW	PCW	clarity of border	PCW	0.17	PCW

**Table 9**

Summary of dimming application and visual objectives in the matching test carried out by Worthey using side-by-side booths (Worthey, 1985). It can be seen that the booth to which dimming is applied is set on average to the lower illuminance.