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Establishing the $^{40}\text{Ca}(p,p\alpha)$ Reaction at 392 MeV under Quasi-Free Scattering Conditions

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 The $(p, p\alpha)$ reaction offers a direct means to probe preformed α -cluster structures in nuclei under quasi-free scattering conditions. Previous studies around 100 MeV provided valuable insights into α clustering, but quantitative comparison with microscopic cluster wave functions remained limited due to strong distortion effects. At higher energies, the reaction mechanism becomes simpler and the distorted-wave impulse approximation (DWIA) provides a more reliable framework for quantitative analysis. In the present work, the $^{40}\text{Ca}(p, p\alpha)$ reaction was measured at an incident energy of 392 MeV using the high-resolution Grand Raiden and Large Acceptance Spectrometer at RCNP. Despite the small cross section in this energy region, the achieved resolution allowed clear separation of the ground and excited states of the residual ^{36}Ar nucleus, and corresponding momentum distributions were extracted. DWIA calculations using a Woods–Saxon $\alpha + ^{36}\text{Ar}$ bound-state wave function yielded an experimental spectroscopic factor of $S_{\text{FAC}}^{\text{WS}} = 0.51 \pm 0.05$, consistent with the previous result at 101.5 MeV (0.52 ± 0.11). This agreement demonstrates that the reaction mechanism is well described across a wide energy range. The present study establishes the feasibility of high-precision $(p, p\alpha)$ measurements at several hundred MeV and highlights their potential as a quantitative probe of α clustering in medium-mass nuclei, forming the basis for systematic studies in both stable and unstable systems.

Subject Index C30, D04, D11, D13, D22

1. Introduction: Quasi-free $(p, p\alpha)$ studies of α clustering

The $(p, p\alpha)$ reaction has been developed as a versatile tool to investigate α -cluster structures in nuclei under quasi-free scattering conditions [1,2]. In this reaction, a proton incident on the target nucleus knocks out a preformed α cluster, allowing the direct extraction of its spectroscopic strength and momentum distribution. Since the outgoing proton and α particle carry information on the internal motion of the cluster, the $(p, p\alpha)$ process provides a powerful means of probing α correlations near the nuclear surface, where clustering is expected to be enhanced.

Early systematic studies were conducted with proton beams of about 100 MeV on light nuclei such as ^6Li , ^9Be , and ^{12}C [3,4]. These experiments established the basic framework of the $(p, p\alpha)$ reaction, demonstrating that coincident detection of the scattered proton and the ejected α particle enables the separation of distinct final states and a quantitative extraction of spectroscopic information. The approach was later extended to medium-mass systems such as ^{40}Ca [5,6], marking a significant step toward exploring the evolution of α clustering beyond the p -shell region. By detecting the scattered proton and the knocked-out α particle in coincidence, information on the existence probability (spectroscopic strength) and the internal momentum distribution of α clusters has been obtained [3,7–12]. Although most of these measurements were performed around 100 MeV, an early attempt at a much higher energy of 600 MeV was also reported [13], providing a first exploration of the reaction in the several-hundred-MeV region where the impulse approximation is expected to be more valid.

At incident energies near 100 MeV, relatively large cross sections allowed measurements with sufficient statistics, making it possible to perform detailed analyses of α -knockout reactions [5,6]. In light nuclei such as ^{12}C , the factorization between the elementary p - α scattering

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amplitude and the nuclear α -cluster wave function was found to hold approximately under quasi-free scattering (QFS) conditions, allowing the measured cross sections to be consistently interpreted in terms of single-step knockout processes [11]. For medium-mass nuclei such as ^{40}Ca , several experiments have also been performed in this energy region. A high-resolution measurement at 101.5 MeV using the Maryland Cyclotron provided detailed α -separation energy spectra and energy distributions of the outgoing proton, from which experimental spectroscopic factors were extracted through distorted-wave impulse approximation (DWIA) analyses [5–7,14]. Subsequent measurements at iThemba LAB examined the analyzing powers and spin observables for $(p, p\alpha)$ reactions at similar energies, showing that, with carefully chosen optical potentials, the data can be consistently described within the impulse approximation framework [9]. These results collectively demonstrate that $(p, p\alpha)$ studies around 100 MeV have provided valuable insights into the α -cluster component of nuclear wave functions, while minor deviations from DWIA predictions at higher ejectile energies suggest the need for a more refined treatment of refraction and absorption effects, particularly in kinematic regions corresponding to large proton energies and small α scattering angles.

Despite the success at 100 MeV, measurements in this energy region remain affected by strong final-state interactions and substantial distortion of the reaction waves, in particular the α -residue scattering at tens of MeV in the final state, which obscure direct connections between the experimental cross sections and the microscopic cluster wave functions. At higher incident energies, on the other hand, these effects become significantly reduced. High-energy $(p, p\alpha)$ experiments therefore offer unique advantages. In the several-hundred-MeV region, the reaction mechanism is greatly simplified, distorting potentials become less absorptive, and the quasi-free condition is more ideally realized. The higher outgoing energies of the proton and α particle also expand the accessible kinematic domain and minimize multistep contributions, leading to a more transparent interpretation of the observed cross sections in terms of direct α -knockout processes. In addition, final-state interactions (FSI) between the outgoing particles and the residual nucleus are strongly suppressed at higher energies, allowing clearer identification of the direct reaction mechanism and more reliable comparison with theoretical models based on DWIA.

Nevertheless, the experimental realization of high-energy $(p, p\alpha)$ measurements has long remained challenging. As the incident energy increases, the reaction cross section decreases rapidly, requiring high-intensity proton beams and efficient coincidence detection systems to obtain sufficient statistics. At the same time, high energy and angular resolutions are essential to resolve closely spaced excited states of the residual nucleus. For example, a measurement at 157 MeV reported the first attempt to extend $(p, p\alpha)$ spectroscopy to higher energies, but the resolution was insufficient to clearly separate the ground and excited states of the residual ^{36}Ar nucleus. Another experiment at 600 MeV achieved access to large momentum transfers, but the low yield limited quantitative analyses [13]. These results highlight a contrast: while ~ 100 MeV measurements achieved good resolution and statistics, experiments at higher energies have been constrained by both yield and resolution, leaving only a few successful examples above 200 MeV [12].

In the present study, to achieve the $(p, p\alpha)$ reaction at several hundred MeV, a high-intensity 392 MeV proton beam was combined with the high-resolution double-arm magnetic spectrometer system at RCNP, and a thin target was employed to optimize the balance between resolution and yield. As a result, efficient coincidence detection and precise energy determination of the

outgoing particles were achieved, providing sufficient resolution to separate individual excited states of the residual nucleus while maintaining high statistical accuracy. The ^{40}Ca nucleus serves as an ideal benchmark for such studies, as it exhibits both shell closure and a well developed α -cluster component. By comparing the results at 392 MeV with the well established 101.5 MeV data [5,6], we examine the consistency of the extracted experimental spectroscopic factors across widely different energy regimes, providing a stringent test of the DWIA reaction framework. Through this comparison, the present work establishes a firm experimental foundation for quantitative (p , $p\alpha$) studies at several hundred MeV and demonstrates the feasibility of high-resolution, high-statistics measurements in medium-mass nuclei. The results pave the way for systematic investigations of α clustering in both stable and radioactive nuclei under quasi-free conditions, linking the spectroscopic strength observed in knockout reactions to the microscopic structure of preformed α clusters at the nuclear surface.

In recent years, interest in α clustering in the ground states of nuclei has been revitalized by the discovery of surface clustering phenomena across a wide mass range, including both stable and neutron-rich systems [15,16]. Systematic (p , $p\alpha$) measurements have been initiated on medium-mass and heavy nuclei to explore the mass and isotopic dependence of α correlations [17]. For instance, (p , $p\alpha$) reactions on tin isotopes have been performed at 400 MeV using the double-arm magnetic spectrometer setup, providing the first comprehensive investigation of α -cluster formation in tin isotopes with increasing neutron number [18]. These pioneering studies revealed valuable systematics of clustering phenomena; however, due to the need for thick targets (40 mg/cm^2) to secure sufficient yield, the achievable energy resolution was limited, and uncertainties remained in the absolute normalization of the proton energy spectra, partly reflecting incomplete acceptance calibration. Consequently, detailed state-by-state analyses could not be performed in those measurements.

2. Experimental setup with the double-arm spectrometer system

The experiment was carried out at the Ring Cyclotron Facility of the Research Center for Nuclear Physics (RCNP), the University of Osaka. A 392 MeV proton beam was accelerated by the ring cyclotron and transported through the WS beam line onto a self-supporting $^{\text{nat}}\text{Ca}$ target. The scattered proton and the α particle produced in the (p , $p\alpha$) reaction were detected in coincidence and analyzed using the double-arm spectrometer system [19] consisting of the Grand Raiden (GR) [20] and the Large Acceptance Spectrometer (LAS) [21], equipped with their focal-plane detectors. This setup enabled event-by-event particle identification and precise determination of the momenta under the selected kinematic condition. A schematic layout of the experimental setup is shown in Fig. 1.

Data were acquired with beam intensities of 50 nA for 4 h and 100 nA for an additional 4 h. The $^{\text{nat}}\text{Ca}$ target had a thickness of 11.8 mg/cm^2 . The foil was mounted perpendicular to the axis pointing from the reaction point toward LAS in order to minimize the energy loss of low-energy α particles emitted in the LAS direction. The proton beam was delivered with an energy spread smaller than $\sim 200\text{ keV}$ in FWHM and a spot size of approximately 1 mm at the target position, ensuring precise definition of the reaction kinematics. The natural isotopic abundance of the ^{40}Ca in the $^{\text{nat}}\text{Ca}$ target is 96.9%. The effect of the finite target thickness on the overall energy resolution was evaluated to be about 0.4 MeV in sigma, mainly due to angular straggling and energy-loss differences of the outgoing particles. The unreacted beam was transported to

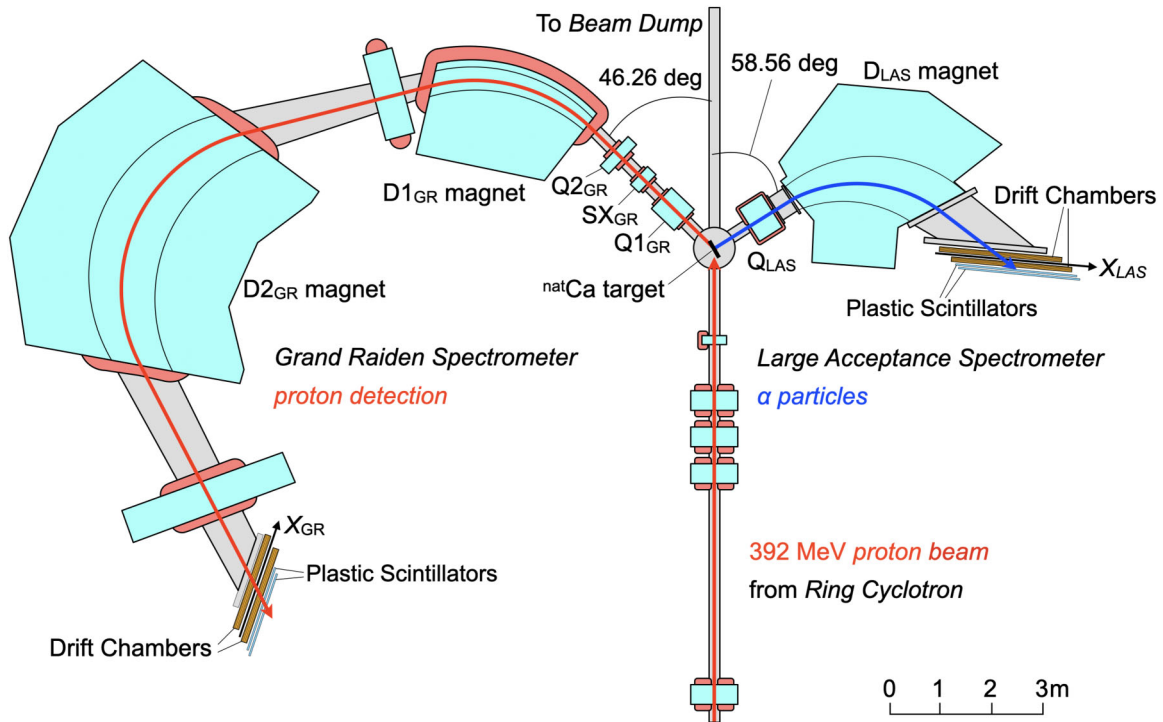


Fig. 1. Schematic layout of the experimental setup with the double-arm spectrometer used for the $(p, p\alpha)$ measurement at RCNP.

a Faraday cup located at the end wall of the experimental hall, where the beam current was monitored.

The coincidence measurement of the outgoing proton and α particle was performed using GR and LAS. The spectrometers were positioned at laboratory polar angles of 46.26° (GR) and 58.56° (LAS). These settings correspond to a p - α scattering angle of 60° in the center-of-mass frame with recoilless conditions when the reaction Q value of -7.038 MeV is taken into account. This angular configuration was chosen to closely match the kinematics of free two-body proton- α elastic scattering at 392 MeV, taking into account the α -separation energy. As a result, the momentum transfer is shared between the outgoing proton and the α particle, minimizing the recoil momentum of the residual nucleus. The central kinetic energies of the analyzed particles were 318.59 MeV for protons and 66.37 MeV for α particles. The corresponding central magnetic fields were 0.9293 T (GR) and 0.6729 T (LAS). After being bent by the spectrometer magnets, the incident particles were dispersed according to their momentum in the horizontal (dispersive) direction. To enable reliable reconstruction of the scattering angles at the target position, a dedicated sieve-slit calibration was performed. A sieve slit with a regular array of holes was placed downstream of the target, providing particles with well defined horizontal and vertical emission angles. By analyzing the correlations between the known geometrical positions of the sieve holes and the focal-plane observables under the same kinematic and optical conditions as the $(p, p\alpha)$ measurement, the ion-optical coefficients relevant for scattering-angle reconstruction were determined. Based on this calibration, the GR Q1 magnet field was reduced by 10% and the LAS Q magnet field was increased by 20%, ensuring sufficient sensitivity to the vertical scattering angle in the present experiment. Details of the sieve-slit calibration and ion-optical analysis are given in Ref. [22].

Table 1. Magnetic-field settings and focal-plane detector configurations of GR and LAS. Software acceptances reflect the analysis cuts applied.

	GR	LAS
Detected particle	proton	α particle
Central polar angle	46.26°	58.56°
Polar-angle acceptance (software)	$\pm 1.15^\circ$	$\pm 3.15^\circ$
Central azimuthal angle	0°	180°
Azimuthal-angle acceptance (software)	$\pm 2.30^\circ$	$\pm 3.32^\circ$
Solid angle (software)	2.5 msr	10.0 msr
Central kinetic energy	318.59 MeV	66.37 MeV
Energy acceptance (software)	303–329 MeV	50–80 MeV
Magnetic field	0.9293 T	0.6729 T
Field adjustment	Q1: -10%	Q: $+20\%$
Exit window	polyimide 125 μm	polyimide 125 μm
Drift chambers	2 sets	2 sets
Plastic scintillators	2 layers (1 cm each)	1 layer (3 mm)
Trigger	1st scintillator	thin scintillator
Energy-loss observable	2nd scintillator light output	drift-chamber TOT

At the GR focal plane, two sets of multiwire drift chambers and two plastic scintillators (each 1 cm thick) were installed. The drift chambers provided trajectory tracking, yielding the horizontal (momentum-dispersive) position and angle. The plastic scintillators covered the entire focal plane horizontally and were read out from both ends by photomultiplier tubes (PMTs); end-to-end coincidences improved the signal-to-noise ratio. The first scintillator layer provided the trigger, while the second layer yielded energy-loss information.

At the LAS focal plane, two sets of drift chambers and a thin (3 mm) plastic scintillator were installed. As in GR, the drift chambers provided position and angle information, and the thin scintillator, read out from both ends, generated the trigger in coincidence. The LAS energy acceptance for α particles was 50–90 MeV. The lowest-energy α particles reached the scintillator with an energy down to ~ 5 MeV; to avoid efficiency loss, the PMT gain was increased and the trigger threshold was set as low as practical. Because the large-area thin scintillator exhibits significant light attenuation, it is not optimal for precise energy-loss measurements; instead, the α energy loss was effectively inferred from time-over-threshold (TOT) signals obtained from the drift chambers (see e.g. Ref. [23]). The spectrometer settings and focal-plane detector configurations are summarized in Table 1.

3. Data analysis

3.1. Particle identification and event selection

The scattered proton and the knocked-out α particle from the $^{40}\text{Ca}(p, p\alpha)$ reaction were identified at their respective focal-plane detectors. In GR, particle identification was performed using the correlation between the light output in the second plastic scintillator and the horizontal position (GR X, momentum-dispersive direction) obtained from drift-chamber tracking, as shown in the left panel of Fig. 2(a). The light output was defined as the geometric mean of the light-output signals from the left and right photomultiplier tubes (PMTs) of the plastic scintillator, in order to remove the position dependence along the GR focal-plane (X) direction. The distribu-

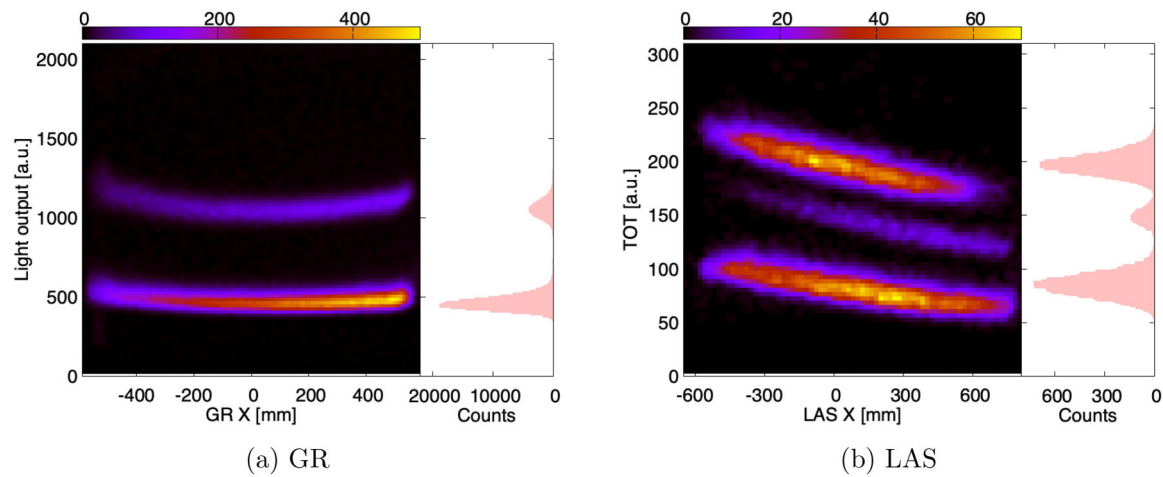


Fig. 2. Particle identification at the focal planes of GR (a) and LAS (b). In each panel, the left plot shows the 2D correlation used for particle identification (horizontal position vs. light output in GR, or horizontal position vs. TOT in LAS), while the right plot displays the corresponding projected spectrum after correcting for the position dependence. Distinct bands of protons, deuterons, and α particles are clearly identified.

tion appearing around a light output of 500 corresponds to protons, while a separate distribution above it originates from deuterons.

In the right panel of Fig. 2(a), the light output is presented as a 1D spectrum. For this purpose, the residual dependence of the light output on the GR focal-plane position, which was not fully removed by the geometric mean, is corrected. Specifically, for the proton locus shown in the left panel, a quadratic function was fitted to reproduce this position dependence, and an event-by-event correction was applied to remove it. Protons were selected within $\pm 2\sigma$ in this spectrum, and the contamination from deuterons was estimated to be less than 0.1%.

In LAS, particle identification was carried out using the correlation between the focal-plane position X and the time-over-threshold (TOT) signals from the drift chambers, as shown in the left panel of Fig. 2(b). Distributions corresponding to protons, deuterons, and α particles were observed. The right panel of Fig. 2(b) shows the TOT spectrum after correcting for the dependence on LAS X . The α particles were selected within $\pm 2\sigma$ in this spectrum, and the contamination from deuterons was estimated to be 0.5% of the total counts.

In addition, the detection efficiencies of the plastic scintillators and drift chambers were evaluated. The detection efficiency associated with multihit handling in the plastic scintillators was 99% for GR and 94% for LAS, while the tracking efficiency of the drift chambers was 93% for protons in GR and 98% for α particles in LAS. The particle-identification efficiency together with these detection efficiencies were included in the cross-section normalization and contribute to the overall systematic uncertainty at the level of 4%.

3.2. Coincidence timing and accidental background estimation

Figure 3 shows the time-difference spectrum between the timing signals obtained from the trigger plastic scintillators at the focal planes of GR and LAS. Multiple peaks reflect the bunch structure associated with the acceleration cycle of the cyclotron. In this spectrum, the protons and α particles have already been identified in GR and LAS, respectively. The prompt peak contains both true and accidental-coincidence events. In contrast, the other peaks consist only

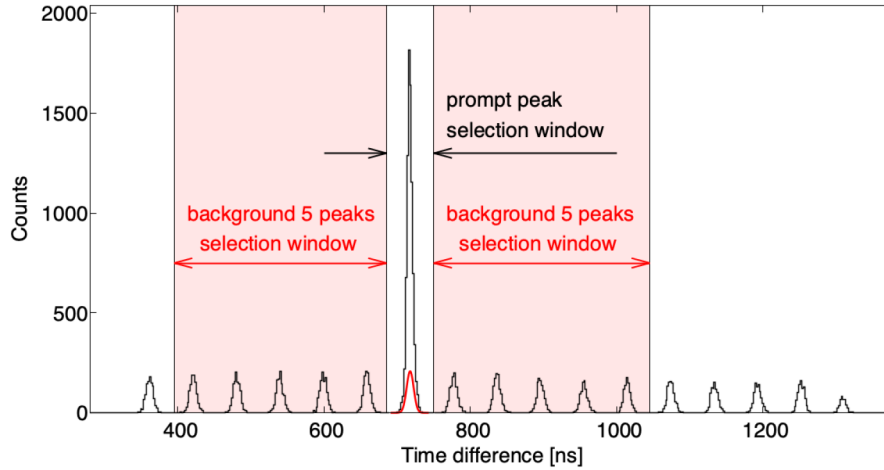


Fig. 3. Time-difference spectrum between the timing signals of GR and LAS. Multiple peaks appear, reflecting the bunch structure of the cyclotron. The prompt-peak selection window and background-selection windows are indicated. The red line represents the contribution of accidental coincidences evaluated from the side peaks.

of accidental coincidences, indicating that accidental coincidences are constantly observed at a uniform rate. Here, to evaluate the contribution of accidental events, the coincidence timing window was deliberately widened to about $1 \mu\text{s}$, so that multiple accidental-coincidence peaks could be clearly observed.

First, the prompt peak (True + Accidental) was defined by a 3σ range around the peak, as shown in the figure. Next, five accidental-coincidence peaks on each side (10 in total) were defined as background-selection windows. Since the prompt peak is expected to contain accidental events similar to those in the side peaks, 10 spectra were summed and averaged (divided by 10), and the result was used to estimate the contribution of accidental events included in the prompt peak, as indicated by the red line in Fig. 3. By summing and averaging multiple spectra, the statistical uncertainty associated with the background subtraction was reduced. By subtracting this background component from the prompt spectrum, true coincidence events were successfully extracted, providing a clean dataset for various spectral analyses, including energy-correlation and separation energy spectra.

3.3. Energy reconstruction and α -separation spectrum

Detailed ion-optics analyses of GR and LAS were first performed, from which the actual focal-plane positions were analytically determined. Based on these results, the horizontal position at the focal plane was directly related to the particle momentum through the magnetic rigidity of the spectrometer, and the corresponding kinetic energy was obtained from the reconstructed momentum. Using this procedure, the energies of the scattered proton in GR and the knocked-out α particle in LAS were determined on an event-by-event basis.

The energy conservation in the $(p, p\alpha)$ reaction is expressed as

$$E_p + E_\alpha + E_r = E_{\text{beam}} + m_t, \quad (1)$$

where E_p and E_α denote the total energies of the scattered proton and the knocked-out α particle, and E_r is the total energy of the residual nucleus. The target mass m_t is given. Rewriting

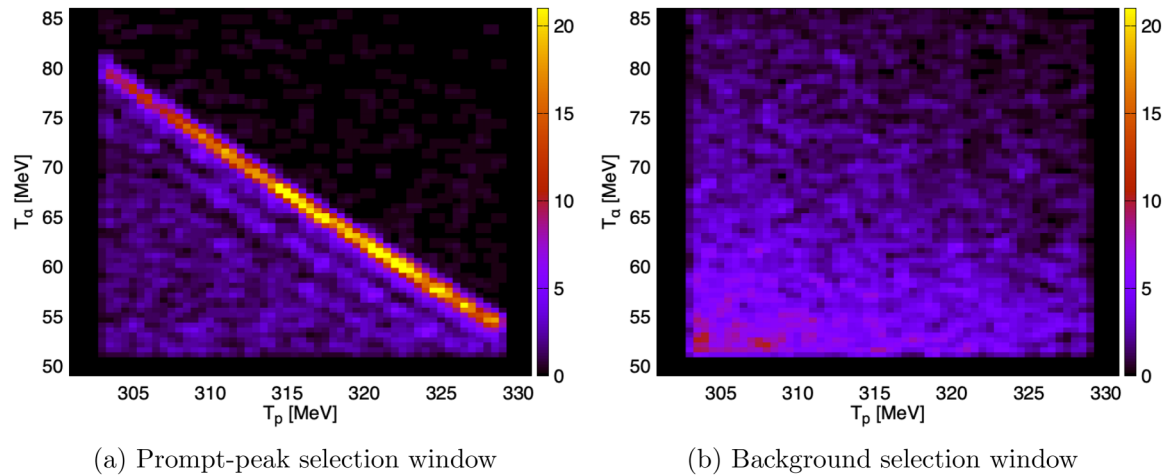


Fig. 4. Energy correlation between the proton and the α particle in each coincidence window. Panel (a) shows the prompt-peak selection, where the events are distributed along a line corresponding to constant $T_p + T_\alpha$, demonstrating energy conservation in the $(p, p\alpha)$ reaction. Panel (b) shows the background selection, where the background originating from accidental coincidences exhibits no structure.

this equation in terms of kinetic energies and masses gives

$$T_{\text{beam}} - (T_p + T_\alpha + T_r) = (m_\alpha + m_r - m_t) \equiv S_\alpha. \quad (2)$$

Here, S_α represents the α -separation energy, i.e. the energy required to remove an α particle from the target nucleus. Since the kinetic energy of the residual nucleus is negligibly small and the beam energy T_{beam} is fixed at 392 MeV, the following approximation holds for a constant S_α :

$$T_p + T_\alpha \approx \text{const.} \quad (3)$$

Figure 4(a) shows the energy correlation between the scattered proton and the knocked-out α particle, displayed as a density plot with the proton energy on the horizontal axis and the α -particle energy on the vertical axis. Only events within the prompt-peak selection window defined in the coincidence timing spectrum are plotted in this figure. The true coincidence events are distributed along a straight line corresponding to $T_p + T_\alpha = \text{const.}$, reflecting energy conservation in the $(p, p\alpha)$ reaction and confirming that an α cluster was knocked out from the target nucleus. In contrast, Fig. 4(b) shows the events selected by the background-selection window, where the background originating from accidental coincidences exhibits no structure.

Based on the relation between the kinetic energies and S_α given in Eq. (2), the S_α energy spectrum was derived. First, the prompt-peak window was selected in the coincidence timing spectrum, and the S_α spectrum constructed under this condition is shown by the black line in Fig. 5. In contrast, when the background window was selected and the spectrum was constructed under the same conditions, the result scaled by a factor of 1/10 (corresponding to the average contribution estimated from 10 accidental peaks) is shown by the red line. This component represents a flat background arising from accidental coincidences. In the subsequent analyses of the S_α spectrum, this red background component was subtracted to isolate the contribution from true coincidence events.

3.4. Target composition analysis

Because calcium is highly prone to oxidation, a detailed analysis of the target composition was required. To quantitatively evaluate the degree of oxidation and possible carbon contamination,

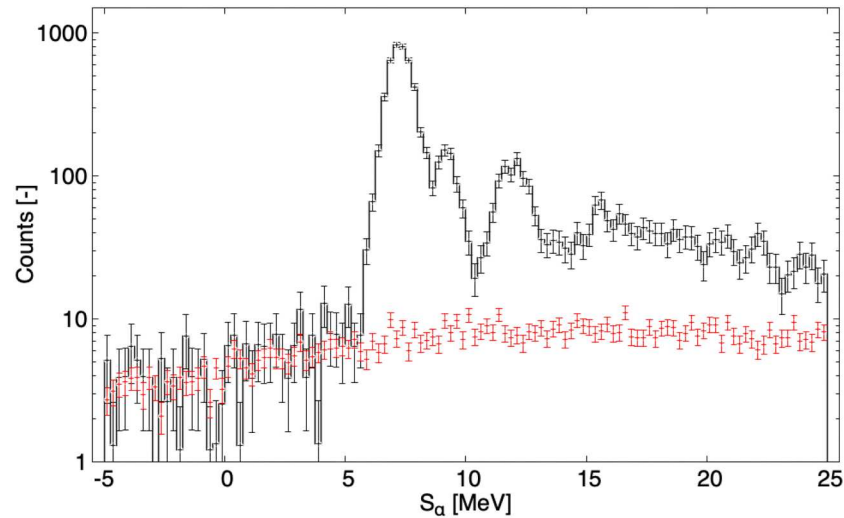


Fig. 5. S_α energy spectra constructed under two different coincidence timing conditions. The black line corresponds to the prompt-peak selection, and the red line shows the background estimated from accidental coincidences.

Table 2. Composition of the $^{\text{nat}}\text{Ca}$ target used in the $(p, p\alpha)$ experiment, including the contaminant fractions of ^{12}C and ^{16}O , the corrected content of ^{40}Ca , and the corresponding α -separation energies (S_α) of each nucleus.

Nucleus	S_α (MeV)	Amount in $^{\text{nat}}\text{Ca}$ target
^{12}C	7.367	0.0371(1) mg/cm ²
^{16}O	7.162	0.326(1) mg/cm ²
^{40}Ca	7.040	11.1(5) mg/cm ²

a high-precision measurement of proton elastic scattering at 65 MeV was performed at the same facility. This measurement was conducted independently of the $(p, p\alpha)$ experiment, immediately after it, using one day of beam time. The Grand Raiden (GR) spectrometer was placed at a laboratory angle of 28° . The measurements were carried out using both the $^{\text{nat}}\text{Ca}$ target and a Mylar reference target under identical magnetic-field settings. The $^{\text{nat}}\text{Ca}$ target used in the elastic-scattering measurement was identical to that employed in the $(p, p\alpha)$ experiment and had a thickness of 11.8 mg/cm^2 . The target thickness was determined from its weight and irradiated area, and the uncertainty of 5% originates primarily from the precision of the area measurement. Mylar, whose chemical composition is well known $(\text{C}_{10}\text{H}_8\text{O}_4)_n$, was used as a reference. By weighing a large sheet ($10 \text{ cm} \times 10 \text{ cm}$), its thickness and the elemental composition were determined with high accuracy. The magnetic field was optimized so that protons elastically scattered from ^{16}O were centered at the focal plane. Under these conditions, the GR energy acceptance also covered protons elastically scattered from ^{12}C and ^{40}Ca . By comparing the elastic-scattering yields of C and O observed with the $^{\text{nat}}\text{Ca}$ target with those measured using the Mylar reference target, the relative abundances of carbon and oxygen in the target were quantitatively evaluated. Table 2 lists the contamination levels of ^{12}C and ^{16}O contained in the $^{\text{nat}}\text{Ca}$ target. Furthermore, by subtracting these major contaminants from the total target thickness and taking into account the natural isotopic abundance of ^{40}Ca , the content of ^{40}Ca in the target was also determined.

Nuclei with similar S_α values contained in the target can produce overlapping peaks in the S_α spectrum. Because light nuclei generally exhibit larger $(p, p\alpha)$ cross sections than medium-mass nuclei, even a small admixture of ^{12}C or ^{16}O can give rise to a noticeable background component. To accurately evaluate and subtract these background contributions, $(p, p\alpha)$ measurements were performed using $^{\text{nat}}\text{C}$ and Mylar targets under the same experimental conditions as for the $^{\text{nat}}\text{Ca}$ target. Since the fractions of ^{12}C and ^{16}O impurities in the $^{\text{nat}}\text{Ca}$ target were known, the S_α spectra originating from the $(p, p\alpha)$ reactions on these nuclei could be predicted on an absolute scale. The reference spectra obtained from these measurements were used in Section 4 to quantitatively subtract the contamination components and extract the pure ^{40}Ca contribution. Specifically, the relative contributions from ^{12}C and ^{16}O were evaluated using proton elastic-scattering measurements at 65 MeV performed under identical experimental conditions for the Ca targets and reference Mylar and $^{\text{nat}}\text{C}$ targets. Because the elastic-scattering yield ratios between the Ca and reference targets depend only on the relative numbers of O and C atoms, these ratios provide a reaction-model-independent determination of the impurity contents in the Ca targets. The experimentally determined O and C atom ratios were then directly applied to the 392 MeV $(p, p\alpha)$ data to predict the corresponding S_α spectra on an absolute scale. Using these predicted spectra, the O and C contributions were quantitatively subtracted from the measured spectra, enabling the extraction of the pure ^{40}Ca component. This procedure avoids assumptions on absolute contamination levels or reaction cross sections and relies solely on experimentally measured yield ratios obtained under identical kinematic and instrumental conditions. The details of this procedure are introduced in Ref. [24].

3.5. Angular acceptance calibration

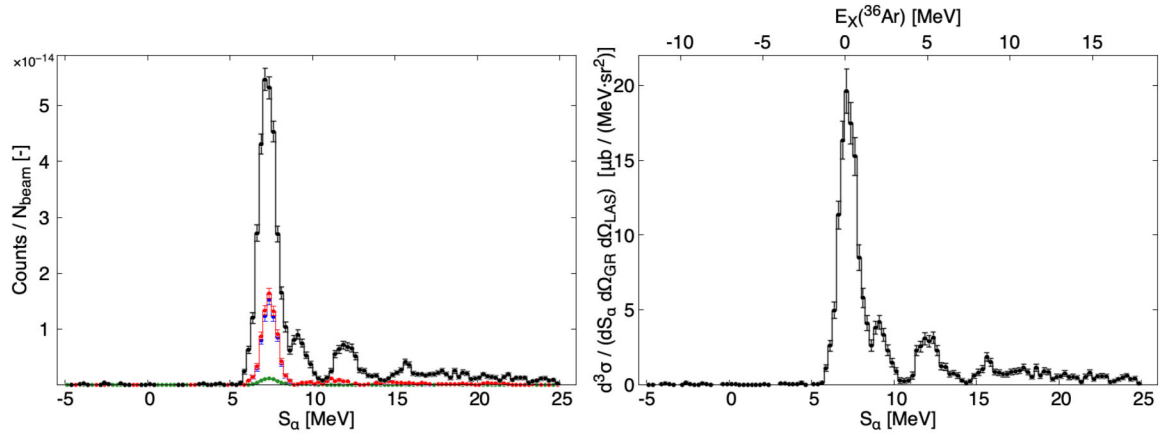
To determine the absolute cross section, it is essential to define the angular acceptance of both GR and LAS. In the present experiment, no mechanical restrictions such as collimators were applied, and data were taken over the full angular range that each spectrometer can cover. Based on a detailed analysis of separately obtained angular-calibration data, a software acceptance was defined with careful consideration to avoid any loss of events due to the geometry of the beam duct or the focal-plane detectors.

4. Results and discussion

As described in Section 3, coincidence events corresponding to the $^{40}\text{Ca}(p, p\alpha)$ reaction were extracted. Accidental coincidences were identified as a smooth background and removed. Contaminant components originating from ^{12}C and ^{16}O were quantitatively corrected based on reference measurements using $^{\text{nat}}\text{C}$ and Mylar targets. Through these procedures, the α -separation energy (S_α) spectrum of pure ^{40}Ca was obtained. The main experimental results are presented below.

4.1. Alpha-separation energy spectra

Figure 6 shows the α -separation energy (S_α) spectra obtained from the ^{40}Ca target. Panel (a) presents the spectrum after subtraction of accidental coincidences, where contributions from contaminant nuclei are visible. The vertical axis represents the yield normalized to the number of incident protons. The green and blue histograms correspond to ^{12}C and ^{16}O , respectively, and indicate the predicted contributions on an absolute scale, derived from measurements with $^{\text{nat}}\text{C}$ and Mylar targets under the same $(p, p\alpha)$ experimental conditions. As evaluated in Section 3,



(a) After subtraction of accidental background. (b) After subtraction of contamination.

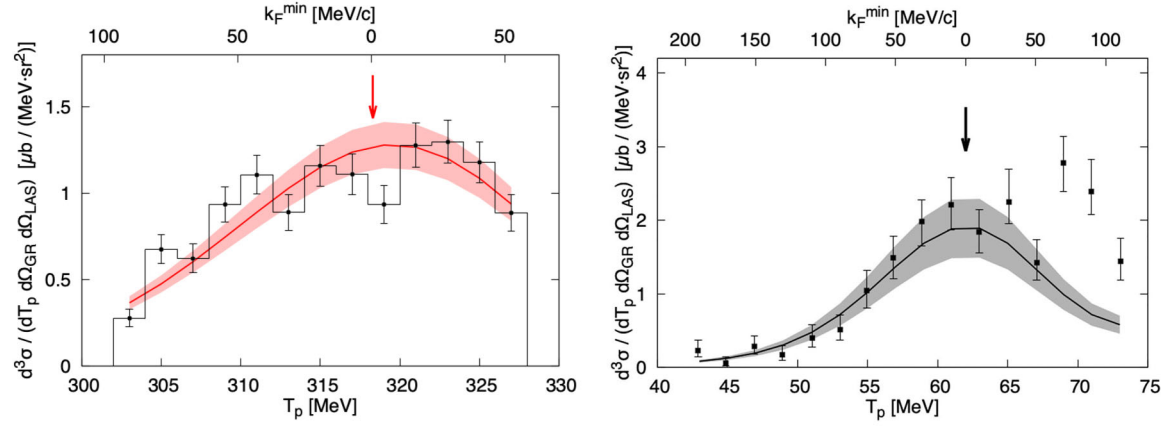
Fig. 6. α -separation energy (S_α) spectra for the ^{40}Ca target. (a) Spectrum after removing accidental background, overlaid with the reference data from $^{\text{nat}}\text{C}$ and Mylar targets. The green curve represents the contribution from carbon, the blue curve corresponds to oxygen contamination, and the red curve shows their sum. (b) Extracted ^{40}Ca spectrum after subtracting oxygen and carbon contributions. The differential cross section is integrated over the proton kinetic-energy acceptance given in Table 1.

the contamination levels of ^{12}C and ^{16}O were small; however, their contributions are nonnegligible compared with the ^{40}Ca component, because the $(p, p\alpha)$ reaction cross sections for light nuclei are relatively large. Panel (b) displays the resulting ^{40}Ca spectrum obtained after subtracting the ^{12}C and ^{16}O components. The vertical axis represents the triple-differential cross section, taking into account the target thickness, angular acceptances, and bin width of the S_α spectrum. The differential cross section is integrated over the proton kinetic-energy acceptance given in Table 1. Gaussian fits to the S_α peaks yielded an experimental resolution of $\sigma = 0.46 \pm 0.01$ MeV, where the quoted uncertainty represents the statistical error obtained from the fit covariance matrix. This resolution can be consistently explained by two dominant contributions. The variation in the energy loss of the emitted α particles, depending on the reaction depth within the target, contributes approximately 0.36 MeV. In addition, the beam energy resolution of 0.25 MeV contributes to the observed width. The quadrature sum of these effects quantitatively reproduces the measured resolution.

The α -separation energy S_α obtained from the ^{40}Ca $(p, p\alpha)$ reaction is directly related to the excitation energy E_x of the residual nucleus ^{36}Ar through the following relation:

$$E_x(^{36}\text{Ar}) = S_\alpha - 7.040 \text{ MeV}. \quad (4)$$

Here, 7.040 MeV represents the α -separation energy required to remove an α cluster from the ground state of ^{40}Ca , leaving the residual nucleus ^{36}Ar in its ground state. In the framework of quasi-free scattering (QFS), it is assumed that the target nucleus is initially in its ground state before the reaction. Therefore, this separation energy serves as a reference for defining the excitation energy of the residual nucleus. The most prominent peak in the spectrum corresponds to the transition to the ground state of ^{36}Ar , while the adjacent peak on the higher-energy side corresponds to the first excited state at 1.97 MeV, which is resolved with a statistical significance of about 2σ . At higher excitation energies, around 5 MeV, several closely spaced states—including 2^+ (4.951 MeV), 2^- (4.974 MeV), and 5^- (5.171 MeV)—are expected to overlap, leading to the formation of a broad composite structure rather than distinct peaks. Because a natural Ca target



(a) Proton energy distribution of present data at 392 MeV (RCNP). (b) Proton energy distribution of previous data at 101.5 MeV (Maryland Cyclotron) [5, 6].

Fig. 7. Proton energy distributions for the $^{40}\text{Ca}(p, p\alpha)$ reaction. The vertical axis represents TDX $d^3\sigma / (dT_p d\Omega_p d\Omega_\alpha)$. The curves are the DWIA results scaled to the experimental data to minimize the χ^2 , and the hatched areas represent the uncertainties of the fit. Error bars indicate statistical uncertainties only.

was used, minor Ca isotopes are present; however, their contributions do not affect the present analysis. In particular, the S_α value of ^{44}Ca (8.854 MeV) differs from that of ^{40}Ca (7.040 MeV) by 1.815 MeV, which is significantly larger than the $\pm 2\sigma$ selection window (± 0.92 MeV) applied to the ^{40}Ca ground-state peak. As a result, the tail of the ^{44}Ca contribution does not enter the ^{40}Ca gate, and its effect can be neglected in view of its small isotopic abundance (2.086%).

4.2. Energy distribution of the emitted proton

To investigate the energy distribution characteristic of each state, events in the α -separation energy region corresponding to the ground-state transition $^{40}\text{Ca}(0^+) \rightarrow ^{36}\text{Ar}(0^+)$ were selected within a range of $\pm 2\sigma$. The energy distribution of the emitted proton, measured with the GR spectrometer, is shown in Fig. 7(a). All background contributions discussed earlier have been removed.

The vertical axis represents the triple-differential cross section (TDX), defined as

$$\frac{d^3\sigma}{dT_p d\Omega_p d\Omega_\alpha} = \frac{Y}{N_{\text{beam}} N_{\text{target}} \Delta T_p \Delta\Omega_p \Delta\Omega_\alpha}, \quad (5)$$

where Y is the yield of detected p - α coincidence events, N_{beam} is the total number of incident protons, and N_{target} is the areal density of target nuclei. T_p denotes the kinetic energy of the scattered proton, while Ω_p and Ω_α represent the solid angles subtended by the proton and α -particle detectors, respectively. All relevant detection efficiencies and normalization factors were taken into account. In a knockout reaction, the reaction kinematics can be uniquely determined by specifying T_p , Ω_p , and Ω_α . The corresponding reaction rate is expressed as the TDX, which serves as a physical quantity directly comparable with theoretical calculations at fixed kinematics.

For the transition from the ground state (0^+) of the target nucleus to the ground state (0^+) of the residual nucleus, no orbital angular momentum transfer is involved. Under this condition, the reaction is expected to reach its maximum cross section when the recoil momentum of the residual nucleus is minimized, i.e. under recoilless conditions. In Fig. 7(a), the upper horizontal

axis shows the minimum recoil momentum k_F^{\min} of the residual nucleus that can be accessed within the angular acceptance, as a function of the proton energy. From momentum conservation in the initial state and the quasi-free condition, the recoil momentum of the residual nucleus is related to the internal momentum of the knocked-out α particle by $\vec{k}_F = -\vec{k}_\alpha$. According to the kinematical calculation, the recoilless condition in Fig. 7(a) corresponds to the arrow at $T_p = 320$ MeV. The measured triple-differential cross-section (TDX) spectrum indeed exhibits a clear maximum around this energy, consistent with the expectation for a recoilless transition.

4.3. Comparison with previous data and reaction calculations

To examine the consistency of the present measurement, the results were compared with the existing $^{40}\text{Ca}(p, p\alpha)$ data taken at 101.5 MeV [5,6]. This dataset represents one of the most thoroughly analyzed and reliable measurements among previous studies. Figure 7(b) shows the energy distribution of the scattered protons. This distribution is compared with the present 392 MeV data. Because the reaction kinematics, the elementary p - α scattering cross section, and the strength of refraction and absorption effects differ between the two energy regimes, a direct comparison of the absolute TDX values is not straightforward. Therefore, detailed reaction calculations are required to perform a meaningful comparison and to assess the consistency of the underlying reaction mechanism.

4.4. DWIA calculation

To interpret the measured cross sections, DWIA calculations were performed using the computer code PIKOE [25]. The α -cluster wave function in ^{40}Ca was obtained as the bound-state wave function of the $\alpha + ^{36}\text{Ar}$ system. A Woods-Saxon form was assumed for the binding potential, and its depth was adjusted to reproduce the empirical α -separation energy. The radius and diffuseness parameters were set to $R_0 = 1.25 \times 36^{1/3}$ fm and $a_0 = 0.76$ fm, respectively. These values were determined in the α -transfer reaction analysis by Fukui et al. [26], in which the α -cluster wave function was adjusted to reproduce, as closely as possible, the shape of the microscopic cluster model. The obtained α -cluster wave function was normalized to unity. This part corresponds to the structural preparation, which is used in the subsequent reaction-theoretical analysis.

In the DWIA framework for knockout reactions, the differential cross section of the p - α elementary process is used as an input. For the entrance and exit channels, the EDAD1 global Dirac phenomenological optical potential [27–29] was adopted for the $p + ^{40}\text{Ca}$ and $p + ^{36}\text{Ar}$ systems, while a global α -nucleus optical potential from Ref. [30] was employed for the $\alpha + ^{36}\text{Ar}$ interaction. The p - α elementary cross section is also obtained using the optical potential by Dirac phenomenology [29], consistently with the optical potentials for the distorted waves. We also confirmed that direct use of the elastic-scattering data at 85 MeV [31] and 350 MeV [32] for the 101.5 MeV and 392 MeV cases, respectively, makes little difference in the extracted S_{FAC} . Using these optical potentials and p - α cross section, the TDXs as a function of proton energy were calculated.

The calculations were performed by sampling the scattering angles within the experimental angular acceptance and taking their weighted average to reproduce the actual acceptance of the spectrometer. This treatment explicitly accounts for the finite angular acceptance, which leads to a slight broadening of the calculated energy distribution.

As discussed in Eqs. (3.52)–(3.57) of Ref. [19] and also in other DWIA references therein, TDX is essentially proportional to the absolute square of the distorted momentum distribution of the α amplitude. The pure momentum distribution, which is the Fourier transform of the α amplitude in the coordinate space, is relevant to the TDX once the plane-wave impulse approximation (PWIA) is adopted. Therefore, the reproduction of the data in Fig. 7 shows that the product of the α amplitude and three distorted waves and thus the distorted momentum distribution are described properly. To quantitatively evaluate the effects of the distortion, PWIA calculations were also performed and discussed in the following analysis.

To quantify the impact of refraction and absorption, the PWIA-to-DWIA ratio is defined as

$$R_{\text{PWIA/DWIA}} \equiv \text{PWIA/DWIA}. \quad (6)$$

For the present systems, the obtained values are $R_{\text{PWIA/DWIA}} = 57.3$ at 101.5 MeV and $R_{\text{PWIA/DWIA}} = 18.1$ at 392 MeV. This result indicates that the PWIA significantly overestimates the absolute cross sections by one to two orders of magnitude compared with the DWIA. Such large PWIA-to-DWIA ratios are not specific to the $(p, p\alpha)$ reaction; e.g. a typical value of $R_{\text{PWIA/DWIA}} \approx 25$ has been reported for the $^{208}\text{Pb}(p, 2p)$ reaction at 200 MeV [33]. The pronounced energy dependence of $R_{\text{PWIA/DWIA}}$ demonstrates that the absorption effect becomes weaker at higher incident energies. Specifically, when the energy increases from 101.5 MeV to 392 MeV, the absorption is reduced by approximately 68% ($1 - 18.1/57.3 \approx 0.68$). This trend is consistent with the general understanding that the distorting potentials become less absorptive as the beam energy increases. Therefore, when comparing the absolute TDX values across different incident energies, it is necessary to take into account this energy-dependent absorption effect in addition to the dependence on the CM scattering angle.

4.5. Experimental spectroscopic factors of α clusters in the Woods–Saxon model

The experimental spectroscopic factor of α clusters based on the Woods–Saxon model, denoted as $S_{\text{FAC}}^{\text{WS}}$, was extracted by comparing the TDX calculated using DWIA, TDX_{calc} , with the experimentally measured value, TDX_{exp} . It is defined as

$$S_{\text{FAC}}^{\text{WS}} = \frac{\text{TDX}_{\text{exp}}}{\text{TDX}_{\text{calc}}}. \quad (7)$$

Because the shapes of the proton-energy (T_p) distributions for TDX_{exp} and TDX_{calc} are not identical, $S_{\text{FAC}}^{\text{WS}}$ was determined by minimizing the chi-squared difference between the two spectra, as shown in Fig. 7. The solid line in the figure represents the calculated TDX_{calc} corresponding to the minimum point-wise χ^2 , while the shaded band indicates the uncertainty range associated with $\Delta\chi^2 = 1$, corresponding to the 1σ confidence interval. The extracted values of the experimental spectroscopic factor are summarized in Table 3. Remarkably, despite the large difference in incident energies and experimental conditions, the extracted experimental spectroscopic factors at 101.5 MeV and 392 MeV are consistent within uncertainties. This agreement demonstrates that the present high-energy measurement reproduces the same underlying reaction mechanism as the well established 101.5 MeV experiment, thereby confirming the reliability of $(p, p\alpha)$ studies in the several-hundred-MeV region. We therefore conclude that the $(p, p\alpha)$ measurement at 392 MeV has been successfully validated. This achievement paves the way for systematic studies under a broader range of kinematic conditions than those accessible around 100 MeV, allowing detailed exploration of the intrinsic momentum distribution of α clusters and providing new insight into their density distributions near the nuclear surface.

Table 3. Comparison of PWIA and DWIA calculations under recoilless kinematics. PWIA TDX_{calc} and DWIA TDX_{calc} are computed with the α -cluster wave function normalized to unity. The input p - α differential cross sections (DX) are taken from experimental data at 85 MeV [31] (for the 101.5 MeV case) and 350 MeV [32] (for the 392 MeV case). The quoted values correspond to the recoilless condition at a CM scattering angle of 85° (for 101.5 MeV) and 60° (for 392 MeV). Calculations were performed using PIKOE [25]. The extracted experimental spectroscopic factors $S_{\text{FAC}}^{\text{WS}}$ from $^{40}\text{Ca}(p, p\alpha)$ are also listed. Uncertainties combine statistical and fitting (stat.&fit.) and systematic (syst.) contributions.

	101.5 MeV	392 MeV
p - α DX_{exp} (mb/sr)	2.31	0.0931
PWIA TDX_{calc} ($\mu\text{b}/(\text{MeV}\cdot\text{sr}^2)$)	257.9	47.1
DWIA TDX_{calc} ($\mu\text{b}/(\text{MeV}\cdot\text{sr}^2)$)	4.5	2.6
$R_{\text{PWIA/DWIA}}$	57.3	18.1
TDX_{exp} ($\mu\text{b}/(\text{MeV}\cdot\text{sr}^2)$)	~ 2.3	~ 1.3
$S_{\text{FAC}}^{\text{WS}}$ (-)	0.52	0.51
$\Delta_{\text{stat.\&fit.}} S_{\text{FAC}}^{\text{WS}}$ (-)	± 0.11	± 0.05
$\Delta_{\text{syst.}} S_{\text{FAC}}^{\text{WS}}$ (-)	± 0.05	± 0.06

It should be noted, however, that the phenomenological α -cluster wave function obtained using a Woods–Saxon potential tends to overestimate the α amplitude in the nuclear interior (see e.g. Fig. 11 of Ref. [6] and Fig. 1 of Ref. [34]). This overestimation arises because the Woods–Saxon model does not explicitly incorporate the Pauli exclusion principle (antisymmetrization) between the nucleons in the α cluster and those in the core. Since the $(p, p\alpha)$ reaction is strongly peripheral owing to absorption effects, DWIA analyses based on such phenomenological wave functions—including the present study—may systematically overestimate the absolute value of the experimental spectroscopic factor $S_{\text{FAC}}^{\text{WS}}$. To address the effect quantitatively, further theoretical investigation is necessary, on both surface sensitivity of the reaction and the suppression on the α amplitude in the internal region due to the antisymmetrization. Consistency among theoretical predictions on the strength of the suppression should also be settled. See Ref. [35] for e.g. the ^{20}Ne case.

Although microscopic cluster models such as OCM and GCM have qualitatively discussed the α -cluster component in ^{40}Ca (e.g. Ref. [36]), fully microscopic approaches—e.g. AMD or large-scale shell-model calculations—have so far been limited in providing quantitative estimates of the absolute α -spectroscopic factor. Further theoretical developments along these lines would be valuable for a more direct connection between reaction observables and nuclear-structure models.

5. Summary and conclusions

In this study, the $^{40}\text{Ca}(p, p\alpha)^{36}\text{Ar}$ reaction was measured using a 392 MeV proton beam, establishing a robust experimental framework for quasi-free scattering at high energies. Whereas previous experiments performed near 100 MeV [6] provided important insights into α -cluster formation, the present work extends these achievements by realizing kinematic conditions that more ideally satisfy the quasi-free scattering requirement in the several-hundred-MeV region.

The α -separation energy (S_α) spectrum has been reconstructed, which directly corresponds to the excitation spectrum of ^{36}Ar residue, and the transitions to both the ground and excited states were clearly identified. For the ground-state transition, the measured energy distributions of the outgoing proton were obtained. The α -spectroscopic factor extracted by the present

DWIA analysis was consistent with the former high-precision data at 100 MeV [6], across widely different beam energies. This agreement demonstrates that the underlying reaction mechanism is common to both low- and high-energy regimes, thereby confirming the reliability of (p , $p\alpha$) studies in the several-hundred-MeV region.

The achieved energy resolution was sufficient to resolve individual excited states, demonstrating the potential for future state-by-state analyses. Since the energy and momentum distributions of the (p , $p\alpha$) reaction reflect the momentum distribution of the α clusters and thus its spatial distribution, extending measurements to a broader range of scattering angles and kinematic conditions will be crucial for mapping their distribution near the nuclear surface. The results extend the knowledge obtained at ~ 100 MeV to higher energies under more favorable kinematic conditions, establishing a firm experimental foundation for systematic studies of α clustering in both stable and unstable nuclei [37].

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REFERENCES

- [1] K. Yoshida and J. Tanaka, Prog. Theor. Exp. Phys. [ptafl19](#) (2025), doi.org/10.1093/ptep/ptafl19.
- [2] A. A. Cowley, Phys. Rev. C **103**, 034622 (2021).
- [3] B. Gottschalk and S. L. Kannenberg, Phys. Rev. C **2**, 24 (1970).
- [4] P. G. Roos, N. S. Chant, A. A. Cowley, D. A. Goldberg, H. D. Holmgren, and R. Woody, Phys. Rev. C **15**, 69 (1977).
- [5] T. A. Carey, P. G. Roos, N. S. Chant, A. Nadasen, and H. L. Chen, Phys. Rev. C **23**, 576 (1981).
- [6] T. A. Carey, P. G. Roos, N. S. Chant, A. Nadasen, and H. L. Chen, Phys. Rev. C **29**, 1273 (1984).
- [7] A. Nadasen, P. G. Roos, N. S. Chant, C. C. Chang, G. Ciangaru, H. F. Breuer, J. Wesick, and E. Norbeck, Phys. Rev. C **40**, 1130 (1989).
- [8] A. Nadasen, J. Brusoe, J. Farhat, K. A. G. Rao, D. Sisan, J. Williams, P. G. Roos, F. Adimi, T. Gu, M. Khayat, and R. E. Warner, Phys. Rev. C **59**, 760 (1999).
- [9] R. Neveling et al., Phys. Rev. C **77**, 037601 (2008).
- [10] D. Bachelier, J. L. Boyard, T. Hennino, H. D. Holmgren, J. C. Jourdain, P. Radvanyi, P. G. Roos, and M. Roy-Stephan, Nucl. Phys. A **268**, 488 (1976).
- [11] J. Mabiala, A. A. Cowley, S. V. Förtsch, E. Buthelezi, R. Neveling, F. D. Smit, G. F. Steyn, and J. J. Van Zyl, Phys. Rev. C **79**, 054612 (2009).
- [12] T. Yoshimura et al., Nucl. Phys. A **641**, 3 (1998).
- [13] G. Landaud, A. Devaux, P. Delpierre, J. Kahane, R. Sené, J. Yonnet, and R. Anne, Phys. Rev. C **18**, 1776 (1978).
- [14] A. Nadasen, P. G. Roos, N. S. Chant, A. A. Cowley, C. Samanta, and J. Wesick, Phys. Rev. C **23**, 2353 (1981).
- [15] S. Typel, Phys. Rev. C **89**, 064321 (2014).
- [16] T. Uesaka and N. Itagaki, Phil. Trans. R. Soc. A **382**, 20230123 (2024).
- [17] Y. Kubota et al., Nucl. Phys. A **1060**, 123123 (2025).

- [18] J. Tanaka et al., *Science* **371**, 260 (2021).
- [19] T. Wakasa, K. Ogata, and T. Noro, *Prog. Part. Nucl. Phys.* **96**, 32 (2017).
- [20] M. Fujiwara et al., *Nucl. Instrum. Methods Phys. Res. A* **422**, 484 (1999).
- [21] N. Matsuoka, T. Noro, K. Tamura, M. Yoshimura, M. Yosoi, A. Okihana, and T. Yoshimura, *Phys. Lett. B* **359**, 39 (1995).
- [22] T. Miyagawa and J. Tanaka [for the ONOKORO Collaboration], [arXiv:2601.00846](https://arxiv.org/abs/2601.00846), EPJ Web of Conferences (2026) in press.
- [23] V. Bashkurov, *Nucl. Instrum. Methods Phys. Res. A* **433**, 560 (1999).
- [24] J. Tanaka, R. Matsumura, and T. Miyagawa [for the ONOKORO Collaboration], [arXiv:2512.22438](https://arxiv.org/abs/2512.22438), EPJ Web of Conferences (2026) in press.
- [25] K. Ogata, K. Yoshida, and Y. Chazono, *Comput. Phys. Commun.* **297**, 109058 (2024).
- [26] T. Fukui, Y. Taniguchi, T. Suhara, Y. Kanada-En'yo, and K. Ogata, *Phys. Rev. C* **93**, 034606 (2016).
- [27] S. Hama, B. C. Clark, E. D. Cooper, H. S. Sherif, and R. L. Mercer, *Phys. Rev. C* **41**, 2737 (1990).
- [28] E. D. Cooper, S. Hama, B. C. Clark, and R. L. Mercer, *Phys. Rev. C* **47**, 297 (1993).
- [29] E. D. Cooper, S. Hama, and B. C. Clark, *Phys. Rev. C* **80**, 034605 (2009).
- [30] V. Avrigeanu, P. E. Hodgson, and M. Avrigeanu, *Phys. Rev. C* **49**, 2136 (1994).
- [31] L. G. Votta, P. G. Roos, N. S. Chant, and R. Woody, *Phys. Rev. C* **10**, 520 (1974).
- [32] G. A. Moss et al., *Phys. Rev. C* **21**, 1932 (1980).
- [33] A. A. Cowley, *J. Phys. Conf. Ser.* **1555**, 012022 (2020).
- [34] K. Yoshida, Y. Chiba, M. Kimura, Y. Taniguchi, Y. Kanada-En'yo, and K. Ogata, *Phys. Rev. C* **100**, 044601 (2019).
- [35] G. H. Sargsyan, K. Yoshida, K. Ogata, K. D. Launey, J. E. Escher, D. Langr, and T. Dytrych, *Phys. Lett. B* **866**, 139563 (2025).
- [36] T. Sakuda and S. Ohkubo, *Prog. Theor. Phys. Suppl.* **132**, 103 (1998).
- [37] J. Tanaka, M. L. Cortés, H. Liu, and R. Taniuchi, *Prog. Theor. Exp. Phys.* [ptaf153](https://doi.org/10.1093/ptep/ptaf153) (2025), doi.org/10.1093/ptep/ptaf153.