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Spatial exploration and evaluation of rail and long-distance bus network integration with a multimodal node-place model

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Abstract

Improving the integration of rail and long-distance bus services is essential for enhancing regional connectivity and sustainable transport accessibility. Existing node-place models mainly focus on station surroundings and do not consider how buses extend access explicitly to support the transit network. Therefore, this study develops a multimodal network-based approach applied to a case of sub-rural Scotland. Three new integration metrics are designed — travel time-weighted population (demand coverage), feeder bus service availability (supply), and network centrality (regional connectivity). These indicators are then incorporated into a three-dimensional Node-Place framework, which evaluates the integration performance of 102 railway stations across the study area. Results reveal spatial differences in integration performance, identifying well-connected hubs such as Inverness and Stirling, alongside stations like Rosyth and Dunfermline City where demand is not matched by service provision. The analysis also shows opportunities to strengthen east–west regional links and improve multimodal access through targeted interventions, such as co-locating bus termini. By extending the Node-Place

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model to include multimodal catchments and network-level connectivity, the framework captures aspects of integration that are overlooked in rail-only assessments and offers a unified diagnostic tool for identifying where rail-bus integration improvements may have the greatest effect. The method is built on publicly available data, enabling its application in other regions and adaptation to support future demand modelling.

Keywords: Node-place model; Multimodal network; Rail bus integration; Sub-rural area; Long-distance services

1. Introduction

The EU has long advocated multimodal interurban transport to reduce over-reliance on cars, driven by environmental concerns, social inclusion and sustainable mobility. As part of this strategy, the integration of rail and long-distance bus networks is frequently proposed as an effective approach (European Commission, 2011). This integration could provide complementary services by expanding geographic coverage and providing service options.

However, Tyler (2022) reported that the UK still faces several barriers to establishing rail and bus integration as a national policy. Rail and bus services are generally operated independently, making it difficult to coordinate between different entities. The situation is further complicated by the passenger rail franchising system and the deregulation of bus services, which may encourage competition between operators, particularly on routes where bus and rail services overlap. Consequently, progress in improving rail-bus integration has been slower than anticipated and public expectations for such integration remain low (Tyler, 2022). It may become easier in the future, with all rail passenger operations (except open access operators) being returned to government hands and the spread of bus franchising and enhanced partnerships.

Considering these national-level obstacles, more integration progress has been made at the local level in UK, where authorities have greater control. For example, Devon County Council successfully launched the 118 bus service to connect towns with the Okehampton and Exeter rail lines following the reopening of the Dartmoor line (Buses Magazine, 2021). For the long distance service integration, there are additional opportunities. Japan's "B&S Miyazaki" system integrates interurban bus with high-speed rail between

27 Miyazaki and Fukuoka, attracting new users rather than diverting passen-
28 gers from existing services. Yashiro and Kato (2019) analysed the success of
29 this system and highlighted the importance of the demand forecasting model
30 during project planning. Such a model could foster collaboration among
31 stakeholders by reducing profitability uncertainty, as it allows them to esti-
32 mate potential patronage before implementation.

33 In the UK, the Passenger Demand Forecasting Handbook (PDFH) is a key
34 reference that provides guidance on evaluating factors influencing rail pas-
35 senger demand (Worsley, 2012). It employs ‘elasticity values’ to measure
36 how sensitive demand is to changes in these factors. Rail–bus integration
37 in the PDFH is treated as a binary outcome—present or absent—without a
38 method for quantifying integration or their effects on demand. In response,
39 this study develops a network-based framework that evaluates rail–bus inte-
40 gration, enabling quantification in a spatial manner. The framework extends
41 the traditional Node–Place model (Bertolini, 1999) by representing not only
42 the local characteristics of stations but also the wider network connections
43 created by long-distance bus services. The analysis incorporates population
44 indicators and station centrality derived from the multimodal network. This
45 allows the framework to capture additional reach and connectivity that are
46 not visible in rail-only networks or binary assessments such as those adopted
47 in the PDFH. Bringing these elements together becomes a new exploration
48 tool that helps to identify stations where coordination between rail and bus
49 services is weak. The framework therefore offers a practical tool for prioritis-
50 ing stations for intervention and supporting targeted integration strategies.
51 It also provides a foundation for future demand studies, as it captures a
52 broad set of station-related factors that may influence travel behaviour.

53 The remainder of the paper is structured as follows. **Section 2** reviews the
54 relevant literature on interurban rail–bus integration and the Node-Place ap-
55 plication. **Section 3** introduces the case study area in Scotland and the
56 relevant datasets. **Section 4** outlines the methodological framework, detail-
57 ing the construction of the integrated rail–bus network, the delineation of
58 multimodal catchment areas, and the application of an extended Node-Place
59 model. **Section 5** reports the main findings while **Section 6** summarises
60 the conclusions and suggests directions for future research.

61 2. Literature review

62 2.1. Optimisation and evaluation methods in multimodal transport planning

63 Optimisation models are widely adopted to support multimodal transport
64 planning, where they help determine stop locations, route layouts and op-
65 erating frequencies (Shafiq et al., 2025). Specifically, these models are com-
66 monly applied in facility location planning, including the identification of
67 suitable sites for new bus stops or interchanges (Shafiq et al., 2025; Alumur
68 et al., 2012; Mahmoudi et al., 2025a). Multimodal network design models can
69 be applied to decide how bus routes should be designed and how frequently
70 they should operate (Mahmoudi et al., 2025b; Deng et al., 2013). They are
71 designed to improve travel efficiency while keeping costs as low as possible
72 by simultaneously setting multiple objectives (Deng et al., 2013; Mahmoudi
73 et al., 2025b; Shafiq et al., 2025).

74 To solve these optimisation problems, researchers have applied exact meth-
75 ods or metaheuristic algorithms. Exact methods, such as branch-and-bound
76 for mixed-integer programming, can produce exact solutions. However, it
77 becomes less practical as the network grows larger and more complex (Mah-
78 moudi et al., 2025a). In such cases, metaheuristic methods are preferred as
79 they can handle problems involving large numbers of variables, non-linear re-
80 lationships, and multiple objectives. Even so, they cannot guarantee finding
81 the best possible solution. The results may vary depending on the initial val-
82 ues and the specific design of the algorithm (Mahmoudi et al., 2025b; Shafiq
83 et al., 2025). Another challenge is that both approaches require substan-
84 tial computing power and technical expertise (Iliopoulou and Kepaptsoglou,
85 2024; Mahmoudi et al., 2025a).

86 In addition, evaluation-based approaches are widely adopted to examine the
87 outcomes of predefined multimodal transport schemes. Cost–benefit anal-
88 ysis, for instance, is commonly applied (De Rus and Nash, 2007; Johnson
89 and Nash, 2012; Nash, 2015). This approach converts changes such as travel
90 time savings, increased fare revenue and other externalities such as reduc-
91 tions in emissions, into monetary values. It then applies indicators such as
92 net present value or benefit–cost ratio to evaluate whether a proposed scheme
93 can generate a positive return. Cost–benefit analysis is effective in evaluating
94 the economic feasibility of a given proposal. However, it mainly focuses on
95 assessing predefined schemes rather than identifying where integration be-
96 tween modes is weak. Moreover, as it relies mainly on financial measures, it

97 offers limited understanding of the spatial coordination between rail and bus
98 services (Hayashi and Morisugi, 2000).

99 Overall, these optimisation- and evaluation-based methods provide impor-
100 tant insights but may not be suitable for examining multimodal integration
101 from a spatial perspective. Optimisation models require detailed operational
102 inputs and substantial computational effort, which limits their use in prac-
103 tice. Evaluation approaches such as cost–benefit analysis focus mainly on
104 predefined schemes and economic outcomes, offering little information about
105 how different services interact across space. Although many other studies
106 consider accessibility, network-based or equity indicators to assess particular
107 aspects of integration performance (Geurs and Van Wee, 2004; Von Ferber
108 et al., 2009; Zhang et al., 2018; Shafiq et al., 2025), they tend to be ap-
109 plied independently and do not provide an integrated view. In the UK, rail
110 and long-distance bus services are planned and operated by different organ-
111 isations (Preston, 2023). Because large-scale coordination across modes is
112 difficult under this institutional structure, a station-level assessment tool be-
113 comes essential and necessary for identifying where integration is weak, so
114 that local authorities can intervene in a more targeted way.

115 *2.2. Land use–transport coordination from a Node–Place perspective*

116 Node–Place analysis provides a structured framework by bringing transport
117 and land-use factors together within a single spatial framework. This model
118 assesses stations based on two dimensions: the “node” value—representing
119 transport connectivity—and the “place” value—reflecting the intensity and
120 quality of surrounding activities (Bertolini, 1999). A wide range of indica-
121 tors has been adopted to evaluate the node and place dimensions. Su et al.
122 (2022) conducted a review of 76 publications and identified 44 relevant in-
123 dicators covering aspects such as service frequency, population density, and
124 land use diversity. To summarise the performance of each dimension, re-
125 searchers typically standardise and aggregate indicators into composite node
126 and place scores based on the same weights. However, to address potential
127 multicollinearity among indicators, dimensionality reduction techniques such
128 as Principal Component Analysis (Liao and Scheuer, 2022; Zhang et al.,
129 2019) or Correlation Matrix Filtering (Li et al., 2019) have been applied.
130 To reflect the importance of indicators, weighted aggregation methods such
131 as the Fuzzy Analytic Hierarchy Process have also been adopted (Li et al.,
132 2019).

133 As shown in **Figure 1**, the resulting node and place scores allow stations to
134 be placed on a two-axis diagram, enabling classification into different groups
135 (Zhang et al., 2019; Olaru et al., 2019; Vale et al., 2018). Stations that
136 are located within the curved area are considered balanced, meaning that
137 their transport functions and surrounding land use levels are relatively well
138 matched. Some of these balanced stations show high values in both node and
139 place dimensions. They are known as stressed stations and usually serve as
140 major transport hubs. In contrast, stations with low node and place values
141 fall into what is called the dependence zone. These stations are commonly
142 found in areas with limited transport services, where residents are more likely
143 to rely on private cars than public transport (Vale et al., 2018). Stations that
144 are located far outside the curved area are considered unbalanced and may
145 require further investigation between transport provision and local develop-
146 ment.

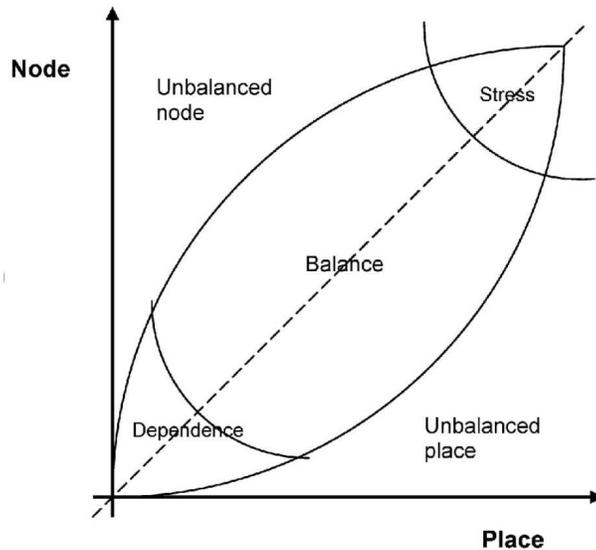


Figure 1: The node-place model (Bertolini, 1999).

147 The Node-Place model has been widely adopted in transit-oriented develop-
148 ment research to help align transport investments with urban development
149 goals (Cao et al., 2020; Caset et al., 2020; Li et al., 2019; Vale et al., 2018). Re-
150 cent studies have expanded the original Node-Place model by incorporating
151 additional dimensions to capture broader aspects of station area functions.

152 One key extension involves the inclusion of accessibility indicators, such as
153 destination accessibility and distance to transit, to better reflect travel op-
154 portunities around stations (Li et al., 2019; Nigro et al., 2019; Cummings and
155 Mahmassani, 2022). Another expansion is the introduction of network struc-
156 ture metrics, including node centrality, betweenness centrality, and closeness
157 centrality, which assess the strategic role of stations within transport net-
158 works (Dou et al., 2021; Liao and Scheuer, 2022; Cao et al., 2020; Zhang
159 et al., 2019). Furthermore, additional dimensions such as urban vibrancy
160 (Yang et al., 2022), morphology (Liao and Scheuer, 2022), and local design
161 attributes (Zhang et al., 2019) have been incorporated in specific studies.
162 These expansions support multi-dimensional evaluation of station areas.

163 Some recent studies have expanded the Node-Place model by adding travel
164 demand as a third dimension. This helps researchers understand how the in-
165 fluence of transport services and land-use features are linked to actual travel
166 behaviour. Statistical methods such as Pearson’s correlation have been ap-
167 plied to analyse the relationship between ridership and Node-Place dimen-
168 sional scores (Liao and Scheuer, 2022; Singh et al., 2017; Yang et al., 2022).
169 Other studies have applied trip-end models to estimate station-level demand
170 based on the Node-Place indicators (Amini Pishro et al., 2022; Caset et al.,
171 2020; Ramos-Santiago, 2021). These further studies show that the Node-
172 Place model not only provides station classification, but also offer insights
173 into how different factors influence passenger flows. This suggests the the
174 node-place model has potential to support both spatial and behavioural eval-
175 uations of multimodal integration.

176 *2.3. Node-Place approach to evaluating rail–bus integration*

177 Most existing studies evaluating rail and bus integration in the Node-Place
178 model focus on the immediate surroundings of railway stations, especially
179 within walking distance. Indicators commonly include the number of nearby
180 bus stops, service frequency, and the distance between these stops and the
181 station (Caset et al., 2020; Olaru et al., 2019; Peng et al., 2023; Su et al.,
182 2022; Vale et al., 2018; Yan et al., 2020; Zhang et al., 2019). Within the
183 Node-Place framework, bus-related measures in the node dimension typi-
184 cally describe how well services connect to the station area, whereas the
185 place dimension is usually represented by the number of activities or the
186 population within a fixed walking distance or time threshold. These mea-
187 sures quantify the degree of local integration around the station and work

188 well in dense urban areas, where bus routes tend to be short, frequent and
189 closely aligned with rail stations.

190 However, this model might not be suitable when applied to rural or lower-
191 density areas, where people need to travel longer distances using different
192 transport modes. Some studies have tried to extend the Node-Place model
193 by going beyond simple walking buffers. Nigro et al. (2019) was among the
194 first to apply this model to small cities and towns, accounting for different
195 access distances by mode, such as 6 km for car, 4.4 km for bus, 2.6 km
196 for cycling, and 1 km for walking. Similarly, Cummings and Mahmassani
197 (2022) used mode-specific isochrones to define catchment areas when mea-
198 suring Node-Place indicators for interurban railway stations. In addition,
199 Nigro et al. (2019) separated the node dimension into two parts, one based
200 on rail connectivity and the other based on access through feeder modes.
201 This distinction helps to identify whether service improvements are needed
202 for the rail network itself or for supporting modes. Although these exten-
203 sions broaden the coverage of possible catchment modes, they still rely on
204 buffer-based assumptions. Since bus services follow corridor-shaped routes
205 rather than circular catchments, buffer-derived populations may not reflect
206 actual service coverage. As Tyler (2020) noted, more than 4.2 million people
207 in Britain live in areas without direct rail access, many of whom could reach
208 a station if suitable bus links were available. Excluding these populations
209 would underestimate station performance within the Node-Place model.

210 At the same time, focusing only on station catchments does not fully cap-
211 ture another important role of bus services in regional and rural contexts. In
212 many such settings, interurban buses play a role beyond feeder services by
213 directly linking towns that are served by rail but lack direct rail connections
214 between them. This is common in the United Kingdom, where interurban
215 bus routes tend to fill the gaps left by historical railway closures, such as
216 those that occurred after the Beeching Cuts (Luke et al., 2018). Reflecting
217 this broader network role, some studies have incorporated network central-
218 ity into the Node-Place model to evaluate how well stations are connected
219 within the rail system (Liao and Scheuer, 2022; Su et al., 2021; Cao et al.,
220 2020; Zhang et al., 2019). However, these approaches are based on rail links
221 alone. A comprehensive evaluation method is needed to consider how buses
222 strengthen and support rail links at the network level.

223 In summary, the above literature review shows that the Node-Place model

224 has been applied to rail–bus integration with a focus only on the immedi-
225 ate surroundings of stations and on rail connectivity alone. These studies
226 rely on walking- or buffer-based catchments, which do not reflect the wider
227 populations that may access stations through interurban buses. Network
228 connectivity is also measured only on the rail network, meaning that the
229 additional links created by bus routes are largely overlooked. In essence,
230 the Node–Place model has not yet been systematically applied within an ex-
231 plicitly defined multimodal network that represents rail and bus services as
232 integrated components of a single system. As a result, the broader role that
233 buses play in shaping regional accessibility is only partly represented, which
234 may lead to an incomplete assessment of station performance. This issue is
235 especially relevant in non-metropolitan areas, where bus services function as
236 essential regional connectors rather than as purely local feeders (Luke et al.,
237 2018; Tyler, 2020).

238 *2.4. Research gap and questions*

239 A fundamental development is needed for a multi-modal network-based Node-
240 Place model that can capture the role of buses within the hierarchy of regional
241 and local transport planning, supporting both exploration and evaluation of
242 rail-bus integration in a systematic manner. To address this fundamental
243 research gap, this study addresses the following research questions:

- 244 1. How can rail and long-distance bus services be represented within a
245 multimodal network for Node–Place analysis?
- 246 2. How is rail–bus integration reflected in the functional roles of stations
247 within the multimodal network, as measured by network centrality?
- 248 3. How can the spatial impact of feeder services be evaluated beyond con-
249 ventional walking catchments, particularly in lower-density and non-
250 metropolitan areas?
- 251 4. How can the Node–Place model provide an integrated assessment of
252 rail–bus integration that captures multimodal network connectivity and
253 feeder-based accessibility?

254 **3. Study area and Data**

255 Long-distance buses are recognised as a cost-effective alternative in regions
256 where low-density travel makes rail services less feasible (Luke et al., 2018).
257 For this reason, Scotland’s eastern regions and the northern Highlands were

258 selected for the case study, as shown in **Figure 2**. These areas are largely
 259 rural and shaped by mountains and coastlines, which limits rail provision and
 260 makes bus expansion a more practical means of improving connectivity (Gov-
 261 ernment, 2023). The institutional separation of rail and bus services in these
 262 regions makes coordination more likely to occur at the local level, which
 263 aligns well with the station or route-focused structure of the Node–Place
 264 model.

265 The selected regions cover around 37,751 square kilometres, which accounts
 266 for 47.06% of Scotland’s total land area. According to the 2011 Census, these
 267 regions have a population of 1,719,930 across 756,432 households. The rail
 268 network includes 102 stations, 14 rail routes, and 1,198 weekday trips, while
 269 the bus network consists of 14,447 stops and approximately 689 routes, sup-
 270 porting 26,893 daily trips. Six key long-distance bus routes connect stations
 271 such as Inverness, Fort William, and Dundee—areas without direct rail links.

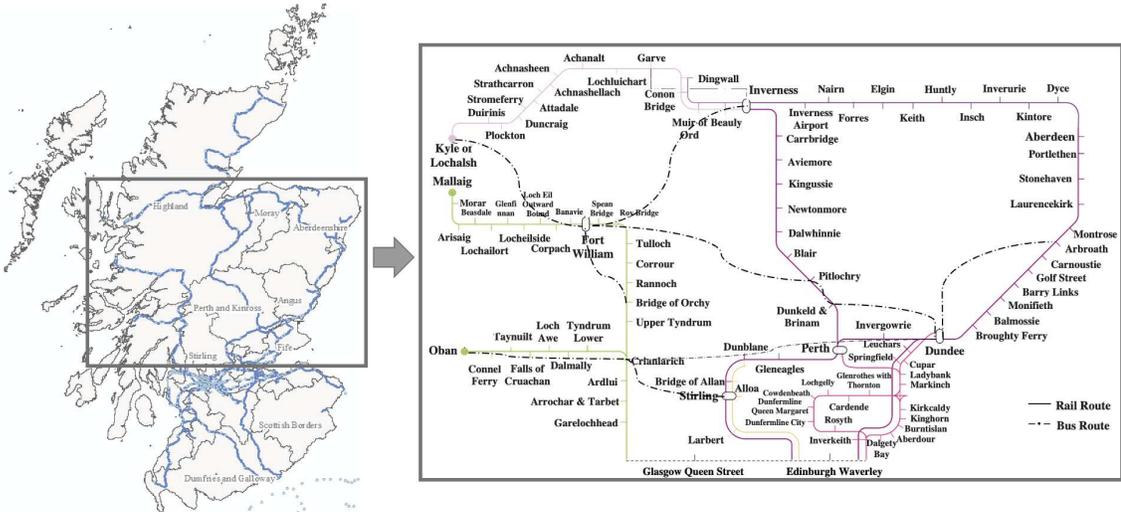


Figure 2: Case study area in Scotland and the rail-bus network.

272 This study captures demographic, spatial, and transport-related characteris-
 273 tics from a range of publicly available datasets. Population and employment
 274 data from the 2011 Census provide the demographic and economic basis
 275 (National Records of Scotland, 2011). Geospatial information—including

276 road networks, car parking locations, and land use—was acquired via Open-
277 StreetMap’s API (OpenStreetMap contributors, 2024). Public transport
278 data, such as rail ¹ and bus schedules, was collected from official transporta-
279 tion websites (Network Rail, 2024; Department for Transport, 2024). To
280 ensure spatial consistency, all datasets were aligned to the defined catchment
281 areas to support the subsequent analysis. For datasets whose original spatial
282 units did not match the catchment boundaries, data values were allocated
283 based on the proportion of spatial overlap.

284 4. Methodology

285 4.1. Constructing a multimodal integrated rail–bus network

286 To quantify rail–bus integration that goes beyond traditional walkable station
287 catchments, this study develops a multimodal network model that regards
288 rail and long-distance bus services as components of a unified transport sys-
289 tem. The model incorporates rail lines, bus routes, and modelled transfer
290 connections. It distinguishes between two primary types of bus–rail integra-
291 tion: direct interurban services that complement rail links between stations,
292 and feeder services that extend access to rail from areas without rail cov-
293 erage (Arup, 2022; Luke et al., 2018). The established multimodal network
294 supports subsequent indicator development as a basis for understanding mul-
295 timodal integration at both station and regional levels.

296 The overall network configuration is illustrated in **Figure 3**. The central
297 panel shows the structure of the Direct Long-Distance Buses (DLD) sub-
298 network across the entire study region. For simplicity, intermediate stops
299 along these bus routes are not included in the DLD network model. Surround-
300 ing the central map, three smaller subfigures show Long-Distance Feeder
301 Services (LFS) integration at the station level, taking Inverness, Oban, and
302 Ladybank as examples. In these diagrams, green lines represent local feeder
303 routes (under 15 miles), while orange lines denote longer-distance feeders (15
304 miles or more), following the threshold defined by the UK Department for
305 Transport (GOV.UK, n.d.).

¹Cross-border rail services such as the Caledonian Sleeper and daytime trains to London were included in the timetable data, and were captured in the indicator of rail routes and rail frequency.

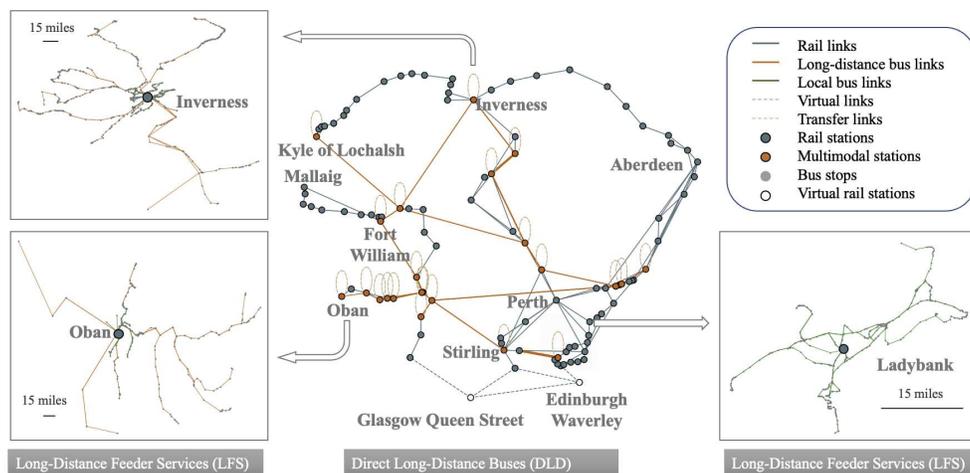


Figure 3: Illustrations of the rail - bus network.

306 *4.2. Multi-criteria analysis framework for evaluating integration*

307 This study adopts a network-based framework of the Node-Place model to
 308 evaluate rail-bus integration. As illustrated in **Figure 4**, the framework
 309 starts from an explicitly defined multimodal network, in which rail and long-
 310 distance bus services are jointly represented. This multimodal network repre-
 311 sentation enables bus services to be incorporated directly into the assessment
 312 of station roles, rather than being considered through simplified catchment
 313 assumptions.

314 Based on the network, three groups of rail-bus integration indicators are
 315 derived, namely network centrality, station accessibility and activity-based.
 316 In particular, network centrality is measured on a multimodal network that
 317 includes both direct bus links and interchange connections, reflecting the role
 318 of bus services in linking stations. Station accessibility is measured through
 319 bus stop counts, bus routes, and service frequency around each station, cap-
 320 turing the intensity of feeder provision. On the activity side, population is
 321 quantified using a travel time-weighted approach, such that demand poten-
 322 tial is expressed as a function of network-based access rather than simple
 323 spatial proximity.

324 These rail-bus integration indicators are then incorporated with conventional
 325 indicators within this three-dimensional Node-Place structure. Building on

326 the conceptual extension proposed by Nigro et al. (2019), the traditional
327 node dimension is disaggregated into Station Accessibility(SA) and Network
328 Accessibility (NA), allowing local access conditions and wider network roles
329 to be evaluated separately alongside the Activity Index (AI). By integrating
330 these network- and feeder-based indicators within the Node-Place framework,
331 the analysis moves beyond isolated measures to provide an integrated and
332 diagnostic assessment of rail-bus integration.

333 All network construction and indicator calculations are based on publicly
334 available open data sources, as summarised on the right-hand side of **Figure**
335 **4**. Details of the indicator calculation process are provided in **Section 4.4**.

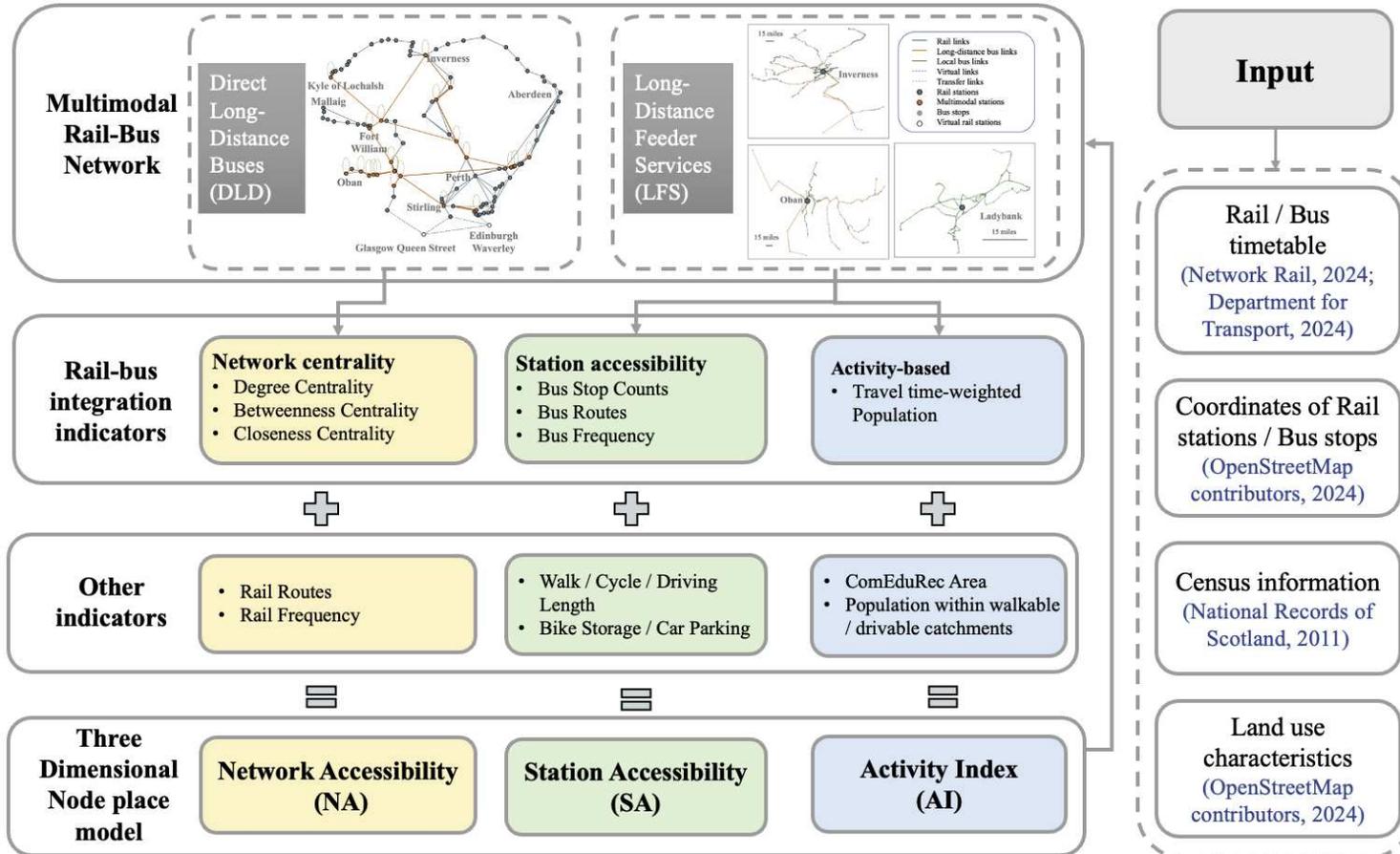


Figure 4: Multi-criteria analysis framework

336 *4.3. Defining multimodal catchment areas for spatial analysis*

337 We define multimodal catchment areas for 102 railway stations in the study
338 area. As shown in **Figure 5**, these catchments represent different ways pas-
339 sengers reach rail services, including a 10-minute driving zone (Type A), a 15-
340 minute walking zone (Type B), and a 7-minute bus-rail transfer zone (Type
341 C) (Ankunda and Venter, 2025; Lauder, 2023; Schakenbos et al., 2016; Ten-
342 nøy et al., 2022). To prevent overlap between walking and driving zones, an
343 additional category (Type D) captures areas accessible by car within 10 min-
344 utes but beyond the 15-minute walking zone. Instead of relying on straight-
345 line buffers, all catchments are computed using network-based travel times,
346 which is more suitable for suburban areas where road layouts and travel times
347 vary significantly (Gao et al., 2022). Besides, this study applies Voronoi di-
348 agrams (Thiessen polygons) to assign each location to its nearest station
349 (Yang et al., 2023). While passengers may not always choose the nearest
350 station due to service quality, this method ensures non-overlapping spatial
coverage for evaluating station-level accessibility and integration.

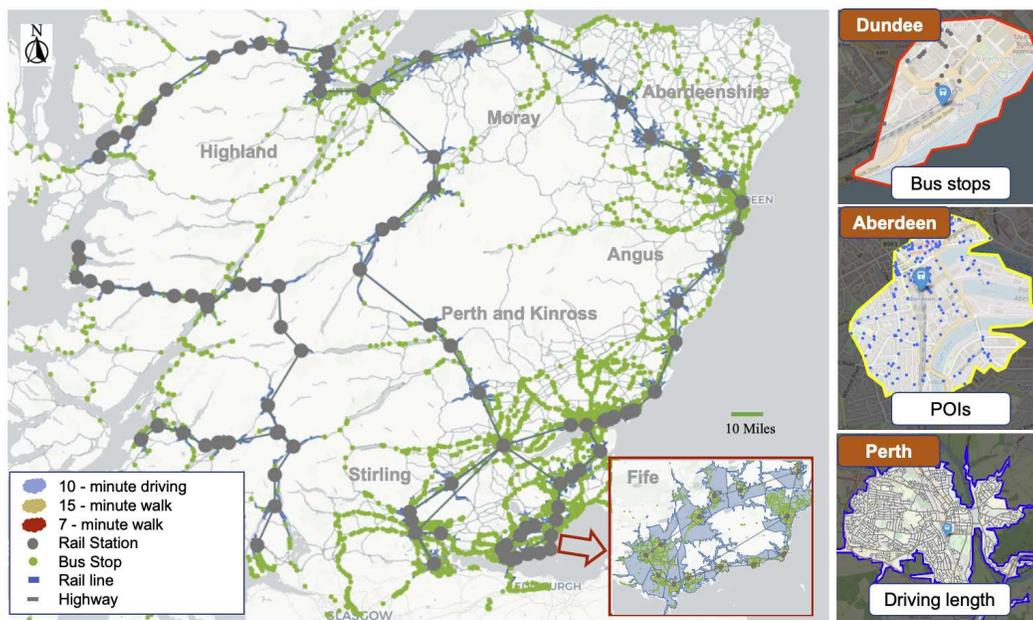


Figure 5: Station-level catchment areas based on network travel times.

352 4.4. Deriving rail-bus integration indicators from the multimodal network
353 Network centrality analysis has been applied in node-place studies to examine
354 the structural role of stations within the rail network (Cao et al., 2020; Dou
355 et al., 2021; Liao and Scheuer, 2022; Zhang et al., 2019). In the present
356 studies, we extend this approach to examine how long-distance bus services
357 reshape connectivity within the multimodal network. Degree, betweenness
358 and closeness centrality are computed by modelling the DLD network as an
359 undirected, weighted L-space graph (Von Ferber et al., 2009), in which nodes
360 represent stations and edges represent direct service links. Edge weights are
361 calculated using the Summed Time Penalty (STP) method, which combines
362 the average scheduled journey time with an equivalent time penalty derived
363 from service intervals (Akbarzadeh et al., 2019). The penalties are based
364 on benchmarks in the PDFH and convert different frequencies into perceived
365 time costs (Worsley, 2012). The benchmarks for non-London interurban flows
366 are adopted for this study area. Full definitions and formulas are provided
367 in **Table 1**.

Table 1: Rail-bus integration indicators.

Indicator	Description	Formula	Weighting
Multimodal network with direct long-distance buses			
Degree Centrality (DC)	The proportion of connections a station has to other stations relative to the maximum possible.	$DC_i = \frac{\sum_m \sum_{j \in S, j \neq i} a_{ij}^m}{n-1}$	Inverse of STP
Betweenness Centrality (BC)	The proportion that a station appears on the shortest paths between all pairs of stations in the network.	$BC_i = \sum_{s \neq j \neq i \in S} \frac{\delta_{sj}(i)}{\delta_{sj}}$	STP
Closeness Centrality (CC)	The reciprocal of the sum of shortest-path travel times from a given station to all other stations in the network.	$CC_i = \frac{1}{\sum_{j \in S, j \neq i} d(i,j)}$	STP
Multimodal network with long-distance feeder services			
Bus Stop Counts (BSC)	The number of bus stops within the catchment area.	$BSC_i = B_i $	/
Bus Routes (BR)	The number of bus routes passing through the catchment area	$BR_i = \sum_{b \in B_i} br_b$	/
Bus Frequency (BF)	The number of buses departing from catchment area per day.	$BF_i = \sum_{b \in B_i} bf_b$	/

Indicator	Description	Formula	Weighting
Travel time-weighted Population (TTWP)	The total population within bus stop catchment areas along feeder routes, weighted by a travel time decay function.	$TTWP_i = \sum_{b \in B_i} \sum_{f \in FBR_b} \sum_{t \in T_{fi}} P_f \cdot e^{-\alpha t}$	Exponential decay
<p>Notation:</p> <p>S = set of all stations in the network; n = total number of stations; a_{ij}^m = adjacency indicator between station i and j under mode m (1 if a link exists, 0 otherwise); δ_{sj} = total number of shortest paths between nodes s and j; $\delta_{sj}(i)$ = number of shortest paths between nodes s and j that pass through node i; $d(i, j)$ = shortest-path travel time between station i and j; B_i = set of bus stops within the feeder catchment (Type C) of station i; br_b = unique feeder routes serving bus stop b; bf_b = scheduled daily frequency of bus stop b; FBR_b = feeder bus routes of bus stop b; f = bus stop f along the feeder bus routes; T_{fi} = set of travel times from bus stop f to station i (measured in minutes); P_f = the population located within the catchment area of bus stop f; α = decay parameter in exponential function, set to 0.01 based on Beria et al. (2017); STP=Summed Time Penalty, calculated by combining scheduled travel time and the equivalent time penalty derived from service frequency.</p>			

368 To evaluate the effectiveness of LFS integration, this study focuses on two
369 key dimensions: service availability and the travel time-weighted population.
370 These are chosen to capture both the supply side (the presence and intensity
371 of bus services) and the demand side (the potential level of usage based on
372 residential population distribution).

373 Key indicators in service availability include: (1) the number of bus stops
374 within the station’s walking catchment area (Type C), (2) the number of
375 feeder routes serving these stops, and (3) the scheduled daily frequency of
376 those routes. These indicators are commonly adopted in the literature to
377 assess bus service provision around railway stations (Guerra et al., 2012;
378 Cardozo et al., 2012; Gutiérrez et al., 2011). In terms of the demand side,
379 the travel time-weighted population estimates the potential reach of each
380 feeder service by aggregating the populations within the catchment areas
381 (Type C) of all bus stops along the routes. This estimate is adjusted using
382 an exponential distance–decay function to reflect the declining likelihood of
383 reaching the railway station as travel time increases (Beria et al., 2017). The

384 decay parameter is set to 0.01, consistent with the value suggested in the same
 385 study. To test the sensitivity of the decay parameter, we compare Activity
 386 Index scores calculated using four values (0.1, 0.01, 0.03 and 0.005) through
 387 a one-way ANOVA. The results show no statistically significant differences
 388 in Activity Index scores ($F = 0.35$, $p = 0.79$), indicating that variations in
 389 the decay parameter do not meaningfully affect the results.

390 4.5. Node-Place based evaluation of multimodal integration

391 The rail-bus integration indicators are incorporated into an extended Node-
 392 Place model to assess each station’s role by examining transport provision in
 393 relation to surrounding economic and social activities. The other indicators
 394 included in the model are widely adopted in previous node-place studies
 395 (Cao et al., 2020; Vale et al., 2018; Yang et al., 2022; Zhang et al., 2019).
 396 The specific indicators are summarised in **Table 2**, along with descriptive
 397 statistics. All indicator values are further transformed using the $\log(x+1)$
 398 function to reduce skewness and the influence of extreme values (McCune and
 399 Grace, 2002). For illustration purposes, the indicators within each dimension
 400 are combined with equal weights to generate the three dimensional scores,
 401 consistent with common practice in the existing literature (Cummings and
 402 Mahmassani, 2022; Yang et al., 2022). Based on these scores, stations are
 403 grouped using K-means clustering, with the number of clusters selected using
 404 the elbow method (Rousseeuw, 1987).

Table 2: Node place indicators from three dimensions.

Indicators	Type	Description	M \pm SD
Activity Index (AI)			
POIs	B	AI1: The number of points of interest, including landmarks, parks and other significant locations that may attract visitors or residents.	45.08 \pm 67.47
ComEduRec Area	B	AI2: The proportion (in %) of an area dedicated to commercial, educational, and recreational uses to the walkable catchment area.	1.86 \pm 2.84
Population	B/ D/ C/ C	AI3/ AI4: The number of people living within the walkable/ drivable catchment area. AI5/ AI6: The number of travel-time weighted population within bus stop catchment area along local/ long distance bus routes.	2392 \pm 2732/ 5915 \pm 10607/ 110764 \pm 172825/ 34690 \pm 72361

Indicators	Type	Description	M ± SD
Employment	B/ D	AI7/ AI8: The number of people aged 16 to 74 in employment within the walkable/ drivable catchment area.	1163±1351 2871±5190
Station accessibility (SA)			
Walk Length/ Cycle Length/ Driving length	B/ B/ D	SA1/ SA2/ SA3: The total distance of paths (in kilometer) accessible by walking/ cycling/ driving within the defined catchment areas.	50.44±41.43/ 40.16±30.93/ 117.76±119.99
Bike Storage/ Car Parking	B/ B	SA4/ SA5: The number of bike storage/ car parking spaces within the walkable catchment area.	13.70±13.85/ 53.98±94.79
Bus Stop Count	C	SA6: The number of bus stops within the catchment area.	6.63±7.15
Bus Routes	C/ C	SA7/ SA8: The number of local/ long-distance bus routes passing through the catchment area.	8.15±8.66/ 3.88±5.53
Bus Frequency	C/ C	SA9/ SA10: The number of local/ long-distance buses departing from catchment area per day.	61.42±98.20/ 16.02±31.87
Network accessibility (NA)			
Rail Routes	/	NA1: The number of rail routes passing through the railway station.	2.35±0.95
Rail Frequency	/	NA2: The number of trains departing from the railway station per day.	44.36±54.10
Degree centrality	/	NA3/ NA4: The proportion of connections a station has to other stations to the maximum possible connections in the rail-only/ rail-bus network.	0.0524±0.0261/ 0.0617± 0.0349
Betweenness centrality	/	NA5/ NA6: The proportion that a station appears on the shortest paths between all pairs of stations in the rail-only/ rail-bus network.	0.0968±0.1201/ 0.0516±0.0807
Closeness centrality	/	NA7/ NA8: The reciprocal of the sum of shortest-path travel times from a given station to all other stations in the rail-only/ rail-bus network.	0.0966±0.0260/ 0.1676±0.0361
Abbreviations: M: Mean; SD: Standard Deviation; Type: Catchment area types; POIs: Points of interest; B: 15-minute walking; C: 7-minute walking; D: within a 10-minute driving but outside the 15-minute walking radius			

405 The framework relies on several modelling assumptions that should be noted
406 when interpreting the results. The indicators representing activity levels, ac-
407 cessibility and network structure are derived from static datasets, meaning
408 that temporal variations, such as peak and off-peak differences, are not fully
409 captured. The approach also summarises station characteristics using aggre-
410 gated values. Stations with similar dimensional scores may therefore differ
411 in practice, which highlights the need to consider the indicator components
412 when examining individual cases. In addition, the interpretation of balance
413 across the three dimensions depends on the context of application, consistent

414 with the discussion in Nigro et al. (2019). Balance in this study reflects the
415 conditions of the Scottish case area rather than an absolute benchmark. Even
416 so, the structure of the framework remains flexible. Catchment definitions,
417 decay parameters and other indicator settings can be adjusted to different
418 planning needs or data availability, and additional dimensions may be added
419 when required. These features allow the methodology to be adapted for other
420 regions and integrated into broader multimodal planning exercises.

421 **5. Results and discussion**

422 We apply the new multimodal network-based Node-Place framework to the
423 Scottish case study. We first show how the inclusion of bus routes reshapes
424 network connectivity, leading to the emergence of new cross-regional links
425 and changes in the stations that function as key nodes within the network.
426 We then examine spatial variation in feeder provision by comparing travel
427 time-weighted population with service frequency, showing where coordination
428 between demand and service supply is relatively strong and where potential
429 gaps are present.

430 These multimodal indicators are subsequently incorporated into the three-
431 dimensional Node-Place model to assess station performance across activity,
432 local accessibility and wider network roles. Clustering analysis is adopted
433 to identify spatial patterns and functional differences among stations. We
434 further demonstrate how dimensional scores change once feeder-based acces-
435 sibility and multimodal centrality are taken into account, revealing aspects
436 of multimodal integration that are not captured by an ordinary Node-Place
437 model. Finally, we illustrate how the framework can support early-stage
438 planning by exploring the potential effects of co-locating selected bus ter-
439 mini with nearby railway stations.

440 *5.1. Assessment of network centrality in a multimodal network*

441 In many non-metropolitan regions, long-distance buses provide cross-regional
442 links where rail coverage is limited. Comparing centrality values in the rail-
443 only and multimodal networks helps show how additional bus services change
444 the patterns through which stations are connected. These changes may in-
445 clude the appearance of stations acting as new interchange points, shifts
446 in the stations that lie on the main shortest paths, and the emergence of
447 alternative cross-regional connections. To examine these effects, we analyse

448 how degree, closeness and betweenness centrality vary once long-distance bus
449 routes are included in the network.

450 Degree and closeness value tend to increase or remain the same once bus
451 routes are added because the new routes create additional links and shorten
452 travel paths. Betweenness centrality (BC) shows a different pattern. As
453 shown in **Figure 6**, in the rail-only network (A), several stations along the
454 Highland Main Line and the West Highland Line lie on many of the shortest
455 paths. Once bus routes are added, the shortest multimodal paths change.
456 Compared to earlier studies that only applied rail-based networks in Node-
457 Place analysis (Liao and Scheuer, 2022; Caset et al., 2020), our findings show
458 how adding long-distance bus services can shift centrality toward previously
459 less important stations. In the integrated rail–bus network (B), stations such
460 as Fort William, Spean Bridge, and Pitlochry show increased BC values (red
461 circle). This pattern suggests that small-town stations can play a stronger
462 role in supporting regional mobility once they are connected to the wider
463 bus network. For example, Pitlochry becomes a transfer point linking the
464 Highland region with Perth and Dundee, while Fort William gains additional
465 connections between northern and southern areas. At the same time, some
466 railway stations experience a decline in BC, as bus services introduce alter-
467 native routes that bypass them. These shifts reveal that bus integration not
468 only improves access to remote areas but also redistributes network impor-
469 tance.

470 We also compare edge-level betweenness centrality before and after integrat-
471 ing long-distance bus services to examine how the structure of travel paths
472 changes across the network. In the rail-only network (A), high betweenness
473 edges (thicker lines) are largely aligned along north–south corridors, particu-
474 larly those connecting Fort William, Inverness, and Dundee to Glasgow. This
475 reflects the dominant orientation of rail travel in the study area. However,
476 the integrated network (B) introduces greater routing flexibility. Connec-
477 tions such as Spean Bridge–Pitlochry–Perth and Crianlarich–Dundee become
478 thicker, illustrating how bus services enhance cross-regional connectivity and
479 reduce dependence on previous rail corridors. These changes indicate that
480 the integrated network has a more even distribution of the routing pathways.
481 The analysis also indicates areas where integration remains limited. Several
482 northern regions continue to exhibit weak east–west connectivity. Likewise,
483 the east coast corridor remains relatively weak in terms of betweenness values.

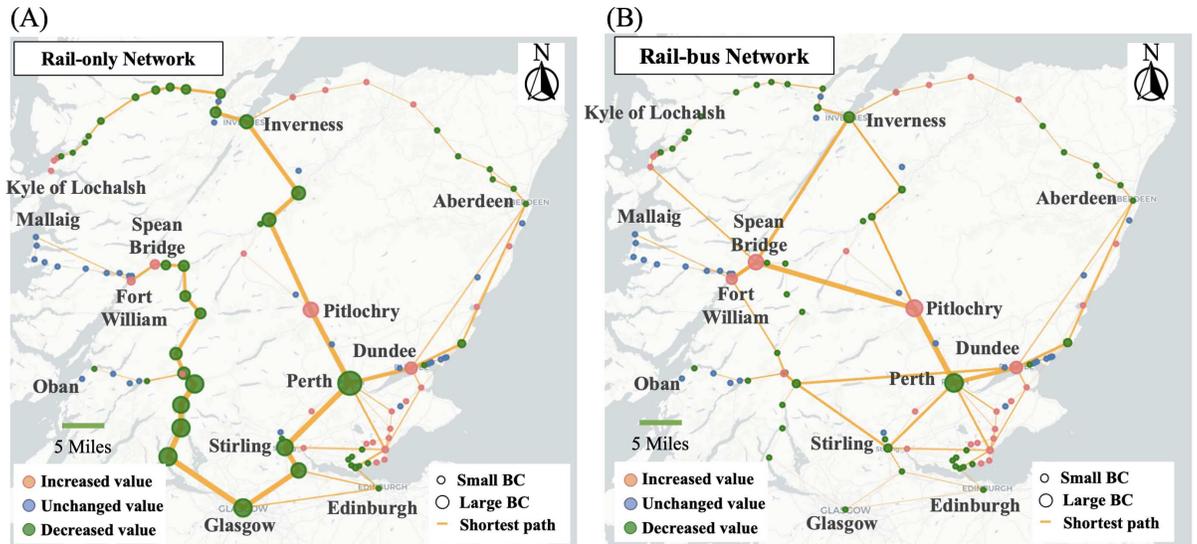


Figure 6: Visualisation of betweenness centrality distribution in the (A) rail-only and (B) rail-bus network.

484 Identifying these gaps help us identify where better coordination between rail
 485 and bus could improve overall connectivity.

486 5.2. Spatial disparities in long-distance feeder service integration

487 In this section, we evaluate the integration between railway stations and
 488 long-distance feeder bus services using two indicators: the frequency of feeder
 489 routes and the population served by these routes, adjusted by a travel time-
 490 decay function. This makes it possible to highlight cases where feeder services
 491 play an important role in supporting station access when the walkable popu-
 492 lation is small. It also helps reveal mismatches between potential demand
 493 and service supply. Such patterns cannot be observed using walking catch-
 494 ments or single-indicator measures alone.

495 **Figure 7(A)** shows clear differences across the study area. Stations such as
 496 Aberdeen, Dundee and Stirling have large multimodal catchments and fre-
 497 quent feeder services (Larger, warm-coloured circles). By contrast, stations
 498 in sparsely populated regions—particularly in the Highlands—tend to ex-
 499 hibit smaller, cooler-coloured circles, reflecting lower service levels and more
 500 limited population coverage. This visualisation helps identify which stations

501 currently act as key integration points, and which ones remain limited in
502 both passenger reach and frequency.

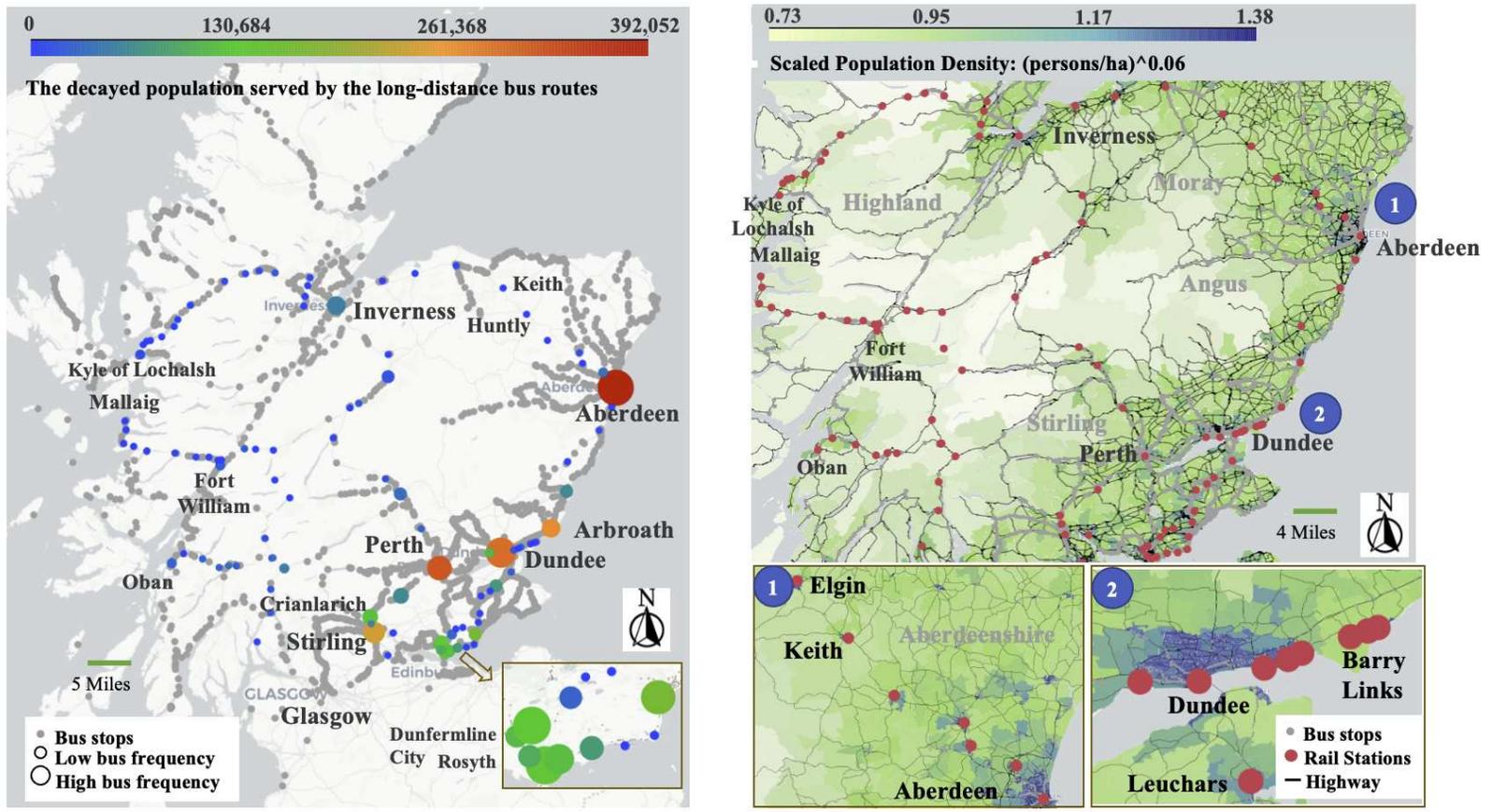


Figure 7: Visualisation of (A) travel time-decayed population served by long-distance feeder buses and their daily frequency at railway stations; (B) population density and transport infrastructure.

503 We provide background information on population density, road infrastruc-
504 ture, and the spatial distribution of feeder bus stops and railway stations in
505 **Figure 7(B)**². This helps explain whether the spatial distribution of services
506 aligns with where people actually live. Some stations, such as Larbert, Mark-
507 inch and Nairn, are close to bus stops that are not served by long-distance
508 services. Others, such as Barry Links, Huntly and Keith, lack nearby stops
509 altogether. Distinguishing between these situations helps identify whether
510 weak integration arises from service design or from spatial disconnection. In
511 some situations, low coordination may reflect the presence of a larger hub
512 nearby, which naturally attracts demand from small stations. For instance,
513 residents near Barry Links may prefer accessing the Dundee station, while
514 those near Huntly and Keith may use the Aberdeen station. Such spatial
515 competition could partially explain the low levels of coordination observed
516 at these locations and indicate the complexity of multimodal planning in
517 overlapping catchment zones.

518 In addition, a comparison between the population served and the frequency
519 of services also indicates several mismatches. For instance, Dunfermline City
520 and Rosyth serve large populations yet receive relatively low feeder frequen-
521 cies. Perth shows a similar imbalance. These disparities show areas where
522 further investigation may be needed to determine whether current service
523 provision adequately meets local demand needs.

524 *5.3. Evaluating station performance applying the three-dimensional Node- 525 Place model*

526 The multimodal indicators are integrated into a three-dimensional Node–Place
527 structure, which enables each station to be assessed across AI, SA and NA.
528 Specifically, AI captures the potential for generating demand, based on sur-
529 rounding population size and the availability of local facilities. SA reflects
530 the ease with which passengers can access the station from nearby areas,
531 while NA indicates the station’s role in supporting longer-distance travel.

532 The three dimensions show a relatively balanced structure, as shown in **Fig-
533 ure 8**. AI and SA are strongly correlated (Pearson coefficient=0.886), in-
534 dicating that areas with higher activity levels also tend to offer better local

²The underlying colour represents scaled population density, calculated using a power transformation (population density^{0.06}) to enhance visual contrast in the figure.

535 access. NA, however, shows a weaker correlation with the other two dimen-
 536 sions. These findings indicate that local demand and local accessibility do
 537 not necessarily correspond to regional connectivity. Similar patterns were
 538 observed by Dou et al. (2021) and Zhang et al. (2019). While these studies
 539 focused mainly on urban contexts, our results suggest that similar relation-
 540 ships also exist in non-urban areas.

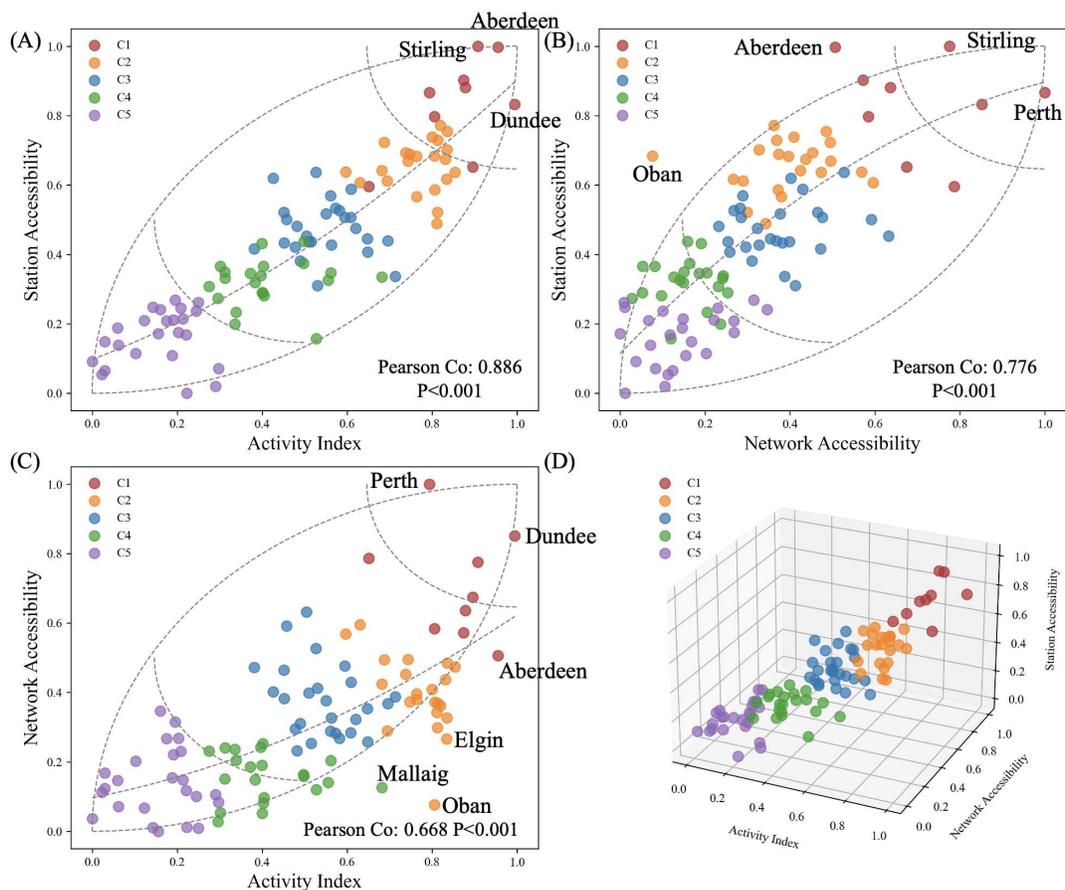


Figure 8: Illustration of the three dimensional node-place indicators.

541 Cluster analysis groups the stations into five categories (**Figure 8**). Cluster
 542 1 ($n = 9$) contains stations that score highly across all three dimensions and

543 are located in or close to the stress zone ³. These stations are mostly found
544 in urban areas and function as major multimodal hubs. Perth, for instance,
545 acts as an important interchange within the rail network, while Inverness
546 supports extensive feeder links to northern settlements including Durness
547 and Kinlochbervie. A special case in Cluster 1 is Pitlochry. Although its
548 scores for SA and AI are low, it is still classified into Cluster 1 because of
549 its high NA score. The station is located along corridors where railways and
550 highways run in parallel, naturally placing them on routes served by both rail
551 and long distance bus services. Similar cases can also be found in Clusters 2
552 and 3, such as Fort William and Spean Bridge.

553 Cluster 2 ($n = 22$) and Cluster 3 ($n = 26$) are mainly located within or close
554 to the balanced zone of the Node-Place model. Stations in Cluster 2 tend to
555 score higher in AI and SA, with several located slightly outside the balanced
556 curve. This suggests that these stations support strong local activity but re-
557 main less integrated within the wider transport network. Many of them are
558 located in Fife and along parts of the East Coast rail corridor, where stations
559 operate on the same railway line and offer similar service frequencies. As a
560 result, their network accessibility values are also similar, largely around 0.4.
561 Some stations in this group, such as Dunfermline City and Dalgety Bay, have
562 AI scores above 0.8. For these locations, improving inter-urban bus connec-
563 tions could help raise their overall network accessibility and meet different
564 types of travel needs. Cluster 3 stations have slightly lower scores across all
565 three dimensions but show a more balanced pattern of development. They
566 are typically located in medium-sized towns or suburban areas.

567 Spatial patterns of the clusters offer further insight (**Figure 9**). Central
568 stations in Cluster 1 tend to be surrounded by stations from Cluster 2 and
569 Cluster 3. These station groups tend to form small radial patterns, similar to
570 those commonly found in urban transport networks (Zhang et al., 2019; Liao
571 and Scheuer, 2022). Such spatial structures are found across different parts
572 of the study area. This pattern suggests that non-urban regions could benefit
573 from encouraging polycentric development, where multiple centres support
574 each other. This idea aligns with Scotland’s National Planning Framework 4,
575 which promotes more balanced regional growth (Scottish Government, 2023).

³The “balanced”, “stress”, and “dependence” zones based on the classification proposed by Bertolini (1999) and were introduced earlier in **Section 2.2**

576 Cluster 4 (n=21) and Cluster 5 (n=24) are close to the dependence zone of
 577 the Node-Place model. These stations are generally located in less developed
 578 areas, often in the Highlands or remote rural regions. They typically have
 579 lower scores across all three dimensions. Their performance is strongly influ-
 580 enced by geographical constraints and sparse settlement patterns, reducing
 both demand and service provision.



Figure 9: Spatial distribution of clustered railway stations based on Node-Place indicators in the case study area.

581
 582 However, spatial balance in the Node-Place model does not necessarily im-
 583 ply effective multimodal integration at the station level. As noted by Nigro
 584 et al. (2019), the balanced curve functions as a diagnostic reference rather
 585 than a normative benchmark. Stations that appear balanced may still per-
 586 form poorly in practice if interchange conditions are weak. This can be seen
 587 in stations such as Keith, Huntly and Barry Links. They fall within the
 588 balanced zone of the Node-Place model, yet **Section 4.2** shows that none
 589 of them have bus stops within seven minutes of walking distance. Besides,
 590 a station that appears balanced in spatial terms may still experience weak
 591 integration due to timetable misalignment, long transfer walking distances,
 592 service unreliability, fare segmentation or capacity constraints (NEA Trans-
 593 port research and training, 2003; Ewhrudjakpor et al., 2019).

594 Conversely, stations located outside the balanced curve are not necessarily
595 problematic. Further analysis is needed to understand the underlying causes.
596 For instance, Aberdeen performs well in terms of local activity and accessi-
597 bility, but its network accessibility is lower. This is mainly due to its strong
598 local bus links within the Aberdeenshire area, where rail accessibility has
599 been reduced by past network closures resulting from the Beeching Cuts.
600 As a result, feeder bus services are mostly concentrated around Aberdeen
601 station. The absence of direct westward highway links limits opportunities
602 for long-distance bus connections to integrate with the Highland Main Line
603 or the West Highland Line, which helps explain its lower NA score. Perth
604 plays an important role in the regional network, yet **Section 4.2** shows
605 that its current feeder services do not match the size of its potential catch-
606 ment population. These examples show how the framework can point out
607 stations where targeted improvements may be possible. Whether such im-
608 provements are feasible would still need to be assessed using further tools
609 such as cost–benefit analysis or geographical feasibility assessment.

610 These station-level patterns also need to be interpreted in light of the wider
611 institutional context in Scotland. While ScotRail operates most internal
612 rail services under public ownership, long-distance buses remain deregulated
613 and are run by private operators (Preston, 2023). This institutional separa-
614 tion makes network-wide coordination challenging, particularly in relation to
615 timetable alignment and fare integration in the whole area (Tyler, 2022). Be-
616 cause national-level integration is difficult to achieve under these conditions,
617 the extended Node–Place framework provides a practical way to identify gaps
618 at the station and route level. Rather than aiming to optimise the entire net-
619 work, the framework shows where improvements in local accessibility, feeder
620 connections or interchange conditions are most needed, and where such in-
621 terventions are likely to have the greater effects.

622 *5.4. Impact of incorporating bus networks on Node–Place scores*

623 To understand how the multimodal indicators change the interpretation of
624 station performance, we examine how they shift the Node–Place dimen-
625 sional scores (**Figure 10**). Overall, the results show statistically significant
626 changes across the dimensions. For the Activity Index (AI), incorporating
627 bus-accessible populations leads to higher scores across most stations, with
628 a significant paired difference ($p < 0.01$) (**Figure 10(A)**). On average, AI
629 scores rise by 0.0284 once bus catchments are included, reflecting the addi-

630 tional passengers that feeder services bring into station catchments.

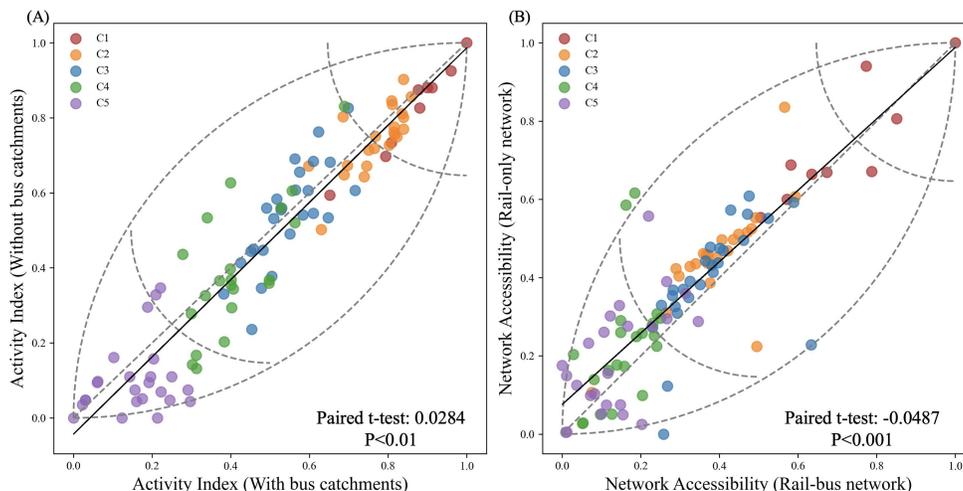


Figure 10: (A) Changes in Activity Index (AI) before and after incorporating bus catchments. (B) Changes in Network Accessibility (NA) between the rail-only and rail-bus networks.

631 We also compare the Network Accessibility (NA) scores in the rail-only net-
632 work and in the rail-bus network (**Figure 10(B)**). Paired t-test shows a
633 significant difference ($p < 0.001$), indicating that adding long distance bus
634 links changes how stations function within the transport network, as we dis-
635 cussed in **Section 5.1**. Some of the stations located to the right of the
636 diagonal line, such as Fort William, Spean Bridge, and Pitlochry, show large
637 increases in NA. These stations are connected by long-distance bus routes,
638 thus improving their connections to more station in the network. While ur-
639 ban stations in Clusters 1 and 2 that are already well connected by rail show
640 limited decline, the change is more substantial for stations in Clusters 4 and
641 5. NA scores based on rail alone may overestimate the network importance
642 of these lower-performing stations. The actual network role could be weaker
643 when bus-based accessibility is accounted.

644 We further examined the share of bus-related indicators to dimensional scores.
645 The share was calculated as the proportion of bus-related indicators, such as
646 the population covered by feeder routes and bus service frequencies, relative
647 to the total value of AI and SA. **Figure 11** shows a clear regional difference.

648 In non-urban areas, the share of bus-related indicators is much higher. This
 649 suggests that feeder services play an important role in increasing the catch-
 650 ment population and improving access to stations. This pattern supports
 651 the idea that bus services are not just an optional service in rural areas. Ac-
 652 cording to Milne and Reid (2022), bus services are essential for maintaining
 653 community life and meeting everyday needs in low-density regions. They
 654 help people without private vehicles, such as older adults, and low-income
 655 groups, to access jobs, services, and social activities. Moseley and Owen
 656 (2008) also found that more than a quarter of bus trips in England (outside
 657 London) occur in towns or rural areas. In **Figure 11**, stations in urban areas
 658 show a relatively small share of bus-related indicators, likely because they
 659 already benefit from dense development and nearby services. As most ear-
 660 lier Node–Place studies were based on urban contexts (Peng et al., 2023; Su
 661 et al., 2022; Vale et al., 2018; Yan et al., 2020; Zhang et al., 2019), excluding
 662 bus-based accessibility may not have had a strong influence on the results.
 663 However, if the same framework is applied to rural stations excluding bus
 664 services, it may misrepresent the Node–Place assessment by underestimating
 both activity levels.

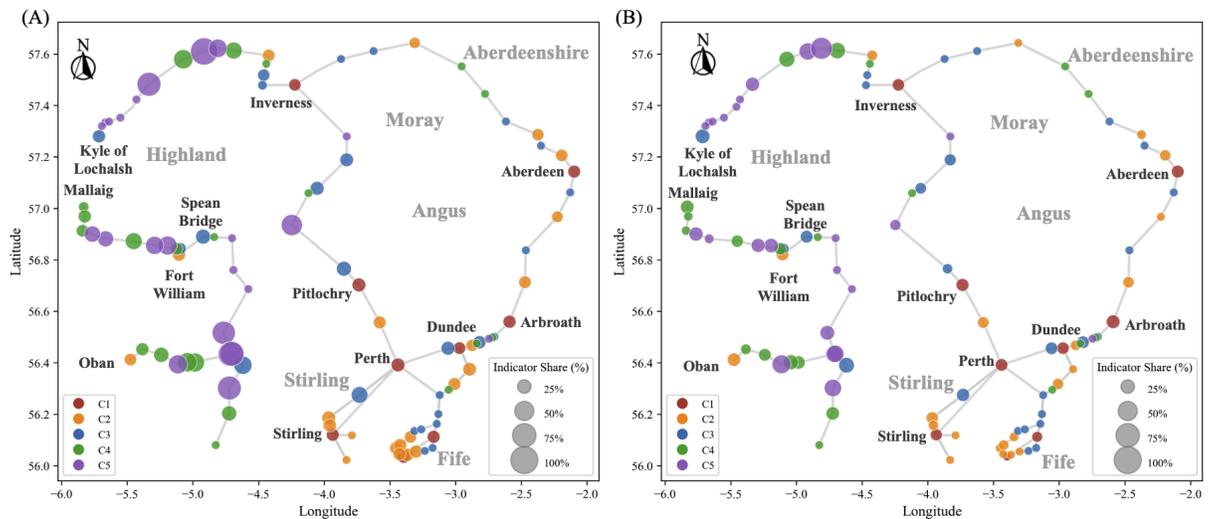


Figure 11: Spatial distribution of indicator shares in Node-Place dimensions. (A) Time-weighted population along bus routes in Activity Index. (B) Bus frequency in Station Accessibility.

665 5.5. *The effects of bus terminus relocation on station integration*

666 To explore the potential benefits of improved spatial integration, we con-
 667 ducted a simulation by estimating how the AI, SA, and NA scores would
 668 change if selected bus termini were relocated to nearby railway stations.
 669 Within the study area, there are 11 major bus termini ⁴. We found that 8
 670 were already within walking distance (Type C), while 3 were located further
 671 away. These include Dunfermline City, Dundee, and Elgin. In the simula-
 672 tion, we assumed these three bus termini were moved to be co-located with
 673 their respective railway stations. Based on this assumption, we reassigned all
 674 bus routes, service frequencies, and population coverage originally associated
 675 with these termini to the new rail-adjacent location. The indicators were
 676 then recalculated using the same method described earlier. The resulting
 677 score changes are illustrated in **Figure 12** with directional arrows.

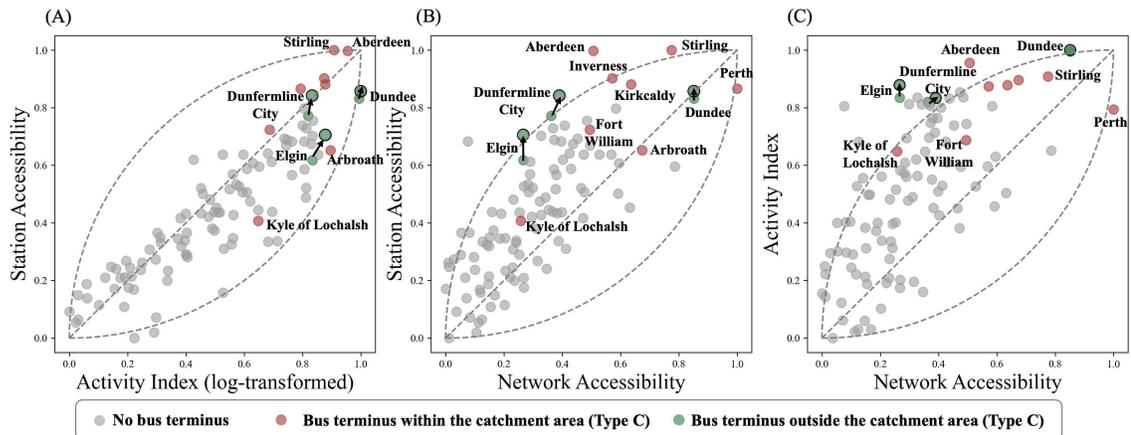


Figure 12: Impact of bus termini relocation on multi-dimensional station performance.

678 Specifically, Dunfermline City contains 14 bus stands, Dundee has 9, and
 679 Elgin has 6. For all three stations considered, relocating the bus termini

⁴Aberdeen, Inverness, Stirling, Kirkcaldy, Dunfermline City, Fort William, Elgin, Arbroath, Kyle of Lochalsh, Perth, Dundee

680 appears to enhance both AI and SA scores. This is because the presence of
681 a nearby bus terminus is expected to increase the number of available bus
682 services, and thereby attracting additional potential passengers. In the case
683 of Dunfermline City, the NA score also improves due to the introduction of
684 a new long-distance bus route (Dunfermline Queen Margaret-Dunfermline
685 City–Alloa), which increases the station’s network centrality.

686 It is also observed that, following the proposed relocation, three stations
687 slightly fall outside the balance curve, moving in the opposite direction to
688 NA. However, this does not imply that the integration strategy is inappropri-
689 ate. Rather, the Node-Place model should be understood as a diagnostic tool
690 for identifying potential mismatches between transport connectivity and sur-
691 rounding activity. The classification of stations as ‘balanced’ or ‘unbalanced’
692 based on the curve is not absolute, but should be interpreted in relation to
693 the specific context and used to guide targeted improvements (Nigro et al.,
694 2019). In the case of Elgin and Dumfermline City, the result may indicate
695 a need to strengthen its network accessibility, such as by introducing new
696 regional connections. Once such improvements are in place, the co-location
697 of rail and bus services could further enhance multimodal connectivity and
698 support more balanced station performance across all three dimensions.

699 **6. Conclusion**

700 In the present study, we propose a new multimodal network-based Node–Place
701 framework that brings rail and long-distance bus networks into a single ana-
702 lytical structure. For the first time, an integrated rail–bus network is intro-
703 duced into a node-place model that explicitly represents long-distance bus
704 links, feeder catchments and interchange connections. By deriving a travel
705 time-weighted population measure and multimodal centrality indicators, the
706 framework enables a more comprehensive evaluation of station activity, ac-
707 cessibility and network roles. It is particularly relevant in non-metropolitan
708 and low-density contexts, where access to rail depends largely on bus ser-
709 vices.

710 The results show that excluding feeder-based accessibility leads to system-
711 atic bias in Node–Place assessments. Comparisons between rail-only and
712 multimodal analyses reveal statistically significant changes in both Activity
713 Index and Network Accessibility once long-distance bus routes and feeder
714 catchments are included. Stations in rural and small-town areas are shown

715 to serve substantially larger populations and to perform different roles within
716 the network than suggested by rail-only analyses. The indicator-share anal-
717 ysis further confirms that bus-related indicators account for a much larger
718 proportion of activity and accessibility dimensional scores in non-urban ar-
719 eas.

720 Beyond these score shifts, the framework reveals several ways in which rail–bus
721 integration shapes station performance and regional connectivity. The multi-
722 modal centrality analysis shows that incorporating long-distance bus services
723 redistributes betweenness and edge-level routing importance across the net-
724 work. This creates new cross-regional paths and strengthens the network
725 roles of several small-town stations that appear less central in rail-only net-
726 works. The feeder integration assessment further highlights spatial disparities
727 in service coordination. Some stations have small walkable populations but
728 rely heavily on feeder services for access. When these multimodal indicators
729 are considered within the new three-dimensional Node–Place structure, the
730 cluster results reveal functional differences across stations. These patterns
731 distinguish major multimodal hubs from stations in remote areas that are
732 constrained by sparse settlement patterns and limited service provision. Im-
733 portantly, the balanced curve should be interpreted as a diagnostic reference
734 rather than the benchmark of successful multimodal integration. Several
735 stations located within the balanced zone still exhibit weak interchange con-
736 ditions, including the absence of nearby bus stops. By contrast, some stations
737 outside the curve reflect geographical or historical constraints rather than in-
738 tegration failures.

739 It should also be noted that the framework can be adapted for different
740 planning priorities or policy targets. For example, the conclusions of this
741 study are based on the defined catchment areas, which can be adjusted to
742 reflect local walking or driving conditions. Decay parameters can also be
743 calibrated using behavioural or empirical data. Because all indicators rely
744 on open data sources, the method can be transferred to other regions where
745 similar datasets are available. This applies not only to rural areas but also
746 to urban settings. In addition, the model supports the visualisation of inte-
747 gration outcomes, which can assist planners in identifying where multimodal
748 improvements may be most effective.

749 This study has several limitations that should be acknowledged. First, all
750 indicators within each Node–Place dimension were assigned equal weights

751 to maintain transparency in indicator construction, consistent with many
752 previous Node–Place studies (Liao and Scheuer, 2022; Yang et al., 2022).
753 Future research could explore alternative weighting schemes based on expert
754 judgement or statistical methods. Second, the analysis focuses on rail–bus
755 integration and does not include other transport modes, such as ferry ser-
756 vices and airport links. These modes form an important part of regional
757 connectivity and may partly explain the relatively strong accessibility scores
758 observed at stations such as Oban and Mallaig. Incorporating these modes
759 in future work would allow a more comprehensive assessment of multimodal
760 accessibility. Future work will also develop a station-level demand model to
761 quantify how rail–bus integration influences rail ridership, providing further
762 evidence to support transport planning and policy decisions.

763 **Declaration of competing interest**

764 There are no conflicts to declare.

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