

## Optimization of the growth of $\text{Sb}_2\text{Te}_3$ by MBE using thermally cracked Sb

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We have performed a materials investigation into the properties of antimony telluride films, grown by molecular beam epitaxy (MBE) as the temperature of an antimony cracking zone was varied. Through x-ray diffraction, magnetotransport studies, and examination using transmission electron microscopy, we find that as the cracker temperature is increased, the formation of defects is suppressed, due to the higher surface mobilities of the smaller antimony molecular species. This work highlights the importance of using a cracker cell and its optimization for the growth of high quality MBE grown films of  $\text{Sb}_2\text{Te}_3$ .

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**Introduction.** Antimony telluride ( $\text{Sb}_2\text{Te}_3$ ) has attracted considerable attention recently as a material system for its topologically insulating properties, principally as part of an alloy [such as  $(\text{Bi}_x\text{Sb}_{1-x})_2\text{Te}_3$ ]. Within such a topological insulator (TI), transport should be dominated by dispersionless, Dirac-like surface states, where  $180^\circ$  backscattering is forbidden by spin-momentum locking [1,2]. In particular, coupling between surfaces and other interesting states of matter, such as magnetic materials or superconductors, is of particular interest to fabricate a new generation of quantum devices (such as novel resistance standards or components within a quantum computer). Additionally, the two-dimensional (2D) nature of the  $\text{Sb}_2\text{Te}_3$  crystal can lead to nonlinear optical properties which are useful for future optoelectronic devices [3–5].

In order to have precise control over these interfaces and the crystal structure of the as-deposited films, molecular beam epitaxy (MBE) has been adopted as the preferred technique for growing high quality films of  $\text{Sb}_2\text{Te}_3$  and its alloys, not only for easily enabling the growth of heterostructures [6,7] but also for the high degree of control over the deposition conditions that can be achieved. This allows the growth of large, uniform, high quality material which can be readily fashioned into interesting devices. However, the quality of MBE grown films of  $\text{Sb}_2\text{Te}_3$  are still not able to match the electrical properties of exfoliated flakes, motivating further optimizations to improve film quality.

A feature of MBE is that the growth is highly sensitive to the substrate conditions. This true even in the case of a material like  $\text{Sb}_2\text{Te}_3$ , which is formed of quintuple layers held together by van der Waals (vdW) forces. The interface

between the substrate and the overlying film can become a nucleation site for defects and dislocations, which can propagate through the lattice [8,9]. While the topologically protected surface states should theoretically be robust against these defects, real topological materials often host topologically trivial, bulk carriers, the number and mobility of which can be modulated by these defects.

It is, therefore, a key challenge to verify the topological properties of the surface states, due to the bulk p-type doping in  $\text{Sb}_2\text{Te}_3$  materials. The most conclusive evidence of topological properties comes from angle-resolved photoemission spectroscopy measurements, where the band structure, and the Dirac cone in particular, can be imaged directly. However, this can only probe filled states below the Fermi level, and hence has difficulty resolving the band structure of p-type materials [10]. Of relevance to applications, magnetotransport studies can reveal the topological character of surface states, but such measurements require samples with extremely high mobility, and thus low defect density. Additionally, topologically trivial residual bulk carriers can obscure topological effects [11,12]. As the electronic properties of a material determine its permittivity, optoelectronic devices are also sensitive to these defects. This is alongside with any effects that reduce the crystalline order or the size of crystalline domains, which can hamper the nonlinear optical properties of these materials [4,13]. As such, improving the quality of  $\text{Sb}_2\text{Te}_3$  is essential to develop topologically insulating and optoelectronic devices from  $\text{Sb}_2\text{Te}_3$ , and to improve the quality of TIs based on it, such as  $(\text{Bi}_x\text{Sb}_{1-x})_2\text{Te}_3$ , where the bulk p-type doping is suppressed by alloying the  $\text{Sb}_2\text{Te}_3$  with n-type  $\text{Bi}_2\text{Te}_3$ . In addition, the interface between  $\text{Sb}_2\text{Te}_3$  and the underlying substrate is itself an interesting topic of study, as conventional Rashba spin split surface states have been identified on the surfaces of thin films [14,15]. In order to probe these states, or utilize them in conventional spintronic devices, sharp, defect free interfaces are required.

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In order to suppress the formation of defects at the substrate-film interface, the mobility of adatoms on the growth surface is a key control parameter within MBE. However, many  $\text{Sb}_2\text{Te}_3$  films and their alloys are grown with the antimony evaporated from a conventional single-filament effusion cell [16–18]. Within such effusion cells, antimony evaporates in a molecular cluster,  $\text{Sb}_4$ , which has a low surface mobility. Within more conventional semiconductors such as GaSb, this low mobility has been linked to the formation of antisite defects and vacancies. If this was to occur within  $\text{Sb}_2\text{Te}_3$ , these defects would act as dopants and result in the topological surface states being obscured. To remedy this, the molecular cluster of antimony can be thermally broken apart in an effusion cell equipped with a cracker zone, with the resulting species ( $\text{Sb}_2$ ,  $\text{Sb}_1$ ) possessing superior surface mobility [19,20]. This is expected to be particularly important in the growth of  $\text{Sb}_2\text{Te}_3$  as the growth will be limited by the sticking coefficient of the antimony species.

Here we report a study of four  $\text{Sb}_2\text{Te}_3$  samples grown using MBE where only the temperature of the Sb cracking zone is varied. We find that there is a substantial improvement in the crystalline quality and electrical mobility when the Sb is cracked down to its atomic form. Transmission electron microscopy (TEM) and selected area electron diffraction (SAED) images show that the films grown with a higher cracker temperature have a lower number of in-plane defects and twinning boundaries. This presents a mechanism by which the properties of  $\text{Sb}_2\text{Te}_3$  and  $(\text{Bi}_x\text{Sb}_{1-x})_2\text{Te}_3$  systems can be optimized.

*Sample preparation and experimental details.*  $\text{Sb}_2\text{Te}_3$  samples were grown on  $\{0001\}$  oriented  $\text{Al}_2\text{O}_3$  substrates by codeposition of evaporated antimony and tellurium from valved cracker sources in a solid-source MBE system, with a base pressure of  $\approx 1 \times 10^{-10}$  mbar. The samples were grown in a two-step process. First, a  $\sim 5$ -nm-thick nucleation layer was deposited at  $170^\circ\text{C}$ . The sample temperature was then raised to the growth temperature of  $225^\circ\text{C}$ , where the rest of the film was grown. Without the nucleation step, adhesion to the substrate was poor, and a uniform film could not be produced. All temperatures were measured with a thermocouple attached to the sample manipulator.

Samples were grown under chalcogenide rich conditions, where the tellurium flux was set to be 20 times that of the antimony flux, as measured by a beam flux monitor close to the sample manipulator. This tellurium-rich environment is essential in order to minimize the formation of chalcogenide vacancies [8]; obtain the correct phase of TI [21]; and ensure that the growth rate is determined solely by the antimony flux [22]. This Sb/Te ratio is maintained by choosing an Sb flux, and then tuning the temperature of the Te reservoir, and the position of the needle valve on the Te cell, to achieve the desired ratio. The temperature of the tellurium cracker zone was held  $200^\circ\text{C}$  above the tellurium reservoir, resulting in cracker zone temperatures between  $550$  and  $580^\circ\text{C}$ . Different samples were then produced by tuning the temperature of the cracker zone on the antimony cell between  $700$  and  $900^\circ\text{C}$ , while maintaining a constant antimony flux. Finally, the samples were cooled under a tellurium flux at  $3^\circ\text{C}/\text{min}$  in order to maintain the surface quality.

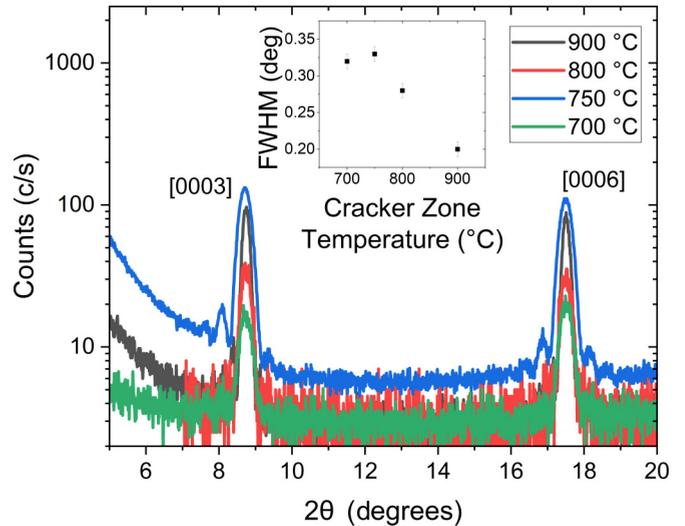


FIG. 1. XRD characterization of the  $\text{Sb}_2\text{Te}_3$  samples. All samples show the expected  $R\bar{3}M$  crystal structure, with the  $c$  axis parallel to the growth direction. Known diffraction peaks are labeled by the relevant Miller indices. The inset shows the variation of the FWHM of the  $[0006]$  peak as a function of Sb cracker temperature.

The crystallographic properties of  $\text{Sb}_2\text{Te}_3$  samples were analyzed by x-ray diffraction (XRD), using  $\text{Cu } K_\alpha$  radiation, before being diced for fabrication. The samples were patterned into Hall bars using optical lithography and chemical wet etching, before Cr/Au ohmic contacts were deposited by thermal evaporation. Transverse and Hall resistances were subsequently recorded by standard lock-in techniques with a source-drain bias current of  $1 \mu\text{A}$  at a frequency of  $119.77 \text{ Hz}$  in a continuous flow He cryostat with a base temperature of  $1.6 \text{ K}$  and an  $8 \text{ T}$  superconducting magnet. TEM analysis was carried out using the FEI Titan Themis Cubed, operated at  $300 \text{ kV}$ . The selected-area electron diffraction patterns were collected using a SAED aperture of projected size  $\approx 180 \text{ nm}$ . Images were collected on the Gatan OneView 16 Megapixel CMOS digital camera.

*Results.* The  $(\omega - 2\theta)$  XRD scans of the  $\text{Sb}_2\text{Te}_3$  samples are shown in Fig. 1. All samples show well ordered  $\{000l\}$  peaks, indicating that the  $c$  axis of the material is ordered parallel to the growth direction with a lattice parameter of  $3.03 \pm 0.02 \text{ nm}$ , being consistent with previously published studies on this material [23,24]. All wafers show Pendellosung fringes around the  $[0003]$  peak, indicating strong ordering along the  $c$  axis. Analysis of these fringes reveal the thickness of all films to be  $21 \pm 3 \text{ nm}$ . When we consider the full width at half maximum (FWHM) of the  $[0006]$  peak, as shown in the inset of Fig. 1, we note that as the cracker temperature is increased, the FWHM of the XRD peaks decreases. This implies that as the Sb is broken down into lighter molecular species, the film becomes more ordered.

This degree of ordering was then probed through measuring the electronic properties. All samples showed sheet resistances that decrease with decreasing temperature, as depicted in Fig. 2(a). Such behavior is indicative of a highly-doped semiconductor, where the transport is limited by the phonon scattering rate at high temperature, rather than the

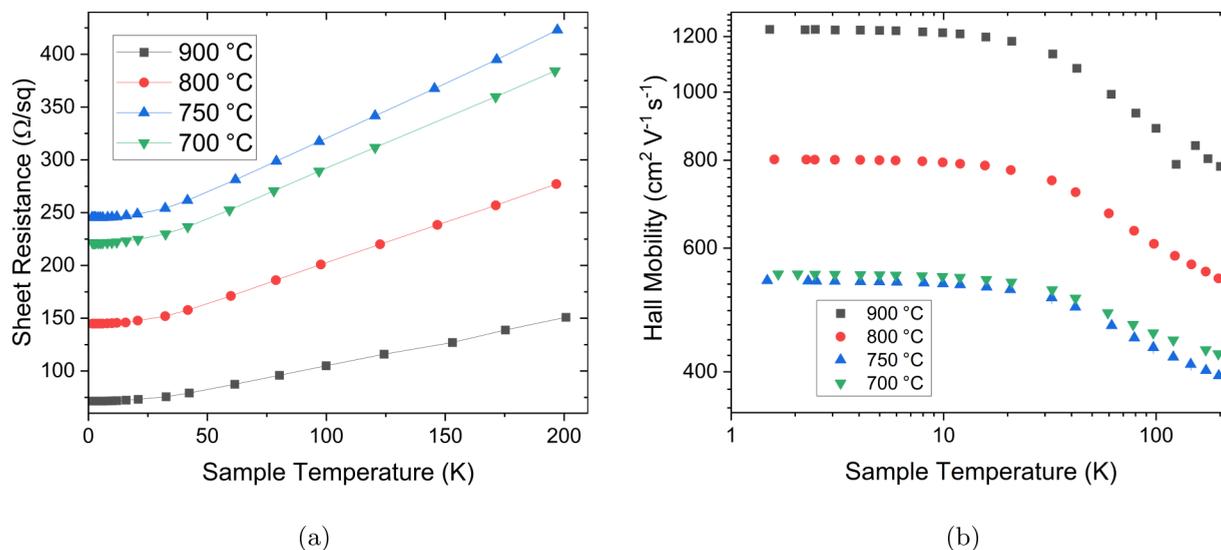


FIG. 2. Temperature-dependent transport properties of the  $\text{Sb}_2\text{Te}_3$  samples. (a) shows the variation in sheet resistance as a function of temperature. (b) shows the effect of temperature on the Hall mobility. Two regimes are apparent for all samples, a low temperature regime  $T < 20 \text{ K}$  where the mobility is temperature independent, and a high temperature regime ( $T > 50 \text{ K}$ ) where the scattering is phonon-mediated.

carrier density. The temperature dependence of the Hall mobility, as shown in Fig. 2(b), also shows scattering typical of a highly doped semiconductor, with the mobility separated into two regimes; a low temperature regime ( $T < 20 \text{ K}$ ), where temperature-independent impurity scattering dominates, and a high temperature regime  $T > 50 \text{ K}$  in which phonon scattering leads to a decrease in mobility with increasing temperature. Across all temperature regimes, the transport through the  $\text{Sb}_2\text{Te}_3$  films is hole-dominated. This is consistent with transport being dominated by the topologically trivial bulk carriers. Previous studies of the band-structure of  $\text{Sb}_2\text{Te}_3$  shows that the Fermi energy is pinned within the bulk valence bands [10]. If the surface states were to dominate the transport we would expect to observe the freeze-out of those bulk carriers at high temperatures, leading to a regime where resistance increases with decreasing temperature, followed by a re-emergence of a regime where the resistance decreases with decreasing temperature as the transport becomes limited by the scattering within the surface states [25,26]. As we do not observe this crossover, we conclude that the surface states make a relatively minor contribution to the overall transport within our samples.

Two additional points emerge from the analysis of this transport data; firstly, the higher the cracker temperature, the lower the defect density within the  $\text{Sb}_2\text{Te}_3$  crystal, as shown by the higher low temperature mobility. Secondly, the phonon-dominated scattering above 50 K results in the mobility showing a power law dependence with temperature,  $\mu \propto T^a$ . Interestingly, the samples with cracker temperatures of 900 °C and 800 °C both show a power law dependence of  $a = -0.17 \pm 0.02$ , whereas the 750 °C and 700 °C samples show power law dependences of  $a = -0.13 \pm 0.01$  and  $a = -0.10 \pm 0.01$ , respectively. As none of these exponents correspond to commonly observed scattering mechanisms [27,28] multiple scattering mechanisms must be present. Fitting the temperature dependence of the sheet resistance to

the Bloch Grüneisen formula [29] reveals a similar Debye temperature of  $185 \pm 5 \text{ K}$  for all samples. This is similar to the bulk Debye temperature of 160 K [30,31], and implies that the behavior of the phonons within these  $\text{Sb}_2\text{Te}_3$  samples is similar. The change in the temperature scaling of the mobility is thus likely to be due to an increased defect density.

All measured samples show weak antilocalization (WAL) at temperatures below 10 K, as shown in the inset of Fig. 3. This behavior can be described by the Bergmann

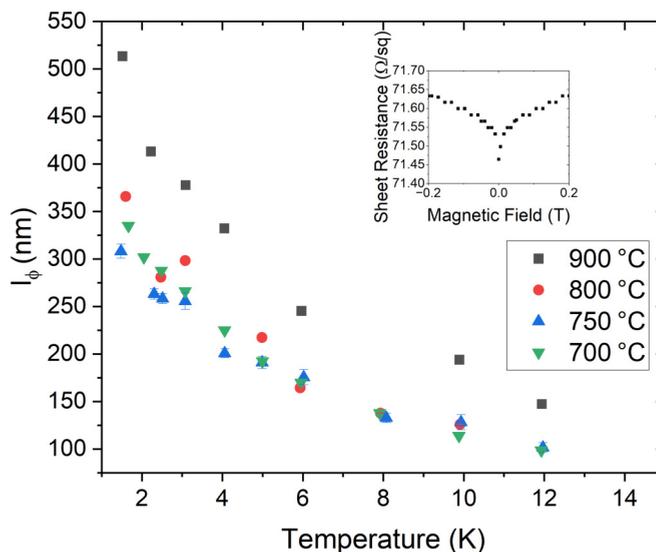


FIG. 3. Temperature variation of the phase-breaking length  $l_\phi$  for the  $\text{Sb}_2\text{Te}_3$  samples. In all samples  $l_\phi$  has a power-law dependence consistent with electron-electron scattering within a 2D Fermi liquid (i.e.  $l_\phi \propto T^{-0.5}$ ). Inset: The WAL response at 1.5 K for the sample grown with a 900 °C cracker temperature.

model (assuming no magnetic scattering) [32]:

$$\Delta\sigma_{xx}(B) = \frac{-e^2}{2\pi^2\hbar} \left[ \left( \Psi \left( \frac{1}{2} + \frac{B_a}{B} \right) \right) - \frac{3}{2} \left( \Psi \left( \frac{1}{2} + \frac{B_b}{B} \right) \right) + \left( \Psi \left( \frac{1}{2} + \frac{1}{2} \frac{B_c}{B} \right) \right) \right]. \quad (1)$$

Here,  $B_a = B_e + B_{so}$ ,  $B_b = B_\phi + \frac{4}{3}B_{so}$ ,  $B_c = B_\phi$ ,  $\Psi$  is the digamma function, and  $\Delta\sigma_{xx}$  is the change in conductivity arising from WAL compared to a classical system.  $B_e$ ,  $B_\phi$ , and  $B_{so}$  are the characteristic fields associated with elastic, inelastic and spin-orbit scattering, respectively, and can be related to their scattering times by  $B_x\tau_x = \frac{\hbar}{4eD}$ , where  $\tau_x$  is the relevant scattering time, and  $D$  is the electronic diffusion coefficient for the material being studied. This scattering time can then be converted into a scattering length;  $l_x = (D\tau_x)^{\frac{1}{2}}$ . It should be noted that  $l_e$  can be estimated from  $\sigma_{xx}(T = T_{\min}, B = 0)$ . As we have shown that the dominant scattering mechanism is temperature-independent impurity scattering within this temperature range,  $l_e$  and thus  $B_e$  can be treated as constant with respect to temperature. As such, the number of fitting parameters can be reduced to two ( $B_\phi$  and  $B_{so}$ ). As expected, all samples show a  $l_{so}$  that is also independent of temperature, with  $l_{so} = 5 \pm 3$  nm,  $20.7 \pm 0.1$  nm,  $12 \pm 1$  nm, and  $33 \pm 1$  nm for the samples grown at cracker temperatures of 900 °C, 800 °C, 750 °C, and 700 °C, respectively.

All samples show  $l_\phi$  (i.e., the scattering length corresponding to inelastic scattering) that scales with a power law of  $T^{-0.55 \pm 0.05}$  (as shown in Fig. 3), consistent with the main phase-breaking mechanism being small energy electron-electron scattering within a 2D Fermi liquid (i.e.,  $l_\phi \propto T^{-0.5}$ ) [33]. Similar responses have been observed in a wide variety of TI systems [34,35], regardless of the level of coupling between bulk and surface states [34] or whether the transport is dominated by bulk or surface conduction [35]. This further reinforces the fact that the main difference between the samples is the increased impurity concentration from samples grown with a lower cracker temperature. Contributions from increased phonon scattering or impurity states would result in a  $T^{-1}$  dependence [33,36,37], whereas a  $T^{-0.25}$  dependence could be indicative of charge puddles within the surface states [36].

In order to understand the microscopic origin of the disorder in the  $Sb_2Te_3$  samples, lamellae were extracted from the as-grown film by focused ion beam milling and measured using TEM. High angle annular dark field (HAADF) images reveal the quintuple layer structure of the  $Sb_2Te_3$  films, as shown in the inset of Fig. 4(a), confirming the  $\{0003l\}$  ordering seen in the XRD. The films were then examined using SAED (Fig. 4). It is important to note that the images show contributions from all three layers within the stack; the sapphire substrate, the  $Sb_2Te_3$  and the amorphous layer used to encapsulate the lamellae. Images taken from only the sapphire and only from the amorphous layer are shown in the insets of Figs. 4(c) and 4(d), respectively.

This analysis reveals two things; first, there is a significant lattice mismatch between the underlying sapphire and the  $Sb_2Te_3$  film (as shown by the differing periodicities in the SAED images), which is expected of a VdW mate-

rial [38]. Secondly, while all the patterns show a similar  $c$  axis periodicity of  $1.0 \pm 0.1$  nm (the thickness of a single  $Sb_2Te_3$  quintuple layer [39]), the diffraction spots are significantly more diffuse for the more disordered samples, particularly away from the central diffraction spots along the  $c$  axis.

Figure 4(d) shows a possible reason for this broadening of the diffraction spots, with doubled  $Sb_2Te_3$  spots (one of which is highlighted with a red circle) becoming visible in the diffraction pattern, indicative of the formation of twinning domains within the crystal structure. A diffracted electron incident on a twinning boundary may be diffracted a second time, resulting in a displacement of the electron and the apparent doubling of diffraction spots within a SAED image [40]. Twinning domains have been observed in other TI films, usually nucleating around dislocation defects at the substrate-TI interface [41,42]. This implies that the defects responsible for the reduced quality of the lower cracker temperature samples arise from an increased density of dislocation defects, resulting in additional scattering sites forming at twin-domain boundaries. These dislocations are likely to be a result of the lower surface mobility of the larger Sb clusters [19,20]. If a cluster of  $Sb_4$  is incident on the surface during growth, one or more atoms in the cluster may not bond to a lattice site, forming a dislocation. If Sb is cracked into its atomic form, this is much less likely to occur, resulting in the suppression of such defects. It is important to note that this is not the case with the Te adatoms, as the substrate temperature is held high enough to re-evaporate any Te that is not well integrated into the lattice [22].

**Conclusions.** We have grown using MBE a series of  $Sb_2Te_3$  samples, where both adatoms were evaporated through valved cracker cells. Through examining the material properties of these materials using XRD, TEM, and selected area electron diffraction, we find that the crystalline order of these materials is substantially enhanced by cracking the antimony down into an elemental form (using a cracker zone temperature of 900 °C), and this enhances the electron mobility and spin orbit coupling strength. This is due to the higher mobility of the antimony adatoms on the growth surface, leading to the suppression of dislocation defects caused by improper integration of Sb clusters into the crystal lattice. As  $Sb_2Te_3$  forms the basis for the bulk-insulating  $(Bi_xSb_{1-x})_2Te_3$  ternary system, these results will help facilitate growth of higher quality material for research into spintronics, Majorana fermions and resistance standards utilizing the Quantum Anomalous Hall effect. Additionally the improved crystallinity of these films will be important to developing optoelectronic devices based on this 2D material.

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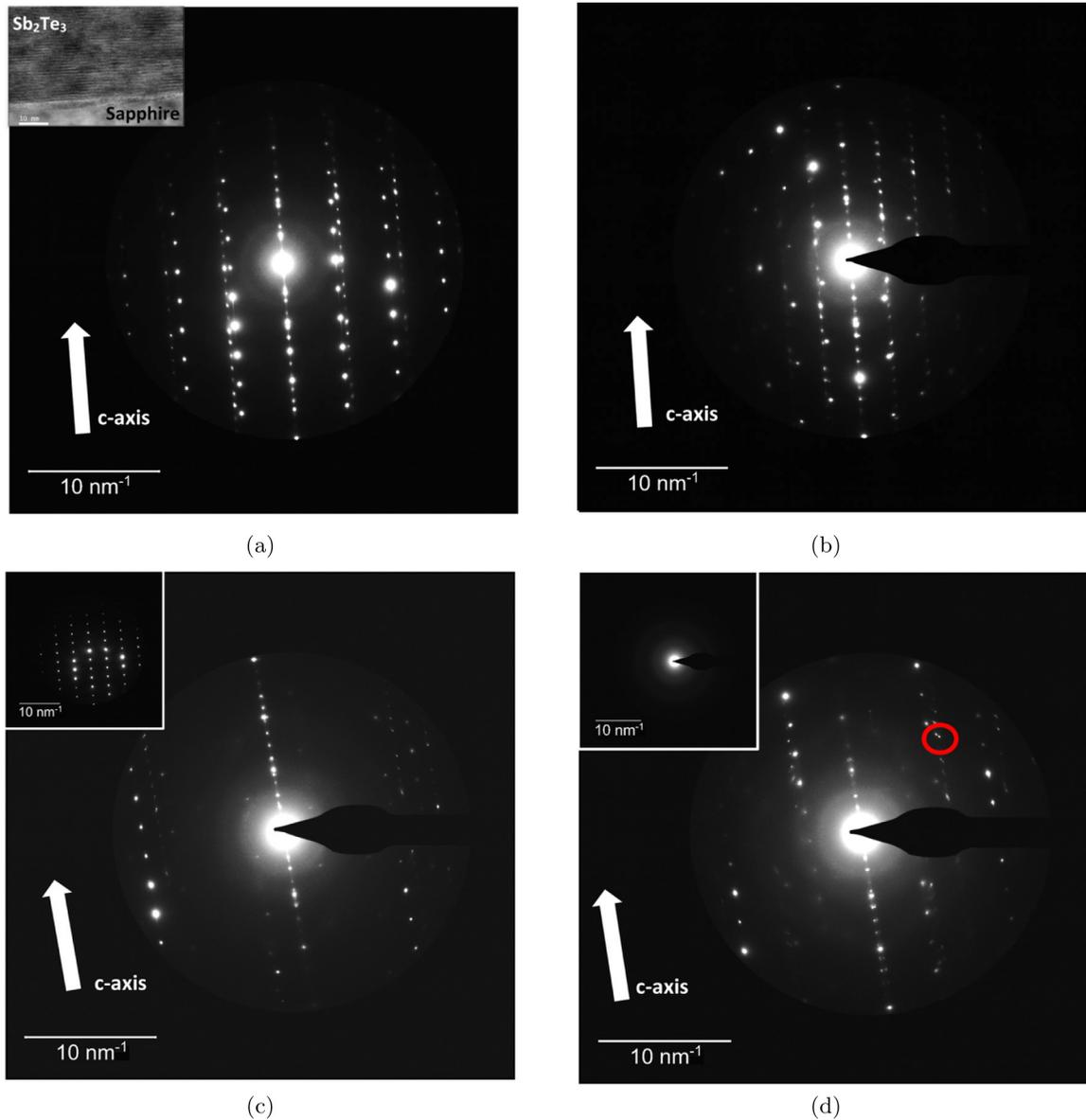


FIG. 4. SAED images of the  $\text{Sb}_2\text{Te}_3$  samples grown with cracker zone temperature of 900 °C (a), 800 °C (b), 750 °C (c), and 700 °C (d). In all images there are two sets of repeating spots: the bright spots from the sapphire substrate, and the weaker spots from the  $\text{Sb}_2\text{Te}_3$  film. The inset of (a) shows a HAADF image of the  $\text{Sb}_2\text{Te}_3$  film, the inset of (c) shows the diffraction pattern from only the sapphire substrate, and the inset of (d) shows the diffraction pattern from only the amorphous layer used to encapsulate the  $\text{Sb}_2\text{Te}_3$  film for FIB milling. All inset images were taken from the wafer grown at a cracker temperature of 900 °C. (b) and (d) show doubled diffraction spots arising from a twinning boundary. One such doubled diffraction spot is highlighted in (d) with a red circle.

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*Data availability.* The data that support the findings of this article are openly available [43], embargo periods may apply.

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