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# 1 Enhancing the impact performance of TaNbHfZr high-

### 2 entropy alloy film by interface strengthening and stress

# **3 dispersion: Microstructure and mechanism**

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- 18 Keywords: High-entropy Alloy Film; TaNbHfZr; Sandwich-structure; Nano-
- 19 impact; Microstructure; Mechanism

# 20 Abstract

The sandwich-structured TaNbHfZr refractory high-entropy alloy film (RHEAF) was fabricated by magnetron sputtering. Nano-impact was utilized to extract the local mechanical response of the film with severe localized strain due to the high instantaneous strain rate (*ISR*). Analysis on dynamic hardness ( $H_D$ ) and toughness of TaNbHfZr film was carried out quantitatively. The plasticity absorption ability in nano-impact is higher indicated by the increased plastic work ( $W_P$ ) with increasing acceleration

force (AF). The decreased  $H_{\rm D}$  is attributed to the contribution of the energy 1 to the fracture at higher AF. Through TEM observation, the dynamic 2 response is confirmed by thickness reduction in nano-impact. Cracks 3 occur where the stress reaches its maximum in the middle layer, near the 4 boundary, serving as the primary energy-storage middle-bottom 5 mechanism in the sandwich-structured TaNbHfZr film. Furthermore, the 6 rate-controlling response can be attributed to the dislocation motion at 7 varing loading rates. This phenomenon is confirmed by FEM simulation. 8 Here, the equiaxed grains within the middle layer mitigate further 9 catastrophic damage by absorbing the localized and concentrated stress 10 through rotation or grain boundary sliding. Consequently, the film was 11 strengthened and stabilized due to the effective stress dispersion and 12 existence of interface in the sandwich structure. 13

#### 14 **1 Introduction**

High-entropy alloys (HEAs), as a fundamentally new alloying concept, has 15 been firstly proposed by Yeh et al. [1] in 2004. HEAs have high 16 configurational entropies at a random state ( $\geq 1.5R$ , R is the ideal gas 17 constant), which can stabilize the simple crystal structure by forming solid 18 19 solutions such as fcc (face-centered cubic) and bcc (body-centered cubic) solid-solution structures, rather than complex intermetallic phases [2]. The 20 high-entropy and severe lattice distortion effects lead to a rugged energy 21 landscape which increases the resistance to dislocation motion and 22 pronounced solid solution strengthening for HEAs [3, 4]. Compared with 23 traditional refractory metals and alloys, HEAs pave a new way for an 24 excellent combination of superior functional properties, which have great 25 potential for practical applications. HEAs composed of high melting-point 26 elements such as Cr, Hf, Mo, Nb, Ta, W, Zr etc. named refractory high-27 entropy alloys (RHEAs), exhibiting outstanding strength and exceptional 28 oxidation resistance [5, 6]. The reported RHEAs with bcc structure such as 29

1 WNbMoTa, WNbMoTaV [5], Hf<sub>25</sub>Nb<sub>25</sub>Ti<sub>25</sub>Zr<sub>25</sub> [7], HfMo<sub>x</sub>NbTaTiZr [8] 2 possess superior mechanical performance. Feng *et al.* [9] have prepared 3 NbMoTaW films via magnetron sputtering and reported its superior 4 nanoindentation hardness (~16 GPa) due to the source strengthening and 5 solid solution hardening mechanisms using a thermally activated 6 dislocation model.

The mechanism of plastic deformation is usually recognized to be rate-7 dependent. Definitely speaking, quasi-static and dynamic high strain rate 8 conditions fall into the strain rate range of  $10^{-5} \sim 10^{-1}$  s<sup>-1</sup> and  $>5 \times 10^{1}$  s<sup>-1</sup>, 9 respectively [10]. The dynamic performance of the HEAFs is often 10 involved in practical applications such as high-speed transportation 11 vehicles and hydraulic machinery etc. [11]. Nano-impact makes it possible 12 to quantify energy absorption of a material surface in nano-/micro-scale 13 and provides valuable highly localized information about deformation 14 acting as an effective measurement of impact energy to determine the 15 16 fracture resistance [12].

As evidenced by Gray and Hirsch et al. [13, 14], the dislocation structures 17 are substantially different between low strain rate and high strain rate via 18 TEM (transmission electron microscopy) micrographs. The rate-19 dependence for bcc metals suggests that the deformation occurs via 20 thermally activated kink-pair nucleation which is a typical screw dislocation 21 propagation mechanism [15]. Twining and shear bands related 22 deformation mechanisms are proposed at lower strain rates and softening 23 24 even occurs at higher strain rates. Nemat-Nasser et al. [16] reported that phenomena like shear bands, dynamic recovery, dislocation lines, 25 dislocation forests and deformation dislocation loops arise in the dynamic 26 deformation with strain rate  $>5 \times 10^4$  s<sup>-1</sup> for bcc Ta, as well as slip of the 27 perfect screw dislocations on {110}-type primary planes as the dominant 28 29 deformation mechanism, which are confirmed via TEM analysis. The yield

strength of as-cast TiHfZrTaNb HEA at the initial strain rates ~3.4×10<sup>3</sup> s<sup>-1</sup> 1 with localized in macroscopic shear bands was about ~40 % higher than 2 that measured at  $\sim 10^{-3}$  s<sup>-1</sup> with evenly distributed shear bands by 3 compression due to the increase of the dislocation density [17]. The 4 dynamic fracture often emerges as one type of the phenomena during the 5 overall process of a target impacted by a projectile [18]. While for 6 nanocrystalline and ultrafine bcc V, shear banding rather than crack 7 initiation and propagation is observed with promoting shear localization in 8 dynamic compression with strain rate of  $\sim 10^3$  s<sup>-1</sup> [19]. 9

However, RHEAs always exhibit apparent brittleness and lack of room-10 temperature ductility, which remains major and important challenges for 11 their processing and application [20]. Combining the ductile material with 12 the hard one to coordinate the comprehensive excellent performance of 13 RHEAs is meaningful and necessary. Zhao et al. [21] prepared a 14 Cu/(NbMoTaW) nanolaminates introducing the hard NbMoTaW HEA 15 laminates into the soft Cu to form the ultra-strong Cu/HEA composites. 16 Besides, as reported by Wei et al. [20], the TiVNbHf RHEA gets more 17 ductile with higher fracture elongation due to the evolution to fully 18 equiaxed grain after homogenization. Herein, we developed a body-19 centered cubic (bcc) sandwich-structured TaNbHfZr film. This designed 20 film integrates exceptional ductility of the middle layer characterized by 21 equiaxed grains, with enhanced resistance to softening in the upper and 22 lower layers which feature columnar grains. We evaluated the mechanical 23 behavior of magnetron-sputtered TaNbHfZr RHEAF in terms of the high 24 strain rate hardness  $H_D$  by nano-impact and also bridge the correlation of 25 the plasticity and toughness under test conditions with different strain 26 rates. At the same time, we introduce the energy-related evaluation to 27 discuss the plasticity evolution during the dynamic impact deformation as 28 29 well as the corresponding mechanisms.

#### **2 Materials and Methods**

#### 2 **2.1** Film deposition and characterization

The TaNbHfZr target ( $\varphi$ 75 × 5 mm) was prepared via powder metallurgy 3 with purities higher than 99.99% and was nominally equiatomic 4 (Ta<sub>25</sub>Nb<sub>25</sub>Hf<sub>25</sub>Zr<sub>25</sub>). The (100) Si wafer substrates were cleaned 5 ultrasonically in acetone, absolute ethyl alcohol and deionized water 6 sequentially before deposition. The base pressure of the vacuum system 7 during deposition via magnetron sputtering (JPG450a dual-chamber 8 magnetron sputtering deposition system) was less than 1×10<sup>-4</sup> Pa. The 9 deposition process was conducted by DC source in an argon atmosphere 10 with a target power of 200 W. The Ar flow rate was maintained at 25 sccm, 11 and the working pressure was 0.4 Pa. The substrate bias was set at -100 12 V with substrate heating to 700 °C before the deposition. To achieve the 13 layered structure, the film was initially deposited at 700 °C for 18 mins, 14 15 marked as stage 1; followed by a 12-minute interruption of the heating process, marked as stage 2. Subsequently, the heater was reactivated for 16 an additional 30 mins, marked as stage 3. During the whole process, the 17 entire deposition was continuous, with only the substrate temperature 18 19 being changed, and the total deposition time was 60 mins. The finer columnar grains in the lower layer were obtained at stage 1, the equiaxed 20 grains in the middle layer were obtained at stage 2, and the coarser 21 columnar grains in the upper layer were obtained at stage 3. 22

The phase structure of the TaNbHfZr film was characterized with Cu Kα radiation on a Bruker D8 discover powder X-Ray diffractometer at room temperature, at a scan speed of 2°/min from 10°-120°. Scanning electron microscopy (SEM, FEI-VERIOS460) was employed to observe the surface morphologies. High-resolution transmission electron microscopy (HR-TEM, JEM-2100F) experiment was conducted to observe and determine the

cross-sectional microstructure of the TaNbHfZr film, as well as the
elemental composition via energy dispersive X-Ray spectroscopy (EDS)
analysis. The atomic force microscope (AFM, INNOVA) was used to
analyze the surface roughness of these films.

The TEM foil for deformed specimen of nanoindentation at load=50 mN 5 with *LR*=0.5 mN/s and nano-impact at *AF*=5 mN were prepared using the 6 Helios G4 CX FIB (Focused Ion Beam) workstation. 30 KeV was used to 7 lift out the cross-section sample from one corner to the opposite side of 8 the indentation imprint. The coarse and fine milling was performed at the 9 current from 0.79 nA, 0.43 nA, 0.23 nA to 80 pA. Low-energy cleaning was 10 then performed at 5 KeV and 2 KeV after the milling. The TaNbHfZr pillars 11 were prepared using FIB with diameter of 400 nm and height/diameter 12 ratio of 2.5. 13

#### 14 **2.2 Nanomechanical tests**

15 The nano-impact and nanoindentation experiments were carried out in a controlled environment (25 °C and 65% relative humidity) using a 16 NanoTest Vantage system (Micro Materials Ltd, Wrexham, UK). A 17 calibrated diamond Berkovich indenter with a nominal tip curvature radius 18 of ~50 nm was utilized for nano-impact and nanoindentation tests. The 19 area function of the indenter was calibrated based on measurements from 20 a fused silica reference sample. The apparatus of nano-impact is 21 illustrated in Figure 1. For the nano-impact test, the AF was set at 5, 15 22 and 30 mN. The indenter was positioned at an accelerated distance (AD) 23 of 15 µm from the sample. The loading coil current was maintained 24 constant throughout the impact. As a result, the kinetic energy (KE) of the 25 pendulum increased until contact occurred, and the indenter reached its 26 27 maximum penetration depth in the sample before rebounding. The 28 indenter ultimately settled on the surface after several "bounces". The plastic deformation was completed in the first cycle, rendering the 29

influence of subsequent rebounds on the final impression depth insignificant [22]. The effective pendulum mass was 210 g. Owing to the flat and smooth surface of the TaNbHfZr film, each nano-impact at an AFwas repeated 3 times with a 50 µm interval. The residual contact area of the nano-impact at AF=5, 15 mN was measured using Image-J software.



6

- 7 **Figure 1** Schematic diagram of experimental apparatus used to quantify
- 8 the impact response (referred and modified from ref. [13])

#### 9 2.3 FEM modeling of cracking

The mechanical model was constructed in a 2D axisymmetric framework, 10 simulating a plane-strain state. The system employed a four-node bilinear 11 plane strain quadrilateral element (CPE4R) governed by reduced 12 integration and hourglass control. During the indentation process, the 13 mesh was refined to a size of 50 nm. The indenter was conceptualized as 14 analytical rigid body, and its conico-spherical profile was designed to fit the 15 area shape function A(h) of a Berkovich indenter (where A(h) is the 16 indenter section at a distance h from the tip apex). The opening angle of 17

the indenter was 70.32°. The simulation cell was taken sufficiently wide to 1 prevent the stress/strain fields generated within the sample during 2 indentation from interacting with the outer boundary. Additionally, a 5 µm 3 thickness for the silicon substrate within the computational cell was 4 deemed adequate. The crack propagation was implemented using a 5 coupled Cohesive Zone Model (CZM), and the crack openings followed 6 the cohesive traction-separation law [23]. In this instance, the maximum 7 8 principal stress criterion was selected for crack initiation. For the constructed model, the set of simultaneous non-linear dynamic equilibrium 9 equations were solved iteratively using Newton's method. 10

# 11 **3 Results and discussion**



#### 12 **3.1 Microstructural analysis**

13

Figure 2 (a) XRD pattern; SEM image of (b) surface morphology; (c) cross-sectional morphology; (d) HR-TEM image, inserts are the SAED (Selected Area Electron Diffraction) and the IFFT (Inverse Fast Fourier Transformation) images of the selected area denoted by a red dotted 1 square for the as-deposited TaNbHfZr film.

The XRD pattern of the as-deposited TaNbHfZr film, depicted in Figure 2 2 (a), reveals that the primary phase structure is body-centred (bcc), 3 characterized by a dominant (110) plane at ~37°. Additionally, a minor 4 secondary  $\beta$  hcp phase is present at ~35°, as indicated in previous work 5 [24, 25]. In Figure 2 (b), the top surface is characterized by needle-like 6 granules with width ranging from 30 to 40 nm. At high deposition 7 temperature, the coarsening driving force through surface atomic diffusion 8 9 and grain boundary movement enhances, thus the particles on the film surface coalesce along preferred orientation as needle shape to reduce 10 the total surface energy and interface energy [9, 26]. Additionally, the 11 surface is densely packed and devoid of any hole. AFM analysis in Figure 12 **S1** shows the surface average roughness  $R_a$  is ~2 nm. The cross-13 sectional morphology in Figure 2 (c) depicts the dense morphology and a 14 sandwich layered structure with a total thickness of 1 µm (300 nm for 15 lower columnar-grain layer, 200 nm for equiaxed-grain middle layer and 16 500 nm for upper columnar-grain layer). In addition, there is a good 17 adhesion between columnar and equiaxed grain structures, characterized 18 by clear and intact interfaces. The EDS analysis indicates that the film 19 possesses nearly equiatomic elemental compositions of Ta, Zr, Nb, Hf (25 20 at. %, 24 at. %, 29 at. % and 22 at. %, respectively). The HR-TEM 21 analysis in Figure 2 (d) exhibits clear and continuous lattice fringes in 22 both the HR-TEM and IFFT images. Besides, some lattice distortion can 23 be discerned due to atomic-size mismatch and elastic-modulus mismatch 24 within the average bcc lattice [27]. 25

26



1

Figure 3 (a) SAED and corresponding DF (dark field) images of different
 layers; (b) EDS-mapping of elemental distribution for as-deposited
 TaNbHfZr film.

TEM analysis of the as-deposited TaNbHfZr film lifted out by FIB is shown 5 in **Figure 3** (a). The distinct layered structure is characterized by 6 7 elongated and coarser columnar grains extending throughout the upper layer, equiaxed grains with sizes differ little in all directions in the middle 8 layer, and finer columnar grains in the bottom layer can be seen. SEAD 9 images help to characterize each layer with clearly separated spots in the 10 11 top layer, fine and continuous spots in the middle layer, and coarser spots compared with those in the top layer. DF images on the right specifically 12 present the shape and size of the grains in each layer (the light part 13 indicates the grains circled in SAED). The elemental distribution of each 14 15 layer was homogeneous as demonstrated in Figure 3 (b). The phase structure of three layers were identical, all keeping BCC structure with 16 crystal plane of (110), (200), (211) and (220). At stage 1, the deposition 17

temperature ( $T_s$ ) is 700 °C, and the melting point ( $T_m$ ) of TaNbHfZr is 1 2385.8 °C,  $T_s$  /  $T_m$ =0.3. In this zone, the film is more prone to form 2 refined grains with a certain texture, thus finer columnar grains formed 3 [26]. At stage 2, the cooling effect during the temperature break-off 4 bringing increased nucleation points and nucleation points, with the high-5 entropy and sluggish diffusion effects, as well as the heavy transition 6 elements composed in the film, lead to variations in diffusion velocity of 7 atoms during deposition. This favors the formation of refined equiaxed 8 grains in the middle layer of the film, due to increased compositional 9 undercooling [28, 29]. Besides, at lower deposition temperature, the ability 10 of atoms to migrate decreases, resulting in limited surface diffusion, 11 increased nucleation points and nucleation density, as well as decreased 12 driving force for recrystallization, which contributes to the formation of 13 equiaxed grains [30]. During the continuous deposition process, 14 compared to stage 1, stage 3 no longer needs to form nucleation sites 15 16 through the diffusion and rearrangement of atoms. At stage 3, a large number of nucleation sites undergo significant growth and recrystallization, 17 giving rise to the formation of numerous coarser columnar grains in the 18 upper layer of the film. 19

#### 1 3.2 Nano-impact

3



#### 2 3.2.1 Analysis of real-time impact depth curves

Figure 4 (a) Typical real time-depth curves; (b) the 1<sup>st</sup> cycle depth-time curves; (c)  $h_{\text{max}}$ ,  $h_r$  vs. *AF* curves; (d)  $h_r/h_{\text{max}}$  of TaNbHfZr HEAFs for nanoimpact at *AF*=5, 15, 30 mN.

The typical real-time depth curves of nano-impact at AF=5, 15 and 30 mN 7 are shown in Figure 4 (a), where the apparent oscillation can be seen due 8 to the dynamic compliance of the pendulum during the reciprocal loading 9 10 of impact. Some error may be introduced to the measurement of the rebound energy and lengthening the period at the maximum depth during 11 12 impact [31]. The deep impact depth indicates strong dynamic response of the film during impact. However, considering that most permanent 13 deformation has been completed in the 1<sup>st</sup> contact cycle, the detailed 14 energy dissipation in this cycle was examined. The contact cycle consists 15 of four phases as depicted in Figure S2 (a): acceleration, indentation, 16 rebound and deceleration. As supposed, higher AF corresponds to the 17 higher  $h_{\text{max}}$  and  $h_{\text{r}}$  in **Figure 4 (c)**. Toughness is the ability of a material to 18

absorb energy during deformation up to fracture, while fracture toughness 1 is the ability to resist the growth of a preexisting crack [32]. We use 2 toughness here to encompass both the energy required to crack and to 3 enable the crack to propagate until fracture, including the cases from 4 lower to higher AF. The calculated  $h_r/h_{max}$  value illustrated in Figure 4 (d) 5 is used as the index to measure the toughness [33], where  $h_r$  denotes the 6 plastic deformation during the impact process. The results exhibit that the 7 8  $h_r/h_{max}$  decreased from 0.82 to 0.78 as AF increases in nano-impact, suggesting an increase in plasticity absorption. 9

3.2.2 SEM morphologies for the impact imprints and microcompression
pillar



12

**Figure 5 (a)** SEM morphologies of impact imprints for TaNbHfZr HEAF and Si substrate at *AF*=5, 15, 30 mN; **(b)** the morphology of the pillar at loading rate of 1 nm/s before (inset) and after compression.

The SEM morphologies of the impact imprints of TaNbHfZr film and Si 16 substrate are displayed in Figure 5 (a). At AF=30 mN, the TaNbHfZr film 17 delaminated from the Si substrate, leaving a shallow imprint. In contrast, 18 uncoated Si exhibited visible radial cracks even at 5 mN, indicating that 19 20 the deleterious effect becomes more pronounced at higher AF. Obviously, 21 the protective film prevents the substrate from further degradation. The emergence of cracks reveals that the film requires increased ductility to 22 resist cracking, fracture or spallation under dynamic impact. It has been 23 confirmed that thinner film experiences higher stresses at the film-24

substrate interface [27, 34]. Failure mechanisms during impact can be 1 attributed to: micro-cracks initiation in the film post-impact; continued 2 nucleation, coalescence, or propagation of cracks at the film-substrate 3 interface, as indicated by minimal depth change in early impact cycles; 4 debonding at the interface due to interfacial mismatch during plastic 5 deformation and relaxation of pre-existing residual stress in the film [31, 6 35]. Microcracks form at the contact edge due to peak stress [33], which 7 can also been verified by the following FEM sumulation results. Rupture 8 behavior near the film-substrate interface, observed in guasi-static micro-9 compression tests at loading rates of 1 nm/s in Figure 5 (b) and 5 nm/s in 10 Figure S3, provides evidence of fracture phenomenon consistent with the 11 aforementioned failure mechanisms. The measured nanoindentation 12 hardness at 50 mN of Si substrate is ~11.7±0.19 GPa, and the reduced 13 modulus is ~177.1±1.55 GPa. For this harder film / softer substrate 14 system, a larger deformation of the Si substrate will occur during impact 15 16 when the penetration depth of the indenter reaches or deeper than the film/substrate interface. Besides, the deformation of Si substrate can 17 cause the film to bend or peel off, aggravating the dynamic effect in 18 19 nano-impact.

20 3.2.3 Dynamic hardness

21 We use the Meyer hardness as a representation of  $H_D$  [36]

22

$$H_D = \frac{P_m}{A}$$
 Equation 1

For a self-similar indenter geometry,  $A_c$  can be measured from microscopic observations of the impact impression,  $P_m$  represents the maximum resistance force obtained at the maximum depth of contact during impact, which is entirely determined by the dynamic compliance of the instrument, the sample properties and the geometry and initial impact energy of the indenter [37]. The proposed model, which includes the motion of the pendulum and the additional resistance accompanying the indenter once contact begins and increases, can be expressed
 mathematically as [22, 38]

3

$$m\vec{a} + c\vec{v} + k\vec{x} + \overline{F(x)} = \overrightarrow{AF}$$
 Equation 2

where *c* represents the damping coefficient, primarily due to air damping. 4 k signifies the spring stiffness,  $\vec{x}$  is the indentation depth vector, and a is 5 the acceleration velocity, which can be derived from the second derivative 6 of the fitted *h*-*t* curve during the indentation phase in 1<sup>st</sup> cycle impact using 7 the 5<sup>th</sup>-order polynomial fitting. As the plastic deformation was completed 8 at the initial contact, we analyzed the first cycle of impact at AF=5 mN 9 qualitatively. When the penetration depth approaches its maximum, 10 damping effects are considerably reduced, and hence, the resistive force 11 F(x) can be approximated as 12

13

#### $F(x) = P_m \approx ma + AF$ Equation 3

The method to obtain a and  $P_m$  is illustrated in **Figure S2.** (b). The 14 theoretical  $H_D$  can be derived using **Equation 1-3**, with the results 15 summarized in Table 1. Based on the one-dimensional model proposed 16 by Andrews and Constantinides *et al.* [38, 39], the  $H_D$  of aluminum 1100 17 measured by nano-impact was slightly higher than its static hardness. 18 While the dynamic hardness experiences obvious reduction when fracture 19 occurs. The contribution of the energy transfers from plastic deformation 20 to crack or fracture so that the resistance for the plastic deformation 21 weakens and correspondingly the hardness decreases sharply. The 22 calculated  $H_D$  is higher at AF=5 mN with 8.57 GPa to 7.09 GPa at AF=15 23 mN in dynamic nano-impact without considering the energy dissipation in 24 cracks and fracture. This can be explained by the strain gradient plasticity 25 (SGP) theory that dislocation density increases at decreased loads 26 caused by the presence of GND [22, 40, 41]. 27

28

<i>AF</i> (mN)	<i>H</i> <sub>D</sub> (GPa)	W <sub>P</sub> (nJ)	<i>E</i> (nJ)	U <sub>fra</sub> (nJ)
5	8.57	18.80	22.79	3.99
15	7.09	40.38	87.11	46.72

**Table 1** The calculated result of nano-impact at *AF*=5, 15 mN.

2 3.2.4 Impact energy

1

The energy loss during acceleration is estimated to be approximately 44.7 3 % due to energy dissipation in the system from damping and friction [35, 4 37]. The effective acceleration transfer work increases with AF [42]. For 5 simplicity, we have omitted the thermal energy and damping effect 6 induced energy loss. As shown in **Table 1**, the contribution to the fracture 7 part also increases from 3.99 nJ of 5 mN to 46.72 nJ of 15 mN, exhibiting 8 the apparent rate-dependent behavior. The kinetic energy difference ( $\triangle E$ ) 9 10 can be equivalently considered as the sum of the  $(W_P)$  and fracture work  $(U_{\rm fra})$ . Specifically, it is assumed that all the fracture work is absorbed by 11 the film only.  $W_{\rm P}$  is calculated using Tabor's method [36]. To determine 12  $U_{\rm fra}$ , we introduce the following relationship 13

14 
$$U_{fra} = 0.553\Delta E - W_P = 0.2765 \text{m}(v_{in}^2 - v_{out}^2) - \frac{1}{3}A_P h_r H_D$$
 Equation 4

where the effective mass of the pendulum is denoted as *m*, with a value of 15 0.21 kg. vin represents the initial velocity before the indentation of the 16 indenter, vout denotes the outgoing velocity at the point where the tip 17 detaches from the sample on the initial rebound,  $A_{\rm P}$  is the projected 18 contact area of the indenter. The calculated results are summarized in 19 **Table 1**. For impact at AF=5 mN of TaNbHfZr film, the energy contribution 20 to  $U_{\rm fra}$  accounts for 17.5% of the kinetic energy difference, which is the 21 primary factor that makes the  $H_D$  much smaller than the hardness in 22 quasi-static circumstances, as shown in Table S1. 23

1 3.2.5 Microstructure characterization by TEM of impact-deformed film



**Figure 6 (a)** SAED image of the areas located beyond (area ①, ② and ③) 3 4 and directly below (area ④, ⑤ and ⑥) the indenter, specific spots in the SEAD images indicate the BF (marked "1") and DF (marked "2" and "3" for 5 area ④, marked "2" for area ⑤ and ⑥) images; a delamination gap 6 between the TaNbHfZr film and Si substrate is highlighted by a red circle; 7 (b) Cracks in the middle layer near the interface; (c) Homogeneous 8 elemental distribution by TEM-EDS mapping of the deformed area 9 throughout the TaNbHfZr film after impact deformation at AF=5 mN. 10

2

Six sites away from (①, ②, ③) and right below (④, ⑤, ⑥) the indenter are
selected to elucidate the microstructural change after impact at 5 mN. As

illustrated in Figure 6 (a), a preferred orientation of the lattice plane is 1 clear and distinct in site ④, which is analogous to that of the as-deposited 2 sample; in site S, dense and continuous pots are connected nearly into 3 separated rings in SAED with visible cracks at the bottom of this zone, 4 enlarged in Figure 6 (b); while in site 6, visibly fuzzy and elongated 5 diffraction spots suggest a distorted lattice plane towards various 6 directions, rather than a preferred orientation as seen in the as-deposited 7 film. The grain size of the upper layer ranges of 20 to 50 nm, which is less 8 homogeneous than that of the as-deposited film with a range of 30 to 40 9 nm; and the grains exhibit a growth direction nearly identical to that of the 10 as-deposited film. The microstructure remains unchanged away from the 11 indenter compared with the as-deposited film. In the deformed area, the 12 extent of deformation is described by the layer thickness change of middle 13 layer: compared with the as-deposited film, the reduction of thickness of 14 the middle layer in nanoindentation at 50 mN was ~9 nm as depicted in 15 16 Figure S4, and ~56 nm in nano-impact at 5 mN. This larger thickness reduction suggests a dynamic response in high-strain-rate nano-impact. 17

During the impact, the stress distribution is inhomogeneous in the 18 deformed area. Typically, the zone of intense plastic deformation is 19 relatively confined and is limited to a region close to the impact surface 20 [31]. Concurrently, since the absolute value of the tensile stress in the 21 interface center is larger than it for the compressive stress in the surface 22 center [43, 44], the region below the indenter in the film-substrate interface 23 experiences tensile stress, causing the film to bend upwards. This 24 phenomenon can be confirmed from the visible delamination gap shown in 25 Figure 6 (a), marked with red circle. The maximum rebound force, 26 combined with the upward tensile stress and the downward compressive 27 stress induced by the indenter, results in the stress concentration in the 28 29 middle layer. While at the interface between the middle and bottom layers,

stress cannot be released promptly due to the complex collaborative deformation of the columnar grains in the bottom layer. The dispersion of stress during dynamic deformation is evident, which can be further confirmed by the subsequent FEM simulation.

Large quantities of grain boundaries are present in the middle layer, with 5 equiaxed grains deforming via rotating or grain boundary sliding. This 6 process involves grain boundary dislocations and boundary migration [45] 7 to coordinate and withstand the most severe plastic deformation, 8 strengthening and preventing the entire film from through-thickness crack, 9 fracture or spallation from the substrate. In the bottom layer, the columnar 10 grains become distorted with disordered orientation due to plastic 11 deformation, resulting in fuzzy and elongated spots on the diffraction rings. 12 In contrast, grain distortion occurs in the top layer in quasi-static plastic 13 deformation (Figure S4), while it happens in the bottom layer during 14 dynamic deformation. The change in the deformation zone may also be a 15 16 product of rate-dependent deformation. The EDS mapping result in Figure 6 (c) illustrates homogeneous element distribution without segregation or 17 precipitation, notably, this lamination structure maintains its composition 18 even under dynamic impact deformation. Generally, energy loss is equal 19 to the energy stored in the material. Energy-storage mechanisms include 20 crack generation, pore collapse, phase transformations interfacial defects, 21 and frictional processes such as sliding of crack surfaces and dislocations 22 motion [18]. In this study, the TaNbHfZr film loses or stores energy by 23 24 forming cracks. The amount of the energy can be measured using the fracture energy  $U_{\rm fra}$ , as listed in **Table 1**. 25

# 1 3.3 Rate-dependent behavior



2

Figure 7. *ISR* of the fitted impact depth-time curve during indentation
phase at *AF*=5, 15 and 30 mN.

5 The *ISR* during indentation can be assumed to be [46]

6

# $ISR = \frac{v(t)}{h(t)}$ Equation 5

As AF increases, ISR in the initial contact of the nano-impact exhibits a 7 corresponding increase, then subsequently decreases over time as shown 8 9 in **Figure 7**. For the impact at AF=5 mN, the initial ISR reaches ~50 s<sup>-1</sup>, which reduces to nearly zero by the end of the indentation process. Pharr 10 has proposed that a larger stress is required to activate the dislocation 11 sources at the early stage of the indentation [47]. For bcc lattice, the 12 motion of screw dislocations often occurs through the thermally assisted 13 formation and migration of kink-pairs [15]. The rate-controlling response is 14 essentially determined by dislocation movement. According to the theory 15 proposed by Hirth & Lothe [48], the nucleation rate of dislocation  $J_c$  can be 16 17 expressed as

18

$$J_c = nexp\left(-\frac{G}{k_BT}\right)$$
 Equation 6

where *n* is a constant of atom sites,  $K_B$  is Boltzmann's constant and *T* represents the temperature. The free energy of a dislocation loop, denoted as *G*, generally includes the elastic strain energy of the dislocation, plus any stacking fault energy, minus the work done by the applied stress [49].
 This can be mathematically expressed by

 $G = 2\pi r_c W + \pi r_c^2 \gamma - \pi r_c^2 b\sigma$ Equation 7 where  $r_c$  is the critical radius of a dislocation loop,  $\gamma$  represents the stacking fault energy, *b* is the Burgers vector of the dislocation, and  $\sigma$  is the applied stress. It is indicated that an increase in the applied stress  $\sigma$ can effectively reduce *G* and consequently increase  $J_c$ .

During impact, the force of inertia can significantly increase the contact 8 force, resulting in a higher density of dislocation nucleation. At higher LR, 9 the film subjected to the indenter experiences higher stress within a unit 10 time, leading to more dislocations near the deformation area. Generally, 11 solute-solution interaction dominates the kinetics of deformation at low 12 flow stress levels, while at higher stress levels, dislocation-dislocation 13 interaction dominates crystal rheology [50]. The deformation mechanism 14 of the nanocrystalline TaNbHfZr film with abundant grain boundaries is 15 16 dominated by the dislocation-dislocation interaction at higher AF with higher strain rate. As the density of dislocation increases at higher strain 17 rates, deformation becomes tougher, providing evidence of the rate-18 dependent behavior of TaNbHfZr film at dynamic deformation. 19

#### 20 **3.4 Simulation of stress distribution in the film**

FEM simulation was conducted to further confirm the stress distribution 21 within the sandwich-structured TaNbHfZr film. The simulation results 22 indicate that cohesive cracking occurs within the middle layer adjacent to 23 24 the indentation loading axis. As shown in Figure 8, which illustrates the maximum principal stress distribution, it is evident that the topmost 25 indented region experiences significant compressive stress, while the 26 bottom portion undergoes bending tensile stress. The middle layer, 27 situated near the loading axis, is predominantly subject to tensile stress 28

throughout the layer. This phenomenon is determined by the structure of 1 the three-layer system, and the cracking mechanism can be deduced to 2 be driven by the coupling effect of bending tensile and shear stress. 3 Moreover, the upper surface of the bottom layer is under compression due 4 to the extensive overlying pressure from the middle layer, a situation partly 5 attributable to the higher stiffness (modulus) of the bottom layer compared 6 to the middle one. The simulation results of stress distribution in Figure 8 7 well matches and elucidates the indentation-induced damage behavior 8 sandwich-layered system with 9 within the the impact-deformed microstructure in Figure 6, where crack events occur when the stress in 10 the middle layer, near the middle-bottom boundary, attains its maximum 11 value. 12



Figure 8 (a) Maximum principal and (b) Mises stress distribution of
 TaNbHfZr film after nanoindentation at 50 mN.

#### 16 **4. Conclusions**

The sandwich-structure TaNbHfZr film exhibits rate-dependent behavior during dynamic nano-impact. Cracks are the primary energy-storage mechanism.  $W_p$  and  $U_{fra}$  increase with strain rates at higher *AF*, and cracks emerge in the middle layer where stress concentrates. The decreased  $H_D$  can be explained by the increased energy contribution to fracture at higher strain rates during nano-impact. The equiaxed grains within the middle layer deform through rotation or grain boundary sliding, thereby accommodating and withstanding the most severe plastic deformation. This process effectively prevents the film from experiencing through-thickness cracking, fracturing, or spallation from the substrate in that the stress was dispersed by interfaces in the sandwich structure.

5 Examination of the microstructure and the mechanism of dynamic nano-6 impact of the sandwich-structured TaNbHfZr film provides insights into the 7 overall mechanical performance at nano-scales. This understanding offers 8 valuable evidence and design strategies for materials, particularly 9 refractory high entropy alloy films, when subjected to equivalent high-10 strain-rate service conditions.

#### **11** CRediT authorship contribution statement

Baorui Song: Writing – Original draft, Investigation, Conceptualization,
Formal analysis, Data curation. Yanhuai Li: Conceptualization, Methodology,
Writing – review & editing, Validation. Jiahong Wei: Investigation. Dan Qian:
Formal analysis. Liuquan Yang: Conceptualization, Visualization. Zhongxiao
Song: Resources, Software. Weihua Li: Project administration, Resources,
Supervision, Funding acquisition.

# **Declaration of Competing Interest**

19 The authors declare that they have no known competing financial interests 20 or personal relationships that could have appeared to influence the work 21 reported in this paper.

#### 22 **Data availability**

23 Data will be made available on request.

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