

# 1 Commuter Departure Time Choice Behavior under Congestion

## 2 Charge: Analysis Based on Cumulative Prospect Theory

### 3 **Abstract:**

4 An often-overlooked problem in the evaluation and prediction of congestion charge  
5 policies is commuters' bounded rationality. Although some studies have sought to account for  
6 this using cumulative prospect theory (CPT), the specific behavioral parameters that reflect  
7 travelers' decision-making process in response to congestion charge scenarios are based on  
8 assumptions and lack empirical evidence. This paper aims to provide empirical evidence to  
9 define the shape parameters in CPT—while accounting for systematic heterogeneity due to  
10 commuters' characteristics—in order to build more realistic behavioral models for car  
11 commuters' departure time choice behavior under congestion charge scenarios. A stated  
12 preference (SP) experiment with four time-based congestion charge scenarios is designed to  
13 obtain commuters' departure time choices when facing uncertain travel conditions. A genetic  
14 algorithm (GA) is used to estimate the CPT coefficients that reflect car commuters' cognitive  
15 biases under the congestion charge. The results suggest that commuters' departure time choice  
16 under the congestion charge policy is consistent with the assumption of CPT. We find evidence  
17 of risk-averse and risk-taking behavior, loss aversion, and large distortion in probability  
18 weighting, and individuals' personal and commuting characteristics had heterogeneous effects  
19 on CPT coefficients. The results shed light on travelers' behavioral responses to congestion  
20 charge schemes and provide an important empirical reference.

21 **Keywords:** Cumulative Prospect Theory, Congestion Charge, Departure Time Choice,  
22 Genetic Algorithm.

## 23 **1. Introduction**

24 Private cars are an essential part of everyday life. Along with their convenience, however,  
25 the negative externality caused by excess travel demand over road capacity is steadily rising.  
26 Traffic congestion is a pervasive problem in most megacities around the world and impacts the  
27 quality of life by increasing air and noise pollution (e.g., Alvanchi et al., 2019; Armah et al.,  
28 2010; Chin, 1996; Greenwood et al., 2007); decreasing the safety of streets (e.g., Albalade &  
29 Fageda, 2019; Noland & Quddus, 2005); and, more directly, increasing travel time variability  
30 and arrival time uncertainty (Li & Hensher, 2012). According to the “2016 China Major Urban  
31 Traffic Analysis Report” released by AutoNavi Software Co., one-third of Chinese urban  
32 commuting trips are threatened by traffic congestion. The peak hour congestion delay index  
33 (which is total travel time divided by free-flow travel time) for cities such as Jinan, Harbin, and  
34 Beijing exceeded 2.0, which means that commuters in these cities spend more than twice as  
35 much commuting time due to traffic congestion as they would otherwise. Of the 60 major cities  
36 in the report, 32 have a peak hour congestion delay index greater than 1.8.

37 Traffic congestion is caused by the mismatch between travel demand and road capacity.  
38 In economics, the standard approach to internalize negative externalities from daily traffic is  
39 congestion charging (Pigou, 1920). Empirical evidence and analytical models in transportation  
40 have found that congestion charging is able to affect commuters’ travel behavior, including  
41 decisions related to departure time choice, route choice, and mode choice (e.g., Saleh & Farrell,  
42 2005; Ubbels & Verhoef, 2006; Yamamoto et al., 2000; Börjesson et al., 2012). Some large  
43 cities worldwide have adopted congestion charging to alleviate urban traffic congestion and  
44 obtained notable results, such as Singapore (1975), London (2003), and Stockholm (2007). In  
45 contrast, other cities have failed to implement congestion charging (e.g., Edinburgh), and still  
46 others hesitated to implement it for a long time (e.g., Beijing). One of the main concerns of

47 decision-makers is uncertainty regarding how travelers will respond to a congestion charge  
48 policy.

49 From a microeconomic standpoint, traffic demand and supply change stochastically, and  
50 travelers seek to make choices that will reduce their disutility of traveling (Lu et al., 2019).  
51 Experimental evidence in behavioral economics shows that individuals are boundedly rational  
52 and affected by cognitive biases when making decisions under risk and uncertainty (Kahneman  
53 & Tversky, 1982). On a daily basis, commuters make decisions in a highly variable  
54 environment and cope with the uncertainty of traffic conditions. Thus, commuters are expected  
55 to make travel choices that largely deviate from the predictions of standard economic theory  
56 (McFadden, 1999) due to multiple factors; these include a lack of road traffic information, a  
57 limited cognitive span to process numerous stimuli present in the traffic environment, and the  
58 complex pattern of risk attitudes exhibited by individuals in experimental studies. A congestion  
59 charge scheme renders traffic decisions more complex, and thus commuters become more  
60 sensitive to the uncertainty and unreliability of traffic conditions (Li & Hensher, 2010).  
61 Therefore, conducting systematic studies before the implementation of congestion charging  
62 and developing predictive models of travelers' responses that account for their bounded  
63 rationality is critical for designing and evaluating ex ante a policy's impact.

64 The majority of research on travelers' behavior under congestion charging uses modeling  
65 frameworks that are consistent with expected utility theory (EUT) (e.g., Brownstone & Small,  
66 2005; Small et al., 2005; Arellana et al., 2012; Lizana et al., 2021). Some work investigates the  
67 impact of bounded rational behaviors in the preference for congestion charge schemes, but still  
68 within the EUT framework (Thorhauge et al., 2019, 2020). However, since the early 1950s,  
69 the EUT framework has proved to not be a close representation of people's decision-making  
70 process in reality (Starmer, 2000). Several empirical studies have found that actual choice

71 behaviors appear to be inconsistent with EUT—notably, violations of the independence axiom  
72 of EUT discovered by Allais (1953), the preference reversal phenomenon observed by  
73 Lindman (1971), and the framing effect identified by Tversky and Kahneman (1981).

74       Given the limitations of EUT, some researchers have expanded the traditional scheduling  
75 model by embedding features from prospect theory, such as the fourfold pattern of risk attitudes  
76 (Li et al., 2012) and reference dependence (Fujii & Kitamura, 2004). Other decision-making  
77 theories developed in the behavioral sciences have been gained attention in the transportation  
78 field and have been used with the goal of enhancing travel behavior models (see Li & Hensher,  
79 2019, for a review). In particular, prospect theory (PT) (Kahneman & Tversky, 1979) and  
80 cumulative prospect theory (CPT) (Tversky & Kahneman, 1992) have attracted great interest  
81 due to their advantages in modeling decisions under risk and uncertainty. PT has been applied  
82 to model a variety of transportation behaviors, including departure time choices (Jou et al.,  
83 2008; Schwanen & Ettema, 2009; Tian et al., 2012). In our view, the application of PT is crucial  
84 in accounting for cognitive biases triggered by the more complex and uncertain traffic  
85 environment that results from implementing a congestion charging scheme. Some studies have  
86 emphasized the importance of considering travelers' behavioral biases when evaluating the  
87 effectiveness of a congestion charge policy by using PT elements in theoretical modeling (Pan  
88 & Zuo, 2014; Xu et al., 2011a), but the specific behavioral parameters that reflect travelers'  
89 decision-making process in response to congestion charge scenarios are based on assumptions  
90 and lack of empirical evidence.

91       The purpose of this paper is to provide empirical evidence to define the shape parameters  
92 in CPT, while accounting for systematic heterogeneity due to commuters' characteristics, to  
93 build more realistic behavioral models for car commuters' departure time choice behavior  
94 under congestion charge scenarios. We aim to address the following three questions: (1) How

95 can we build a more realistic behavioral model for travelers' time choices under congestion  
96 charge scenarios based on CPT? (2) What are the most relevant shape parameters in CPT to  
97 model departure time choices under congestion charge scenarios? (3) How will these CPT  
98 parameters change among commuters with heterogeneous characteristics? To answer these  
99 questions, the shape parameters in CPT functions are fitted using mixed logit models and data  
100 collected from a stated preference (SP) experiment. The parameter search was performed using  
101 a genetic algorithm (GA) to optimize a highly non-concave likelihood function.

102 The remainder of the paper is organized as follows. Section 2 reviews the literature on  
103 travelers' behavioral responses to a congestion charge and the application of PT in  
104 transportation studies. Section 3 introduces the model specification and estimation procedure.  
105 Section 4 describes the survey design, data collection, and descriptive statistics. Section 5  
106 reports the estimated results. Section 6 concludes with a further discussion of the results and  
107 policy implications.

## 108 **2. Literature review**

### 109 **2.1 Behavioral responses to a congestion charge**

110 The idea of congestion charges can be traced back to the Pigouvian tax proposed by Pigou  
111 (1920). He argued for a tax on congestion to internalize the negative externality caused by  
112 travelers. By levying a specific charge for each road section based on its marginal cost, the  
113 user's equilibrium travel pattern can achieve the social optimum (Beckmann et al., 1956). Road  
114 traffic in cities that implemented congestion charge schemes provides empirical evidence of  
115 the effectiveness of this policy (Börjesson & Kristoffersson, 2018; Lehe, 2019). Hence, a  
116 number of studies support the use of congestion charges, and abundant research has been

117 conducted to explore travelers' short-term and long-term behavioral responses to different  
118 congestion charge schemes (see Li & Hensher, 2012, for a review).

119 Looking at the methodology, previous work on congestion charging can be divided into  
120 three categories. The first category explores the effectiveness of congestion charge schemes  
121 for managing traffic flows using theoretical models and numerical examples. For example, Zhu  
122 et al. (2015) compared social welfare before and after imposing congestion charges on taxis  
123 and developed a bilevel programming model that solves the network equilibrium in the lower  
124 level and maximizes social welfare in the upper level. Knockaert et al. (2016) used a traditional  
125 bottleneck model and explored measures to improve the efficiency of a coarse charge by  
126 differentiating across heterogeneous travelers. De Palma et al. (2018) estimated the  
127 performance of a congestion charge in a parallel road and public transport network under  
128 uncertainty and compared its performance with a tradable credit scheme. They found that when  
129 the congestion charge can be adapted from day to day, it can be equivalent to a quantity  
130 instrument (i.e., tradable credits)—but when the congestion charge cannot be adaptive, it  
131 performs worse.

132 The second category of studies uses simulation-based approaches to evaluate and predict  
133 the practical impact of congestion charge schemes at city level. For example, Cipriani et al.  
134 (2019) designed and tested different zone-based pricing policies for Rome while accounting  
135 for equity. Zhang et al. (2019) proposed and tested a dynamic traffic assignment system that  
136 could precisely predict traffic conditions when applying a congestion charge in a real network.  
137 In their system, travelers made route choices based on discrete choice models, and toll revenue  
138 was the optimization object. He et al. (2021) evaluated a congestion charge plan using a multi-  
139 agent simulation model for New York City that can capture traffic dynamics and the  
140 substitution effects of multiple modes in different segments of the city. They found that the

141 number of trip reductions evaluated by their model was more than the government proposal  
142 under the same charging scheme, even though the annual revenues collected were similar.

143 Empirical work has conducted SP experiments to study consumers' preference for  
144 congestion charge policies that are not currently in place. Compared with the above categories,  
145 this stream of research helps us better understand how individuals respond to congestion charge  
146 schemes from a behavioral perspective. The congestion charge mechanism analyzed mainly  
147 includes charges by transit times, charges by distance, flat time charges, and differentiated time  
148 charges (Siddique & Choudhury, 2017; Arellana et al., 2012; Tillema et al., 2010a, b; Ubbels  
149 et al., 2008). Most studies have shown that a dynamic charge that changes over time has the  
150 best effect on alleviating traffic congestion (Ubbels & Verhoef, 2006). In terms of the group  
151 charged, papers have mostly focused on car commuters (Andani et al., 2021; Arellana et al.,  
152 2012). In terms of charging area, a congestion charge scheme for the whole road network is  
153 considered to have the greatest impact (Siddique & Choudhury, 2017). Most studies have been  
154 conducted in European countries (such as the Netherlands, Greece, Denmark, the United  
155 Kingdom, and Sweden); a few countries in Asia (such as Singapore); Chile; and Australia, and  
156 travelers' responses to congestion charge policies are likely to differ depending on culture and  
157 political circumstances. Congestion charge studies that focus on Chinese contexts and Chinese  
158 travelers are still limited.

159 Some studies on behavioral departure time models have applied descriptive behavioral  
160 theories that consider travelers' bounded rationality in travel behavior research. For example,  
161 Koster and Verhoef (2010) took into account that travelers could treat the probabilities of  
162 arrivals in a nonlinear way, following rank-dependent utility theory. Koster et al. (2015)  
163 modeled commuters' scheduling choices with the assumption that individuals showed limited  
164 memory capacity, retrieval constraints, and anchoring, which was also termed "memory-based

165 adaptive expectations.” De Borger and Fosgerau (2008) developed a reference-dependent  
166 choice model to explain individuals’ valuation of travel time within the framework of prospect  
167 theory. Using data from a large-scale choice experiment, they found that models that account  
168 for reference dependence had a better fit than their counterparts. Their parameter estimates also  
169 supported the presence of loss aversion. Hjorth and Fosgerau (2012) further extended the above  
170 research by reformulating the model proposed by De Borger and Fosgerau (2008) in a way that  
171 separates the value of travel time from value functions. They also identified and tested all  
172 model parameters using data from a new SP experiment in Norway.

173 In congestion charge contexts, Lindsey (2011) developed a model of reference-dependent  
174 preferences to analyze travelers’ aversion to price variation based on the theory developed by  
175 Köszegi and Rabin (2006). He divided travelers’ utility into two elements: an intrinsic utility  
176 and a gain-loss utility. Xu et al. (2011a) proposed a user equilibrium model with endogenous  
177 reference points based on PT and developed an optimal pricing model that could capture  
178 travelers’ route choices in response to pricing signals under risk. They found that commuter  
179 decisions under congestion charge scenarios are affected by subjective factors, such as risk  
180 preferences. They argue that when commuters’ bounded rational responses are considered in  
181 the design stage of a congestion charge policy, it is more likely to achieve the expected outcome.  
182 Pan and Zuo (2014) developed an improved stochastic user equilibrium model based on  
183 prospect theory. They proposed the concept of perceived prospect and assumed that the  
184 prospect of each route was constituted by a fixed term and a random one. Then, they analyzed  
185 optimal congestion pricing to manage users’ route choices.

186 As suggested by theoretical work, when evaluating a congestion charge scheme with a  
187 differentiated toll—which could create more uncertainty for drivers (Li & Hensher, 2010)—it  
188 is crucial to understand travelers’ bounded behavioral rules. However, the empirical evidence  
189 is still limited. Zou et al. (2016) provided empirical insight into travelers’ bounded rational



190 behavior under a time-flat congestion charge policy. The authors developed an agent-based  
191 choice model for travel mode and departure time in which travelers' searching and decision  
192 process is represented by a production rule based on fuzzy set theory. The model is validated  
193 using data collected from an online SP survey in Beijing in which respondents dynamically  
194 switched their choices based on the latest scenario after the last adjustment. This work  
195 considers travelers' bounded rationality when searching for the traffic equilibrium, but it does  
196 not consider the uncertainty or behavioral biases that travelers would face when making such  
197 choices. Other work has investigated the impact of bounded rational behavior on travelers'  
198 departure time choices in their preference for congestion charge schemes, such as habit-driven  
199 behavior or the effect of intention, but still within the EUT framework (Thorhauge et al., 2019,  
200 2020).

**Table 1** Key characteristics of reviewed studies on congestion charge

Study	Methodology	Whether behavioral biases for travel choices are considered	Whether behavioral parameters are estimated	Type of congestion charge	Behavioral choices	Country/City
Zhu et al., 2015	Modeling and numerical example	No	No	Link toll	Mode choice, route choice	None
Knockaert et al., 2016	Modeling and numerical example	No	No	Coarse charge	Time choice	None
de Palma et al., 2018	Modeling and numerical example	No	No	Tolls versus tokens	Number of trips	None
Cipriani et al., 2019	Simulation	No	No	Zone-based toll	Mode choice	Rome
Zhang et al., 2019	Simulation	No	No	Real-time proactive charging system	Route choice	Texas
He et al., 2021	Simulation	No	No	Time- and link-based toll	Mode choice	New York
Ubbels & Verhoef, 2006	SP experiment	No	No	Fixed, distance-based, and time-based charge	Mode choice and number of trips	Netherlands
Siddique & Choudhury, 2017	SP experiment	No	No	Trip duration and purpose-based toll	Mode choice	Dhaka

Andani et al., 2021	SP experiment	No	No	Link toll	Residential location, route, and mode choices	Indonesia
Arellana et al., 2012	Three-step RP–SP– attitudinal survey	No	No	Time-based charge	Mode choice and time choice	Santiago
Lizana et al. 2021	Forecasting RP-SP	No	No	Time-based charge	Mode choice and time choice	Santiago
Lindsey, 2011	Modeling and numerical example	Yes	No	State-dependent toll	Whether to use a congestible facility	None
Xu et al, 2011a	Modeling and numerical example	Yes	No	Link toll	Route choice	None
Pan & Zuo, 2014	Modeling and numerical example	Yes	No	Link toll	Route choice	None
Zou et al., 2016	SP experiment	Yes	No	Fixed toll	Mode, time, route, and number of trips change	Beijing
Thorhauge et al., 2019	SP experiment	Yes	No	Time-based toll	Time choice	Copenhagen
Thorhauge et al., 2020	SP experiment	Yes	No	Time-based toll	Time choice	Copenhagen

## 203 **2.2 Applications of prospect theory in travel behavior modeling**

204 Prospect theory is one of the most common frameworks used to study decision-making  
205 under risk and uncertainty (Kahneman & Tversky, 1979). Compared with EUT, PT is based on  
206 a new specification of the deterministic component of the utility function, which makes it more  
207 advantageous to describe travelers' decision-making under uncertainty (Avineri & Ben-Elia,  
208 2015). PT models are typically estimated as random utility models in which the deterministic  
209 component of the utility function accounts for both the S-shaped value function and the  
210 probability weighting function. The CPT proposed by Tversky and Kahneman (1992) further  
211 generalizes PT by using a rank-dependent weighting function. Although the difference between  
212 PT and CPT is not significant, the application of CPT is expected to provide a more scientific  
213 and realistic approach to modeling commuters' choice behavior (Yang & Liu, 2018).

214 The systematic utility structure in PT and CPT can capture various kinds of behaviors that  
215 fail to be reflected in EUT, including:

- 216 • Reference dependence: In the EUT model, preferences do not depend on current assets  
217 but on states of wealth, which is a great simplification of the actual decision process  
218 (Tversky & Kahneman, 1991). To generalize the EUT model, a value function in which  
219 the outcomes are defined as gains and losses relative to a reference point is introduced  
220 in PT and CPT models (Kahneman & Tversky, 1979, 1984; Tversky & Kahneman,  
221 1991).
- 222 • Loss aversion: Although EUT doesn't distinguish between different evaluations of  
223 gains and losses, the asymmetry between gains and losses has been observed in a  
224 variety of field data (Tversky & Kahneman, 1991). Hence, the principle that losses  
225 loom larger than corresponding gains has been applied in PT and CPT by using a steeper

226 value function for losses than for gains (Kahneman & Tversky, 1984; Tversky &  
227 Kahneman, 1992).

228 • Framing effect: The assumption of description invariance is implicit in EUT, which  
229 means that equivalent formulations of a choice problem should induce the same  
230 preference order (Arrow, 1982). However, widespread evidence has shown that  
231 variations in the framing of prospects can dramatically impact preference and choice  
232 (Tversky & Kahneman, 1981, 1986). As a result, PT embodied such violations of EUT  
233 based on the psychological principles of evaluation (Tversky & Kahneman, 1986).

234 • Risk seeking: Given the assumption of EUT, individuals' risk preference should be  
235 independent of the probability of losses and gains, which has been found to be  
236 inconsistent with empirical data (Starmer, 2000). Tversky and Kahneman (1992)  
237 proposed a distinctive fourfold pattern of risk attitudes in CPT, which considered both  
238 risk aversion and risk seeking. The pattern shows risk aversion for gains and risk  
239 seeking for losses of high probability, and risk seeking for gains and risk aversion for  
240 losses of low probability.

241 • Nonlinear probability weighting: According to EUT, the utility of a risky outcome is  
242 linear in its objective probability, and individuals' preferences should follow the  
243 independence axiom. However, the empirical evidence of Allais (1953) challenged this  
244 principle by demonstrating that a reduction of probabilities from 1.00 to 0.99 has more  
245 impact on preference and choice than from 0.11 to 0.10. This phenomenon was  
246 explained by Kahneman and Tversky (1979) as the certainty effect and is captured in  
247 the original PT. They introduced a nonlinear weighting function, which overweights  
248 small probabilities and underweights moderate and high probabilities. Considering that  
249 the separable decision weights cannot always satisfy stochastic dominance and be

250 extended to prospects with a large number of outcomes (Tversky & Kahneman, 1992),  
251 they further used a cumulative functional representation of probability in CPT.

252 A number of recent studies on travel behavior use PT or CPT (see Li & Hensher, 2011, for  
253 a review). Most of these studies highlight the advantages of PT and CPT in describing  
254 commuters' decision-making compared with EUT (e.g., Fujii & Kitamura, 2004; Huang, Burris,  
255 & Shaw, 2017; Yang & Jiang, 2014). In an attempt to challenge the premises of EUT in travel  
256 behavior models, Fujii and Kitamura (2004) hypothesized that (1) car commuters consider  
257 uncertain travel time as a time interval; (2) car commuters choose their departure time based  
258 on the time interval and use their preferred early departure time and preferred departure time  
259 as reference points. Their empirical data verified their hypotheses and refuted previous studies  
260 based on EUT that argue that travel time conforms to a subjective continuous distribution. The  
261 authors concluded that EUT is not suitable for describing car commuters' departure time choice  
262 behavior.

### 263 **2.2.1 Exogenous versus endogenous estimation**

264 Many early studies based on PT or CPT fix the shape parameters of the value and  
265 weighting functions using the estimates obtained by Tversky and Kahneman (1992) from  
266 financial experiments (Avineri, 2004; Avineri & Prashker, 2005; Gao et al., 2010; Tian et al.,  
267 2012). As Li and Hensher (2011) demonstrate, however, biased or even incorrect findings and  
268 conclusions may occur because PT parameters are highly context-dependent. For instance,  
269 Yang and Liu (2018) theoretically proved that different subjective gain-loss ratios highly  
270 influence the optimal solution of commuters' departure time choice. While some studies  
271 estimate the parameters of PT models using choice data, a subset of the parameters is always  
272 fixed arbitrarily, mainly for identification purposes. Using experimental data on route choice  
273 behavior, Xu et al. (2011b) estimate the risk preference parameter and loss aversion parameter

274 in the value function of PT but fix the parameter in the weighting function to 0.74 based on  
275 results of previous studies. Using both revealed preference household travel survey data and  
276 empirically observed travel time data, Ghader et al. (2019) study travel mode behavior based  
277 on CPT. Since they model all outcomes as losses, the loss aversion parameter has been fixed  
278 to one and other parameters in CPT have been estimated using a logit model.

279 With increasing awareness of the particularity of travel behaviors in different contexts,  
280 few studies jointly estimate all CPT parameters based on their specific travel context. For  
281 example, Schwanen and Ettema (2009) explore the CPT parameters of employed parents'  
282 choice regarding collecting their child(ren) from the nursery by themselves at the end of the  
283 workday or letting their partner do it. They designed an SP experiment and set three reference  
284 points: (1) the time when most parents pick up children, (2) the time specified by the nursery,  
285 and (3) the nursery's closing time. They used a binary logit model and a GA to estimate the  
286 CPT parameters. Results show that the value function curve has an inverse "S" shape: slightly  
287 convex for gains (arrive early or on time) and concave for losses (arrive late). The results  
288 suggest that parents exhibit risk seeking behavior for gains and risk aversion for losses. Though  
289 this is opposite to Tversky and Kahneman's (1992) results, they consider their results plausible  
290 because arriving late for collecting children should become more objectionable as lateness  
291 increases. Also, individual characteristics, such as gender and share of collection duties, have  
292 significant effects on the parameters.

293 The use of more advanced discrete choice model techniques has also enhanced the  
294 development of PT models. Wen et al. (2019) estimate passengers' loss aversion, diminishing  
295 sensitivity, and probability-weighting coefficients for alternative travel arrangements when  
296 facing flight delays. They use an SP experiment to obtain empirical data on passengers' choices  
297 to retain the booked flight or the next available flight on the same airline, or to transfer to

298 another airline. A mixed logit model combined with CPT is used to estimate passengers'  
299 preferences for each alternative. The results show that air travelers with different travel  
300 distances have different sensitivity to delay times.

### 301 **2.2.2 Multiple reference points**

302 The choice of reference points is a critical component of PT models, since they define  
303 whether time outcomes are framed as gains or losses in utility. Seminal work used PT defined  
304 a single reference point to model monetary decisions, but travel behavior models have extended  
305 this definition to allow for multiple reference points. Jou and Chen (2013) estimate CPT  
306 parameters to reflect the risk attitudes of freeway drivers in route choices. They use three  
307 reference points: free-flow travel time, average travel time, and longest travel time. CPT  
308 parameters are estimated using data from an SP survey and a logit model. Consistent with CPT,  
309 drivers were risk averse in the gain domain and risk seeking in the loss domain. Drivers  
310 exhibited loss aversion for travel time losses and distortion in probability weighting, especially  
311 in the loss domain. Moreover, drivers who usually encounter traffic congestion show higher  
312 sensitivity to gains. In another study, Jou et al. (2008) set three reference points: the earliest  
313 arrival time, the expected arrival time, and the work starting time. They divided the value  
314 function into two gain parts and two loss parts, then estimated the risk preference parameter  
315 and loss aversion parameter in PT using empirical data. Senbil and Kitamura (2004a) proposed  
316 two reference points for work activity: the earliest tolerable arrival time and the latest tolerable  
317 arrival time. A key assumption is that commuters perceive losses when arriving before the  
318 earliest acceptable arrival time and after the latest tolerable arrival time.

## 319 **2.2 Research gaps and contribution of the present study**

320 Overall, the evidence from previous studies suggests that travelers' preferences vary  
321 among different travel decisions in various travel contexts. The choice of reference points, the



322 construction of travelers' utility functions, and the sociodemographic and traveling  
323 characteristics of samples may all lead to different estimates of CPT parameters. Evidence  
324 provided by theoretical work has shown that when assuming that travelers' utility function  
325 follows CPT, the traffic equilibrium condition can be far from a context that uses the EUT  
326 assumption (Pan & Zuo, 2014; Xu et al., 2011a). However, the numerical results of the above  
327 studies are directly applied to behavioral parameters estimated by previous studies in quite  
328 different contexts from ours, and thus might not correctly reflect commuters' departure time  
329 choice mechanisms under congestion charge scenarios. As a result, evaluation of the policy's  
330 effectiveness may be biased. Therefore, it is necessary to conduct more empirical studies to  
331 further examine travelers' behavioral responses to the congestion charge and calibrate CPT  
332 parameters in each context.

333 This study contributes to filling these gaps in three ways. First, it presents new evidence  
334 on congestion charging using an SP experiment that includes CPT-based scenarios and a time  
335 choice model with CPT. Second, it expands previous PT/CPT studies by empirically examining  
336 specific CPT parameters and Beijing commuters' value of time in congestion charge scenarios.  
337 In addition, the effects of commuters' heterogeneous characteristics on CPT parameters have  
338 been analyzed.

### 339 **3. Model specification and estimation procedure**

#### 340 **3.1 Cumulative prospect theory**

##### 341 **3.1.1 Reference point**

342 Following Senbil and Kitamura (2004a) and Jou et al. (2008), in this study we set up three  
343 reference points for commuters: Earliest Acceptable Arrival Time (TE), Work Starting Time  
344 (TW), and Latest Acceptable Arrival Time (TL). An important difference from previous studies

345 that consider only the time change (e.g., Jou et al., 2008; Schwanen & Ettema, 2009) is that we  
 346 consider both temporal and monetary change relative to reference points, and hence CPT is  
 347 applied to gains and losses in multi-attribute utility.

### 348 **3.1.2 Observable component of the utility function**

349 Let's define  $v_s$  and  $t_s$  as the observable components of commuters' utility function and  
 350 the reference time in the scenario  $s = \{r, c\}$ ; and  $\beta_\tau$  and  $\beta_{VOT}$  as commuters' travel cost  
 351 coefficient and commuters' value of time, respectively. It should be noted that  $v_s$  is linear in  
 352 the parameters utility function that does not account for loss aversion, reference dependence,  
 353 or distortion in probability weighting, as in PT models.

354 The reference scenario ( $s = r$ ) corresponds to a pre-congestion charge situation in which  
 355 net utility  $v_r$  is composed of a free toll with no charge ( $\tau = 0$ ) and the benefit attained by  
 356 arriving at the reference arrival time ( $t_r$ ). In the post-congestion charge situation ( $s = c$ ), each  
 357 commuter needs to pay a congestion charge  $\tau$  and the benefit of arriving at the actual arrival  
 358 time ( $t_c$ ) is based on their departure time choices under congestion charge scenarios, in which  
 359 the actual arrival time is their arrival time in the congestion charge. Hence, when changing  
 360 from the pre-congestion charge situation to the post-congestion charge situation, travelers will  
 361 suffer a monetary loss from the congestion charge and will perceive a benefit or loss depending  
 362 on the deviation  $\Delta T = t_c - t_r$  between the actual and reference arrival time. Thus, the  
 363 deviation of observable utilities  $\Delta v$  between the post-congestion charge situation  $v_c$  and the  
 364 reference situation  $v_r$  is given by

$$365 \Delta v = v_c - v_r = \beta_\tau((\beta_{VOT}t_c) - \tau) - \beta_\tau(\beta_{VOT}t_r) = \beta_\tau(\beta_{VOT}(t_c - t_r) - \tau) = \beta_\tau(\beta_{VOT}\Delta T - \tau) \quad (1)$$

366 Note that the weight between  $\beta_{VOT}$  and  $\Delta T$  is by construction in monetary units, and the  
 367 parameter  $\beta_\tau$  multiplies the entire remainder of the function, which means that we seek to  
 368 obtain direct estimates of  $\beta_{VOT}$  through working in the willingness-to-pay space (Train &

369 Weeks, 2005). Here, several important assumptions have been used to formulate Eq. (1): First,  
370 commuters' Value-of-Time (VOT) is assumed to be linear in travel time; second, income  
371 effects are assumed away by using the willingness-to-pay space. These assumptions can be  
372 empirically tested using the data. However, since this study focuses on the estimation of CPT  
373 parameters, we chose not to test these effects, which could be explored in future studies.

374       There are three possible arrival times after implementing the congestion charge: on-time,  
375 earlier, and later arrivals; however, in this study we focus on the late and on-time arrival cases  
376 (i.e.,  $t_c \geq t_r$ ). This is based on the following considerations. (1) The results of previous  
377 empirical studies show that offering three or more possibilities would confuse respondents in  
378 the test phase and lead to lower response rates (Schwanen and Ettema, 2009). (2) Although  
379 including both early arrival and late arrival is the most typical choice in scheduling models  
380 (e.g., Adnan, 2010; Arnott et al., 1990; Cantelmo & Viti, 2019; Feil et al., 2009), focusing only  
381 on the late one or the early one is still correct, because it depends on the context under study  
382 (e.g., Arnott & Kraus, 1993, 1995; Kraus & Yoshida, 2002; Kraus, 2003; van den Berg &  
383 Verhoef, 2014). These theoretical studies usually ignore the late arrival of commuters, under  
384 the assumption that the shadow value of time late is infinite, since commuters will incur a  
385 heavy penalty for arriving late. However, in this empirical study, late arrival is an important  
386 situation that will lead to additional time costs for commuters and affect their departure time  
387 choices. (3) We followed the setup of Senbil and Kitamura (2004), which considers only three  
388 parts of the decision frame rather than the whole picture of commuters' departure time decision  
389 frame. Two are loss regions, which are defined as when commuters arrive later than the work  
390 starting time or the acceptable latest arrival time. Another is a gain region, which is defined as  
391 when commuters arrive after the acceptable earliest arrival time. The CPT parameters are thus  
392 estimated for these three alternative decision frames.

393 Finally, we also note that Chinese workers live in a culture that promotes overtime work,  
394 which means that they cannot go home earlier if they start working earlier. This causes workers  
395 to have no incentive to arrive early, and instead prefer to arrive at work right on time. At the  
396 same time, workers who choose to arrive early may not perceive the loss as we assume, since  
397 arriving early can help them establish a good image in the mind of their supervisor. We are  
398 unclear whether early arrival is a gain or loss for workers. Thus, we treat early arrival and on-  
399 time arrival indifference in our work—and given that the value of schedule delay late is always  
400 more negative than the value of early arrival (i.e., Small, 1982; Arellana et al., 2012), we  
401 believe that the penalty of late arrival is important and sufficient to cause commuters to choose  
402 their departure time. Hence, in this study we assume that commuters will incur additional time  
403 costs for late arrival and no time cost for arriving on time, without designing detailed gains for  
404 arriving early.

405 It is important to note that the difference between the actual and the reference arrival time  
406 ( $\Delta T$ ) is a quantity that is assumed to be known and a result of the information presented to  
407 participants across the decision scenarios. For on-time arrivals, the actual arrival time  $t_c$  is  
408 assumed to be equal to the reference arrival time  $t_r$ , and thus the deviation  $\Delta T$  is zero by  
409 construction (Eq. 1). For late arrivals, a predefined amount of lateness is assigned to  $\Delta T$  and  
410 it is allowed to vary depending on the reference point. As a consequence, the outcome of on-  
411 time arrivals only depends on the congestion charge commuters would have to pay.

412 For late arrivals (i.e., arrivals after the reference arrival time), it is plausible to assume that  
413 commuters will perceive a loss when arriving late if TW or TL are used as reference points.  
414 This loss can be interpreted as the value of time loss for the schedule delay that corresponds to  
415 the reference time. In contrast, when using TE as the reference point, late arrival will be  
416 perceived as a gain. This is because arriving before TE will be too early and will be a loss for  
417 commuters who value staying at home more than waiting at the workplace for that amount of

418 time. Conversely, arriving after TE will be perceived as a gain (Jou et al., 2008). Therefore,  
 419  $\Delta T$  will be negative with respect to the reference arrival times TW or TL and positive with  
 420 respect to TE. Hence, the absolute value of  $\Delta T$  becomes equals to

$$421 \quad |\Delta T| = \begin{cases} t_r - t_c, & \text{if } t_r = TW \text{ or } t_r = TL \\ t_c - t_r, & \text{if } t_r = TE \end{cases} \quad (2)$$

### 422 3.1.3 CPT value function

423 According to the CPT, the value function is

$$424 \quad V(x) = \begin{cases} x^\alpha, & x \geq 0 \\ -\lambda x^\beta, & x < 0 \end{cases}$$

425 where  $x$  represents the deviation between an outcome value—e.g., monetary charge, travel  
 426 time, or the utility of an alternative (Ghader et al., 2019)—and the reference point. Our model  
 427 equates  $x$  with  $\Delta v = v_c - v_r$ , which is the difference between the observable utilities with  
 428 and without a congestion charge. Thus, the CPT value function can be expressed as

$$429 \quad V(v_r, v_c) = \begin{cases} (v_c - v_r)^\alpha, & v_c \geq v_r \\ -\lambda(v_r - v_c)^\beta, & v_c < v_r \end{cases} \quad (3)$$

430 When the post-congestion charge situation is better than the reference situation,  
 431 commuters would perceive a gain ( $v_c - v_r \geq 0$ ); when it is worse, commuters would perceive  
 432 a loss ( $v_c - v_r < 0$ ). If  $(v_c - v_r)$  is replaced by Eq. (1), the value function can be expressed in  
 433 terms of  $T$  and  $\tau$  as shown below:

$$434 \quad V(T, \tau) = \begin{cases} [\beta_\tau(\beta_{VOT}\Delta T - \tau)]^\alpha, & v_c - v_r \geq 0 \\ -\lambda\{-[\beta_\tau(\beta_{VOT}\Delta T - \tau)]\}^\beta, & v_c - v_r < 0 \end{cases} \quad (4)$$

435 where  $\alpha$  and  $\beta$  ( $0 < \alpha, \beta < 1$ ) are risk preference parameters and represent the corresponding  
 436 degree of risk aversion or risk-seeking behavior in the gain and loss domains.  $\lambda$  is the loss-  
 437 aversion coefficient, which is expected to be greater than 1 ( $\lambda > 1$ ). Except for the case in  
 438 which the reference point is set as the Acceptable Earliest Arrive Time (TE), we only consider

439 the loss domain of the value function ( $\Delta T \leq 0, \tau \geq 0$ ). In addition, to avoid overfitting the  
 440 model, we set  $\alpha = \beta$ , which means that a single parameter is fitted for the exponents of both the  
 441 gain and loss domains of the value function (Tversky & Kahneman, 1992; Harrison & Rutström,  
 442 2008; Schwanen & Ettema, 2009).

443 To further explore commuters' heterogeneities of behavior under uncertainty, we also  
 444 incorporated the interactions of each CPT parameter with social economics variables in the  
 445 value function and the weighting function. The covariates interact with the parameters  
 446 according to the following specification:

$$447 \quad \alpha = \bar{\alpha} * (1 + \Delta\alpha * \mathbf{X}_i)$$

$$448 \quad \lambda = \bar{\lambda} * (1 + \Delta\lambda * \mathbf{X}_i)$$

$$449 \quad \gamma = \bar{\gamma} * (1 + \Delta\gamma * \mathbf{X}_i)$$

450 where  $\bar{\alpha}$ ,  $\bar{\lambda}$ ,  $\bar{\gamma}$  are the means of parameters  $\alpha, \lambda, \gamma$ .  $\mathbf{X}_i$  is a vector of covariates, and  $\Delta\alpha$ ,  
 451  $\Delta\lambda$ ,  $\Delta\gamma$  are parameter vectors associated with characteristics  $X_i$ , which captures the  
 452 heterogeneous impact of covariates on each CPT coefficient.

### 453 3.1.4 Probability-weighting function

454 In the original PT, the weighting function is

$$455 \quad W(p)^+ = \frac{p^{\gamma^+}}{(p^{\gamma^+} + (1-p)^{\gamma^+})^{1/\gamma^+}} \cdot W(p)^- = \frac{p^{\gamma^-}}{(p^{\gamma^-} + (1-p)^{\gamma^-})^{1/\gamma^-}} \quad (5)$$

456 where  $W^+$  and  $W^-$  indicate the decision weights in the gains and losses domains,  
 457 respectively. In our application,  $p$  is defined as the probability of arriving on time or late, and  
 458 thus  $\gamma^+$  and  $\gamma^-$  are estimable parameters that moderate the level of distortion in the  
 459 probability judgment regarding on-time arrival. A common parameter is estimated for both  
 460 gain and loss domains ( $\gamma^+ = \gamma^- = \gamma$ ) to avoid overfitting (Harrison and Rutström, 2008;

461 Harrison and Rutström, 2009; Schwanen and Ettema, 2009; Ghader et al., 2019). Also,  
 462 following the setting of Schwanen and Ettema (2009), we assume that  $p$  is departure time-  
 463 specific. This is to say that the probability of arriving on time or late will change along with  
 464 the user's departure time choices. The earlier the user chooses to depart, the higher the  
 465 probability they will arrive on time.

466 According to Tversky and Kahneman (1992), to define the cumulative weighting function,  
 467 the outcome of each position should be arranged in increasing order. Then, decision weight  $\pi_i$   
 468 associated with an outcome  $i$  is the difference between the weight of outcomes that are strictly  
 469 better/worse than the outcome  $i$  and outcomes that are at least as good/bad as outcome  $i$ .  
 470 Then, the cumulative decision weight of outcome  $i$  can be deemed to be its marginal  
 471 contribution. In this study, commuters only face two outcomes: arrive on time  $\Delta v^o$  or arrive  
 472 late  $\Delta v^l$ . There are three types of situations:

473 1. When  $\Delta v^o < 0 < \Delta v^l$ , which occurs when using TE as the reference point,

$$474 \quad \pi_o = W(p_o)^-, \pi_L = W(p_L)^+ \quad (6)$$

475 2. When  $\Delta v^o < \Delta v^l \leq 0$  or  $\Delta v^o > \Delta v^l \geq 0$ ,

$$476 \quad \pi_o = W(p_o)^{+/-}, \pi_L = 1 - W(p_o)^{+/-} \quad (7)$$

477 3. When  $\Delta v^l < \Delta v^o \leq 0$  or  $\Delta v^l > \Delta v^o \geq 0$ ,

$$478 \quad \pi_L = W(p_L)^{+/-}, \pi_o = 1 - W(p_L)^{+/-} \quad (8)$$

### 479 3.1.5 The prospect

480 In CPT, commuters' utility attained by some outcome (e.g., arriving late) is given by the  
 481 cumulative prospect value (CPV) function. Similar to the expected utility function,  $EU =$   
 482  $\sum_I p_i u(x_i)$ —i.e., the cumulative prospect value is the product of the subjective value

483 (calculated by the value function) and the associated probability (calculated by the weighting  
484 function), which in this case is

$$485 \quad CPV(T, \tau, p) = \pi_o V(\Delta v^o) + \pi_L V(\Delta v^l) \quad (9)$$

486 Since we didn't include early arrival in the experimental setup, only three parts of the  
487 decision frames have been considered, rather than the whole picture of commuters' departure  
488 time decision frame (Senbil & Kitamura, 2004). Two are loss regions, which are defined as  
489 when commuters arrive later than the working starting time (TW) or the acceptable latest  
490 arrival time (TL). Another is the gain region, which is defined as when commuters arrive after  
491 the acceptable earliest arrival time (TE). CPT parameters are thus estimated for these three  
492 alternative decision frames.

493

### 494 **3.2 Mixed logit model**

495 The logit formulation has been widely used in studies that estimate travelers' behavioral  
496 choices based on PT/CPT (Ghader et al., 2019; Schwanen & Ettema, 2009; Wen et al., 2019).  
497 Given that respondents were asked a series of hypothetical choice questions on the SP survey,  
498 a mixed logit model was used to account for panel effects (Train, 2009). We specified the utility  
499 of alternative departure time  $j$  for individual  $n$  in scenario  $t$  as

$$500 \quad CPU_{jnt} = CPV_{jnt} + \mu_{jn} + \varepsilon_{jnt} \quad (10)$$

501 where  $CPU_{jnt}$  is the CPV for individual  $n$  associated with alternative  $j$  in scenario  $t$ .  $\mu_{jn}$   
502 follows a normal distribution across individuals but is constant across all scenarios answered  
503 by the same respondent, which accounts for the panel correlation;  $\varepsilon_{jnt}$  is a random term with  
504 *iid* extreme value distribution.



505 Let us consider a sequence of alternatives, one for each scenario,  $\mathbf{j} = \{j_1, \dots, j_T\}$ . Once  
 506  $CPV_{jnt}$  is calculated for all of the alternatives using CPT, conditional on  $\mu_{jn}$ , the probability  
 507 that individual  $n$  makes this sequence of choices is the product of logit formulas (Train, 2009):

$$508 \quad L_{nj}(\mu) = \prod_{t=1}^T \left[ \frac{e^{(CPV_{jnt} + \mu_{jn})}}{\sum_j e^{(CPV_{jnt} + \mu_{jn})}} \right] \quad (11)$$

509 The unconditional probability is the integral of  $L_{nj}(\mu)$  over the distribution of the random  
 510 term  $\mu$ :

$$511 \quad P_{nj} = \int L_{nj}(\mu) g(\mu|\Omega) d\mu \quad (12)$$

512 where  $g(\mu|\Omega)$  is the probability density function of  $\mu$  with a vector of parameters  $\Omega$ .

513 Since the integral in Eq. (13) does not have a closed form, this is approximated by  
 514 simulation. The simulated log-likelihood (SLL) function is given by

$$515 \quad SLL(\Omega) = \sum_{n=1}^N \ln \left[ \frac{1}{R} \sum_{r=1}^R L_{nj}(\mu_{r,jn}) \right] \quad (13)$$

516 where  $\mu_{r,jn}$  is the  $r^{th}$  draw from  $g(\mu|\Omega)$  for each alternative departure time  $j$  and  
 517 individual  $n$ .  $R$  is the total number of draws.

518 To ease optimization of the highly non-convex likelihood function that arises due to the  
 519 functional form of the CPT utility function, a GA is used in this study. A distinctive feature of  
 520 this method is that it is gradient free and has been successfully applied in prior work using CPT  
 521 to model departure time choices (Schwanen and Ettema, 2009). Details of the estimation  
 522 procedure are provided in Appendix A. However, it is important to note here that when using  
 523 a GA, solutions vary in different estimation runs. The estimation process must be repeated  
 524 several times and estimated parameters of the best solutions in each run averaged. In this study,  
 525 for the basic ML model, we repeated the estimation process 10 times. Each time we used  $R=500$   
 526 draws for a total of 5,000 iterations. A disadvantage of the GA is that the estimation process is

527 extremely time-consuming, and the estimation time increases exponentially with R. For these  
528 reasons, only results for the best ML model estimated, including panel effects and  
529 heterogeneity, is included.

## 530 **4. Research design**

### 531 **4.1 Stated preference experiment**

#### 532 **4.1.1 The design of congestion charge schemes**

533 Since congestion charges have not been implemented in Beijing or in other Chinese cities,  
534 we used an SP experiment to collect data on how respondents would choose their departure  
535 time if hypothetical congestion charging scenarios were implemented. In designing the  
536 congestion charging scheme, the most important and basic aspects are charging type, charging  
537 time, and charging fee.

538 For the charging type and charging time, according to Jou et al.'s (2007) study of the  
539 acceptability of congestion charging for car and motorbike drivers in Taiwan, a time-based  
540 charge in a certain area is more acceptable than a fixed charge. Therefore, in this study, we  
541 designed a time-based congestion charge on congested roads.

542 For the charging fee, international experience has shown that the daily congestion charge  
543 is about 5%-10% of local residents' average daily disposable income (Lu & Cui, 2016). In  
544 2017, Beijing's per capita disposable income was 57,230 yuan (about 7,390.91 euros). Thus,  
545 based on this research, a reasonable charging fee in Beijing would range between 10.96 and  
546 21.92 yuan (about 1.42-2.83 euros) per day.

547 In addition, we chose 7:00 a.m. to 9:30 a.m. as the charging time, based on the morning  
548 peak hours used in the 2016 Beijing Transportation Development Annual Report. As shown in

549 **Table 2**, the charging time is evenly divided into five periods. The charging fee changes in  
 550 each scenario and takes a symmetrical inverse-U shape, which means that the congestion fee  
 551 is the highest during the most congested time. We designed four charging schemes, in which  
 552 the charging fee gradually increases from scheme 1 to scheme 4.

553 **Table 2** Congestion charge schemes

Time- based congestion charge	Time when you reach the congested road	Charging fee (¥)			
		Scheme 1	Scheme 2	Scheme 3	Scheme 4
	7:00 a.m. -7:30 a.m.	5	10	15	20
	7:30 a.m. -8:00 a.m.	10	15	20	25
	8:00 a.m. -8:30 a.m.	15	20	25	30
	8:30 a.m. -9:00 a.m.	10	15	20	25
	9:00 a.m. -9:30 a.m.	5	10	15	20

554

#### 555 **4.1.2 Design of arrival situations for multiple reference points**

556 Three reference points—Acceptable Earliest Arrival Time (TE), Work Starting Time (TW),  
 557 and Acceptable Latest Arrival Time (TL)—were considered in this study. Based on our pilot  
 558 survey, we found that the majority of respondents were willing to accept being late within 10  
 559 minutes. Therefore, under each reference point we presented three possible arrival times: (1)  
 560 arriving at the reference arrival time, (2) arriving 5 minutes late, and (3) arriving 10 minutes  
 561 late. It is plausible that commuters could arrive later than the TE reference point. As shown in  
 562 **Table 3**, the situation corresponding to a 5-minute late arrival was used for TW and TL, and  
 563 the situation of a 10-minute late arrival was used for TE. When commuters arrived at the  
 564 reference arrival time, the deviation between actual and reference arrival time is  $\Delta T = 0$ .  
 565 When commuters arrive 5 minutes late,  $\Delta T = -5$  for TW and TL. When commuters arrive  
 566 10 minutes late,  $\Delta T = 10$  for TE.

**Table 3** Reference points and possible arrival situations

Reference point	Possible situation	Probability
Acceptable Earliest Arrival time (TE)	Arriving at the company at the reference time. Arriving at the company 10 minutes after the reference time.	50% 50%
Work Starting Time (TW)	Arriving at the company at the reference time. Arriving at the company 5 minutes after the reference time.	50% 50%
Acceptable Latest Arrival Time (TL)	Arriving at the company at the reference time. Arriving at the company 5 minutes after the reference time.	50% 50%

Each outcome had an initial 50% probability (i.e.,  $p_O^* = p_L^* = 0.5$ ). This is based on respondents' feedback on the pilot survey. In the experiment, however, the probability of each outcome changes based on respondents' departure time choice. If they depart earlier, the probability of arriving late decreases and otherwise increases.

#### 4.1.3 Scenarios and the questionnaire

The scenarios used in this study manipulated three components: reference points, possible arrival situations, and congestion charge schemes. We kept all combinations of the three reference points and four congestion charge schemes—i.e., 12 scenarios. To reduce cognitive effort and improve the accuracy of their answers, we blocked these 12 scenarios into three groups of four scenarios each. Each group contains four congestion charge schemes with one reference point; thus we have three types of questionnaires with different scenarios. Each respondent was randomly assigned one type of questionnaire. In each questionnaire, respondents were presented with four scenarios in sequence; each included two possible arrival situations and one congestion charge scheme (as shown in **Figure 2**). Note that learning effects may be observed in experiments that consider sequential choices. However, this effect is not

583 strong, with only 4 sequential choices, since it usually appears with more iterations (Viti et al.,  
 584 2005). Thus, we did not capture learning effects in our models.

585 Several measures have been used to encourage respondents to recall an actual commuting  
 586 trip and reduce hypothetical bias as much as possible (Arellana et al., 2012). First, before the  
 587 four scenarios, a general description was shown to respondents. For example, for respondents  
 588 who were assigned to the questionnaire with TW as the reference point, the description was:  
 589 “Assume that the Work Starting Time will be the reference arrival time for your morning  
 590 commuting trip, and a time-different congestion charge policy will be implemented on the road  
 591 you use. That is to say, the congestion charge fee that you are asked to pay varies based on the  
 592 time you enter the congested road. Under the following four different congestion charge  
 593 scenarios, when would you like to depart?” Second, before responding to the first scenario, we  
 594 asked respondents to write down their reference arrival time for the morning commuting trip  
 595 (e.g., work starting time for the questionnaire on TW). This is to say that the values of each  
 596 reference point were customized with respect to the actual working time participants declared.  
 597 Then, we asked them to report their regular departure time if they were using the above self-  
 598 reported arrival time as a reference, in order to remind them of an actual commuting context.

1. Work starting time \_\_\_\_\_  
 2. When is your regular departure time? \_\_\_\_\_

Scenario 1		
Reference time	Work starting time	
Arrival situations	Possible arrival time	
	Arriving at the company at the reference time.	50%
	Arriving at the company 5 minutes later.	50%
Charging time-differentiated congestion fee	The time when you reach the congested road section.	
	7:00a.m.-7:30a.m.	5¥
	7:30a.m.-8:00a.m.	10¥
	8:00a.m.-8:30a.m.	15¥
	8:30a.m.-9:00a.m.	10¥
9:00a.m.-9:30a.m.	5¥	

3. According to the above scenario, will you change your departure time? (Every 10 minutes earlier/later, the probability of arriving on time will increase/decrease by 10%)

A. 50 and more than 50 minutes earlier	B. 40 minutes earlier	C. 30 minutes earlier
D. 20 minutes earlier	E. 10 minutes earlier	F. Not change
G. 10 minutes later	H. 20 minutes later	I. 30 minutes later
J. 40 minutes later	K. 50 and more than 50 minutes later	

599  
 600 **Figure 2** A sample question in the SP experiment using TW as the reference point (translated from Chinese)

601 In each scenario, respondents made departure time choices. We assumed that the departure  
602 time change did not affect travel time itself, but rather the probability of being early or late  
603 (Noland & Small, 1995). Hence, the probability of arriving on time  $p_o$  and the probability of  
604 arriving late  $p_L$  in each scenario changed depending on respondents' departure time choice.  
605 They were also told that departing 10 minutes earlier or later increased/decreased  $p_o$  by 10%,  
606 and  $p_L$  correspondingly decreased/increased by 10%, which means:

$$607 \quad p_o = \begin{cases} p_o^* + t10\% & \text{if depart earlier} \\ p_o^* - t10\% & \text{if depart later} \end{cases} \quad (14)$$

$$608 \quad p_L = \begin{cases} p_L^* - t10\% & \text{if depart earlier} \\ p_L^* + t10\% & \text{if depart later} \end{cases} \quad (15)$$

609 where  $p_o^*$  and  $p_L^*$  are the initial probabilities of on-time and late arrivals, which are set to 50%  
610 based on respondents' feedback in the pilot survey, and  $t$  is the tenth digit of the advance or  
611 delay time. Also, the charging fee  $\tau$  respondents would pay depends on the congestion charge  
612 scheme, their regular departure time, and the departure time change they chose. Respondents  
613 could immediately know the congestion charge cost and possible arrival situations when they  
614 made the choice decision for each scenario.

615 On the questionnaire, we also asked about individuals' socioeconomic, household, and  
616 commuting characteristics. The socioeconomic characteristics are gender, age, income,  
617 education, and job. The household characteristics are marital status, number of school-age  
618 children, car ownership, and need to pick up children/partner or not. The commuting  
619 characteristics are commuting distance, commuting time, commuting mode, residential  
620 location, and workplace; working time flexibility; transportation information: the quality of  
621 traffic information during their travel and road familiarity; and tolerance of lateness. These  
622 factors, which are likely to influence commuters' departure time choices, have been discussed

623 in previous literature (Ben-Elia & Ettema, 2011; Hamed & Olaywah, 2000; Saleh & Farrell,  
624 2005; Steed & Bhat, 2000).

625 For working time flexibility, we did not ask details about constraints at work (as  
626 recommended by Thorhauge et al., 2016), but instead whether respondents were fully flexible,  
627 not flexible at all, or if they could arrive up to 30, between 30 and 60, or between 60 and 90  
628 minutes later/earlier<sup>1</sup>. The maximum late arrival respondents could tolerate also indicates the  
629 maximum late flexibility they can accept subjectively. In addition, we asked about their value  
630 of time: “Suppose that you depart 30 minutes earlier so as to avoid rush-hour congestion in  
631 your commuting trip. That means you have to give up time for resting or doing other things.  
632 Compared with half an hour’s salary, how much do you think is the cost of departing half an  
633 hour early?”

## 634 **4.2 Participants and data collection**

635 The survey was conducted in November 2017, and questionnaires were distributed online  
636 and on-site. Network platforms such as Wechat, QQ (social software), and Wenjuanxing (a  
637 professional questionnaire distribution website) were used for online distribution. The target  
638 population was car commuters in Beijing. Two screening questions were included at the  
639 beginning of the questionnaire to exclude respondents who used travel modes other than a car  
640 (“What is your regular travel mode for morning commuting?”). Those who could set their  
641 working time themselves and work from home were also excluded, since they were not  
642 considered to be regular morning peak commuters. We collected a total of 400 questionnaires,  
643 of which 317 were valid after excluding respondents who met either of the above conditions.  
644 Since each respondent has 4 observations, we obtained 1,268 observations in total. This sample

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<sup>1</sup> In Beijing, the morning peak can last for 3 hours (7 a.m. to 9 a.m.) in some places. It is thus possible that 90 minutes after the usual starting time is still within the morning peak.

645 size is in line with many SP studies on departure time (e.g., Arellana et al, 2012, use a sample  
646 of 357 respondents, and Thorhauge et al., 2016, used 286). Our sample is also larger than many  
647 previous studies that also estimated PT or CPT parameters. For example, Ghader et al. (2019)  
648 used 409 observations; Jou et al. (2008) used 152 respondents and 454 observations; and Senbil  
649 and Kitamura (2004) used 210 respondents and 630 observations. Since the CPT model is  
650 highly nonlinear, future studies could use even more respondents and observations to fit the  
651 models.

652 **Table 4** Sample description

Variables	Categories	Percentage
Gender	male	53.0
	female	47.0
Age	20-25	12.6
	26-30	38.2
	31-40	29.3
	41-50	17.0
	>50	2.8
Education	≤ high school	8.8
	junior college	23.0
	college	48.6
	master	18.3
Income per month	Ph. D	1.3
	≤5,000 yuan	11.4
	5,000~10,000 yuan	39.1
	10,001~15,000 yuan	26.5
Marital status	15,001~20,000 yuan	14.8
	>20,000 yuan	8.2
	single	29.0



	married	71.0
	0	.9
Car ownership	1	73.2
	$\geq 1$	25.9
	no flexibility	71.3
Working flexibility	up to 30 mins earlier/later	17.4
	between 30 and 60 mins earlier/later	9.8
	between 60 and 90 mins earlier/later	1.6
	0	56.8
	1~5 mins	19.2
Tolerance of lateness	6~10 mins	11.7
	11~15 mins	6.9
	>15 mins	5.4

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653 As shown in **Table 4**, the percentage of males (53%) is slightly higher than that of females  
654 (47%), which is consistent with the gender ratio of the population (male: 51.11%; female:  
655 48.89%) in Beijing in 2017 (NBS, 2017). Most of our respondents are 26 to 40 years old, and  
656 more than 50% have a bachelor's degree or above. Also, 60.1% of respondents have a monthly  
657 income greater than 10,000 yuan, and about 26% have more than one car. According to the  
658 China Population and Employment Statistics Yearbook 2017 (NBS, 2017), 52.7% of urban  
659 employed persons in China are younger than 40 years old, 34.4% of employed persons in  
660 Beijing have a bachelor's degree or above, and the 2017 mean per capita monthly income for  
661 Beijing is about 8,467 yuan. Compared with the average employed population in Beijing, our  
662 sample is younger, higher educated, and richer. However, given that our sample only includes  
663 private car commuters, these results are not surprising. Also, 71.3% of respondents do not have  
664 flexible working time, and 56.8% can't tolerate any late arrivals. Of those who could tolerate  
665 arriving late, more than two-thirds report a tolerance within 10 mins, with the largest share  
666 being within 1~5 mins.

**Table 5** Commuting characteristics

Variables	Categories	Mean	S.D.
Commuting time	10 mins, 20 mins, ....., 100 mins	33.18	41.04
Commuting distance	<2 km, 2~6 km, 6~10 km, ....., 26~30 km, >30 km	12.19	7.05
VOT (yuan/min)	0~5 yuan/half hour, 6~10, 11~15, 16~20, 21~30, 31~40, >40	0.69	0.53
Quality of traffic information	1 (Low) to 3 (High)	1.54	0.50
Degree of road familiarity	1 (very unfamiliar) to 7 (very familiar)	3.91	1.81
Degree of traffic congestion	1 (very uncongested) to 7 (very congested)	4.73	1.58

668 As shown in **Table 5**, the average commuting time and commuting distance are 33.18  
669 minutes and 12.19 km separately. According to the Fifth Comprehensive Investigation Report  
670 of Beijing Urban Traffic (BMCT & BTI, 2016), the average commuting time and commuting  
671 distance by private car are 49.1 minutes and 13.5 km, which is slightly longer than what our  
672 sample reported. The average score for the quantity of traffic information they obtained during  
673 commuting is 1.54, with 14.8% of commuters choosing high and 31.5% choosing low. The  
674 average score for road familiarity is 3.91, and the percentage for commuters who are not  
675 familiar with the road network in Beijing is 45.1%. The average score for traffic congestion is  
676 4.73, which shows that the majority (65.6%) believe that traffic is congested when they  
677 commute in the morning. The stated average value of time (VOT) for our sample is 0.69 yuan  
678 per minute, with the highest value of 1.67 yuan per minute and the lowest value of 0.17 yuan  
679 per minute.

### 680 **4.3 Descriptive statistics**

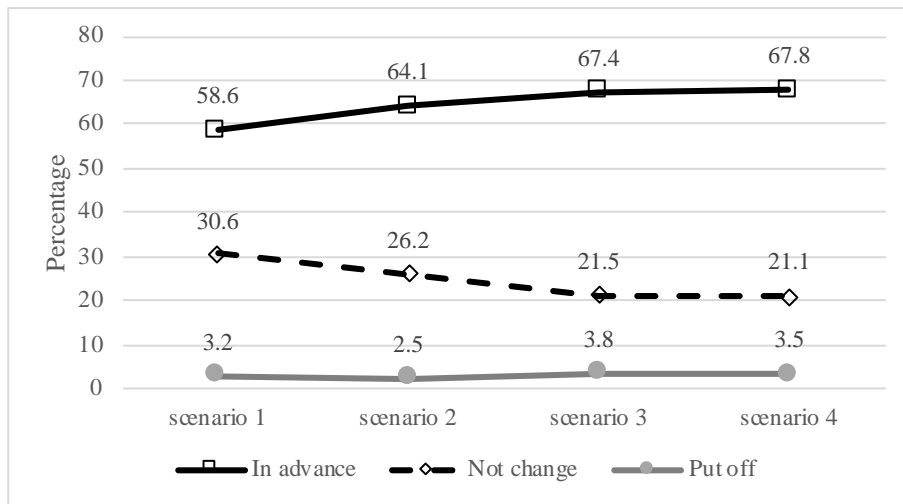
681 We first analyze the results using simple descriptive analyses. Results show that the  
682 majority (58.6%~67.8%) of car commuters would change their departure time under the

683 congestion charge scenarios presented (shown in **Table 6** and **Figure 3**). With the increase in  
 684 charging fees (from scenarios 1 to 4), the proportion of respondents who would not change  
 685 their departure time gets smaller. Most commuters choose to depart early rather than late, which  
 686 is in line with previous results in departure time choice models, and is related to constraints on  
 687 work starting time (Thorhauge et al., 2016).

688 **Table 6** Departure time change under different congestion charge scenarios

Departure time change	Scenario 1	Scenario 2	Scenario 3	Scenario 4
≥50 mins	5.4%	6.9%	9.1%	12.6%
40 mins	10.7%	13.2%	15.5%	13.6%
30 mins	18.3%	19.2%	21.1%	21.1%
20 mins	11.7%	13.2%	11.7%	10.7%
10 mins	12.6%	11.4%	10.1%	9.8%
Sum	58.6%	64.1%	67.4%	67.8%
Not change	30.6%	26.2%	21.5%	21.1%
10 mins	3.2%	2.5%	3.8%	3.5%
20 mins	3.2%	2.8%	3.2%	2.5%
30 mins	3.8%	3.5%	3.5%	4.1%
40 mins	0.3%	0.6%	0.3%	0.6%
≥50 mins	0.3%	0.3%	0.3%	0.3%
Sum	10.8%	9.7%	11.15	11.15

689 With the increase in charging fees, the proportion of commuters who depart earlier  
 690 increases faster than the proportion of those who depart later (see **Figure 3**). However, when  
 691 the charging fee reaches a relatively high level (scenario 3), the changes are negligible. We can  
 692 see that private car commuters prefer to depart early rather than late under congestion charge  
 693 scenarios.



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**Figure 3** Departure time change under different congestion charge scenarios

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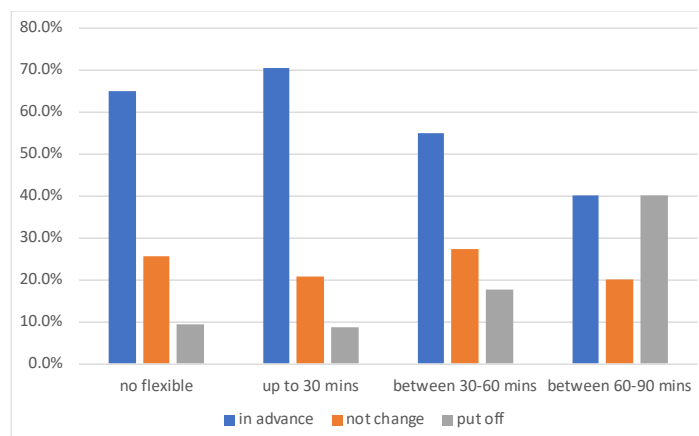
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We then compared the departure time choice among commuters with different degrees of work flexibility. The percentages of three departure time choices within each flexibility group are shown in **Figure 4**. From left to right, we can see that as work flexibility increases (from not flexible to “can arrive 60-90 mins earlier/later”), the percentage of respondents who chose to depart earlier decreases (from 70% to 40%) and the percentage of those departing later increases (from 10% to 40%). The percentage of respondents who did not change their departure time is similar among these four flexibility groups. This may imply that commuters with less work flexibility are more likely to depart earlier to avoid being late when the congestion charge is introduced. In contrast, those who have greater work flexibility have more choices; they can avoid rush hour congestion by departing either earlier or later.



706

707

**Figure 4** Departure time changes for commuters with different flexibility

708 **5. Results**

709 **Table 7** shows the average value of each coefficient, the average value of the log-  
 710 likelihood, and the corresponding BIC value over the multiple runs of GA in the basic ML  
 711 model. A backward stepwise procedure has been implemented manually, whereby  
 712 specifications have been assessed based on the improvement in log-likelihood and BIC, the  
 713 statistical significance of each socioeconomic variable, and conceptual plausibility.

714 A one-tailed t-test was conducted for  $\alpha$ ,  $\lambda$ ,  $\gamma$ , and  $\beta_{VOT}$  against 1 for the parameter's  
 715 value and against zero for  $\beta_{\tau}$ , the ASC of departing later, and the ASC of departing earlier.  
 716 The alternative specific constants (ASCs) for departing later and earlier are significantly  
 717 negative, which implies that commuters are more likely to keep their current departure time  
 718 rather than departing earlier or later.

719 **Table 7** Estimated coefficients for models with socioeconomic variables

Parameters	Values	(st. errors)
$\alpha$	0.459***	(0.092)
$\lambda$	1.429**	(0.163)
$\gamma$	0.567***	(0.060)
$\beta_{VOT}$	0.605***	(0.084)
$\beta_{\tau}$	0.248***	(0.056)
$\Delta\alpha_{\text{Male}}$	0.891***	(0.292)
$\Delta\alpha_{\text{Need to pick up children/partner}}$	-0.220**	(0.264)
$\Delta\lambda_{\text{School child(ren)}}$	0.235**	(0.386)
$\Delta\lambda_{\text{Need to pick up children/partner}}$	-0.367***	(0.388)
$\Delta\gamma_{\text{Degree of traffic congestion}}$	0.033***	(0.035)
ASC of departing later	-6.684***	(1.210)
ASC of departing earlier	-3.298***	(0.804)

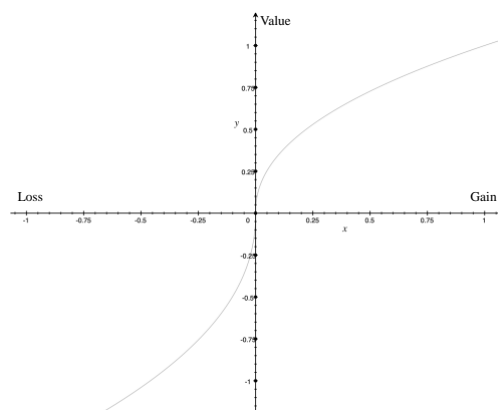
Standard deviation of $\mu$	-1.358	(5.796)
Number of observations	1,268	
Log-likelihood	1,342.965	
BIC	2,757.382	

720 Note: The results of each model are the average results of 10 runs. \*\*\*p < 0.01, \*\*p < 0.05.

721

## 722 5.1 CPT parameters

723 The estimation results provide evidence of risk-aversion/-seeking behavior, loss aversion,  
724 and probability distortion. Risk preference parameter  $\alpha$  equals 0.459 and is significantly  
725 smaller than 1, which implies that commuters are not risk neutral. In line with previous studies  
726 (e.g., Senbil & Kitamura, 2004b, 2004a; Tversky & Kahneman, 1992), our results show that  
727 car commuters are risk averse when they perceive gains and risk seeking when they perceive  
728 losses under congestion charge contexts. **Figure 5** shows the resulting S-shaped value function,  
729 which is concave for time gains and convex for time losses. Loss-aversion parameter  $\lambda$  is  
730 significantly larger than 1, with a magnitude larger on departure time choices than in previous  
731 studies (Senbil & Kitamura, 2004b, 2004a). This result suggests that commuters are more  
732 sensitive to losses in a congestion charge scenario.

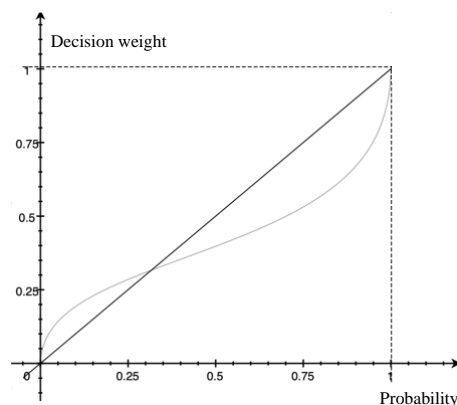


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**Figure 5** Estimated value function

735 Commuters exhibited a distortion in probability weighting when facing the uncertainty of  
736 the congestion charge context. The weighting function parameter  $\gamma$  equals 0.567, which is  
737 significantly lower than 1 and lower than the estimates ( $\gamma=0.61-0.69$ ) obtained by Tversky and  
738 Kahneman (1992) in monetary experiments. As shown in **Figure 6**, the curvature of the  
739 estimated weighting function is far from a straight line. In fact, the largest gap between  
740 objective probability and decision weighting was about 0.5, which means that commuters  
741 overweight small probabilities and underweight larger probabilities; thus the degree of  
742 distortion is considerable. Note that this result is smaller than that of previous studies on road  
743 users' mode decisions (Ghader et al., 2019; Schwanen & Ettema, 2009). This suggests that  
744 commuters have a less accurate valuation of the objective probability (i.e., are more irrational)  
745 when making departure time choices. Given that effects such as inflating small probabilities  
746 become evident when losses are perceived as significant, we compared our results and in  
747 particular, the estimates of Schwanen and Ettema (2009). They use a similar setup for delay  
748 values (on-time, 5-minute delay, 10-minute delay) in their study of Dutch parents, but show  
749 lower weighting distortion. This demonstrates that our results reflect the special behavioral  
750 characteristics of Beijing commuters, rather than a bias caused by the setup using small delay  
751 values.



752

753

**Figure 6** Estimated decision-weighting curve

754 Moreover, the average  $\beta_{VOT}$  of our samples equals 0.605 and is statistically significant at  
755 the 99% confidence level. This means that the average VOT across our sample is 0.61 yuan  
756 per minute—i.e., 36.6 yuan per hour—which is much lower than their stated value in the survey  
757 (0.69 yuan per minute). Given the average hourly wage in Beijing, calculated based on the  
758 average monthly wage in 2017 (BMHRSSB & BMBS, 2018) and the hourly wage conversion  
759 function used in China (MOHRSS, 2008)—50.81 yuan per hour—commuters would choose to  
760 spend 72% of their hourly wage to avoid a 1-hour travel delay.

## 761 **5.2 Systematic heterogeneities in CPT parameters**

762 Results show that the risk preference parameter  $\alpha$  is the parameter most sensitive to  
763 commuters' heterogeneous characteristics. Factors such as gender and whether they need to  
764 pick up children or a partner are statistically significant in terms of affecting the value of  $\alpha$ .  
765 The results show that gender (male=1, female=0) has a positive effect on  $\alpha$ , which implies that  
766 male commuters are less risk averse; this result is consistent with Schwanen and Ettema's  
767 (2009) findings. Compared with female commuters, male commuters are closer to risk neutral.  
768 Commuting time has a significantly negative impact on  $\alpha$ : The need to pick up children or a  
769 partner during commuting trips significantly decreases the value of  $\alpha$ . Commuters who have to  
770 consider not only their own schedules but also others' schedules are more risk averse. This  
771 additional consideration has the largest impact on  $\alpha$  of all the socioeconomic factors used in  
772 this study.

773 Compared with the risk preference parameter  $\alpha$ , the parameters  $\lambda$  and  $\gamma$  are relatively  
774 consistent among commuters with different socioeconomic characteristics. The loss-aversion  
775 parameter  $\lambda$  is impacted by having or not having school-age child(ren) and by having or not  
776 having to pick up children/a partner. Commuters who have school-age child(ren) are more loss  
777 averse than others. However, this increase could be offset if commuters also need to pick up



778 their children during commuting trips, since the need to pick up others can significantly  
779 decrease the value of  $\lambda$ . One possible explanation is that commuters share their losses with all  
780 passengers. Although they themselves suffer losses, their passengers may obtain gains from  
781 the same trip. Thus, commuters who also need to pick up other family passengers can be less  
782 sensitive to their own losses. The degree of traffic congestion has a positive effect on the  
783 weighting-function parameter  $\gamma$ . Commuters who regularly face congested commuting trips  
784 demonstrate a smaller degree of probability distortion—because they more are accustomed to  
785 coping with uncertain congestion than commuters who are used to smooth traffic—and this  
786 allows more accurate estimation of the objective probability of arriving late.

## 787 **6. Conclusion and policy implications**

788 This study contributes to the empirical estimation of travelers' behavioral mechanisms  
789 when making departure time choices under uncertain congestion charge scenarios. We  
790 conducted a stated preference experiment among commuters in Beijing to examine their  
791 departure time choice behavior under congestion charge scenarios based on cumulative  
792 prospect theory (CPT). Four time-differentiated congestion charge scenarios at different  
793 charging levels were designed for the experiment. Three reference points—Acceptable Earliest  
794 Arrival Time, Work Starting Time, and Acceptable Latest Arrival Time—were considered in  
795 the experiment. CPT utility functions and mixed logit models with panel effects have been used  
796 to estimate the departure time choice problem in congestion charge contexts. A genetic  
797 algorithm was adopted to estimate CPT parameters by maximizing the simulated log-likelihood  
798 function.

799 Our results are consistent with previous findings in the transport literature that apply CPT  
800 to travel decisions different from a congestion charge. Our findings support the presence of the  
801 bounded rational decision-making processes of commuters, which is more realistic and

802 counters the assumption of perfect rationality used in expected utility theory. Our evidence  
803 suggests that car commuters exhibit cognitive biases when making departure time choices  
804 under congestion charge scenarios. Therefore, all parameters that define the shape of the CPT  
805 value function—the exponents that moderate the risk preferences, the level of probability  
806 distortion, and the linear parameter for loss aversion—are statistically significant. The  
807 estimated CPT parameters differ from the results obtained by Tversky and Kahneman (1992)  
808 in lab experiments and in the context of monetary decisions. The difference in the parameters’  
809 estimates could be attributed to the fact that commuters show different levels of behavioral  
810 biases when making departure choices in congestion charge contexts compared with other  
811 contexts. The parameters estimated by this study could yield more accurate predictions to  
812 model travel behavior in congestion charging contexts. Also, we found significant systematic  
813 heterogeneity, and particularly in the risk preference parameter. Commuters’ characteristics,  
814 including gender, having school-age child(ren), commuting time, picking up child(ren)/a  
815 partner during the trip, the quantity of traffic information, and the degree of congestion during  
816 daily commuting trips significantly affect the value of CPT parameters. The results of this study  
817 could help decision makers better understand commuters’ behavioral responses to congestion  
818 charges and provide an important empirical reference for the design of congestion charge  
819 schemes.

820 From a policy insight, given the loss-aversion preference, more behavioral change among  
821 real commuters—in contrast to when we assume they are *homo economicus*—can be achieved  
822 by congestion charge. If policymakers realize the cognitive biases of commuters in the policy  
823 design stage, they can achieve the same policy target with less congestion charge levying on  
824 commuters, which is better for public acceptability. Also, commuters’ distortion in probability  
825 weighting is larger when making travel decisions under a congestion charge policy than  
826 previous estimations without policy incentives. This implies that commuters make their travel

827 choices less rationally under uncertain traffic contexts when facing a congestion charge policy.  
828 Another thing to notice is that a higher congestion charge may not always lead to more  
829 behavioral changes, given the risk-seeking behavior elicited when outcomes are framed as  
830 losses. When commuters get used to a relatively high congestion charge level, it is harder for  
831 them to change their behavior under a higher charge level. In that case, the better way to  
832 manage road demand is not to blindly increase the charge level, but to adjust the charging  
833 structure, for example, or try other policy instruments.

834 Future studies could further expand on our findings by designing decision scenarios that  
835 consider not only travel delays but also travel time savings and that allow travel times to vary  
836 among different departure time choices and congestion charge scenarios. Also, given the reality  
837 of Chinese workers' norms and the complexity of potential experimental designs, we only offer  
838 on-time arrival and late arrival as two possible arrival situations in the scenario. Future studies  
839 could include the full combination of early arrival, on-time arrival, and late arrival. More values  
840 of early arrival and late arrival can be used to describe a more precise value function curve and  
841 weighting function curve for commuters. Fitting the CPT value functions for time and  
842 monetary attributes separately could also reduce variance in the parameter estimates, and thus  
843 increase confidence in the hypothesis testing. In addition, CPT parameters for time choice,  
844 mode choice, and route choice, as well as specific behavioral parameters for evaluating the  
845 value of departure time and the value of the charging price, could be allowed to differ.  
846 Moreover, future studies can seek to account for unobserved heterogeneities of CPT parameters  
847 among travelers. Latent class models can be used for such analysis. Other congestion charge  
848 schemes rather than a time-differential charge can be used to test travelers' behavior in  
849 response to different congestion charge schemes.

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## 1081 **Appendix A**

1082 A genetic algorithm (GA) is a metaheuristic algorithm that can identify optimal solutions  
1083 through multiple iterations and transform the solution process into a process similar to the  
1084 crossing and mutation of genes in biological evolution (Goldberg, 1989). It has been used in  
1085 travel behavior studies (e.g., Schwanen & Ettema, 2009; Zong et al., 2012). Compared with  
1086 conventional optimization algorithms, the advantage of GA is that can help to avoid falling  
1087 into local optima. In addition, GA can find optimum solutions from the population with  
1088 maximal probability, regardless of whether the fitness function is discontinuous and unstable  
1089 or surrounded by great noise (Liu et al., 2007).

1090 In this paper, we use the GA toolbox in MATLAB software. The procedure can be  
1091 described as follows (Ettema & Timmermans, 2003; Goldberg, 1989) and is shown in **Figure**  
1092 **1**:

- 1093 1) Population: Define  $Q$  sets of estimated coefficients, where  $Q$  indicates the number  
1094 of candidate solutions and each candidate solution includes all coefficients that need  
1095 to be estimated.  $Q$  has been set to 200 which is the default choice in MATLAB for  
1096 models with more than five coefficients.
- 1097 2) Parameter encoding: We used the double vector as our population type, which is  
1098 also the default choice.
- 1099 3) Fitness scaling: Calculate SLL values for each candidate solution and convert the  
1100 raw fitness scores to values in a range that can be used by the selection function.  
1101 Here, we used the rank scaling function. Candidate solutions are ranked. A  
1102 candidate with rank  $r$  has a scaled score proportional to  $1/\sqrt{r}$ .
- 1103 4) Selection: Choose candidate solutions as the parents to be propagated to the next  
1104 iteration based on their scaled fitness scores. We used the remainder selection

1105 function, which means that candidates with higher scaled value will be listed as  
1106 parents more times.

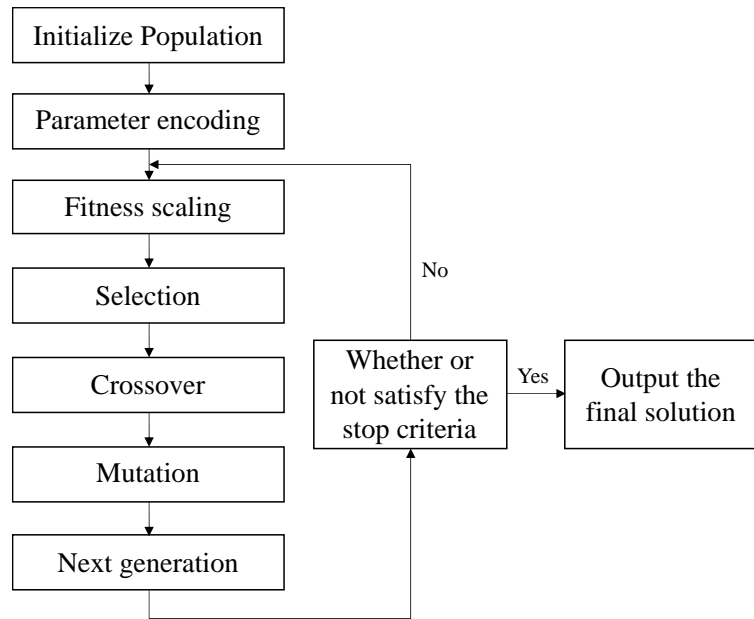
1107 5) Crossover: Combine two parents to form a new individual for the next generation.  
1108 First, two solutions are randomly selected from the matching pool generated by  
1109 propagation. Then, the binary solution strings are cut at a random point to cross  
1110 over.

1111 6) Mutation. Make small random changes in individuals to provide genetic diversity.  
1112 Since all CPT parameters have their own constraints, the default adaptive feasible  
1113 mutation function is chosen.

1114 7) For procedures that cover propagated, crossed over, and mutated parameters, the  
1115 SLL of each candidate solution is calculated and a new generation of populations is  
1116 generated for iteration. Go back to step 3 and repeat steps 3-6 until all coefficients  
1117 converge and output the coefficients.

1118 8) Several criteria are used to decide when to stop the procedure. We used the default  
1119 function tolerance and constraints tolerance. Also, the procedure will stop when it  
1120 has repeated 100 times the number of parameters. If there is no improvement within  
1121 30 generations, the procedure will stop.

1122 Given the above setting, the fitness function was calculated about 10,000 to 36,000 times  
1123 to find the best solution for each generation. Then, the procedure was repeated 3 times (i.e., 3  
1124 generations) and stopped—given that the function tolerance and constraint tolerance had been  
1125 reached—to obtain the best solution (i.e., the final point) for each run. Since the solutions of  
1126 GA vary in different estimation runs (Schwanen & Ettema, 2009), for each model we repeated  
1127 the estimation process 10 times. Then, t-tests of each coefficient were computed for the best  
1128 solutions in each run.



1129

1130

**Figure A1** The procedure for parameter estimation by GA