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Sanjay, Y., Prasad, S.K., Erdélyi, R. et al. (2024) On the formation height of low-corona and chromospheric channels of the atmospheric imaging assembly (AIA) onboard the solar dynamics observatory (SDO). *The Astrophysical Journal*, 975 (2). 236. ISSN: 0004-637X

<https://doi.org/10.3847/1538-4357/ad7d8c>

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On the Formation Height of Low-corona and Chromospheric Channels of the Atmospheric Imaging Assembly (AIA) onboard the Solar Dynamics Observatory (SDO)

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Received 2024 June 25; revised 2024 September 4; accepted 2024 September 14; published 2024 November 6

Abstract

The multiwavelength data from the Solar Dynamics Observatory is extensively used in studying the physics of the Sun and its atmosphere. In this study, we estimate the formation heights of low-corona and chromospheric channels of the Atmospheric Imaging Assembly (AIA) over the atmospheres of sunspot umbrae during the quiet condition period within 20 different active regions. The upward propagating slow magnetoacoustic waves of a 3 minute period, which are perpetually present in sunspots, are utilized for this purpose. Employing a cross-correlation technique, the most frequent time lag between different channel pairs is measured. By combining this information with the local sound speed obtained from the characteristic formation temperatures of individual channels, we estimate the respective formation heights. The median values of formation heights obtained across all active regions in our sample are 356, 368, 858, 1180, and 1470 km, respectively, for the AIA 1600, 1700, 304, 131, and 171 Å channels. The corresponding ranges in the formation heights are 247–453, 260–468, 575–1155, 709–1937, and 909–2585 km, respectively. These values are measured with respect to the Helioseismic Magnetic Imager continuum. We find the formation height of UV channels is quite stable (between 250 and 500 km) and displays only a marginal difference between the AIA 1600 and 1700 Å channels during quiet conditions. On the other hand, the formation height of coronal channels is quite variable.

Unified Astronomy Thesaurus concepts: [Magneto hydrodynamics \(1964\)](#); [Sunspots \(1653\)](#)

1. Introduction

One of the rapidly expanding realms within solar physics pertains to oscillations in the solar atmosphere, a domain widely explored through data derived from various instruments observing the Sun. The intricate wave behavior observed in the Sun can be ascribed to the density stratification, robust magnetic fields, and nonuniform temperature structure inherent in the solar plasma. The investigation into wave processes is particularly compelling due to their potential role in addressing crucial issues in coronal physics, including solar wind acceleration, coronal mass ejections, flare energy release, and the perplexing matter of solar atmospheric heating. The predominant periods in sunspot oscillations range from 3 to 5 minute bands (e.g., see the review by D. B. Jess et al. 2015). According to A. Bhatnagar et al. (1972), the photospheric oscillations in sunspots typically exhibit notable 5 minute periodicities combined with traces of 3 minute oscillations, but their power is very small as compared to the surrounding quiet Sun.

Interference between sound waves (p -modes) that propagate through the Sun's interior due to chaotic convection causes a dominant 5 minute global oscillation on the solar surface. In higher altitudes, the 5 minute oscillation is evanescent as the acoustic cutoff period around the temperature minimum is 280 s (B. Roberts 1983), and waves will not be able to travel against gravity above a cutoff period (H. Lamb 1909; N. Bel & B. Leroy 1977). But, 5 minute oscillations have also been

observed in higher altitudes (e.g., M. S. Marsh & R. W. Walsh 2006; K. Nagashima et al. 2007) because waves guided by inclined flux tubes have a higher cutoff period and allow for wave leakage into the solar environment (B. De Pontieu et al. 2004, 2005). But in the umbra, magnetic field lines are mostly vertical. So, the 5 minute period is the most prevalent in the photosphere of a sunspot, but as one rises into the chromosphere and corona, the 3 minute period becomes the dominant period (J. H. Thomas et al. 1987; J. T. Su et al. 2016). The driving mechanism behind these 3 minute oscillations remains a subject of debate. Currently, magnetoconvection (J. Chae et al. 2017) and external p -mode absorption (S. Krishna Prasad et al. 2015) are thought to be the two likely mechanisms causing the sunspot waves (E. Khomenko & M. Collados 2015).

At the photosphere, due to the high plasma- β ($\beta \approx 100$), p -modes are typically considered acoustic waves (N. R. Owen 2012). However, within the umbra, where $\beta \approx 1$ (I. H. Cho et al. 2017), these acoustic waves interact with the magnetic field in the magnetized environment of a sunspot, transforming into magnetoacoustic waves (MAWs). As these waves are often compressible, their propagation affects the plasma pressure, which makes them easily detectable through intensity oscillations.

According to L. H. M. Rouppe van der Voort et al. (2003) and V. M. J. Henriques et al. (2015), umbral flashes, originally observed by J. M. Beckers & P. E. Tallant (1969), are brightenings with 3 minutes in chromospheric umbrae caused by magnetoacoustic oscillations propagating upward, eventually transforming into localized shock waves. Propagating slow waves were first detected alongside coronal loops with the Transition Region and Coronal Explorer (TRACE;

B. N. Handy et al. (1999) by R. W. Nightingale et al. (1999) and I. De Moortel et al. (2000) and with the Solar and Heliospheric Observatory (S. Domingo et al. 1995) by D. Berghmans & F. Clette (1999). Recently, A. Rawat & G. R. Gupta (2023) deduced that the 3 minute propagating slow MAWs in coronal loops are instigated by the 3 minute oscillations observed at the footpoints of the fan loops in the photospheric umbrae. The presence of standing slow MAWs is also found in the solar corona, especially in hot coronal loops (e.g., T. Wang et al. 2002, 2021; S. Krishna Prasad & T. Van Doorsselaere 2021). The prevailing consensus is that 3 minute period oscillations are the slow MAWs that travel along magnetic field lines from the photosphere to the corona where they eventually dissipate.

The speeds at which MAWs travel are a combination of Alfvén v_A and sound speeds c_s . For uniform, static, and infinite background plasma, the fast wave propagates in all directions and has a maximum speed, v_f , perpendicular to the magnetic field (J. P. H. Goedbloed & S. Poedts 2004) given as

$$v_f = \sqrt{c_s^2 + v_A^2}. \quad (1)$$

The slow wave, on the other hand, cannot propagate perpendicular to the magnetic field. Along the magnetic field, it propagates at a tube speed of v_t (for a slender flux tube of radius much less than that of the wavelength of disturbance (P. M. Edwin & B. Roberts 1983) given by

$$v_t = \frac{c_s v_A}{\sqrt{c_s^2 + v_A^2}} = \frac{c_s * v_A}{v_f}. \quad (2)$$

The plasma β is related to v_A and c_s as

$$\beta = \frac{2 c_s^2}{\gamma v_A^2}. \quad (3)$$

Here, γ is the polytropic index. For regions where the plasma $\beta < 1$, Equation (3) implies $c_s^2 < v_A^2$. So, Equation (1) becomes $v_f \approx v_A$, i.e., the fast MAWs propagate at the Alfvén speed. Similarly, Equation (2) reduces to $v_t \approx c_s$, indicating that the slow MAWs propagate at roughly the speed of sound along magnetic field lines. In the absence of a magnetic field, all that exists are simple acoustic waves that propagate isotropically at sound speed. In the photospheric umbra, the plasma $\beta \approx 1$ (I. H. Cho et al. 2017), and as one ascends higher into the atmosphere, it begins to decrease ($\beta < 1$). Under coronal conditions, the propagation speed of slow MAWs was measured to be consistent with the projected local sound speed over several coronal loops within active regions (e.g., see the review by I. De Moortel 2009). Therefore, it is safe to assume that, in the umbral atmosphere, slow MAWs predominantly propagate along magnetic field lines with the speed of sound (M. S. Marsh et al. 2002).

Helioseismic Magnetic Imager (HMI; P. H. Scherrer et al. 2012; J. Schou et al. 2012) and the Atmospheric Imaging Assembly (AIA; P. Boerner et al. 2012) data from the Solar Dynamics Observatory (SDO; W. D. Pesnell et al. 2012) provides new avenues for the investigation of oscillations because of their full disk coverage with a high cadence and a high spatial resolution. In this study, we aim to explore the formation height of different SDO/AIA channels within the atmospheres of sunspot umbrae. A. Fossum & M. Carlsson (2005) calculated the formation height of TRACE 1700 and

1600 Å channels using non-LTE radiation hydrodynamic simulations. These authors find the formation heights of respective channels as 360 ± 162 km and 430 ± 92 km. V. E. Reznikova et al. (2012) employed the time lag between different SDO/AIA channels to determine the average wave speed, assuming a certain formation height for each channel. Alternatively, A. S. Deres & S. A. Anfinogentov (2015) applied the cross-correlation technique to determine the average time lags between different SDO/AIA channel pairs and thereby derived the formation height of multiple EUV and UV channels considering the wave propagation speed between the layers as the average local sound speed. Later, A. Deres & S. Anfinogentov (2018) estimated both the height separation and the wave propagation speed between the AIA 1600 and 304 Å channels using the projected separation in wave paths and the corresponding time lags. The authors utilize the magnetic field inclination information obtained from the nonlinear force-free field extrapolations of photospheric vectors magnetograms from SDO/HMI for this purpose. They assume a constant field inclination between the 1600 and 304 Å channels and a fixed formation height of 500 km for the 1600 Å channel in their calculations. Over three different active regions, they obtain a height separation of 500–800 km and an average propagation speed of 30 km s^{-1} between the 1600 and 304 Å channels. Notably, there are certain underlying assumptions in every technique. In the current study, since our objective is to find out the typical formation height of different SDO/AIA channels, we follow an approach similar to A. S. Deres & S. A. Anfinogentov (2015), albeit with some important changes, as will be discussed in the subsequent sections. Furthermore, we analyze 20 active regions here as opposed to isolated cases (or only a few) in the previous studies.

In Section 2, we describe the details of the data employed, in Section 3 we describe the analysis techniques along with the obtained results, and finally, in Section 4 we present our summary and conclusions.

2. Data

We utilize multiwavelength imaging data acquired by the AIA and HMI telescopes onboard the SDO. Using a robust IDL pipeline developed by Rob Rutten,⁵ the desired subfield data encompassing 20 different active regions were extracted from HMI and AIA. This pipeline derotates and coaligns multi-channel images using low-cadence data from a large disk center subfield. In addition, it applies the necessary roll angle and plate scale corrections to the downloaded level 1.0 data using `aia_prep.pro` upgrading them to science-grade level 1.5. The final images are rescaled to ensure that each pixel precisely represents $0''.6$ on disk.

The start times of each data set and the corresponding NOAA active region numbers are listed in Section 3.3. The duration of each data set is 1 hr. The extracted field of view is about $180'' \times 180''$. These data are a subset of the active regions presented in S. Krishna Prasad et al. (2018), where further details are available.

In this work, we analyze data from six wavelength channels, namely, 1700, 1600, 304, 131, and 171 Å from AIA and the continuum channel from HMI. The sunspots within these data sets correspond to different Mount Wilson classes, but no flare

⁵ <https://robrutten.nl/rriidl/sdolib/dircontent.html>

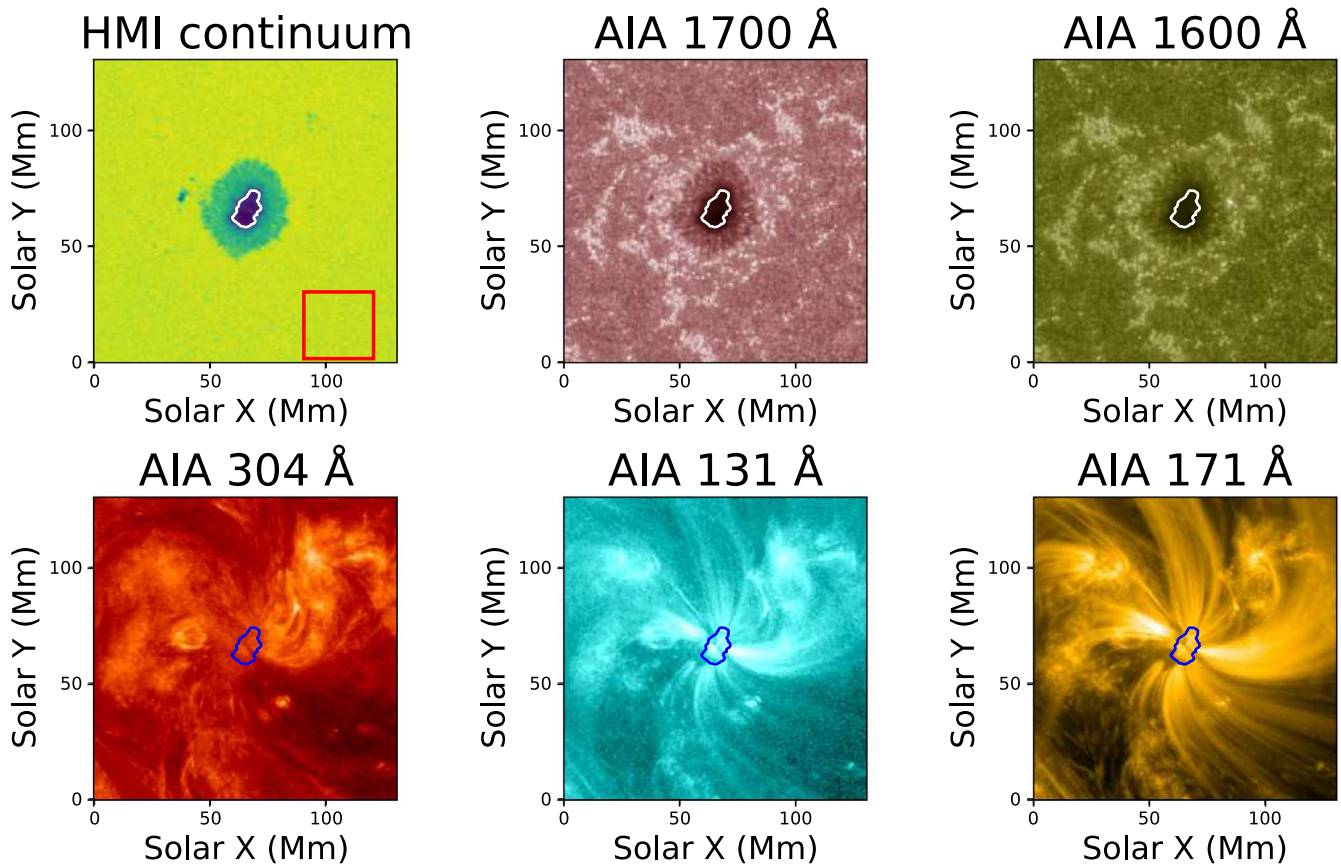


Figure 1. Sample images of a sunspot within AR 12553 captured on 2016 June 16, across various wavelengths of SDO channels as shown. The HMI continuum image represents the average intensity over the 1 hr duration, while the rest of the images depict the intensity within the first frame. The red box on the HMI continuum image denotes the selected region for calculating the median intensity. The white and blue solid curves delineate the identified boundary between the umbra and penumbra (see the text for details).

was associated with them in the considered period, as identified from the solar monitor site.⁶ However, eight of the sunspots exhibit the presence of a light bridge (LB; indicated by an asterisk in the formation height table in Section 3.3), although we exclude the portion of an LB in our analysis.

3. Analysis and Results

The near vertical field in a sunspot umbra means it is easier to track a single structure across multiple heights in the solar atmosphere. Therefore, we restrict our analysis to umbral regions of leading sunspot within each active region in our sample. The determination of the umbral region in each data set is performed on the HMI continuum data following the methodology employed in S. Krishna Prasad et al. (2017). Essentially, this involves calculating a median intensity value over a time-averaged quiet Sun subfield within the HMI continuum data. A fraction of the median value is then used as a threshold to mark the umbra-penumbra boundary. Since LB pixels have higher intensity, selecting a certain percentage value will also eliminate the LB sites. The fraction is manually selected until a suitable match with the visual boundary between the umbra, penumbra, and LB pixels is reached.

Owing to the varied characteristics of different active regions in our data set, we obtain a threshold value of 20%–55% of the median quiet Sun intensity. Figure 1 illustrates the umbra-

penumbra boundary identified over a sample data set corresponding to AR 12553, which was observed on 2016 June 16. Here, a value of 25% of the median intensity is used. The nearby quiet Sun region identified for computing the median value is also shown in the figure by a red square. The umbral area identified in this manner for all the active regions is listed in the formation height table in Section 3.3.

Given that the 3 minute slow MAWs are predominant in the umbral atmosphere and also generally exhibit a propagating nature, the time series at each umbral pixel within each channel is then Fourier filtered to retain oscillations within a narrow period band of 2–4 minutes. The filtration is accomplished using a third-order Butterworth filter (K. Kraus 1977) due to its flat response in the selected passband. Figure 2 displays a time series along with the corresponding Fourier power spectrum before and after applying this filter. This time series is built from the spatially averaged AIA 131 Å intensity within the umbral region of AR 12553 shown in Figure 1 where a dominant 3 minute signal can be observed.

The filtered data within different channels are then cross-correlated in pairs to obtain a peak cross-correlation coefficient and the corresponding time lag. For this purpose, we select eight channel pairs, namely, [continuum, 1700], [continuum, 1600], [1700, 1600], [1700, 304], [1600, 304], [304, 171], [304, 131], and [171, 131]. We do not consider all possible combinations here as in A. S. Deres & S. A. Anfinogentov (2015), as we reckon that extreme combinations such as [continuum, 171] are prone to large uncertainties.

⁶ <https://solarmonitor.org/>

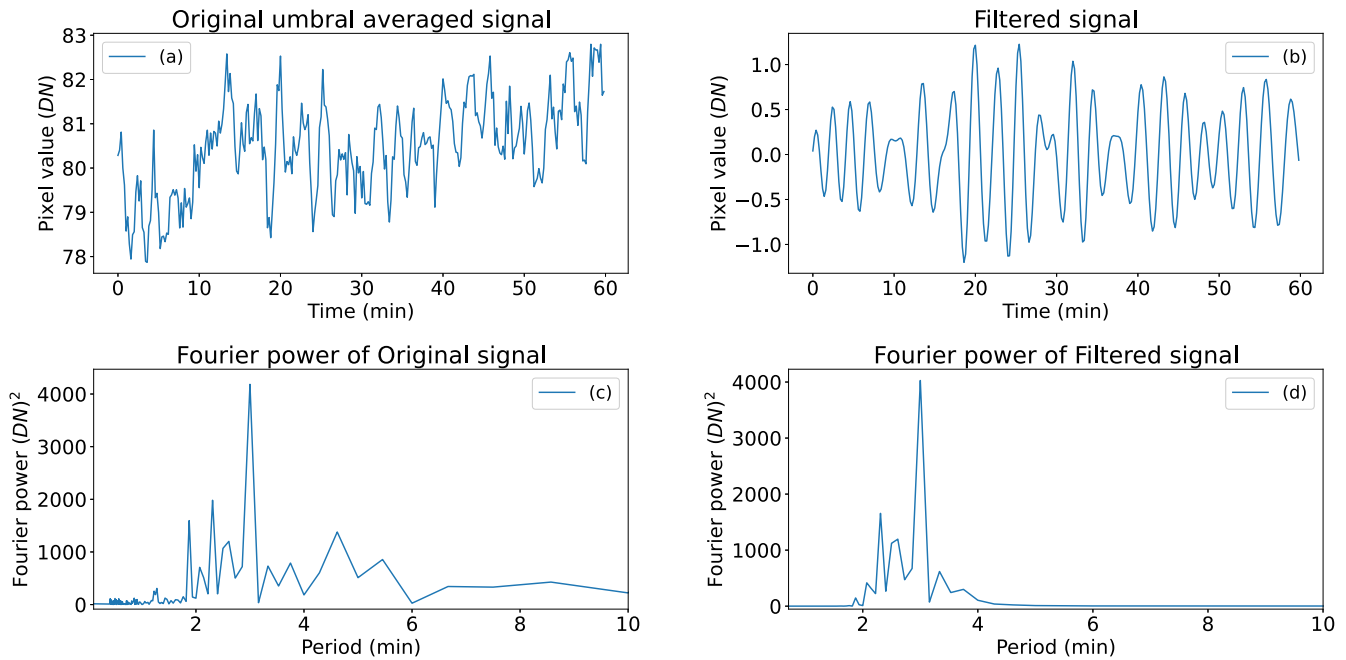


Figure 2. (a) Spatially averaged AIA 131 Å intensity from the umbral region of AR 12553 is shown in Figure 1. (b) The signal in (a) after passing through a bandpass Butterworth filter retaining oscillations in a 2–4 minute range. (c) and (d) represent the Fourier power spectra of the original and filtered signals displayed in (a) and (b), respectively.

Before cross-correlation, the data were linearly interpolated wherever necessary. For instance, when cross-correlating the HMI continuum data with AIA 1700 Å, we interpolated the HMI continuum data to match the cadence of AIA 1700 Å. But, in cases where the cross-correlation is performed between two channels with the same cadence (e.g., EUV channels), no interpolation was done. In each of the channel pairs, the first channel is considered as the reference channel, and the second as the test channel. Considering the dominant vertical field in the umbra leading to a near vertical propagation of slow MAWS, in an ideal scenario, the filtered signal in each pixel in the reference channel can be cross-correlated with the signal from the corresponding pixel in the test channel to estimate the respective wave propagation times. However, it is quite possible that the direction of wave propagation is not aligned precisely with the line of sight, either because the location of the active region is further away from the disk center or because the magnetic field in the umbra inherently possesses some inclination. Both effects could also be in play at the same time. From the location information provided in Section 3.3, clearly not all active regions are near the disk center. So, this effect is likely not ignorable.

To alleviate this problem, the signal at each pixel in the reference channel is cross-correlated with the signal from all the pixels within an 11×11 pixel² box centered over the corresponding pixel (i.e., ± 5 pixels in both dimensions) in the test channel. The corresponding time lag values are then obtained from the pixel location that shows the maximum cross-correlation. For a precise estimation of the time lag, the respective cross-correlation curves are fitted with a parabola near the maximum.

Figure 3 displays the final cross-correlation coefficient, time lag, and absolute pixel shift maps obtained for AR 12553 considering a [304, 131] channel pair. Pixel locations that do not show good correlation (correlation coefficient ≥ 0.6) are excluded from our results as a standard. These observations

reveal that the time lag values are not uniform across the umbral region. This spatial nonuniformity can originate from a combination of factors, including the complexity of the magnetic field structure and local changes in thermal properties. More particularly, the larger time lag values near the core of the umbra, where a near vertical field is expected, suggest that it is not simply an effect of field inclination. On the other hand, the dominant blue color in the pixel shift map, corresponding to a shift of 1 pixel or less, confirms that the field is nearly vertical for most of the region. Note that these values represent the absolute magnitude of the shift. Therefore, there are some locations with fractional values exceeding a 1 pixel shift but shown with the same color for simplicity. Nevertheless, the fact that a majority of the pixel locations show a much smaller shift than 5 pixels, with a strong correlation, supports our choice of the box. These results are consistent with A. Deres & S. Anfinogentov (2018) and A. Rawat & G. R. Gupta (2023), who found a maximum shift of 2–3 pixels between various AIA channels.

In order to further verify if the ± 5 pixel box is a suitable choice, we perform linear force-free field extrapolations on two of our active regions using the corresponding HMI-SHARP data (M. G. Bobra et al. 2014). The specific technique we use employs a fast Fourier transform similar to that pioneered by C. E. Alissandrakis (1981). The force-free parameter (α) is taken from the SHARP data header. Among the two active regions selected, the first is AR 12186, which is quite far from the disk center with position coordinates [166'', -436''], and the second is AR 12553, which is relatively near the disk center with position coordinates [11'', -129'']. The obtained field extrapolations for AR 12186 are illustrated in Figure 4. Most of the field lines within the umbra are vertical, as expected. To put this quantitatively, we follow each field line within the umbra and estimate the expected horizontal shift in pixels to be on the same field line up to a height of 2.2 Mm. Note that this specific value simply comes from the fact that our height resolution in

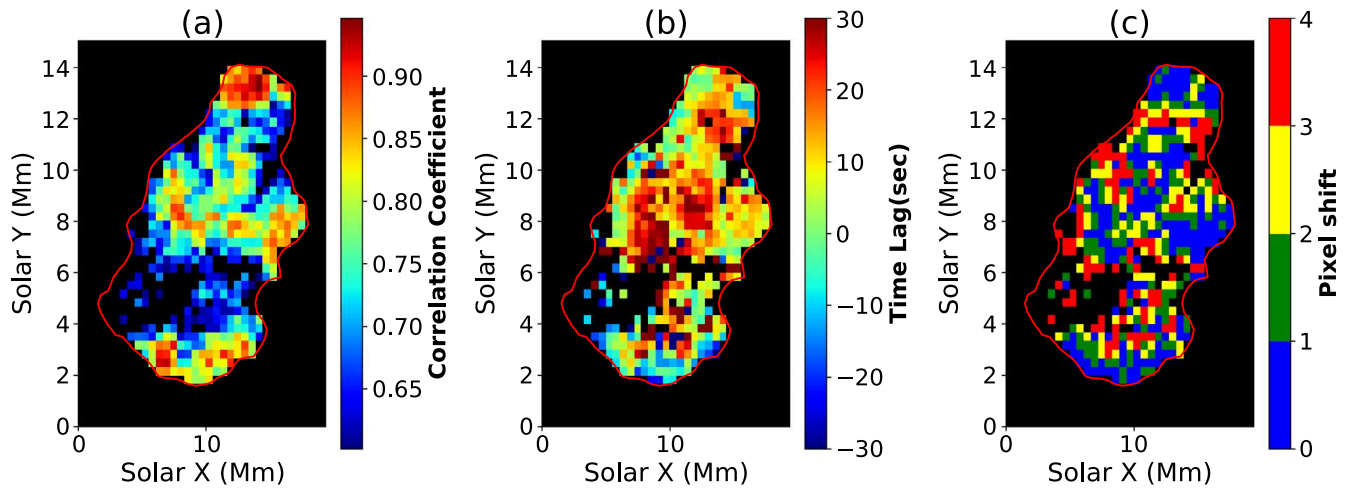


Figure 3. The correlation coefficient (a), time lag (b), and absolute pixel shift (c) maps obtained for AR 12553, considering the AIA 304 Å and AIA 131 Å channel pair. Pixel locations with a correlation coefficient below 0.6 are ignored from the time lag and pixel shift calculations. The red curve delineates the boundary between the umbra and penumbra.

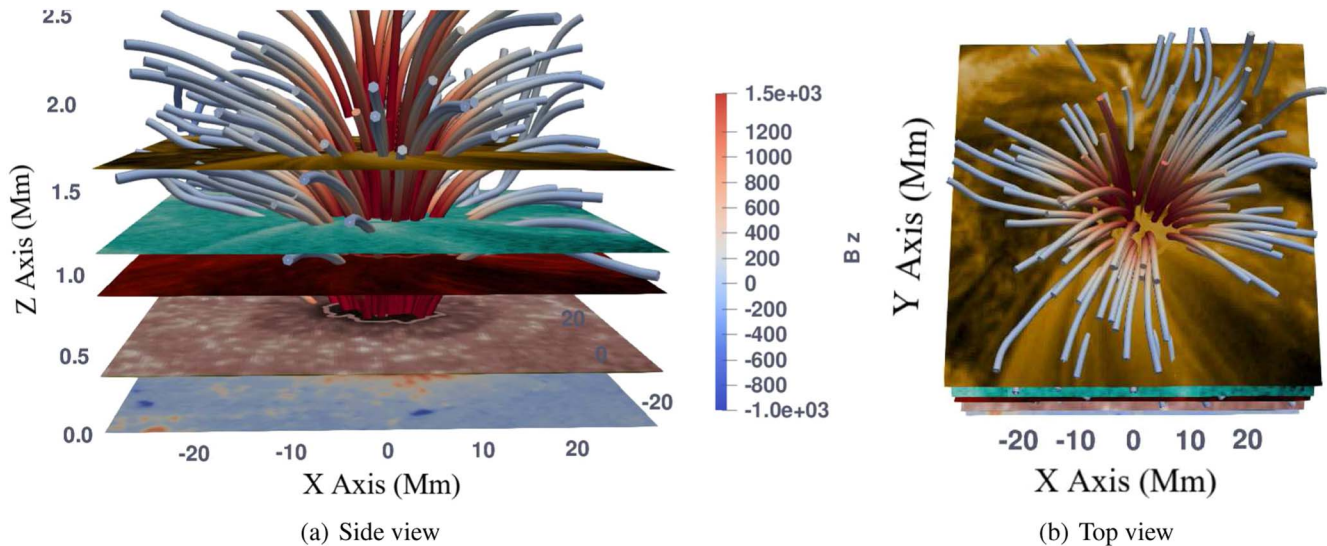


Figure 4. Linear force-free field extrapolations for AR 12186 observed on 2014 October 14. Our focus was on a restricted area around the sunspot to observe the magnetic field lines nearby. All AIA images are stacked according to their formation height obtained from our analysis (see Section 3.1 for details). Note that AIA 1600 Å and AIA 1700 Å images form very close to each other as compared to other channels so it is difficult to see them distinctly here. (a) and (b) represent the side view and top view of the extrapolated field lines, respectively.

the z-direction is about 0.36 Mm. We find that the maximum shift for AR 12186 is about 5.2 pixels, and the same for AR 12553 is about 4.2 pixels. It may be noted that the locations with large shifts are mostly concentrated near the periphery of the umbra. Besides, as we will find later, the height separation between any of the channel pairs investigated here is much less than 2.2 Mm, so it is likely that the expected shifts are well below 5 pixels at all locations.

Another effect that may prevent the wave propagation direction from being radial is the inclination of the local normal with respect to our line of sight. This is only an apparent effect and is caused primarily due to the projection of the 3D surface to a 2D plane, normal to our line-of-sight direction. However, because we know the exact 3D coordinates at each pixel location, we can easily calculate the expected shifts as a function of height using simple trigonometric transformations. A pixel shift map, thus obtained for AR 12186, is shown in Figure 5 for three different heights as labeled. The values

within the umbral region are only shown in this figure. The obtained shifts in the southwest region of the umbra are noticeably pronounced. This is because of the position of this active region in the southwest quadrant (see Section 3.3). Regarding the absolute magnitude, at a height of 2 Mm, we obtain a shift of ≈ 2 pixels. This value is on the higher side because AR 12186 is one of the furthest from the disk center in our sample. For instance, at the same 2 Mm height, the corresponding shift obtained for AR 12553 is about 0.7 pixel. Furthermore, if one considers a height separation of 1000 km or less between the selected channel pairs, the expected shifts, even for AR 12186, are going to be of the order of only 1 pixel. In addition, depending on the local orientation of the magnetic field, this shift shall be either added or subtracted. Therefore, the contribution of this effect to the overall shifts can be ignored here.

In summary, our selection of the ± 5 pixel box in the test channel appears quite reasonable to properly find and trace the

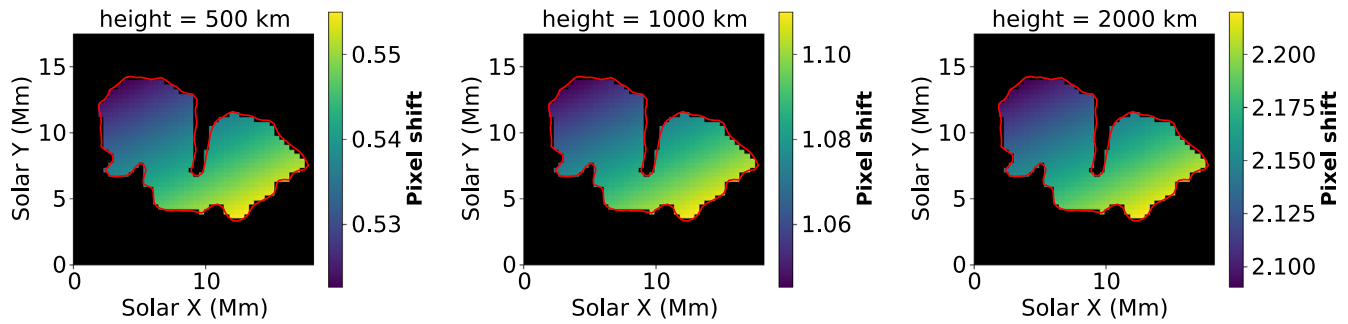


Figure 5. Expected pixel shifts for AR 12186 due to its projection along the line of sight. Different panels show the shifts at different heights as labeled. The red curve represents the boundary between the umbra and the penumbra. The values within the umbra are only displayed.

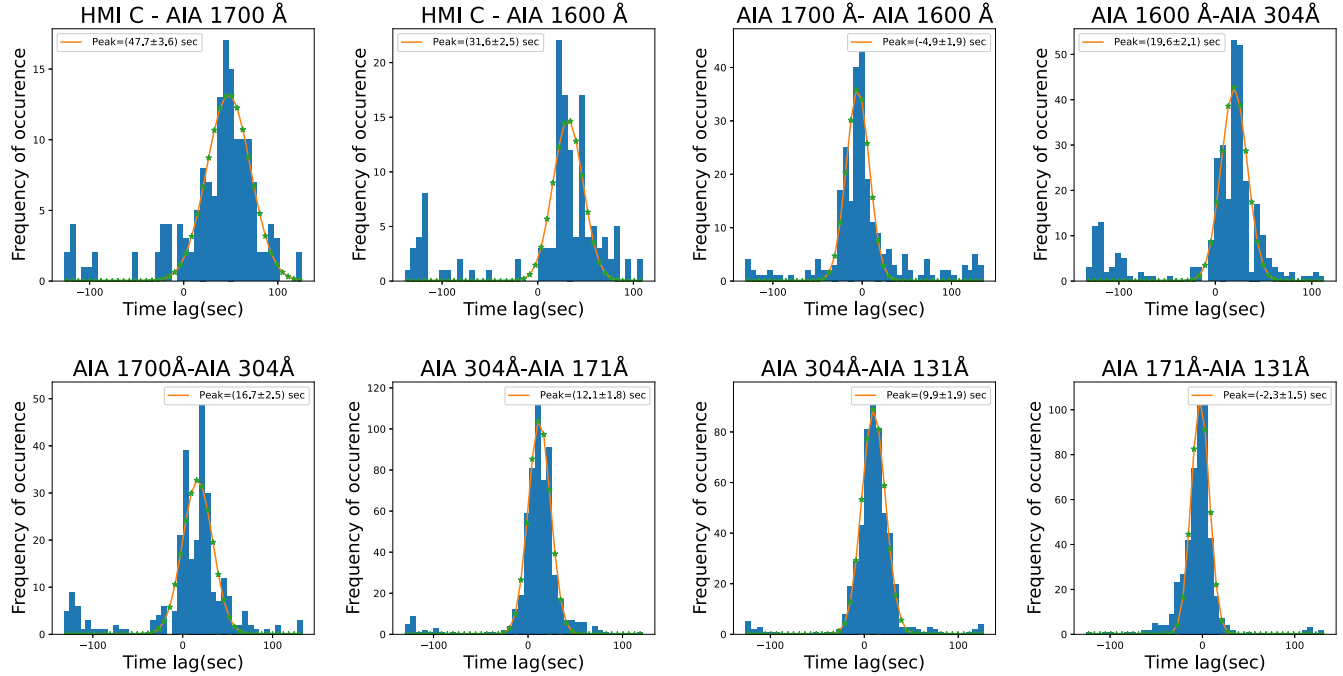


Figure 6. Histograms of time lag values obtained for all eight channel pairs corresponding to AR 12553 data. A bin size of 6 s is used in these plots. The orange curves represent a Gaussian fit to the histogram data. The corresponding peak values and the respective uncertainties obtained from the fit are listed in the plots.

wave propagation direction. Note that we use the same size box for all the test channels, irrespective of their height. Although the field lines are likely more inclined at greater heights, as we demonstrated above a ± 5 pixel box is acceptable for a large height range.

3.1. Estimating the Most Probable Time Lag

The peak correlation coefficient and the corresponding time lag are measured for all pixels within the umbral region between all eight channel pair combinations selected, as illustrated in Figure 3. This exercise is applied to all 20 active regions. The obtained time lag values are not uniform across the umbra, as can be seen from Figure 3. It is possible that this is due to an inherent change in the morphological structure across the umbra, but there is also a likely chance that part of the pixel-to-pixel variation is due to the statistical noise. In either case, we would like to identify a representative time lag value between the layers. This is typically done by taking a simple average across the region (A. S. Deres & S. A. Anfinogentov 2015), but rather, we opted for the most frequent value here (see, e.g., A. Deres & S. Anfinogentov 2018).

To achieve this, we first build histograms of all the time lag values obtained for each channel pair and then fitted these data with a Gaussian curve considering the bin center points. The bin size is considered as 6 s. The peak of the fitted Gaussian is taken as the representative time lag for a particular channel pair. The standard deviation of the Gaussian fit normalized with the square root of the number of bins gives the corresponding uncertainty in the time lag value.

For illustration, the histograms obtained from all eight channel pairs for AR 12553 are shown in Figure 6. The Gaussian fits to the data are shown by orange curves, and the respective peak time lag values obtained are listed in the plot.

3.2. Sound Speed Estimation

Now that the time lag values are estimated, one could calculate a relative formation height of the test channel with respect to the reference channel, if the propagation speed of the waves is known. Considering the prevailing interpretation of the 3 minute intensity oscillations we observe here as slow MAWs and under the assumption of low plasma- β conditions in the umbral atmosphere, the propagation speed can be approximated to the local sound speed. The expression for the

sound speed, c_s , is given as

$$c_s = \sqrt{\frac{\gamma k_B T}{\mu m_H}}. \quad (4)$$

Here, γ ($=5/3$) is the polytropic index, k_B is the Boltzmann's constant, T is the temperature, and μm_H is the mean mass per particle. The μ value varies with the degree of ionization but a reasonable choice can be 0.61 for corona and 1.25 for the photosphere (J. T. Mariska 1992). The characteristic temperature for the optically thin EUV channels (AIA 304, 131, and 171 Å) can be obtained from the peak of the temperature response functions. In case of multiple peaks in the response curves, one can choose the peak appropriate for nonflaring plasma conditions. However, this estimation is not as straightforward for the UV channels (AIA 1600 and 1700) because of the optically thick emission. According to P. J. A. Simões et al. (2019), the active region plage emission in AIA 1700 and 1600 Å is mainly sourced from the continuum created close to the temperature minimum during non-flare times. Indeed, the authors show that the continuum contribution to the overall emission in the 1600 and 1700 Å channels is about 67% and 87%, respectively, during quiet periods. So, the temperature distinction between them could be marginal.

On the other hand, during flare periods, AIA 1600 exhibits a dominant contribution from C IV, and AIA 1700 shows a dominant contribution from C I, which highlights a perceptible difference in their formation. Therefore, considering the nonflaring conditions in our data, the characteristic temperatures of the AIA 1600 and 1700 Å channels can be assumed as ≈ 5011 K (J. R. Lemen et al. 2012; S. Toriumi et al. 2020). It may be noted that this is different from the usual consideration of 10^5 K as the characteristic temperature for the AIA 1600 Å channel (e.g., A. S. Deres & S. A. Anfinogentov 2015), but we do not believe such a high value would be applicable here. For the HMI continuum, to determine the characteristic temperature, we assume the emission coming from this layer is a blackbody radiation. The temperature within the umbra can then be obtained from the intensity ratio, e.g., between the umbra and the quiet Sun simply by using a Planck's function as described earlier by S. K. Solanki et al. (1993) and I. H. Cho et al. (2017). The intensity ratio between the umbra and the quiet Sun (I/I_{QS}), can be expressed using Planck's law as

$$\frac{I}{I_{QS}} = \frac{e^{hc/\lambda k_B T_{QS}} - 1}{e^{hc/\lambda k_B T} - 1}, \quad (5)$$

where h is Planck's constant, c is the speed of light, λ is the wavelength of HMI continuum (6173 Å), T_{QS} is the temperature of quiet Sun (6000 K), k_B is the Boltzmann's constant, and T is the temperature of the umbra. Based on the observed umbral intensity at each pixel, an average umbral temperature is obtained. Because the umbral intensity varies from one active region to the other, we obtain different temperatures for different active regions with the overall values ranging from approximately 4176–4764 K. With these considerations in mind, we estimate characteristic sound speeds for all the six wavelength channels as listed in Table 1.

Table 1

The Primary Ion, Characteristic Temperature, and the Sound Speed for All Six Channels Used in This Study Considering Nonflaring Conditions (J. R. Lemen et al. 2012; S. Toriumi et al. 2020)

Channel	Primary Ion	Characteristic Temperature (K)	Sound Speed (km s ⁻¹)
HMI continuum	Continuum	4176–4764	6.8–7.2
AIA 1700	Continuum	5011	7.4
AIA 1600	Continuum	5011	7.4
AIA 304	He II	50118	33.6
AIA 131	Fe VIII	0.45 M	100.6
AIA 171	Fe IX	0.79 M	133.3

Note. The temperature of the HMI continuum is estimated from the umbral brightness using Planck's function (see the text for details). The obtained range across all active regions is listed here.

3.3. Formation Height Calculation

Let us now compute the formation height separation between the two channels by utilizing the average sound speed between each channel pair and the respective time lag. The obtained height separation values for all channel pairs from AR 12553 are listed in Table 2 along with other relevant parameters. The number of “good pixels” in this table corresponds to the number of pixel locations with a correlation coefficient ≥ 0.6 . The average correlation coefficient across all the good pixels is also listed in the table. Note that we did not take into account the horizontal pixel shifts in converting the time lags to height differences. Although this value is of the order of 1 pixel or less for a majority of the locations (see Figure 3), it is largely limited by the pixel scale and therefore, prone to accumulate large uncertainties.

So far, we have found a height separation between each channel pair, but as can be seen from the table, we still cannot assign a particular height to each channel with respect to the photosphere (HMI continuum). This is because the value will change depending on the channel pair chosen. Mathematically speaking, we have more equations than the variables, and therefore, it is an overdetermined problem with no particular solution. In such cases, one can obtain a pseudo-solution, or in other words, a solution that is not exact but matches *closely* with all the equations in the least squares sense. This can be achieved by using a singular value decomposition (SVD) method, for example, as followed in A. S. Deres & S. A. Anfinogentov (2015).

Essentially, the procedure involves building a set of linear equations from the height separations and solving them using the least square fitting by the SVD method. The set of equations for AR 12553 considering the HMI continuum height (H_c) as reference are listed below

$$\begin{aligned} H_c &= 0 \\ H_{1600} - H_c &= \mathbf{225} \\ H_{1700} - H_c &= \mathbf{339} \\ H_{1600} - H_{1700} &= -36 \\ H_{304} - H_{1700} &= 342 \\ H_{304} - H_{1600} &= 401 \\ H_{131} - H_{304} &= 662 \\ H_{171} - H_{304} &= 1005 \\ H_{131} - H_{171} &= -264. \end{aligned} \quad (6)$$

Table 2
The Time Lag, Average Sound Speed, and the Computed Separation in Formation Height between Each Channel Pair for AR 12553

Channel Combination	Time Lag (s)	Average Correlation Coefficient	Average Sound Speed (km s ⁻¹)	Separation Height (km)	Good Pixels (No.)
HMI C-1600	31.6 ± 2.5	0.65	7.2	225 ± 18	132
HMI C-AIA 1700	47.7 ± 3.6	0.65	7.2	339 ± 25	152
AIA 1700-1600	-4.9 ± 1.9	0.66	7.4	-36 ± 14	254
AIA 1700-304	16.7 ± 2.5	0.67	20.5	342 ± 52	280
AIA 1600-304	19.6 ± 2.1	0.67	20.5	401 ± 43	314
AIA 304-131	9.9 ± 1.9	0.75	67.1	662 ± 130	507
AIA 304-171	12.1 ± 1.8	0.78	83.4	1005 ± 152	565
AIA 171-131	-2.3 ± 1.5	0.78	116.9	-264 ± 174	488

Note. The values under “good pixels” denote the number of pixel locations with a cross-correlation coefficient of at least 0.6. The total umbral pixels identified for this active region are 637, which is considered the same at all heights. The mean correlation coefficient over the good pixels is also listed.

This set can be represented as $AX = B$, where A contains the coefficient matrix of each channel’s height, B contains the observed height separations (in kilometers), X is what we solve for, which gives the final height (in kilometers) of each channel relative to the HMI continuum. In principle, the solution can be simply obtained from $X = A^{-1} \cdot B$.

However, as discussed earlier, the number of independent variables is fewer than the equations, resulting in mismatched dimensions between A and B . Hence, using the SVD matrix method (T. Strutz 2010), we decompose A into $U \cdot S \cdot V^T$, where U is the matrix of the orthonormal eigenvectors of $A \cdot A^T$, V^T is the transpose of the matrix containing the orthonormal eigenvectors of $A^T \cdot A$, and S is the diagonal matrix with elements equal to the root of eigenvalues of $A \cdot A^T$ or $A^T \cdot A$. Thus, the solution for X can be written as $X = V \cdot S^{-1} \cdot U^T \cdot B$.

Furthermore, in order to incorporate the uncertainties we obtained on the height separations, instead of solving $AX = B$, we solve $A'X = B'$, where $A' = w \cdot A$ and $B' = w \cdot B$ with w as the matrix that contains the reciprocals of the respective errors.

Finally, the solution in X will have an uncertainty given by the covariance matrix, C , expressed as $C = V \cdot S^{-2} \cdot V^T$. The formation heights thus obtained for AR 12553 are 247 ± 15 km, 297 ± 17 km, 644 ± 36 km, 1325 ± 119 km, and 1623 ± 130 km, respectively, for the AIA 1600, 1700, 304, 131, and 171 Å channels with respect to the HMI continuum. Similarly, the formation heights obtained for all 20 active regions are listed in Table 3. Additionally, Figure 7 shows a graphical representation of these data.

4. Discussion and Conclusions

Utilizing the time lags between propagating 3 minute oscillations within the sunspot umbrae, we estimated the formation heights of five AIA channels, 1600, 1700, 304, 131, and 171 Å, with respect to the HMI continuum over 20 different active regions (see Figure 7 and Table 3). The median values of the obtained formation heights for these channels are 356_{247}^{453} , 368_{260}^{468} , 858_{575}^{1155} , 1180_{709}^{1937} , and 1470_{909}^{2585} km, respectively. The subscript and superscript values here indicate the overall range in heights obtained across all the active regions studied. According to A. A. Norton et al. (2006), the continuum near FeI 6173 Å forms at an altitude of 21 km in the umbral atmosphere. If one takes this into account, all our formation heights shall be shifted accordingly.

Among the UV channels, it is observed that in about 17 cases, the 1700 Å channel forms above 1600 Å, while it is the

other way around in the rest. The 304 Å channel forms above both the UV channels, followed by the 131 Å channel, in all cases. The 171 Å channel forms higher than the 131 Å in all cases except two (AR 11665 and AR 12090). However, the height separation between the channels in those two cases is marginal. For AR 11665 and AR 12236, the formation heights of all three EUV channels are very close to each other. Also, as can be seen from Figure 7, the variation in formation heights of coronal channels (131 and 171 Å) is substantial in comparison with that from the lower atmospheric channels.

Some of our active regions contain sunspots with LBs, as noted before. K. D. Leka (1997) reported that LBs can cause magnetic field disruptions. When compared to the surrounding umbra, they found that LBs had more horizontal fields. More recently, S. Feng et al. (2020) suggested that magnetoconvection could cause LBs and penumbrae to be split at the photosphere, suggesting that both could share the same magnetic source. According to R. Rezaei (2018), LBs encompass multithermal structures extending up to the transition region (TR). Moreover, the chromospheric temperature, as well as AIA 171, 211 Å intensity, are shown to be enhanced in the LBs (R. E. Louis et al. 2023).

In light of these results, we propose that the magnetic structure within the LBs is significantly different from that in the umbra. Therefore, we strictly excluded the pixel locations of LBs from our analysis. Perhaps as a consequence of this selection, we do not observe any peculiar behavior in the formation heights of AIA channels, even in the case of active regions with LBs.

In Table 3, we also list the umbral area and the average absolute magnetic field strength of the sunspots within individual active regions. The data of the umbral area are a bit discontinuous, with a large gap between ≈ 150 and 280 (Mm)², but within this sample, we did not find any systematic dependence of formation height on the umbral area. The magnetic field strength, too, did not appear to show any influence on the formation height, but perhaps our sample is not large enough to show a consistent behavior.

In general, our formation height values agree well with the results reported in the literature. Employing 1D radiation hydrodynamic simulations, A. Fossum & M. Carlsson (2005) obtained a formation height of 360 ± 162 and 430 ± 92 km for the TRACE 1700 and 1600 Å channels, respectively. Using RATAN-600 multiwavelength radio observations, T. I. Kaltman et al. (2012) find the altitudes of the base of the TR (10,000 K plasma) and the corona (2.5 MK plasma) as 500 and 2000 km, respectively. A. S. Deres & S. A. Anfinogentov

Table 3
The Computed Formation Heights of UV and EUV Channels with Respect to the HMI Continuum for All 20 Active Regions

Start Time (UT)	Location (")	NOAA Number	Umbral Area (Mm) ²	Avg. Abs. Mag. Field (G)	AIA 1600 (km)	AIA 1700 (km)	AIA 304 (km)	AIA 131 (km)	AIA 171 (km)
2012 Aug 5 12:00	(172, 221)	11535	48	1534	389 ± 20	433 ± 19	885 ± 21	1390 ± 127	1441 ± 146
2012 Sep 23 12:00	(−215, 15)	11575*	94	1294	325 ± 17	336 ± 17	859 ± 26	1250 ± 123	1800 ± 201
2012 Oct 12 13:00	(−83, −303)	11586	41	1379	383 ± 16	417 ± 16	1155 ± 48	1160 ± 177	1308 ± 192
2012 Oct 19 12:00	(240, 30)	11591	100	1525	340 ± 19	357 ± 19	824 ± 22	953 ± 160	1287 ± 176
2012 Dec 4 12:00	(230, 116)	11623*	78	1474	390 ± 24	396 ± 23	876 ± 27	989 ± 122	1179 ± 143
2013 Feb 5 12:00	(355, 289)	11665	78	1447	453 ± 16	468 ± 15	928 ± 23	1030 ± 191	909 ± 224
2013 Sep 3 12:00	(276, 70)	11836*	50	1400	353 ± 23	371 ± 22	831 ± 24	1746 ± 129	2431 ± 179
2013 Nov 14 13:00	(−278, −316)	11895	56	1339	333 ± 16	338 ± 16	837 ± 20	1614 ± 145	2164 ± 221
2013 Dec 28 13:30	(576, −215)	11934	53	1282	298 ± 16	272 ± 16	769 ± 19	1317 ± 157	1587 ± 170
2014 Mar 18 12:00	(13, 317)	12005	100	1529	417 ± 23	425 ± 23	912 ± 26	1937 ± 115	2585 ± 154
2014 Apr 13 12:00	(−68, 280)	12032	88	1497	355 ± 19	422 ± 19	910 ± 30	1143 ± 183	1765 ± 208
2014 May 3 12:00	(48, −80)	12049*	93	1571	378 ± 22	419 ± 22	816 ± 39	912 ± 152	1224 ± 174
2014 Jun 16 03:50	(−196, 380)	12090	62	1374	399 ± 21	319 ± 19	890 ± 26	1621 ± 162	1500 ± 153
2014 July 7 12:00	(−209, −193)	12109*	289	1572	291 ± 22	324 ± 23	575 ± 40	709 ± 145	1245 ± 162
2014 July 28 12:00	(87, 40)	12121*	57	1457	358 ± 15	365 ± 16	814 ± 21	1492 ± 152	2147 ± 204
2014 Aug 11 12:00	(33, 132)	12135	86	1441	422 ± 25	448 ± 22	894 ± 29	1199 ± 144	1440 ± 153
2014 Oct 14 12:00	(166, −436)	12186	93	1282	357 ± 24	360 ± 24	858 ± 28	1114 ± 143	1617 ± 181
2014 Dec 17 12:00	(−35, 492)	12236*	38	1285	355 ± 14	387 ± 13	885 ± 16	916 ± 185	1052 ± 204
2015 Jan 29 10:30	(347, 330)	12268*	139	1535	280 ± 21	260 ± 21	781 ± 26	798 ± 149	1153 ± 153
2016 Jun 16 11:00	(11, −129)	12553	123	1774	247 ± 15	297 ± 17	644 ± 36	1325 ± 119	1623 ± 130

Note. The start times of the data sets, the respective NOAA active region numbers, the umbral area, and the umbral average magnetic field are also listed. The asterisk next to the active region numbers denotes the cases where an LB is present.

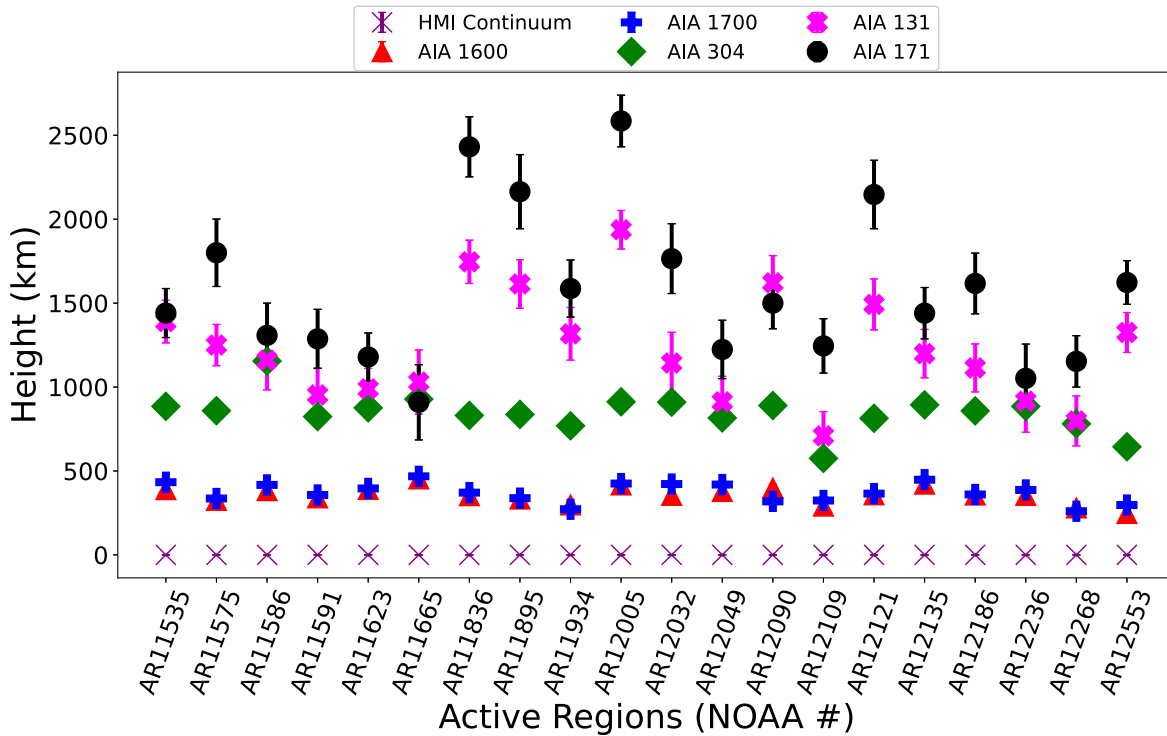


Figure 7. Formation heights of different SDO/AIA channels with respect to the HMI continuum. The vertical bars denote the corresponding uncertainties. Different colors/symbols represent the data for different channels as listed. The uncertainties for AIA 1600, 1700, and 304 Å cases are smaller than the symbol size and, therefore, not clearly visible in the plot. Notably, AIA 1700 Å can be seen to form above AIA 1600 Å in a majority of cases. The AIA 131 Å channel appears to form consistently between the AIA 304 Å and AIA 171 Å channels except in two cases.

(2015), A. Deres & S. Anfinogentov (2018) observe that the separation between AIA 1600 and 304 Å channels lies in the range of 500–800 km. More recently, A. J. de Oliveira e Silva et al. (2022) showed that the TR above a solar umbra with a temperature of $\approx 131,440$ K (analogous to our 304 Å channel) is situated at 1080 ± 20 km. Our results for the respective channels fall in the same range of heights.

However, if one looks at the order of formation, most previous studies consider the 1600 Å channel to be forming above the 1700 Å channel in agreement with the results of A. Fossum & M. Carlsson (2005). But, as we find here, this is not the case for 17 out of 20 active regions. As discussed in Section 3.2, this discrepancy is mainly due to the assumption that 1600 Å channel has a dominant contribution from C IV, which is only true during flare periods (P. J. A. Simões et al. 2019). Under quiet atmospheric conditions that are applicable here, the continuum contribution is rather dominant, resulting in marginal differences in height with respect to the 1700 Å channel, as is the case found here. One could also argue that the negative time lags found between the [1700, 1600] channel pair (see Table 2) actually implies a downward propagation of the wave.

Indeed, numerous studies in the literature suggest both upward and downward propagating waves, especially in the lower solar atmosphere (see the reviews by E. Khomenko & M. Collados 2015; D. B. Jess et al. 2023). While this is certainly a possibility if we only consider the [1700, 1600] channel pair, the results from [continuum, 1600] and [continuum, 1700], when considered in combination, would not be compatible with this scenario. Therefore, we are confident that our results indicate a dominant upward propagation of slow MAWs. Nevertheless, if one is interested

in oscillations at individual pixels, we agree that there may be cases representing both upward and downward propagating waves (see Figure 6).

Lastly, we would like to note some of the important caveats of these results: (i) The formation heights estimated here are limited to the umbral atmosphere under quiet conditions. These values may differ for other atmospheric structures, including the surrounding penumbra; (ii) Also, the presence of any sort of activity in the region can impact the results; (iii) Furthermore, we consider a single formation height for the entire umbra, albeit in a particular wavelength channel. Given the dynamic and complex nature of the solar environment, this assumption may not be always valid; (iv) In addition, the propagation speed of slow MAWs is assumed to be the local sound speed in each layer which in turn is dependent on the characteristic temperature of the respective wavelength channel. While this is valid for low plasma- β conditions, which are typical for an umbra, any deviations, especially in the periphery of the umbra, can affect the overall results.

We hope that future follow-up studies are inspired here that will improve upon our results by addressing these issues.

Acknowledgments

The data used here are courtesy of NASA/SDO and the HMI and AIA science teams. S.K.P. is grateful to SERB for a startup research grant (No. SRG/2023/002623). M.B.K. acknowledges support by UNKP-22-4-II-ELTE-186, ELTE Hungary and is grateful for the Leverhulme Trust Found ECF-2023-271. R.E. is grateful to STFC (UK, grant No. ST/M000826/1) and PIFI (China, grant No. 2024PVA0043). R.E. and M.B.K. are also thankful for the support received from NKFIH OTKA

(Hungary, grant No. K142987). This work was also supported by the NKFIH Excellence grant TKP2021-NKTA-64.

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