



This is a repository copy of *Probing Purcell enhancement and photon collection efficiency of InAs quantum dots at nodes of the cavity electric field.*

White Rose Research Online URL for this paper:

<https://eprints.whiterose.ac.uk/213382/>

Version: Published Version

Article:

Jordan, M. orcid.org/0009-0000-3521-8884, Androvitsaneas, P., Clark, R.N. orcid.org/0000-0002-6623-1499 et al. (4 more authors) (2024) Probing Purcell enhancement and photon collection efficiency of InAs quantum dots at nodes of the cavity electric field. *Physical Review Research*, 6 (2). L022004. ISSN 2643-1564

<https://doi.org/10.1103/physrevresearch.6.l022004>

Reuse

This article is distributed under the terms of the Creative Commons Attribution (CC BY) licence. This licence allows you to distribute, remix, tweak, and build upon the work, even commercially, as long as you credit the authors for the original work. More information and the full terms of the licence here:

<https://creativecommons.org/licenses/>

Takedown

If you consider content in White Rose Research Online to be in breach of UK law, please notify us by emailing eprints@whiterose.ac.uk including the URL of the record and the reason for the withdrawal request.



eprints@whiterose.ac.uk
<https://eprints.whiterose.ac.uk/>

Probing Purcell enhancement and photon collection efficiency of InAs quantum dots at nodes of the cavity electric field

Matthew Jordan ^{1,2}, Petros Androvitsaneas,^{1,2} Rachel N. Clark ^{1,2}, Aristotelis Trapalis ³, Ian Farrer ^{3,4},
Wolfgang Langbein ⁵ and Anthony J. Bennett ^{1,2,5,*}

¹*School of Engineering, Cardiff University, Queen's Buildings, The Parade, Cardiff CF24 3AA, United Kingdom*

²*Translational Research Hub, Maindy Road, Cardiff CF24 4HQ, United Kingdom*

³*Department of Electronic and Electrical Engineering, University of Sheffield, Mappin Steet, Sheffield S1 3JD, United Kingdom*

⁴*EPSRC National Epitaxy Facility, University of Sheffield, Broad Lane, Sheffield S3 7HQ, United Kingdom*

⁵*School of Physics and Astronomy, Cardiff University, Queen's Buildings, The Parade, Cardiff CF24 3AA, United Kingdom*



(Received 12 October 2023; revised 22 December 2023; accepted 16 January 2024; published 4 April 2024)

The interaction of excitonic transitions with confined photonic modes enables tests of quantum physics and design of efficient optoelectronic devices. Here we study how key metrics such as Purcell factor, β factor, and collection efficiency are determined by the non-cavity modes that exist in real devices, taking the well-studied micropillar cavity as an example. Samples with dots at different positions in the cavity field allow us to quantify the effect of the non-cavity modes and show that the zero-phonon line and the phonon-assisted emission into the cavity mode HE_{11} is suppressed by positioning dots at the field node.

DOI: [10.1103/PhysRevResearch.6.L022004](https://doi.org/10.1103/PhysRevResearch.6.L022004)

Introduction. Single-photon sources are crucial to applications in quantum metrology [1], secure quantum communications [2], and optical quantum computing [3,4]. In solid state devices the local photonic environment can be structured to promote the efficient collection of photons into a lens. This can be achieved by suppressing emission into unwanted directions, such as in a photonic crystal [5,6], or by promoting emission into a single mode that couples well to the far-field optics, such as with a nanoantenna [7,8]. Numerical design of these structures often focuses on the localized “cavity” modes of high-quality factor because these modes show a clear initial decay and can be calculated using a small simulation volume, and thus in a practical run-time. Simulations are less able to predict non-cavity (often called “leaky”) modes that are spectrally broad, overlapping, and are difficult to extract from numerical finite-difference time-domain (FDTD) and finite element method (FEM) simulations. Understanding the role of these non-cavity decay channels is essential for a complete understanding of photon source behavior, as they provide alternative radiative decay channels.

A popular design for efficiently generating single photons embeds semiconductor quantum dots (QDs) in a monolithic micropillar cavity [9–11]. A cavity spacer layer between distributed Bragg reflectors (DBRs) forms cavity modes within the stop band of the DBRs, and the lateral mode is confined by etching the planar structure into pillars. QDs are typically

positioned at an antinode in the cavity field to maximize coupling to the fundamental HE_{11} cavity mode [12,13]. Recent years have seen steady progress towards unity efficiency, single-photon purity, and indistinguishability in such sources [14–18] driven by advances in processing [14], *in situ* lithography [19], and coherent excitation [20,21].

In the “weak-coupling” regime, where coupling strength is well below the mode or emitter linewidth, a transition’s emission rate is increased on resonance via Purcell enhancement [9,22], leading to reduced emission into non-cavity modes [23]. The coupling between a single transition and the cavity mode at zero detuning is quantified by the Purcell factor F_P , typically defined as the ratio of the radiative decay rate inside the cavity, given by the sum of the decay into the localized cavity mode Γ_C and the decay into the non-cavity modes Γ_L [24], relative to the radiative decay rate in a uniform homogeneous medium Γ_0 . In the case where $\Gamma_C \gg \Gamma_L$ the Purcell factor can also be approximated analytically using the mode volume V , quality factor Q , and effective refractive index n_{eff} [25]:

$$F_P = \frac{\Gamma_C + \Gamma_L}{\Gamma_0} \approx \frac{3Q\lambda^3}{4\pi^2 V n_{\text{eff}}^3}. \quad (1)$$

The fraction of photons emitted into the cavity mode is called the spontaneous-emission coupling factor, or β factor. It is thus related to the Purcell factor by

$$\beta = \frac{\Gamma_C}{\Gamma_C + \Gamma_L} = \frac{F_P}{F_P + \Gamma_L/\Gamma_0}. \quad (2)$$

Multiple methods exist for experimentally determining F_P [26], but the most direct is to measure the decay of the emission intensity in time. In solid state systems, it is not always possible to make a comparable measurement of the decay Γ_0 for the same source, and therefore authors estimate Γ_0

*Corresponding author: BennettA19@cardiff.ac.uk

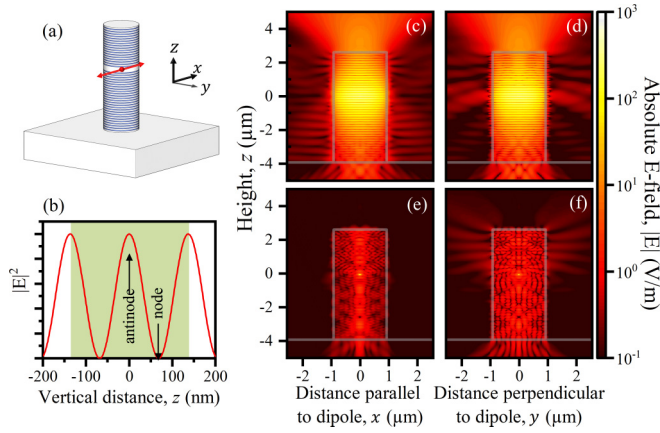


FIG. 1. (a) Simulation geometry containing a micropillar with 17 (26) upper (lower) DBR pairs, excited by a dipole orientated along the x axis. (b) Sketch of the standing wave in the cavity mode electric field intensity in the GaAs spacer (green). (c)–(f) Absolute electric field $|E|$ cross-sectional profiles for a $1.85 \mu\text{m}$ micropillar (gray outline) at the HE_{11} mode wavelength. (c), (d) for a dipole at the antinode position in the center of the spacer layer: (c) on the $y = 0$ plane ($x - z$), parallel to the dipole and (d) on the $x = 0$ plane ($y - z$), perpendicular to the dipole. (e), (f) as (c), (d), but for a dipole at the lower node.

from an emitter assumed to be comparable in another sample [27]. Alternatively, the transition-mode detuning can be varied by temperature [26,28], deposition [29], static electric [30], or magnetic [31] fields. Besides the fact that these control parameters may lead to a change in Γ_0 and Q to some extent, there is an implicit assumption that a decay rate detuned from a mode, Γ_L , is comparable to that in a homogenous medium, Γ_0 . However, this is generally not the case, as we show here, because the inhomogeneous dielectric environment and its influence on the local photon density of states (LPDOS) remains. We note that the notion of emission into individual modes is approximate, as this LPDOS should be expressed as a sum over all modes of the system and interference occurs between modes [32].

Here we investigate the effect of the non-cavity modes, comparing a pair of nominally identical micropillar samples, differing only in that one has QDs located at a field antinode where Purcell-enhanced emission into HE_{11} dominates, and the other has QDs at a node, where coupling into HE_{11} is suppressed. We compare the emission of QD transitions in both cases averaged over several cavities to quantify the emission that is collected from non-cavity modes. Furthermore, individual cavities with a small number of well-resolved transitions are studied to investigate phonon-assisted emission into HE_{11} . Single transitions are tuned across the cavity mode using a Faraday-geometry magnetic field, to determine the change in decay time arising from the Purcell effect. This study provides a toolset to quantify the effects of non-radiative decay, non-cavity modes, and phonon-assisted coupling in this well-studied system.

Simulations of dot-cavity coupling. We begin by simulating $1.85\text{-}\mu\text{m}$ -diameter circular GaAs- $\text{Al}_{0.95}\text{Ga}_{0.05}\text{As}$ micropillars in Ansys Lumerical FDTD, as shown in Fig. 1(a). The micropillar consists of a 267.9-nm GaAs spacer layer, with

DBRs of $17 \lambda/4$ alternating GaAs and $\text{Al}_{0.95}\text{Ga}_{0.05}\text{As}$ pairs above and 26 pairs below, standing on a planar GaAs substrate. The refractive indices of the materials include dispersion but no absorption, i.e., the imaginary part is zero. QD emission is modeled as an electric dipole source at $x = y = 0$, oriented along the x axis. The height of the dipole (z) is varied to probe nodes and antinodes of the mode as sketched in Fig. 1(b). The dipole is driven with a Gaussian pulse with 5.6 fs full width at half maximum (FWHM), covering a spectral range from 840 to 1070 nm. A total spectral average power of 3.79 fW is injected by the dipole. The simulation volume has x and y dimensions of $5.5 \mu\text{m}$ and a z dimension of $10 \mu\text{m}$, with perfectly matched layers at the simulation boundaries. Each surface of the simulation volume has a planar frequency-domain field monitor to record the electric field and transmission. The spectrally resolved power through the top surface monitor reveals a HE_{11} quality factor of $\sim 21\,600$, consistent with analytical models [33]. Additional planar field monitors normal to each dimension x , y , and z intersect the origin. Simulations ran until the system energy dropped to 10^{-6} of its initial value.

The electric field amplitude at the HE_{11} mode wavelength of 937.827 nm on the $y = 0$ (x - z) and $x = 0$ (y - z) planes are shown in Figs. 1(c)–1(f). For a dipole at the antinode of the electric field ($z = 0$), the distribution on the plane $y = 0$ parallel to the dipole reveals a dominant component of emission in the vertical direction [Fig. 1(c)]. The distribution on the plane $x = 0$, orthogonal to the dipole [Fig. 1(d)] also shows strong emission in the vertical direction, but also some guiding in the horizontal direction at the spacer layer, which will not be collected by an optic above the sample. This is not seen on the plane parallel to the dipole, which cannot emit along its axis. Conversely, when the dipole is placed at the lower node of the cavity electric field, at one-quarter of the spacer height ($z = -0.067 \mu\text{m}$), the field intensity does not become enhanced and guided modes of high radial quantum number dominate. A large fraction of the light escapes downward into the high index substrate.

To quantify the direction of emission, we define an out-coupling efficiency parameter ξ , describing the fraction of the total power integrated over all directions $\Gamma_C + \Gamma_L$ that is directed towards the top of the micropillar via the cavity mode Γ_1 :

$$\xi = \frac{\Gamma_1}{\Gamma_C + \Gamma_L}. \quad (3)$$

To optimize collection efficiency it is thus desired to maximize this value [34].

In Fig. 2(a), we show the spontaneous-emission coupling factor β , out-coupling efficiency ξ , and Purcell factor F_P as functions of the dipole position z within the spacer. β was calculated using Eq. (2) based on the energy-resolved total transmission through the closed volume around the simulation volume, isolating the HE_{11} mode from the spectrally broad non-cavity-mode emission by fitting a Lorentzian function. We find $\beta = 0.989$ when the dipole is at the antinodes in the bottom, middle, and top of the spacer, and $\beta = 5 \times 10^{-4}$ at the nodes. The out-coupling efficiency ξ is determined using the ratio of the energy-resolved emission through the top planar monitor, again isolating the HE_{11} mode

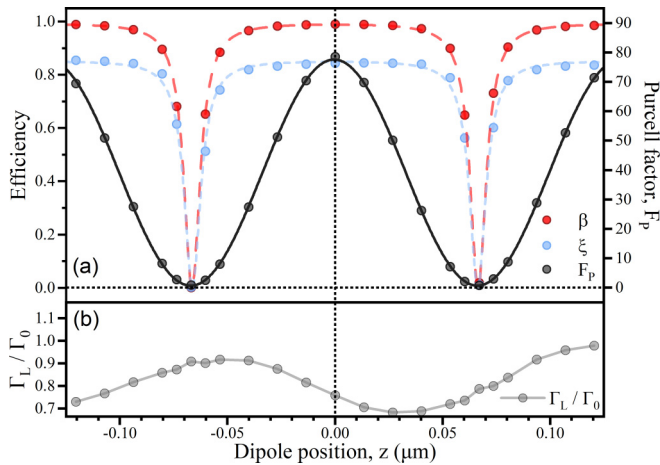


FIG. 2. Simulation results showing how (a) spontaneous-emission enhancement factor β (red), out-coupling efficiency ξ (blue), and Purcell factor F_p (black), and (b) the ratio of non-cavity modes decay rate to the decay rate in a homogeneous medium Γ_L/Γ_0 vary with dipole source height z .

from the background using a Lorentzian function, to the total emissions in all directions, as per Eq. (3). ξ reaches 0.849 at the antinode and falls to 3×10^{-6} at the nodes.

F_p was also calculated from the total power emitted in all directions at the HE_{11} mode energy, normalized to the dipole source power in a homogenous medium of the local refractive index. It closely follows a sinusoidal pattern peaking at $F_p \sim 78$ at antinode positions. Conversely, F_p falls to 0.91 at the lower node, indicating some suppression of radiative emission at the mode wavelength at these source heights. It should be noted that the FDTD simulations do not simulate rough sidewalls on the cavities, which have been reported [10–12] to dominate losses for cavity diameters below $2.5 \mu\text{m}$, suppressing Q and decreasing F_p towards unity.

Figure 2(b) shows the emission via non-cavity modes relative to the emission in a homogenous medium, Γ_L/Γ_0 , calculated from F_p and β as a function of z . This also shows a near-sinusoidal pattern but with lower contrast, a different phase, and longer period than the variation in F_p shown in Fig. 2(a). This variation in non-cavity modes is a result of the semiconductor-air interfaces. The difference in period clearly shows that the cavity mode has no direct influence on the non-cavity modes and there is no conservation in LPDOS at a given frequency. We note that at all heights Γ_L/Γ_0 is below unity, being 0.76 at position $z = 0$. As the non-cavity modes are different from the cavity mode HE_{11} , observing a different periodicity in Fig. 2(b) is expected. Specifically, higher-order guided modes of the extended cylindrical pillar, outside the stop-band of the Bragg mirrors, are reflected at the top GaAs-air interface. Due to the high index contrast, the reflection is strong, creating a standing-wave pattern, which leaks to the GaAs substrate.

Experimental comparison of dots at nodes and antinodes in the electric field. In the following experimental work, we study samples with emitters at different heights, nominally identical to the simulated structures. Using direct-write projection photolithography, two samples grown on 3-in. wafers by molecular beam epitaxy were etched into cylindrical

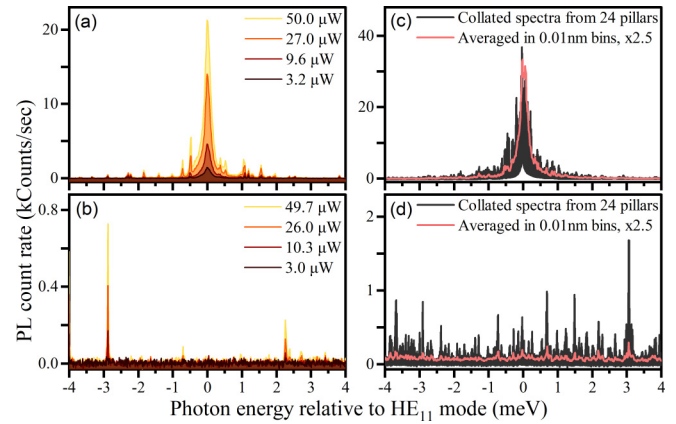


FIG. 3. PL spectra integrated over 10 s at varying powers for $1.85 \mu\text{m}$ pillars without transitions resonant with the HE_{11} mode in (a) sample A and (b) sample B. Averaged spectra from twenty-four $1.85 \mu\text{m}$ pillars at low power in (c) sample A and (d) sample B.

micropillars of a range of sizes [11], although here we focus on those of $1.85 \mu\text{m}$ diameter, as simulated. Sample A contains InAs QDs at the midpoint of the cavity spacer, at a cavity mode antinode. Conversely, sample B contains InAs QDs at one-quarter of the spacer height, at a node of the cavity mode. The cavity mode energy, measured for a planar structure, varies between the samples by 0.73%. Therefore, the following data is plotted against energy relative to the cavity mode determined from the white light reflectivity spectra at 4 K.

Photoluminescence (PL) spectra under 850 nm continuous wave (CW) laser excitation were recorded from single micropillars using a confocal arrangement with an objective lens of numerical aperture $\text{NA} = 0.81$. Exemplary cavities, shown in Figs. 3(a) and 3(b) were selected to show no sharp transitions near the HE_{11} cavity mode at 4 K and $50 \mu\text{W}$ excitation power. Sample A displays an emission peak at the HE_{11} mode energy, as if driven by a spectrally broad internal light source in the cavity, such that the intensity at the mode energy is a factor of 418 ± 48 greater than when far from the mode. This “cavity feeding” is the result of cavity-enhanced phonon-assisted emission by spectrally detuned transitions within the cavity [35,36]. The intensity at the mode energy increases and saturates at higher powers, as the zero-phonon transitions also do. Conversely, when sample B is exposed to identical excitation conditions there is no visible mode, confirming that positioning the dots at a node suppresses the cavity-enhanced phonon-assisted emission. This is consistent with the simulations in Fig. 2 for a dipole at the node. The ratio of intensities at the mode energy for the two cavities is 764 ± 70 , suggesting that even if emission is reaching the collection optic via the non-cavity modes, it does not display any spectral structure within the 35 nm range acquired with the spectrometer, and is strongly suppressed relative to photon collection via the HE_{11} mode in sample A.

It is nontrivial to compare two individual cavities in any experiment where the $x - y$ position of the dot, its Γ_0 , and photophysics, are unknown. We therefore also probe, under identical conditions, 24 neighboring micropillars of $\sim 1.85 \mu\text{m}$ diameter at 4 K under $50 \mu\text{W}$ power. For each cavity, the spectrum is offset by the mode energy determined

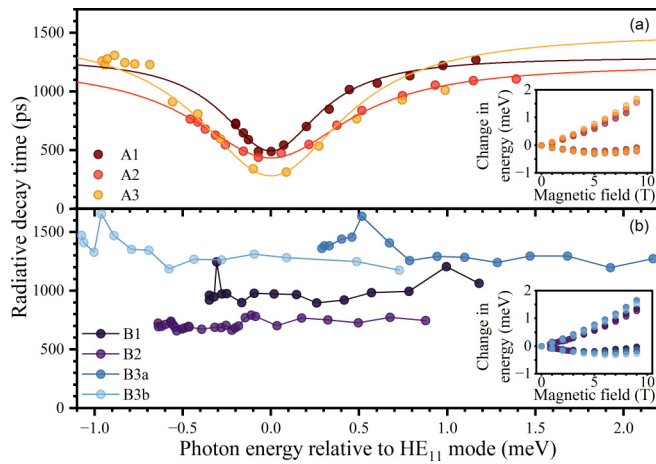


FIG. 4. Radiative decay time as a function of transition-mode detuning via magnetic field tuning in Faraday geometry for (a) sample A and (b) sample B. Different transitions are indicated in different colors, as labeled. Insets show the dependence of the transitions' energy as a function of magnetic field.

from a reflectivity measurement to produce, in Figs. 3(c) and 3(d), plots of the mean spectrum. Sample A shows an intensity enhancement for transitions near the mode. We estimate a Q factor of ~ 5000 in PL, and an enhancement of the photon collection by a factor of 560 ± 150 over the transitions spectrally detuned from the mode. Conversely, in sample B, there is no enhancement at the mode energy; the transitions' brightness displays no trend with energy. The intensity at the mode energy is a factor of 395 ± 5 below the comparable value in sample A. The absence of the cavity mode in the spectra of sample B is consistent with the simulations which suggest only a small fraction of light collected via the cavity mode ξ . Any light we do collect may have been scattered from the rough pillar sidewalls, explaining the lack of spectral features.

In order to tune a given QD transition relative to the cavity mode, we performed measurements under a magnetic field B applied along the z axis. In this Faraday geometry the Zeeman effect and diamagnetic response tunes the transition energy relative to the cavity mode, as shown in the inset to Fig. 4(a). It is assumed that the magnetic field does not modify the Γ_L and Γ_0 emission rates. A 76-MHz pulsed laser and avalanche photodiodes of 247 ps Gaussian FWHM timing jitter were used to record the decay time of each transition at a time-averaged power of $14.4 \mu\text{W}$, where the transition is substantially below saturation. The data was collected from pre-selected bright, isolated transitions less than 1 nm in the wavelength above the cavity resonance at $B = 0$ T. Most transitions studied are in separate micropillars, except B3a and B3b. The Zeeman energy splitting increases linearly, consistent with excitonic g factors between 2.639 and 3.525, as would be expected for InAs QDs of this type [37,38]. There is also a quadratic diamagnetic blueshift with coefficients ranging from 6.67 to $9.66 \mu\text{eV}/\text{T}^2$.

In sample A [Fig. 4(a)] we observe a reduction of the decay time for transitions resonant with the cavity mode, consistent with Purcell enhancement. The data has been fitted with a Lorentzian curve, which matches the data in most cases, but

some asymmetric deviation far from the mode is observed for A3. The ratio of the lifetime at large detunings to the minimum lifetime, for transitions A1, A2, and A3, is 2.53 ± 0.05 , 3.80 ± 0.09 , and 5.02 ± 0.69 , respectively. Noting that as the lifetime at large detuning is determined by Γ_L, F_P as defined in Eq. (1) will be a factor of $\Gamma_L/\Gamma_0 = 0.76$ lower than these ratios. The corresponding β values of 0.72 ± 0.02 , 0.79 ± 0.04 , and 0.83 ± 0.16 are found using Eq. (2).

In contrast, for sample B there does not appear to be any cavity-mode-dependent enhancement or suppression of the lifetime of a quantum dot transition, confirming that the coupling of the transition to the cavity mode is strongly suppressed. The minimal variation in lifetime also confirms the LPDOS given by the sum of the non-cavity modes is spectrally flat over the tuning range of a few meV. The reduced density of states at this location in the cavity, $\Gamma_L/\Gamma_0 = 0.91$ found in the simulations [Fig. 2(b)], implies a small Purcell suppression of radiative decay for all these transitions.

F_P and β are lower than predicted, which we attribute to the differences between the ideal case modeled and a real quantum dot in a micropillar. Firstly, the quality factors of the micropillars studied experimentally are significantly lower than those simulated, which we attribute to the roughness of the sidewalls. This roughness can be quantified by a single value that benchmarks how cavity loss is affected by scattering, known as the sidewall loss coefficient, previously shown to be $k_s = 50 \pm 20$ pm in these samples [11]. Assuming roughness leaves the mode volume of the micropillar unchanged, one might expect a decrease in F_P , based on Eq. (1). The micropillars in each sample displayed $Q \sim 5000$, a factor of about 4 below the simulated value, which reduces the maximum F_P to 18. Secondly, the QDs may not be located on the central axis of the pillar. Assuming a uniform density of QDs over the cross-sectional area of the pillar, we can estimate a median radial displacement of $0.654 \mu\text{m}$. Simulations of $1.85 \mu\text{m}$ pillars with dipole sources displaced from $x = y = 0$ indicate that the Purcell factor decreases rapidly with displacement from the center of the micropillar in a Gaussian-like pattern, such that we might expect the median F_P to be further reduced to 5.8. A slightly larger radial displacement of $>0.7 \mu\text{m}$ would be sufficient to reduce F_P to the experimentally observed values.

Conclusion. In the cavity we have considered here, the LPDOS of the non-cavity modes results in $\Gamma_L/\Gamma_0 = 0.68$ – 0.98 as the dipole position is varied along z . This implies the common experimental practice of tuning transitions relative to the cavity mode systematically overestimates the Purcell factor, because the system moves from an enhanced decay rate on resonance to suppression of emission at large detuning. Using a sample with emitters at a node in the cavity mode, we have confirmed experimentally that the non-cavity modes are spectrally broad. Further simulations would be required to determine the broadband structure of the non-cavity modes LPDOS. Also, future work may focus on the design of cavities with modified mirrors, spacer, and diameter that result in a reduced Γ_L/Γ_0 over an increased volume in the cavity, to increase F_P and β for a larger number of dots. This study underlines the importance of a proper understanding of the interplay between cavity and non-cavity modes in experimental determination of the Purcell factor, which has implications for

the characterization of photon sources in all nanostructured systems including nanolasers, photonic crystals, open cavities, nanoantennas, and integrated photonics.

Information on the data underpinning the results presented here, including how to access them, can be found in the Cardiff University data catalogue at Ref. [39].

Acknowledgments. We acknowledge financial support from EPSRC Grants No. EP/T017813/1 and No. EP/T001062/1. Sample processing was carried out in the cleanroom of the ERDF funded Institute for Compound Semiconductors at Cardiff University. R.C. was supported by EPSRC Grant No. EP/S024441/1 and the National Physical Laboratory.

-
- [1] S. Magnitskii, D. Frolovstev, D. Agapov, A. Demin, V. Krutikov, and G. Levin, Metrology of single photons for quantum information technologies, *Meas. Tech.* **60**, 235 (2017).
- [2] J. Kołodęski, A. Máttar, P. Skrzypczyk, E. Woodhead, D. Cavalcanti, K. Banaszek, and A. Acín, Device-independent quantum key distribution with single-photon sources, *Quantum* **4**, 260 (2020).
- [3] T. Rudolph, Why I am optimistic about the silicon-photonics route to quantum computing, *APL Photon.* **2**, 030901 (2017).
- [4] R. Raussendorf and J. Harrington, Fault-tolerant quantum computation with high threshold in two dimensions, *Phys. Rev. Lett.* **98**, 190504 (2007).
- [5] D. Englund, D. Fattal, E. Waks, G. Solomon, B. Zhang, T. Nakaoka, Y. Arakawa, Y. Yamamoto, and J. Vučković, Controlling the spontaneous emission rate of single quantum dots in a two-dimensional photonic crystal, *Phys. Rev. Lett.* **95**, 013904 (2005).
- [6] L. Sapienza, H. Thyrestrup, S. Stobbe, P. D. Garcia, S. Smolka, and P. Lodahl, Cavity quantum electrodynamics with Anderson-localized modes, *Science* **327**, 1352 (2010).
- [7] J. Claudon, J. Bleuse, N. S. Malik, M. Bazin, P. Jaffrenou, N. Gregersen, C. Sauvan, P. Lalanne, and J.-M. Gérard, A highly efficient single-photon source based on a quantum dot in a photonic nanowire, *Nat. Photon.* **4**, 174 (2010).
- [8] A. G. Curto, G. Volpe, T. H. Taminiau, M. P. Kreuzer, R. Quidant, and N. F. Van Hulst, Unidirectional emission of a quantum dot coupled to a nanoantenna, *Science* **329**, 930 (2010).
- [9] K. J. Vahala, Optical microcavities, *Nature (London)* **424**, 839 (2003).
- [10] J. Gerard, D. Barrier, J. Marzin, R. Kuszelewicz, L. Manin, E. Costard, V. Thierry-Mieg, and T. Rivera, Quantum boxes as active probes for photonic microstructures: The pillar microcavity case, *Appl. Phys. Lett.* **69**, 449 (1996).
- [11] P. Androvitsaneas, R. N. Clark, M. Jordan, M. Alvarez Perez, T. Peach, S. Thomas, S. Shabbir, A. D. Sobiesierski, A. Trapalis, and I. A. Farrer, Direct-write projection lithography of quantum dot micropillar single photon sources, *Appl. Phys. Lett.* **123**, 094001 (2023).
- [12] S. Reitzenstein and A. Forchel, Quantum dot micropillars, *J. Phys. D: Appl. Phys.* **43**, 033001 (2010).
- [13] F. R. Connor, *Wave Transmission* (Edward Arnold, London, 1972).
- [14] X. Ding, Y. He, Z.-C. Duan, N. Gregersen, M.-C. Chen, S. Unsleber, S. Maier, C. Schneider, M. Kamp, and S. Höfling, On-demand single photons with high extraction efficiency and near-unity indistinguishability from a resonantly driven quantum dot in a micropillar, *Phys. Rev. Lett.* **116**, 020401 (2016).
- [15] H. Wang, Y.-M. He, T.-H. Chung, H. Hu, Y. Yu, S. Chen, X. Ding, M.-C. Chen, J. Qin, and X. Yang, Towards optimal single-photon sources from polarized microcavities, *Nat. Photon.* **13**, 770 (2019).
- [16] B.-Y. Wang, E. V. Denning, U. M. Gür, C.-Y. Lu, and N. Gregersen, Micropillar single-photon source design for simultaneous near-unity efficiency and indistinguishability, *Phys. Rev. B* **102**, 125301 (2020).
- [17] A. J. Bennett, J. P. Lee, D. J. Ellis, T. Meany, E. Murray, F. F. Floether, J. P. Griffiths, I. Farrer, D. A. Ritchie, and A. J. Shields, Cavity-enhanced coherent light scattering from a quantum dot, *Sci. Adv.* **2**, e1501256 (2016).
- [18] N. Tomm, A. Javadi, N. O. Antoniadis, D. Najer, M. C. Löbl, A. R. Korsch, R. Schott, S. R. Valentin, A. D. Wieck, and A. Ludwig, A bright and fast source of coherent single photons, *Nat. Nanotechnol.* **16**, 399 (2021).
- [19] A. Dousse, J. Suffczynski, A. Beveratos, O. Krebs, A. Lemaître, I. Sagnes, J. Bloch, P. Voisin, and P. Senellart, Ultrabright source of entangled photon pairs, *Nature (London)* **466**, 217 (2010).
- [20] A. Muller, E. B. Flagg, P. Bianucci, X. Wang, D. G. Deppe, W. Ma, J. Zhang, G. Salamo, M. Xiao, and C.-K. Shih, Resonance fluorescence from a coherently driven semiconductor quantum dot in a cavity, *Phys. Rev. Lett.* **99**, 187402 (2007).
- [21] A. Nick Vamivakas, Y. Zhao, C.-Y. Lu, and M. Atatüre, Spin-resolved quantum-dot resonance fluorescence, *Nat. Phys.* **5**, 198 (2009).
- [22] E. Moreau, I. Robert, J. Gérard, I. Abram, L. Manin, and V. Thierry-Mieg, Single-mode solid-state single photon source based on isolated quantum dots in pillar microcavities, *Appl. Phys. Lett.* **79**, 2865 (2001).
- [23] P. Androvitsaneas, A. B. Young, C. Schneider, S. Maier, M. Kamp, S. Höfling, S. Knauer, E. Harbord, C.-Y. Hu, and J. G. Rarity, Charged quantum dot micropillar system for deterministic light-matter interactions, *Phys. Rev. B* **93**, 241409(R) (2016).
- [24] A. M. Fox, *Quantum Optics: An Introduction* (Oxford University Press, New York, 2006), Vol. 15.
- [25] E. Purcell, Spontaneous emission probabilities at radio frequencies, *Phys. Rev.* **69**, 681 (1946).
- [26] M. Munsch, A. Mosset, A. Auffèves, S. Seidelin, J.-P. Poizat, J.-M. Gérard, A. Lemaître, I. Sagnes, and P. Senellart, Continuous-wave versus time-resolved measurements of Purcell factors for quantum dots in semiconductor microcavities, *Phys. Rev. B* **80**, 115312 (2009).
- [27] J.-M. Gérard, B. Sermage, B. Gayral, B. Legrand, E. Costard, and V. Thierry-Mieg, Enhanced spontaneous emission by quantum boxes in a monolithic optical microcavity, *Phys. Rev. Lett.* **81**, 1110 (1998).
- [28] L. Engel, S. Kolatschek, T. Herzog, S. Vollmer, M. Jetter, S. L. Portalupi, and P. Michler, Purcell enhanced single-photon emission from a quantum dot coupled to a

- truncated Gaussian microcavity, *Appl. Phys. Lett.* **122**, 043503 (2023).
- [29] K. Hennessy, C. Högerle, E. Hu, A. Badolato, and A. Imamoglu, Tuning photonic nanocavities by atomic force microscope nano-oxidation, *Appl. Phys. Lett.* **89**, 041118 (2006).
- [30] A. Nowak, S. Portalupi, V. Giesz, O. Gazzano, C. Dal Savio, P.-F. Braun, K. Karrai, C. Arnold, L. Lanco, and I. Sagnes, Deterministic and electrically tunable bright single-photon source, *Nat. Commun.* **5**, 3240 (2014).
- [31] F. Jenkins and E. Segre, The quadratic Zeeman effect, *Phys. Rev.* **55**, 52 (1939).
- [32] E. A. Muljarov and W. Langbein, Exact mode volume and Purcell factor of open optical systems, *Phys. Rev. B* **94**, 235438 (2016).
- [33] E. F. Schubert, *Light-Emitting Diodes* (E. Fred Schubert, New York, 2018).
- [34] P. Androvitsaneas, A. Young, J. Lennon, C. Schneider, S. Maier, J. Hinchliff, G. Atkinson, E. Harbord, M. Kamp, and S. Höfling, Efficient quantum photonic phase shift in a low Q-factor regime, *ACS Photon.* **6**, 429 (2019).
- [35] U. Hohenester, A. Laucht, M. Kaniber, N. Hauke, A. Neumann, A. Mohtashami, M. Seliger, M. Bichler, and J. J. Finley, Phonon-assisted transitions from quantum dot excitons to cavity photons, *Phys. Rev. B* **80**, 201311(R) (2009).
- [36] U. Hohenester, Cavity quantum electrodynamics with semiconductor quantum dots: Role of phonon-assisted cavity feeding, *Phys. Rev. B* **81**, 155303 (2010).
- [37] T. Nakaoka, T. Saito, J. Tatebayashi, S. Hirose, T. Usuki, N. Yokoyama, and Y. Arakawa, Tuning of g -factor in self-assembled In(Ga)As quantum dots through strain engineering, *Phys. Rev. B* **71**, 205301 (2005).
- [38] T. Nakaoka, T. Saito, J. Tatebayashi, and Y. Arakawa, Size, shape, and strain dependence of the g factor in self-assembled In(Ga)As quantum dots, *Phys. Rev. B* **70**, 235337 (2004).
- [39] Doi: [10.17035/d.2024.0305910438](https://doi.org/10.17035/d.2024.0305910438)