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# High performance thermoelectrics from low-cost and abundant CuS/CuI composites

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# 1 High performance thermoelectrics from low-cost and abundant CuS/CuI composites

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# 16 Abstract:

17 Materials with simultaneously excellent electrical conductivity ( $\sigma$ ) and high Seebeck coefficient (S) are important for thermoelectric applications. However, obtaining such 18 19 materials is a challenging task as  $\sigma$  and S vary inversely with respect to each other. Here, a 20 new fabrication process has been demonstrated that produces composite materials with 21 desired properties. Electrically highly conducting copper sulphide (CuS) particles are 22 encapsulated within a compound with a high Seebeck coefficient, i.e. copper iodide (CuI), to form core-shell type composites. The presented results show that the concept of producing 23 such composites allows the optimisation of both  $\sigma$  and S to provide enhanced 24 25 thermoelectric performance (measured by the figure of merit, zT) when compared to the individual starting materials. Quantum mechanical calculations are performed to elaborate 26 27 on the Schottky barrier formed at the interface between copper iodide and copper sulphide and elucidate aspects of the improved transport mechanism. Furthermore, an optimized 28 29 compositional ratio between the respective composite parts is identified, which at the same time exhibits a high power factor and reduced thermal conductivity. As a result, an 30 improved value of 0.46 at room temperature has been observed, demonstrating that these 31 simple, abundant, and non-toxic CuS/CuI composites are attractive candidates for 32 thermoelectrics. 33

34

- 35 Keywords: thermoelectrics; composites; core-shell; environmentally friendly; high
- 36 performance thermoelectrics
- 37

#### 38 Introduction

The majority of present thermoelectric devices are primarily based on heavy elements like tellurium, bismuth and lead.<sup>1</sup> These well-known toxic and expensive elements cause major constraints on the widespread implementation of thermoelectrics,<sup>1</sup>and as such, the development of new and abundant thermoelectric materials are essential to replace the expensive and toxic elements.<sup>1-3</sup> Such new materials should also possess improved or at least comparable thermoelectric performance as that of well-known "state-of-the-art" compounds for them to become widely used in device fabrication.<sup>4-7</sup>

The thermoelectric efficiency, also known as the "figure of merit" (zT) of a material depends on the electrical conductivity ( $\sigma$ ), the Seebeck coefficient (S), and the thermal conductivity ( $\kappa$ ). The thermoelectric figure of merit is defined by<sup>8</sup>

49 
$$zT = \frac{S^2 \sigma T}{\kappa}, \#(1)$$

The primary challenge in optimizing materials is the fact that all these properties ( $\sigma$ , S, 50 and  $\kappa$ ) are strongly interrelated<sup>9</sup> and furthermore have different dependences on the 51 carrier density. For illustration, the electrical conductivity of a material increases with an 52 increase in carrier density, which is beneficial for zT, but simultaneously, the Seebeck 53 54 coefficient decreases, which is detrimental to  $zT.^9$  In addition, the third parameter  $\kappa$  also tends to increase due to the electrical contribution to the thermal conductivity, which is 55 again detrimental to zT. Therefore, careful tuning of these properties is a key factor to 56 achieve improvements in the performance of any thermoelectric material. 57

Among various schemes that have been shown to effectively enhance zT, developing a multi-58 phase composite thermoelectric compound is an emerging improvement strategy.<sup>10, 11</sup> 59 These multiphase composites can break the strongly coupled electronic and thermal 60 61 parameters, which helps to achieve high thermoelectric performances. In this work, copper 62 sulphide (CuS) particles are encapsulated with copper iodide (CuI) in a facile synthesis 63 methodto produce CuS:CuI composites. The composites show highly conductive CuS particles uniformly dispersed in the matrix of Cul, forming an interesting "core-shell type" 64 65 structure. Thus, the as-formed composites provide a combination of high electrical conductivity (from CuS) and high Seebeck coefficient (from CuI) and as a result, significant 66 67 enhancements in the zT, with a maximum value of 0.46 (at 300 K), have been observed for the optimised compositions of the composite material. It is predicted that the observed 68 69 phenomenon is a typical case of energy filtering mechanism commonly observed in different thermoelectric materials.12-14 70

71 It is wellknown that only very few materials show practically useful zT values at room 72 temperature, and most of these are expensive, toxic and require energy-intensive 73 manufacturing processes.<sup>15-18</sup> Therefore, the developed low-cost and abundant CuS:CuI 74 composites are potential candidates for low-grade heat recovery.

# 76 Experimental Section

# 77 Synthesis of starting materials-copper sulphide (CuS) and copper iodide (CuI):

Gram-scale CuS particles were produced from elemental Cu and S powders following a previously reported method.<sup>19</sup> Cu (99.9%, Alfa Aesar) and S (99.5%, Alfa Aesar) powders were directly mixed according to the required composition in hydrazine hydrate/water solvent under continuous magnetic stirring at 80 °C for ~ 4 hr. The resulting dark brown particles were washed, collected and dried in an oven at 50 °C. Cul powder was synthesised using an aqueous route by mixing copper sulphate (AR grade, Alfa Aesar) and potassium iodide (AR grade, Alfa Aesar) solutions at room temperatures.

# 85 Synthesis of Cul encapsulated CuS particles:

Cul powder was dissolved in acetonitrile (CH<sub>3</sub>CN, Alfa Aesar) by ultrasonication to form a 86 transparent solution. Then the Cul solution was slowly added (~ 1 mL each time) into a 87 pestle mortar containing CuS particles with continuous and gentle grinding. The mixing was 88 89 carried out at  $\sim$  30 (±2) °C to accelerate solvent evaporation. The stepwise addition of Cul solution was carried out until a desired amount of CuI was added to the mixture and finally, 90 91 Cul encapsulated CuS composites were collected and dried at 50 °C. A schematic illustration of the synthesis is shown in Figure 1. A series of samples of composition CuS:CuI (wt%) = 1:0, 92 1:0.5, 1:1, 1:2, 1:3, 1:4, 1:5, and 0:1 were prepared for the thermoelectric study. 93

#### 94 <u>Characterisation:</u>

Crystal structures of the composites and starting materials were characterised using a 95 Bruker D8 diffractometer with Cu Kα radiation. SEM (Scanning electron microscope) images 96 were recorded using a Hitachi TM3030 SEM equipped with an Oxford X-map energy 97 dispersive X-ray spectrometer (EDX) system. For thermoelectric measurements, thin pellets 98 99 of the composite samples were obtained from pressing the powders (pressure  $\sim$  12 ton, 100 pressing time  $\sim$  30 min, pellet diameter 16 mm) at room temperature and were cut into bar 101 shapes. The Seebeck coefficient (S) measurements were obtained with a lab built apparatus. 102 The voltage difference ( $\Delta V$ ) and temperature difference ( $\Delta T$ ) between the hot and the cold sides of the samples were used to estimate S by<sup>20</sup> 103

104 
$$S = -\left(\frac{\Delta V}{\Delta T}\right), \#(2)$$

105 The electrical conductivity was measured through a standard four probe method. The 106 thermal conductivities of all the samples were measured by a steady state method in a 107 vacuum (10<sup>-4</sup> mbar) using a home build system. The measurement procedure was carried 108 out according to the parallel thermal conductance method.<sup>21, 22</sup> In a typical measurement, 109 the thermal conductivity of a sample was obtained by measuring the total thermal 100 conductivity (sample + test setup) and the baseline thermal conductivity of the test setup (no sample). The difference of which gave the sample's thermal conductivity.<sup>22</sup> All the measurements were repeated in order to confirm the reproducibility of the obtained results.

#### 114 **Computational details**

The DFT calculations presented throughout this work were performed using the CRYSTAL17 115 code.<sup>23, 24</sup> The short-range corrected range-separated hybrid Heyd–Scuseria–Ernzerhof (HSE, 116  $\omega = 0.2$  Bohr<sup>-1</sup>)<sup>25-27</sup> functional was employed to approximate the exchange-correlation 117 118 functional in association with atom-centred Gaussian-type basis sets: copper was described by (86)-(4111)-(41d)G contractions of primitive functions as used in Doll et al,<sup>28</sup> iodide by an 119 effective-core pseudo-potential (EC) taken from Doll et al,<sup>29</sup> and sulphur by the (86)-(311)G\* 120 all-electron basis of Lichanotet al.<sup>30</sup> The s and p shells of iodide were merged for 121 122 computational efficiency and an all-electron basis set was tested for iodide when extracting the electrostatic potential (full basis information found in the Supplementary Information 123 124 file). For the evaluation of the Coulomb and exchange integrals, the tolerance factor values of 8, 8, 8, 8, and 16 were used (TOLINTEG). The convergence threshold on the self-125 consistent-field energy was set to 10<sup>6</sup> Ha for single-point and to 10<sup>7</sup> Ha for geometry 126 127 relaxations. Long range dispersion corrections were included using the semi-empirical D3 approach of Grimmeet al with Becke-Johnson damping.<sup>31-33</sup> Band structure calculations 128 129 were performed on optimized geometries along high-symmetry directions obtained using the SeeK-path interface.<sup>34, 35</sup> The diagonalization of the Hamiltonian matrix was conducted 130 in the reciprocal space using Monkhorst-Pack meshes  $^{36}$  of 15  $\times$  15  $\times$  15 for bulkCuI and 11  $\times$ 131 11  $\times$  11 for bulk CuS. The Fermi surface was smeared using a Fermi function<sup>37</sup> and a 132 temperature of 0.001 Ha.Graphical drawings were created using Ovito.<sup>38</sup> 133

The surfaceswere modelled as two-dimensional slabs, and no three-dimensional periodicity was imposed, which means that no parameter is needed for the vacuum thickness. To characterise the surface, the surface energy ( $\gamma$ ) as a measure of the thermodynamic stability has been calculated through the following expression:

138 
$$\gamma = \frac{E(n) - n \cdot E_{bulk}}{2 \cdot A}, \#(3)$$

139 where E(n) is the energy of the slab containing *n*-layers,  $E_{bulk}$  the energy of the bulk, and *A* 140 the area of one side of the slab.

The specific adhesion energy, a measure of the gained energy once the interface boundarybetween two surfaces (s1 and s2) is formed, is given by:

143 
$$\beta_{s1/s2} = \frac{E_{s1} + E_{s2} - E_{s1/s2}}{A}, \#(4)$$

where  $E_{s1}$  and  $E_{s2}$  are total energies of the respective slabs and  $E_{s1/s2}$  is the final interface energy. 146 Thermoelectric properties such as the Seebeck coefficient (S), electrical conductivity ( $\sigma$ ), and 147 electron contribution to the thermal conductivity ( $\kappa_{el}$ ) were computed using the semi-148 classical Boltzmann transport equation theory and the frozen band approximation, as 149 implemented by Sansone*et al.* in CYRSTAL.<sup>39</sup> The constant relaxation time approximation for 150 carriers was assumed and fixed at 10fs for all systems and temperatures. A dense mesh of 151 up to 120x120x120 k-points was used in the first Brillouin zone for the calculation of 152 transportcoefficients.

153

# 154 **Results and discussion**

As illustrated in Figure 1, the synthesis procedure is facile and requires no energy-intensive 155 processes. Various compositions of the CuS:Cul composites were prepared by mixing CuS 156 157 and Cul in the desired quantities. In the process, CuS particles were encapsulated within Cul, to form core-shell type composites. A schematic structure of the pelletised solid composite 158 159 is shown in figure. In order to explore the effects of CuI encapsulation of CuS particles on the thermoelectric properties of the CuS:CuI composites, CuS:CuI ratios (wt%) of x = 1:0, 160 161 1:0.5, 1:1, 1:2, 1:3, 1:4, 1:5, and 0:1 were selected in the formation of the composites. X-ray diffraction patterns of the composites along with the starting materials, CuS and CuI, are 162 163 shown in Figure 2. The starting materials confirm the single phase formation, which can be indexed to JCPDS card numbers 06-0464 (hexagonal covellite phase CuS) and 06-0246 (cubic 164 165 phase CuI), respectively. The diffraction patterns of all the composites show well-defined Bragg peaks corresponding to the crystalline planes for Cul, and the presence of minor 166 167 peaks corresponding to CuS at 32° and 47° can be observed in the composites of 1:1 and 1:2 compositions. The very small intensity of the CuS peaks in the composites could be due to 168 169 the formation of thick layers of Cul on CuS particles as well as its highly crystalline nature.



170

171 Figure 1.Schematic illustration of the synthesis procedure for CuS:CuI core-shell type composites

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When the resulting CuS:CuI composite powders were pressed into solid pellets, the samples show CuI particles distributed in the matrix of CuI as shown by an SEM image (see Figure 3) of a sample with CuS:CuI (wt%)-1:4.The CuI crystallisation on CuS can be confirmed from the well-defined elemental S and I colour distributions in Figure. High resolution images of elemental mapping and the composition are also provided in the Supporting Information (Figure S1).



Figure 2.X-ray diffraction patterns of the composites and starting materials, CuS and CuI (patterns a, b, and c
 correspond to the CuS:CuI composites of composition 1:1, 1:2, and 1:4, respectively).



182

Figure 3.SEM-EDX elemental mapping of a broken solid pellet of CuS:CuI composite sample with CuS:CuI (wt%)1:4 (b, c, and d are elemental mapping images for Cu, S, and I, respectively). The white dotted regions indicate
the presence of larger CuS islands in the sea of CuI.

The choice of the starting compounds CuS and CuI was made owing to their exceptionally 187 188 different thermoelectric properties. Both CuS and Culare well-known p-type semiconductors, where CuS exhibits an excellent metallic-like electrical conductivity and CuI 189 achieves a higher Seebeck effect.<sup>40-44</sup> As shown in Figure 4, the difference between the 190 Seebeck coefficient (S) of the starting compounds CuS and CuI was found to be quite large. 191 192 CuS has a very small S of ~10  $\mu$ VK<sup>-1</sup>, whereas CuI exhibits a high S of ~280  $\mu$ VK<sup>-1</sup>. With the addition of Cul, initially, to create composites with small quantities ofCul, no notable 193 194 changes were observed in the S values. However, after the x=1:2 composition, there was a significant increase in the S, which is mostly dominated by the properties of CuI. In contrast, 195 the electrical conductivity ( $\sigma$ ) of CuS decreased with the increase of CuI content. The 196 observed  $\sigma$  of CuS is 1.2 x 10<sup>3</sup> Scm<sup>-1</sup> but it is only 20.7 Scm<sup>-1</sup> for CuI. Although the  $\sigma$  of CuS 197 and CuI differ widely, the decrease in  $\sigma$  is slow with the increase of CuI content for the 198 composite compounds, which is a beneficial factor. As a result, the power factor (PF) has 199

200 improved in the case of all composites and reached a maximum value of  $\sim$ 1400  $\mu$ Wm<sup>-1</sup>K<sup>-2</sup> 201 for the x=1:4 composite.



202

Figure 4.Room temperature Seebeck coefficient (a), electrical conductivity (b), power factor (c), and thermal
 conductivity (d) of the CuS:CuI composites.

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Figure 4d displays the composition dependence of the total thermal conductivity ( $\kappa$ ) of the 206 CuS:CuI composites. The k values of all the composites are lower than that of pristine CuS 207 and similar to Cul. Such reduction in the  $\kappa$  of the composites indicates enhanced phonon 208 scattering at the interfaces of CuS and CuI. Simultaneously, enhanced PF and reduced κ have 209 resulted in a peak zT value of 0.46 at 300 K for x = 1:4 composite (Figure 5). Thus, our 210 presentedresults revealthe enhanced potential of CuS:CuI composite materials for room 211 temperature thermoelectric applications when compared to the individual starting 212 213 compounds.



Figure 5.Room temperature zT values of CuS:CuI composites (Inset shows the schematic structure of the
 composites).

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#### 218 <u>Calculated bulk crystal structures and electronic properties</u>

CuS, or covellite, adopts a hexagonal crystal structure (space group 194, P63/mmc) with 219 twelve atoms in the unit cell, two of which inequivalent sites for both Cu and S, and a unit 220 cell length of a = b = 3.796 Å and c = 16.36 Å.<sup>45</sup> CuI crystallizes in a cubic (zinc blende) 221 222 structure (space group 216, F-43m) with eight atoms in the unit cell and one inan equivalent position for each Cu and I. The lattice parameters are measured around 6.1 Å.<sup>46</sup>The 223 224 calculated structural parameters reproduce the experimental geometry very well, with the lattice parameters reading a = b = 3.807 Å, c = 16.249 Å for CuS and a = 6.037 Å for CuI, 225 226 obtained using the hybrid HSE functional.

The electronic band structures of CuS and CuI are shown in Figure 6. CuS is correctly described as a conductor, with copper *d*states and sulphur  $sp^3$  states dominating around the Fermi level. In contrast, CuI is an insulator, with a direct band gap found at the  $\Gamma$ -point in reciprocal space, whose Kohn-Sham value equals 3.18 eV, agreeing well with the experimentally measured separation of 3.1 eV.<sup>47</sup> The top of the valence band (VB) is

- dominated by admixed copper d and iodide  $sp^3$  states, while the bottom of the conduction
- band is mostly formed by empty copper *sp*-orbitals.



Figure 6. Calculated electronic band structure and orbital-projected densities of states for copper iodide and
copper sulphide, together with the corresponding crystallographic unit cells. Results obtained using a hybrid
HSE functional.

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# 239 <u>Calculated bulk thermoelectric properties</u>

The simulated transport properties of bulk CuS and CuI are shown in Figure 7 (individual 240 241 transport coefficients are plotted in Figure S2). The calculated electronic conductivity and Seebeck coefficient are 36.8  $\times$  10<sup>3</sup> Scm<sup>-1</sup> and 7.47  $\mu$ VK<sup>-1</sup> for CuS (values reported along the x-242 direction for a *p*-type concentration of  $1 \times 10^{21}$  cm<sup>-3</sup>at 300 K), and 3.3 Scm<sup>-1</sup> and 595.5  $\mu$ VK<sup>-</sup> 243 <sup>1</sup> for CuI (values reported for a *p*-type concentration of  $1 \times 10^{18}$  cm<sup>-3</sup> at 300 K), respectively. 244 In CuS, the x- and y-directions are isotropic, while values in the z-direction differ by up to an 245 order of magnitude, e.g.,  $5.5 \times 10^3$  Scm<sup>-1</sup> for the electrical conductivity (*p*-type concentration 246 of  $1 \times 10^{21}$  cm<sup>-3</sup> at 300 K). 247

The calculated values are in good agreement with the measurements, reproducing both the order of magnitude as well as the trend between the two compounds, further validating the accuracy of our DFT model. The simulated electronic part of the thermal conductivity of 26.8 CuS reads 26.8 Wm<sup>-1</sup>K<sup>-1</sup> in the x- and y-directions and 4.1 Wm<sup>-1</sup>K<sup>-1</sup> in the z direction, whereas

it is 0.04 Wm<sup>-1</sup>K<sup>-1</sup> for Cul. When compared to experiments (taking an average over the three 252 directions of CuS as 19.2 Wm<sup>-1</sup>K<sup>-1</sup>), the calculations overestimate the thermal conductivity, 253 which is not necessarily a surprise since he model does not include the phonon 254 255 contributions to the thermal conductivity and phonon scattering processes. However, the relation between CuS and CuI is captured correctly, where CuS demonstrates a much higher 256 257 thermal conductivity than Cul. What the simulations do reveal is that there is a strong directional dependence in CuS, where values across the xy-crystallographic plane are one 258 order of magnitude higher than those in the z-direction. This potentially serves as further 259 insight when optimizing the thermal conductivity of CuS particles and tuning their 260 properties. 261



262

Figure 7. Temperature dependence of the calculated figure of merit for bulk CuS and CuI for both p and n type doping, at the HSE level, obtained from computedSeebeck coefficient (S), electrical conductivity ( $\sigma$ ), and electronic contribution to the thermal conductivity ( $\kappa_{el}$ ). The ionic contribution to the thermal conductivity has not been taken into account.

267

With the calculated values discussed above, the dimensionless figure of merit can be 268 estimated. For CuS, a very low zT of  $3 \times 10^{-3}$  at 300 K is obtained, matching well the 269 measured values. No directional dependence of zT is noted for CuS, as the computed 270 variations are too small to make a significant difference in the thermoelectric properties 271 along a preferred crystallographic direction. The zT of CuI is computed at 0.95 at 300 K and a 272 carrier concentration of  $1 \times 10^{18}$  cm<sup>-3</sup>, which is much higher than the experimental value of 273 approximately 0.05. The origin of this large discrepancy stems from the underestimated 274 computed thermal conductivity (which neglects phononic contributions). However, if in the 275 calculation of the figure of merit for CuI we replace the computed thermal conductivity by 276 the experimental value (containing all possible contributions, not only the electronic one) of 277 approximately 0.6 Wm<sup>-1</sup>K<sup>-1</sup>, the zT value is reduced to 0.06 (p-type concentration of  $1 \times$ 278  $10^{18}$  cm<sup>-3</sup>at 300 K), matching the measured figure of merit extremely well. This indicates a 279

non-negligible lattice contribution to the thermal conductivity of Cul and the strong
 influence on the final output transport properties. At the same time this confirms that our
 DFT simulations are able to capture the correct electronic contributions (electrical
 conductivity, Seebeck coefficient, and thermal conductivity) to the overall transport
 coefficients of Cul and CuS.

285

#### 286 Modelling the interfaces between Cul and CuS

For the subsequent generation and study of the interfaces, we focused on stoichiometric (if 287 available, symmetric) and non-polar surfaces of both copper sulphide and copper iodide. All 288 seven low Miller index cleaved surfaces of CuSare non-polar, so-called type I and II 289 according to the Tasker classification.<sup>48</sup> The CuS (001) and (110) surfaces were selected for 290 291 further analysis, as they have been reported to be thermodynamically the most stable ones (by DFT)<sup>49</sup> and identified as the dominant planes in the measured XRD spectrum. For Cul, 292 293 cleaving the relaxed bulk geometry results in only one non-polar surface, the (110) planes, while the (001) and (111) surfaces exhibit a non-vanishing dipole moment across the slab. 294 295 (For easier distinction between CuS and Cul, we use the (220) surface of Cul in the remaining work, which is equivalent in structure to the (110) due to the isotropy of the 296 297 system). Such dipolar surfaces undergo significant atomic and structural reorganizations to cancel the intrinsic dipole moment, which are currently outside the scope of this study. 298 299 Surface properties obtained from relaxed slab geometries are reported in Table 1.

300

#### 301 Table 1. Calculated properties of chosen CuS and CuI surfaces: surface termination, relaxed surface energy, final

302 slab thickness, electronic band gap. Reported values obtained using the HSE functional. AE – all-electron basis 303 set, EC – effective-core potential. Reported work function, ionization potential, and electron affinity are

304 obtained using a bulk-based definition.

Surface label	Termination	Surface energy (J/m <sup>2</sup> )	Band gap (eV)	Work function Or IP/EA (eV)
CuS(110)	Cu-S	0.409	Conductive	-5.74
CuS(001)-t1	S	1.054	Conductive	-6.75
CuS(001)-t3	Cu-S	0.413	Conductive	-6.11
Cul(220)	Cu-I	0.182 (AE iodide)	2.63	-5.77/-2.44
		-0.002 (EC iodide)	2.45	N/A

305

The computed surface energies are in line with earlier theoretical values, e.g. 0.1 Jm<sup>-2</sup> for the (110) surface of Cul,<sup>50</sup> and 0.4 Jm<sup>-2</sup> and 0.3 Jm<sup>-2</sup> for the (001) and (110) surfaces of CuS, respectively (values depending on the functional). For all surface terminations chosen, the structural and electronic properties are converged reasonably wellwith models of more than 1nm thick. However, the calculated band gap of the Cul(220) surface is found to be around



312 on the under-coordinated Cu atoms.



Figure 8. Band alignment based on individual compounds between copper sulphide and copper iodide together with the respective relaxed surface geometries. Values reported for two utilized definitions of the ionization potential and electron affinity, once taken from the respective bulk and once surface values. Values calculated

317 using the HSE functional.HOCO/LUCO denote to the highest occupied/lowest unoccupied crystalline orbital.

The calculated ionization potential (IP, -5.77 eV) of CuI is found to be in good agreement with available experimental IP values of -5.26 eV and -5.05 eV for solution-processed and evaporated CuI samples.<sup>51</sup> The electron affinity (EA) of CuI is computed at -2.44 eV, with no experimental values to compares with, to the best of our knowledge.The work function of CuS is found to be in the range from -5.74 eV to -6.75 eV, in line with earlier works.<sup>52</sup>

From the computed position of the band edges of the chosen individual surfaces, a band 323 alignment scheme can be estimated, as shown in Figure 8. Since we are describing an 324 325 interface between a metallic and a semi-conducting material, instead of speaking of VB/CB offsets, by definition we are dealing with Schottky barriers. The barrier height is an intrinsic 326 property of the interface and is given by the difference between theFermi level of the 327 metallic contact compound and the semiconductor VB maximum (for the p-type barrier,  $\phi_n$ ) 328 or CB minimum (for the n-type,  $\phi_n$ ).<sup>53</sup> Based on the analysis undertaken on separate 329 surfaces (and aligned to bulk reference values), the  $\varphi_p$  value for an interface between the 330 Cul(220) and CuS(110) surfaces is 0.03 eV, while for a junction between the Cul(220) and 331 Cul(001) surfaces it equals-0.33 eV, indicating that the CuS Fermi level would be located 332 below the VB maximum of Cul. For comparison, the Schottky barriers werealso computed 333 from the ionization potential/electron affinity and work function in the surface-sensitive 334 definition, which is taken as the difference between the vacuum level and highest occupied 335 levels in the slab model.<sup>54</sup> This is done to probe the eventual influence of the surface states 336 337 on the alignment and future interface creation. The surface-sensitive  $\phi_{o}$  is found to show the same trend as the bulk-based barriers, with valuesof0.27 eV and 0.17 for the Cul(220)-338 CuS(110) and CuI(220)-CuS(001) alignments, respectively. 339

From the alignment of the independent compounds, it is clear that a definite conclusion for 340 the junction type and Schottky barrier height (SBH) between CuI and CuS cannot be 341 reached. Therefore, to gain further information about the interface structure and how it 342 affects the band alignment, explicit interfaces have been simulated. Two heterostructures 343 have been created: one matching the CuI(220) and CuS(110) surfaces and one matching the 344 Cul(220) and CuS(001)-t3 surfaces (labelled as Cul(220)/CuS(110) and Cul(220)/CuS(001), 345 respectively). In both cases, we treat CuI as the epitaxially strained film whose lattice 346 parameters accommodate themselves to those of the CuS substrate. The atomically relaxed 347 structures of the two heterojunction interfaces are shown in Figure 9 and Figure 10. 348

The calculated adhesion energy, by definition the energy required to separate the two slabs forming the interface tocreate two free surfaces,  $is\beta_{Cul(220)/CuS(110)} = 0.76 \text{ Jm}^{-2}$  and  $\beta_{Cul(220)/CuS(001)} = 0.79 \text{ Jm}^{-2}$ . These energies are very close in magnitude, indicating the stability of both interfaces and, moreover, their likely formation and presence in the experimentally measured samples. The minimal energetic difference most likely arises from the differing binding features at the two interfaces, as well as strain present in the lattice mismatch.



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Figure 9. Relaxed atomic structure of the interface formed between the Cul(220) slab acting as a film and the
CuS(110) slab acting as the substrate (left) together with the species-resolved layer-projected electronic
densities of states (LPDOS, right). Dashed lines in the relaxed structure indicate the layers separation chosen for
the LPDOS projections. Zero on the energy axis of LPDOSrefers to the Fermi level of the interface. Values
calculated using the HSE functional.

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The computed electronic layer-projected densities of states reveal distinct features between the two simulated interfaces. In the bulk region, far enough from the interface as well as bounding surfaces, the electronic structure of pristine Cul (band gap of more than 3 eV) and

CuS (metallic character throughout the slab)is recovered. However, in the interface region, a 365 finite density of states is found in the valence band of the first few layers around the 366 interface of the Cul(220)/CuS(110) heterostructure, in the range of energies which 367 otherwise span the gap of forbidden states (Figure 9). These states are found to propagate 368 2-3 atomic layers into the structure of CuI and then they decay rapidly onwards. The density 369 of these states is high enough to pin the Fermi level in the vicinity of the VB maximum of the 370 semi-conducting Cul. This can arise from two potentially relevant mechanisms: the pinning 371 of the Fermi level to so-called metal-induced gap states (MIGS) or the pinning of the Fermi 372 level to interface states (Bardeen limit<sup>55</sup>). Interface states are usually characterized by 373 strong localization in the vicinity of the interface, connected to a rapid decay on both sides 374 of the interface. However, this is not the case at the Cul(220)/CuS(110) contact as the states 375 are found present mainly on the CuI side and are broadened out to a maximal width of 1 eV, 376 strongly resembling the shape of the electronic DOS from the CuS side. 377

One additional option for the origin of the interface states could be the Cul(220) surface 378 states found responsible for the Cul band gap reduction of around 0.5-0.7 eV. However, this 379 was found to originate from predominantly empty Cu surface states positioned around the 380 CB minimum and hence can be ruled out as being present at the discussed interface or 381 responsible for the Fermi level alignment. Taking all of the above into account, it is 382 concluded that Fermi level pinning is present at the Cul(220)/CuS(110) formed 383 heterostructure as a result of newly formed MIGS in the contact region. 384



CuI(220)/CuS(001)

#### 385

386 Figure 10. Relaxed atomic structure of the interface formed between the Cul(220) slab acting as a film and the CuS(001) slab acting as the substrate (left) together with the species-resolved layer-projected electronic 387 densities of states (right). Dashed lines in the relaxed structure indicate the layers separation chosen for the 388 LPDOS projections. Zero on the energy axis of LPDOS refers to the Fermi level of the interface. Values calculated 389 390 using the HSE functional.

In contrast, the Cul(220)/CuS(001) heterostructure does not undergo any protrusion of 391 392 metallic states into the semi-conducting side, yielding a Schottky barrier with a height of 393 approximately  $\phi_p = 0.4$  eV between the CuS Fermi level and the VB maximum of the semiconducting Cul. Moreover, empty states are found on the Cul side of the heterojunction 394 penetrating a maximum of 2-3 layers into the CuI structure. These are mostly confined to Cu 395 396 states, indicating the presence of newly formed holes when the interface is formed. As a result, the band gap of CuI is reduced to 1.6 eV in the vicinity of the junction, and a Schottky 397 barrier of  $\phi_n$  = 1.2 eV is found between the CuS Fermi level and CuI CB minimum. Further 398 empty states are found on the Cul(220) surface side exposed to vacuum, but these are not 399 400 of interest for this discussion. Furthermore, the conduction band edge is found to be flat 401 across the semiconductor side, without significant bending occurring near the interface. The 402 outlined results indicate that the Cul(220)/CuS(001) heterostructure displays rectifying 403 characteristics and potential applicability as a diode.

The behaviour of the Cul/CuS interactions is further illustrated by evaluating the charge 404 density difference ( $\Delta \rho$ ), defined as  $\Delta \rho = \rho_{s1/s2} - (\rho_{s1} + \rho_{s2})$  and shown in Figure S3, which is 405 useful to estimate the extent and sign of interface dipoles.<sup>56-58</sup> Upon formation, charge 406 redistribution occurs at the interface between the first few layers, with a charge 407 accumulation at the Cul side for both studied systems. Moreover, states at the Fermi level 408 409 of the Cul(220)/CuS(110) heterostructure are clearly identified, corroborating the LPDOS results of Fermi pinning outlined earlier. This charge transfer results in the formation of an 410 interface dipole which is found to be stronger for the Cul(220)/CuS(110) interface than the 411 Cul(220)/CuS(001) structure. For both structures, the valence band edges are found flat 412 413 throughout the Cul slab, while the conduction band edge potential is lowered at the 414 interface, i.e., band bending is present towards the metal.

It is also worth noting that the electronic structure of the explicitly treated interfaces is 415 416 substantially different than the one that would be predicted in the alignment of independent compounds. For many, mostly semi-conducting materials with a minimal 417 418 lattice mismatch at the interface, the independent alignment produces satisfactory results. However, this is not the case when aligning copper iodide with copper sulphide due to the 419 420 intricate bonding features at the interface and formation of new states at the interface, 421 which are responsible for altering the position of the Fermi level. Finally, in both simulated 422 instances, the Fermi level of CuS is found positioned higher than the VB maximum of CuI, which cannot be resolved from the alignment based on individual materials. 423

Based on the given analysis, certain aspects of the improved thermoelectric composite properties may be elucidated. Upon CuI addition to the CuS matrix, layers of CuI are formed on CuS particles, effectively creating a multitude of interfaces at the nanoscale level. Based on the illustrated heterostructure analysis, the final Schottky barrier height, band bending, possibility of Fermi level pinning, and dipole strength depend on the exact nature of the planes coming into contact at the interfaces. However, the injection of electrons from the metal to the semi-conductor impedes the deterioration of the electrical conductivity from high CuS to low Cul values. Since the thermal conductivity of any given CuS:Cul composite ratio is reduced almost instantly to Cul values, the overall composite zT value is found to be increased, as it depends linearly on the electrical conductivity. As the content of Cul increases, the positive effect on the electrical conductivity wears off, since the bulk content begins to dominate over the interface region and the semi-conducting properties are restored.

Note on computing interface transport coefficients. At this point we refrain from reporting 437 transport coefficients computed via DFT for the individual slabs of CuI and CuS as well as the 438 aforementioned explicitly considered interfaces, despite the fact that we have obtained 439 them. The reasoning for that is two-fold: i) there is an intrinsic difficulty of defining two 440 441 dimensional electrical and thermal conductivities in relation to their bulk counterparts (see reference of Wu et al.<sup>59</sup> for a detailed discussion of the problem); and ii) the required 442 accuracy and convergence of sampling the reciprocal space and associated electronic band 443 structure via DFT needs to be scrutinized (on which we are preparing a separate discussion 444 in a follow-up work). 445

#### 446 Conclusion

447 The present work has revealed a very simple synthesis route to unique CuS:CuI composites, 448 which are a new and promising p-type high-performance thermoelectric material. The CuS structures encapsulated by Cul in the composites enable simultaneous higher power factors 449 450 and lower thermal conductivity at room temperature. Density functional theory simulations corroborate further the band alignment and Schottky barrier formation at the interface 451 452 between CuI and CuS and the positive effect on the overall electrical conductivity of the heterostructure. Depending on the planes in contact at the interface, Fermi level pinning 453 454 was identified, as well as electron injection from the metal to the semi-conducting side. This reveals the complex interplay between the CuI layers formed on the CuS matrix, where a 455 456 multitude of interfaces between various crystallographic planes is created, which are not all beneficial for the final output thermoelectric values. The observed maximum zT value of 457 458 0.46 suggests great potential for applications at low temperatures from low-cost and 459 abundant materials.

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# 470 **Conflict of Interest**

471 The authors declare no conflict of interest.

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# 473 Data Availability Statement

- 474 The data that support the findings of this study are available from the corresponding
- 475 author upon reasonable request.

476	Bibliography	
477	1.	O. Caballero-Calero, J. R. Ares and M. Martín-González, Advanced Sustainable Systems, 2021,
478		<b>5</b> , 2100095.
479	2.	A. Vora-ud, K. Chaarmart, W. Kasemsin, S. Boonkirdram and T. Seetawan, Physica B:
480		Condensed Matter, 2022, <b>625</b> , 413527.
481	3.	F. F. Jaldurgam, Z. Ahmad, F. Touati, A. A. Ashraf, A. Shakoor, J. Bhadra, N. J. Al-Thani and T.
482		Altahtamouni, Journal of Alloys and Compounds, 2022, 904, 164131.
483	4.	E. Isotta, J. Andrade-Arvizu, U. Syafiq, A. Jiménez-Arguijo, A. Navarro-Güell, M. Guc, E.
484		Saucedo and P. Scardi, Advanced Functional Materials, 2022, <b>32</b> , 2202157.
485	5.	G. Ersu, C. Munuera, F. J. Mompean, D. Vaquero, J. Quereda, J. E. F. S. Rodrigues, J. A.
486		Alonso, E. Flores, J. R. Ares, I. J. Ferrer, A. M. Al-Enizi, A. Nafady, S. Kuriakose, J. O. Island and
487	-	A. Castellanos-Gomez, ENERGY & ENVIRONMENTAL MATERIALS, n/a, e12488.
488	6.	I. Cao, XL. Shi and ZG. Chen, Progress in Materials Science, 2023, <b>131</b> , 101003.
489	7.	A. Liu, H. Zhu, M. G. Kim, J. Kim and Y. Y. Noh, Advanced science (Weinheim, Baden-
490	0	Wurttemberg, Germany), 2021, <b>8</b> , 2100546.
491	8.	M. S. Dresseinaus, G. Chen, M. Y. Tang, R. G. Yang, H. Lee, D. Z. Wang, Z. F. Ren, JP. Fieurial
492	0	allu P. Goglia, Auvalicea Malellais, 2007, <b>19</b> , 1043-1053.
495 494	9.	1704386.
495	10.	R. Fortulan and S. Aminorroaya Yamini, <i>Materials (Basel, Switzerland)</i> , 2021, <b>14</b> .
496	11.	R. Mulla and C. W. Dunnill, Materials Advances, 2022, <b>3</b> , 125-141.
497	12.	C. Gayner and Y. Amouyal, Advanced Functional Materials, 2020, <b>30</b> , 1901789.
498	13.	P. P. Murmu, V. Karthik, Z. Liu, V. Jovic, T. Mori, W. L. Yang, K. E. Smith and J. V. Kennedy,
499		ACS Applied Energy Materials, 2020, <b>3</b> , 10037-10044.
500	14.	A. Pakdel, Q. Guo, V. Nicolosi and T. Mori, Journal of Materials Chemistry A, 2018, 6, 21341-
501		21349.
502	15.	X. Mo, J. Liao, G. Yuan, S. Zhu, X. Lei, L. Huang, Q. Zhang, C. Wang and Z. Ren, <i>Journal of</i>
503		Magnesium and Alloys, 2022, <b>10</b> , 1024-1032.
504	16.	J. Jiang, H. Zhu, Y. Niu, Q. Zhu, S. Song, T. Zhou, C. Wang and Z. Ren, <i>Journal of Materials</i>
505	. –	Chemistry A, 2020, <b>8</b> , 4790-4799.
506	17.	C. Yang, D. Souchay, M. Kneiß, M. Bogner, H. M. Wei, M. Lorenz, O. Oeckler, G. Benstetter, Y.
507	10	Q. Fu and M. Grundmann, Nature Communications, 2017, 8, 16076.
508	18.	and L. Forroira, <i>BSC Advances</i> , 2010, <b>0</b> , 25284, 25201
509	10	aliu I. Ferreira, ASC AUVUILES, 2019, <b>3</b> , 55564-55591. R. Mulla, D. R. Jones and C. W. Dunnill, ACS Sustainable Chemistry & Engineering, 2020. <b>8</b>
510	19.	1/23/1/2/2
512	20	R Mulla K Glover and C W Dunnill IEEE Transactions on Instrumentation and
512	20.	Measurement 2021 <b>70</b> 1-7
514	21.	B. M. Zawilski, R. T. L. IV and T. M. Tritt, <i>Review of Scientific Instruments</i> , 2001, <b>72</b> , 1770-
515		1774.
516	22.	D. Ding, F. Sun, F. Xia and Z. Tang, <i>Nanoscale Advances</i> , 2020, <b>2</b> , 3244-3251.
517	23.	R. Dovesi, A. Erba, R. Orlando, C. M. Zicovich-Wilson, B. Civalleri, L. Maschio, M. Rérat, S.
518		Casassa, J. Baima, S. Salustro and B. Kirtman, WIREs Computational Molecular Science, 2018,
519		<b>8</b> , e1360.
520	24.	R. Dovesi, F. Pascale, B. Civalleri, K. Doll, N. M. Harrison, I. Bush, P. D'Arco, Y. Noël, M. Rérat,
521		P. Carbonnière, M. Causà, S. Salustro, V. Lacivita, B. Kirtman, A. M. Ferrari, F. S. Gentile, J.
522		Baima, M. Ferrero, R. Demichelis and M. D. L. Pierre, The Journal of Chemical Physics, 2020,
523		<b>152</b> , 204111.
524	25.	J. Heyd, G. E. Scuseria and M. Ernzerhof, The Journal of Chemical Physics, 2003, 118, 8207-
525		8215.
526	26.	J. Heyd and G. E. Scuseria, <i>The Journal of Chemical Physics</i> , 2004, <b>121</b> , 1187-1192.

527	27.	J. Heyd, G. E. Scuseria and M. Ernzerhof, <i>The Journal of Chemical Physics</i> , 2006, <b>124</b> , 219906.
528	28.	K. Doll and N. M. Harrison, Chemical Physics Letters, 2000, 317, 282-289.
529	29.	K. Doll and H. Stoll, <i>Physical Review B</i> , 1998, <b>57</b> , 4327-4331.
530	30.	A. Lichanot, E. Aprà and R. Dovesi, physica status solidi (b), 1993, 177, 157-163.
531	31.	S. Grimme, J. Antony, S. Ehrlich and H. Krieg, <i>The Journal of Chemical Physics</i> , 2010, <b>132</b> ,
532		154104.
533	32.	S. Grimme, S. Ehrlich and L. Goerigk, Journal of Computational Chemistry, 2011, <b>32</b> , 1456-
534		1465.
535	33.	S. Grimme, A. Hansen, J. G. Brandenburg and C. Bannwarth, <i>Chemical Reviews</i> , 2016, <b>116</b> ,
536		5105-5154.
537	34.	A. Togo and I. Tanaka, arXiv: Materials Science, 2018.
538	35.	Y. Hinuma, G. Pizzi, Y. Kumagai, F. Oba and I. Tanaka, Computational Materials Science, 2017,
539		<b>128</b> , 140-184.
540	36.	H. J. Monkhorst and J. D. Pack, <i>Physical Review B</i> , 1976, <b>13</b> , 5188-5192.
541	37.	N. D. Mermin, <i>Physical Review</i> , 1965, <b>137</b> , A1441-A1443.
542	38.	A. Stukowski, Modelling and Simulation in Materials Science and Engineering, 2010, <b>18</b> ,
543		015012.
544	39.	G. Sansone, A. Ferretti and L. Maschio, The Journal of Chemical Physics, 2017, 147, 114101.
545	40.	G. Dennler, R. Chmielowski, S. Jacob, F. Capet, P. Roussel, S. Zastrow, K. Nielsch, I. Opahle
546		and G. K. H. Madsen, Advanced Energy Materials, 2014, 4, 1301581.
547	41.	A. Liu, H. Zhu, MG. Kim, J. Kim and YY. Noh, Advanced Science, 2021, 8, 2100546.
548	42.	R. Mulla and M. K. Rabinal, Energy Technology, 2018, <b>6</b> , 1178-1185.
549	43.	R. Mulla and M. K. Rabinal, Ultrasonics Sonochemistry, 2017, <b>39</b> , 528-533.
550	44.	R. Mulla, D. R. Jones and C. W. Dunnill, <i>Materials Today Communications</i> , 2021, <b>29</b> , 102738.
551	45.	L. G. Berry, <i>American Mineralogist</i> , 1954, <b>39</b> , 504-509.
552	46.	R. W. G. Wyckoff and E. Posnjak, Journal of the American Chemical Society, 1922, 44, 30-36.
553	47.	P. Storm, M. S. Bar, G. Benndorf, S. Selle, C. Yang, H. v. Wenckstern, M. Grundmann and M.
554		Lorenz, APL Materials, 2020, <b>8</b> , 091115.
555	48.	P. W. Tasker, Journal of Physics C: Solid State Physics, 1979, 12, 4977.
556	49.	Á. Morales-García, J. He, A. L. Soares and H. A. Duarte, CrystEngComm, 2017, 19, 3078-3084.
557	50.	J. Zhu, M. Gu and R. Pandey, Applied Surface Science, 2013, <b>268</b> , 87-91.
558	51.	Y. Peng, N. Yaacobi-Gross, A. K. Perumal, H. A. Faber, G. Vourlias, P. A. Patsalas, D. D. C.
559		Bradley, Z. He and T. D. Anthopoulos, Applied Physics Letters, 2015, 106, 243302.
560	52.	BF. Shan, J. Deng and ZY. Zhao, <i>physica status solidi (b)</i> , 2021, <b>258</b> , 2100268.
561	53.	M. Peressi, N. Binggeli and A. Baldereschi, Journal of Physics D: Applied Physics, 1998, 31,
562		1273.
563	54.	Y. Hinuma, F. Oba, Y. Kumagai and I. Tanaka, Physical Review B, 2012, <b>86</b> , 245433.
564	55.	J. Bardeen, <i>Physical Review</i> , 1947, <b>71</b> , 717-727.
565	56.	G. Di Liberto, S. Tosoni and G. Pacchioni, Catalysis Science & Technology, 2021, 11, 3589-
566		3598.
567	57.	K. Cheng, N. Han, Y. Su, J. Zhang and J. Zhao, Scientific Reports, 2017, 7, 41771.
568	58.	Y. Jiao, A. Hellman, Y. Fang, S. Gao and M. Käll, <i>Scientific Reports</i> , 2015, <b>5</b> , 11374.
569	59.	X. Wu, V. Varshney, J. Lee, Y. Pang, A. K. Roy and T. Luo, Chemical Physics Letters, 2017, 669,
570		233-237.