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High-power density, single plasmon, terahertz quantum cascade lasers via transverse mode control

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ABSTRACT

Terahertz (THz) quantum cascade lasers (QCLs) have been shown to emit peak powers greater than 1 W from a single facet in a single plasmon geometry. However, this is typically achieved by increasing the laser ridge width, resulting in higher-order transverse modes, limiting the achievable power density. Here, we control and fully suppress these modes through thin metallic side-absorbers, showing laser action solely on the fundamental transverse mode operation without sacrificing high THz peak powers. This leads to enhanced power densities and electric fields of up to 1.8 kW/cm^2 and 1.17 kV/cm, respectively, opening up the possibility of applying THz QCLs as pump sources for investigations of nonlinear THz physical phenomena.

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The generation of intense terahertz (THz) frequency radiation has become an important domain to study THz nonlinear interactions in a variety of low energy phenomena ranging from high harmonic generation in Dirac materials^{1,2} to spin excitations.^{3,4} However, the THz sources used are based on downconversion of extremely powerful, large, and complex optical ultrafast lasers to the THz range⁵ with little control of the central frequency and spectral bandwidth. THz quantum cascade lasers (QCLs), on the other hand, provide an electrically driven, compact semiconductor source where the emission characteristics can be entirely chosen by design.

THz QCLs⁶ are unipolar semiconductor lasers based on electronic intersubband transitions in multi-layered heterostructures. QCLs have shown considerable developments over recent years, from high temperature operation,^{7–10} broad coverage of the THz range^{11,12} to frequency comb operation.^{13–16} Furthermore, in THz range, peak output powers of >1 W have been demonstrated from single plasmon waveguides.^{17,18} Wafer bonded ridges have also shown 470 mW output powers.¹⁹ This was achieved using high performance thick (24 μ m) active regions combined with large ridge widths (>400 μ m). However, large ridge widths will result in higher order transverse modes that can have negative side-effects for the laser. For example, different modes have different effective refractive indices, resulting in

different group velocities and affecting the generation of ultra-short pulses.²⁰ Importantly, for this work, higher order transverse modes will results in an uneven power distribution over the cavity and an multi-mode far-field.²⁰ This will, in turn, result in a large spot size when focused and, hence, a reduced power density when compared to the fundamental mode. These higher order modes, then, are detrimental for the observation of THz nonlinear phenomena.

Previous work on transverse mode control has been applied to metal-metal THz QCLs using doped or thin metallic (a few nanometers) ridge side-absorbers that are placed on the extremity of the ridge and along the entirety of the laser cavity.^{20,21} These permit to increase the THz losses on higher order modes without effecting the fundamental mode, resulting in laser action only on the latter. However, as this approach has only been applied to metal-metal waveguides, the resulting output power densities remain relatively low. Other methods to control the modal profile include structuring of the top metal of metal-metal waveguides²² or metasurfaces²³ for high power surface emission. Here, we demonstrate single transverse mode operation from single plasmon THz QCLs with >1 W peak output powers using thin nickel side-absorbers. This permits to increase the losses on higher order modes with little effect on the emitted peak powers and, therefore, enhancing the power density. Although THz nonlinear interactions have been investigated using THz QCLs through upconversion and downconversion,^{24–26} this has been based on the inherent QCL nonlinearities within a QCL cavity where the power density is high. The work here opens interesting perspectives for investigating THz nonlinearities using these compact laser systems as external pump sources.

Two-dimensional electromagnetic simulations (COMSOL Multiphysics) were used to illustrate the impact of lossy side-absorbers on THz QCLs structures and to determine the threshold gain. The geometry investigated is shown in Figs. 1(a) and 1(b). The ridge thickness and width here were 25 and 440 μ m, respectively. A 5 nm thick nickel side-absorber was introduced along the entire length of the two edges of the ridge with various widths in order to increase the difference in losses between the fundamental and higher order transverse modes, permitting to suppress laser action on the higher-order competing modes. The Ni layer was modeled using its complex refractive indices. (Other thin lossy metals such as Pt could also be used.) The upper gold contact layer was 150 nm thick. The lower 700 nm heavily Si-doped $(2 \times 10^{18} \text{ cm}^{-3})$ GaAs contact layer lies between the active region and substrate (thickness \sim 180 μ m). The upper doped layer is Si-doped to $5 \times 10^{18} \, \text{cm}^{-3}$ and a thickness of 70 nm. Frequencydependent simulations were performed in order to adapt them to broadband emission of THz QCLs. Figure 1(c) shows the simulated fundamental and higher order modes (TM₀₀ and TM₀₁).

The threshold gain g_{th} is defined as²

$$g_{th} = \frac{\alpha_m(\nu) + \alpha_w(\nu)}{\Gamma(\nu)},\tag{1}$$

where α_m presents the mirror losses and α_w indicates the waveguide losses of the laser cavity. Γ represents the confinement factor of the

electric field with the active region. The mirror losses α_m can be expressed as

$$\alpha_m(\nu) = -\ln(R_1 R_2)/2L,\tag{2}$$

where R_1 and R_2 are the front and back facet reflectivity, and L is the cavity length. The waveguide losses α_w can be expressed as

$$\alpha_w(\nu) = \frac{4\pi}{\lambda} k(\nu), \tag{3}$$

where *k* represents extinction coefficient of the modes propagating in the waveguide. The confinement factor Γ can be defined as the ratio of the overlap of the mode with the active region to that over the total intensity,²⁰

$$\Gamma(\nu) = \frac{\int dy dx E_y^2(y, x, \nu) \varepsilon(y, x, \nu)}{\int_{y, x = -\infty}^{\infty} dy dx E^2(y, x, \nu) \varepsilon(y, x, \nu)},$$
(4)

where $E(y, x, \nu)$ is the electric field at position (y, x) with a frequency ν , $E_y(y, x, \nu)$ is the part of the electric field that couples to the intersubband transition, and $\varepsilon(y, x, \nu)$ is the dielectric function at the frequency ν .

Here, the width of nickel side-absorbers was varied as 0 (reference), 20, 40 to $60 \,\mu\text{m}$. Figure 2(a) shows the confinement factor as a function of frequency with only small decrease in about 0.04 with the nickel width increasing from 0 to $60 \,\mu\text{m}$ (a ridge width of $420 \,\mu\text{m}$), indicating that the side-absorbers have little influence on the overlap factor. Figure 2(b) shows the much stronger impact of the different side-absorbers on the waveguide losses. When there is no nickel side-



FIG. 1. Schematic of the single plasmon THz QCLs with a (a) 3D view and (b) front view with Ni sideabsorbers to limit higher order modes. (Top doped layer is not shown.) (c) Calculated mode profiles of fundamental mode TM_{00} and first high order mode TM_{01} .

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FIG. 2. (a) Confinement factor and (b) waveguide losses of the QCL with different side-absorbers widths. Solid lines are calculations for TM₀₀ modes and dashed lines are for TM₀₁ modes.



FIG. 3. The optical microscope images of (a) the entire reference QCL (without side-absorbers) and (b) zoom showing QCLs with 60 μ m (left) wide side-absorbers and the reference (right) (437 μ m ridge width). (c) Voltage–current/current density and peak power–current/current density characteristics of THz QCLs without (red) and with 60 μ m (blue) side-absorbers. (d) Spectrum of QCLs without (red at 709 A/cm²) and with 60 μ m (blue at 671 A/cm²) side-absorbers for a 437 μ m ridge width.

Appl. Phys. Lett. **122**, 121108 (2023); doi: 10.1063/5.0142359 Published under an exclusive license by AIP Publishing absorbers, the difference of waveguide losses between TM_{00} and TM_{01} is small. However, as the width of lossy side-absorbers increases to 20, 40, and 60 μ m, the difference between the losses of TM_{00} and TM_{01} mode increases. For example, the waveguide loss of TM_{01} (>8 cm⁻¹) is more than twice that of TM_{00} (~4 cm⁻¹) with 60 μ m wide sideabsorbers. This will mean that the higher order TM_{01} mode will be suppressed, favoring laser action on the fundamental mode only. Higher order modes (>TM_{01}) have higher losses and will, therefore, be suppressed. (Since the QCLs discussed here have the same long cavity length and processed from the same material, the mirror losses are low and similar between the modes.^{28,29})

The THz QCL investigated is based on a hybrid active region (Bound-To-Continuum-Resonant-Phonon)³⁰ operating at \sim 3.2 THz, with a 25 μ m thick active region (\sim 190 periods). The THz QCLs were processed into the surface-plasmon ridge waveguide structures using photolithography and wet chemical etching. A 5 nm thick nickel side-absorber was introduced along the entire length of the two edges of the ridge with various widths (20, 40, and 60 μ m). There was an overlap of $3 \mu m$ between the nickel side-absorber and the upper gold contact layer, which was 150 nm thick. Two set of ridges with widths of 399 and 437 μ m were formed. The 700 nm heavily Si-doped $(2 \times 10^{18} \text{ cm}^{-3})$ GaAs contact layer was contacted with annealed AuGeNi side contacts. The substrate was thinned to \sim 180 μ m by wet chemical etching to improve heat dissipation. The devices were also cleaved into 3 mm long cavities, wire bonded, and indium-soldered to copper submounts for measurement [Fig. 3(a)]. Figure 3(b) shows the optical microscope images of THz QCLs (437 µm ridge width) with and without side-absorbers, where the nickel side-absorbers are visible in the former.

The THz QCLs were characterized in a pulsed mode, with a repetition rate of 10 kHz and a duty cycle of 2%, electrically gated by a 167 Hz square-wave for THz detection, in a liquid-helium continuousflow cryostat (temperature \sim 10 K) equipped with 3 mm-thick poly-4methylpentene (TPX) windows. The radiation was collected and focused from a single facet with two plastic Zeonex lenses (f = 50 mm). The power was measured using an absolute THz power meter (Thomas Keating Ltd.) directly in front of the cryostat window. Figure 3(c) shows the voltage-current/current density and peak power-current/current density characteristics of THz QCL reference and with $60 \,\mu\text{m}$ side-absorbers (a ridge width of $437 \,\mu\text{m}$). Similar results were found for the other side absorbers. The peak power for the device without the side-absorber was 1.45 W, with a small reduction (to 1.23 W) observed when the side-absorbers were incorporated. Figure 3(d) shows the frequency spectrum of the QCLs, showing a central frequency of emission of 3.2 THz. The side-absorber shows a smaller spectral bandwidth, possibly a result of the suppression of the higher order modes (see below). A similar spectrum is obtained for the thinner ridge.

To categorically show that higher modes are suppressed leading to higher power densities, we investigated the THz focused beam pattern of the realized QCLs. The focused beam was characterized using a THz camera (SwissTHz, model S2X) and two 50 mm focusing length lenses placed between the cryostat and THz camera. As can be observed from Fig. 4(a) for the 437 μ m ridge width, the reference sample (no side-absorbers) shows two focused spots, corresponding to laser action on a higher order mode. However, as the width of the side-absorbers is increased to 60 μ m, a single focused spot can be realized. The cut profiles in the "x" direction (parallel to the QCL ridge surface) at the peak amplitude of the QCL intensity with the different side-absorber widths are shown in Fig. 4(c). Here, it is shown that the beam spot width decreases with increasing width of side-absorbers from 0, 20, 40 to 60 μ m, with a single lobe appearing for the widest



FIG. 4. Focused beam 3D view profiles from 437 μ m wide QCLs (a) without and (b) with 60 μ m nickel side-absorber. (c) Cut profile in x (parallel to QCL ridge surface) at the peak intensity of the QCL beam with the different side-absorber widths (offset for clarity).

Appl. Phys. Lett. **122**, 121108 (2023); doi: 10.1063/5.0142359 Published under an exclusive license by AIP Publishing side-absorber. (The full width at half maximum in the "y" direction was 350, 350, 325, and 250 μ m, respectively.) A similar behavior was observed for the THz QCLs with 399 μ m ridge width. The experimental results clearly show that the higher order modes are suppressed via the addition of nickel side-absorbers.

From the acquired spot profiles and the measured peak powers, the THz power densities can be obtained. The spot profiles were fitted with a Gaussian curve (single Gaussian for the 60 μ m side absorber QCL, double Gaussian for the other samples) to determine the spot area. This was performed for the two sets of ridges (399 and 437 µm ridge). Figure 5 summarizes all samples and shows that the power density increases from 0.63 to $1.07 \,\mathrm{kW/cm^2}$ as the nickel side-absorber width is increased from 0 to 60 μ m for ridges of 399 μ m width. For the QCL ridges of 437 μ m width, the power density increases from 0.995 to 1.8 kW/cm² illustrating that the power density can be significantly enhanced with the correct nickel side-absorbers. The corresponding electric field of the highest power is determined to be 1.17 kV/cm [from $P = E^2/(2Z_0)$, where P is the power density, E is the peak electric field, and Z_0 is the impedance of free space (377 Ω)]. (Further increase in the side-absorber width is not expected to increase the power density owing to increased losses and reduced overlap.) For comparison, although THz pulsed systems based on amplified femtosecond pulses can reach higher peak power densities, this is over a broad spectral distribution and centered typically around 1 THz.

In this work, we have shown that high power densities can be realized from single plasmon THz QCLs, limiting the effect of high order modes despite the use of very wide laser ridges. This was achieved using lossy nickel side-absorbers that increase the losses of higher order transverse modes without affecting the fundamental mode. A THz camera was used to show control of the THz spot form and dimensions. The application of these side-absorbers permits the power density to be almost doubled when compared to the case without side-absorbers, reaching $1.8 \, \text{kW/cm}^2$, corresponding to electric fields $\sim 1.17 \, \text{kV/cm}$. Further enhancements can be achieved through HR coatings on the back facet, wider ridges, smaller f# optics, as well as combining the THz QCL emission with metasurfaces or resonators.



FIG. 5. QCL power density as a function of nickel side-absorber width for 399 μm (blue) and 437 μm (red) wide ridges. All devices were 3 mm long.

The latter approach has shown that THz electric fields can be enhanced by more than an order of magnitude.^{31,32} This could be used to realize fields exceeding tens of kV/cm that compares favorably with the recent work using FEL to study harmonic generation in graphene, which required a field of ~10 kV/cm for observation of the third harmonic.¹ This resonator approach could also be combined with THz pulse generation through QCL mode locking for further enhancements of the peak power densities and ultrafast exitations.^{33,34} This work, therefore, will be particularly important in the application of THz QCLs as a compact pump source for the study of nonlinear THz physical phenomena where high power densities are vital.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

Author Contributions

C. Song and M. Salih contributed equally to this paper.

Chao Song: Conceptualization (equal); Data curation (equal); Formal analysis (equal); Investigation (equal); Methodology (equal); Writing – original draft (equal); Writing – review & editing (equal). Mohammed Salih: Investigation (equal); Methodology (equal); Resources (equal); Validation (equal); Writing – original draft (equal); Writing – review & editing (equal). Lianhe Li: Investigation (equal); Methodology (equal); Resources (equal). Juliette Mangeney: Investigation (equal); Methodology (equal). Jerome Tignon: Investigation (equal); Methodology (equal). A. Giles Davies: Investigation (equal); Methodology (equal); Resources (equal). Edmund H. Linfield: Investigation (equal); Methodology (equal); Resources (equal). Sukhdeep S. Dhillon: Conceptualization (equal); Funding acquisition (equal); Investigation (equal); Methodology (equal); Project administration (equal); Supervision (equal); Validation (equal); Writing – original draft (equal); Writing – review & editing (equal).

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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