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1 **Three-dimensional Simulation of a Secondary Circular Settling Tank: Flow Pattern and**  
2 **Sedimentation Process**

3  
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9 **Abstract**

10 A secondary circular settling tank (SCST) with low hydraulic load was numerically analyzed for flow patterns,  
11 velocity field, turbulence interactions and sedimentation process. A transient, three-dimensional model with  
12 three phases was employed, clean water was considered as a continuous phase and the sludge as a dispersed  
13 phase, an air layer under atmospheric conditions was considered above the surface of the water to help establish  
14 an opening boundary condition at the top of the tank. ~~The governing equations are solved~~Regarding the model  
15 ~~solution, using~~ the software ~~used was the~~ Ansys CFX commercial code. For the model validation, 2D and 3D  
16 approaches were analyzed and simulated flow patterns were compared with experimental data from the  
17 literature and then 3D approach was preferred for SCST simulation. The model was used to evaluate the flow  
18 in a pilot plant. The amount and location of sludge present in the SCST at the time was measured from its  
19 volumetric fraction. Higher velocity and turbulent kinetic energy generated by the inlet flow stream were  
20 observed at the bottom of the tank led to re-suspension of sludge particles. With the sludge outlet opened, after  
21 30 minutes of simulation there was stabilization of the sludge and improvement in the settling process. With  
22 the sludge outlet closed, after 30 minutes of simulation there was an increase of approximately 1% of sludge  
23 concentrated at the bottom of the decanter. The results provided detailed insight into the hydrodynamic flow  
24 within the SCST and they will serve as a first step for further improvements in process efficiency.

25  
26 **Keywords:** Secondary circular settling tank, Sedimentation, Computational fluid dynamics, Multiphase flow,  
27 Wastewater treatment.

28

## 29 Introduction

30 In the treatment of domestic and industrial wastewater it is essential to separate the treated wastewater  
31 from the biological sludge. The secondary settling tank (SST) is widely employed in the separation of solid  
32 and liquid phases in activated sludge processes treating domestic and industrial wastewater, such separation  
33 occurs by gravitational sedimentation (EKAMA *et al.*, 1997). There are many important factors that directly  
34 affect the design of SST, such as local climatic conditions, variations in plant operating conditions,  
35 sedimentation velocity, geometric tank configurations and wastewater characteristics, such as density and  
36 viscosity (Clercq 2003, Bajcar, Steinman *et al.* 2011, Patziger 2016).

37 The flow inside a SST is quite complex, it consists of a variety of particles, with different sizes, shapes  
38 and densities, all under the effects of gravity, currents and turbulence, which may impair the deposition of  
39 particles in settling tanks (Al-Sammaraee, Chan *et al.* 2009). Further, complete understanding of the  
40 sedimentation process is dependent on tank geometry, operational parameters, physical, chemical and  
41 biological characteristics of the sludge. Hence, there is still great difficulty in completely modeling such  
42 sedimentation process. The existing computational ~~methodology~~~~technology~~ only allows to work with a number  
43 of simplifications (Gong, Xanthos *et al.* 2011, Patziger 2016, Samstag, Ducoste *et al.* 2016).

44 The suspended solid particles in the influent settle to its bottom, separating the sludge from the  
45 remaining fluid, i.e., a mixture of solid particles in liquid establishing a multiphase liquid-solid flow. So in  
46 sedimentation process, a clear fluid will emerge at the top, while, at the bottom, the particles will slow down  
47 and form a sludge layer leaving the middle as a constant settling zone. Therefore, low concentration of  
48 suspended solids on the effluent leaving the SST can be an indicative of sedimentation efficiency.

49 The design of SCST can be done using some reference manual (WEF, 2005) however there are some  
50 assumptions that need to be considered. To ~~overcome~~~~overcame~~ ~~some of this~~ ~~these~~ assumptions ~~we have used~~  
51 ~~it has been used the simulation in~~ Computational fluid dynamics (CFD), which has been shown to be a very  
52 useful tool in the prediction of multiphase flow patterns and process efficiency of a large number of water  
53 treatment processes (Wu 2010, Guo, Zhou *et al.* 2013, Li Lei and Ni 2014), e.g., in chemical and biological  
54 processes involving suspended growth nutrient removal and anaerobic digestion among others (Samstag,  
55 Ducoste *et al.* 2016). The separation process in settling tanks is an example of multiphase liquid-solid flow,  
56 where the suspended solids represent the dispersed phase in a continuous phase. Sometimes dispersed-phase  
57 volume fraction is designated as concentration (Crowe 2005).

58 When discussing the validation of CFD predictions, there has been a lack of experiments involving  
59 solid particles to corroborate with simulations (Lakghomi, Lawryshyn et al. 2015). Some relevant  
60 computational work on the efficiency of (SCST) has been published in the literature; however, since the settling  
61 process involves more than one phase, with great variability in the physical properties of the sludge, the  
62 complete modeling of the process is still quite difficult (Goula, Kostoglou et al. 2008, Al-Sammaraee, Chan  
63 et al. 2009). Most of the published numerical studies consider simplifications of the process with good  
64 approximations. Clercq (2003) covered several aspects regarding the modeling of a circular settler, using a  
65 two-dimensional model in a single phase, however, quite comprehensive, which considered the concentration  
66 of sludge as a passive scalar. It also considers the effects of the decanter bottom scraper (solids removal  
67 mechanism), changes in sludge rheology and sedimentation velocity. The passage of the scraper forced the  
68 lower flow discharge, neutralizing the gravitational force, after passage of the scraper only a certain  
69 concentration of dispersed solids in the main volume was observed, not a thick layer at the bottom of the  
70 sedimentation tank. The numerical work obtained good agreement when compared with the concentration of  
71 suspended solids obtained from experimental measurements.

72 The performance and the central feed capacity in a SST are very sensitive ~~sensible~~ to the inflow  
73 intensity, due to the limited tank volume in where the kinetic energy will be dissipated. Therefore, changes in  
74 the tanks geometry or the addition of parts like baffles aim to dissipate this energy, reducing the turbulence in  
75 the fluid and avoiding particles re-suspension. Around the SST inflow entrance, turbulent currents cause  
76 variations in sludge concentration, which influence the depth of the thickening zone; hence, the efficiency of  
77 the sedimentation process (Bürger, Diehl et al. 2011). Patziger, Kainz et al. (2012), noted, when working with  
78 a single-phase two-dimensional model, non-Newtonian fluid and with a transport equation for suspended solids  
79 concentration, ~~the~~ low hydraulic load resulted in low turbulence level in the SST, providing better sludge  
80 settling and thickening as well as positively increasing sludge concentration.

81 Using a two dimensional (2D) model, Patziger (2016), ~~also with 2D model~~ studied two distinct sludge  
82 inflow configurations to determine changes in flow pattern and suspended solid concentration. It has been  
83 shown that by reducing the baffle height, there was a decrease in the high velocity uplift components (fluid  
84 velocity greater than sedimentation velocity). In this study a less extensive region of turbulence characterized  
85 by high values of turbulent kinetic energy is observed. This resulted in better sedimentation and thickening

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86 conditions therefore a more dense sludge layer at the bottom and characterizing cleaner water at the upper  
87 water outlet.

88 Although 2D models result in optimum results, certain three-dimensional features such as rotational  
89 structures in the flow cannot be captured by two-dimensional models (Kleine and Reddy 2006). In the literature  
90 there is a lack of numerical simulation of SCST using the three-dimensional approach. Thus, at the beginning  
91 of the present work, a comparison between two-dimensional and three-dimensional models for flow in an  
92 SCST is made.

93 In terms of validation and reliability of the results, qualitatively comparing the simulated results with  
94 similar case studies is already an indication that the results are physically coherent (Kleine and Reddy 2006);  
95 it is a way to guarantee the physical validation of the simulation. The validation of the mathematical model is  
96 a fundamental step of the numerical simulation. Thus, data from a literature work with images of the sludge  
97 flow pattern inside a circular decanter were used for the validation of the model presented in this work. Then,  
98 the Element Based Finite Volume Method (EbFVM) was used to visualize the flow pattern and quantify  
99 variables such as sludge velocity and concentration and consequently being able to improve the design of the  
100 SCST considered. In this work, the flow in a SCST, with low hydraulic load was studied from numerical CFD  
101 simulation with a multiphase, transient and three-dimensional model.

102

## 103 2. Methodology

### 104 2.1 Mathematical Model

105 We ~~use proposed~~ the mathematical model based on the Navier-Stokes equation of conservation of  
106 mass ~~(1)(1)~~, of the amount of movement weighted by the Reynolds mean (RANS) ~~(2)(2)~~ with the  $k-\omega$  Shear  
107 Stress Transport model of turbulence (eq. ~~(3)(3)~~ ~~(4)(4)~~) was used.

#### 108 2.2.1 Multiphase flow

109 The multiphase homogeneous model was employed for the simulations. In homogeneous multiphase  
110 flow, a common flow field, such as velocity and turbulence, is shared by all phases. The fluid is composed of  
111 three phases: air, water and sludge:

$$112 \frac{\partial}{\partial t}(\tilde{\rho}_\alpha) + \nabla \cdot (\tilde{\rho}_\alpha U_\alpha) = 0 \quad (1)$$

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$$\frac{\partial}{\partial t}(\tilde{\rho}_\alpha U_\alpha) + \nabla \cdot (\tilde{\rho}_\alpha U_\alpha \otimes U_\alpha) = \nabla \cdot (r_\alpha \bar{\mathbf{T}}_\alpha) + \tilde{\rho}_\alpha \mathbf{g} + \mathbf{M}_\alpha + \Gamma_\alpha U_\alpha, \quad (2)$$

where  $r_\alpha$  is the volumetric fraction of the  $\alpha$  phase (water, sludge and air),  $\tilde{\rho}_\alpha = r_\alpha \rho_\alpha$  is the effective density for the  $\alpha$ -phase  $U_\alpha$  is the velocity vector and  $\bar{\mathbf{T}}_\alpha = -p\bar{\mathbf{I}} + 2\mu\bar{\mathbf{D}}$  here  $p$  is the pressure,  $\mu$  is the dynamic viscosity and  $\bar{\mathbf{D}}$  is the tensor strain rate,  $\bar{\mathbf{D}} = (\nabla U_\alpha + \nabla U_\alpha^T)$ ,  $\mathbf{M}_\alpha$  is the interfacial force per unit volume and  $\Gamma_\alpha$  is the mass transfer rate per unit volume.

## 2.2.2 Turbulence

The Reynolds number at the tank inlet is  $Re = 3000$ , which characterizes a turbulent flow. The  $k$ - $\omega$  based Shear-Stress-Transport (SST) model (Menter 1994) was employed in this work to determine the influence of turbulence in the settling processes. The model works by solving a turbulence frequency-based model  $k$ - $\omega$  at the wall and  $k$ - $\varepsilon$  in the bulk of flow. The SST model introduce three new variables into the system of equations: turbulent kinetic energy  $k$  (per unit mass), the dissipation (per unit mass) of the kinetic energy  $\varepsilon$  and the turbulent frequency,  $\omega$ . The turbulent viscosity is linked to the turbulent kinetic energy and turbulent frequency in this way:  $\mu_t = \rho_\alpha k / \omega$ . A blending function ensures a smooth transition between the two models.

In equations (3) and (4), the stress tensor is computed from the eddy-viscosity concept,  $P_k$ 's are the production rate of turbulence, the model constants are given by:  $\beta' = 0.09$ ,  $\gamma = 5/9$ ,  $\beta = 0.075$ ,  $\sigma_k = \sigma_\omega = 2.0$  (Wilcox 1986). The  $k$ - $\omega$  model accounts for the transport of the turbulent shear stress and gives highly accurate predictions of the onset and the amount of flow separation under adverse pressure gradients by the inclusion of transport effects into the formulation of the eddy-viscosity resulting in a major improvement, regarding flow separation predictions. The superior performance of this model has been demonstrated in a large number of validation studies presented in (Bardina, Huang et al. 1997).

$$\frac{\partial}{\partial t}(\tilde{\rho}_\alpha k_\alpha) + \nabla \cdot (\tilde{\rho}_\alpha U_\alpha k_\alpha) = \nabla \cdot \left( r_\alpha \left( \mu_\alpha + \frac{\mu_{t_\alpha}}{\sigma_k} \right) \nabla k_\alpha \right) + r_\alpha (P_{k_\alpha} - \beta' \rho_\alpha k_\alpha \omega_\alpha) + P_{k_{\beta\alpha}} \quad (3)$$

$$\frac{\partial}{\partial t}(\tilde{\rho}_\alpha \omega_\alpha) + \nabla \cdot (\tilde{\rho}_\alpha U_\alpha \omega_\alpha) = \nabla \cdot \left( r_\alpha \left( \mu_\alpha + \frac{\mu_{t_\alpha}}{\sigma_\omega} \right) \nabla \omega_\alpha \right) + \frac{r_\alpha}{k_\alpha} (\gamma \omega_\alpha P_k - \beta \rho_\alpha k_\alpha \omega_\alpha^2) + P_{\omega\beta}, \quad (4)$$

## 2.2.3 Terminal velocity of the particle

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136 The separation of the solid particles from the fluid in the sedimentation processes occurs by gravity  
137 acting on the particles, which are a force that acts downwards, also, two other forces acts on the particles: the  
138 buoyancy force acting upwards and the drag force in the direction of the relative velocity between the fluid  
139 and the particle.

140 If the mixture velocity is greater than the terminal velocity of the particle, the re-suspension of the  
141 particles will occur. The particles will decay with speed  $v_t$  (Eq. (5)) and particle drop time  $t_q$  is given as a  
142 function of the terminal velocity by:  $t_q = H/v_t$ , where  $H$  is the height of the tank, then, when a particle of size  $dp$   
143 falls through a fluid, the free fall velocity can be estimated through the expression (Tchobanoglous, Burton et  
144 al. 2003):

$$145 \quad v_t = \left( \frac{4d_p g (\rho_p - \rho)}{3\rho C_D} \right)^{1/2} \quad (5)$$

146 where  $\rho_p$  is the density of the particle,  $\rho$  is the density of the water and  $C_D$  is the drag coefficient, which, for  
147 spherical particles in turbulent regions, is  $C_D = 0.44$ . In this work,  $d_p = 1.0 \times 10^{-4}$  m,  $\rho_p = 1400.0$  kg m<sup>-3</sup> and  $\rho = 997.0$   
148 kg m<sup>-3</sup>.

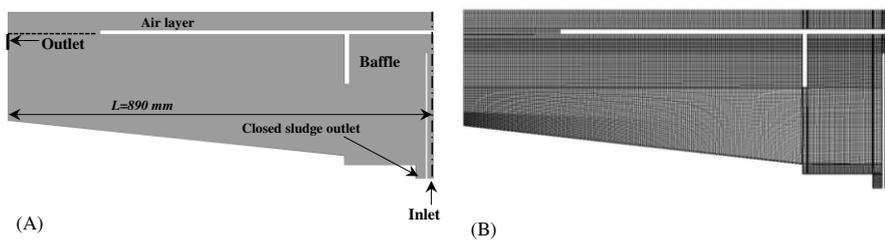
## 149 2.2 Methodology for Model Validation

150 Initially two approaches were considered: two-dimensional and three-dimensional simulations were  
151 carried out with the purpose of verifying which approach would give better results when compared with  
152 experimental results. The two-dimensional approach computation time was approximately 48 hours and in the  
153 three-dimensional approach, this was approximately 200 hours.

154 Digital images of the experimental flow on SCST from the study of BAJCAR *et al.* (2011) were used.  
155 The images capture the whole flow field ~~on~~ in the space at once, which provides the ability to measure  
156 instantaneous velocities and analyze eventual spatial changes in the flow field through time. With the  
157 parameters and our geometry, a 2-D and 3-D mesh were created, as shown in Figure 1 and 2 respectively. The  
158 model considered has a length  $L = 890$  mm, which represent the radius of an analogous SCST, as can be seeing  
159 on the 3-D geometry in Figure 2. For the simulations, a three phase flow was considered: water, sludge and an  
160 air layer at the top of the tank as indicated in Figure 1. For the initialization of the simulations, the tank was  
161 filled with water. The volumetric flow rate in the system was 6.0 L min<sup>-1</sup> with the sludge outlet permanently

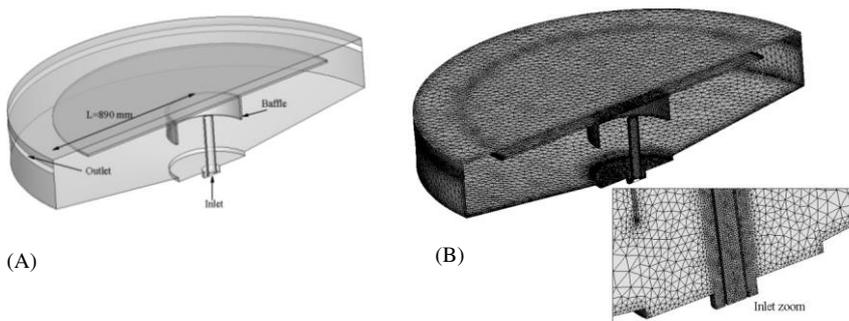
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162 closed. According to Bajcar, Steinman et al. (2011), a material called "sludge" was created in the Ansys CFX  
 163 software. Sludge, was considered with particle of 0.25 mm diameter (particle size large enough so that it is  
 164 possible to clearly observe changes in suspension concentration after time intervals selected). With a density  
 165 of  $1450 \text{ kg m}^{-3}$  and a viscosity of  $0.8 \text{ kg m}^{-1} \text{ s}^{-1}$  this material was considered to be a dispersed fluid, with  
 166 particles of diameter 0.25 mm, in water. The mesh with hexahedral elements containing 219829 elements and  
 167 144234 nodes was made in software ICEM-CFD 14.5.



168  
 169 **Figure 1: Two-dimensional geometry according to Bajcar et al. (2011) (A) with the entrance of sludge from the**  
 170 **bottom (inlet), the outlet of water from the top tank (outlet) and the baffle at the top at the entrance; And (B) the**  
 171 **hexahedral mesh employed.**

172 For the three-dimensional simulation a circular tank was considered. The 2-D geometry of Figure 1  
 173 (A) was rotated 180 degrees around of vertical central symmetry axis. A mesh with tetrahedral elements was  
 174 generated, as in Figure 2 (B).



175 **Figure 2: Three-dimensional geometry according to Bajcar et al. (2011) (A) with the entrance of sludge from the**  
 176 **bottom (inlet), the outlet of water from the top tank (outlet) and the baffle at the top at the entrance; and (B) the**  
 177 **Tetrahedral mesh employed.**

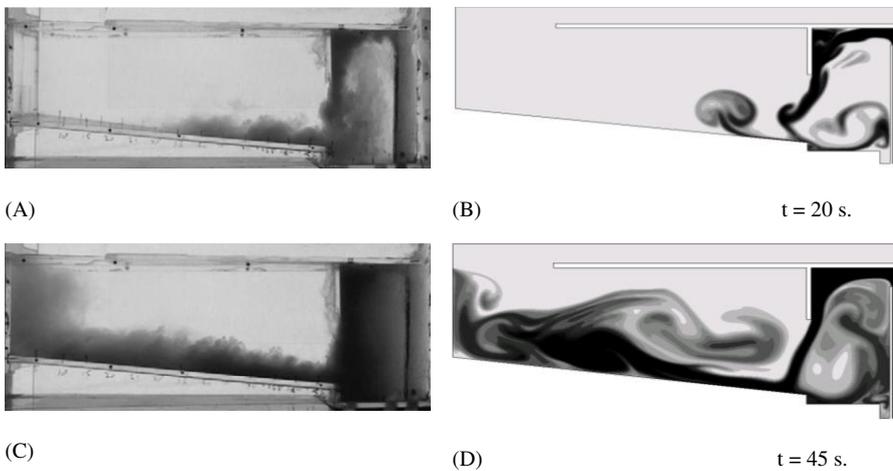
178 **2.2.1 Boundary Conditions**

179 The boundary conditions at the inlet consists of a mass flow rate of  $6.0 \text{ L min}^{-1}$  and a sludge volumetric  
180 fraction of 1.5%. At the water exit, the flow was considered as opening boundary condition, but with zero  
181 sludge volume fraction. At the top of the tank it was considered a 0.05m layer with only air, with an opening  
182 boundary condition. This boundary condition can be used at boundaries in which the flow occurs in or out of  
183 the domain. The remaining boundaries of the domain were considered as walls with non-slip condition.

184 **2.2.2 Validation Test: Two-dimensional Simulation**

185 The comparisons of the results of the two-dimensional simulations obtained in this work, with the one  
186 from the literature, can be seen in Figure 3 and Figure 4. There is **qualitative agreement** between the flow  
187 patterns. In Figure 3 (B) and (D), as well as in (A) and (C), there is a significant density current at the bottom  
188 of the inner chamber. But in the **images-flow field** obtained with computational simulation in this work, **the**  
189 **flow presents shows** larger areas of fluid recirculation at the bottom of the tank as shown in Figure 3 (B), (D).  
190 In the experimental work the flow is more regular than when compared to the computational simulation. Such  
191 a difference may be due to the three-dimensional nature of the flow.

Commented [AK2]: If quantitative, please show graphs



192 **Figure 3: Sequence of images of suspension flow obtained from Bajcar et al. (2011) (A) e (C); Contour maps colored**  
193 **by the volumetric fraction of sludge, obtained in this work with the two-dimensional approach (B) e (D).**

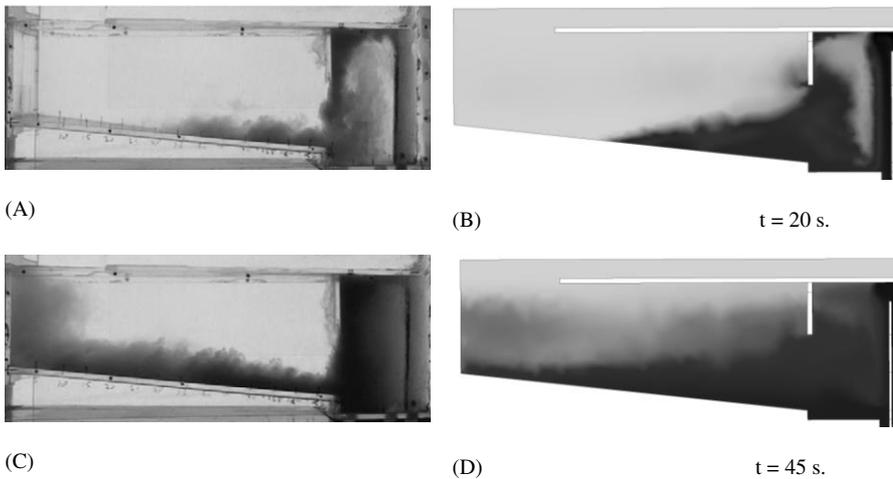
194

195 **2.2.2 Validation Test: Three-dimensional Simulation**

196 The mathematical model and ~~boundary contour~~ conditions described above were employed to obtain  
 197 3-D results with the mesh shown in Figure 2 (B). The comparative results with the same experimental images  
 198 of Figure 3 (A) and (C) are done with the results of the 3D simulation in Figure 4, in which a central cutting  
 199 plane to the geometry was colored with the variable volumetric fraction of sludge in the same color scale  
 200 described in Bajcar et al. (2011). Comparing the images (A) and (B) of Figure 4, it is observed that in the first  
 201 20s of simulation, there are some differences in the amount of sludge present at the bottom of the settler, but a  
 202 good agreement was obtained on the flow pattern. At 45 s, a larger sludge spread is observed in the region  
 203 below the baffle Figure 4 (D) when compared to Figure 4 (C). Bajcar et al. (2011) ~~measured got that~~ the fluid  
 204 flow along the bottom tank ~~and obtained a flow have~~ velocity of about 4 cm/s. ~~and Similarly along~~ the outer  
 205 wall of the settling tank (left side of images in Figure 4(C)) ~~and reaches it with the he measured a~~ velocity of  
 206 approx. 2.5 cm s<sup>-1</sup>. In ~~our this~~ study, the velocity at the bottom tank was about 3.7 cm s<sup>-1</sup> and the outer wall of  
 207 the settling tank (left side of images in Figure 4(D)) the velocity was about 1.7cm s<sup>-1</sup>.

Commented [AK3]: Do you mean boundary conditions??

Commented [AK4]: Clarify good in terms of numbers. How do you know it is good, are the predictions within few percent of the measurements?



208 **Figure 4: Comparative images between the concentration of sludge in the experimental work of Bajcar**  
 209 **et al. (2011) at approximately t = 20s and t = 45s of operation (A) and (C) respectively; and the volume**  
 210 **fraction of sludge at t = 20s and t = 45s of 3D simulation, (B) and (D), respectively.**

211  
 212 Both approaches 2D and 3D showed agreement with the chosen experimental case. However, when  
 213 considering the 3D domain, the fluid waves have more space to dissipate, so they are expected to be lower and  
 214 last for less time, thus generating smaller oscillations with less intensity. Thus, even with high computational

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215 time, the 3D case is more adequate for the sludge distribution inside the settling tank and was chosen to  
216 simulate a SCST pilot plant with similar operating conditions.

## 217 **2.3 Simulation of the flow pattern for a new SCST**

### 218 **2.3.1 Geometry**

219 The new SCST tank has 2m of height and 1m of diameter and total volume 1.57m<sup>3</sup>. The mass transport,  
220 as well as the regions of the computational domain of water, sludge inlet, sludge outlet and clean water outlet  
221 is indicated in Figure 5 (A), where Q and QRS are inflow rate and return sludge flow rate in m<sup>3</sup>s<sup>-1</sup>  
222 respectively. Views of the project detail plane as well as the dimensions of the tank under study are shown in  
223 Figure 6. For the CFD simulations, from the detailed design (Figure 6 (A)) some geometric simplifications  
224 must be considered (Figure 6 (B)): the internal scrapers responsible for scraping the sludge from the bottom of  
225 the tank were removed, as well as parts of the fixation of inlet pipe and baffle.

226

### 227 **2.3.2 Mesh independence**

228 In order to test the independence of the mesh employed, four meshes with increasing refinement on  
229 the computational domain were considered. Simulations preliminaries considering steady state regime with  
230 just clean water on the tank were made for each mesh using the boundary conditions of Table 2. Meshes with  
231 tetrahedral elements and with different densities were tested. For each mesh, by setting the inlet flow rate, the  
232 outlet velocity was measured and compared to the measured outlet velocity experimentally. The values  
233 obtained for each mesh can be compared from Table 1.

234 From the mesh number 02 onwards, the velocity fields practically did not vary significantly present  
235 modifications when compared with the same fields obtained with the meshes 03 and 04. And the velocity  
236 values measured at the outlet did not suffer variations as well, as shown in Table 1. Thus, it was opted for to  
237 use mesh 02 for all the multiphase transient simulation containing water and sludge.

238

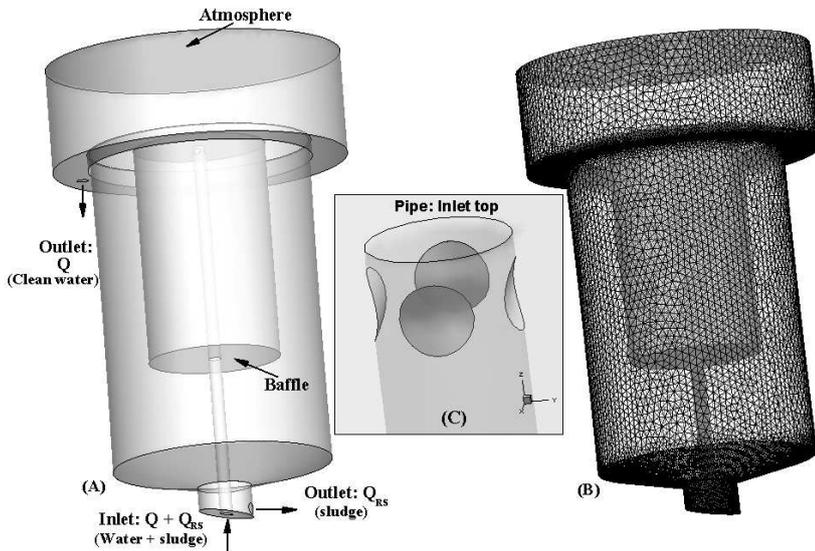
239 **Table 1: Calculated and simulated velocity values at the clean water outlet (tank top) for the four test**  
240 **meshes.**

Top outlet velocity [m/s]		Number of elements (million)	Theoretical	Simulation	Error %
	Mesh 01	1.50	0,0103	0,0111	7.7
	Mesh 02	1.87		0,0110	6.7
	Mesh 03	5.39		0,0110	6.7
	Mesh 04	7.16		0,0110	6.7

241

242 With that information, the mesh employed on the considered geometry consists of approximately 1.87

243 million tetrahedral elements and the distribution of such elements can be seen in Figure 5 (B).



244

245 **Figure 5: Three-dimensional geometry with the inlet and outlet regions (A); And tetrahedron mesh over**  
 246 **the computational domain (B); Zoom of holes at inlet pipe top (C).**

247

### 248 2.3.3 Boundary Conditions

249 An “inlet” contour boundary condition was employed at the sludge inlet, under a flow rate of 3 m<sup>3</sup> day<sup>-1</sup>.  
 250 The outlets boundary conditions "opening" was specified in the outlet of clean water and in the lower sludge  
 251 outlet, in those boundaries of the computational domain the “Bulk mass flow rate” option was established. The

Commented [AK6]: ??

252 specific values and their respective units used in the simulation are shown in Table 2. The recirculation flow  
253 rate was considered constant.

254 **Table 2: Values specified in the boundary conditions.**

Inlet flow rate [kg s <sup>-1</sup> ]	0.034
Recirculation flow rate [kg s <sup>-1</sup> ]	0.013
Turbulence at the inlet [%]	1.0
Volumetric fraction of sludge in the inlet [-]	0.1
Turbulence at the Sludge outlet [%]	1.0
Sludge outlet flow rate [kg s <sup>-1</sup> ]	0.0195
Turbulence at the sludge outlet [%]	5.0
Turbulence at the outlet of clean water [%]	1.0

255  
256 A common problem in SCST is the effluent inlet geometry, directly responsible for the increased  
257 turbulence in the system (Patziger 2016). From the use of a baffle it is possible to redirect the flow of liquid to  
258 reduce the formation of instabilities in the velocity field caused by the inlet kinetic energy and to reduce the  
259 sludge re-suspension. For the geometry studied here, the effluent enters in the tank through a central pipe with  
260 circular holes at the top (Figure 5 (C)), those four holes were set as the inlet boundary condition, also a baffle  
261 of 0.6 m in diameter by 1.0 m height was used, according to Figure 6 (B). On the walls of the baffle, as well  
262 as on the walls of the tank, boundary conditions of “no slip” were applied.

### 263 2.3.3 Numerical details

264 The tank filled with water was considered as initial condition, the initial time step for the discretization  
265 of the differential equations in time was  $\Delta t = 0.01s$  for the first 20s of simulation, from there the system  
266 remained stable with residual error down to  $10^{-5}$ , then to decrease the computational time was considered  $\Delta t =$   
267  $0.1s$  and for all variables the residual error remained below  $10^{-4}$ .

268 As for the numerical schemes employed, high resolution advection scheme was used and for transient  
269 scheme a second order Backward Euler scheme was employed.

270 ~~All the simulations were performed on a workstation with 64-bit operating system,~~  
271 ~~system with four processors running at with 2.26 GHz and 16GB of memory (RAM). and 64 bit operating~~  
272 ~~system to calculate the solution.~~

273

### 2.3.4 Initial Conditions

274

275

For the transient simulation, the SCST was filled with clean water up to 1.58m height with an air layer of 0.42m above this specified height. Such condition is given by equation (6) and indicated in Figure 6 (B):

276

$$H(z) = \begin{cases} Water_{vf} = 1, & \text{if } 0 \leq z \leq 1.58 \\ Water_{vf} = 0 & \text{if } 1.58 \leq z \leq 2.0 \end{cases} \quad (6)$$

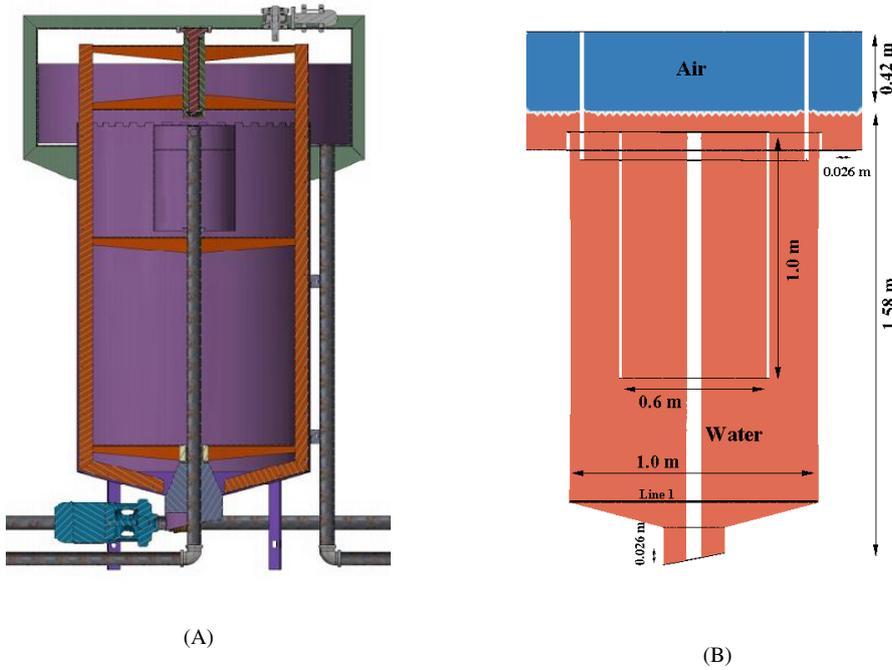
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where  $Water_{vf}$  is the volumetric fraction of water and  $z$  is the Cartesian axis in which the height of the tank is

278

located. Spatial initial condition: null pressure and null Cartesian velocity components.

279



280

281

Figure 6: Views of the central plane of settling tank; A) Detailed design of the original settling tank geometry; B)

282

CFD design of settling tank with initial condition for transient simulation and geometric dimensions.

283

284

### 3. Results and discussion

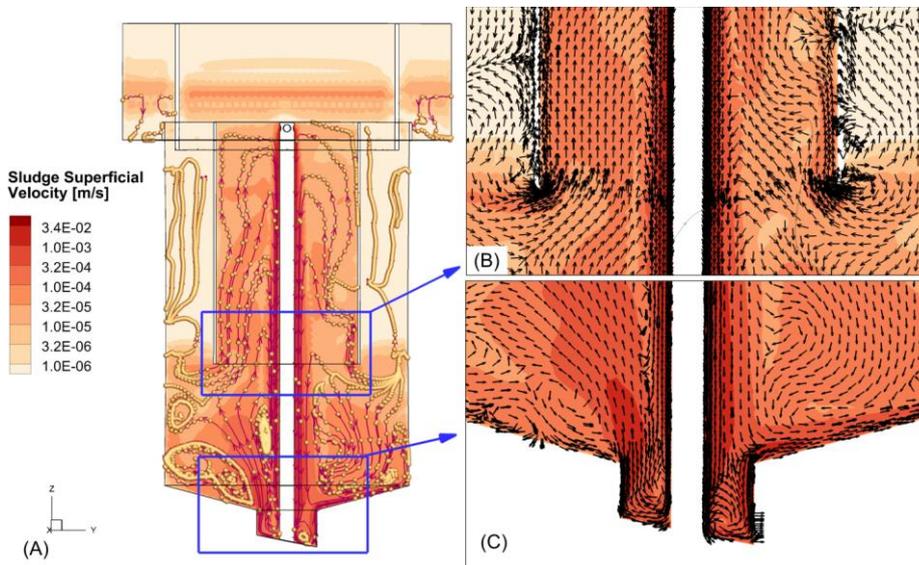
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286 **3.1 Velocity field**

287 In the homogeneous model employed in this work, the water velocity field as well as the dispersed  
288 solids velocity field is the same. However, to recover information about water velocity and sludge velocity  
289 separately, one can analyze the variable superficial velocity. The superficial velocity is important in the  
290 representation of phenomena typical of multiphase flows; it is defined as the fluid volume fraction multiplied  
291 by the fluid velocity. So, this variable is used in vector plots at multiphase flow, as we will only see a vector  
292 where a significant amount of that phase exists. A cut plane colored by the sludge superficial velocity and  
293 overlapped by your streamlines and sludge superficial velocity vectors is shown at Figure 7, it can be seen  
294 that there is a significant amount of sludge in the bottom region, higher sludge velocity at the bottom of the  
295 tank and that there is much fluid recirculation throughout the tank interior.

296 The fluid entering the tank at reaches its bottom forming areas of recirculation near the outlet of the  
297 sludge, Figure 7 (A)-(C). This fluid returns upward with sufficient velocity so that by finding the inclined  
298 bottom walls of the tank and the side walls form other small recirculation regions. Then part of the fluid is  
299 drawn back for inside the baffle, Figure 7 (B), where, on the top of the baffle, there is a fresh fluid encounter  
300 with the upward current and part of this mixture descends again around the central tube toward the bottom of  
301 the tank.

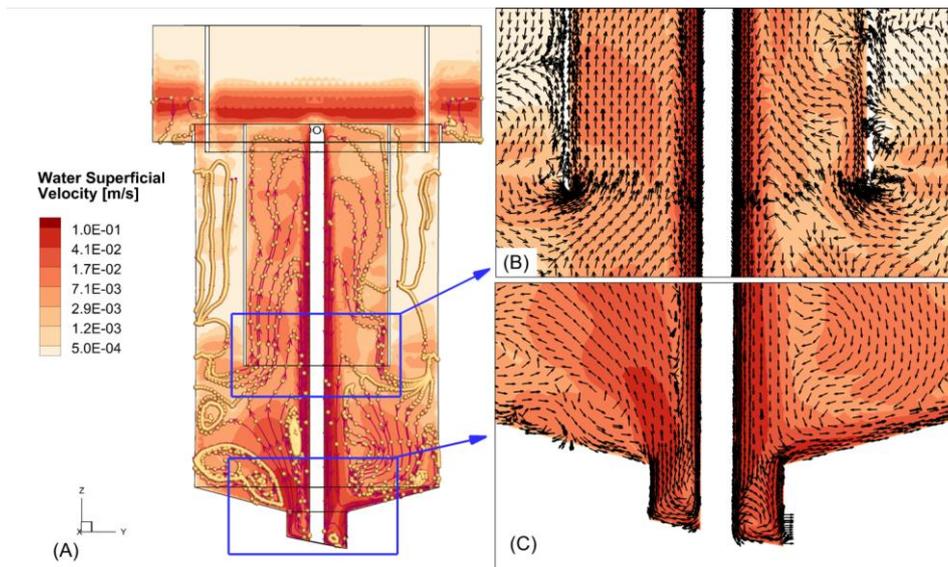


302

303

304 **Figure 7: Central cut plane colored by sludge superficial velocity overlapping with streamlines (A); (B) region of**  
 305 **the baffle outlet colored by sludge superficial velocity overlapping with the superficial velocity of sludge vectors;**  
 306 **(C) region of the tank bottom (sludge outlet) colored by superficial velocity of sludge overlapping with the**  
 307 **superficial velocity of sludge vectors.**

308  
 309 The velocity of the jet formed at the inlet from the holes at the top of the tank is high, around 0.1 m / s and  
 310 continues high around the inlet tube until it reaches the bottom, where there are small and tortuous recirculation zones.  
 311 As can be seen from figure 7 and 8, the superficial velocity of the water is greater than the superficial velocity of the  
 312 sludge by an order of magnitude. At very low velocity the fluid travels down smaller paths losing energy and the particles  
 313 settle. On the other hand, for very high velocity the particles are drawn by the continuous phase, towards the exit. The  
 314 equation (5)(5) gives an idea of the magnitude of the terminal velocity of the particle.



315  
 316  
 317 **Figure 8: Central cut plane colored by water superficial velocity with streamlines overlapping (A); (B) the region**  
 318 **of the sludge inlet colored by superficial velocity of water and vectors; (C) region of the tank bottom colored by**  
 319 **superficial velocity of water and vectors.**

320  
 321  
 322 Then, with the equation (5)(5) we got  $v_t = 0.034$  m/s. In Figure 9 it is possible to compare the  
 323 magnitude of the calculated fluid velocity  $v$ , in a few instants of time, in a sampling line, indicated in Figure 6

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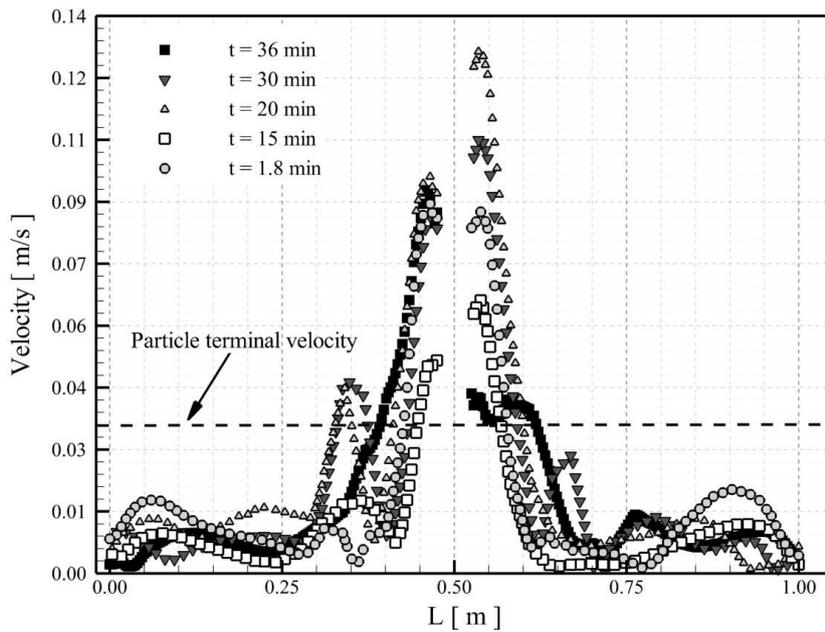
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324 (B) as line 1. The line is located horizontally, in the center, at the bottom of the tank (0.01m from the bottom).  
 325 It can be observed that at the bottom of the tank there is high fluid velocity mainly in the center around the  
 326 inlet pipe (0.12 m/s), the dotted line indicate in the graph the particle terminal velocity, which gives the  
 327 dimension of how much the terminal velocity  $v_t$  is smaller than surrounding fluid velocity. It can be stated that  
 328 the particles settled at the center and bottom of the tank will undergo re-suspension because in this region  $v >$   
 329  $v_t$ . In Figure 9 it can be observed that the velocity of the fluid in the center of the tank increases until the time  
 330  $t = 20$  min. At  $t = 30$  min and  $t = 36$  min the fluid velocity at the bottom of the tank in its central region  
 331 decreases. In the region near the walls at the bottom of the tank,  $v \leq v_t$ . This indicates that in this region,  
 332 particles are less likely to undergo re-suspension.

333  
 334



335  
 336 **Figure 9: Magnitude of the velocity variable evaluated on line 1 located at the central plane at the bottom of the**  
 337 **tank, evolution over time.**  
 338

339 The contour maps of Figure 7 show the velocity field ranging from 0 m/s to 0.034 m/s at a central  
340 plane of the geometry. The water and sludge mixture runs a distance of 1.74m from the inlet holes at the top  
341 of the tank until it reaches the bottom of the tank in the region of the sludge outlet. Thus, when it reaches the  
342 bottom and as discussed above, it can be seen that the higher velocity zones are around the central inlet pipe.  
343 Then, it can be said that inlet jet causes disturbances in the bottom of the tank. This makes its performance  
344 difficult. When the fluid recirculates, irregular velocity regions are formed, still with high speed entering the  
345 baffle. From the moment that fluid reaches the bottom of the tank, over time (30min and 36min), there is a  
346 small decrease in the velocity as in Figure 9, around the bottom of the tank there are oscillations of fluid  
347 velocity.

348  
349 In Figure 8, we also note that at a height of 0.65 m, the superficial velocity of water decreases to the  
350 order of  $5e^{-4}$  m/s in the region outside the baffle (from the region above the baffle outlet). In this region the  
351 superficial velocity of the sludge is around  $1e^{-6}$  m/s. It can be said then that in the upper part of the tank, above  
352 the baffle outlet, there is little possibility of particle re-suspension.

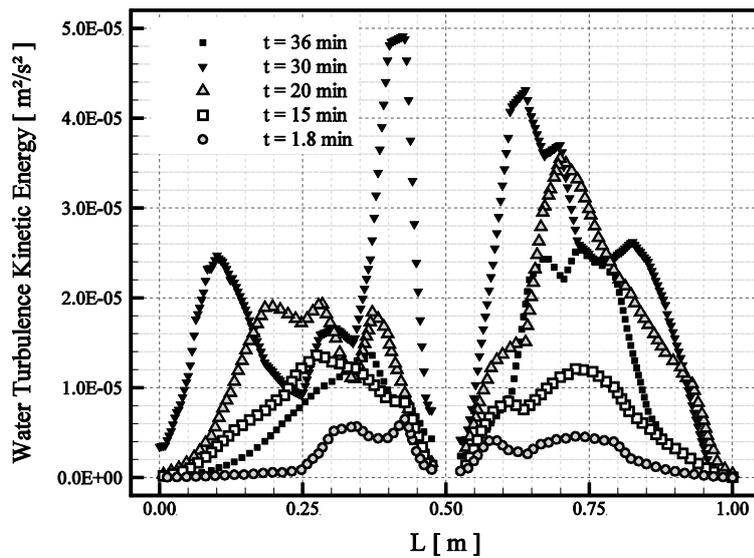
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354

### 355 **3.2 Turbulence**

356 The magnitude of turbulent kinetic energy remains low inside the tank. The flow starts with the  
357 formation of a jet of fluid denser than water and formation of initial instabilities near the central inlet tube, as  
358 can be seen in Figure 11 from  $t=2$ min. When the fluid with sediment touches the bottom of the tank, currents  
359 are formed in which turbulent instabilities are observed. The turbulent kinetic energy was calculated on a line  
360 of sampling points (Figure 7(B) - Line 1). It can be observed in the Figure 10 that with the increase of the time,  
361 until  $t=30$ min, there is turbulence increase at the bottom of the tank. As observed in the previous section, the  
362 fluid that reaches the bottom of the tank presents high velocity, being able to load particles to regions closer to  
363 the baffle impacting the clarified quality. But at  $t=36$  min, it is observed that there is a decrease in the value  
364 of the turbulent kinetic energy, around  $0.25 \text{ cm}^2/\text{s}^2$ , this indicates that with the increase in time, particles can  
365 decant more easily. This fact can be observed when analyzing Figure 12 at  $t = 36$  min, that is, there is a higher  
366 concentration of sludge at the bottom of the sedimentation tank, around 1.4%. In general the turbulent kinetic

367 energy in the liquid phase varied very little, from 0-0.5  $\text{cm}^2/\text{s}^2$ , being that the maximum was observed around  
368 the central pipe of inlet. And the highest values (about 40  $\text{cm}^2/\text{s}^2$ ) were observed in the air layer that was  
369 considered above the liquid phase as already shown in Figure 7 (B).



370  
371 **Figure 10: Turbulent kinetic energy evaluated on line 1 located in the central plane at the bottom of the tank.**

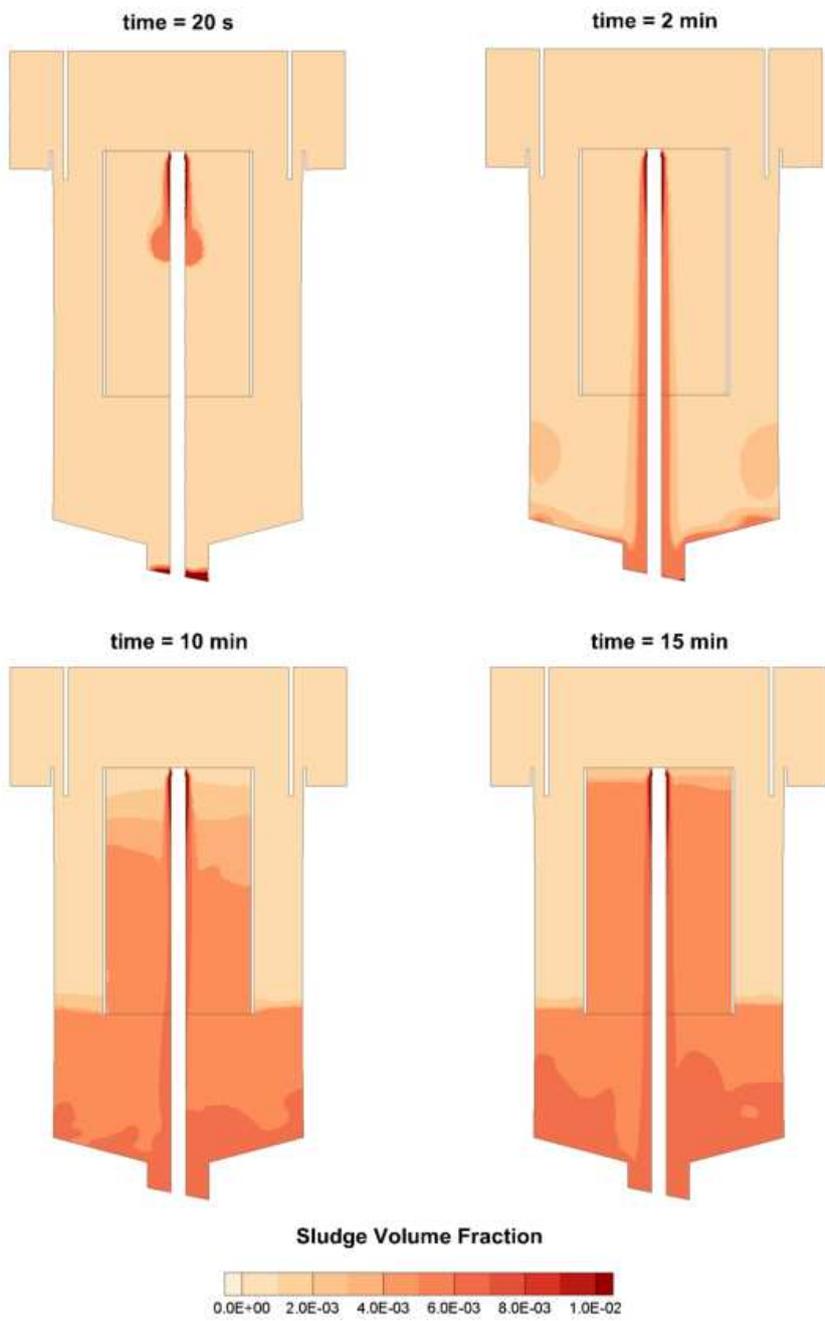
372  
373 **3.3 Concentration of suspended solids**

374 In the present study the scraper was not considered at the bottom of the tank, so the sludge was able to  
375 build up. In the first 36 minutes of simulation the sludge outlet was kept open. After this time it was closed  
376 and simulated another 24 minutes.

377 In Figure 11 and Figure 12, the increase in the height of the concentrated sludge layer is observed  
378 over time, that is, the evolution of the volume fraction of sludge with time in the tank. Therefore, it is possible  
379 to visualize the sedimentation process. It is observed that at the initial time  $t=20\text{s}$ , the jet with sludge and water  
380 is beginning its development, at  $t=2\text{min}$  the portion of fluid containing 0.6% of sludge is deposited in the  
381 bottom. And in the following instants the volume of the tank occupied with such amount of sludge increases.

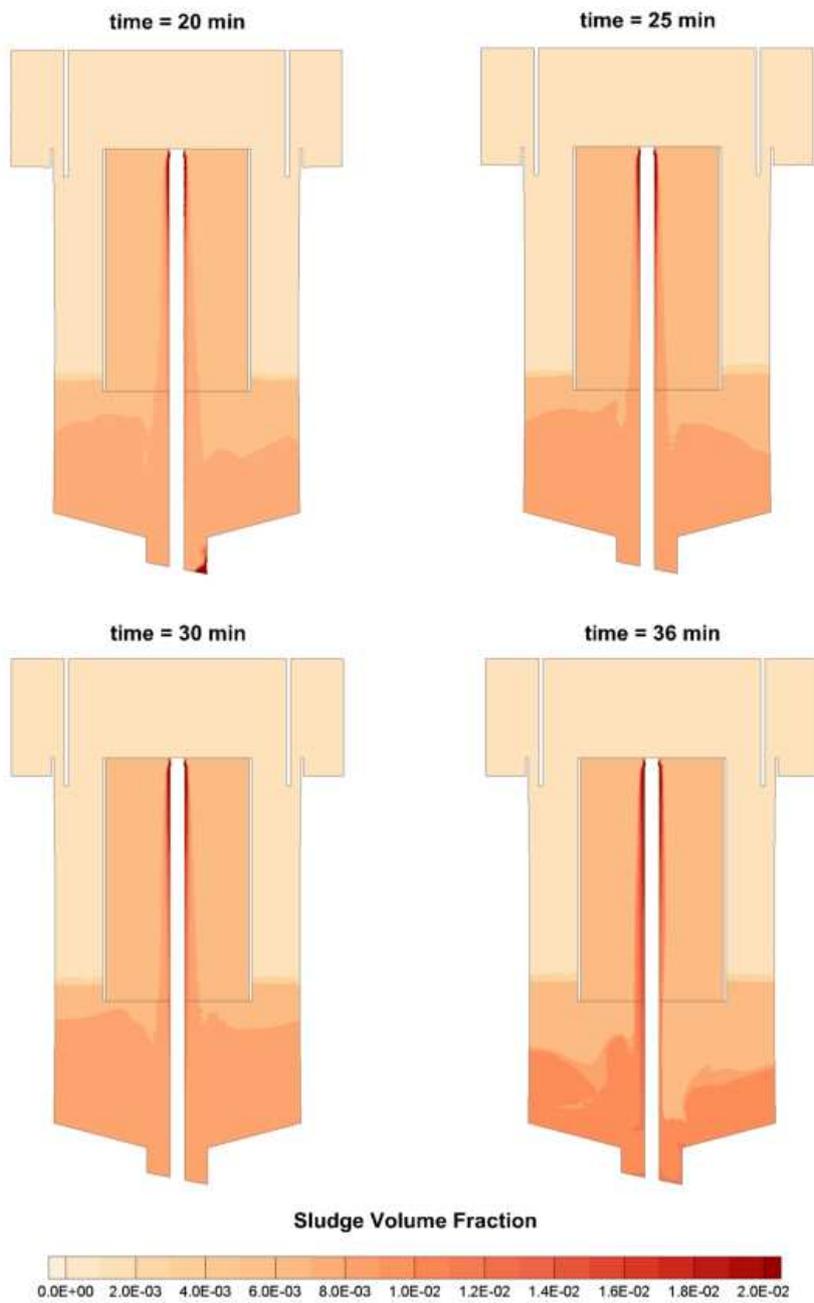
382 At  $t=20$  min, about 0.8% sludge portion reaches approximately the height of the baffle outlet, even this  
383 percentage of sludge enters the interior of the baffle.

384 At  $t=36$ min it is already possible to observe 1.2% of sludge fraction accumulated in a thinner layer at  
385 the bottom of the tank. This indicates that in 36min there is greater accumulation of sludge at the bottom of  
386 the tank. This fact is in agreement with the data obtained in Figures 9 and 10, with less magnitude of velocity  
387 and less turbulence at the bottom of the decanter, there is less re-suspension of particles and a greater amount  
388 of sludge accumulates at the bottom of the tank.



389

390 **Figura 11: Sludge volume fraction in the initial instants of the simulation with sludge outlet opened.**



391

392 **Figura 12: Sludge volume fraction in the final moments of the simulation with sludge outlet opened.**

393

394

395           The operation of the decanter was also simulated with the outlet of sludge closed, to observe the denser  
396 and rich microorganism sludge depositing in the bottom of the tank, then the microorganisms that grow in the  
397 system need to be discarded and posteriorly the sludge outlet must be reopened. The heavier sludge is scraped  
398 to a central well; the scraper system was not simulated in this work. After 36 minutes of simulation, the sludge  
399 outlet was closed and the most intensive sedimentation process could be observed.

400           As expected, the increase of concentrated sludge at the bottom of the decanter is observed at  $t = 60$   
401 min (2% of sludge) as seen in Figure 13. To illustrate the increase of settled sludge particles in units of mass  
402 concentration, see Figure 14.

403           Na opening boundary condition was chosen for the sludge outlet boundary condition and also for the  
404 clean water outlet boundary condition because it was numerically more stable. An opening condition can be  
405 used at a boundary where the flow is into or out of the domain. All of the fluid might flow into the domain at  
406 the opening, or all of the fluid might flow out of the domain, or a mixture of the two might occur. For this  
407 reason, it was observed an increase in the volume fraction of sludge very close to the sludge outlet in some  
408 stages of the simulation, as in  $t=10\text{min}$ ,  $t=15\text{min}$  and  $t=20\text{min}$  in Figure 13 and on the chart  $t=20\text{min}$  in Figure  
409 14.

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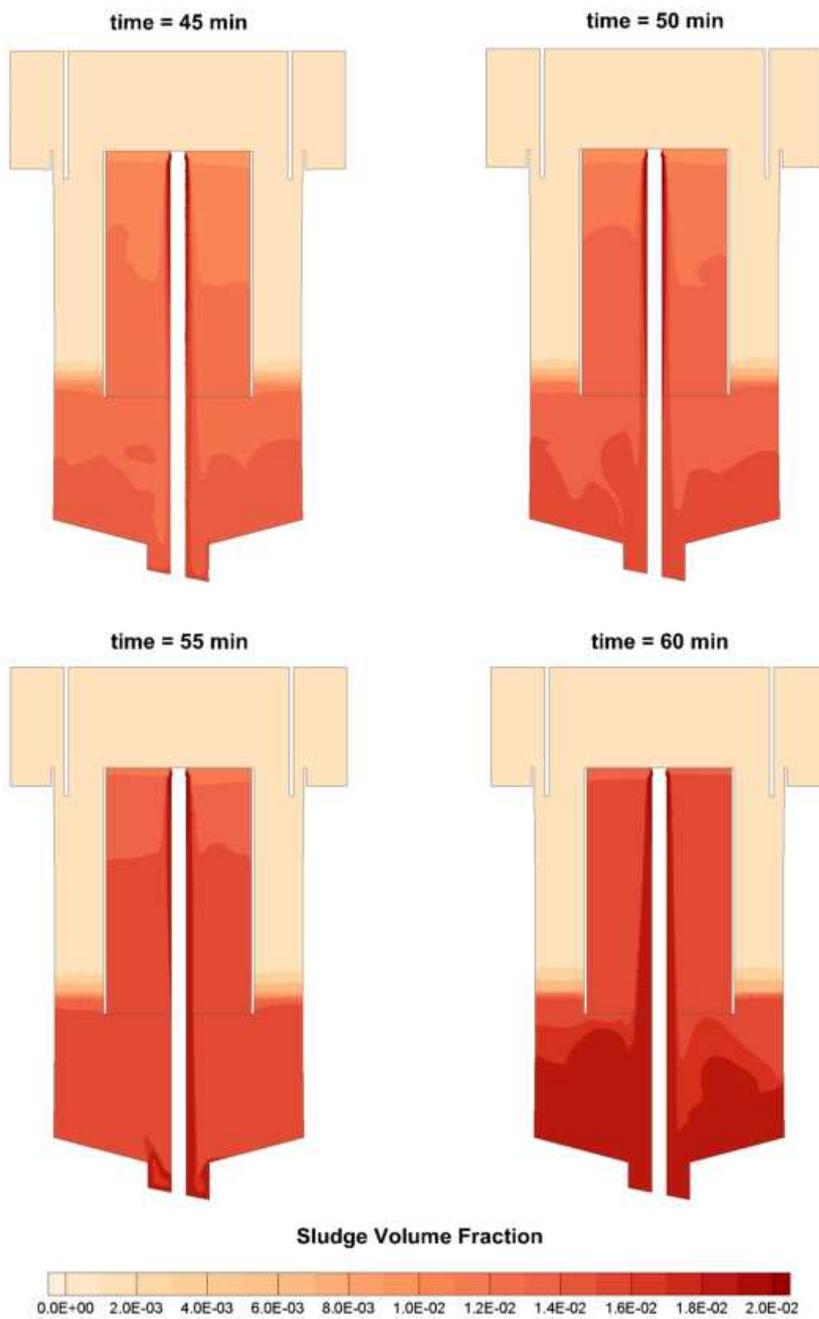
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418

419 **Figura 13: Sludge volume fraction in the final moments of the simulation with sludge outlet closed.**

420 To evaluate the magnitude of the sludge concentration at specific sites of the tank, two sampling lines were  
421 considered inside the tank, both in the vertical position (parallel to the z-axis), the first, **line 2** is situated in the  
422 central plane ( $y \times z$ ) at 0.02m from the sludge outlet. The second line, **line 3** is situated in the center plane ( $x \times z$ ) at 0.09m from the side wall of the tank.

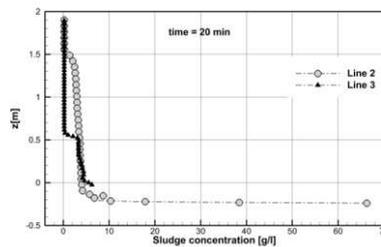
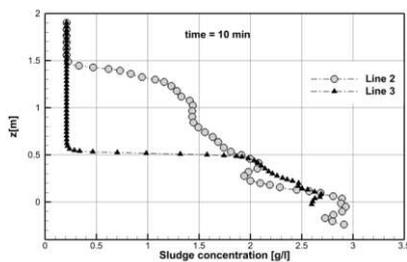
424 As can be seen in Figure 14, at the beginning of the simulation, at  $t=10\text{min}$  at a height of 1.5m there is a sludge  
425 concentration of approximately 0.25g/l on line 2 near the center of the tank and such concentration increases  
426 as the height decreases. At the bottom of the tank near the outlet of sludge on line 2, there is concentration of  
427 2.8g/l. However, on the line 3 situated closest to the wall, it is observed an increase in the concentration of  
428 sludge from a height of 0.5m with 2.0g/l and of 2.7g/l at the bottom of the tank. In line 2 (near the center) there  
429 is a significant concentration of 1.5 m, since line 2 is located in the region of the inside of the baffle where  
430 there is sludge recirculation and in line 3 (near the wall) a significant concentration of sludge is observed only  
431 from 0.5m in height. In both lines there is greater concentration in the bottom of the tank.

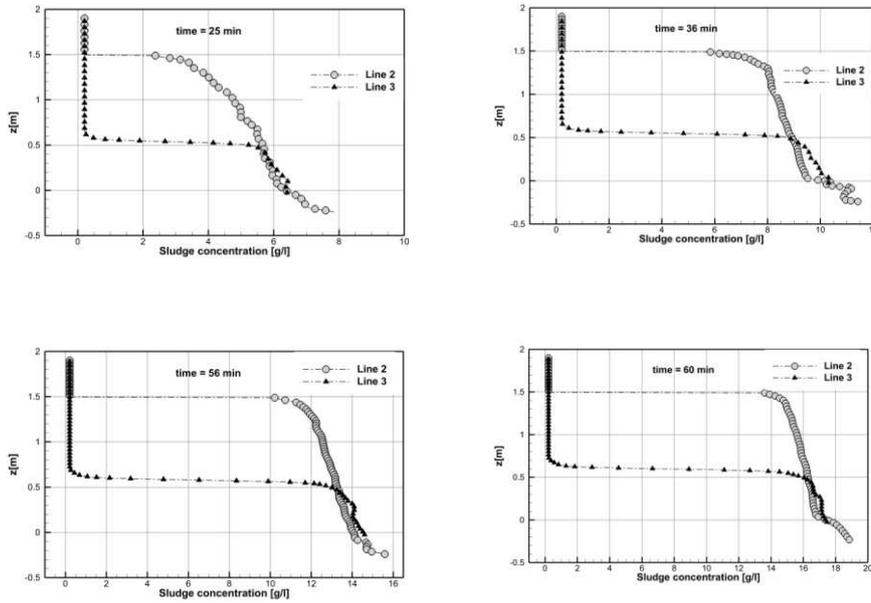
432 At  $t=36\text{min}$ , concentration at the bottom of the tank is observed around 11.5g/l and 10.4g/l in lines 2 and 3  
433 respectively. These values in their magnitude are in agreement with the work of (Patziger, Kainz et al. 2012).  
434 And after the sludge exit is closed it is observed at the bottom of the tank an increase of approximately 40%  
435 of sludge in both sampling lines.

436

437

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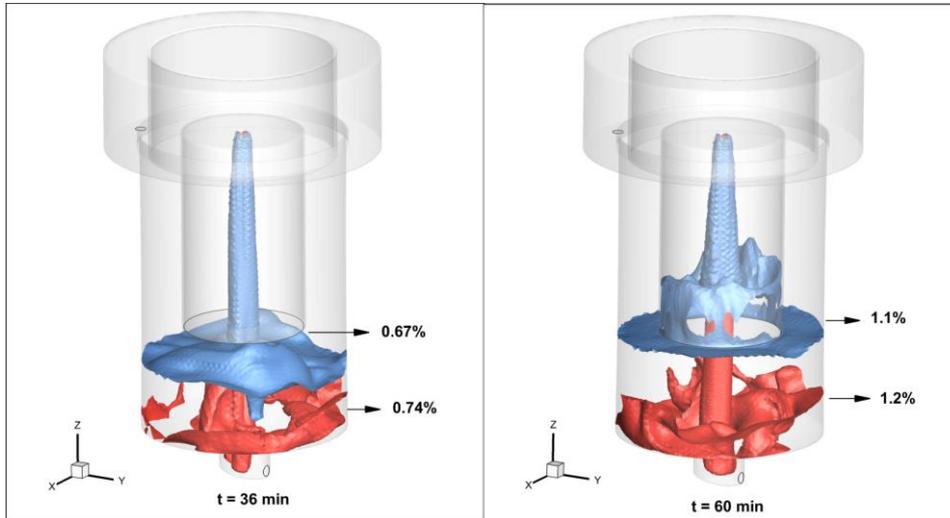


439 **Figure 14: SS concentrations in line 1 and line 2, representative vertical profiles of the SCST**

440

441 An isosurface is a surface of constant value for a given variable. That is, a three-dimensional surface  
 442 that defines a single magnitude of a flow variable such as volume fraction. The Figure 15 shows the chaotic  
 443 nature of the fluid's behavior in the tank in  $t=36\text{min}$  and  $t=60\text{min}$ . The rapid increase of sludge particles is  
 444 observed when the sludge outlet is closed  $t=60\text{min}$ . When the fluid with higher density (water + sludge) enters  
 445 with high velocity in the tank containing water, this is pushed up by the fluid recirculating into the baffle and  
 446 reaches the walls of the baffle as it is possible to visualize from the isosurface with 1.1% sludge volume fraction  
 447 at  $t = 60\text{ min}$  for example.

448 The fluid with larger volumetric fractions of sludge that are observed at the bottom of the tank also  
 449 has many small recirculation zones, both at  $t=36\text{min}$  and at  $t = 60\text{min}$ , this may cause resuspension of sludge  
 450 particles. To reduce the disturbances in the bottom of the tank it would have to have a larger diameter and  
 451 lower height, like this, there would be greater area in the bottom so that the high velocity observed in the center  
 452 could decrease.



453

454 **Figure 15: Sludge volume fraction by isosurfaces with two different values for t=36min and t=60min respectively.**

455

456 **4. Conclusions**

457 A three-dimensional model in a three-phase transient regime was used to obtain information about the  
 458 flow behavior in an SCST.

459

460 Comparisons between two-dimensional and three-dimensional simulations of an experimental SCST  
 461 case from the literature showed that the 2-D mathematical model captures flow patterns, but with the 3-D  
 462 model there is better agreement when comparing the sludge volume fractions in the tanks.

463

464 With the sludge outlet open, the velocity field shows that even working with low hydraulic loading  
 465 will re-suspend the particles accumulated at the bottom of the tank because this is a region of high velocity  
 466 and turbulence. The turbulent kinetic energy and the velocity at the bottom of the tank are smaller after 30  
 467 minutes of simulation. Also, analysis of the fields of sludge volume fractions display the water-sludge interface  
 468 and it is observed that in the final time instants of the simulation the decanting process is more stable, there is  
 469 a layer of higher concentration of particles at the bottom of the tank.

470

471 With the sludge outlet closed, as expected, an increase in the sludge volume fraction was observed,  
472 consequently in its concentration.

473

474 The model proved to be numerically stable and able to predict the distribution of sludge in the tank.  
475 The computation time for one hour of simulation was 180 days. The present study is the first step in the  
476 understanding of the hydrodynamic parameters involved in the optimization of a pilot plant of a SCST, from  
477 here, the model may be employed in future works to test other operating conditions, geometric modifications  
478 and the simulation time should be increased.

479

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482

#### 483 **References**

484 Al-Sammarraee, M., A. Chan, S. M. Salim and Mahabaleswar (2009). "Large-eddy simulations of particle  
485 sedimentation in a longitudinal sedimentation basin of a water treatment plant. Part I : Particle settling  
486 performance." Chemical Engineering Journal **152**: 7.

487 Bajcar, T., F. Steinman, B. Sirok and T. Preseren (2011). "Sedimentation efficiency of two continuously  
488 operating circular settling tanks with different inlet - and outlet arrangements." Chemical Engineering Journal  
489 **178**: 8.

490 Bardina, J. E., P. G. Huang and T. J. Coakley (1997). Turbulence Modeling Validation Testing and  
491 Development. NASA Technical Memorandum 110446.

492 Bürger, R., S. Diehl and I. Nopens (2011). "A consistent modelling methodology for secondary settling tanks  
493 in wastewater treatment." Water Research **45**(6): 2247-2260.

494 Clercq, B. D. (2003). Computational Fluid Dynamics Of Settling Tanks: Devevelopment of Experiments and  
495 Rheological, Settling, and Scraper Submodels., University of Gent.

496 Crowe, C. T. (2005). Multiphase Flow Handbook, Taylor & Francis Group - CRC Press.

497 Gong, M., S. Xanthos, K. Ramalingam, J. Fillos, K. Beckmann, A. Deur and J. A. McCorquodale (2011).  
498 "Development of a flocculation sub-model for a 3-D CFD model based on rectangular settling tanks." Water  
499 Science & Technology **9**: 8.

500 Goula, A. M., M. Kostoglou, T. D. Karapantsios and A. I. Zouboulis (2008). "A CFD methodology for the  
501 design of sedimentation tanks in potable water treatment." Chemical Engineering Journal **140**(1): 110-121.

502 Guo, X., X. Zhou, Q. Chen and J. Liu (2013). "Flow field and dissolved oxygen distributions in the outer  
503 channel of the Orbal oxidation ditch by monitor and CFD simulation." J Environ Sci (China) **25**(4): 645-651.

504 Kleine, D. and B. D. Reddy (2006). Finite Element Simulation Of Unsteady Flows In Secondary Settling  
505 Tanks. Fifth International Conference on CFD in the Process Industries. CSIRO, Melbourne, Australia: 6.

506 Lakghomi, B., Y. Lawryshyn and R. Hofmann (2015). "Evaluation of flow hydrodynamics in a pilot-scale  
507 dissolved air flotation tank: a comparison between CFD and experimental measurements." Water Science et  
508 Technology **72**: 7.

509 Li Lei and J. Ni (2014). "Three-dimensional three phase model for simulation of hydrodynamics, oxygen mass  
510 transfer, carbon oxidation, nitrification and denitrification in a oxidation ditch." Water Research: 14.

511 Menter, F. R. (1994). Two-equation eddy-viscosity turbulence models for engineering applications. AIAA-  
512 Journal.

513 Patziger, M. (2016). "Computational fluid dynamics investigation of shallow circular secondary settling tanks:  
514 Inlet geometry and performance indicators." Chemical Engineering Research and Design: 10.

515 Patziger, M., H. Kainz, M. Hunze and J. Józsa (2012). "Influence of secondary settling tank performance on  
516 suspended solids mass balance in activated sludge systems." Water Research **46**(7): 2415-2424.

517 Patziger, M., H. Kainz, M. Hunze and J. Józsa (2012). "Influence of Secondary Settling Tank Performance on  
518 Suspended Solids Mass Balance in Activated Sludge Systems." Water Research **46**: 11.

519 Samstag, R. W., J. J. Ducoste, A. Griborio, I. Nopens, D. J. Batstone, J. D. Wicks, S. Saunders, E. A. Wicklein,  
520 G. Kenny and J. Laurent (2016). "CFD for wastewater treatment: an overview." Water Science et Technology  
521 **74** (3): 14.

522 Tchobanoglous, G., F. L. Burton and H. D. Stensel (2003). Wastewater engineering : treatment and reuse/  
523 Metcalf&Eddy.Inc.

524 , Fourth edition / revised by George Tchobanoglous, Franklin L. Burton, H. David Stensel. Boston : McGraw-  
525 Hill, [2003] ©2003.

526 Wilcox, D. C. (1986). Multiscale model for turbulent flows. In AIAA 24th Aerospace Sciences Meeting.  
527 American Institute of Aeronautics and Astronautics.

528 Wu, B. (2010). "CFD simulation of mixing in egg-shaped anaerobic digesters." Water Research **44**(5): 1507-  
529 1519.

530

531