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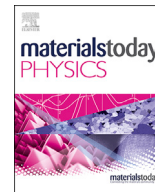
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In situ poling X-ray diffraction studies of lead-free BiFeO₃–SrTiO₃ ceramics



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ABSTRACT

The origin of the large electrostrain in BiFeO₃–BaTiO₃ (BF–BT) ceramics is controversial and has been attributed to either a field-induced transition to a long-range ferroelectric (FE) state or to multi-symmetry, polar nanoregions within a pseudocubic matrix whose vectors approximately align with the direction of the applied field. The (1–x)BiFeO₃–xSrTiO₃ (BF–xST) solid solution is structurally and microstructurally similar to BF–BT and provides a further case study to assess the origin of electrostrain. In BF–xST, electrostrain is optimized at x = 0.4 (0.15%) which zero field, room temperature full-pattern X-ray diffraction (XRD) Rietveld refinement and scanning/transmission electron microscopy suggest is composed of 15% rhombohedral (R) cores, surrounded by 85% pseudocubic (PC) shells. *In-situ* poling synchrotron XRD reveals that all peaks remain singlet and exhibit no change in full width half maximum up to 100 kV cm^{–1}, confirming the absence of long-range FE order and the retention of short-range polar order, despite the large applied field. Strain anisotropy (calculated from individual peaks) of $\epsilon_{220} > \epsilon_{111} > \epsilon_{200}$ and the associated strain orientation distribution however, indicate the existence of local orthorhombic (O), R and tetragonal (T) symmetries. The data therefore imply the existence under poling of multi-symmetry polar nanoregions in BF–0.4ST rather than a long FE phase, supporting the model described by Wang and co-workers (2019) for BF–BT compositions.

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1. Introduction

BiFeO₃ (BF) ceramics possess a large polarization of 90–100 $\mu\text{C cm}^{-2}$ and a very high ferroelectric (FE) Curie temperature (T_C) of 1093 K [1,2]. However, the difficulty of fabricating single phase BF ceramics has limited material characterization and device

applications, leading to most attention being focused on BF-based solid solutions [3–6]. One of the most promising examples is (1–x)BiFeO₃–xBaTiO₃ (BF–xBT). Although often reported as having a morphotropic phase boundary (MPB) between BF-rich rhombohedral (R) phase and BT-rich tetragonal (T) phase, properties are optimized within a diffuse mixed phase region consisting of R and pseudocubic (PC) phases at 0.25 < x < 0.35, where high FE T_C, large maximum and remanent polarizations (P_{max} and P_r), and excellent piezoelectric coefficients (d₃₃) and electric field-induced strain (electrostrain) [7–10] have been reported. Compared to other lead-free piezoelectrics, e.g. Na_{0.5}Bi_{0.5}TiO₃ (NBT)-based materials, BF based materials have a more complex, core-shell structure. The formation of a core-shell structure, the core/shell volume ratio and their composition can potentially affect the electrical properties. Quenching has proved an effective method to modify the core-shell structure and therefore, electrical properties [11].

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BF-BT however, suffers from volatilization of Bi and the formation of mixed valence Fe ions during sintering [12,13], leading to high levels of conductivity, particularly at elevated temperatures ($>100\text{ }^{\circ}\text{C}$). This has driven extensive investigations into the role of A-site (e.g. La and Nd) [14–16] and/or B-site stoichiometric dopants (e.g. Al, Co, Ga, $\text{Ni}_{1/2}\text{Ti}_{1/2}$, $\text{Mg}_{1/2}\text{Ti}_{1/2}$) [17–23] on electrical resistivity and piezoelectric properties of BF-BT ceramics. Aliovalent doping has also been investigated and electrical conductivity of BF-based materials is suppressed by Nb and Mn [24–29], with excellent electrostrain ($S_{\text{max}} > 0.4\%$, strain coefficient $d_{33}^* > 500\text{ pm V}^{-1}$) reported in BF-BT-based solid solutions with 0.1%–0.5% excess Mn, e.g. BF-BT-Nd, BF-BT-Bi($\text{Mg}_{2/3}\text{Nb}_{1/3}$) O_3 and BF-BT-Bi($\text{Zn}_{2/3}\text{Nb}_{1/3}$) O_3 [16,21,30].

Despite extensive studies of BF-BT-based solid solutions, the origin of the excellent electrostrain for BF-BT-based materials remains controversial. Chen and co-workers [31] reported a high electrostrain of 0.38% at 60 kV cm^{-1} for 0.64BF-0.36BT ceramics due to a combination of lattice distortion, domain switching and a field-induced phase transition. Wada and co-workers proposed that the origin of electrostrain in BF-BT-0.1Bi($\text{Mg}_{1/2}\text{Ti}_{1/2}$) O_3 ceramics was associated with off-centered Bi ion grain-to-grain interactions [32]. Wang, Reaney and co-workers reported electrostrain of $\sim 0.6\%$ in BF-BT-0.01Nd($\text{Li}_{1/2}\text{Nb}_{1/2}$) O_3 ceramics at 150 kV cm^{-1} under *in-situ* poling synchrotron X-ray diffraction (XRD) [33]. Prior, during and after application of electric field, the structure remained PC without any change in full width half maximum (FWHM) of XRD peaks. Instead, strain anisotropy of XRD peaks ($\epsilon_{200} > \epsilon_{220} > \epsilon_{111}$) indicated the presence of multi-symmetry polar nanoregions, which permitted a large average distortion in the direction of the applied field. Similar characterization and strain behavior were also reported in BF-BT-BiScO₃ and BF-BT-Bi($\text{Mg}_{2/3}\text{Nb}_{1/3}$) O_3 [33]. In contrast to BF-BT [19,32,34–36], there is a consensus that the origin of the large electrostrain in NBT based materials results from a field-induced transition from a short to a long range ordered state [37–41]. The wider understanding of electrostrain in polar materials would therefore, benefit from further in-depth studies of BF-based systems.

BiFeO₃-SrTiO₃ (BF-ST) is a promising candidate to investigate further the origin of electrostrain in BF-based materials but most studies to date have focussed on magnetic [42–45] rather than FE and piezoelectric properties, because of its high leakage current [43] and high coercive field (E_c) compared to BF-BT. However, BF-ST ceramics were recently doped with donor Nb-ions (1–3 mol%) which suppressed the high leakage current, resulting in large breakdown strength at room temperature [46]. Therefore, these modified BF-ST compositions are suitable to not only evaluate electrical, FE and piezoelectric properties but also to undertake *in-situ* synchrotron studies under large applied fields.

In this work, the detailed phase structure, dielectric, FE and piezoelectric properties of Nb-doped (1-x)BF-xST ($x = 0.1\text{--}0.5$) ceramics are investigated with optimized electrical and piezoelectric properties obtained at $x = 0.4$ within a mixed R and PC region, in which a small volume core of R phase is surrounded by a large volume of PC shell regions. *In-situ* poling synchrotron XRD is employed for the first-time in BF-ST ceramics to rationalise the origin of the optimized electrostrain for $x = 0.4$. Under electric field, the average structure of $x = 0.4$ remains PC (singlet XRD reflections) but exhibits strain anisotropy with $\epsilon_{220} > \epsilon_{111} > \epsilon_{200}$, confirming the absence of electric field-induced long-range order and supporting the “multi-symmetry polar nanoregion” model, described by Wang and co-workers [33].

2. Methods

(1-x)BF-xST-0.01Nb ($x = 0.1, 0.2, 0.3, 0.4$ and 0.5) ceramics were

prepared using analytical-grade Bi₂O₃, Fe₂O₃, SrCO₃, TiO₂ and Nb₂O₅ by a solid state reaction method. Stoichiometric amounts of dried raw powders were weighed and ball-milled 12 h in isopropanol using Y₂O₃-stabilized ZrO₂ as grinding media. The mixed powders were dried, calcined 2 h at 800 °C and then ball milled 12 h. After uniaxially pressing, ceramic samples were sintered 3 h at 1030–1150 °C. The densities of the sintered ceramics were measured using the Archimedes method. Surfaces of sintered ceramics were ground, and gold paste electrodes applied. Impedance spectroscopy (IS) data was obtained by an Agilent E4980A (Agilent Technologies Inc., Palo-Alto, CA) from 20 Hz to 1 MHz at 100 mV. Electrical conductivity was obtained by fitting the experimental data using ZView software (Scribner Associates, Inc., Southern Pines, NC). Temperature dependence of dielectric properties were measured using an Agilent 4184A precision LCR meter from room temperature to 550 °C at 10, 100, 250 kHz and 1 MHz. IS and dielectric data were corrected by a geometric factor (thickness/surface area). Bipolar polarisation–electric field (*P-E*) and strain–electric field (*S-E*) loops were obtained using an aixACCT TF 2000E FE tester at 1Hz. The polished surface of the ceramic samples was observed using an FEI Inspect F50 scanning electron microscope (SEM) with backscattered electron (BSE) and energy-dispersive spectroscopy (EDS) detectors. Transmission electron microscopy (TEM) data were obtained using a JEOL JEM 2100F (JEOL, Tokyo, Japan) operated at 200 kV.

To evaluate the electrostrain of (1-x)BF-xST ceramics, *in-situ* poling synchrotron XRD was employed, as schematically shown in Fig. 1. *In-situ* poling synchrotron XRD experiments were performed at the I15 Diamond light source with a photon energy of 72 keV (0.1722 Å). Ceramic samples were cut into bars ($L5 \times W1 \times T0.2\text{ mm}$) and annealed 2 h at 800 °C to eliminate residual stresses. During *in-situ* experiments, the bar-shaped samples were polished down to 0.2 mm thickness and placed in a custom-designed polyimide holder with silicone oil. The sample holder was electrically connected with a high voltage amplifier (Matsusada EC-10). The X-ray beam was focused and collimated to 70 μm diameter. Transmission and two-dimensional (2D) diffraction patterns were collected simultaneously under electric field up to 100 kV cm^{-1} with 12.5 kV cm^{-1} intervals using Pilatus 2 M detector located approximately 1 m downstream of the sample and converted every 15° into conventional one-dimensional (1D) XRD patterns with intersection angle (ψ) to the direction of the electric field [33]. XRD patterns of $\psi = 0^\circ$ and $\psi = 90^\circ$ correspond to the direction parallel and perpendicular to the applied electric field,

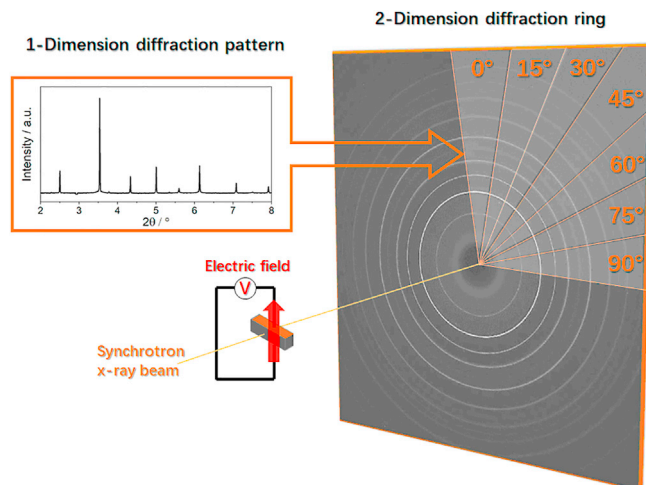


Fig. 1. The schematic of the setup of the *in-situ* poling synchrotron XRD experiment.

respectively. Peak fitting was conducted in TOPAS using a pseudo-Voigt function with crystallographic information of the ceramic obtained from full-pattern Rietveld refinements.

3. Results and discussions

3.1. Phase structure

The full-pattern Rietveld refinement results of $(1-x)\text{BF}-x\text{ST}$ ($x = 0.1, 0.2, 0.3, 0.4$ and 0.5) ceramics obtained at room temperature and zero field are presented in Fig. 2 and Table 1. The XRD full-pattern is refined using several single or mixed-phase models, such as the R ($R3m/R3c$), T ($P4mm$) and cubic (C , $\text{Pm}\bar{3}m$). Lattice parameters for each phase are fitted with fixed background, instruments information and peak type to obtain the phase fraction,

cell volume and refined parameters. At the highest BF concentration, $x = 0.1$, only R ($R3c$) phase is observed while for low BF concentrations ($x = 0.5$), XRD pattern is best fitted with single C ($\text{Pm}\bar{3}m$) phase. For $0.2 \leq x \leq 0.4$, XRD patterns is well refined with mixed $R3c$ and $\text{Pm}\bar{3}m$ phases, as evident by fitting of the $\{111\}_p$ and $\{200\}_p$ XRD representative peaks in Fig. 2a. The XRD full-pattern for $x = 0.4$ is best refined with 85% C and 15% R phases, consistent with previous reports [44].

4. Dielectric, ferroelectric and piezoelectric properties

The temperature-dependent dielectric permittivity (ϵ_r vs. T) and loss ($\tan\delta$ vs. T) data of $(1-x)\text{BF}-x\text{ST}$ ($x = 0.1, 0.2, 0.3, 0.4$ and 0.5) ceramics are shown in Fig. 3. The broad ϵ_r peaks for $x = 0.1$ and 0.2 have been previously proposed to relate to the onset of

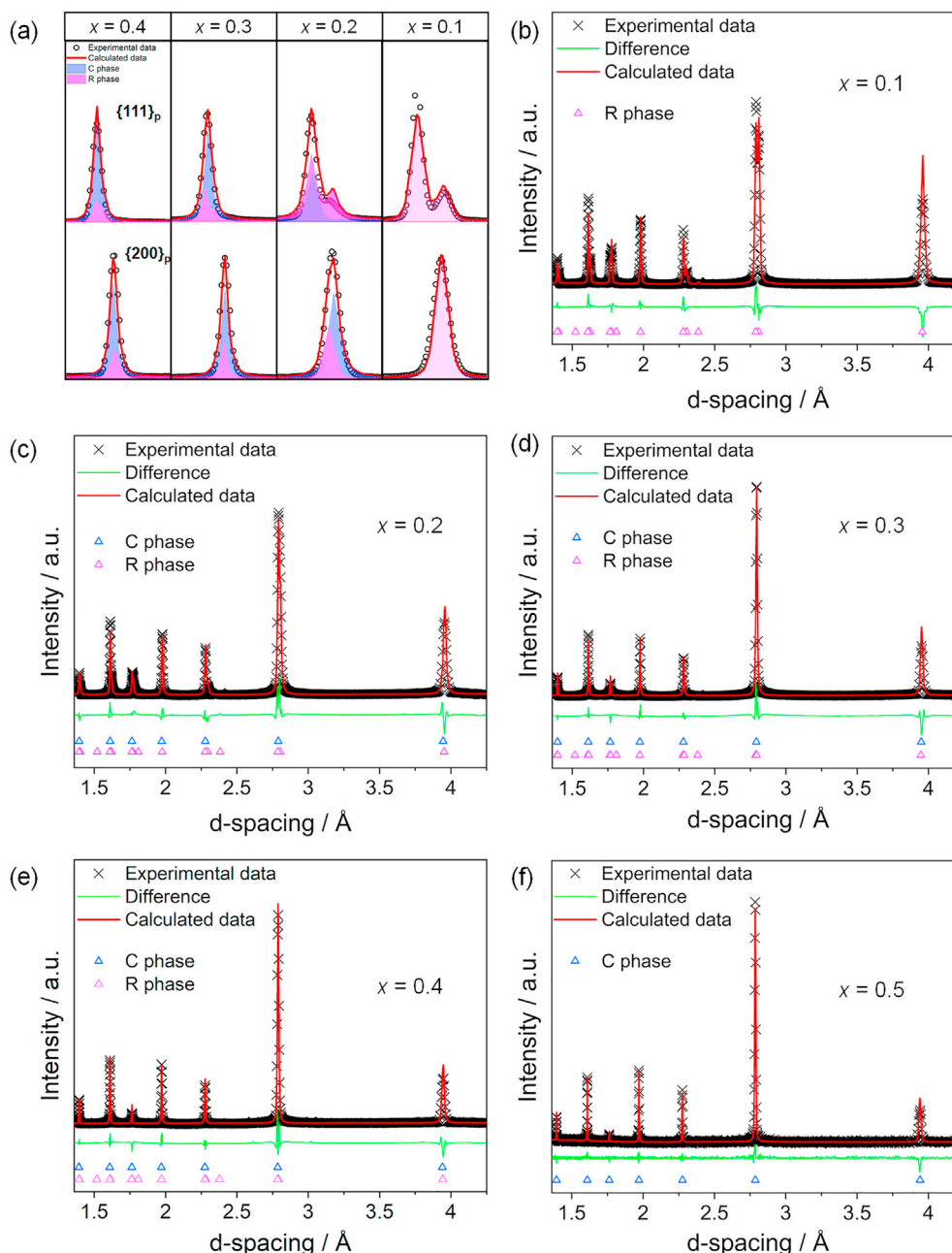


Fig. 2. Synchrotron XRD pattern and corresponding Rietveld refinement results for $(1-x)\text{BF}-x\text{ST}$ ceramics at room temperature.

Table 1
Summary of XRD Rietveld refinement results for (1-x)BF-xST ceramics.

x	GOF	R_{exp}	R_{wp}	C phase-Pm $\bar{3}m$			R phase-R3c			
				Phase fraction	Cell volume (\AA^3)	Lattice a (\AA)	Phase fraction	Cell volume (\AA^3)	Lattice a (\AA)	Lattice c (\AA)
0.1	1.06	11.06	11.88	0%	N/A	N/A	100%	371.94(3)	5.5766(2)	13.8104(6)
0.2	1.08	11.11	11.98	30%	61.445(11)	3.9460(2)	70%	370.52(6)	5.5731(4)	13.7746(10)
0.3	1.07	13.2	14.17	74%	61.569(5)	3.94871(11)	26%	368.95(9)	5.5749(5)	13.7080(19)
0.4	1.08	11.56	12.48	85%	61.189(5)	3.94056(7)	15%	367.75(15)	5.5706(9)	13.684(3)
0.5	1.12	10.67	11.95	100%	61.23(3)	3.9415(7)	0%	N/A	N/A	N/A

GOF: goodness of fitting.

ferroelectricity or the existence of a relaxor/FE phase [6] but there is no evidence of Curie-Weiss behavior. There is some frequency dispersion within the ϵ_r vs. T plots for $x = 0.1$ and 0.2 but the high $\tan\delta$ above 300°C casts doubt as to whether these maxima can be ascribed to relaxor behavior. Compositions with $0.3 \leq x \leq 0.5$ however, have well-defined broad Curie maxima (T_m) which decrease in temperature with increasing ST concentration. We propose that any phase transitions (T_m) for $x = 0.1$ and 0.2 are above 500°C and are not recorded in the data. Even if higher temperature data are available, the high conductivity would likely obscure changes in the ϵ_r vs. T that relate to the onset of FE/relaxor behavior. With increasing ST concentration, T_m decreases and becomes visible in ϵ_r vs. T plots below 500°C for $0.3 \leq x \leq 0.5$. Irrespective of the interpretation, all ϵ_r vs. T plots are consistent with previously published data [6] with the broad peaks for $0.3 \leq x \leq 0.5$ presumably arising from a combination of the FE R core and the relaxor PC shell within grains.

Room temperature P - E and S - E loops of (1-x)BF-xST ($x = 0.1, 0.2, 0.3, 0.4$ and 0.5) ceramics at an electric field of 150 kV cm^{-1} are presented in Fig. 4. Compositions with $x = 0.1$ and 0.2 exhibit behavior consistent with a 'lossy' linear dielectric, often associated with BF-rich compositions [47,48]. We propose that the high

transition temperature ($>500^\circ\text{C}$), implied from the ϵ_r vs. T data in Fig. 2, may inhibit FE switching with opening of the loop only related to polarization from space-charge regions. The P - E and S - E loops for $x = 0.3$ and 0.4 exhibit FE hysteresis with the largest $P_r \sim 45.5\ \mu\text{C cm}^{-2}$, $E_c \sim 86\text{ kV cm}^{-1}$ and $S_{max} \sim 0.09\%$ for $x = 0.3$ [49]. These compositions also have small negative strains in the S - E loops, suggesting at least, in part, a contribution from FE behavior (R phase) to the strain but which diminishes at $x = 0.5$. Optimized electromechanical properties, P_{max} of $52.7\ \mu\text{C cm}^{-2}$ and S_{max} of 0.15% are observed for $x = 0.4$. The P - E for $x = 0.5$ becomes significantly slimmer with an absence of negative strain in the S - E , exhibiting a typical relaxor behavior. A combination of XRD refinements, ϵ_r vs. T and P/S - E plots therefore, suggests a transition from a FE to relaxor state as a function of increasing x . The trend is identical to that observed for BF-BT compositions by several authors [8,50].

5. Microstructure for $x = 0.4$

Backscattered Electron (BSE) images of the polished surface of $x = 0.4$ ceramic are presented in Fig. 5a. Ceramics exhibit polygonal grains with an average $\sim 2\ \mu\text{m}$ diameter and minimal porosity

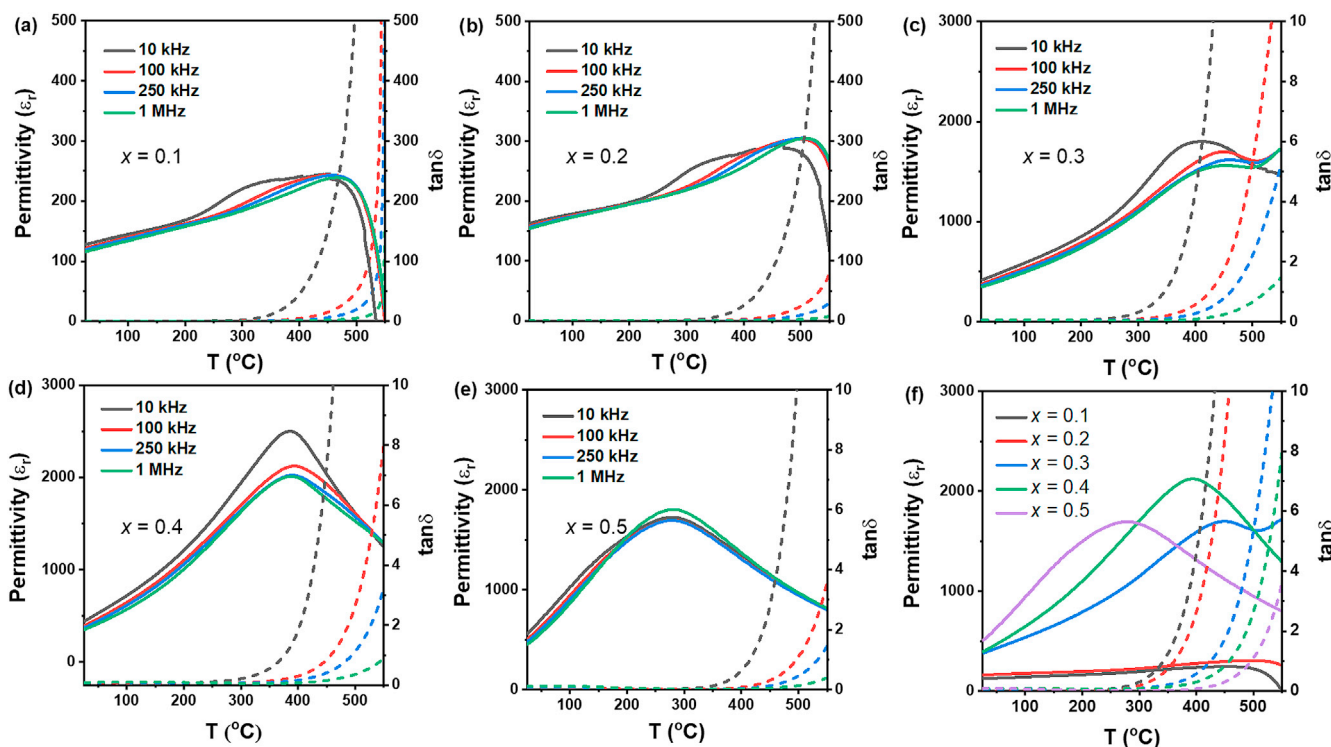


Fig. 3. (a) The temperature dependence of dielectric permittivity (ϵ_r vs. T) and loss ($\tan\delta$ vs. T) of (1-x)BF-xST ceramics, (a) $x = 0.1$, (b) $x = 0.2$, (c) $x = 0.3$, (d) $x = 0.4$, (e) $x = 0.5$ and (f) The temperature dependence of ϵ_r and $\tan\delta$ compared at 100 kHz.

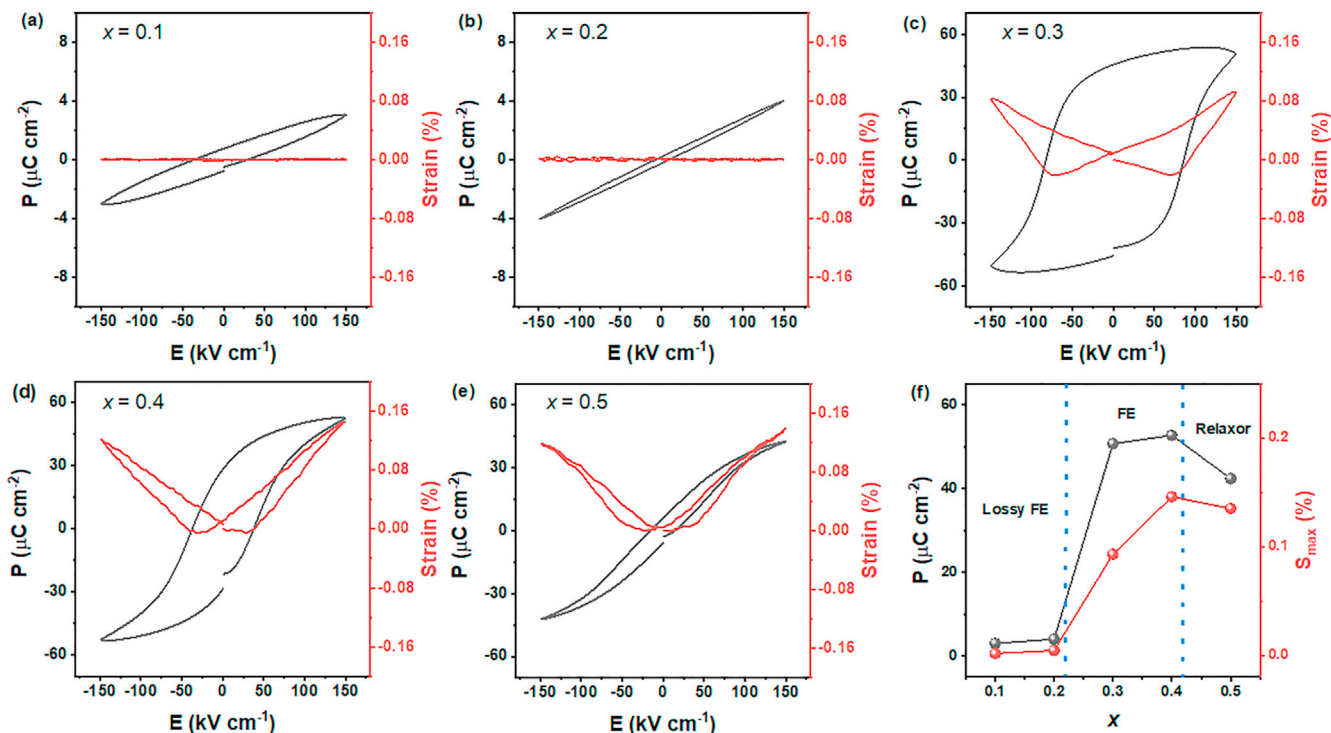


Fig. 4. Room temperature P - E and S - E loops under 150 kV cm^{-1} of $(1-x)\text{BF-xST}$ ceramics, (a) $x = 0.1$, (b) $x = 0.2$, (c) $x = 0.3$, (d) $x = 0.4$ and (e) $x = 0.5$. (f) Variation of P_{max} and S_{max} as function of x .

(relative density > 95%). Core-shell regions are observed, with most grains displaying bright cores (Bi/Fe rich) and dark shells (Sr/Ti rich). The detailed quantitative data for each microstructural feature are shown in Table 2. We propose that the C phase from XRD refinements is Sr/Ti rich and resides within the shell and the R phase is Bi/Fe rich within the core. A core-shell microstructure is associated with immiscibility on cooling from the sintering temperature that leads to microchemical segregation, commonly observed in BF-based ceramic systems [33,46]. TEM images reveal the presence of a meso-domain structure within the grain core as displayed in Fig. 5b, consistent with a FE R phase with minimum diffraction contrast in the PC shell regions.

6. In-situ poling synchrotron XRD for $x = 0.4$

Synchrotron XRD patterns of ceramics with $x = 0.4$ are recorded

Table 2

Average atomic percentage (excl. O) calculated from EDS spectra obtained from different phases presented in $x = 0.4$.

Elements	Bright Core (mol%)	Dark Shell (mol%)
Bi	35.5	29.2
Fe	40.6	28.9
Sr	13.8	20.8
Ti	10.1	21.1

from an unpoled ($E = 0 \text{ kV cm}^{-1}$) to poled ($E_{\text{max}} = 100 \text{ kV cm}^{-1}$, beyond E_c) to unpoled ($E = 0 \text{ kV cm}^{-1}$) state with a step size of 12.5 kV cm^{-1} . Contour surface plots (Fig. 6) show variations in the $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ peak profiles under a full cycle of bipolar electric field ($E_{\text{max}} = 100 \text{ kV cm}^{-1}$) for $x = 0.4$ at $\psi = 0^\circ$ and 90° , representing the longitudinal strains (positive) and transverse

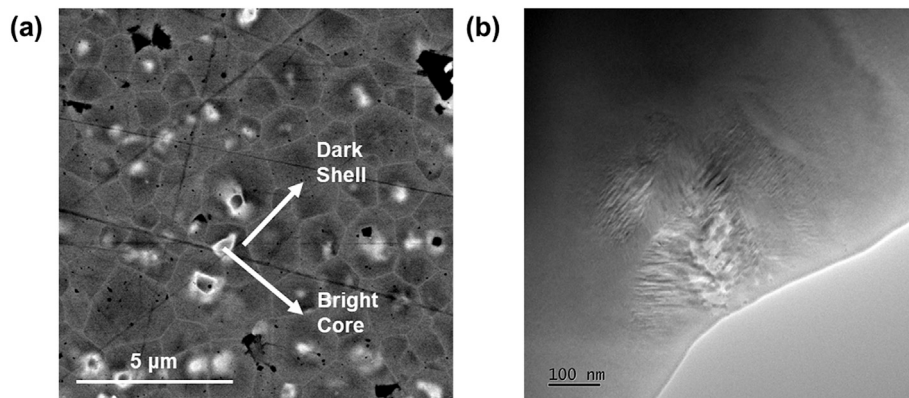


Fig. 5. (a) Backscattered Electron (BSE) image of the polished surface and (b) TEM bright field image.

strains (negative), respectively. Prior, during and after application of electric field of 100 kV cm^{-1} , $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ peaks remain singlet without splitting, suggesting no occurrence of macroscopic domain switching and phase transitions. Similar behavior was also reported in our previous work on BF-BT-based materials under an electric field of 150 kV cm^{-1} [33]. Fig. 6 confirms that BF-ST solid solutions are less prone to field-induced structural phase transition to a long-range FE state than other relaxor materials, such as La-doped lead zirconate titanate (PZT) and NBT-based materials [51,52].

With increasing electric field, $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ peaks shift to smaller 2θ angles at $\psi = 0^\circ$, indicating increased d spacing and tensile stresses parallel to the direction of the electric field. In contrast, the peaks shift to higher angle at $\psi = 90^\circ$, corresponding to compressive stress perpendicular to the electric field direction. The peak positions of initial unpoled state ($E = 0 \text{ kV cm}^{-1}$), $+E_{\text{max}}$, 0 , $-E_{\text{max}}$ and poled state ($E = 0 \text{ kV cm}^{-1}$) are also plotted in Fig. 6, showing the variation of each single peak under application of electric field. There are no significant changes of FWHM in Fig. 7a, confirming again the absence of a macroscopic transition or changes in domain correlation [33]. More importantly, the peak position at the poled remanent state is slightly offset in comparison with the initial unpoled state, which will be further discussed in the later sections.

The electrostrain for lead-based and lead-free piezoelectrics is commonly contributed by a combination factors, i.e. structural transformation, domain switching and lattice strain, which can be calculated from XRD peaks, as reported by Jones [53,54] and Chen [55,56]. For compositions that remain PC phase during application of external electric field, the effective total electrostrain ($\epsilon_{\text{eff total}}$) obtained from *in-situ* XRD poling experiment can also be simply estimated based on the weighted-average strain of individual $\{hkl\}$ planes [57], as given by Eq. (1):

$$\epsilon_{\text{eff total}} = \frac{\sum_{hkl} T_{hkl}(\psi) m_{hkl} \epsilon_{hkl}(\psi)}{\sum_{hkl} T_{hkl}(\psi) m_{hkl}} \quad (1)$$

where $T_{hkl}(\psi)$ is the domain texture index with angle ψ to the

electric field, m_{hkl} is the multiplicity of $\{hkl\}$ planes, and $\epsilon_{hkl}(\psi)$ is the effective individual electrostrain with angle ψ to the electric field, which can be calculated from Eq. (2):

$$\epsilon_{hkl}(\psi) = \frac{d_{hkl} - d_{hkl}^0}{d_{hkl}^0} \quad (2)$$

Here, d_{hkl} and d_{hkl}^0 are the hkl interplanar spacings under electric field and without electric field, respectively. In the present case, $T_{hkl}(\psi) = 1$ due to the absence of crystallographic texture. The m_{hkl} values of $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ planes are 8, 6 and 12, respectively, according to a PC setting [58]. $\epsilon_{hkl}(\psi)$ values are obtained from Eq. (2) through fitting of the $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ diffraction peaks from which the $\epsilon_{\text{eff total}}$, may be estimated using Eq. (1).

The ϵ_{111} , ϵ_{200} and ϵ_{220} calculated from $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ peaks for $x = 0.4$ at $\psi = 0^\circ$ and 90° up to a bipolar electric field of 100 kV cm^{-1} are shown in Fig. 7b. Positive and negative values are obtained in $\psi = 0^\circ$ and 90° , indicating tensile and compressive strain, respectively. The highest strain under electric field of 100 kV cm^{-1} at $\psi = 0^\circ$ for ϵ_{220} , ϵ_{111} and ϵ_{200} is $+0.13\%$, $+0.10\%$ and $+0.08\%$. Combined data of ϵ_{111} , ϵ_{200} and ϵ_{220} , Eq. (1) is employed to obtain the effective total electrostrain, as shown in Fig. 7c. The $\epsilon_{\text{eff total}}$ are $\sim +0.11\%$ at $\psi = 0^\circ$ and -0.04% at $\psi = 90^\circ$, which is close to that obtained from macroscopic S-E results (Fig. 4d).

Compared to BF-BT [33], a smaller electrostrain ($<0.15\%$) is attained for BF-ST at higher fields ($>100 \text{ kV cm}^{-1}$). The difference in response may be qualitatively related to the decrease in average cubo-octahedral and octahedral volumes in ST with respect to BT based solid solutions. Ba (1.64 \AA) is a significantly larger ion than Sr (1.44 \AA) [59] which would generally increase polarization and strain in solid solutions of the latter, in accordance with a simplistic ‘rattling ion’ model; i.e. the larger the average site volume, the greater the potential for displacement of the most polarizable species (Ti and Bi).

A contribution to strain from the FE R3c core (observed in SEM and TEM images) which would be expected to contribute either through lattice distortion and/or domain switching, resulting in

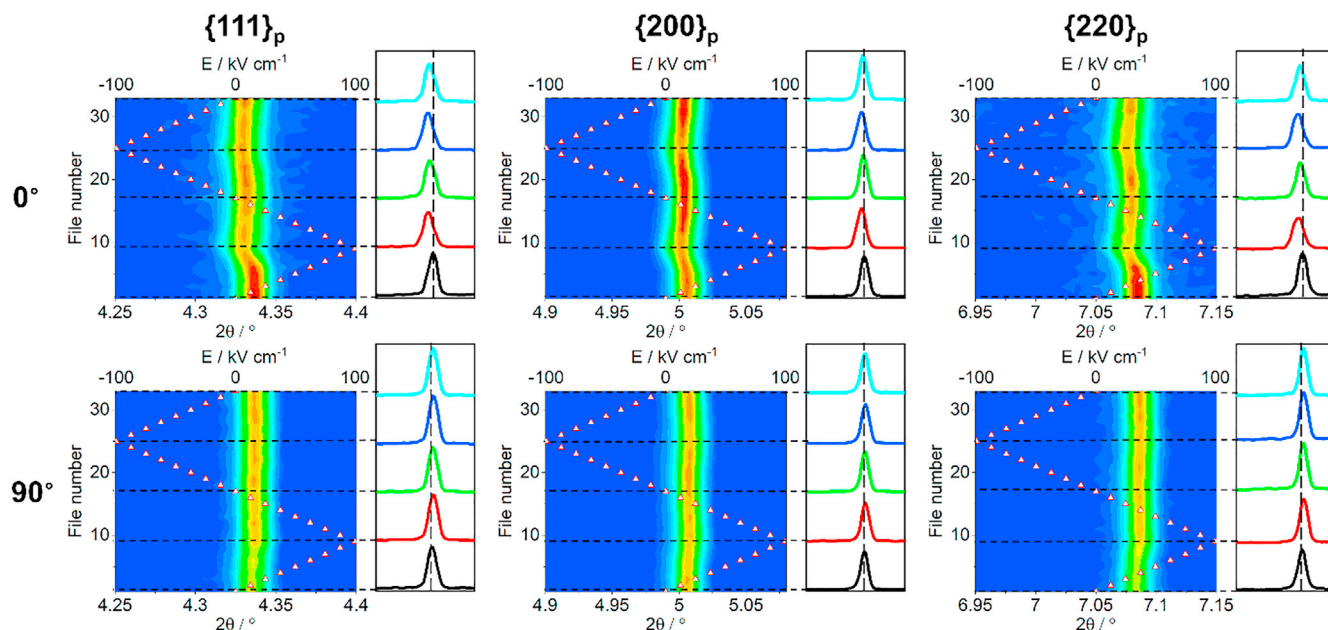


Fig. 6. Contour plots of the $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ peak profiles at $\psi = 0$ and 90° as a function of the variations up to maximum electric field ($\pm 100 \text{ kV cm}^{-1}$) obtained from the *in-situ* poling synchrotron XRD experiment for $x = 0.4$.

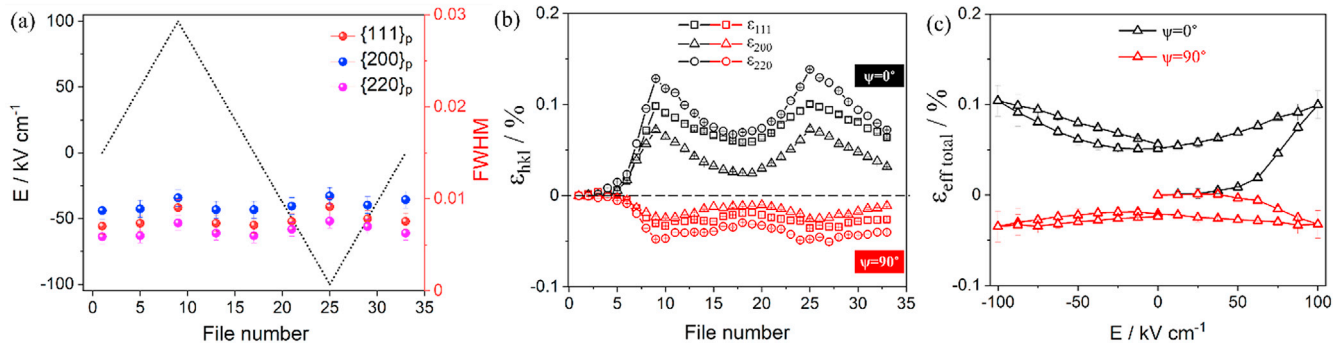


Fig. 7. (a) FWHM of the $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ peaks. (b) The ϵ_{111} , ϵ_{200} and ϵ_{220} for $x = 0.4$ as function of record file number with bipolar electric field up to 100 kV cm^{-1} at $\psi = 0^\circ$ and 90° . (c) The $\epsilon_{\text{eff total}}$ at $\psi = 0^\circ$ and 90° .

splitting of the $\{111\}_p$ peak [60]. The absence of a clear contribution through splitting or widening of peaks associated with the R3c cores may be due to the relatively small volume fraction of R (15%) with respect to PC (85%) phase, giving only a negligible contribution to the peak profile. However, the absence of any change in the FWHM of the $\{111\}_p$ peak (Fig. 7a) may also suggest that the R3c cores are partially clamped by the surrounding shell matrix and do not undergo significant domain switching/distortion [11]. Some evidence of domain switching is present in the P - E loops (Fig. 4) but the negative strain is negligible for $x = 0.4$ and electrostriction rather than piezoelectricity is the dominant contribution to the total strain. Clamping and/or finite size effects leading to suppressing of FE behavior have been reported previously for, e.g., lead titanate ceramics as a function of grain size [61].

Given the dominant shift in $\{220\}_p$ rather than $\{111\}_p$ XRD peaks (Fig. 7b), we propose that electrostrictive behavior arises mainly from the larger PC shell volume rather than the core regions and is consistent with the “multi-symmetry polar nanoregion” model proposed by Wang and Reaney in 2019 [33]. Here, the symmetries of polar nanoregions (10–50 Å) include but are not limited to orthorhombic (O), R and T distortions. The absence of dominant R , even though the cores remain R3c, suggests that they remain inactive or insignificant due to a combination of their low volume fraction and clamping effect. The absence of any significant increase in the FWHM of the XRD peaks at 100 kV cm^{-1} suggests that any field-induced transition does not propagate throughout the grains and the coherence of distorted regions remain short-range, as reported previously in BF-BT-based compositions [11].

To further justify the “multi-symmetry polar nanoregion” model, strain orientation distribution (SOD) analysis for $x = 0.4$ on the poled remanent state ($E = 0 \text{ kV cm}^{-1}$) is examined. Generally speaking, SOD refers to strain variations in the lattice as a function of ψ [40]. However, in this work, the length scale of the active polar nanoregions is nanometric and SOD refers to their strain azimuthal angle-dependence and anisotropy. The variations of ϵ_{hkl} as a function of ψ (the angle of the strain to the electric field) can be quantified. Azimuthal angle-dependence of representative XRD peaks of $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ at unpoled and poled states are shown in Fig. 8a and b. Individual XRD reflections at $\psi = 0^\circ$, 30° , 60° and 90° are plotted to examine ϵ_{hkl} before and after poling. For the initial state (unpoled), there is no discrepancy in the peak position for four ψ values, corresponding to no apparent strain anisotropy, Fig. 8a. As shown in Fig. 6, a small irreversible change of the peak position between unpoled and poled states is induced by application of external electric field at $\psi = 0$ and 90° with peak shifts at other different ψ values also likely to occur, Fig. 8b. All three representative peaks exhibit a minor shift to higher 2θ angles with increasing ψ from 0 to 90° .

Here, the SOD (polar nanoregions) analysis at the poled remanent state is calculated from Eq. (2) using the difference on peak position between poled and unpoled states, as illustrated on (111), (200) and (220) poles in Fig. 8c. The ϵ_{hkl} exhibit azimuthal angle-dependence, with the highest (positive) and lowest (negative) levels of ϵ_{hkl} being observed at $\psi = 0^\circ$ and 90° , respectively. The positive ϵ_{hkl} are found to be approximately $\epsilon_{111} \sim +0.07\%$, $\epsilon_{200} \sim +0.04\%$ and $\epsilon_{220} \sim +0.08\%$ for longitudinal direction ($\psi = 0^\circ$, centre of the pole) while the negative strains are obtained to be $\epsilon_{111} \sim -0.03\%$, $\epsilon_{200} \sim -0.02\%$ and $\epsilon_{220} \sim -0.04\%$ for transverse direction ($\psi = 90^\circ$, edge of the pole). Combining the ϵ_{hkl} with strain anisotropy ($\epsilon_{220} > \epsilon_{111} > \epsilon_{200}$) discussed in the previous section (Fig. 7), we propose that electrostrain in BF-ST arises from a polar nanoregion model with likely, but not exclusively, O , R and T symmetries within the PC shell under applied field.

7. Conclusions

Structural and electrical performance of BF-ST electroceramics are evaluated for the first-time. Rietveld refinements confirm that, as x increases, the phase structure transforms from R to PC in $(1-x)$ BF- x ST solid solutions. Optimized electro-mechanical properties are obtained for compositions $x = 0.4$, $\epsilon_r \sim 2500$ at $\sim 380^\circ \text{C}$, $P_{\text{max}} \sim 52.7 \mu\text{C cm}^{-2}$ and $S_{\text{max}} \sim 0.15\%$. The origin of optimized electrostrain is further investigated using *in-situ* poling synchrotron XRD. For $x = 0.4$, $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ XRD reflections remain single prior, during and after application of external electric field. The absence of R3c core (represented by splitting in $\{111\}_p$ peak) in XRD maybe hidden by the complex core (small volume)-shell (large volume) microstructure. Thus, only electrostrictive (contributed from PC) but no piezoelectric response (contributed from R3c) is found during *in-situ* poling, exhibiting strain anisotropic behavior at E_{max} (100 kV cm^{-1}) and remanent states (after poling, 0 kV cm^{-1}) with $\epsilon_{220} > \epsilon_{111} > \epsilon_{200}$. The optimized electrostrain behavior in a retained, averagely PC structure throughout the entire poling procedure can be only interpreted by the “multi-symmetry polar nanoregion” model, in which, presence of local short-range O , R and T distortions that cannot be probed under synchrotron XRD. Moreover, the absence of changes on FWHM even at highest electric field (100 kV cm^{-1}) suggest that any formation of local short-range distortions cannot correlate to medium- or long-range after poling. This behavior contrasts with conventional lead-based and NBT-based electrostrictors which undergo field-induced transition to a long-range FE state [62–65]. The occurrence of this unusual behavior in BF-BT and BF-ST solid solutions poses the question as to whether this is a general phenomenon across many systems or restricted uniquely to compositions derived from BF.

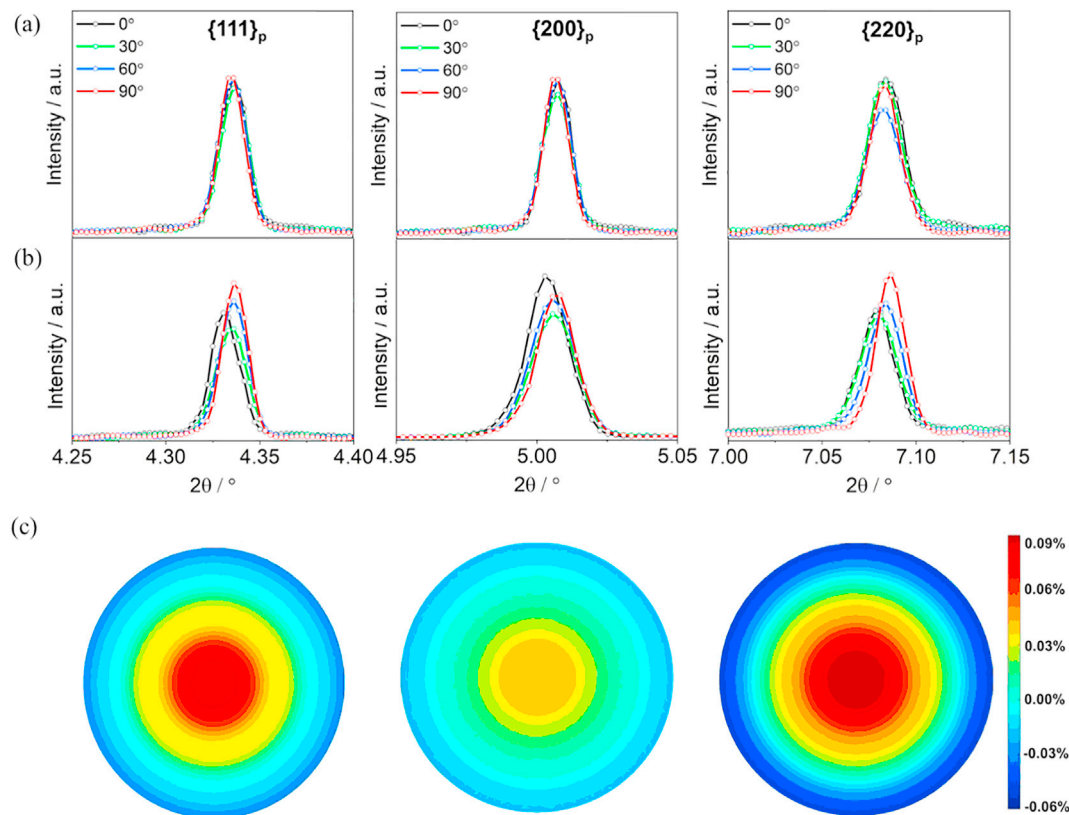


Fig. 8. Azimuthal angle-dependence of three representative peaks of $\{111\}_p$, $\{200\}_p$ and $\{220\}_p$ for (a) unpoled, (b) poled $x = 0.4$ ceramics and (c) ϵ_{hkl} for (111), (200) and (220) poles.

CRediT author statement

Dawei Wang and Ian M. Reaney supervised the project, Zhilun Lu wrote the article, carried out all property measurements and contributed to all microstructure characterizations, Zhilun Lu, Ge Wang, Linhao Li, Dawei Wang and Annette K. Kleppe contributed to the in-situ synchrotron X-ray experiment. Ge Wang and Zhilun Lu contributed to the corresponding data analysis, Weichao Bao and Fangfang Xu conducted the transmission electron microscopy characterizations, Antonio Feteira and Yuhe Huang contributed to data discussion, All the authors discussed the results and commented on the manuscript.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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