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1 Relative rates of fluid advection, elemental diffusion and replacement govern reaction
2 front patterns

3

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22 Highlights

23 • Reactive fluid infiltration into granular rocks produces very variable reaction
24 front roughness

25 • Reaction front roughness is suppressed by fast reactions

26 • Reaction patterns mimic microstructure best with advective transport and
27 slow reaction

- We present a diagram of resulting patterns according to Péclet and Damköhler numbers

30

31 Abstract

32 Replacement reactions during fluid infiltration into porous media, rocks and buildings
33 are known to have important implications for reservoir development, ore formation as
34 well as weathering. Natural observations and experiments have shown that in such
35 systems the shape of reaction fronts can vary significantly ranging from smooth,
36 rough to highly irregular. It remains unclear what process-related knowledge can be
37 derived from these reaction front patterns. In this contribution we show a numerical
38 approach to test the effect of relative rates of advection, diffusion, and reaction on
39 the development of reaction fronts patterns in granular aggregates with permeable
40 grain boundaries. The numerical model takes (i) fluid infiltration along permeable
41 grain boundaries, (ii) reactions and (iii) elemental diffusion into account. We monitor
42 the change in element concentration within the fluid, while reactions occur at a pre-
43 defined rate as a function of the local fluid concentration. In non-dimensional phase
44 space using Péclet and Damköhler numbers, results show that there are no rough
45 fronts without advection ($Péclet < 70$) nor if the reaction is too fast ($Damköhler > 10^{-3}$).
46 As advection becomes more dominant and reaction slower, roughness develops
47 across several grains with a full microstructure mimicking replacement in the most
48 extreme cases. The reaction front patterns show an increase in roughness with
49 increasing Péclet number from Péclet 10 to 100 but then a decrease in roughness
50 towards higher Péclet numbers controlled by the Damköhler number. Our results
51 indicate that reaction rates are crucial for pattern formation and that the shape of
52 reaction fronts is only partly due to the underlying transport mechanism.

53

54 Keywords: Reaction front, advection, diffusion, roughness, replacement, grain
55 boundary network

56

57 1. Introduction

58 Fluid infiltration, material transport, and related reactions induce mineralogical
59 changes that can dramatically modify the physiochemical properties of rocks
60 affecting their mechanical and hydrodynamic properties (Jamtveit et al., 2000; Putnis
61 and Austrheim, 2010). Incomplete element and mineralogical redistribution are both
62 preserved in the rock record in the form of chemical reaction fronts – the more or less
63 localized interface between reacted and unreacted material. Such fronts control
64 geochemical exchange between the atmosphere, [hydrosphere](#), and the geosphere
65 with importance for weathering at the Earth's surface in rocks as well as building
66 stones (Kondratiuk et al., 2017; Ruiz-Agudo et al., 2016) and diagenesis.
67 Understanding reaction fronts also has strong fundamental implications to
68 reconstruct large-scale geodynamic histories based on the occurrence of prograde
69 and retrograde metamorphic reactions that include fluids (Austrheim, 1987; Ague,
70 2003; Centrella et al., 2016; Plümper et al., 2017) as well as retrogressive reactions
71 when buried rocks are exhumed (Rudge et al., 2010; Yardley and Cleverley, 2013).
72 Furthermore, changes due to fluid-rock interaction are of importance for the
73 prediction of reservoir characteristics (e.g. Rochelle et al., 2004), the understanding
74 of geothermal systems including their scaling and the development of mineral
75 deposits (Merino and Canals, 2011). Reaction fronts that are linked to fluid-mediated
76 replacement reactions (fig. 1) have been shown to be common in the rock record
77 (Putnis, 2009). Such reactions require the presence of a fluid in chemical
78 disequilibrium with the surrounding minerals. Fluids in chemical disequilibrium need
79 to be transported to the site of reaction, hence such fluids need pathways to infiltrate
80 the system at a certain rate (Jamtveit et al., 2009; Putnis and Austrheim, 2010; Ulven
81 et al., 2014). Transport occurs within the fluid as well as in the solid where chemical
82 constituents are moving according to both advective and diffusive laws. At the same
83 time, the chemical constituents needed for the replacement reaction must be present

84 allowing the existing phase to dissolve, the interfacial mineral-fluid boundary layer to
85 become supersaturated and a new more stable phase to grow (Ruiz-Agudo et al.,
86 2014). Fluid transport, reaction, and diffusion each have a certain rate, that may be
87 all interrelated. Conceptually, different transport rates should result in different rates
88 of reaction front progression but also in different reaction front patterns with
89 differences in chemical, isotopic and trace-element signatures (Centrella et al.,
90 2016).

91 Thus, if we can link the pattern of the reaction front to the relative rates of the three
92 main processes involved, we can use the rock record directly to determine these.

93 If the reaction only takes place around a fracture in the rock one can of course
94 assume that fluid flow along a fracture network was responsible for the reaction (fig.
95 1a). However, reaction fronts of large bodies are quite often smooth on the larger
96 (meter to deca-meter) scale and seem to have preserved a pattern that indicates, at
97 least locally, important fluid infiltration along fractures, bedding planes or grain
98 boundaries (fig. 1b). It is not clear how this “fluid-flow” or “infiltration” pattern (fig. 1b)
99 can so clearly be preserved in a reaction.

100 Reactants, i.e. the chemical constituents that can trigger reactions in rocks, can enter
101 the system by two main transport mechanisms: advection and diffusion (Jamtveit and
102 Meakin, 1999). Diffusion takes place where the concentration of the chemical
103 constituent changes along the chemical gradient. This process is relatively slow and
104 scales non-linearly with the square root of time (Jamtveit and Meakin, 1999).
105 Therefore, it is either important on the very small scale or over very long (geological)
106 timescales. Advection on the other hand involves fluid-flow through the system either
107 by wetting a dry rock or through convection cells driven by thermal or salinity induced
108 density contrasts, for example in geothermal systems (Lipsey et al., 2016). The
109 reactants are then brought in with the fluid and the timescale of this process depends
110 on the fluid velocity (Zhao et al., 2007; Szymczak and Ladd, 2009). The fluid velocity
111 can be enhanced along permeable structures or zones in the rock, so that fractures,

112 faults, grain boundaries and porous zones can favour flow and thus transport of
113 chemical constituents. As advection is much faster than diffusion, it is much more
114 effective in larger-scale systems such as large hydrocarbon reservoirs or mineral
115 deposits.

116 Reaction and advection/diffusion may influence each other. For example, they can
117 be coupled in the sense that reactions may increase permeability causing a reactive
118 infiltration instability (e.g. Chadam et al., 1986) where fluid-flow and hence further
119 reaction is localized leading in the extreme case to “worm-holes” or caves in Karst
120 systems (Szymczak and Ladd, 2009), replacement of relatively dense crystals
121 through reaction-induced porosity development (Putnis and Putnis, 2007; Beaudoin
122 et al., 2018) and infiltration of fluids and reactions into otherwise dry, impermeable
123 systems (Jamtveit et al., 2000). Reactions may decrease permeability and arrest the
124 reaction front propagation (Ruiz-Agudo et al., 2016). If reactions drive shrinkage and
125 expansion, fracturing may occur, leading to additional pathways for advecting fluids
126 (Ulven et al., 2014; Jamtveit et al., 2000). These positive feedback processes
127 localize reactions and transport and drive faster material changes and strong
128 localization. Reactive transport in reservoir rocks has been modelled extensively with
129 an emphasis on the evolution of permeability (Saripalli et al., 2001; Zhao et al., 2007;
130 Jamtveit et al., 2009; Chen et al., 2014; Kang et al., 2014; Mostaghimi et al., 2016).
131 Methods range from smooth particle hydrodynamics to lattice Boltzmann methods
132 and computational fluid dynamic techniques (Manwart et al., 2002; Tartakovsky and
133 Meakin, 2006; Fredrich et al., 2006; Shabro et al., 2012; Chen et al., 2013). These
134 studies show that there is a richness of complex interactions of fluid infiltration and
135 reactions on permeability and porosity evolution in porous systems.

136 In a system where advection and diffusion are important, the dimensionless Péclet
137 number (Pe) is used to describe the relationship between advection rate and
138 diffusion rate for chemical transport as

139 $Pe = \frac{vL}{D},$ (eq. 1)

140 with v the fluid velocity, L the characteristic length scale of the system and D the
141 diffusion coefficient. At high Pe , advection is dominating, whereas at low Pe diffusion
142 takes over. For example, the spacing and shape of wormholes in Karst systems
143 changes as a function of the Pe number (Szymczak and Ladd, 2009). A fracture-
144 dominated system where fluid infiltrates along the fractures would have a relatively
145 high Pe number. In contrast, in a system where the fluid is stationary diffusion is
146 dominant and its Pe number would therefore be low. Pe may change over time if the
147 driving forces for the advection are changing, especially if the reaction changes the
148 permeability (Ortoleva et al., 1987).

149 In a system, where reactions occur along with advection and diffusion, two additional
150 dimensionless numbers are used to assess the influence of the relative rates of
151 these processes. These two numbers are: (i) the Damköhler number I for reaction
152 rate relative to advection rate

153 $Da_I = \frac{R}{v},$ (eq. 2)

154 and Damköhler number II to relate reaction rate relative to diffusion rate

155 $Da_{II} = \frac{RL}{D},$ (eq. 3)

156 with R the reaction rate. For example, Szymczak and Ladd (2009) show that both
157 Damköhler numbers influence the shape and spacing of wormholes. A change in the
158 Damköhler I number modifies the localization, width and spacing of wormholes. If the
159 reaction is too fast, the localization of wormholes is hindered with the reaction front
160 being smooth. In contrast, if the reaction is too slow the patterns become very fuzzy
161 without developing wormholes (Szymczak and Ladd, 2009). Recent reactive
162 transport simulations of reservoir rocks have also shown the importance of the
163 Damköhler number for the alteration of pore space (Mostaghimi et al., 2016).

164 In this contribution we present a coupled numerical approach where reaction textures
165 develop in a system that allows fluid advection, chemical diffusion, and reaction to

166 take place. We study the formation of reaction front patterns that develop in a simple
167 granular aggregate with porous grain boundary regions representing a granular
168 aggregate or breccia. We explore the phase-space between advection, [diffusion](#), and
169 reaction rates to present a new classification of reaction front patterns and their link
170 to the relative rates of the three main processes involved. Finally, we compare the
171 numerical outcomes with natural examples and experiments of fluid-mediated
172 replacement reactions, which emphasize that not only fluid pathways, but also the rate
173 of reaction, have a major influence on reaction front patterns.

174

175 2. Numerical Set-up

176 2.1. General Model

177 We use a coupled hydro-dynamic model “Latte” within the microstructural [modelling](#)
178 environment “ELLE” (Koehn et al., 2003; 2005; 2019; Bons et al., 2008; Sachau and
179 Koehn, 2010; Sachau and Koehn, 2013; Ghani et al., 2013, 2015) and expand the
180 model by adding advective and diffusive matter transport as well as a simplified iso-
181 volumetric replacement reaction. We set-up the model to simulate the infiltration of a
182 grain aggregate with more permeable grain boundaries and the progression of the
183 reaction front where reactions are triggered by the presence of certain element
184 concentrations that are changing due to advection, diffusion and reaction (fig. 2a).
185 The numerical two-dimensional representation of a square slice of solid is
186 represented by a triangular mesh of cells where clusters of cells make up grains. The
187 run-cycle of the model starts with the initial granular geometry that defines the local
188 porosity (fig. 2b). Fluid pressure and concentration are applied as boundary
189 conditions. Note that the fluid pressure is ramping up linearly per time step. These
190 are followed by a calculation of the infiltrating fluid represented by changes in fluid
191 pressure and deriving the local Darcy velocity. The Darcy velocity is then used to
192 calculate the advective matter flux followed by the diffusive flux. The new
193 concentration of the reactant is finally used to drive the reaction and the local change

194 in replacement is determined followed by a new cycle (fig. 2b). The granular
 195 aggregate has a porosity defined by the local solid fraction of the network with a
 196 background variation on the cell-scale and with grain boundaries having a higher
 197 porosity. The local permeability $K(\phi_{x,y})$ is calculated using the Carman-Kozeny
 198 relation (Carman, 1937; Ghani et al., 2013) according to

$$206 \quad K(\phi_{x,y}) = \frac{r^2(\phi_{x,y})^3}{45(1 - \phi_{x,y})^2} \quad (eq\ 4)$$

199 where r is a fixed grain size and $\phi_{x,y}$ the local porosity. The fluid infiltrates the model
 200 realm from all four boundaries (fig. 2) where the fluid pressure is increased to initiate
 201 flux. These boundary conditions represent experiments of fluid infiltration into
 202 reactive samples in autoclaves with increased temperature, which we want to
 203 compare with the simulations. In natural settings high-pressure hydrothermal fluids
 204 will enter rocks from permeable fractures or faults. The fluid pressure evolution into
 205 the cell is derived using the following relation

$$211 \quad \phi\beta \left[\frac{\partial P}{\partial t} \right] = \nabla \cdot \left[(1 + \beta P) \frac{K}{\mu} \nabla P \right] \quad (eq\ 5)$$

207 where ϕ is the porosity, β the fluid compressibility, P the fluid pressure, K the
 208 permeability, μ the fluid viscosity. For a more detailed derivation see Ghani et al.
 209 (2013). For each time-step, equation 5 is used to calculate the fluid velocity v from
 210 the Darcy flux $\phi\vec{v}$ for the advection of reactants according to

$$212 \quad \vec{v} = -\frac{\frac{K}{\mu} \nabla P}{\phi} \quad (eq\ 6)$$

213 To derive the transport of reactant into the system it is assumed that the four
 214 boundaries of the numerical model retain a constant concentration C . The different
 215 physical effects of advection, diffusion and reaction are separated (see eq. 9-11
 216 below) and added after each time step according to

$$217 \quad C^t = C^{t-1} + \delta C_{adv}^t + \delta C_{diff}^t + \delta C_{react}^t \quad (eq. 7)$$

218 solving the general transport equation

219 $\frac{\partial C}{\partial t} + \vec{v} \nabla C - D \Delta C = f.$ (eq. 8)

220 The IMEX (IMplicite+Explicit; Asher et al., 1997) approach is used, where the
 221 advection is treated in an explicit and the diffusion in an implicit way with internal time
 222 loops in the advection to increase stability. This approach offers the possibility to
 223 study both, diffusion and advection dominated domains of the problem. Explicit in this
 224 case means solving the transport equation in a forward way in terms of time whereas
 225 the implicit solution of the diffusion equation uses a matrix inversion and solves the
 226 future time step at once. The advection is calculated in an explicit time-stepping
 227 method using the Lax-Wendroff scheme (Lax and Wendroff, 1960) according to

228 $\delta C_{adv}^t = -dt \vec{v} \nabla C^{t-1}$ (eq. 9)

229 with $\phi \vec{v}$ the local Darcy velocity of the fluid determined from equation 6. The diffusion
 230 is calculated with an implicit method using the ADI algorithm (Alternating Direction
 231 Implicit, Bons et al., 2008) according to

232 $\delta C_{diff}^t = dt \Delta (C^{t-1} + \delta C_{diff}^t).$ (eq. 10)

233 Finally, the reaction term in the equation calculates the reaction rate R according to
 234 (Koehn et al., 2003)

235 $R = k_r V_s \left(1 - \frac{C_a}{C_a^{eq}} \right),$ (eq. 11)

236 with k_r a rate constant, V_s the molecular volume of the solid, C_a the concentration of a
 237 and C_a^{eq} the equilibrium concentration of a in the fluid. Finally, the reaction rate is
 238 used to calculate the local replacement based on the existing replacement and the
 239 volume of particles. Particles that have been replaced by 100% become inactive.

240 For the sake of simplicity, the numerical model is based on several underlying
 241 assumptions. The reaction is assumed to be isothermal, thus there is no exothermal
 242 or endothermal process active, and the reaction is isovolumetric and does not affect
 243 the elastic properties nor the porosity of the material. Furthermore, the concentration
 244 in the fluid is thought to be sufficiently enough to lead to a replacement of the
 245 mineral. We assume that the permeability-porosity relation can be approached

246 through equation 4 following a Carman-Kozeny relation, for the matrix as well as
247 grain boundaries, which are thought to contain material and act as granular media as
248 well. The diffusion constant is thought to be constant across the model irrespective of
249 the porosity. Most of these assumptions can be changed in future models; however,
250 this would complicate the interpretation, which is the reason why we currently use the
251 most simplified setup for our study.

252

253 2.2. Set-up of simulations:

254 In all simulations the following parameters are used: dimensions of the solid 2.5x2.5
255 mm², porosity of the solid $\phi = 0.01 - 0.02$ (with the grain boundaries represented by
256 zones of twice the porosity of the matrix), Carman-Kozeny grain size $r = 0.001$ mm,
257 fluid viscosity $\mu = 1.0 \times 10^{-3}$ Pa s, fluid compressibility $\beta = 4.5 \times 10^{-10}$ m²/N, diffusion
258 constant = 1.0×10^{-10} m²/s. For the reaction we vary the relative boundary
259 concentration and use a reaction rate constant k_r from 0.0001 to 0.01 mol/(m².s) and
260 molecular volume $V_s = 0.00004$ m³/mol for calcite (Clark, 1966; Renard et al., 2004;
261 Koehn et al., 2007), giving reaction rates of about 10^{-6} to 10^{-8} m/s. However, these
262 values are only benchmark values and are rescaled to percentages in the plots such
263 that 100% means full replacement for the reaction and 100% means full boundary
264 concentration for the advecting and diffusing constituents. Models are run between
265 10000 to 100000 steps representing 2 minutes to about 10 hours, the time step for
266 each model changes between 0.001 second to 0.3 seconds depending on the speed
267 of the processes involved. The external pressure is ramped up simulating the heating
268 of the fluid in the autoclave. This process takes a few minutes (between 2 and 3
269 minutes) and gives a second timescale to the pressure equation and influences the
270 Darcy velocity and the advection.

271 The simulation is comprised of a complete infiltration of the material with fluid by
272 increasing the fluid pressure at the boundaries leading to a continuous fluid flux into
273 the model while the relative advection, diffusion and reaction rates are varied

274 systematically allowing for a sensitivity analysis. The pressure was ramped up by
275 100 to 500 Pascal per time step up to pressures of 1 to 50 MPa representing the
276 heated fluid in the autoclave.

277

278 2.3. Methods of analysis and representation

279 During the progression of the experiments the concentration in the fluid changes as a
280 function of advection and diffusion and the composition of the mineralogy of the solid
281 changes representing the exchange reaction. We show these changes in two ways,
282 as 2-dimensional plots of the experiments showing the concentration change (fig. 2c)
283 and the replacement reaction (fig. 2d, fig. 3) as well as profiles through the centre of
284 the solid square recording both, concentration and replacement for single time steps
285 (fig. 2e, fig. 4). Concentration changes in the 2-dimensional plots are shown in a
286 linear colour-scale between blue (0%) and red (100%) and the replacement reaction
287 is shown in a stepped colour scale between green (0-85%) and brown (85– 00%) to
288 visualize the reaction front morphology. The reaction front morphology is described
289 as smooth, irregular, rough, and replaced as a function of the amplitude of the
290 boundary roughness relative to the average grain size representing the wavelength
291 of the signal (fig. 3). If the amplitude/wavelength ratio is below 0.5 the roughness is
292 defined as smooth, if the ratio is between 0.5-1.5 it is defined as irregular, and if it is
293 above 1.5 the boundary is defined as rough. If the reaction front is absent, i.e. it runs
294 across the whole aggregate, the pattern is referred to as replaced. We characterize
295 the transport using the Péclet number (eq. 1), with high Péclet representing
296 advection-dominated fluid infiltration, and low Péclet representing a more diffusion-
297 dominated system. The reaction is first represented by the reaction rate (so that it is
298 independent of transport) and plotted versus the Péclet number (figs. 5, 6). In a final
299 plot of non-dimensional phase-space the Damköhler I number (eq. 2) representing
300 the relative advection to reaction rate is plotted versus the Péclet number (fig. 7).

301

302 3. Results

303 3.1 Concentration and replacement pattern-development through time

304 Figure 3 shows the replacement of grains in the mineral aggregate through time for
305 three example simulations developing a smooth, irregular, and rough reaction front.
306 The brown dark-colour represents a high percentage of new mineral growth whereas
307 green represents a low percentage of new mineral growth. The first simulations (fig.
308 3a) show a reaction with a slow advection represented by a Péclet number of 10
309 where diffusion becomes important. The reaction rate is fast and the corresponding
310 Damköhler I number 10^{-3} . The second experiment (fig. 3b) shows a reaction with
311 medium to fast advection rate with a Péclet number of 75 and a fast growth with a
312 Damköhler I number of 10^{-3} . The third experiment (fig. 3c) shows a reaction with a
313 high Péclet number of 100 and a slow growth with a Damköhler I number of 10^{-4} . The
314 three experiments (fig. 3a-c) show different timescales of reaction front progression
315 and distinctly different reaction front roughness. The front in the first experiment (fig.
316 3a, slow advection, fast growth) is smooth, the front progresses relatively slowly over
317 20 minutes into the simulation box, while the reaction front becomes smeared out,
318 i.e. the width of the mixed reacted and unreacted material (green area in Fig. 3a)
319 increases, and the corners of the reaction front are rounded. The grain boundaries
320 cannot be seen signifying that there is no preferred reaction along grain boundaries.
321 The front in the second experiment (fig. 3b, medium-fast advection, fast growth) is
322 irregular on the scale of single grains, as the reaction front *enters* the grain
323 boundaries, i.e. there is a clear preference of reaction along grain boundaries. The
324 reaction front becomes visible at the boundaries after about 1.7 minutes and is then
325 filling out most of the box within 2-3 minutes. The front in the third experiment (fig. 3c,
326 fast advection, slow growth) is rough on the scale of several grains where the grain
327 boundaries are marked by reaction products. The reaction front enters the simulation
328 box after about 50 minutes and then fills out most of the box where the grain

329 boundary infiltration front is followed by an outer rim of fully reacted material. All
330 three simulations show a reaction front morphology that is not changing over time.
331 Figure 4 illustrates the difference between a concentration and a reaction profile
332 through the different experiments, with the profiles running along the x-axis and
333 through the centre of the simulation box (fig. 2). The dashed blue line shows the
334 relative fluid concentration infiltrating the sample, whereas the solid orange line
335 shows the relative growth of the new mineral (or the replacement), and both are
336 scaled to 100%. Figure 4a show an experiment with slow advection and fast growth
337 similar to experiment I in figure 3a, figure 4b shows an experiment with medium
338 advection and fast growth similar to experiment II in figure 3b and figure 4c shows an
339 experiment with fast advection but slow growth similar to experiment II in figure 3c.
340 Figure 4a shows an example that is diffusion dominated and has a fast growth
341 (relative to diffusion timescales). Diffusion leads to a smooth reaction front that is
342 blurred but still relatively narrow (see reaction front in inset). The simulation with fast
343 advection and fast growth on the other hand (fig 4b) shows a steep infiltration
344 gradient of the concentration that is followed by a similarly steep gradient of the
345 growth front. Therefore, these experiments show a thin, steep front (see reaction
346 front in inset) that infiltrates the sample and is irregular on the grain-scale.
347 Simulations with fast advection and slow growth (fig. 4c) show an advection
348 dominated step, where the fluid is infiltrating the material with some roughness at the
349 infiltration front due to fingering and grain boundary infiltration. This infiltration of
350 concentration is followed by a relatively slow growth with a minor gradient into the
351 sample. This slow growth results into an apparent preferential growth along the grain
352 boundaries over time and shows a very shallow slope as a relic of the initial
353 infiltration front (figs. 4d, e). Therefore, the resulting pattern will show a relatively
354 wide zone where the grain boundaries become visible and the front is very rough,
355 and infiltration and growth are almost completely coupled (see inset in fig. 4c).
356 Finally, a very fast reaction traces the advection completely and therefore has a very

357 steep front and leads to a complete reaction without minor porosity and thus
358 infiltration variations (fig. 4f).

359

360 3.2. Scaling of reaction front pattern as a function of Péclet number, reaction rates
361 and Damköhler number

362 In order to illustrate the different reaction front patterns that develop in the different
363 advection-diffusion-reaction scenarios we first plot a matrix of experiments in a
364 diagram of Péclet number versus the reaction rate on a broad (fig. 5) and then on a
365 more detailed scale (fig. 6) and finally show the patterns of the two dimensionless
366 numbers Péclet versus Damköhler I in phase-space (fig. 7). The extreme variation of

367 patterns on a broad scale is shown in figure 5 where a low Péclet number of 1
368 produces diffusion dominated rounded, smooth and relatively sharp reaction fronts.

369 For a very slow reaction rate of 10^{-8} m/s the pattern becomes rough on a very small
370 scale driven by the reaction. Towards Péclet numbers around 10, reaction front
371 propagation becomes more advection dominated resulting in a smooth, at corners
372 rounded reaction front. At Péclet numbers around 100 advection dominates and the
373 reaction front becomes irregular to rough. At fast reaction rates of 10^{-6} m/s the front is
374 irregular on the grain scale but towards slower reaction rates of 10^{-7} and 10^{-8} m/s the
375 front is rough, where grain boundaries start to show up and dominate the pattern.

376 Figure 7 shows a more detailed matrix of figure 6 illustrating the transition from
377 smooth through irregular and rough reaction front patterns. The matrix clearly
378 illustrates that increasing Péclet numbers from 10 towards 100 increases the
379 irregularity of the front. However, especially at higher Péclet numbers the reaction
380 rate becomes also important with fast reaction rates (10^{-6} m/s) producing a front with
381 irregularities on the grain-scale, whereas slow reaction rates (10^{-7} m/s) lead to rough
382 fronts with grain boundaries showing up in the reaction. The most extreme infiltration
383 takes place when the Péclet number is high and the reaction rate is low. The
384 variation of the pattern and the changing roughness of the interface can be illustrated

385 in phase-space of the two dimensionless numbers Péclet and Damköhler I (fig. 7).
386 Note that the Damköhler I number on the vertical axis is plotted from high to low
387 numbers to compare with literature data (Szymczak and Ladd, 2009). In the lower left
388 hand corner of the diagram at low Péclet and high Damköhler I numbers, the reaction
389 front is smooth (amplitude/wavelength ratio < 0.5). At lower Damköhler I
390 accompanied by higher Péclet numbers, the reaction front becomes irregular on the
391 single grain-scale (ratio between 0.5-1.5). The boundary between a smooth and
392 irregular front is almost diagonal across the diagram. The zone where the reaction
393 front is irregular curves around from low Damköhler I to high Péclet numbers.
394 Towards the upper right-hand corner of the diagram the pattern becomes rough (ratio
395 > 1.5) and is dominated by multi-grain boundary infiltration. In the uppermost right-
396 hand corner of the diagram (ratio > 10) complete infiltration or replacement occurs.
397 The phase-boundaries illustrate an increase of roughness with increasing Péclet
398 number from Péclet 10 to 100 but then a decrease in roughness towards higher
399 Péclet numbers controlled by the Damköhler I number.

400

401 4. Discussion

402 4.1. General model behaviour

403 Our numerical simulations illustrate different scenarios that produce rough, irregular
404 and smooth reaction fronts. In the most extreme cases of “roughness” all grain
405 boundaries in the aggregate are marked by reaction products, a pattern that is very
406 similar to replacement reactions in fossils, sedimentary basins and metamorphic
407 terrains. Advection is the main driving force for fluid infiltration into the system and for
408 the development of roughness due to more permeable grain boundaries and
409 advection fingering (Jonas et al., 2014; Kar et al., 2015; Plümper et al., 2017;
410 Beaudoin et al., 2018). Advection, however, is not always enough to produce very
411 rough fronts. In the case of complete infiltration, the roughness only develops
412 significantly if the reaction is slow. This is related to the fact that a fast reaction will

413 follow the infiltration front and will only be able to superimpose the local anisotropic
414 advection on the grain-scale or on the scale of advective fingers. However, if the
415 reaction is slow, the mineral growth front into the material does not represent the
416 advection front moving inwards, but rather the anisotropy of the grain boundary
417 infiltration. The growth has a memory effect of the advective infiltration and preserves
418 this pattern when it slowly replaces the whole aggregate. We envisage that this
419 scenario can produce replacement of large bodies, by infiltrating them through
420 advection followed by a slow growth that preserves heterogeneity of the rocks, even
421 though the material is replaced. In this case the reaction does show the differential
422 permeability of the rock but not the actual fluid infiltration, even though advection is
423 still needed to attain a memory effect of the rock fabric. A slow reaction after
424 infiltration also means that if the reaction fills pore-space and reduces the
425 permeability, it is not clogging the fluid pathway, at least for one single infiltration
426 event as modelled here. However, there is no reason why multiple fluid infiltration
427 events in a cyclic manner into the material do not produce very similar structures to
428 our simulations. The simulations have several timescales defined by the pressure
429 diffusion equation, the external boundary condition of ramping up the pressure, the
430 associated fluid velocity, and the diffusion timescale. Diffusion-time scales as a
431 function of the diffusion coefficient divided by the length scale squared. For the
432 pressure equation this gives a time of roughly one second to diffuse the pressure into
433 the experimental sample of 2.5 mm. In this case the external boundary condition of
434 ramping up the pressure becomes important, because every increase in pressure
435 leads to a new fluid pressure diffusion into the sample. The pressure ramping up
436 takes 2 to 3 minutes and this timescale is then controlling the flux of material into the
437 sample. In this case the fluid velocity from equation 6 gives a velocity of 10^{-6} mm/sec
438 for the initial advection. Since the fluid velocity is dependent on the pressure gradient
439 this velocity goes up linearly with an increase of the pressure at the boundary, if this
440 increase is faster than the pressure diffusion timescale, which it is in the simulations.

441 A pressure gradient of 1MPa/model-unit then leads to a fast infiltration of matter
442 through advection filling the box within one minute. The pressure diffusion timescale
443 becomes much smaller for larger systems with a time scale of 18 seconds for a cm
444 size domain, 50 hours for a meter size domain and 60 years for a reservoir-type
445 domain of 100m. The matter-diffusion timescale into the system is in the order of
446 7min for a domain of 0.2mm and 44 days for the whole experimental domain of
447 2.5mm.

448

449 4.2. Comparison of results to experimental replacement reactions

450 In this section we compare the numerical simulations with results from replacement
451 experiments. In many replacement-reaction experiments the setup is similar to the
452 numerical setup presented here, where a square piece of material is exposed by a
453 reactive fluid at all four sides and the replacement reaction is monitored through time.
454 Here we present two sets of replacement experiments in which polycrystalline
455 Carrara marble (pure white marble from Carrara, Italy, 99.7% calcite, average grain
456 size diameter of 100 μm) cut into regular cubes (2-3 mm), is replaced by calcium
457 phosphates. Experiments were performed following previously published protocols
458 (Kasioptas et al., 2008; Pedrosa et al., 2016) where samples are immersed into a
459 reactive fluid and inserted into a hydrothermal autoclave at temperatures of 180°C.
460 Only the reaction rate of the replacement varied by reacting the marble with either
461 (set 1) fluorine-containing phosphate solutions (1.0 M $(\text{NH}_4)_2\text{HPO}_4$ + 0.1 M NH_4F) or
462 (set 2) sodium chloride-containing phosphate solutions (1.0 M $(\text{NH}_4)_2\text{HPO}_4$ + 0.5 M
463 NaCl). Set 1 shows a reaction that proceeds normal to the outer perimeter of the
464 sample with fast reaction rates, the sample being [half](#) replaced in about 5 days and
465 the interface being rough on the grain scale (fig. 8a). Set 2 experiments show a slow-
466 moving reaction with only 10% of the sample replaced after [15](#) days and the reaction
467 being primarily associated with grain boundaries and fractures in the sample (fig. 8c).
468 Figure 8a and c show the experiments of Set 1 (fig. 8a) and Set 2 after [5 days](#) (fig.

469 8c) compared to two simulations (fig. 8b and d). The simulations mimic the patterns
470 of the replacement reactions very well with simulation shown in figure 8b showing a
471 small roughness on the grain boundary scale whereas the simulation shown in figure
472 8d shows infiltration along grain boundaries along the rim of the experimental charge.
473 The settings for the simulation shown in figure 8b is set to model fast reaction rate,
474 and fast advection and fast growth (Fig. 6) resulting in a rough front on the grain
475 scale whereas the simulation shown in figure 8d is set to model slow reaction rate
476 coupled with fast advection relative to slow growth i.e. high Pe number resulting in
477 strong grain boundary infiltration (fig. 5). One has to note however, that the time
478 scales in the numerical simulations and the experiments are not the same with the
479 experiments taking longer (days) than the simulations (minutes to hours). This
480 discrepancy may be present due to the lack of data on the exact setting of the
481 experiments in terms of external pressure, temperature gradients, reaction rates as
482 well as diffusion constants. The experiments are still within a time frame where
483 diffusion is only present at small scales, and the slow reaction of experiment two
484 could be reproduced in the model. However, experiment one with sharp reaction
485 front has a faster advective timescale in the simulations in the order of a couple of
486 minutes driven by ramping fluid pressure boundary. An additional parameter may
487 slow down this advection in the experiments, potentially through a reaction that
488 changes the porosity. An alternative advective transport mechanism that is not
489 pressure-driven is chemically-driven convective-flow into dead-end pores through
490 transient diffusioosmosis (Kar et al., 2015). This process leads to fluid velocities of 10
491 to 50 micrometers/second, so that fluid could infiltrate the experimental setup within
492 minutes. Even though this driving mechanism is different, the resulting patterns
493 should look similar to those of our simulations. However, the timescales may vary.

494 [In order to compare the experiments better with the simulations we estimate the](#)
495 [infiltration velocity into the experimental samples, calculate Péclet and Damköhler](#)
496 [numbers and compare them to simulations \(fig. 8e-h\). We model the infiltration](#)

497 velocity by considering temperature diffusion into the sample as a function of the
498 temperature of the autoclave (180°C) and the temperature in the sample (20°C)
499 using a simple one-dimensional finite difference approach (T-diffusion constant at
500 low porosity $10^{-9}\text{m}^2/\text{s}$). The temperature is then used to calculate the local fluid
501 pressure that progresses into the sample and the pressure gradient from the
502 boundary towards the centre using the bulk Modulus of water G (2 GPa) and the
503 coefficient of thermal expansion α (0.00006 K^{-1}) as $\delta P = \delta T \frac{\alpha}{1/G}$. The pressure
504 gradient is then used to determine the fluid velocity or infiltration velocity using
505 equation 6 (fig. 8e). We then can derive the **Péclet** number for the experiments and
506 using the time scale of the reaction from Figure 8b,d **allows us to** determine the
507 Damköhler number as well (fig. 8g). For the simulations we use the progression of
508 the infiltration front as a function of time to determine the velocity directly (fig. 8f). The
509 velocity is then also used to determine the **Péclet** number and the velocity of the
510 reaction front can be used to determine the Damköhler number (fig. 8h). This gives
511 us a direct comparison of the experiments and the simulations with the fluid
512 infiltration decaying in both examples where the experimental infiltration velocity
513 seems to be higher. In **addition**, the infiltration slows down completely in the
514 simulations after 200 seconds whereas the infiltration takes longer in the
515 experiments. However, the overall behaviour is similar with both simulations and
516 experiments having an infiltration velocity that decays over time as a function of the
517 fast driving processes in the beginning followed by a diffusion like decay. The plots of
518 Damköhler versus **Péclet** number show a very similar trend between experiment and
519 simulation with both showing a decay in **Péclet** number as a function of the slowing
520 down infiltration velocity and an increase in Damköhler number because of this. The
521 Damköhler numbers of the slow simulation are not as low as those of the slow
522 experiment illustrating the mentioned fact that the growth in the experiments is
523 slower than the growth in the simulations.

524

525 4.3. Applicability of results to natural examples and use of reaction front pattern in
526 determining relative rates of reaction, advection and diffusion

527 Our experiments show that reaction patterns in rocks can be used as a toolbox to
528 understand paleo-reaction and transport rates. For example, figure 1a shows a

529 natural example of a reaction around a fracture in a sandstone where Fe^{3+} is reduced
530 to Fe^{2+} . The pattern is frozen in time and shows an irregularly rough front, either with

531 a low Péclet number of around 10 or a higher Péclet number and a higher Damköhler
532 number I of around 10^{-3} . Figure 1b shows a dolomitization front with the darker lower

533 part of the rock being dolomitized with low porosity whereas the upper part has a
534 high porosity and is not dolomitized. The front is rough and mimics a fluid infiltration

535 that is frozen into the rock record by the reaction. The infiltration into the rock seems
536 to be more driven by fractures/sedimentary layer boundaries than grain boundaries.

537 According to our study this pattern needs a high Péclet number so that advection
538 dominates the transport mechanism and an intermediate to low Damköhler number

539 so that the anisotropy in permeability along for example grain boundaries or fractures
540 is preserved by the reaction. Figure 1c shows a naturally occurring dolomitization

541 front (brownish in outcrop) within a carbonate. The reaction front is rough on the
542 scale of several grains. This pattern would need a Péclet number larger than 100 and

543 a low Damköhler number in the range of 10^{-4} (Fig. 7).

544 The Damköhler number also influences the alteration of pore-space in reservoir
545 rocks where the rocks dissolve homogeneously at a high Péclet and low Damköhler I

546 number similar to patterns that we see in our reactions (Mostaghimi et al., 2016). A
547 difference occurs at high Damköhler numbers that leads to the development of large

548 channels and a high porosity in the model of Mostaghimi et al. (2016). This is also in
549 contrast to wormhole formation, where a high Damköhler I number hinders the

550 localization and thus formation of wormholes with the front being smooth (Szymczak
551 and Ladd, 2009), which is similar to our patterns. In summary it is important to notice

552 that what we see in the rock record as reaction patterns is a function of both, the
553 rates and mode of transport and reaction. The presented work shows the complexity
554 of the interplay of these processes. Coupling the influence of both processes to a
555 dynamic porosity promises to provide a toolbox that can be used as a deductive and
556 predictive tool for (paleo-) fluid-flow and reaction, reservoir evolution, ore body
557 formation and in general fluid-rock interaction in the Earth's crust.

558

559 5. Conclusion

560 In this contribution we modelled the infiltration of fluid into a small rock sample (2.5 x
561 2.5 x 2.5 mm) with permeable grain boundaries, with mass transport as a function of
562 advection and diffusion and a consecutive reaction. Advection-dominated infiltration
563 produces irregular to rough boundaries with grain boundary infiltration and fingering,
564 whereas diffusion-dominated transport favours smooth boundaries. In addition, the
565 rate of the reaction relative to the fluid infiltration process is crucial where fast
566 reaction produces reaction fronts that are smooth or only irregular on the grain
567 boundary scale whereas slow reactions memorize the anisotropy of the infiltration
568 process, develop rough interfaces and produce a grain boundary network. These
569 patterns can also be illustrated in non-dimensional phase-space using the Péclet and
570 Damköhler I numbers, with smooth fronts at low Péclet and irregular to rough fronts
571 at high Péclet and low Damköhler numbers. In the extreme case at very high Péclet
572 and low Damköhler numbers the complete grain boundary network can be
573 reproduced by the reaction in a manner that is reflecting a replacement process. Our
574 study indicates that a dominating advection process as well as a slow reaction are
575 important for rough fronts. We show that our results mimic patterns found in
576 experiments and in nature and argue that replacement reactions of large areas that
577 preserve the initial rock texture (fossils, sedimentary or crystalline structures) may be
578 driven by initial advection of fluids into the system followed by a slow reaction that
579 "freezes" the initial pattern. Our results indicate that what we observe as patterns in

580 rocks is not only a function of transport mechanisms but also and importantly its
581 dynamic interplay with reaction and reaction rates.

582

583 Data availability

584 The simulation input and output data used to support the findings of this study are
585 available from the corresponding author upon request. The basic software for the
586 simulations can be found and downloaded at <http://elle.ws> and the corresponding
587 author will make the additional code available upon request.

588

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597 References

598 Ague, J.J., 2003. Fluidflow in the deep crust. In: Holland, H.D., Turekian, K.K.,
599 Rudnick, R.L (Eds.), Treatise on Geochemistry, vol. 3. The Crust. Elsevier, Amsterdam,
600 pp. 195–228.

601

602 Austrheim, H., 1987. Eclogitization of lower crustal granulites by fluid migration
603 through shear zones. Earth Planet. Sci. Lett. 81, 221–232.

604

605 Ascher, U.M., Ruuth, S.J., Spiteri, R.J., 1997. Implicit-Explicit Runge-Kutta Methods
606 for Time-Dependent Partial Differential Equations, Appl Numer Math, vol. 25(2-3).

607

608 Beaudoin N., Hamilton, A., Koehn, D., Shipton, Z.K., Kelka, U., 2018. Reaction-
609 induced porosity fingering: replacement dynamic and porosity evolution in the KBr-
610 KCl system. *Geochimica et Cosmochimica Acta*, 232, 163-180.
611
612 Bons, P.D., Koehn, D., Jessell, M.W., 2008. *Microdynamics Simulation*. Springer
613 *Lecture Series in Earth Sciences*, pp. 406.
614
615 Carman, P.C., 1937. Fluid flow through granular beds. *Trans. Inst. Chem. Eng.* 15,
616 150.
617
618 Centrella, S., Austrheim, H., Putnis, A., 2016. Mass transfer and trace element
619 redistribution during hydration of granulites in the Bergen Arcs, Norway. *Lithos* 262,
620 1-10.
621
622 Chadam, D., Hoff, D., Merino, E., Ortoleva, P., Sen, A., 1986. Reactive infiltration
623 instabilities. *IMA J Appl Math.* 36, 207–21.
624
625 Chen, L., Kang, Q., Robinson, B.A., He, Y.-L., Tao, W.-Q., 2013. Pore-scale
626 modeling of multiphase reactive transport with phase transitions and dissolution-
627 precipitation processes in closed systems. *Phys Rev E* 87(4):043306
628
629 Chen, L., Kang, Q., Carey, B., Tao, W.-Q., 2014. Pore-scale study of diffusion-
630 reaction processes involving dissolution and precipitation using the lattice Boltzmann
631 method. *Int J Heat Mass Tran* 75:483–496
632
633 Fredrich J.T., DiGiovanni A.A., Noble D.R., 2006. Predicting macroscopic transport
634 properties using microscopic image data. *J Geophys Res-Sol Ea* 111(B3)
635

636 Ghani, I., Koehn, D., Toussaint, R., Passchier, C. W., 2013. Dynamic development of
637 hydrofracture. *Pure Appl. Geophys.* 170, 1685–1703.
638
639 Ghani, I., Koehn, D., Toussaint, R., Passchier, C., 2015. Dynamics of hydrofracturing
640 and permeability evolution in layered reservoirs. *Front. Phys.* 3, 67.
641
642 Gomez-Rivas, E., Bons, P. D., Urai, J. L., Arndt, M., Virgo, S., Laurich, B., Zeeb, C.,
643 Stark, L., Blum, P., 2014. The Jabal Akhdar Dome in the Oman Mountains:
644 devolution of a dynamic fracture system. *American Journal of Science*, 314, 1104-
645 1139.
646
647 Hilgers C., Urai, J., 2002. Experimental study of syntaxial vein growth during lateral
648 fluid flow in transmitted light, first results. *Journal of Structural Geology*, 24, 1029-
649 1043.
650
651 Jamtveit B, Meakin P., 1999. Growth, Dissolution and Pattern Formation in
652 Geosystems. Dordrecht: Springer
653
654 Jamtveit, B., Austrheim, H., Malthe-Sørensen, A., 2000. Accelerated hydration of
655 the Earth's deep crust induced by stress perturbations. *Nature* 408, 75-78.
656
657 Jamtveit, B., Putnis, C.V., Malthe-Sørensen, A., 2009. Reaction induced fracturing
658 during replacement processes. *Contributions to Mineralogy and Petrology*, 157, 127-
659 133.
660
661 Jonas, L., John, T., King, H. E., Geisler, T., & Putnis, A., 2014. The role of grain
662 boundaries and transient porosity in rocks as fluid pathways for reaction front
663 propagation. *Earth and Planetary Science Letters*, 386, 64-74.

664

665 Kang Q., Chen L., Valocchi AJ, Viswanathan H.S., 2014. Pore-scale study of
666 dissolution-induced changes in permeability and porosity of porous media. J Hydrol
667 517:1049–1055

668

669 Kar, A., Chiang, T. Y., Ortiz Rivera, I., Sen, A., & Velegol, D., 2015. Enhanced
670 transport into and out of dead-end pores. ACS nano, 9(1), 746-753.

671

672 Kasiopas, A., Perdikouri, C., Putnis, C. V., Putnis, A., 2008. Pseudomorphic
673 replacement of single calcium carbonate crystals by polycrystalline apatite. Mineral.
674 Mag. <http://dx.doi.org/10.1180/minmag.2008.072.1.77>.

675

676 Koehn, D., Arnold, J., Malthe-Sørenssen, A., Jamtveit, B., 2003. Instabilities in
677 stress corrosion and the transition to brittle failure. Am. J. Sci. 303, 956–971.

678

679 Koehn, D., Arnold, J., Passchier, C. W., 2005. Fracture and Vein Patterns as
680 Indicators of Deformation History: a Numerical Study. Geological Society, London,
681 pp. 11–24 Special Publications 243.

682

683 Koehn, D., Steiner, A., Aanyu, K., 2019. Modelling of extension and dyking-induced
684 collapse faults and fissures in rifts. Journal of Structural Geology, 118, 21-31.

685

686 Kondratiuk, P., Tredak, H., Upadhyay, V., Ladd, A. J., & Szymczak, P., 2017.
687 Instabilities and finger formation in replacement fronts driven by an oversaturated
688 solution. Journal of Geophysical Research: Solid Earth, 122(8), 5972-5991.

689

690 Lax, P. D., Wendroff, B., 1960. Systems of conservation laws. Commun. Pure Appl.
691 Math., **13**, pp. 217–237

692

693 Lipsey, L., Pluymaekers, M., Goldberg, T., van Oversteeg, K., Ghazaryan, L.,
694 Cloetingh, S., van Wees, J.-D., 2016. Numerical modelling of thermal convection in
695 the Luttelgeest carbonate platform, the Netherlands. *Geothermics* 64, 135-151.

696

697 Manwart C., Aaltosalmi U., Koponen A., Hilfer R., Timonen J., 2002. Lattice-
698 Boltzmann and finite-difference simulations for the permeability for three-dimensional
699 porous media. *Phys Rev E* 66(1):016702

700

701 Merino, E. and Canals, A., 2011. Self-Accelerating Dolomite-for-Calcite
702 Replacement: Self-Organized Dynamics of Burial Dolomitization and Associated
703 Mineralization. *American Journal of Science* 311, 573-607.

704

705 Mostaghimi, P., Liu, M., Arns, C.H., 2016. Numerical Simulation of Reactive
706 Transport on Micro-CT Images. *Math Geosci*, 48: 963-983.

707

708 Pedrosa, E. T., Putnis, C. V., & Putnis, A., 2016. The pseudomorphic replacement of
709 marble by apatite: The role of fluid composition. *Chemical Geology* 425, 1-11.

710

711 Plümpner, O., Botan, A., Los, C., Liu, Y., Malthe-Sørensen, A., & Jamtveit, B., 2017.
712 Fluid-driven metamorphism of the continental crust governed by nanoscale fluid flow.
713 *Nature geoscience*, 10(9), 685-690.

714

715 Putnis, A. and Putnis, C.V., 2007. The mechanism of re-equilibration of solids in the
716 presence of a fluid phase. *Journal of Solid State Chemistry* 180, 1783-1786.

717

718 Putnis A., 2009. Mineral replacement reactions. *Reviews in Mineralogy and*
719 *Geochemistry*, 70, 87-124.

720

721 Putnis, A. and Austrheim, H., 2010. Fluid-induced processes: metasomatism and
722 metamorphism. *Geofluids* 10, 254-269.

723

724 Rochelle, C. A., Czernichowski-Lauriol, I., & Milodowski, A. E., 2004. The impact of
725 chemical reactions on CO₂ storage in geological formations: a brief review.
726 Geological Society, London, Special Publications, 233(1), 87-106.

727

728 Rudge, J. F., Kelemen, P. B., & Spiegelman, M., 2010. A simple model of reaction-
729 induced cracking applied to serpentinization and carbonation of peridotite. *Earth and*
730 *Planetary Science Letters*, 291(1-4), 215-227.

731

732 Ruiz-Agudo, E., Putnis, C. V., Putnis, A., 2014. Coupled dissolution and precipitation
733 at mineral-fluid interfaces. *Chemical Geology* 383, 132-146.

734

735 Ruiz-Agudo, E., King, H. E., Patino-Lopez, L. D., Putnis, C. V., Geisler, T.,
736 Rodriguez-Navarro, C., Putnis, A., 2016. Control of silicate weathering by interface-
737 coupled dissolution- precipitation processes at the mineral-solution interface.
738 *Geology*, 44, 567-570.

739

740 Ortoleva, P., Chadam, J., Merino, E., and Sen, Z., 1987. Geochemical self-
741 organization ii: the reactive-infiltration instability, *Am. J. Sci* 287, 1008.

742

743 Sachau, T., Koehn, D., 2010. Faulting of the lithosphere during extension and rift-
744 flank uplift: a numerical study. *Int. J. Earth Sci.* 99, 1619–1632.

745

746 Sachau, T., Koehn, D., 2013. A new mixed-mode fracture criterion for large scale
747 lattice models. *Geosci. Model Dev.* 7 (1), 243–247.

748

749 Saripalli K.P., Meyer P.D., Bacon D.H., Freedman V.L., 2001. Changes in hydrologic
750 media due to chemical reactions: a review critical reviews. *Environ Sci Tech*
751 31(4):311–349

752

753 Shabro V., Torres-Verdín C., Javadpour F., Sepehrnoori K., 2012. Finite-difference
754 approximation for fluid flow simulation and calculation of permeability in porous
755 media. *Transport Porous Med* 94(3):775–793.

756

757 Szymczak, P. and Ladd, A.J.C., 2009. Wormhole formation in dissolving fractures.
758 *Journal of Geophysical Research* 114.

759

760 Tartakovsky A. M., Meakin P., 2006. Pore scale modeling of immiscible and miscible
761 smoothed particle hydrodynamics. *Adv Water Resour* 29(10):1464–1478

762

763 Ulven, O. I., Jamtveit, B., Malthe-Sørenssen, A., 2014. Reaction-driven fracturing of
764 porous rock, *Journal of Geophysical Researc, Solid Earth*, 119, 7473-7486.

765

766 Yardley, B.W.D. and Cleverley, J.S., 2013. The role of metamorphic fluids in the
767 formation of ore deposits. *Journal of the Geological Society London, Special*
768 *Publications* 393.

769

770 Zhao, C., Hobbs, B. E., Hornby, P., Ord, A., Peng, S., Liu, L., 2007. Theoretical and
771 numerical analyses of chemical-dissolution front instability in fluid-saturated porous
772 rocks, *Numerical and Analytical Methods in Geomechanics*, 32, 1107-1130.

773

774 Figure Captions

775 Figure 1. Two examples of reaction textures in natural examples that illustrate the
776 importance of advection. a) Bleaching reactions around a fracture network in red
777 sandstone on the Isle of Cumbrae in Scotland. The reacting fluid clearly came along
778 a fracture network and then affected an area around the fractures. b) Reaction front
779 from the Parnozany mine in Poland. The light top area in the picture is composed of
780 porous dolomite whereas the dark material is composed of very dense dolomite with
781 ore minerals at the bottom of the section. In this case the front is very rough and
782 follows a fracture network upwards and then infiltrates in bedding planes and
783 stylolites sideways. Even though the pattern shows a reaction it does look like the
784 image of an infiltrating fluid. c) Dolomitization front details with dolomitized material
785 on the left-hand side in a brown colour. The sample is from a zone of fluid driven
786 dolomitization with associated ore deposits in the Oropesa Ranges near Benicassim,
787 Spain. On the sub-centimetre scale, the mineralization front is rough with infiltration
788 along grain-boundaries or zones of smaller grains.

789 Figure 2. Illustration of the numerical model setup. a) 2D setup of the model where
790 fluid and concentration are set at the boundaries with the concentration a constant
791 and the fluid pressure increasing to produce a constant flux into the model. Grain
792 boundary network with permeable grain boundaries appear in lighter colour. b)
793 Numerical calculations loop in the model with the input from the grain aggregate
794 (porosity/permeability) and the boundary pressure, then the fluid pressure evolution
795 that gives the Darcy velocity followed by the mass transport equations related to
796 advection and diffusion and finally the reaction. c) Concentration change into the
797 model after a number of model runs; d) Related growth or mineral replacement
798 patterns; e) 1D profile of the fraction of the maximum concentration (dotted blue line)
799 and fraction of complete replacement profile (solid orange line) at a given time,
800 represented as a function of the particle position along a line passing through the
801 middle of the simulations (reported on c, d).

802

803 Figure 3. Three simulations with variably rough reaction fronts and images showing
804 the mineral growth over time. a) Simulation 1 shows a slow advection where diffusion
805 becomes important producing smooth interfaces and rounded corners. b) Simulation
806 2 shows a medium advection and a fast growth so that the developing structures are
807 irregular on the grain scale. c) Simulation 3 shows a faster advection and much
808 slower growth so that the final growth features accentuate the grain boundaries in a
809 relatively wide zone and the reaction front is rough.

810

811 Figure 4. 1D profiles of the relative infiltration of the fluid concentration (fraction of
812 maximum concentration) into the model (dotted blue line) and the following growth
813 front (solid orange line, fraction of complete volume reacted) following a horizontal
814 line crossing the model as illustrated on fig. 2c, d. a-f profiles relate to a number of
815 different models at variable time steps. a-c) Fast growth that keeps up either with
816 advection or diffusion and thus mainly covers the incoming front. d-f) Difference
817 between the advective front coming in fast followed by a very slow reaction front with
818 a small slope inwards that can capture and enhance the grain boundary network.

819

820 Figure 5. The developing reaction patterns on a rough scale in Péclet number versus
821 reaction rate space. Rough reaction interfaces develop towards high Péclet numbers
822 and slow reactions. Smooth and progressively rounded patterns develop in the low
823 Péclet number domain where diffusion is dominating.

824

825 Figure 6. Magnified and more detailed version of fig. 5 at the transition between
826 smooth and rough reaction interfaces. The matrix shows that an increase in Péclet
827 number in general leads to an increase in the roughness with an important transition
828 after a Péclet number of about 50. However, the figure also illustrates that in order to
829 develop a reaction front with significant roughness that is on a larger scale than the
830 grains the reaction needs to be slower than about 5×10^{-7} m/s.

831

832 Figure 7. Evolution of the different reaction patterns in non-dimensional phase space
833 of Péclet versus Damköhler I numbers. The roughness is defined by the
834 amplitude/wavelength ratio of the signal (number next to dashed lines). Four main
835 areas of patterns can be seen, smooth interfaces at the lower left-hand corner with
836 low Péclet and high Damköhler I numbers (yellow zone). This zone is followed by a
837 zone with irregular interfaces that curves from low Damköhler I numbers down and
838 then up again towards high Péclet numbers (green zone). Rough interfaces on the
839 scale of several grains are shown in the blue zone at high Péclet and low Damköhler
840 I and a full replacement with rough growth across more than 10 grains is shown in
841 red at the uppermost corner of the diagram. Data points are shown as black dots with
842 example images of interfaces.

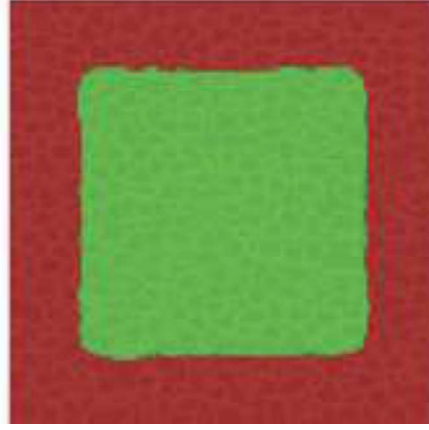
843

844 Figure 8. Experimentally produced patterns versus the simulations. a) Back-scattered
845 SEM (Scanning Electron Microscope) image of a cross section of a Carrara marble
846 sample after a replacement experiment where the fluid infiltrates the material from
847 the sides and the reaction takes place parallel to the boundaries with a minor
848 roughness that develops on the grain boundary scale. Unreacted calcite grains are
849 grey, reaction products are white. b) Simulation that produces the same pattern at a
850 Péclet number between 75 and 500 and a Damköhler I number of 10^{-3} . In this case
851 the high Péclet number indicates that the transport is advection dominated whereas
852 the Damköhler number indicates that the reaction is relatively fast. c) Back scatter
853 SEM image of a cross section of a Carrara marble sample after a replacement
854 experiment where the fluid infiltrates from the lower and the left hand side boundaries
855 (the figure shows the lower left hand corner of an experiment with a similar setup to
856 a)). The reaction takes place mainly along the grain boundaries. Unreacted calcite
857 grains are grey, reaction products are white. d) Simulation with a similar setting to c
858 where the grain boundaries react. In this case the Péclet number is about 500 and

859 the Damköhler I number 10^{-4} . The transport is advection dominated but the reaction
860 is relatively slow. [e\) Modelled infiltration velocity for the experiments as a function of](#)
861 [time \(see text for derivation\).](#) [f\) Infiltration in a simulation determined from the](#)
862 [infiltration front progression over time.](#) [g\) Plot showing Damköhler versus Péclet](#)
863 [number for the two experiments. Both experiments show a decrease in Péclet and an](#)
864 [increase in Damköhler numbers over time.](#) [h\) Damköhler versus Péclet number for a](#)
865 [slow simulation showing the same decrease in Péclet over time that can be observed](#)
866 [in the experiments.](#)
867

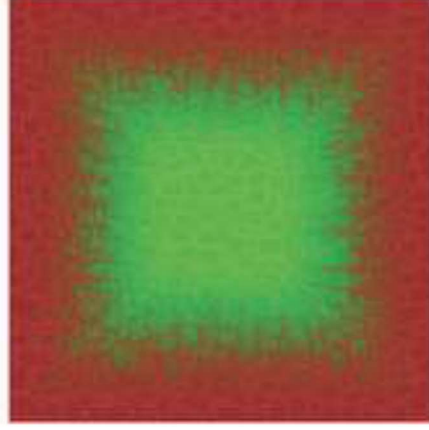
Flow and Reaction Matter

fast growth, slow advection

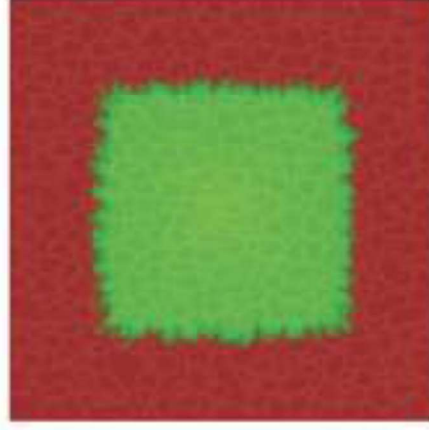


smooth

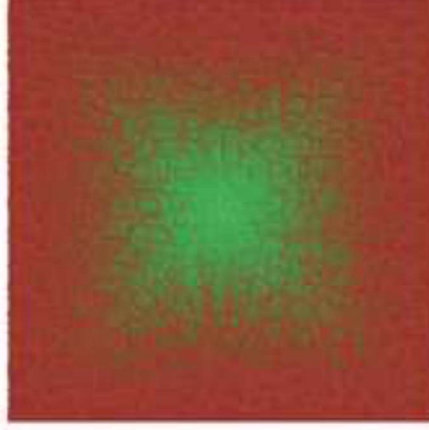
slow growth, fast advection



rough



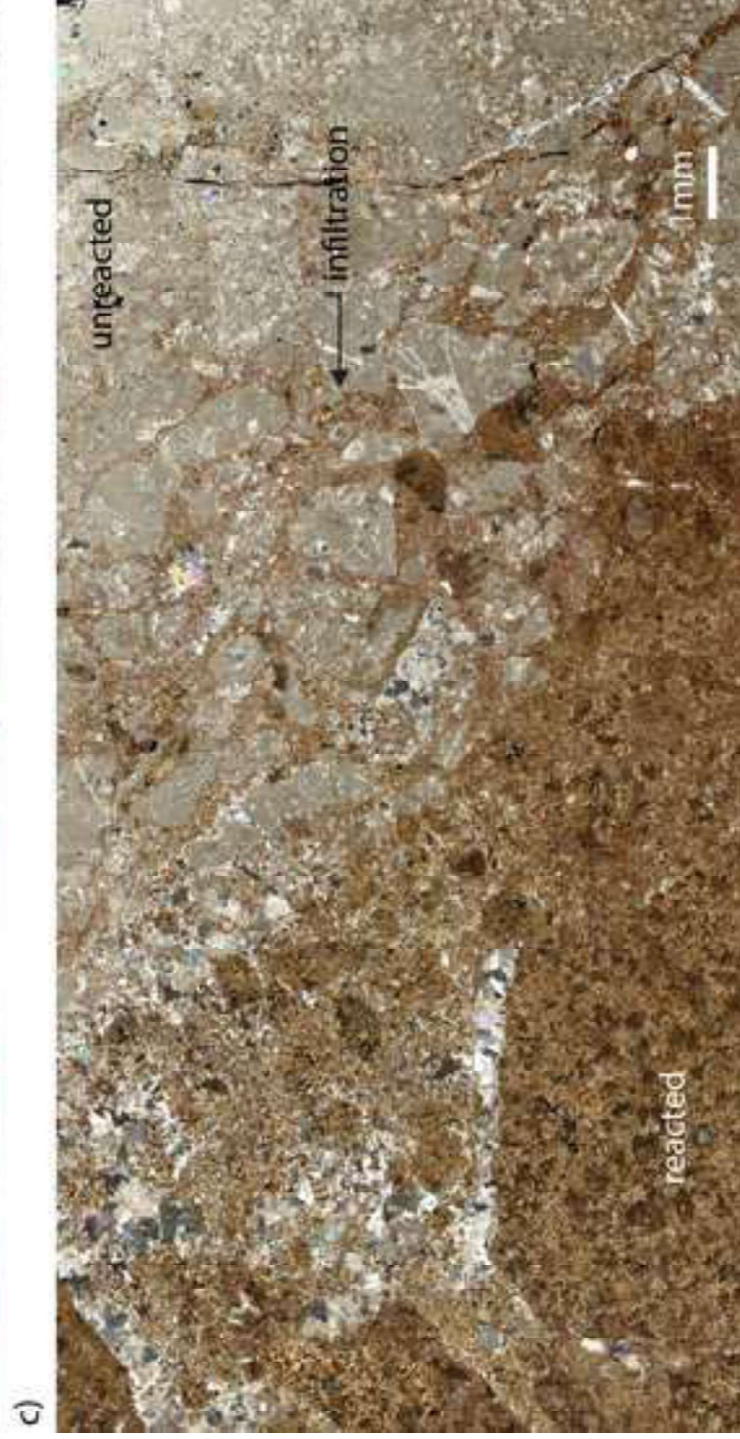
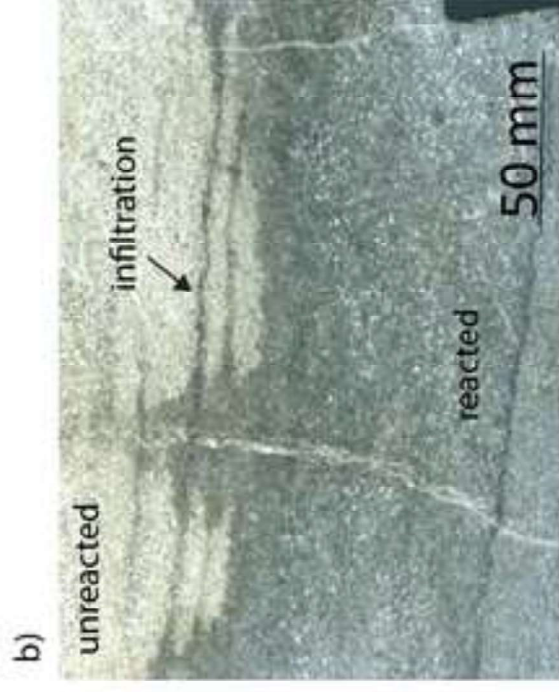
irregular

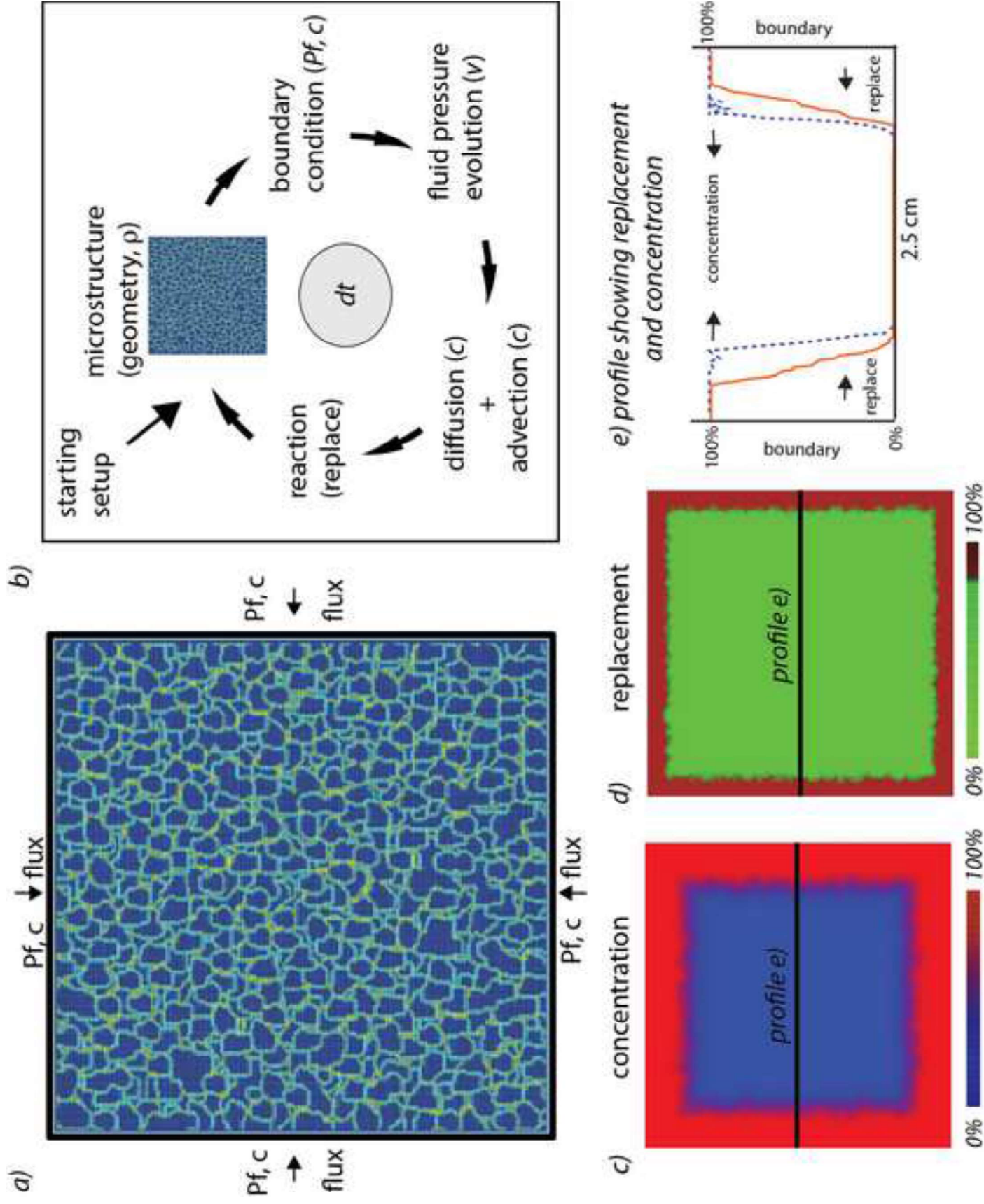


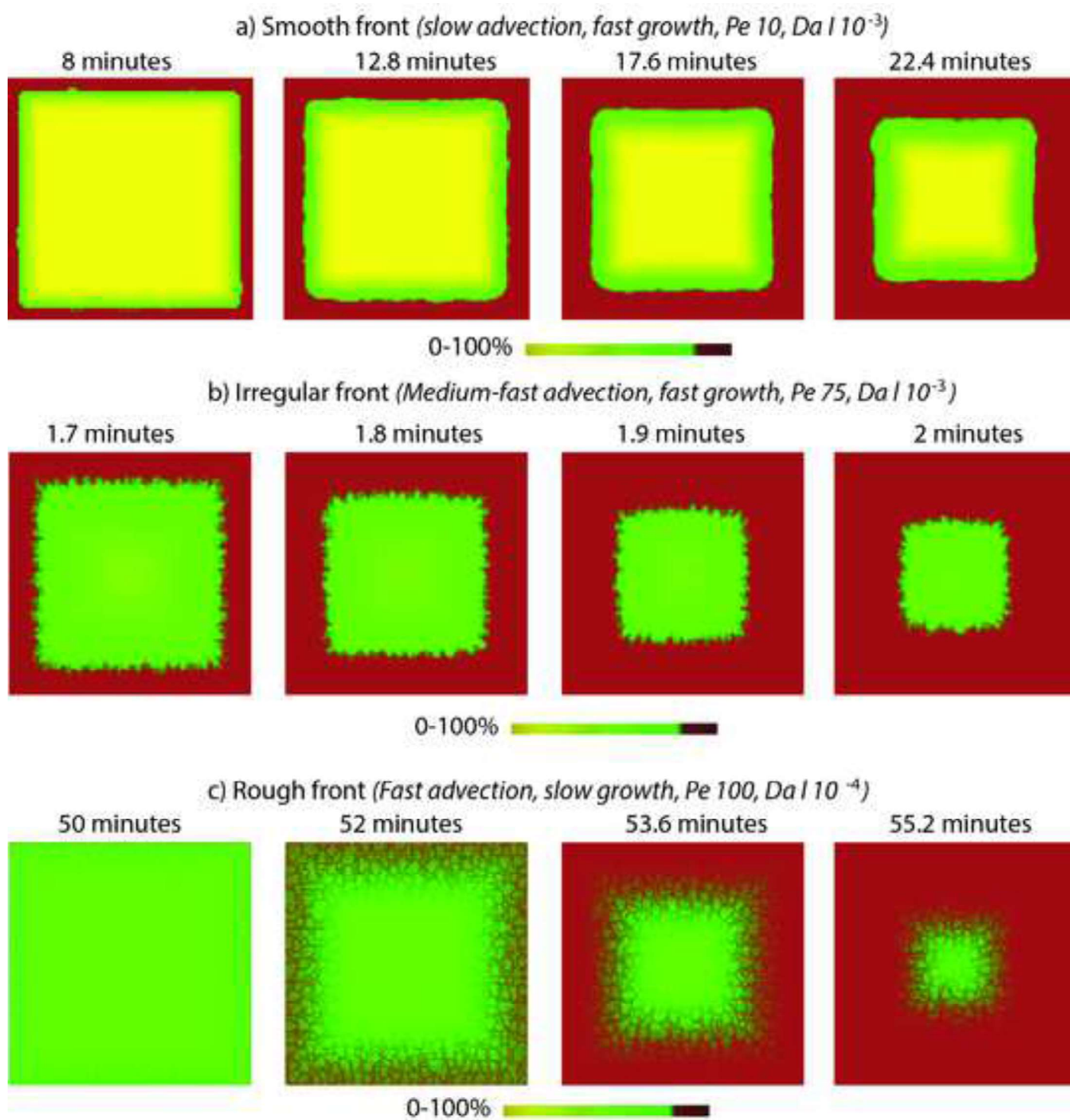
replaced

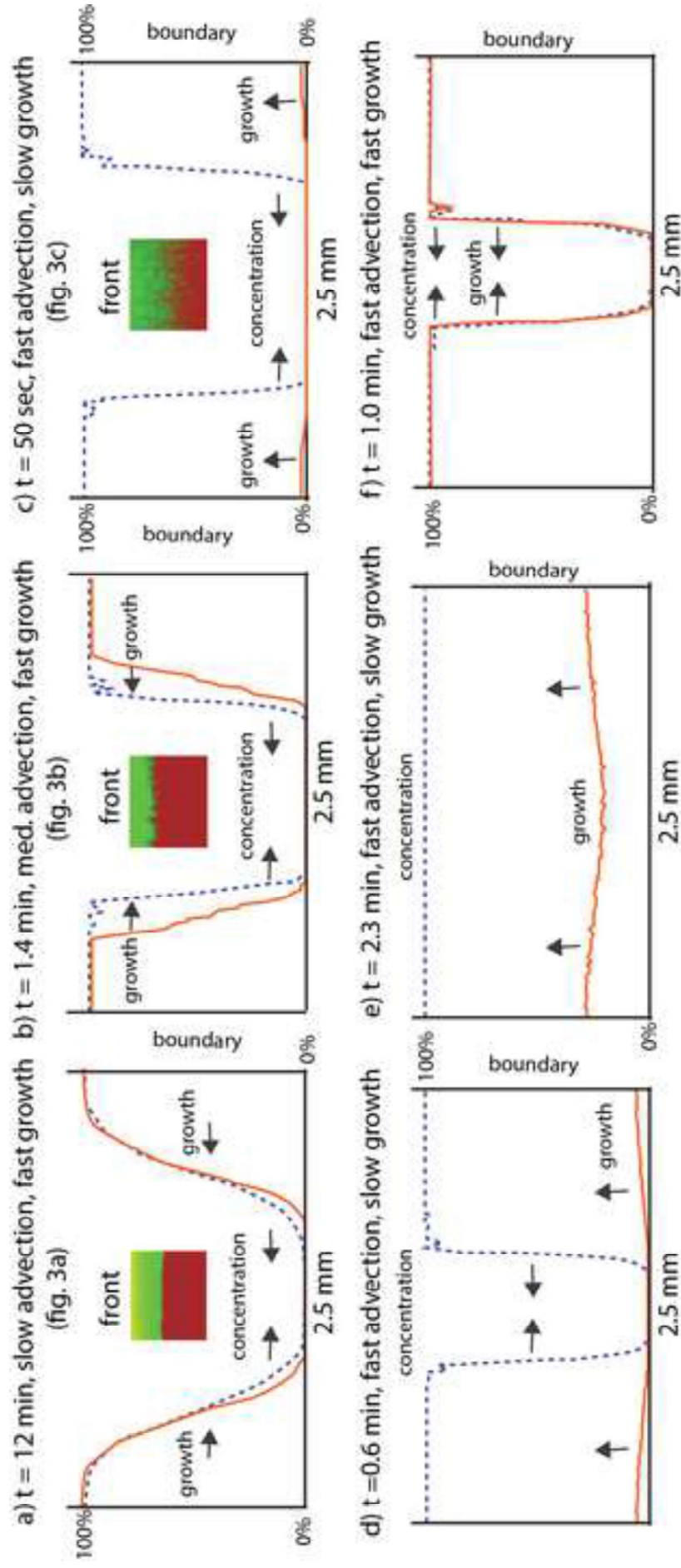
increasing Péclet number, decreasing Damköhler I number

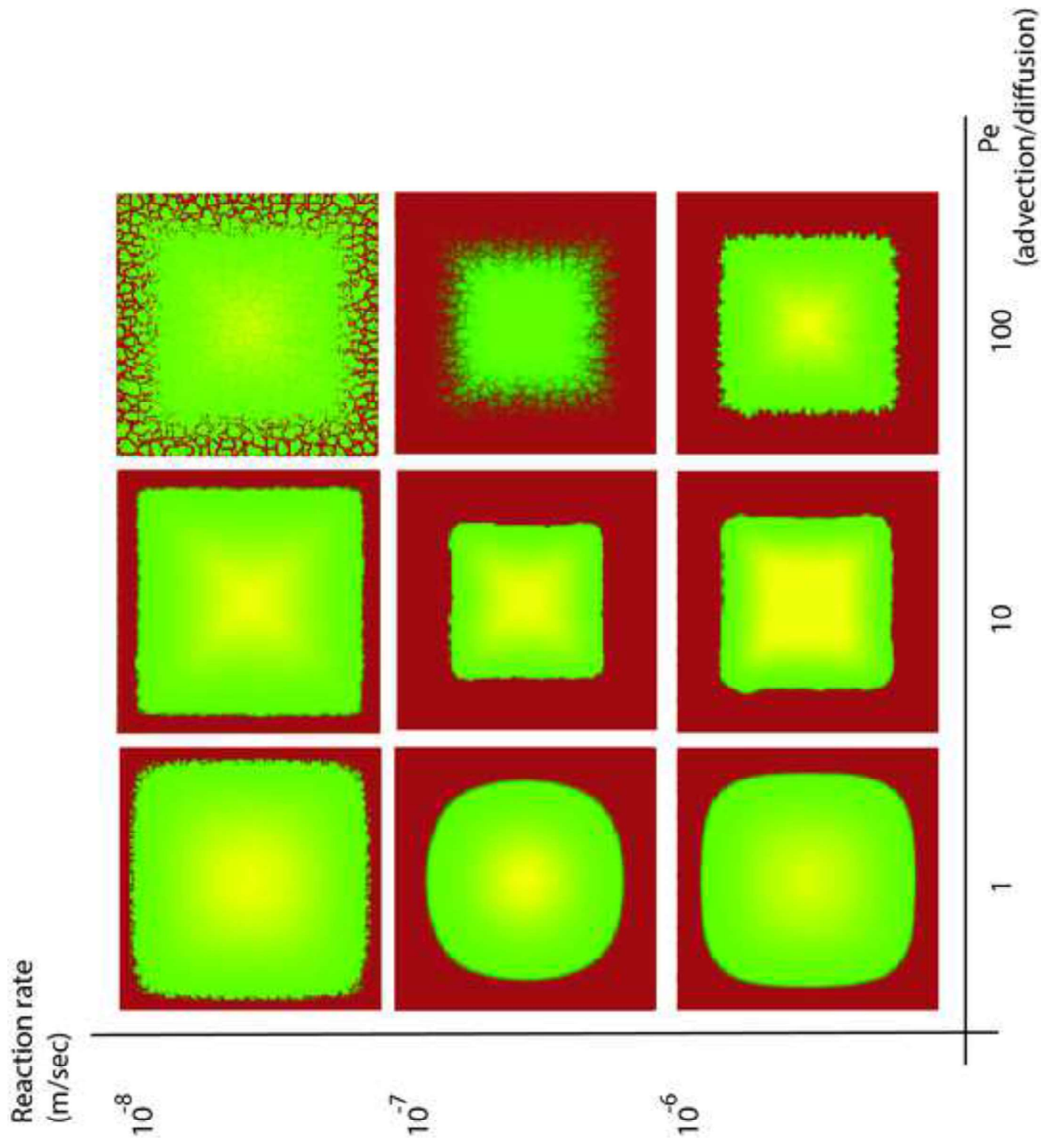




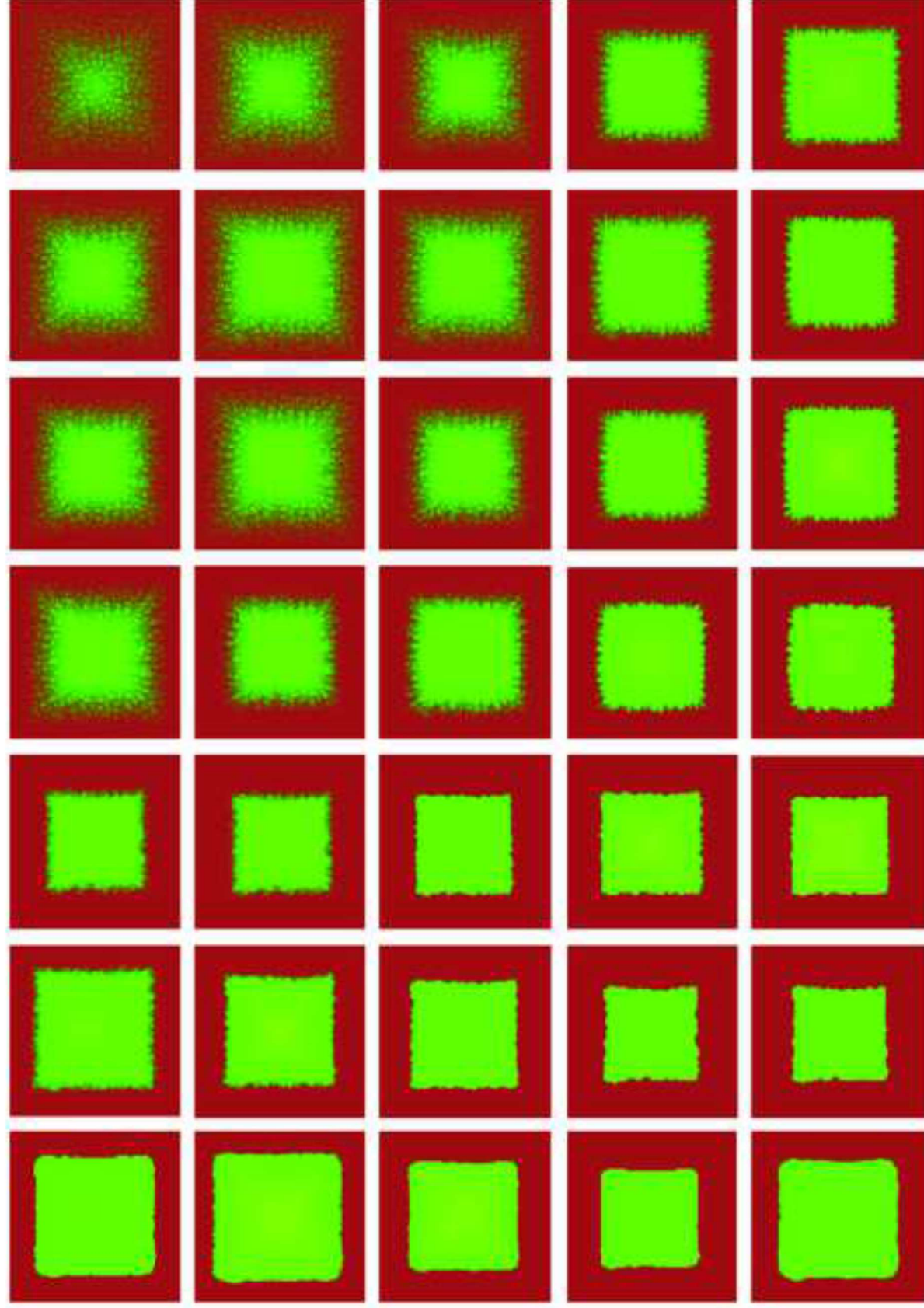








Reaction rate (m/sec)



Pe
(advection/diffusion)

100

10

