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1 Aggregation in economies with search frictions*

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3 March 8, 2021

4 **Abstract**

5
6 We derive an aggregation result in economies with indivisible labor supply choices and
7 frictional labor markets, obtaining a tractable model of gross worker flows in aggregate
8 labor markets with search frictions. Our result explores the fact that economies with
9 non-convex choice sets and idiosyncratic shocks allow for sunspot equilibria à la [Kehoe](#)
10 [et al. \(2002\)](#). We use comparative steady state analysis to demonstrate the applicability
11 of our aggregation result. Our framework reconciles the neoclassical growth model with
12 search frictions with a mildly procyclical participation rate and matches the gross worker
13 flows underpinning those dynamics.

14 **Keywords:** indivisibilities, sunspots, search frictions, gross worker flows.

15 **JEL Classification:** D50, D60, D91, J22.

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1 Introduction

Since the seminal work of Merz (1995) and Andolfatto (1996), dynamic stochastic general equilibrium (DSGE) models with labor market search frictions have been widely used to study unemployment fluctuations. However, these two approaches place different restrictions on individual choices. In turn, Merz (1995) assumes the existence of a representative “large family”, constrained by budget sets and an employment law of motion, while Andolfatto (1996) assumes a game of “musical chairs” (exogenous shocks), that randomly allocate individuals to labor market states, with perfect insurance against idiosyncratic risk.¹ We take our cue from the latter approach and make the following contribution: we generalise the musical chairs’ approach to a model with gross worker flows and individual participation choices, using results from the literature on sunspots and lotteries, along the lines of Kehoe et al. (2002). To the best of our knowledge, ours is the first paper to offer an aggregation result in economies with three state labor markets, indivisible labor and search frictions, based on individual choices (without having to impose the assumption of the “large family”), that yields a constrained efficient competitive equilibrium.

Our approach delivers a tractable characterization of equilibrium in economies combining indivisible labor supply choices (participation margin), and labor market frictions. The literature has often restricted attention to two-state labor markets, ignoring participation and focusing on the margin between employment and unemployment.² However, recent empirical work attributes an important role to the participation margin for labor market transitions. Elsby et al. (2015) showed that the participation margin accounts for one-third of the cyclical variation in the unemployment rate. Moreover, unlike the Merz (1995) large family set-up,

¹Also, Merz (1997) used a randomisation device analogous to Andolfatto to decentralise the constrained optimum in a two-state labor market.

²Several papers consider participation in DSGE models with search frictions. Some early examples are Veracierto (2008), Ravn (2008) and Shimer (2013). This notwithstanding, the inclusion of an intertemporal labor supply margin in economies with indivisibilities and search frictions remains a difficult task. All examples above use the Merz (1995) “large family” model to achieve aggregation, and deliver stark counterfactual predictions about the labor market (for example, procyclical unemployment).

38 which only identifies net worker flows, our model yields a characterization of equilibrium gross
39 worker flows. This is important, since [Krusell et al. \(2010, 2011\)](#) and [Krusell et al. \(2017\)](#)
40 stressed the importance of gross worker flows and developed models with missing insurance
41 markets and indivisibilities in labor supply choice to account for these transitions.

42 We develop a general equilibrium model of gross worker flows with complete markets,
43 where individuals face heterogeneous employment histories and idiosyncratic risk. Following
44 [Andolfatto \(1996\)](#), musical chairs allocate individuals to different labor market states each
45 period; conditional on this, individuals face an indivisible participation choice, in labor market
46 with search frictions. To overcome indivisibilities, individuals play lotteries over participation
47 as in [Rogerson \(1988\)](#) and [Hansen \(1985\)](#). The decision of each individual is based on the joint
48 outcome of public (“musical chairs”) and contrived randomness (lotteries) and the realisation
49 of idiosyncratic shocks. This hybrid decision process may seem unusual, but we argue it can
50 be microfounded as follows. We demonstrate that one can mimic the joint effects of musical
51 chairs and lotteries by indexing on the basis of two naturally occurring random variables
52 (sunspots) prior and after the realisation of the idiosyncratic shocks. Such an arrangement is
53 consistent with the existence of the usual Arrow-Debreu contingent commodities.

54 Subsequently, similarly to [Christiano et al. \(2020\)](#) we use comparative steady state analysis
55 as a short-cut for analyzing model dynamics. Two main insights emerge from this analysis.
56 First, our model reconciles the neoclassical growth model with search frictions with a mildly
57 procyclical participation rate. This result is particularly important given the tendency for
58 models featuring intertemporal substitution in frictional labor markets to deliver excessively
59 procyclical participation and, thus, procyclical unemployment (a problem stressed by [Ravn,](#)
60 [2008](#); [Veracierto, 2008](#); [Shimer, 2013](#), for example). Second, we show using a calibrated
61 example that the model accounts well for the observed flows. In particular, it is able to match
62 the high transition rate from unemployment to inactivity, which early papers by [Garibaldi and](#)
63 [Wasmer \(2005\)](#) and [Krusell et al. \(2010, 2011\)](#) have shown to be challenging for equilibrium
64 models of gross worker flows, under either complete or incomplete markets.

65 The literature on sunspots and lotteries in economies with non-convexities and complete
66 markets includes, among others, [Prescott and Townsend \(1984\)](#), [Shell and Wright \(1993\)](#),
67 [Garratt \(1995\)](#), [Garratt et al. \(2002\)](#), [Kehoe et al. \(2002\)](#), and [Garratt et al. \(2004\)](#). Our
68 results generalise models with indivisibilities to include idiosyncratic risk arising from frictional
69 labor markets. To achieve that, we introduce the distinction between public randomisations
70 prior and after the realisation of idiosyncratic shocks in each period—although this distinction
71 is already discussed by [Kehoe et al. \(2002\)](#), it is not important for their analysis.

72 Our paper contributes to a recent literature that combines indivisible labor supply choices
73 in models with intertemporal substitution (what [Krusell et al., 2008](#), call “non-trivial labor
74 supply choices”), together with search frictions in the labor market. [Krusell et al. \(2008\)](#)
75 show that in a set-up with indivisibility and incomplete markets (similar to [Chang and Kim,](#)
76 [2006, 2007](#)), search frictions avoids indeterminacy in labor supply choices.³ Building on
77 this framework, [Krusell et al. \(2010, 2011\)](#) study individual transitions across employment,
78 unemployment and non-participation, in a three-states labor market model, with incomplete
79 markets, search frictions and non-trivial labor supply choices.⁴ They show that whilst the
80 benchmark model is unable to match the persistence of the employment and non-participation
81 states found in the data, a version of the same model with persistent idiosyncratic productivity
82 shocks affecting the individual value of work is able to match the transition flows well.

83 Further, [Krusell et al. \(2011\)](#) study a version of their model with complete markets (with
84 insurable idiosyncratic shocks), but do not discuss decentralization and, instead, consider the
85 solution to the social planner’s problem, in which each individual receives equal weight. The

³[Krusell et al. \(2008\)](#) show how an economy with indivisible labor and incomplete markets, current labor supply is indeterminate for individuals with intermediate levels of wealth. They subsequently suggest labor market frictions, à la [Lucas and Prescott \(1974\)](#) as a mechanism to break this indeterminacy.

⁴There are, of course, several empirical papers studying gross worker flows in three-state frictional labor markets, but without modelling optimal intertemporal labor supply choices. These studies extend the matching function model ([Mortensen and Pissarides, 1994](#)), and employ a stock-flow accounting framework to model unemployment duration dependence, long-term unemployment, and non-participation. Recent examples, establishing the importance of workers’ heterogeneity and the participation margin include [Barnichon and Figura \(2015\)](#), [Elsby et al. \(2015\)](#), and [Kroft et al. \(2016\)](#).

86 resulting equilibrium allocations imply labor market gross flows that are comparable to those
87 obtained in the incomplete market economy. Thus, they conclude that uninsurable risk is not
88 a necessary ingredient to obtain a satisfactory representation of labor market transitions.⁵ In
89 our paper, we show how the decentralized competitive equilibrium with complete markets can
90 be obtained using either lotteries or sunspots, to produce constrained efficient allocations. At
91 the same time, the resulting model is as successful at matching empirical gross worker flows as
92 the incomplete markets model. In particular, using sunspots as the randomization mechanism
93 generates heterogeneous employment histories across individuals that are conforming with
94 realistic transitions across labor market states (comparable to what is achieved by [Krusell](#)
95 [et al.](#), 2010, 2011, using idiosyncratic productivity shocks).

96 Finally, [Krusell et al.](#) (2017) augment the set-up developed in [Krusell et al.](#) (2010, 2011) with
97 job-to-job transitions and aggregate shocks to labor market frictions, in order to study gross
98 worker flows over the business cycle. We consider shocks to the job finding rate, and show
99 how the model with indivisible labor supply, complete markets, and extrinsic randomization,
100 can deliver either a countercyclical or a procyclical participation rate. Thus, the neoclassical
101 growth model with search frictions can be reconciled with a mildly procyclical participation
102 rate, that is supported by empirically realistic gross worker flows.

103 The remainder of the paper is organized as follows: Section 2 explains the environment;
104 Section 3 establishes that an equilibrium with musical chairs and lotteries corresponds to
105 a sunspot equilibrium; Section 4 presents the comparative steady state analysis; Section 5
106 concludes.

⁵In a model with indivisible labor supply choices but without frictional unemployment, [Ljungqvist and Sargent](#) (2008) obtain a similar result.

2 Model

2.1 Agents and markets

Time is discrete, indexed $t = 0, 1, \dots$. The economy is populated by a continuum of infinitely-lived individuals, $i \in [0, 1]$. There is a single good, produced with capital and labor. Individuals buy consumption, c and invest in capital, k , depreciating at rate $\delta \in (0, 1)$, and face an indivisible participation choice: labor market participation imposes a utility loss, $\xi \geq 0$. Conditional on participation, individuals may be employed or unemployed. If employed, they incur an additional utility cost $-\ln(1 - \underline{h}) > 0$, as they sacrifice $\underline{h} \in (0, 1)$ units of their endowment of time (with \underline{h} an exogenous parameter). Workers transition between three states: employment (e), unemployment (u), and non-participation (o). We denote labor market states by $\iota \in \mathcal{L} \equiv \{e, u, o\}$. Individuals have flow utility, $U(c) - \psi(\iota)$, with $U'(c) > 0$ and $U''(c) < 0$, and with $\psi(e) \equiv \xi - \ln(1 - \underline{h})$, $\psi(u) \equiv \xi$ and $\psi(o) \equiv 0$.

Competitive firms have (identical) constant returns to scale technology which turns labor and capital into output, $F(k, n)$, that satisfy standard Inada conditions and (k, n) denote the demand for capital and labor. Firms pay wages w to hire workers, r to rent capital, and maximize profits, $F(k, n) - wn - rk$.

The economy consists of three islands, which we refer to as employment island, unemployment island and leisure island. Individuals that were unemployed (non-participants) in the previous period, start at the beginning of date t in the unemployment (leisure) island. If they decide not to participate, they relocate (remain) to the leisure island; and, if they decide to participate, they relocate to the employment island with probability f , or they remain (relocate) to the unemployment island with probability $1 - f$. New jobs become immediately productive.

Individuals previously employed, start date t in the employment island. An existing job is destroyed with probability λ , and upon destruction, previously employed individuals are allowed to search for another job and remain to the employment island with probability

132 f . With probability $1 - \lambda$ the job is not destroyed and they continue with the existing
133 employment relationship.

134 Labor frictions restrict access to the employment island; however, conditional on access, the
135 labor market is competitive and wages reflect the marginal product of labor.⁶ Goods markets
136 are competitive, with capital moving freely across islands. There is no aggregate uncertainty,
137 but frictional labor markets generate idiosyncratic risk.

138 2.2 Institutions

139 We consider two institutional trading arrangements. In the first, as in [Andolfatto \(1996\)](#), at
140 the start of date t a game of musical chairs allocates individuals to different labor market
141 states $\iota \in \mathcal{L}$. Subsequently, individuals buy lotteries over labor force participation and
142 idiosyncratic shocks realise. Each period, insurance markets open before the realization
143 of musical chairs and lotteries, with contracts traded at actuarial fair prices. At the end
144 of each date, spots market open where individuals receive income, execute contracts, buy
145 consumption and invest.

146 In the second market structure (the sunspot economy), we assume markets open only once, at
147 date -1 . Individuals trade contracts contingent on “sunspot” activity and idiosyncratic risk.
148 Sunspots act as a coordination device much like the musical chairs and affect welfare because
149 of indivisibilities in labor supply choices. This structure yields a competitive equilibrium
150 with voluntary trade in contingent commodities, where sunspots coordinate actions among
151 individuals. We label the first model “musical chairs” and the second “sunspots”, and we
152 study each in turn.

⁶The assumption of competitive markets in coexistence with search frictions has a long tradition and follows, for example, [Lucas and Prescott \(1974\)](#), [Alvarez and Veracierto \(1999\)](#) and [Krusell et al. \(2008, 2010, 2011\)](#). This approach is fruitful because, as we show in Proposition 2, it yields a constrained efficient equilibrium despite the search frictions. However, having competitive factor prices is not essential for the success of our model to match labor market transitions rates. In fact, in the steady state equilibrium, factor prices are constant and, thus, assuming non-competitive factor prices would not alter our analysis.

153 **2.2.1 Musical chairs**

154 At the beginning of date t a game of musical chairs assigns individuals to a labor market
 155 state $\iota \in \mathcal{L} \in \{e, u, o\}$, with probability $\alpha_t(\iota)$. Figures 1a and 1b show the sequence of events
 156 conditional on the musical chairs randomisation. Specifically, individuals assigned to the
 157 employment island ($\iota = e$) observe the realisation of the idiosyncratic shock $\kappa \in \{e_d, e_{nd}\}$,
 158 where $\kappa = e_d$ denotes destruction (d) with probability λ , and $\kappa = e_{nd}$ denotes no destruction
 159 (nd) with $1 - \lambda$; subsequently they buy lotteries over labor force participation, and conditional
 160 on the lottery outcome engage (or not) in search activity. Individuals assigned to the
 161 unemployment or leisure island ($\iota \in \{u, o\}$) buy lotteries over labor force participation and
 162 then engage (or not) in search activity. We denote by $\tilde{i} \in \{e_d, e_{nd}, u, o\}$ the consolidated set
 163 of states prior to the participation lottery stage, by $j \in \mathcal{L} \in \{e, u, o\}$ the labor market state
 164 at the end of the period and by $\pi(\tilde{i})$ the lottery over labor force participation. The pair (\tilde{i}, j)
 165 denotes the labor market transitions of individuals during each period. Individuals discount
 166 the future with $\beta \in (0, 1)$.

The Bellman equation characterising each individual's decision is

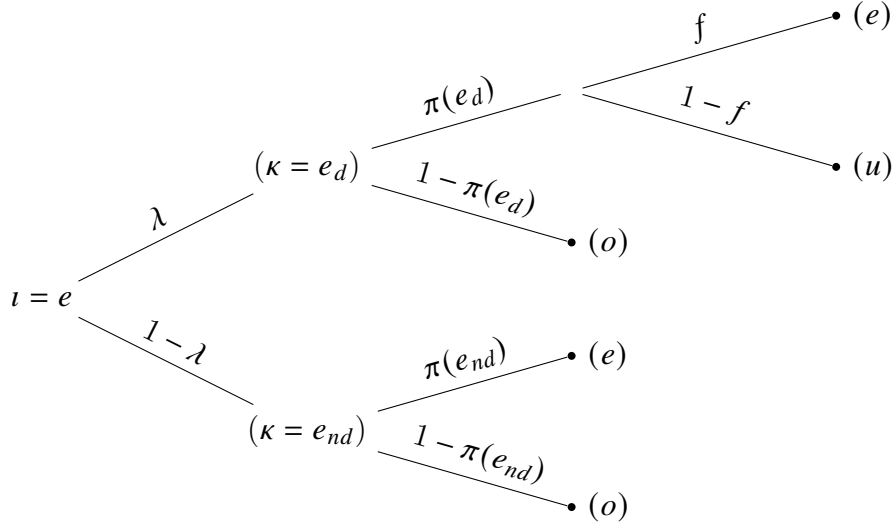
$$V_t(k_t, \bar{k}_t) = \max_{\{c, k, y, \pi\}} \left\{ \alpha_t(e) [(1 - \lambda_t)v_t(e_{nd}) + \lambda_t v_t(e_d)] + \alpha_t(u)v_t(u) + \alpha(o)v_t(o) \right\}$$

with

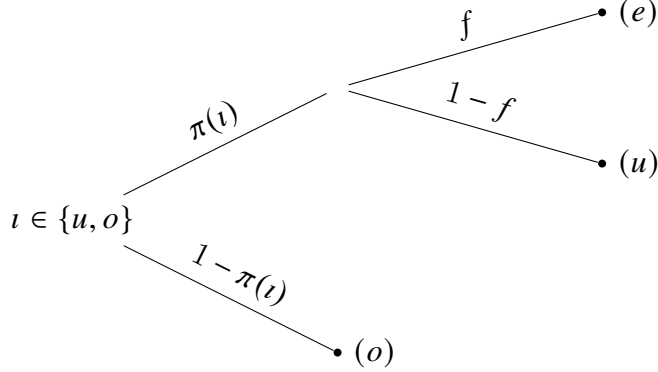
$$v_t(e_{nd}) = \pi_t(e_{nd}) [U[c_t(e_{nd}, e)] - \psi(e) + \beta V_{t+1}(k_{t+1}(e_{nd}, e), \bar{k}_{t+1})] + \\ (1 - \pi_t(e_{nd})) [U[c_t(e_{nd}, o)] + \beta V_{t+1}(k_{t+1}(e_{nd}, o), \bar{k}_{t+1})],$$

and, for $\tilde{i} \in \{e_d, u, o\}$,

$$v_t(\tilde{i}) = \pi_t(\tilde{i}) f_t(U(c_t(\tilde{i}, e)) - \psi(e) + \beta V_{t+1}(k_{t+1}(\tilde{i}, e), \bar{k}_{t+1})) + \\ \pi_t(\tilde{i})(1 - f_t)(U(c_t(\tilde{i}, u)) - \psi(u) + \beta V_{t+1}(k_{t+1}(\tilde{i}, u), \bar{k}_{t+1})) + \\ (1 - \pi_t(\tilde{i}))(U(c_t(\tilde{i}, o)) + \beta V_{t+1}(k_{t+1}(\tilde{i}, o), \bar{k}_{t+1})),$$



(a) Sequence of events conditional on $\iota = e$



(b) Sequence of events conditional on $\iota \in \{u, o\}$

Figure 1: Sequence of events conditional on musical chairs' randomisation

subject to the budget constraint for each pair (\tilde{i}, J) ,

$$c_t(\tilde{i}, J) + k_{t+1}(\tilde{i}, J) + \sum_{\tilde{i}} \sum_J q_t(\tilde{i}, J) y_t(\tilde{i}, J) = y_t(\tilde{i}, J) + (r_t + 1 - \delta) k_t + w_t \underline{h} \mathbb{1}_J,$$

167 where $\mathbb{1}_J$ is an indicator function that is equal to unity if $J = e$ and zero otherwise. The
 168 relevant state space for individual optimisation consists of predetermined individual and
 169 aggregate capital stock, k and \bar{k} , respectively, and is independent of the previous period
 170 individual labor market state. At the end of date t , individuals buy consumption $c_t(\tilde{i}, J)$,

171 invest in capital stock $k_{t+1}(\tilde{i}, j)$, execute contracts $y_t(\tilde{i}, j)$ that are purchased at the beginning
 172 of date t (ex-ante) at price $q_t(\tilde{i}, j)$, receive capital income and, if employed, labor income.

173 Actuarially fair insurance implies that marginal utilities of consumption $U_c[c(\tilde{i}, j)]$ are
 174 equalised across all labor market states, which implies that $c(\tilde{i}, j) = c$ for all pairs (\tilde{i}, j) .
 175 In turn, it follows that the marginal return of one additional unit of capital $V_k(k(\tilde{i}, j), \bar{k})$
 176 is equalised across labor market states, which implies $k(\tilde{i}, j) = k$ for all pairs (\tilde{i}, j) . The
 177 individual's decision is consolidated as follows:

$$V_t(k_t, \bar{k}_t) = \max \left\{ U(c_t) - \alpha_t(e)(1 - \lambda_t)\pi_t(e_{nd})(\xi - \ln(1 - \underline{h})) - \right. \\ \left. (\xi - f_t \ln(1 - \underline{h})) [\alpha_t(e)\lambda_t\pi_t(e_d) + \alpha_t(u)\pi_t(u) + \alpha(o)\pi_t(o)] + \beta V_{t+1}(k_{t+1}, \bar{k}_{t+1}) \right\} \quad (1)$$

178 subject to

$$c_t + k_{t+1} = \\ \left[\alpha_t(e)\pi_t(e_{nd})(1 - \lambda_t) + \left(\alpha_t(e)\lambda_t\pi_t(e_d) + \alpha_t(u)\pi_t(u) + \alpha(o)\pi_t(o) \right) f_t \right] w_t \underline{h} + (r_t + 1 - \delta)k_t, \\ 0 \leq \pi_t(\tilde{i}) \leq 1. \quad (2)$$

179 This represents the decision of a stand-in agent who chooses consumption, investment and
 180 lotteries over participation to maximise (1) subject to (2).

181 Wages and rental prices earn their respective marginal products. Insurance markets are
 182 segmented, in the sense that there exist separate markets for each contingency (\tilde{i}, j) . Insurers
 183 in each market offer contracts $y(\tilde{i}, j)$ at actuarially fair prices $q(\tilde{i}, j)$, and free entry drives
 184 profits to zero.

185 Equilibrium is defined as follows:

186 **Definition 1** (*Musical chairs*) A full insurance equilibrium is a price system $\{w, r, q\}$ and
 187 probability measures $\alpha(\iota)$ for $\iota \in \mathcal{L}$, a law of motion for aggregate capital \bar{k} , a collection of

188 individual choices $\{c, k, \pi, y\}$, an individual value function $V(k, \bar{k})$ and a collection of firm
 189 choices $\{k, n\}$ such that:

- 190 1. At given prices and $\alpha(i)$, $\{c, k, \pi, y\}$ and $V(k, \bar{k})$ solve the individual's problem;
- 191 2. At given prices, all firms maximise profits;
- 192 3. Good's market clears, $c + k_{+1} = f(k, n) + (1 - \delta)k$;
- 193 4. Capital market clears, $k = \bar{k}$;
5. Labor market clears,

$$n = \left[\alpha(e)\pi(e_{nd})(1 - \lambda) + \left(\alpha(e)\lambda\pi(e_d) + \alpha(u)\pi(u) + \alpha(o)\pi(o) \right) f \right] \underline{h};$$

- 194 6. $\alpha(i)$ is equal to the previous period measure of individuals in labor market state i .

195 The following remarks are in order. First, we show that any interior equilibrium satisfies
 196 $\pi(e_{nd}) = 1$ (corner solution) and $\pi(i) \in (0, 1)$, $i \in \{e_d, u, o\}$ (see Appendix A for details).
 197 Second, probabilities $\alpha(i)$ are determined by the measures of individuals in state $i \in \{e, u, o\}$
 198 at the end of the previous period. Hence, although $\alpha(i)$ are taken as given by individuals,
 199 they are determined endogenously in equilibrium. Third, in Section 4 we offer a detailed
 200 characterisation of the equilibrium and discuss various comparative static exercises.

201 The hybrid model that we have analysed so far includes the musical chairs' framework
 202 of [Andolfatto \(1996\)](#) as a special case.

203 **Lemma 1** *If $\xi = 0$, then our framework reduces to the musical chairs' model of [Andolfatto](#)*
 204 *(1996).*

Proof. Suppose $\xi = 0$. Set

$$N_t = \alpha_t(e)\pi_t(e_{nd})(1 - \lambda_t) + \left(\alpha_t(e)\lambda_t\pi_t(e_d) + \alpha_t(u)\pi_t(u) + \alpha_t(o)\pi_t(o) \right) f_t,$$

205 with $N \equiv n/\underline{h}$ (see Section 4 for full details).

206 Then, (1)–(2), reduce to:

$$V_t(k_t, \bar{k}_t) = \max_{\{c, k\}} \left\{ U(c_t) + N_t \ln(1 - \underline{h}) + \beta V_{t+1}(k_{t+1}, \bar{k}_{t+1}) \right\}, \quad (3)$$

207 subject to

$$c_t + k_{t+1} = w_t N_t \underline{h} + (r_t + 1 - \delta)k_t. \quad (4)$$

208 This corresponds to Andolfatto’s model with N_t denoting the probability that an individual
 209 is allocated to employment and $1 - N_t$ the probability that is allocated to nonemployment. ■

210 This result requires that if the opportunity cost of participation is negligible, $\xi = 0$, then the
 211 randomisation devices prior and after the realisation of idiosyncratic shocks (see figures 1a
 212 nd 1b) reduce to the simple musical chair’s randomisation in Andolfatto (1996).

213 2.2.2 Sunspots

214 In this Section we abstract from sequential trading and assume Arrow-Debreu (AD) markets,
 215 with trade occurring at date -1 . Individuals trade contracts contingent on the publicly
 216 observed sunspot activity and idiosyncratic risk. Sunspot activity is constructed so that each
 217 period it induces a distribution of individuals across labor market states (islands) $\mathcal{L} = \{e, o, s\}$.
 218 We employ the distinction between ex-ante and ex-post public randomisations (sunspots)
 219 within a given period that is discussed in Kehoe et al. (2002).⁷ Figure 2 shows the sequence
 220 of events at date t . We denote ex-ante sunspot shocks with a superscript “0”, and ex-post
 221 shocks with a superscript “1”. At the beginning of date t individuals observe the ex-ante

⁷In their framework, only ex-post randomisations are important to overcome non-convexities arising from private information; and in fact, they show that the model with ex-ante and ex-post sunspots is equivalent in terms of allocations to the model with only ex-post sunspots. However, Cole (1989) showed that in a set-up with ex-ante sunspots and convex set of feasible allocations, the introduction of ex-post sunspots is still welfare improving because lotteries conditional on private information separate individuals with different risk profiles.

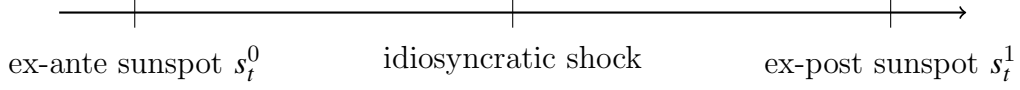


Figure 2: Sequence of events at date t

222 sunspot shock s_t^0 , subsequently the idiosyncratic shock is realised and at the end of the period
 223 the ex-post sunspot shock s_t^1 is realised and transactions take place. For example, individuals
 224 induced by the ex-ante sunspot to start date t in the employment island, observe if the job is
 225 destroyed or not and the ex-post sunspot realisation allocates them to a labor market state
 226 at the end of the period; similarly, individuals induced by the ex-ante sunspot to start date t
 227 in the unemployment island, find employment with probability f and remain unemployed
 228 with probability $1 - f$, and at the end of the period observe the realisation of the ex-post
 229 sunspot and execute all their obligations.

230 The distinction between ex-ante and ex-post sunspots is important. It serves the following
 231 purpose. Ex-ante public randomisations replicate the distribution of musical chairs, overcome
 232 non-convexities arising from indivisibilities in labor supply, and influence the distribution of
 233 idiosyncratic risk (see below); while ex-post randomisation separate those individuals whose
 234 pre-existing jobs have been destroyed and need to be assigned into a labor market state,
 235 from those individuals whose jobs have survived (see Figure 1a). Hence, in the absence of
 236 idiosyncratic risk arising from job destruction, the ex-post public randomisation device is
 237 irrelevant.

238 Time and the resolution of uncertainty are described by an event-tree, a countable set.
 239 Denote the history of ex-ante and ex-post sunspot realisations up and until date t by $s^{0t} =$
 240 $[s_0^0, s_1^0, \dots, s_t^0]$, $s^{1t} = [s_0^1, s_1^1, \dots, s_t^1]$, the joint history by $s^t = [(s_0^0, s_0^1), (s_1^0, s_1^1), \dots, (s_t^0, s_t^1)]$
 241 and the history of idiosyncratic shocks up and until date t by $\phi^t = [\phi_0, \phi_1, \dots, \phi_t]$. Let σ_t be
 242 the date-event consisting of ex-ante and ex-post sunspot realisations, s_t , and idiosyncratic
 243 shocks, ϕ_t , with history up to and including date t , $\sigma^t = [\sigma_1, \sigma_2, \dots, \sigma_t]$. We require the

244 probability distribution of ex-post shocks to have a continuous density. We assume that s_t^1
245 is distributed uniformly on $[0, 1]$ and let $\mu_t^1(s^{0t}, \phi^t, s^{1t-1})$ be the measure of date t ex-post
246 sunspots states conditional on history $\{s^{0t}, \phi^t, s^{1t-1}\}$. The probability distributions of ex-ante
247 and idiosyncratic shocks are obtained by appropriate construction as we demonstrate below.
248 Let the unconditional probability of s^{0t} be $\mu_t^0(s^{0t})$ and the probability of ϕ^t conditional on
249 s^{0t} be $\gamma_t(\phi^t | s^{0t})$. Let $\mu_t(s^{0t}, \phi^t) = \gamma_t(\phi^t | s^{0t}) \mu_t^0(s^{0t})$. We assume that histories of ex-post
250 shocks do not influence the distributions of ex-ante and idiosyncratic shocks.⁸ Individuals
251 trade contingent claims against future events σ^t at price $p_t(\sigma^t)$ and firms buy inputs and
252 sell output against s^t at $p_t(s^t)$. Prices $p_t(s^t)$ are derived from $p_t(\sigma^t)$ by summing over ϕ^t .
253 The decision of an individual is

$$\max_{c,k} \sum_t \beta^t \sum_{\{s^{0t}, \phi^t\}} \mu_t(s^{0t}, \phi^t) \int_{s^{1t}} \left[U(c_t(\sigma^t)) - \psi(\sigma^t) \right] ds^{1t}, \quad (5)$$

254 subject to

$$\begin{aligned} & \sum_t \sum_{\{s^{0t}, \phi^t\}} \int_{s^{1t}} p_t(\sigma^t) \left[c_t(\sigma^t) + k_{t+1}(\sigma^t) \right] ds^{1t} = \\ & \sum_t \sum_{\{s^{0t}, \phi^t\}} \int_{s^{1t}} p_t(\sigma^t) \left[(r_t(s^t) + 1 - \delta) k_t(\sigma^{t-1}) + \underline{h} w_t(s^t) \mathbb{1}(\sigma^t) \right] ds^{1t}, \end{aligned} \quad (6)$$

255 where the indicator function $\mathbb{1}(\sigma^t)$ is equal to unity at date-events where individuals work
256 and zero otherwise. We define multiple integrals $\int_{s^{1t}} \equiv \int_{s_0^1} \cdots \int_{s_t^1}$ up to and including date t
257 and differentials $ds^{1t} \equiv ds_t^1 \cdots ds_0^1$ back to date zero.

258 Firms choose capital and labor to maximise profits:

$$\max_{k,n} \sum_t \sum_{s^{0t}} \int_{s^{1t}} p_t(s^t) \left[F(k_t(s^{t-1}), n_t(s^t)) - r_t(s^t) k_t(s^{t-1}) - w(s^t) n_t(s^t) \right] ds^{1t}. \quad (7)$$

259 Consider the following definition of a sunspot equilibrium.

⁸This assumption follows [Prescott and Townsend \(1984\)](#), who assume that histories of lottery outcomes do not influence the distribution of types across the population.

260 **Definition 2** (*Sunspots*) A sunspot equilibrium is a price system $\{w, r, p\}$, a collection of
 261 individual choices $\{c, k\}$, and a collection of firm choices $\{k, n\}$ such that:

262 1. At given prices, $\{c, k\}$ solve the individual's problem (5)-(6);

263 2. At given prices, firms maximise profits (7);

3. Good's market clears,

$$\int \left(c_t(\sigma^t) + k_{t+1}(\sigma^t) - (1 - \delta)k_t(\sigma^{t-1}) \right) di = f \left(k_t(s^{t-1}), n_t(s^t) \right);$$

264 4. Capital market clears, $\int k_t(\sigma^t) di = k(s^t)$;

265 5. Labor market clears, $n_t(s^t) = \int \underline{h} \mathbb{1}(\sigma^t) di$.

266 3 Equivalence

267 The purpose of this Section is to demonstrate that the equilibrium allocations achieved by
 268 the sunspot economy and the musical chairs economy are equivalent. This equivalence result
 269 microfounds the hybrid model of musical chairs, idiosyncratic risk and lotteries over labor
 270 force participation. Subsequently, we demonstrate that the sunspot allocation is constrained
 271 Pareto optimal.

272 To demonstrate equivalence of equilibria between the two economies, we proceed in two steps.
 273 First, we establish in Proposition 1 that the same equilibrium allocations obtained with
 274 musical chairs and lotteries can be implemented as sunspot-equilibrium allocations and, thus,
 275 the lottery equilibrium corresponds to an equilibrium with sunspots. Specifically, in the proof
 276 of Proposition 1 we present a detailed construction of the sunspot probability distribution,
 277 so that the sunspot economy achieves the same equilibrium allocation as the target lottery
 278 equilibrium allocation. Second, using well-known results in the literature (see Garratt et al.,
 279 2002; Kehoe et al., 2002), we establish that the converse of Proposition 1 is also true if the

280 sunspot state-space is sufficiently rich.

281 **Proposition 1** *An equilibrium with musical chairs and lotteries corresponds to a sunspot*
 282 *equilibrium.*

283 **Proof.** The proof is constructive. Suppose an equilibrium with musical chairs exists. Then,
 284 we construct an equilibrium with sunspots supporting the same allocations as the musical
 285 chairs equilibrium.

Consider the stand-in agent's problem in the musical chairs economy, given by (1)–(2),
 implying the first-order conditions

$$U_c(c_t) = \beta R_{t+1} U_c(c_{t+1}), \quad (8)$$

$$\xi - f_t \ln(1 - \underline{h}) = f_t w_t \underline{h} U_c(c_t), \quad (9)$$

$$\xi - \ln(1 - \underline{h}) < w_t \underline{h} U_c(c_t), \quad (10)$$

286 where $R_{t+1} \equiv r_{t+1} + 1 - \delta$. Condition (8) is the Euler equation and (9), (10) are optimality
 287 conditions with respect to $\pi(\tilde{i}) \in (0, 1)$, $\tilde{i} \in \{e_d, u, o\}$ and $\pi(e_{nd}) = 1$ (corner solution). Firm's
 288 optimality requires $r_t = F_k(k, n)$ and $w_t = F_n(k, n)$. We denote the equilibrium allocation
 289 under musical chairs with superscript “*”.

Next, we construct a sunspot equilibrium where agent decisions are identical to those in the
 musical chairs equilibrium. To that end, we set the wage rate and the return on capital in
 the sunspot equilibrium to be equal to (R_t^*, w_t^*) . Define AD prices as follows:

$$p_t(\sigma^t) \equiv \mu_t(s^{0t}, \phi^t) \times \left(\prod_{\tau=0}^t (R_\tau^*)^{-1} \right), \quad (11)$$

290 with $R_0 \equiv 1$. Define the investment portfolio x_{t+1} as follows:

$$x_{t+1} \equiv \sum_{\{s^{0t}, \phi^t\}} \mu_t(s^{0t}, \phi^t) \int_{s^{1t}} k_{t+1}(\sigma^t) d^{s^{1t}}, \quad (12)$$

291 The investment portfolio x_{t+1} , and not its composition, is the relevant choice variable. In
 292 particular, individuals buy x_{t+1} at price $\prod_{\tau=0}^t (R_\tau^*)^{-1}$, and receive return $\left[\prod_{\tau=0}^{t+1} (R_\tau^*)^{-1}\right] R_{t+1}^* x_{t+1}$.
 293 Individual optimality with respect to x_{t+1} is satisfied at prices given by (11). Moreover, (11)
 294 implies that individual marginal utilities are equal across date-events, implying $c(\sigma^t) = c_t$,
 295 for all histories σ^t . Finally, under the given price system, the decisions of all the agents in the
 296 economy are well defined since $\lim_{t \rightarrow \infty} \sum_t \left(\prod_{\tau=0}^t (R_\tau^*)^{-1}\right)$ converges (equivalently, the musical
 297 chairs equilibrium is dynamically efficient).

298 Thus, problem (5)–(6) reduces to

$$\max \sum_t \beta^t \left(U(c_t) - \sum_{\{s^{0t}, \phi^t\}} \mu_t(s^{0t}, \phi^t) \int_{s^{1t}} \psi(\sigma^t) ds^{1t} \right), \quad (13)$$

299 subject to

$$\sum_t \left(\prod_{\tau=0}^t (R_\tau^*)^{-1} \right) (c_t + x_{t+1}) = \sum_t \left(\prod_{\tau=0}^t (R_\tau^*)^{-1} \right) \left(R_t^* x_t + w_t^* \underline{h} \sum_{\{s^{0t}, \phi^t\}} \mu_t(s^{0t}, \phi^t) \int_{s^{1t}} \mathbb{1}(\sigma^t) ds^{1t} \right). \quad (14)$$

300 Optimality with respect to consumption between two consecutive dates yields (8), so that
 301 $c_t = c_t^*$ is consistent with optimality. Moreover, we set $x_{t+1} = k_{t+1}^*$. To complete the argument
 302 we need to show that optimal allocations satisfy conditions (9)–(10) as well. From the
 303 consolidated problem (13)–(14) we can observe that keeping track the histories of ex-post
 304 realisations s^{1t-1} is not relevant anymore. To that end, we construct the conditional measure
 305 of ex-post states $\mu_t^1(s^{0t}, \phi^t)$ —dropping histories s^{1t-1} —and the probability measure $\mu_t^0(s^{0t})$.

306 Let, in turn, $S^1(s^{0t})$ denote the set of individuals who, following history s^{0t} , are allocated to
 307 a pre-existing job that is destroyed with probability λ and survives with probability $1 - \lambda$, as
 308 if starting from the employment island; $S^2(s^{0t})$ the set of individuals who purchase lottery
 309 profile yielding employment with probability f , and unemployed with probability $1 - f$, as
 310 if they started from the unemployment island; $S^3(s^{0t})$ the set of individuals who purchase

311 lottery profile yielding employment with probability f , and unemployed with probability
 312 $1 - f$, as if they started from the leisure island; and, $S^4(s^{0t})$ the set of individuals who choose
 313 not to participate upon observing s^{0t} .

314 Consider the following equilibrium conditions at history s^{0t} :

$$\begin{aligned}
 \int_{i \in S^1(s^{0t})} di &= \alpha_t^*(e), \\
 \int_{i \in S^2(s^{0t})} di &= \alpha_t^*(u) \pi_t^*(u), \\
 \int_{i \in S^3(s^{0t})} di &= \alpha_t^*(o) \pi_t^*(o),
 \end{aligned} \tag{15}$$

315 and for each individual i

$$\begin{aligned}
 \sum_{s^{0t}: i \in S^1(s^{0t})} \mu_t(s^{0t}) &= \alpha_t^*(e), \\
 \sum_{s^{0t}: i \in S^2(s^{0t})} \mu_t(s^{0t}) &= \alpha_t^*(u) \pi_t^*(u), \\
 \sum_{s^{0t}: i \in S^3(s^{0t})} \mu_t(s^{0t}) &= \alpha_t^*(o) \pi_t^*(o),
 \end{aligned} \tag{16}$$

316 where the pair (α^*, π^*) denotes the musical chairs' and participation probability measures
 317 evaluated at the musical chairs equilibrium. Conditions (15) are equilibrium conditions so
 318 that the measure of individuals at history node s^{0t} who face the prospect of job destruction
 319 or purchase each lottery profile after the sunspot realisation, is equal to the corresponding
 320 measure in the musical chairs equilibrium. Conditions (16) are consistency conditions so that
 321 the measures across history nodes where each individual faces the prospect of job destruction
 322 or purchases each lottery profile is equal to the measure of individuals at each history node
 323 s^{0t} who faces job destruction or purchase each lottery profile. Finally, construction of set
 324 $S^4(s^{0t})$ follows residually.

325 Let, in turn, $Q^1(s_t^1|s^{0t}, \phi^t)$ denote the fraction of individuals, among the measure of individuals
 326 who start from the employment island with a job that is destroyed following history $\{s^{0t}, \phi^t\}$,
 327 who end up being employed at s_t^1 ; $Q^2(s_t^1|s^{0t}, \phi^t)$ denote the fraction of individuals, among
 328 the measure of individuals who start from the employment island with a pre-existing job that
 329 is destroyed, who end up being unemployed; $Q^3(s_t^1|s^{0t}, \phi^t)$ denote the fraction of individuals,
 330 among the measure of individuals who start from the employment island with a pre-existing
 331 job that is destroyed, who end up out of the labor force; $Q^4(s_t^1|s^{0t}, \phi^t)$ the fraction of
 332 individuals, among the measure of individuals who start from the employment island with a
 333 job that is not destroyed, who end up employed; and $Q^5(s_t^1|s^{0t}, \phi^t)$ the fraction of individuals,
 334 among the measure of individuals who start from the employment island with a job that is
 335 not destroyed, who end up out of the labor force.

336 Consider the following equilibrium conditions:

$$\begin{aligned}
 \int_{i \in Q^1(s_t^1|s^{0t}, \phi^t)} di &= \pi_t^*(e_d) f_t, & \int_{i \in Q^4(s_t^1|s^{0t}, \phi^t)} di &= \pi_t^*(e_{nd}) \\
 \int_{i \in Q^2(s_t^1|s^{0t}, \phi^t)} di &= \pi_t^*(e_d) (1 - f_t), & \int_{i \in Q^5(s_t^1|s^{0t}, \phi^t)} di &= 1 - \pi_t^*(e_{nd}) \\
 \int_{i \in Q^3(s_t^1|s^{0t}, \phi^t)} di &= 1 - \pi_t^*(e_d), & &
 \end{aligned} \tag{17}$$

337 and for each individual i

$$\begin{aligned}
 \mu_t^1(s^{0t}, \phi^t) &= \pi_t^*(e_d) f_t, & \text{for each } i &\in Q^1(s_t^1|s^{0t}, \phi^t) \\
 \mu_t^1(s^{0t}, \phi^t) &= \pi_t^*(e_d) (1 - f_t), & \text{for each } i &\in Q^2(s_t^1|s^{0t}, \phi^t) \\
 \mu_t^1(s^{0t}, \phi^t) &= 1 - \pi_t^*(e_d), & \text{for each } i &\in Q^3(s_t^1|s^{0t}, \phi^t) \\
 \mu_t^1(s^{0t}, \phi^t) &= \pi_t^*(e_{nd}), & \text{for each } i &\in Q^4(s_t^1|s^{0t}, \phi^t) \\
 \mu_t^1(s^{0t}, \phi^t) &= 1 - \pi_t^*(e_{nd}), & \text{for each } i &\in Q^5(s_t^1|s^{0t}, \phi^t)
 \end{aligned} \tag{18}$$

338 where as before π^* denotes participation probability measures evaluated at the musical

339 chairs' equilibrium. Conditions (17)–(18) are equilibrium and consistency conditions similar
 340 to (15)–(16). Finally, for individuals not belonging to the set $S^1(s^{0t})$, the realisation of
 341 ex-post sunspots are irrelevant, so that the conditional measure of ex-post states is degenerate
 342 and equal to $\mu_t^1(s^{0t}, \phi^t) = 1$.

343 We require that idiosyncratic shocks and public signals are not independent events so that
 344 $\gamma_t(\phi^t | s^{0t})$ depends on histories s^{0t} . In particular, we construct a dependence structure between
 345 shocks and signals consistent with summations over histories $\{s^{0t}, \phi^t\}$ in (13)–(14) which
 346 yields the problem

$$\max \sum_t \beta^t \left[U(c_t) - \alpha_t^*(e)(1 - \lambda_t)\pi_t(e_{nd}) (\xi - \ln(1 - \underline{h})) - \right. \\ \left. (\xi - f_t \ln(1 - \underline{h})) [\alpha_t^*(e)\lambda_t\pi_t(e_d) + \alpha_t^*(u)\pi_t(u) + \alpha_t^*(o)\pi_t(o)] \right] \quad (19)$$

347 subject to

$$\sum_t \left(\prod_{\tau=0}^t (R_\tau^*)^{-1} \right) (c_t + x_{t+1}) = \sum_t \left(\prod_{\tau=0}^t (R_\tau^*)^{-1} \right) R_\tau^* x_t + \\ \sum_t \left(\prod_{\tau=0}^t (R_\tau^*)^{-1} \right) \left[\alpha_t^*(e)\pi_t(e_{nd})(1 - \lambda_t) + \left(\alpha_t^*(e)\lambda_t\pi_t(e_d) + \alpha_t^*(u)\pi_t(u) + \alpha_t^*(o)\pi_t(o) \right) f_t \right] w_t^* \underline{h}. \quad (20)$$

348 Optimality with respect to consumption and probability measures π satisfy (8)–(10). Thus,
 349 $c_t = c_t^*$, $x_{t+1} = x_{t+1}^*$, $\pi_t(e_d) = \pi_t^*(e_d)$, $\pi_t(e_{nd}) = \pi_t^*(e_{nd})$, $\pi_t(u) = \pi_t^*(u)$, $\pi_t(o) = \pi_t^*(o)$ satisfy
 350 optimality. Feasibility at the given prices follows by multiplying (2) with $\prod_{\tau=0}^t (R_\tau^*)^{-1}$, and
 351 adding across time to obtain (20). Finally, this allocation is consistent with firm's optimality
 352 and market clearing conditions. ■

353 The construction of the proof in Proposition 1 establishes that for any lottery-equilibrium,
 354 there is an associated sunspot-equilibrium. The proof is based on the property that sunspot
 355 prices are collinear with probabilities.⁹ Moreover, we have assumed that the sunspot space is

⁹Garratt et al. (2002) call these prices constant probability adjusted prices. Furthermore, they show that in economies with complete markets all sunspot allocations can be supported by price functions that are collinear with probabilities if the sunspot variable is continuous.

356 rich, allowing even for continuous ex-ante sunspot variables, so that the stochastic allocations
357 induced by the coordination on the sunspot mimics the set of gambles available to an
358 individual in the lottery economy.¹⁰ Taken together, these two points imply that the converse
359 of Proposition 1 is also true, completing our equivalence result. Below we elaborate on this,
360 building on results in Garratt et al. (2002) and Kehoe et al. (2002).

361 In Proposition 1, we start with a target musical chairs equilibrium allocation, and show that
362 it can be implemented as a sunspot equilibrium allocation, unique up to a relabelling of
363 states, by using the construction (15)–(18). Conversely, a sunspot equilibrium allocation
364 with prices collinear to probabilities as in expression (11) (which Garratt et al., 2002, call
365 probability adjusted constant prices), corresponds to a musical chairs allocation with lotteries
366 being pinned down by expressions (16) and (18). By construction, this candidate allocation
367 is feasible in the musical chairs economy, yields the same factor prices, and provides the
368 same utility level as the sunspot equilibrium allocation.¹¹ To complete the argument, we
369 show that it is an equilibrium in the musical chairs economy. To that end, first, we show
370 that any alternative lottery allocation that yields higher utility is not affordable; and second,
371 that the candidate musical chairs allocation is affordable. The proof of the first part follows
372 directly from the proof of Theorem 6.2 in Kehoe et al. (2002). A sketch of the argument is as
373 follows. Suppose there exists an alternative lottery allocation that yields higher utility and
374 is affordable. Then, from Proposition 1 we can use this alternative allocation to construct
375 a sunspot allocation that is affordable at the given sunspot equilibrium prices yielding the
376 same utility as the target allocation; hence, we arrive at our desired contradiction. Finally,
377 the candidate allocation is affordable, since it induces the same factor prices as in the sunspot
378 economy and, hence, satisfies budget constraints.

¹⁰Garratt (1995) shows that for any lottery equilibrium there is an associated sunspot equilibrium, but the converse is not necessarily true. The equivalence fails when the sunspot variable is restricted. He provided an example where a sunspot equilibrium exists when trade is restricted to three equiprobable states, but the same allocation is not an equilibrium in the lottery economy.

¹¹In the terminology of Kehoe et al. (2002) these two allocations are equivalent.

379 Proposition 1 has welfare implications. The sunspot allocation is Pareto efficient, given labor
 380 market frictions, if there is no alternative feasible allocation in which almost all households
 381 have no less utility and a positive measure of households have strictly more utility.

382 The following result applies.

383 **Proposition 2** *The sunspot equilibrium allocation is Pareto efficient.*

384 **Proof.** Proposition 2 is a direct consequence of non-satiation of utility, and the first welfare
 385 theorem. To see this, consider (13)–(14) and rewrite it as an AD equilibrium under certainty
 386 so that the first welfare theorem applies. To this end, consider the following definitions:

$$\psi_t = \sum_{\{s^{0t}, \phi^t\}} \mu_t(s^{0t}, \phi^t) \int_{s^{1t}} \psi(\sigma^t) ds^{1t}, \quad h_t = \underline{h} \sum_{\{s^{0t}, \phi^t\}} \mu_t(s^{0t}, \phi^t) \int_{s^{1t}} \mathbb{1}(\sigma^t) ds^{1t}, \quad p_t = \prod_{\tau=0}^t (R_\tau^*)^{-1}. \quad (21)$$

387 Problem (13)–(14) modify as follows

$$\max \sum_t \beta^t [U(c_t) - \psi_t], \quad (22)$$

388 subject to

$$\sum_t p_t (c_t + x_{t+1}) = \sum_t p_t (R_t^* x_t + w_t^* h_t), \quad (23)$$

389 where ψ_t denotes the time-varying disutility cost at date t ; h_t denote the time-varying
 390 endowment of time at date t ; and, p_t denotes AD prices with $\sum_t p_t < \infty$. This is equivalent
 391 to the neoclassical growth model with time-varying endowments and preferences, so that the
 392 first welfare theorem applies. ■

393 4 Steady state analysis

In this Section we restrict attention to the steady state of the model and discuss comparative
 statics. We assume $U(c) = \ln(c)$ and $F(k, n) = k^\theta n^{1-\theta}$ with $0 < \theta < 1$. The system of

equilibrium conditions consists of two blocks. The first block includes conditions (8)–(10) and market clearing conditions. The second block consists of motion equations for the aggregate labor market variables, as follows

$$n_t/\underline{h} \equiv N_t = (1 - u_t)\Pi_t, \quad (24)$$

$$N_t = \pi_t(e_{nd})(1 - \lambda_t)N_{t-1} + H_t f_t, \quad (25)$$

$$\Pi_t = \pi_t(e_{nd})(1 - \lambda_t)N_{t-1} + H_t, \quad (26)$$

$$H_t = \pi_t(u)U_{t-1} + \pi_t(o)O_{t-1} + \pi_t(e_d)\lambda_t N_{t-1}, \quad (27)$$

394 where N_t , U_t and O_t , denote measures of individuals, in turn, in the employment island,
 395 the unemployment island, and the leisure island (non-participants), at the end of date t ;
 396 $\Pi_t \equiv U_t + N_t$, is the labor force measure, H_t denotes the measure of individuals searching for
 397 jobs, and $u_t \equiv U_t/\Pi_t$ is the unemployment rate.

The equilibrium is described by the following two systems of equations

$$\left\{ \begin{array}{l} c_t^{-1} = \beta R_{t+1} c_{t+1}^{-1}, \\ \xi/f_t - \ln(1 - \underline{h}) = w_t \underline{h} c_t^{-1}, \\ c_t + k_{t+1} = k_t^\theta (\underline{h} N_t)^{1-\theta} + (1 - \delta)k_t, \\ w_t = (1 - \theta) \left(\frac{k_t}{\underline{h} N_t} \right)^\theta, \\ R_{t+1} = 1 - \delta + \theta \left(\frac{\underline{h} N_t}{k_t} \right)^\theta, \end{array} \right. \quad (28)$$

$$\left\{ \begin{array}{l} N_t = (1 - u_t)\Pi_t, \\ N_t = (1 - \lambda_t)N_{t-1} + H_t f_t, \\ \Pi_t = (1 - \lambda_t)N_{t-1} + H_t, \\ H_t = \pi_t(u)U_{t-1} + \pi_t(o)O_{t-1} + \pi_t(e_d)\lambda_t N_{t-1}. \end{array} \right. \quad (29)$$

398 System (28) corresponds to the neoclassical growth model, with an endogenous labor market

399 wedge in the second equation of the system, given by

$$\begin{aligned}
 w_t \underline{h} &= \text{labor wedge} \times \text{MRS} \\
 &= \left[\frac{(\xi/f_t) - \ln(1 - \underline{h})}{-\ln(1 - \underline{h})} \right] \left[\frac{-\ln(1 - \underline{h})}{1/c_t} \right], \tag{30}
 \end{aligned}$$

400 where $\text{MRS} = -\ln(1 - \underline{h}) c_t$, corresponds to the marginal rate of substitution between leisure
 401 and consumption in the absence of an opportunity cost of participation. The labor wedge is
 402 an outcome of search frictions, because the opportunity cost of participation is different from
 403 zero.¹²

404 It follows from system (29) that the composition of H is indeterminate (see [Ljungqvist and](#)
 405 [Sargent, 2008](#), for a related result). In the sunspot equilibrium, an equilibrium composition for
 406 H is selected through sunspots. Specifically, any restriction on parameters $[\pi(u), \pi(o), \pi(e_d)]$,
 407 maps into a sunspot equilibrium via conditions (16) and (18).

408 Next, we focus on the steady state of (28) and (29), and study how changes in search frictions
 409 affect the equilibrium level of employment, unemployment and participation. Moreover, using
 410 the same example, we examine the ability of the model to match gross worker flows, since an
 411 advantage of our model is that it identifies individual labor market transitions (in contrast to
 412 the [Merz, 1995](#), large family model). Finally, we look at dynamics away from the steady state

¹²Our analysis follows much of the literature (for example, [Chang and Kim, 2007](#); [Shimer, 2013](#); [Krusell et al., 2011, 2017](#)) by only considering the extensive margin of adjustment in hours (hence, \bar{h} is held constant). As we are considering steady state gross flows for a given labor market, relaxing this assumption would have no implications for the analysis of the competitive equilibrium that follows and, in particular, the results reported in Table 1. However, allowing for an intensive and an extensive margin is interesting if one wants to compare outcomes across economies with different sets of labor market policies. For example, different countries with different institutions (including unemployment insurance, employment protection and other tax and transfer policies) might have a different split of total hours between the intensive and extensive margins, and this would affect gross worker flows too. [Fang and Rogerson \(2009\)](#) offer a detailed treatment of how such policies may affect the split between employment and hours per worker across countries with different labor market institutions, in a canonical labor supply model with search frictions. If one extends our analysis beyond steady state comparisons, allowing for cyclical fluctuations in the amount of hours per worker is also interesting because it implies fluctuations in the opportunity cost of employment. In an influential paper, [Chodorow-Reich and Karabarbounis \(2016\)](#) explore this channel and show empirically that procyclical hours per worker contribute to making the opportunity cost of employment procyclical.

413 equilibrium by changing the job finding rate to mimic a typical recession and characterise
414 the transition back to the steady state.

415 **4.1 Search frictions and aggregate participation**

416 The steady state of (28) and (29) is presented in Appendix B. In particular, the steady state
417 labor market allocations are determined by the cost of participation, ξ , and parameters
418 describing the labor market frictions, (λ, f) , the Ins and Outs of unemployment. Following
419 Krusell et al. (2010, 2011, 2017), we analyse how a reduction in the job-finding rate affects
420 steady state labor market outcomes.

421 We establish the following Proposition:

422 **Proposition 3** *A fall in the job finding rate f has the following impact on steady state labor*
423 *market outcomes:*

- 424 1. *lowers aggregate employment, N ;*
- 425 2. *raises the unemployment rate, u ;*
- 426 3. *has an ambiguous effect on the labor force participation, Π .*

427 The proof of Proposition 3 is in Appendix B.

428 The reduction in the job finding rate lowers aggregate employment through the increase in
429 the labor wedge, which from (30) implies that the MRS must fall (since the real wage is
430 pinned down by technology and preferences, and is not affected by search frictions in steady
431 state). Thus, consumption must fall, requiring a lower level of capital and employment.

432 The unemployment rate must increase since the steady state unemployment rate is determined
433 only by the balancing between the inflow rate into unemployment and the outflow rate. As
434 the inflow rate is constant, determined by the destruction rate λ , a reduction in the outflow
435 rate, determined by f , must raise the unemployment rate in steady state.

436 The ambiguous effect on aggregate participation lead us to the following proposition.

437 **Proposition 4** *There exists a threshold level of ξ , denoted $\widehat{\xi}$, such that at $\xi > \widehat{\xi}$ an increase*
 438 *in the finding rate, f , raises participation, and at $\xi < \widehat{\xi}$ an increase in f lowers participation.*
 439 *At $\xi = \widehat{\xi}$, participation is acyclical. The threshold level is equal to*

$$\widehat{\xi} = - \left[\frac{\lambda \ln(1 - h)}{1 - \lambda} \right]. \quad (31)$$

440 The proof of Proposition 4 is in the Appendix B.

441 A (permanent) change in the finding rate, f , affects the aggregate level of participation via
 442 three channels. The first channel is through returns to market work via the “effective” real
 443 wage rate, wf (the substitution effect). The second channel is through the opportunity cost
 444 of employment, the left hand side of the intratemporal condition in (28), so that increases in
 445 the finding rate increase the opportunity cost, which, in turn, discourages participation in the
 446 labor market. The net substitution effect, taking into account the opportunity cost channel,
 447 affects labor supply decisions via the labor wedge in expression (30). The third channel is
 448 the income effect from a permanent change in the finding rate, which affects the budget set
 449 of the stand-in agent through the effective real wage.

450 At $\xi = \widehat{\xi}$, the net substitution and income effects cancel out and aggregate participation is
 451 acyclical; while at $\xi > \widehat{\xi}$, the net substitution dominates and participation is procyclical, and
 452 at $\xi < \widehat{\xi}$, the income effect dominates and participation is countercyclical.

453 It follows from Proposition 4 that the model can deliver both a countercyclical or a procyclical
 454 participation rate, depending on the elasticity of the labor wedge to changes in f , controlled by
 455 the parameter ξ , the opportunity cost of participation. Thus, the neoclassical growth model
 456 with search frictions can be reconciled with a mildly procyclical participation rate. In turn,
 457 this result is particularly important given the tendency for models featuring intertemporal
 458 substitution in frictional labor markets to deliver excessively procyclical participation and,

459 thus, procyclical unemployment (a problem stressed by [Ravn, 2008](#); [Shimer, 2013](#), for
 460 example).

461 4.2 Gross worker flows

462 Unlike the [Merz \(1995\)](#) large family set-up which only identifies net worker flows, our model
 463 yields equilibrium outcomes for gross worker flows. To illustrate this point, we present a
 464 simple quantitative exercise to evaluate the model's ability to explain the average gross flows
 465 in the data. In particular, despite its parsimony the model is able to account well for the
 466 transitions between unemployment and inactivity, which previous literature has shown to be
 467 challenging.

468 The model yields gross flows across the three states of employment, unemployment, and
 469 non-participation, resulting from individual optimal behaviour, given by

$$\begin{aligned}
 \phi_{ee,t} &= (1 - \lambda_t) + \pi_t(e_d)\lambda_t f_t, & \phi_{ue,t} &= \pi_t(u) f_t, & \phi_{oe,t} &= \pi_t(o) f_t, \\
 \phi_{eu,t} &= \pi_t(e_d)\lambda_t (1 - f_t), & \phi_{uu,t} &= \pi_t(u) (1 - f_t), & \phi_{ou,t} &= \pi_t(o) (1 - f_t), \\
 \phi_{eo,t} &= \lambda_t (1 - \pi_t(e_d)), & \phi_{uo,t} &= 1 - \pi_t(u), & \phi_{oo,t} &= 1 - \pi_t(o),
 \end{aligned} \tag{32}$$

470 with $\phi_{ss',t}$ the transition rate from state s to state s' , for $s, s' \in \{e, u, o\}$, in period t , implied
 471 by the labor market parameters, f and λ and the randomisation induced by the optimal
 472 choices for the lotteries over labor force participation. The latter may induce in equilibrium
 473 different participation probabilities chosen by the individuals starting in employment but
 474 who lose their jobs, those unemployment and those out of the labor force, in turn, $\pi_t(e_d)$,
 475 $\pi_t(u)$ and $\pi_t(o)$. We argue below that this feature is important for the success of the model
 476 to match the gross worker flows across the unemployment and non-participation states.

477 In the sequel we focus on steady state transition probabilities. For the US, we measure
 478 gross worker flows empirically from the longitudinal monthly Current Population Survey
 479 (CPS), as explained for example in [Elsby et al. \(2015\)](#) and [Krusell et al. \(2017\)](#). We test the

Table 1: Gross worker flows (model and data)

$\phi_{s,s'}$	to s' :		
	e	u	o
from s :			
e	0.977 (0.972)	0.017 (0.014)	0.006 (0.014)
u	0.229 (0.228)	0.637 (0.637)	0.134 (0.135)
o	0.010 (0.022)	0.027 (0.021)	0.963 (0.957)
<u>calibrated values</u>			
λ	0.0290		
f	0.2645		
$\pi(o)$	0.0373		
$\pi(e_d)$	0.7848		
$\pi(u)$	0.8660		

Notes: In the first panel, values outside parenthesis are obtained from the model and the values in parenthesis are the empirical counterpart, obtained from [Krusell et al. \(2017\)](#), and used as targets. The lower panel reports the calibrated value for each parameter.

480 model’s ability to explain labor market transitions with a simple calibration experiment. We
 481 select values for the parameters determining labor market transitions, $[\lambda, f, \pi(o), \pi(e_d)]$,
 482 to minimise a distance criterion function of the deviations of the gross transitions from their
 483 empirical counterparts, given the equilibrium conditions (29), and for an employment rate
 484 set to $N = 65\%$.

485 Table 1 compares the gross flows implied by the calibrated example economy to their empirical
 486 counterparts (as reported in [Krusell et al., 2017](#), based on the CPS longitudinal micro data),
 487 and reports the implied calibrated values for the vector vector of parameters. Despite the
 488 parsimonious set of parameters to match nine targets, the model does a relatively good job at
 489 matching gross flows, comparable to the results in [Krusell et al. \(2017\)](#), who develop a richer
 490 incomplete market model with heterogeneous agents. The model is particularly successful at

491 matching the high transition rate from unemployment to inactivity, ϕ_{uo} , which the literature
492 has found challenging.¹³

493 Key to the success of the model to match the transition from unemployment to inactivity is
494 the indeterminacy in the composition of the stock of job searchers, H . This indeterminacy is
495 resolved by the sunspot mechanism which yields different participation probabilities chosen
496 by the individuals starting in employment but who lose their jobs, those unemployment and
497 those out of the labor force, in turn, $\pi_t(e_d)$, $\pi_t(u)$ and $\pi_t(o)$. From equation (32) we see that
498 $\phi_{uo} = 1 - \pi_t(u)$, the transition rate from unemployment to inactivity is entirely determined by
499 $\pi_t(u)$. Thus, it is possible to construct a sunspot equilibrium from (15) and (16), to match
500 successfully the ϕ_{uo} transition rate.

501 5 Conclusion

502 This paper shows that the same aggregation as in [Andolfatto \(1996\)](#) can be obtained without
503 either lotteries or additional exogenous randomization (the game of musical chairs), when
504 individual choices over contingent commodities are coordinated by sunspots. We show that
505 this aggregation approach offers a tractable method to construct a general equilibrium model
506 of gross worker flows. The upshot is that the economy with sunspots yields testable predictions
507 about gross workers flows, which may be confronted with micro level data on labor market
508 transitions.

509 Although lotteries are socially optimal in economies with indivisibilities, they have been
510 repudiated by some as an employment allocation mechanism, on the grounds that such ideal
511 device is not empirically plausible ([Browning et al., 1999](#); [Ljungqvist and Sargent, 2011](#)).

¹³[Garibaldi and Wasmer \(2005\)](#), in a model with linear utility, and [Krusell et al. \(2011\)](#), in a model with concave utility and incomplete markets, both show that the transition rates from unemployment to inactivity are difficult to account for in three-state equilibrium models of the labor market, without additional heterogeneity across individuals to achieve the calibration target. [Garibaldi and Wasmer \(2005\)](#) experiment with permanent heterogeneity across workers, while [Krusell et al. \(2011\)](#) consider transitory productivity shocks to match the transition from unemployment to inactivity.

512 Previous work by [Shell and Wright \(1993\)](#), [Garratt et al. \(2002\)](#) and [Kehoe et al. \(2002\)](#)
513 shows how to avoid the need for such implausible randomization mechanisms, by establishing
514 the close connection between lottery economies and sunspot economies. We extend their
515 approach to accommodate economies with labor market search frictions. The resulting model
516 can obtain plausible individual employment histories, as illustrated by the empirically realistic
517 gross worker flows in a calibrated example.

518 Turning to future work, the fact that an equilibrium with musical chairs can be decentralized
519 with sunspots, opens the possibility to study adverse selection and moral hazard in labor
520 markets with search frictions, using results for sunspot equilibria in incentive constrained
521 economies ([Kehoe et al., 2002](#)).

522 Appendix

523 A Lottery equilibrium

524 **Proposition 5** *An equilibrium with musical chairs and lotteries is characterised by $\pi_t(\tilde{i}) \in$*
525 *$(0, 1)$, for $\tilde{i} \in \{e_d, u, o\}$, and $\pi_t(e_{nd}) = 1$.*

Proof. Let us argue by contradiction. Suppose $\pi_t(e_{nd}) \in [0, 1)$ and $\pi_t(\tilde{i}) \in [0, 1]$. Then, $\pi_t(e_{nd}) \in [0, 1)$ requires (10) to modify as follows:

$$\xi - \ln(1 - \underline{h}) \geq w_t \underline{h} U_c(c_t) \quad (\text{A.1})$$

Multiplying both sides of (A.1) by f_t , yields

$$\xi - f_t \ln(1 - \underline{h}) > f_t \xi - f_t \ln(1 - \underline{h}) \geq f_t w_t \underline{h} U_c(c_t), \quad (\text{A.2})$$

526 which in turn, requires $\pi_t(\tilde{i}) = 0$, for $\tilde{i} \in \{e_d, u, o\}$. Subsequently, the employment law of
527 motion in (25) requires $H = 0$ and imposing the steady state restriction, it follows that
528 $\pi(e_{nd}) = 1/(1 - \lambda) > 1$, which is a contradiction. ■

529 B Steady state and comparative statics

530 In this Section we compute the steady state allocation and the comparative statics for the
531 example economy presented in Section 4.

The steady state of the first block, system (28), after imposing steady state, reduces to

$$\frac{y}{k} = \left(\frac{1/\beta - 1 + \delta}{\theta} \right) \quad (\text{B.1})$$

$$\frac{n}{k} = \left(\frac{1/\beta - 1 + \delta}{\theta} \right)^{1/(1-\theta)}, \quad (\text{B.2})$$

$$\frac{c}{k} = \left(\frac{1/\beta - 1 + \delta}{\theta} \right) - \delta \quad (\text{B.3})$$

$$n = \frac{f}{\xi - f \ln(1 - \underline{h})} \frac{1 - \theta}{1 - \delta(k/y)}. \quad (\text{B.4})$$

In turn, the steady state of the second block yields

$$H = \frac{\lambda}{\xi - f \ln(1 - \underline{h})} \frac{1 - \theta}{1 - \delta(k/y)} \frac{1}{\underline{h}}, \quad (\text{B.5})$$

$$\Pi = \left(\frac{\lambda}{f} + 1 - \lambda \right) \frac{n}{\underline{h}}, \quad (\text{B.6})$$

$$O = 1 - \Pi, \quad (\text{B.7})$$

$$U = \Pi - \frac{n}{\underline{h}}, \quad (\text{B.8})$$

$$u = \frac{\lambda(1 - f)}{\lambda + f(1 - \lambda)}. \quad (\text{B.9})$$

It follows from (B.4), (B.6), (B.9) that the elasticity of employment, unemployment rate and participation, respectively, with respect to f is equal to

$$\epsilon_{N,f} = \frac{\xi}{\xi - f \ln(1 - \underline{h})} > 0, \quad (\text{B.10})$$

$$\epsilon_{u,f} = - \frac{1}{1 - \lambda + \lambda/f} \frac{1}{1 - f} < 0, \quad (\text{B.11})$$

$$\epsilon_{\Pi,f} = \frac{\xi}{\xi - f \ln(1 - \underline{h})} - \frac{\lambda/f}{\lambda/f + 1 - \lambda}, \quad (\text{B.12})$$

⁵³² where $\epsilon_{X,Y} \equiv (dX/dY)(Y/X)$ denotes the elasticity of X with respect to Y . The result below
⁵³³ follows directly from (B.12).

Corollary 1 *There exist $\widehat{\xi}$ such that $\epsilon_{\Pi,f} = 0$. For $\xi > \widehat{\xi}$ it follows that $\epsilon_{\Pi,f} > 0$ whereas for*

$\xi < \widehat{\xi}$ it follows that $\epsilon_{\Pi, f} < 0$. The threshold level is equal to

$$\widehat{\xi} = - \left[\frac{\lambda \ln(1 - h)}{1 - \lambda} \right]. \quad (\text{B.13})$$

References

- 535 Alvarez, F. and M. Veracierto (1999). Labor-market policies in an equilibrium search model.
536 *NBER macroeconomics annual* 14, 265–304.
- 537 Andolfatto, D. (1996). Business cycles and labor-market search. *American Economic*
538 *Review* 86(1), 112–132.
- 539 Barnichon, R. and A. Figura (2015). Labor market heterogeneity and the aggregate matching
540 function. *American Economic Journal: Macroeconomics* 7(4), 222–49.
- 541 Browning, M., L. P. Hansen, and J. J. Heckman (1999). Micro data and general equilibrium
542 models. *Handbook of macroeconomics* 1, 543–633.
- 543 Chang, Y. and S.-B. Kim (2006). From individual to aggregate labor supply: A quanti-
544 tative analysis based on a heterogeneous agent macroeconomy. *International Economic*
545 *Review* 47(1), 1–27.
- 546 Chang, Y. and S.-B. Kim (2007). Heterogeneity and aggregation: Implications for labor-
547 market fluctuations. *American Economic Review* 97(5), 1939–1956.
- 548 Chodorow-Reich, G. and L. Karabarbounis (2016). The cyclicity of the opportunity cost of
549 employment. *Journal of Political Economy* 124(6), 1563–1618.
- 550 Christiano, L. J., M. S. Eichenbaum, and M. Trabandt (2020). Why is unemployment so
551 countercyclical? Technical report, National Bureau of Economic Research.
- 552 Cole, H. L. (1989). General Competitive Analysis in an Economy with Private Information:
553 Comment. *International Economic Review* 30(1), 249–252.
- 554 Elsby, M. W. L., B. Hobijn, and A. Şahin (2015). On the importance of the participation
555 margin for labor market fluctuations. *Journal of Monetary Economics* 72, 64–82.

- 556 Fang, L. and R. Rogerson (2009). Policy analysis in a matching model with intensive and
557 extensive margins. *International Economic Review* 50(4), 1153–1168.
- 558 Garibaldi, P. and E. Wasmer (2005). Equilibrium search unemployment, endogenous par-
559 ticipation, and labor market flows. *Journal of the European Economic Association* 3(4),
560 851–882.
- 561 Garratt, R. (1995). Decentralizing lottery allocations in markets with indivisible commodities.
562 *Economic Theory* 5(2), 295–313.
- 563 Garratt, R., T. Keister, C.-Z. Qin, and K. Shell (2002). Equilibrium prices when the sunspot
564 variable is continuous. *Journal of Economic Theory* 107(1), 11–38.
- 565 Garratt, R., T. Keister, and K. Shell (2004). Comparing sunspot equilibrium and lottery
566 equilibrium allocations: the finite case. *International Economic Review* 45(2), 351–386.
- 567 Hansen, G. D. (1985). Indivisible labor and the business cycle. *Journal of Monetary*
568 *Economics* 16(3), 309–327.
- 569 Kehoe, T. J., D. K. Levine, and E. C. Prescott (2002). Lotteries, sunspots, and incentive
570 constraints. *Journal of Economic Theory* 107(1), 39–69.
- 571 Kroft, K., F. Lange, M. J. Notowidigdo, and L. F. Katz (2016). Long-term unemployment and
572 the great recession: the role of composition, duration dependence, and nonparticipation.
573 *Journal of Labor Economics* 34(S1), S7–S54.
- 574 Krusell, P., T. Mukoyama, R. Rogerson, and A. Şahin (2008). Aggregate implications of
575 indivisible labor, incomplete markets, and labor market frictions. *Journal of Monetary*
576 *Economics* 55(5), 961–979.
- 577 Krusell, P., T. Mukoyama, R. Rogerson, and A. Şahin (2010). Aggregate labor market
578 outcomes: the roles of choice and chance. *Quantitative Economics* 1(1), 97–127.

- 579 Krusell, P., T. Mukoyama, R. Rogerson, and A. Sahin (2011). A three state model of worker
580 flows in general equilibrium. *Journal of Economic Theory* 146(3), 1107–1133.
- 581 Krusell, P., T. Mukoyama, R. Rogerson, and A. Şahin (2017). Gross worker flows over the
582 business cycle. *American Economic Review* 107(11), 3447–76.
- 583 Ljungqvist, L. and T. J. Sargent (2008). Taxes, benefits, and careers: Complete versus
584 incomplete markets. *Journal of Monetary Economics* 55(1), 98–125.
- 585 Ljungqvist, L. and T. J. Sargent (2011). A labor supply elasticity accord? *American*
586 *Economic Review* 101(3), 487–91.
- 587 Lucas, R. E. and E. C. Prescott (1974). Equilibrium search and unemployment. *Journal of*
588 *Economic Theory* 7(2), 188–209.
- 589 Merz, M. (1995). Search in the labor market and the real business cycle. *Journal of Monetary*
590 *Economics* 36(2), 269–300.
- 591 Merz, M. (1997, May). A market structure for an environment with heterogeneous job-
592 matches, indivisible labor and persistent unemployment. *Journal of Economic Dynamics*
593 *and Control* 21(4-5), 853–872.
- 594 Mortensen, D. T. and C. A. Pissarides (1994). Job creation and job destruction in the theory
595 of unemployment. *The review of economic studies* 61(3), 397–415.
- 596 Prescott, E. C. and R. M. Townsend (1984). General competitive analysis in an economy
597 with private information. *International Economic Review* 25(1), 1–20.
- 598 Ravn, M. O. (2008). The consumption-tightness puzzle. In *NBER International Seminar on*
599 *Macroeconomics 2006*, pp. 9–63. University of Chicago Press.
- 600 Rogerson, R. (1988). Indivisible labor, lotteries and equilibrium. *Journal of Monetary*
601 *Economics* 21(1), 3–16.

- 602 Shell, K. and R. Wright (1993). Indivisibilities, lotteries, and sunspot equilibria. *Economic*
603 *Theory* 3(1), 1–17.
- 604 Shimer, R. (2013). Job search, labor force participation, and wage rigidities. In *Advances*
605 *in Economics and Econometrics: Volume 2, Applied Economics: Tenth World Congress*,
606 Volume 50, pp. 197. Cambridge University Press.
- 607 Veracierto, M. (2008). On the cyclical behavior of employment, unemployment and labor
608 force participation. *Journal of Monetary Economics* 55(6), 1143–1157.