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1 **Management of Conjugate Heat Transfer Using Various Arrangements of Cylindrical**  
2 **Vortex Generators in Micro-Channels**

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7  
8 **Abstract**

9 Placing cylindrical vortex generators (VGs) at the base of a uniform micro-channel heat sink (MCHS)  
10 enhances the heat transfer, but incurs a substantial pressure drop. The effect of different VG parameters,  
11 including position (front, middle or back), radius (R) in the range of (100-300)  $\mu\text{m}$  and distance (D)  
12 between them (0-500)  $\mu\text{m}$  are considered to enhance the conjugate heat transfer. Laminar flow and heat  
13 flux conditions relevant to microelectronics water cooling systems (100  $\text{W}/\text{cm}^2$ ) are used. The  
14 numerical approach, using COMSOL Multiphysics<sup>®</sup> software, is validated and found to be in good  
15 agreement against benchmark experimental and numerical studies. It is generally found that VGs  
16 enhance heat transfer but that the pressure drop increases. The lowest thermal resistance is achieved  
17 when placing VGs at the front of the MCHS with no distance between them and  $R=300 \mu\text{m}$ , but this  
18 also results in the highest pressure penalty. Results also show that it is not necessarily the best heat  
19 transfer enhancement that leads to the highest thermal-hydraulic performance (PEC) index. The highest  
20 PEC index is achieved at the front position, with  $R=100$ ,  $D=0\mu\text{m}$  and  $\text{Re} > 250$ .

21  
22 **Keywords:** Thermal-hydraulic performance (PEC), Micro-scale cooling system, Thermal  
23 management, Vortex generators position, pressure drop reduction.

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27 **Nomenclature**

28	$A_s$	surface area of the whole heat sink ( $\mu\text{m}^2$ )	$T$	Temperature, K
29	$CFD$	Computational Fluid Dynamics	$X$	Axial distance, $\mu\text{m}$
30	$C_p$	Specific heat, J/Kg.K	<b>Greek Symbols</b>	
31	$D$	Distance between VGs, $\mu\text{m}$	$\mu$	Viscosity, Pa.s
32	$FEM$	Finite Element Method	$\theta$	Thermal resistance, K/W
33	$K$	Thermal conductivity, W/m.K	$\rho$	Density, $\text{kg/m}^3$
34	$L$	Channel length, $\mu\text{m}$	<b>Subscripts</b>	
35	$VGs$	Vortex generators (VGs)	<i>ave</i>	Average
36	$\Delta P$	Pressure Drop, $\text{N/m}^2$	<i>In</i>	Inlet
37	$q$	Uniform heat flux, $\text{W/cm}^2$	<i>max</i>	Maximum
38	MCHS	Micro-Channel Heat Sink	<i>Out</i>	Outlet
39	$R$	Radius of VGs, $\mu\text{m}$	$S$	Surface
40	$Re$	Reynolds number	$s$	Solid
41			$L$	Liquid

41

42 **1. Introduction**

43 Effective thermal management in electronic micro-chips is crucial since the excessive heat  
44 generated can cause damage to the micro-chip components [1]. Inexorable reductions in the  
45 size of the components and increases in processor power makes it even more challenging for  
46 thermal researchers to produce an effective cooling method and/or a design to remove the  
47 generated heat.

48 Researchers have made several important discoveries about the potential of using air and liquid  
49 cooling to remove heat effectively from the micro-system [2]. Different methods of cooling  
50 have been introduced such as micro-jet impingement, thermo-electron coolers, forced air  
51 cooling, micro-heat pipes, micro-electro-hydrodynamics, and micro-channel heat sinks  
52 (MCHSs) [3-5]. The best method of cooling discovered from these methods is to use MCHS  
53 due to its higher surface area to volume ratio value [2]. One of the earliest MCHS systems used  
54 an air-cooled system, but due to increasing rates of energy dissipation required, different  
55 working fluids have been used (i.e. nanofluids or ionic liquids) to provide more effective heat  
56 removal systems, albeit with a high pressure penalty [6-13]. Interestingly, even though the  
57 overall enhancement (Performance Evaluation Criteria (PEC) index) is not significant, this has  
58 motivated researchers to investigate the possibility of implementing advanced fluids that have  
59 high thermal properties in heat transfer systems. For example, the PECs for nanofluids are often

60 poor (with  $PEC < 1$ ) [1], but they are still attracting researchers to investigate the heat transfer  
61 enhancement neglecting the pressure penalty[14].

62 It is necessary to enhance the heat transfer rate of MCHS due to the rapid developments of  
63 micro-chips whilst avoiding infeasible growth in the associated pressure drop. One potential  
64 method, which is examined here, includes adding extra geometry (extended surface area) to the  
65 channel which is called a vortex generator (VG). VGs were first introduced in 1969 by Johnson  
66 and Joubert for heat transfer improvement [15]. VGs come in different shapes including wings,  
67 winglets, blocks, protrusions, fins and ribs [16-22]. The goal of a VG is to disturb the flow in  
68 the channel to improve heat transfer performance. The disturbed flow will create vortices which  
69 can be categorised into transverse and longitudinal vortices [23, 24]. A transverse vortex has its  
70 rotation axis at a right angle to the direction of flow and a longitudinal vortex has it parallel to  
71 the direction of flow [25-29]. The installed VG can be either at the bottom or on the side walls  
72 of the MCHS or both. The effective use of VGs has led to significant improvements in the heat  
73 transfer performance of micro-channels [27]. For instance, Wong and Lee [30] found that heat  
74 transfer was enhanced by placing triangular ribs in the transverse micro-chamber and concluded  
75 that incrementing the width and the height of the ribs improves heat transfer, while increasing  
76 the pressure drop [12].

77 Ebrahimi et al. [18] and Datta et al. [24] considered inclined longitudinal VGs (LVGs) within  
78 a straight rectangular micro-channel heat sink. From their findings, vortices size increases with  
79 increasing LVG angle and Reynolds number. As the size of vortices increases, the convective  
80 heat transfer increases since there is continuous breaking of the boundary layer and flow re-  
81 initialisation. But this enhanced rate of heat transfer is at the expense of a large pressure drop.  
82 Samadifar and Toghraie [31] introduced six new type of VGs on fin-plate heat exchangers using  
83 triangular channel profiles. From their results, the simple rectangular VG (SRW) has the highest  
84 rate of heat transfer with 7% increment compared to other five VGs shapes. All VGs shapes  
85 studied show an increase in pressure drop within the channel. Convective heat transfer is  
86 increased as the height of VGs increased. For a  $45^\circ$  angle of attack of VG, the highest overall  
87 performance achieved.

88 Khoshvaght-Aliabadi et al. [32] used longitudinal spacing among delta-winglets VGs in straight  
89 channels. They stated that the heat transfer coefficient is enhanced by 50% using two side cuts  
90 and four delta-winglets and a high to low (HL) arrangement compared to a smooth channel.  
91 The use of the HL arrangement shows a great increase in heat transfer coefficient while the  
92 Low to High (LH) arrangement shows an increase in pressure drop. The pressure drop is greatly

93 influenced by the number of delta-winglets used. Overall hydrothermal performance is  
94 achieved when using the one side cut and one delta-winglet configuration and uniform (U)  
95 arrangement as well as the HL arrangement with two side cuts and two delta-winglets. Lu and  
96 Zhai [33] utilised winglet-type VGs with dimples in their micro-channel heat sink. Five  
97 different configurations tested were smooth micro-channel, micro-channel with only VGs,  
98 micro-channel with only dimples, micro-channel with both dimples and VGs – “common flow  
99 up” and “common flow down”. Their results showed that using dimples and VGs induces  
100 significant improvement in heat transfer with a lower pressure penalty. The “common flow up”  
101 and “common flow down” configurations of VGs shows an improvement in heat transfer when  
102 they are used together with dimples with a 2.4-4.7% enhancement. The “common flow down”  
103 shows better performance in heat transfer compared to the “common flow up” configuration.  
104 Li et al. [34] used VGs to increase the thermal performance of pin-fin heat sinks. Increasing the  
105 height of VGs results in a decrease in thermal resistance. Using the common-flow-up  
106 configuration gives lower thermal resistance compared to the common-flow-down  
107 configuration. An angle of attack of 30° give the best overall performance for both thermal  
108 resistance and pressure drop. Setting the shortest distance between VG would also give the best  
109 thermal-hydraulic performance of heat sink. From this work, only a small thermal resistance  
110 enhancement is achieved while there is a very large pressure drop increase.

111 Li et al. [35] used rectangular VGs combined with triangular cavities on the side walls and  
112 achieved improved heat transfer performance due to the fluid mixing from the flow disturbance  
113 and the formation of a hydrodynamic layer. As the width increases, the friction factor and  
114 Nusselt number are improved. The heat transfer enhancement factor improved by 1.61 when  
115 using cavity and rib widths of 0.3 and 2.24, respectively, at a Reynolds number of 500 compared  
116 to conventional MCHS. Khoshvaght-Aliabadi et al. [36] utilised plate-fin heat exchanger  
117 (PFHE) with VGs. They concluded that, rectangular wings enhance the performance of heat  
118 transfer by 58.3% compared to PFHE without wings. The pressure drop values increases when  
119 wings’ pitch and height decrease and wings’ width, channel length and angle of attack increase.  
120 The wings’ height and angle of attack has the most significant effect on the performance  
121 evaluation criteria. Chai et al. [37] compared five shapes of sidewall ribs (forward triangular,  
122 backward triangular, equal triangular and semi-circular) inside a rectangular channel.  
123 Enhancement of heat transfer was achieved using ribs but with a higher pressure drop penalty.  
124 The results showed the circular ribs to have the lowest thermal resistance compared to other  
125 VG shapes.

126 Considering the use of cylindrical VGs, Al-Asadi et al. [26] confirmed that the semi-circular  
127 VGs offered the lowest thermal resistance compared to the other shapes when VGs were placed  
128 at the bottom of the channel. Al-Asadi et al. [27] investigated subsequently the influence of  
129 cylindrical VGs and reported that cylindrical VGs (half-cylinder and quarter-cylinder VGs)  
130 increase MCHS performance. The radius of the VGs (0-400  $\mu\text{m}$ ) and the heat flux were varied  
131 in the study with Re ranging from 100 to 2300. It was found that half-circle VGs are more  
132 effective than quarter-circle VGs for heat transfer improvement. The half-circle VG resulted in  
133 lower pressure drop compared to the quarter-circle VG. Moreover, Al-Asadi et al. [23]  
134 thoroughly studied three different models of placing the VG for full span, centred and split  
135 configurations. The results showed that the centred VG offered better heat transfer  
136 improvement compared to the other two models with an optimum number of VGs (5 circular  
137 VGs).

138 Using VGs offered heat transfer enhancements, however, the pressure penalty was increased.  
139 Thus, the literature has shown a gap of knowledge in how to enhance the heat transfer in micro-  
140 channel heat sinks (MCHSs) while controlling the increase in pressure drop. This point has  
141 motivated researchers to propose novel ways in which heat transfer can be enhanced while  
142 trying to reduce the increase in pressure drop and one promising alternative is to employ  
143 cylindrical vortex generators (VGs) [23]. To the best of the authors' knowledge, there is  
144 currently a significant knowledge gap on how VGs distribution can be used to provide effective  
145 thermal management by enhancing heat transfer while controlling the increase in pressure drop.  
146 Therefore, this study proposes a simple geometrical modification to mitigate the increase in  
147 pressure drop when using VGs in micro-channels. From the reviewed literature, it can be seen  
148 that having very small thermal resistance reduction while having very large pressure drop  
149 increase can reduce the effectiveness of heat sinks [34, 38], this will be discussed further in  
150 **Section 5.3** regarding the PEC index analysis.

151 This study extends a series of publications [23, 26, 27, 37], to explore the influence of different  
152 positions of VGs (at the front, middle and back) and determine the optimum radius, R, and  
153 distance between VGs, which have not been considered previously. These changes will be  
154 beneficial by enhancing the heat transfer and reduce the increase in pressure drop  
155 simultaneously. The paper is organised as follows. The problem specification is given in  
156 **Section 2**. The 3-D computational method (conjugate heat transfer model, boundary conditions  
157 and heat transfer performance) are described in **Section 3**. A mesh independence study is

158 presented in **Section 4**. The results and discussion and conclusion are given in **Section 5** and  
 159 **Section 6** respectively.

160

## 161 2. Problem Specification

162 The geometry of the MCHS has the dimensions given in Table 1, and a base area of  $25 \times 10^8$   
 163  $\mu\text{m}^2$  as shown in **Fig. 1 (A1)**. To compare the performance of the modified MCHS, a baseline  
 164 micro-channel is constructed as a guideline (**see Fig. 1 (B)**). The MCHSs have VGs added at  
 165 the bottom of the micro-channel. The channel is divided into 3 equal lengths of front, middle,  
 166 or back which act as a full channel where the VGs are positioned evenly in each division (**see**  
 167 **Fig. 1 (D)**). The VGs are placed only in one division at a time for analysis in this study and not  
 168 simultaneously between divisions. Each division has five VGs, each with a range of radii,  $R$ ,  
 169 and rib distances,  $D$ .

170

## 171 3. Computational method

### 172 3.1 Conjugate heat transfer model

173 The model of the MCHS employs a number of simplifying assumptions. The flow of water is  
 174 considered as laminar, steady, and Newtonian and to have a temperature-dependent density and  
 175 viscosity [23, 26, 39]. Gravitational effects are neglected in such a small domain with forced  
 176 convection. The 3D velocity of water  $\mathbf{u} = (u, v, w)$  in the  $(x, y, z)$  cartesian coordinate  
 177 directions with  $p$ ,  $\rho$  and  $\mu$  the pressure, density and the viscosity of the liquid respectively. The  
 178 governing equations used are the continuity and Navier-Stokes equations:

$$179 \quad \nabla \cdot \mathbf{u} = 0 \quad (1)$$

$$180 \quad \rho(T)(\mathbf{u} \cdot \nabla)\mathbf{u} = \nabla \cdot \left[ -p\mathbf{I} + \mu(T)(\nabla\mathbf{u} + (\nabla\mathbf{u})^T) - \frac{2}{3}\mu(T)(\nabla \cdot \mathbf{u})\mathbf{I} \right] \quad (2)$$

181

182 For the liquid phase, the energy equation is as follows:

$$183 \quad \rho C_p \mathbf{u} \cdot \nabla T_L = k \nabla^2 T_L \quad (3)$$

184 where  $C_p$ ,  $T_L$ , and  $k$  are respectively the specific heat, temperature, and thermal conductivity of  
 185 the liquid. Conduction in the solid is modelled by:

$$186 \quad \nabla \cdot (k_S \nabla T_S) = 0 \quad (4)$$

187 where  $T_S$  and  $k_S$  are respectively the temperature and thermal conductivity of the solid.

188 The  $\rho$ ,  $\mu$ ,  $C_p$  and  $k$  are temperature dependent and are defined as follows [23, 26, 39]:

$$189 \quad \rho(T) = 838.466135 + 1.40050603T - 0.0030112376T^2 + 3.71822313 \times 10^{-7}T^3$$

$$\begin{aligned}
190 \quad \mu(T) &= 1.3799566804 - 0.021224019151T + 1.3604562827 \times 10^{-4}T^2 \\
191 \quad &\quad - 4.6454090319 \times 10^{-7}T^3 + 8.9042735735 \times 10^{-10}T^4 \\
192 \quad &\quad - 9.0790692686 \times 10^{-13}T^5 + 3.8457331488 \times 10^{-16}T^6 \\
193 \quad C_p(T) &= 12010.1471 - 80.4072879T + 0.309866854T^2 \\
194 \quad &\quad - 5.38186884 \times 10^{-4}T^3 + 3.62536437 \times 10^{-7}T^4 \\
195 \quad k(T) &= -0.869083936 + 0.00894880345T - 1.58366345 \times 10^{-5}T^2 + 7.97543259 \\
196 \quad &\quad \times 10^{-9}T^3
\end{aligned}$$

197  
198 The Reynolds number,  $Re$ , is given by:

$$199 \quad Re = \frac{\rho_f U_{in} D_h}{\mu_f} \quad (5)$$

200 where  $\mu_f$  and  $\rho_f$  are the viscosity and density of the fluid respectively while  $U_{in}$  is the inlet  
201 fluid velocity and  $D_h$  as the hydraulic diameter given by  $\left(D_h = \frac{4A_{ch}}{P_w} = \frac{2(W_{ch} \cdot H_{ch})}{W_{ch} + H_{ch}}\right)$  where  $P_w$ ,  
202  $A_{ch}$ ,  $W_{ch}$  and  $H_{ch}$  are the wetted perimeter, microchannel cross-sectional area, width and height  
203 of the channel respectively. The inlet velocity,  $U_{in}$ , is varied using different Reynolds numbers,  
204  $Re$ , while the other parameters of  $\mu_f$ ,  $\rho_f$  and  $D_h$  are constant.

205

### 206 **3.2 Boundary conditions**

207 A single channel with symmetry conditions applied on the side is used to minimise the  
208 computational time. The symmetry conditions are applied for both the liquid and solid phases.  
209 At the top, front and back solid faces of the MCHS adiabatic conditions are imposed while at  
210 the base of the MCHS a uniform heat flux is applied at the bottom of the micro-channel as  
211 presented in **Fig. 1(B and D)** using  $(-\mathbf{n} \cdot (-k_s \nabla T) = q/A_h)$  where  $\mathbf{n}$  represents the outward  
212 normal vector on domain boundary. At the MCHS inlet, the temperature is set to be 293.15K  
213 and velocity inlet normal to the boundary while the outlet pressure is set to be 0 Pa (gauge  
214 pressure at atmospheric pressure as the flow is assumed to exit the MCHS into an ambient  
215 atmosphere). A no slip velocity boundary condition is applied to the solid walls ( $u_s = 0$ ), where  
216  $u_s$  is the liquid velocity at the solid boundaries of the micro-channel with wall temperatures  
217 defined as  $T_s = T_f at wall$  where  $T_s$  is the solid temperature and  $T_f at wall$  is the fluid  
218 temperature at the wall. For the liquid-solid boundaries, the conductive and convective heat  
219 transfer to the fluid are coupled using the continuity of heat flux between the fluid and solid  
220 wall interfaces (refer to **Fig. 1 (D)**) where  $T_{f,r}$  and  $T_{s,r}$  are the interface temperatures of the liquid  
221 and the solid [40].



### 222 3.3 Heat transfer performance

223 The rate of heat transfer is measured using the average thermal resistance,  $\theta$ , defined as:

$$224 \quad \theta = \frac{T_{w,avg} - T_{in}}{A_s q} \quad (6)$$

225 where  $T_{w,avg}$  is the average MCHS base temperature,  $T_{in}$  is the water inlet temperature,  $q$  is the  
226 heat flux applied to the base of heat sink and  $A_s$  is the MCHS base surface area.

227 Pressure drop,  $\Delta P$  is calculated using the following formula:

$$228 \quad \Delta P = P_{in} - P_{out} \quad (7)$$

229 where  $P_{in}$  and  $P_{out}$  are the inlet and outlet pressure.

230 To measure the overall performance of the MCHS, the  $\theta$  and  $\Delta P$  are included together in one  
231 equation called the Performance Evaluation Criteria (PEC) [23, 26]. These parameters are  
232 equivalent to the Nusselt number and hydraulic measurement. The PEC index is defined as  
233 follows:

$$234 \quad \text{PEC} = \frac{\theta_s / \theta}{(\Delta P / \Delta P_s)^{1/3}} \quad (8)$$

235 where  $\Delta P$  and  $\theta$  are the  $\Delta P$  and  $\theta$  in a micro-channel containing VGs, and  $\Delta P_s$  and  $\theta_s$  are the  
236 same quantities in the corresponding uniform (i.e. uniform) micro-channel.

237

### 238 4. Numerical method

239 Equations (1) - (4) are solved simultaneously using the finite element method (FEM) in  
240 COMSOL Multiphysics 5.2a. For the current work, tetrahedral type unstructured meshes are  
241 used since they have the ability to perform element structuring for complex geometries and the  
242 domain does not have to undergo domain decomposition [41]. A segregated solver is used  
243 because it can balance memory requirements and solution accuracy simultaneously. First order  
244 discretisation is used together with quadratic elements for the temperature field. Second order  
245 discretisation is only suitable for creeping flows which will not be exploited in this work since  
246 viscous flow study is not considered. The relative error tolerance is set at 0.001 and a grid  
247 independence test (GIT) is performed to identify a suitable mesh to get an accurate output with  
248 the shortest simulation running time. Different numbers of elements (76316, 196887, 386092,  
249 1034900 and 3276705) were used, as shown in **Fig. 2**. On the basis of these results, the mesh  
250 with 1034900 elements is considered a suitable compromise between accuracy and  
251 computational cost. It has significant mesh refinement at the base of the channel and at the  
252 contact region between the fluid and the solid areas to resolve the boundary layer accurately.

253 The present model was compared to previous numerical and experimental studies. The first  
254 study was an experimental investigation of a straight micro-channel MCHS conducted by

255 Kawano et al. [42]. The second validation was against the numerical study presented by Qu and  
256 Mudawar [43]. Both studies, used the same material (silicon) and dimensions of the micro-  
257 channel were  $180\mu\text{m}$ ,  $57\mu\text{m}$ ,  $10\text{mm}$  the height, width and length, respectively. The top of the  
258 micro-channel was subjected to a uniform heat flux of  $90\text{W}/\text{cm}^2$ , while the side walls of the  
259 micro-channel were set to be symmetric in terms of heat transfer, with an adiabatic boundary  
260 condition at the bottom wall. Laminar flow was utilized in the studies with  $\text{Re}$  ranging from 80  
261 to 400. **Fig. 3** shows that the present numerical method agrees very well with the previous  
262 experimental and numerical studies.

263

## 264 **5. Results and discussion**

265 In this study, the effect of different parameters has been studied under laminar flow conditions  
266 ( $\text{Re}$  ranging from 100 to 2300) using the CFD model. The parameters cover a wide range of  
267 radii, sizes and positions of the VGs to explore their effect on the conjugate heat transfer. The  
268 VGs are semi-circular cylinders with length,  $W_2 = 350\mu\text{m}$  (see **Fig. 1**) and a constant heat flux  
269 relevant to micro-chips water cooling applications is applied at the bottom of the micro-channel  
270  $100\text{W cm}^{-2}$  [27].

271

### 272 **5.1 $\theta$ and the temperature distribution analysis**

273  $\theta$  decreases with increasing velocity of the liquid phase (increasing  $\text{Re}$ ) since heat is transferred  
274 away at a higher rate for larger velocities. There is however an unwanted increase in  $\Delta P$  as  
275 velocity increases.

276

#### 277 **5.1.1 Effect of varying the radius of VGs on $\theta$**

278 From **Fig. 4**, for uniform channels and all channels with VGs at all values of  $\text{Re}$ ,  $\theta$  decreases  
279 monotonically as  $\text{Re}$  increases since at higher velocity the rate of heat transfer increases.

280 This is because at low Reynolds number, the inertia of liquid flow moving over the VGs does  
281 not provide sufficiently large vortices to transfer the heat from the hot region to the cold region  
282 of the water. Instead, the fluid immediately behind the VGs is essentially stagnant, resulting in  
283 local hotspots and the associated increase in thermal resistance. More generally at low  $\text{Re}$ , there  
284 is much less intermixing between hot and cold fluid regions. Of key influence on the level of  
285 intermixing is that, at higher  $\text{Re}$ , the VGs will generate increasingly larger vortices which break  
286 the hydrodynamic and thermal boundary layers, as shown in **Fig. 5**. Interestingly, **Fig. 5** also  
287 shows two types of vortices which are transverse and longitudinal, which combine increasingly  
288 to enhance the heat transfer as  $\text{Re}$  is increased. However, the pressure penalty is also increased.

289 From **Fig. 4**, it is seen that the reduction in  $\theta$  at high Re is consistent, for a range of VG radii,  
290 at all Re.

291 Referring to **Fig. 4**, it shows clearly that  $\theta$  decreases as the radii of the VGs are increased. This  
292 is due to more effective breakage of the thermal boundary layer improving heat transfer when  
293 using a large radius of 300  $\mu\text{m}$ , whereas the highest  $\theta$  is for the uniform channel. Furthermore,  
294 **Fig. 6** explains the reduction in  $\theta$  when increasing the radius, for instance, at  $R = 300\mu\text{m}$ , results  
295 from increased liquid mixing – this is shown by the contrast between the blue (hot liquid) and  
296 red (cold liquid) particles (see **Fig. 6(C)**). This observation is further clarified by the velocity  
297 contours and arrow surface plot from **Fig. 6**. It shows how the recirculation region expands as  
298 the VGs' radii are increased (see the enlarged image of red dashed box in **Fig. 6**) improving the  
299 heat transfer as the boundary layer is broken up. Furthermore, as the radius increases the  
300 velocity contour above the VGs indicates higher liquid velocities are induced. Higher liquid  
301 velocity results in increased rate of heat transfer as more liquid passes through the channel  
302 compared with low liquid velocity. The temperature distribution for various VG radii are shown  
303 in **Fig. 7** as the temperature distribution is consistent with the plot of **Fig. 4** where  $\theta$  decreases  
304 when the radius is increased. The average percentage  $\theta$  improvement for R at 100 $\mu\text{m}$ , 200 $\mu\text{m}$   
305 and 300 $\mu\text{m}$  are 3.06%, 3.85% and 5.46% respectively which corresponds to **Fig. 4**. From **Fig.**  
306 **6**, at increasing radius of 100 $\mu\text{m}$ , 200 $\mu\text{m}$  and 300 $\mu\text{m}$ , the velocity contours change significantly  
307 between the moving fluids and the static fluid. The same behaviour occurs for the VGs placed  
308 at the middle and back positions. In fact, the increase in radius results in higher  $\Delta P$  due to more  
309 restricted flow through the narrow channel; this is discussed in detail in **section 5.2**.

310

### 311 **5.1.2 Effect of varying the distance between VGs on $\theta$**

312 The temperature distributions at the y-z and y-x cross sections are presented in **Fig. 8**. The  
313 cross-section is just upstream of the last rib. This demonstrates the temperature distribution and  
314 flow structure after fluid vortices have hit the earlier VGs, indicating the effectiveness of the  
315 proposed variables to remove heat from the system. It can be observed that the temperature of  
316 the substrate increased when the distance between VGs  $D = 100\mu\text{m}$ , but that increasing  $D$  for  
317  $D \geq 100\mu\text{m}$ , has only a minimal effect. The lowest temperature can be achieved when the VGs  
318 are adjacent to one another. The same trend occurs when VGs are placed at the middle or the  
319 back of the MCHS. The reason behind this behaviour is explained by using a particle tracing  
320 method, shown in **Fig. 9**, where the blue particles which are moving in between the gap of the  
321 VGs and the MCHS wall are displaced to the positive y-direction of the MCHS after going  
322 through all the 5 VGs.

323 This behaviour improves heat transfer as it covers most of the bottom surface area of the MCHS  
324 and carries more heat away from it. In addition, the red particles moving over the VGs meet the  
325 blue particles downstream of the last rib, as can be seen clearly in **Fig. 9 (B)**. The mixing of  
326 blue and red particles improves the heat transfer and at  $D = 0\mu\text{m}$  this effect is greatest. With  
327 larger distances between the VGs, the fluid behaviour is more predictable and less fluid mixing  
328 occurs where the fluid is almost moving in a straight path. Furthermore, the observation from  
329 the particle tracing analysis is clarified by the addition of arrow surfaces created in **Fig. 8 (A)**  
330 and **Fig. 8 (B)**. At  $D = 0\mu\text{m}$ , it is observed that the recirculation regions occur near the bottom  
331 of the MCHS (anti-clockwise) and at the upper part of the fluid region (clockwise). The  
332 opposing directions of the recirculation regions enhances the mixing of the hot and cold fluid  
333 regions. The hot fluid from the bottom of the MCHS recirculates upwards towards the centre  
334 of the channel while the upper part recirculation region brings the recirculated hot fluid from  
335 sidewalls. This mixing breaks the boundary layer at both the bottom and sidewalls of the  
336 channel.

337 The temperature plot in **Fig. 8** agrees with the  $\theta$  plot in **Fig. 10**. From **Fig. 10**, the trend is  
338 similar for all cases. At distances of  $100\mu\text{m}$ ,  $200\mu\text{m}$  and  $300\mu\text{m}$  the plot almost overlaps with  
339 the uniform channel ( $R = 0\mu\text{m}$ ) plot indicating the conjugate heat transfer improvement is not  
340 significant with higher distances between the VGs. On the other hand, the plot at  $D = 0\mu\text{m}$   
341 shows more significant improvements in  $\theta$  improvement in **Fig. 10**, represented by the red line.  
342 The red plot does not overlap with the other plots and has the lowest  $\theta$  at every  $Re$  which agrees  
343 with the temperature plot in **Fig. 8 (A)**. The average percentage  $\theta$  improvement for  $D$  values at  
344  $0\mu\text{m}$ ,  $100\mu\text{m}$ ,  $200\mu\text{m}$  and  $300\mu\text{m}$  compared to uniform channel are 3.06%, 1.97%, 2.11% and  
345 2.10% respectively which corresponds to **Fig. 10** which agrees with temperature distribution in  
346 **Fig. 8**.

347

### 348 **5.1.3 Effect of VG positioning on $\theta$**

349 The same procedure was carried out for the other 2 VG locations at the middle and back and  
350 similar conclusions were drawn: in **Fig. 10** the lowest  $\theta$  is at  $D = 0\mu\text{m}$  for the reasons discussed  
351 in relation to **Fig. 9**. A comparison between the lowest  $\theta$  values trend at each position is  
352 however carried out in **Fig. 11** where the lowest  $\theta$  is achieved at the front position but there are  
353 insignificant differences between the plots. VGs at the front position have the lowest  $\theta$   
354 compared to the other two positions. Using the same cross-section utilised by **Fig. 8**, referring  
355 to **Fig. 12**, the temperature contours (left side plot) from three positions show that the front  
356 position has the lowest temperature magnitude while the back position has the highest, which

357 agrees with the  $\theta$  plot in **Fig. 11**. From the z-direction velocity contour plot in **Fig. 12** (right  
358 side plot), as the vortices formed from the three positions of the VGs it can be seen that the  
359 front position (**Fig. 12 (A)**) creates the highest downwards velocity magnitude near the  
360 sidewalls of the microchannel indicating more heat is being carried away from the sidewalls.  
361 The average percentage improvement in  $\theta$  for the front, middle and back cases are 3.06%, 2.75%  
362 and 2.98% respectively which corresponds to **Fig. 11**. Based in **Fig. 11**, the position of the VGs  
363 does not have a significant effect on the conjugate heat transfer in the system. The different  
364 positions of the VGs also affect the  $\Delta P$  and this will be discussed thoroughly in the next part of  
365 the study.

366

## 367 **5.2 $\Delta P$ analysis**

368  $\Delta P$ , the pressure difference between the inlet and outlet of the MCHS, is another important  
369 parameter. It should be reduced to a minimum in order to minimize the hydraulic power input  
370 required to generate the flow.

371

### 372 **5.2.1 Effect of varying the radius of VGs on $\Delta P$**

373 The effect of varying the radius between  $0\mu\text{m}$  to  $300\mu\text{m}$  is investigated first. **Fig. 13** shows how  
374  $\Delta P$  increases when the radius increases and that this effect becomes more pronounced as  $\text{Re}$  is  
375 increased too. This is due to increased constriction of the flow at larger radii which leads to  
376 larger localised flow velocities and increased separation behind the VGs. The former effect in  
377 particular is shown in **Fig. 14**. The average percentage increase of  $\Delta P$  for  $R$  values of  $100\mu\text{m}$ ,  
378  $200\mu\text{m}$  and  $300\mu\text{m}$  are 3.91%, 14.27% and 40.04% respectively which corresponds to **Fig. 13**,  
379 indicating that very large pressure drops are induced compared to the enhancement of thermal  
380 resistance in **section 5.1.1**.

381

### 382 **5.2.2 Effect of varying the distance between VGs on $\Delta P$**

383 The effect of the distance between the VGs is investigated for the constant radius of  $100\mu\text{m}$ .  
384 The distance is varied from  $0\mu\text{m}$  to  $300\mu\text{m}$  in each case. **Fig. 15** shows that generally the  
385 pressure is slightly higher than for the uniform channel, but that the influence is small since no  
386 turbulence is generated. The lowest  $\Delta P$  is achieved at  $D = 100\mu\text{m}$  at every position, while the  
387 highest  $\Delta P$  is when the distance between VGs is  $0\mu\text{m}$ . At distances of  $200\mu\text{m}$  and  $300\mu\text{m}$ , the  
388 pressure increases lie between these two extremes, with that for  $300\mu\text{m}$  higher than for  $200\mu\text{m}$ .  
389 The highest  $\Delta P$  at  $0\mu\text{m}$  separation distance between VGs, is due to the channel having a  
390 converging/diverging profile which acts like a nozzle increasing the local flow velocities near

391 the VGs. The higher  $\Delta P$  with  $D = 0\mu\text{m}$  can also be explained by **Fig. 8 (A)** where vigorous  
392 mixing between recirculation regions is evident, providing increased flow resistance in the  
393 stream-wise direction. The lowest pressure difference at  $D = 100\mu\text{m}$  is due to the greater flow  
394 uniformity compared to other distances, **Fig. 9. Fig. 15**, shows the results for high  $Re$  since  
395 these are the most significant ones in terms of  $\Delta P$ . The average percentage increase of  $\Delta P$  for  
396  $D$  values of  $0\mu\text{m}$ ,  $100\mu\text{m}$ ,  $200\mu\text{m}$  and  $300\mu\text{m}$  are 4.40%, 2.31%, 2.58% and 3.14% respectively,  
397 which agrees with **Fig. 15**.

398

### 399 **5.2.3 Effect of VGs positioning on $\Delta P$**

400 Since the distance between VGs is not very influential the case with  $D = 0\mu\text{m}$  is chosen to study  
401 the influence of the front, middle and back position on the  $\Delta P$  of the system. **Fig. 16** compares  
402 the  $\Delta P$  for different positions of the VGs. It is found that the largest  $\Delta P$  is at the front position,  
403 while the lowest is at the back position due to the higher intensity of downwards velocity of  
404 fluid near the sidewalls of the channel. The average percentage  $\Delta P$  increase for front, middle  
405 and back position are 2.70%, 2.53% and 2.32% respectively which are very close to each other  
406 (refer to **Fig. 16** for the graph).

407

### 408 **5.3 Thermal-hydraulic performance index analysis**

409 To measure the overall performance of the heat sink, in terms of the balance between  $\theta$  and  $\Delta P$ ,  
410 the parameters of  $\theta$  and  $\Delta P$  are combined in equation (8). Values of  $PEC > 1$  means the overall  
411 performance of a modified micro-channel is better than the uniform conventional channel. From  
412 **Fig. 17**, the highest  $PEC$  region occurred for a radius of  $100\mu\text{m}$  whereas the  $PEC$  indices at  
413  $300\mu\text{m}$  are much lower than for minor rib radii. This is because the minor improvements in  $\theta$   
414 are dominated by the corresponding large increase in  $\Delta P$ . The highest  $PEC$  occurred at the  
415 radius of  $100\mu\text{m}$  and the distance between VGs of  $0\mu\text{m}$  for the front position of the VGs.  
416 Referring to **Fig. 17**, the highest  $PEC$  index occurred at  $R = 100\mu\text{m}$  and  $D = 0\mu\text{m}$ . Only at  $R =$   
417  $100\mu\text{m}$  does the  $PEC$  exceeds unity which means its overall performance is better than the  
418 uniform conventional channel. Every position shows the highest  $PEC$  index at  $R=100\mu\text{m}$  and  
419  $D=0\mu\text{m}$ . **Fig. 18** compares the effect of VG position for  $R=100\mu\text{m}$  and  $D=0\mu\text{m}$ .

420 The effects of the VG distance on the  $PEC$  index is carried out for  $Re = 900$ . The distance  
421 between VGs is varied from  $0\mu\text{m}$  to  $500\mu\text{m}$  at every position. **Fig. 19** shows that the  $PEC$  index  
422 increases as the distance between VGs decreases, at  $D=0\mu\text{m}$ , the  $PEC$  index is the highest for  
423 all cases, however, the front position is found to be the highest. The high  $PEC$  index is due to

424  $\Delta P$  decreasing at a faster rate than  $\theta$ . Thus, it can be concluded that increasing the distance  
425 between VGs is not beneficial for the overall performance of the micro-channel.

426 The above results show that the best combination is to use VGs at the front position with 0 $\mu\text{m}$   
427 distance between them. Finally, with this combination, the effect of changing the radius of the  
428 VGs (from 0 $\mu\text{m}$  to 300 $\mu\text{m}$ ) on the PEC index is shown in **Fig. 20**. The PEC index decreases  
429 gradually for  $R > 150\mu\text{m}$  and it increases at the radius below 150 $\mu\text{m}$ . The results show that the  
430 highest PEC index is found at the radius of 100 $\mu\text{m}$ . This is the best compromise between  
431 improving thermal performance and mitigating the inevitable rise in  $\Delta P$ . From all PEC plots, it  
432 can be seen that the PEC values do not show a significant increase when calculated against the  
433 smooth channel since the thermal resistance reduction is dominated by large pressure drop  
434 increase which is similar to the findings of Liu et al. [34, 38]

435

## 436 **6. Conclusion**

437 This study explores the enhancement in conjugate heat transfer that can be achieved using  
438 cylindrical vortex generators (VGs). A group of five VGs is applied at the base of a uniform  
439 micro-channel heat sink (MCHS) using three positions (front, middle and back). The influence  
440 of the VGs' radii in the range of (0-300)  $\mu\text{m}$  and the distance between the VGs (0-300)  $\mu\text{m}$   
441 across a water-filled micro-channel are also investigated by COMSOL Multiphysics<sup>®</sup> software.  
442 The geometries are assessed for Re in the range of 100 to 2300 using thermal resistance ( $\theta$ ),  
443 pressure drop ( $\Delta P$ ) and a thermal hydraulic performance index (PEC) which combines both of  
444  $\theta$  and  $\Delta P$ . The performance of VGs is evaluated with reference to the uniform micro-channel  
445 (without VGs). The main findings are as follows.

- 446 • It was found that using cylindrical VGs enhances the thermal performance of the MCHS  
447 but incurs a high pressure penalty. The cylindrical VGs promote vortices which improve  
448 the heat transfer by fluid mixing which is visualised effectively using three-dimensional  
449 tracer particle-trajectory plots. It is also found that the  $\theta$  decreases (the heat transfer  
450 performance is enhanced) with an increase of the VGs' radii. The results showed that  
451 the best heat transfer enhancement is achieved at front position using radii of 300  $\mu\text{m}$   
452 and no distance between the VGs ( $D=0 \mu\text{m}$ ).
- 453 • The influence of the distance between VGs was also investigated, and it was shown that  
454 a short distance (e.g. 100  $\mu\text{m}$ ) between the VGs improves  $\theta$  more effectively compared  
455 to larger distances (e.g. 500  $\mu\text{m}$ ).

- 456       • The effect of the position of the VGs was also considered. It was found that the front  
457           position is the best for enhancing the heat transfer and the pressure penalty was reduced  
458           very slightly when moving the VGs to the back of the channel.
- 459       • The thermal hydraulic performance (PEC) was investigated by measuring the overall  
460           performance of the micro-channel accounting for the combination of the  $\theta$  and  $\Delta P$  terms.  
461           Interestingly, it is not necessarily the lowest thermal resistance that gives the highest  
462           PEC index, for instance, the lowest  $\theta$  at  $R=300\ \mu\text{m}$  and  $\text{Re}$  of 2300, but in terms of PEC,  
463           the radius of  $100\ \mu\text{m}$  has its highest value at  $\text{Re}=900$ .
- 464       • From the PEC index perspective, results demonstrate that the PEC index is an effective  
465           means of showing that increasing the radius is not beneficial due to the higher rate of  
466           pressure increase compared to the reduction in  $\theta$ . This means that longer distances  
467           resulted in a reduction in the performance of the PEC index to values  $< 1$ .

468

469

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617 **Table captions**

618

619 **Table1:** Dimensions of the MCHS. The variables R and D of the cylindrical VGs placed are  
620 also defined.

621

622 **Table1:** Dimensions of the MCHS. The variables R and D of the cylindrical VGs placed are  
623 also defined.

624

Parameters	Magnitude, $\mu\text{m}$
L	50000
H <sub>1</sub>	900
H <sub>2</sub>	700
W <sub>1</sub>	250
W <sub>2</sub>	175
W <sub>3</sub>	150
R	0, 100, 200, 300
D	0, 100, 200, 300

625

626 **Figure captions**

627 **Figure 1:** (A) Full size of MCHS with the dimensions defined in Table 1. The geometrical  
628 representation of the MCHS, (B) The uniform channel without VGs, (C) The boundary  
629 conditions applied to the MCHS base. (D) MCHS having VGs placed at the bottom of the  
630 channel with the front view and side view and the interface surface between the liquid and  
631 solid.

632 **Figure 2:** Effect of mesh density on  $\theta$  and the  $\Delta P$ .

633 **Figure 3:** Validation of the present work against experimental and Numerical work [42, 43].

634 **Figure 4:** Thermal resistance for different radii (100 $\mu\text{m}$  to 300 $\mu\text{m}$ ) at the front position.

635 **Figure 5:** Water flow of VGs (R=400 $\mu\text{m}$  and the D=0 $\mu\text{m}$ ) at the back of the channel; (A)  
636 Re=100, (B) Re=1900.

637 **Figure 6:** Particle tracing (red and blue streams) with the corresponding velocity (m/s)  
638 contours with a front arrangement (D=0  $\mu\text{m}$ ); (A) R=100 $\mu\text{m}$ , (B) R=200 $\mu\text{m}$ , (C) R=300 $\mu\text{m}$ .

639 **Figure 7:** Temperature contours (K) distribution (side-view) for various radii at the front  
640 position.

641 **Figure 8:** Temperature contours (K) with variable distances between VGs from 0  $\mu\text{m}$  to 300  
642  $\mu\text{m}$  at Re=2300 for VGs in the front arrangement for y-z (front view) and y-z plane (top  
643 view).

644 **Figure 9:** Particle tracing; (A) for different distances ranging from of (0-500)  $\mu\text{m}$  at front  
645 position (B) zoomed in view at distance 0 $\mu\text{m}$ .

646 **Figure 10:** Thermal resistance against Re at difference distances between VGs (0 $\mu\text{m}$ , 100 $\mu\text{m}$ ,  
647 200 $\mu\text{m}$  and 300 $\mu\text{m}$ ) at the front position.

648 **Figure 11:** Comparison of  $\theta$  at the front, middle and back positions with the uniform channel  
649 case.

650 **Figure 12:** Temperature contours (K) (left side plot) and velocity contours ( $\text{ms}^{-1}$ ) in z-  
651 direction (right side plot); (A) front (B) middle and (C) back.

652 **Figure 13:** Pressure drop against Re from 100 to 2300 and at the front position with the  
653 distance between VGs of 0 $\mu\text{m}$ .

654 **Figure 14:** The y-z cross section of the MCHS, with velocity contours (m/s) at different radii  
655 of 100 $\mu\text{m}$ , 200 $\mu\text{m}$  and 300 $\mu\text{m}$  at distance between VGs of 0 $\mu\text{m}$  for the front position.

656 **Figure 15:** Pressure drop against Re at every distance between VGs ranging from (0-300)  $\mu\text{m}$   
657 for the front position at R = 100 $\mu\text{m}$  with zoomed in view.

658 **Figure 16:** Pressure drop for VGs placed at the front, middle and back with zoomed in view.

659 **Figure 17:** PEC index for different radii and distances between VGs of 0 $\mu\text{m}$ , 100 $\mu\text{m}$ , 200 $\mu\text{m}$ ,  
660 and 300 $\mu\text{m}$  at the front position.

661 **Figure 18:** PEC index of different arrangements of VGs (front, middle and back) against Re  
662 with the boundary limit set to be 1 for a uniform channel.

663 **Figure 19:** PEC index plot against the distance between VGs at Re= 900 for 3 different  
664 positions.

665 **Figure 20:** PEC index for increasing radii at constant Re of 900 with distance, D = 0 $\mu\text{m}$  at the  
666 front position.

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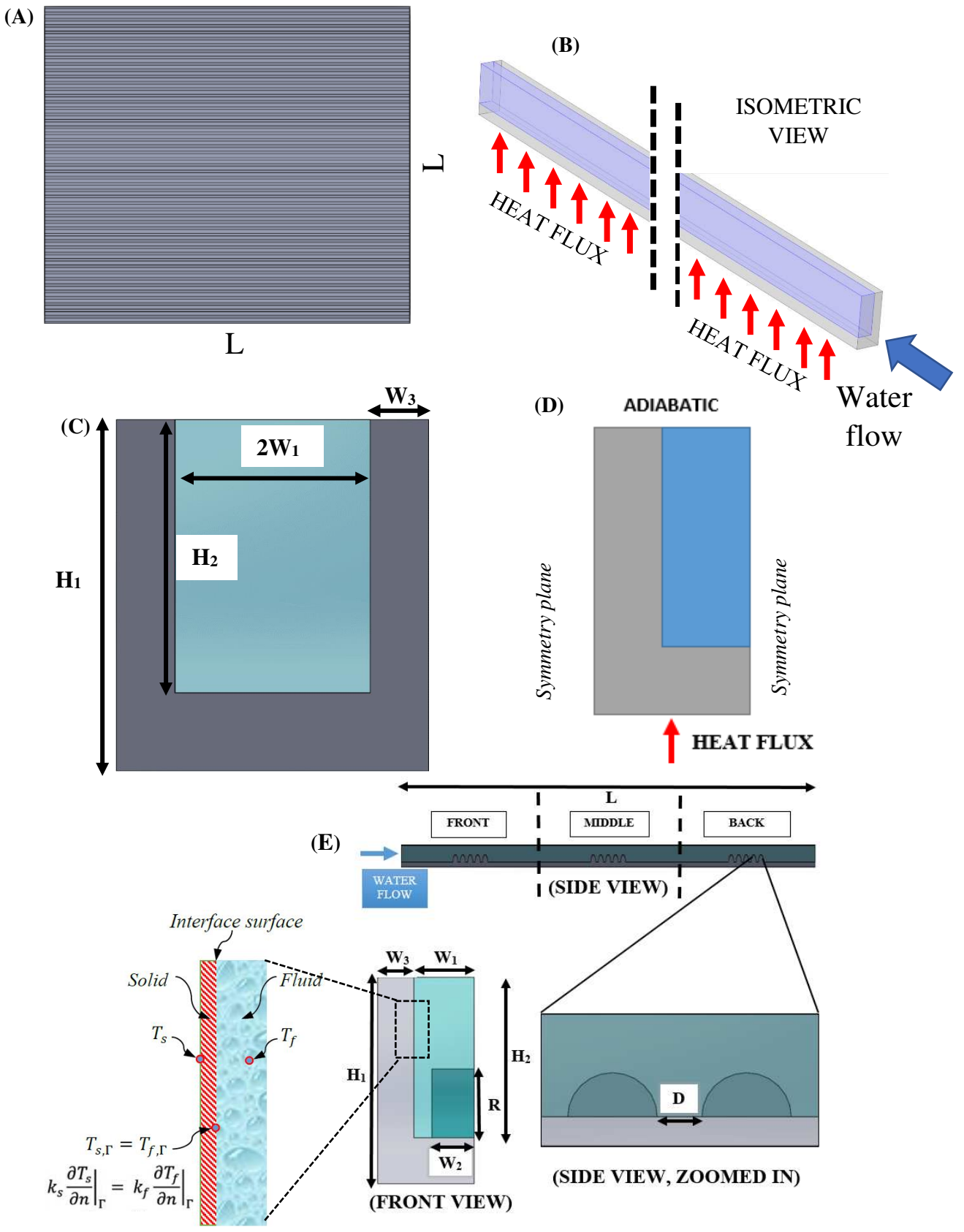
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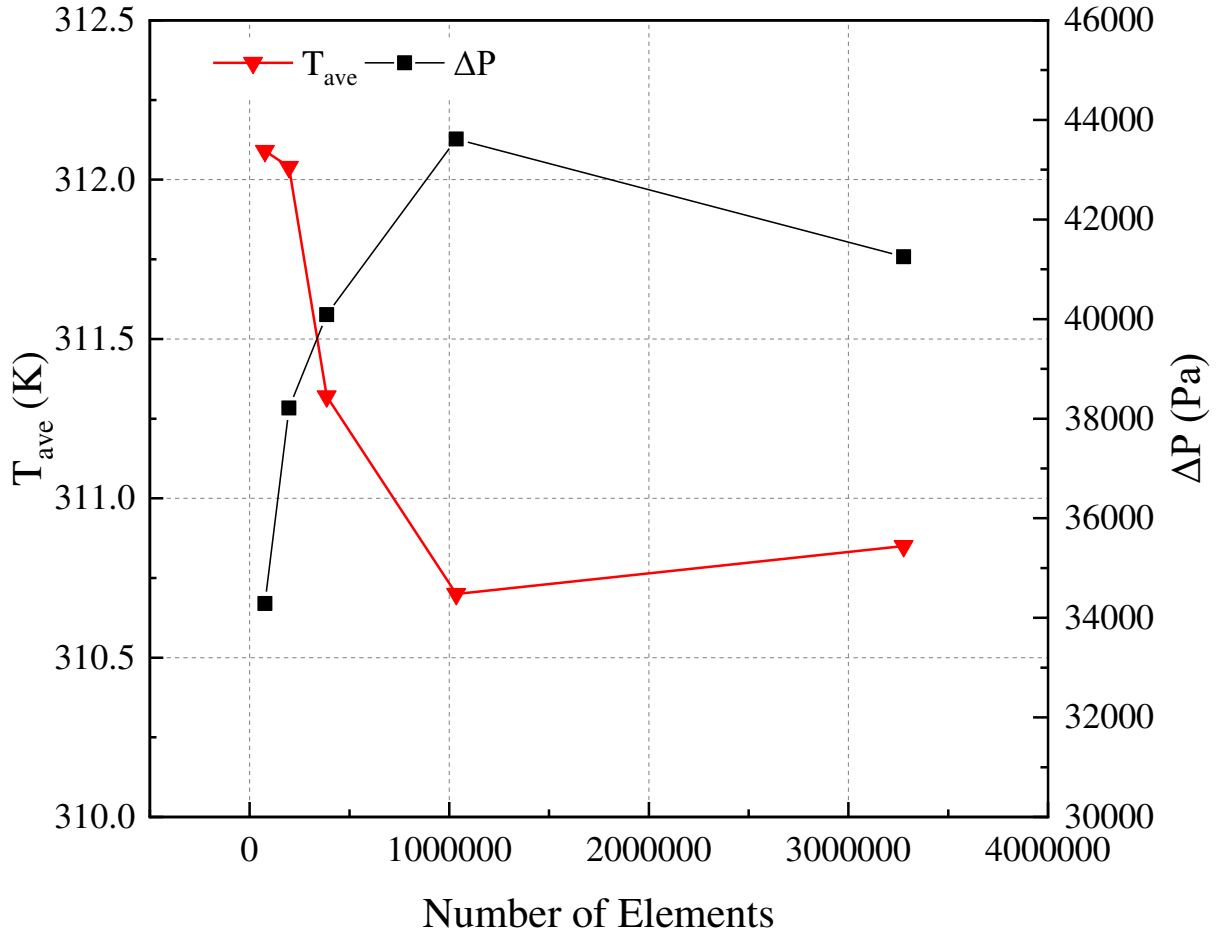
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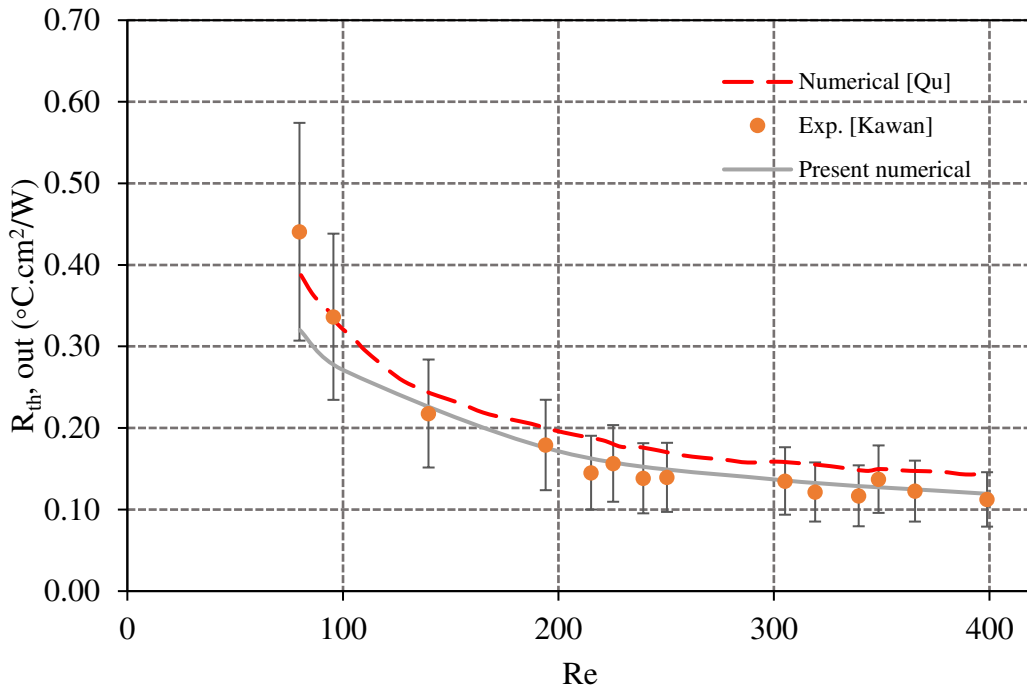
707 **Figure 1:** (A) Full size of MCHS with the dimensions defined in Table 1. The geometrical  
 708 representation of the MCHS, (B) The uniform channel without VGs, (C) The boundary  
 709 conditions applied to the MCHS base. (D) MCHS having VGs placed at the bottom of the  
 710 channel with the front view and side view and the interface surface between liquid and solid.



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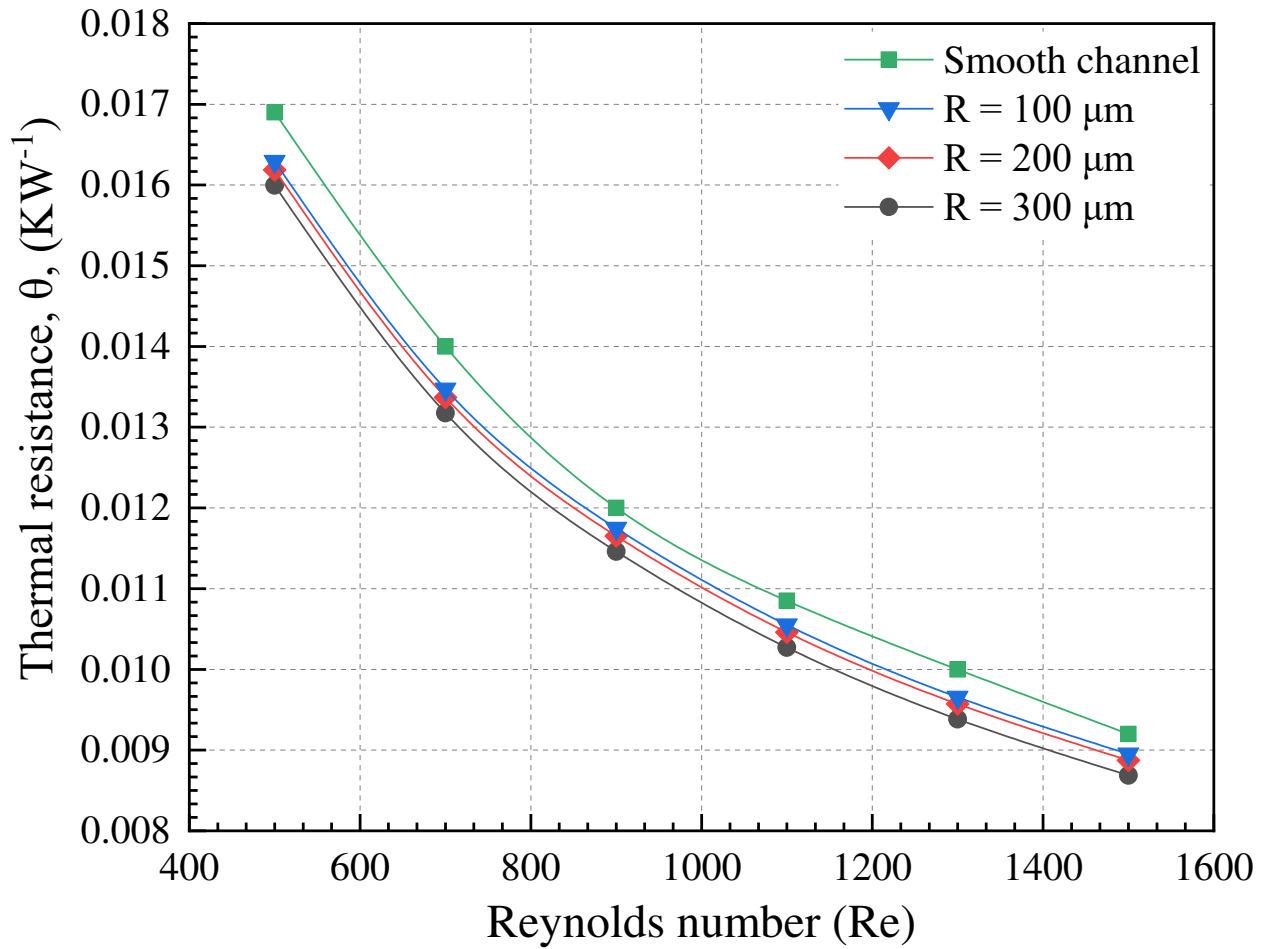
**Figure 2:** Effect of mesh density on  $\theta$  and the  $\Delta P$ .



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**Figure 3:** Validation of the present work against experimental and Numerical work [42, 43].



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**Figure 4:** Thermal resistance for different radii (100µm to 300µm) at the front position.



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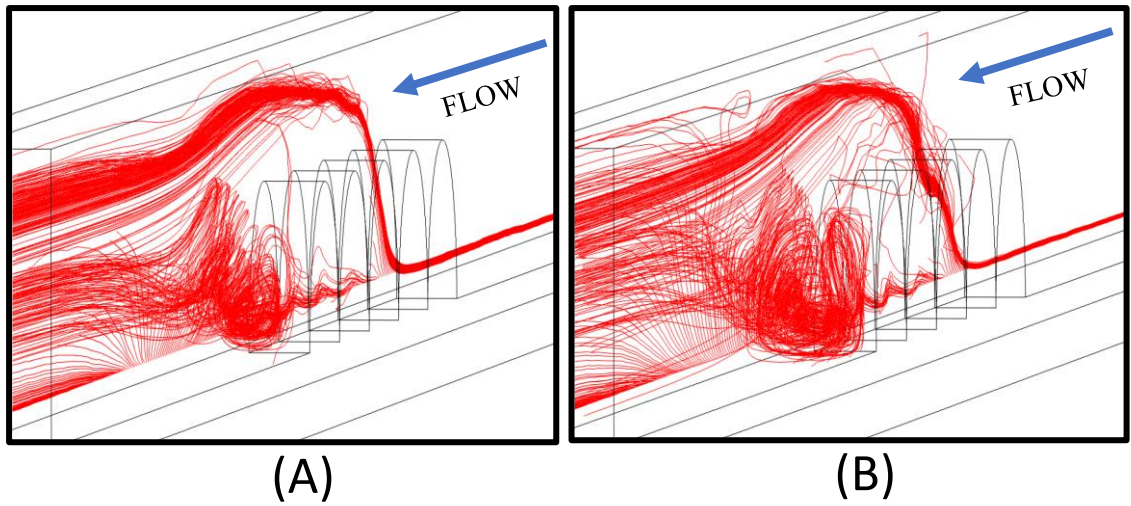
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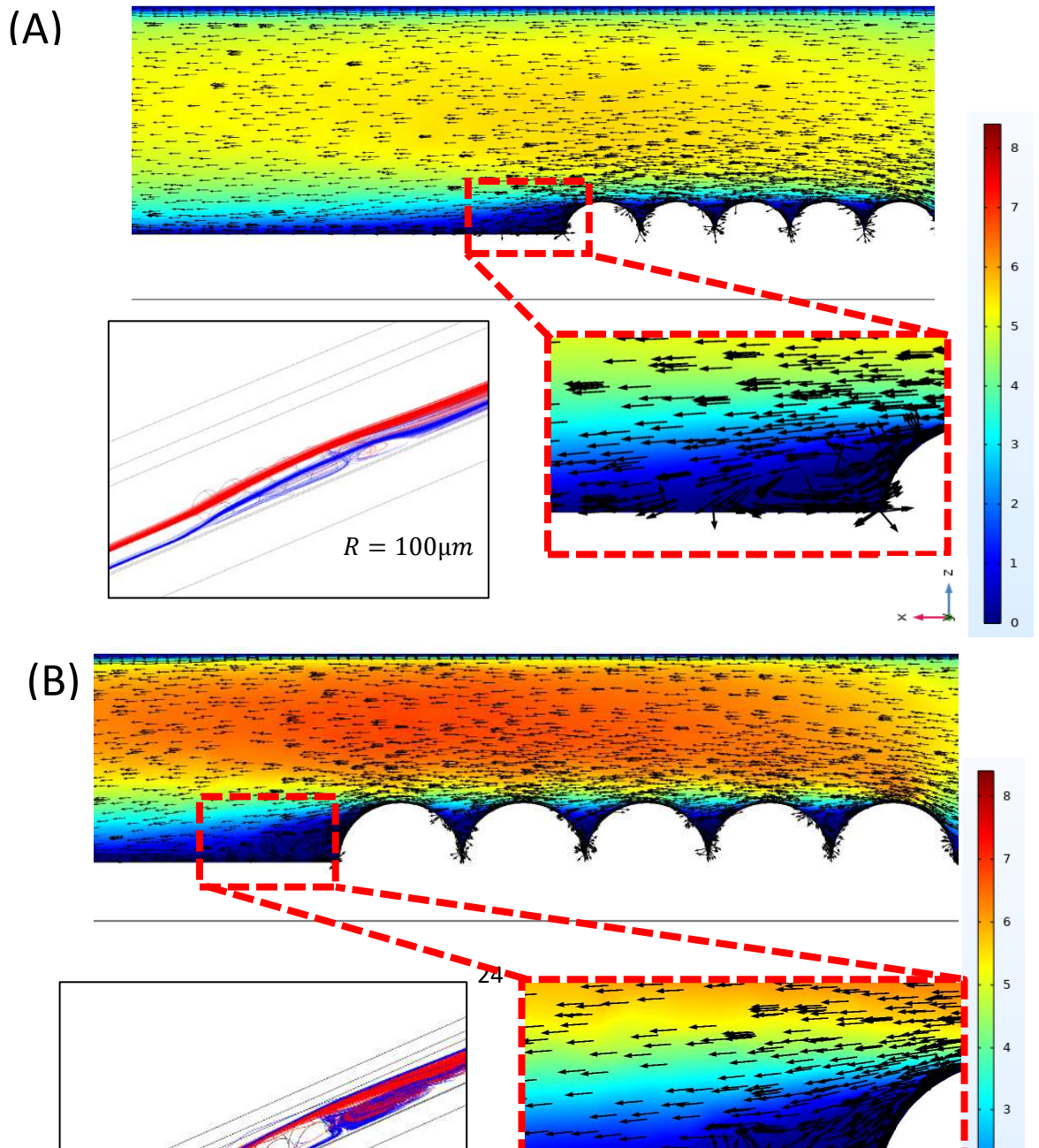
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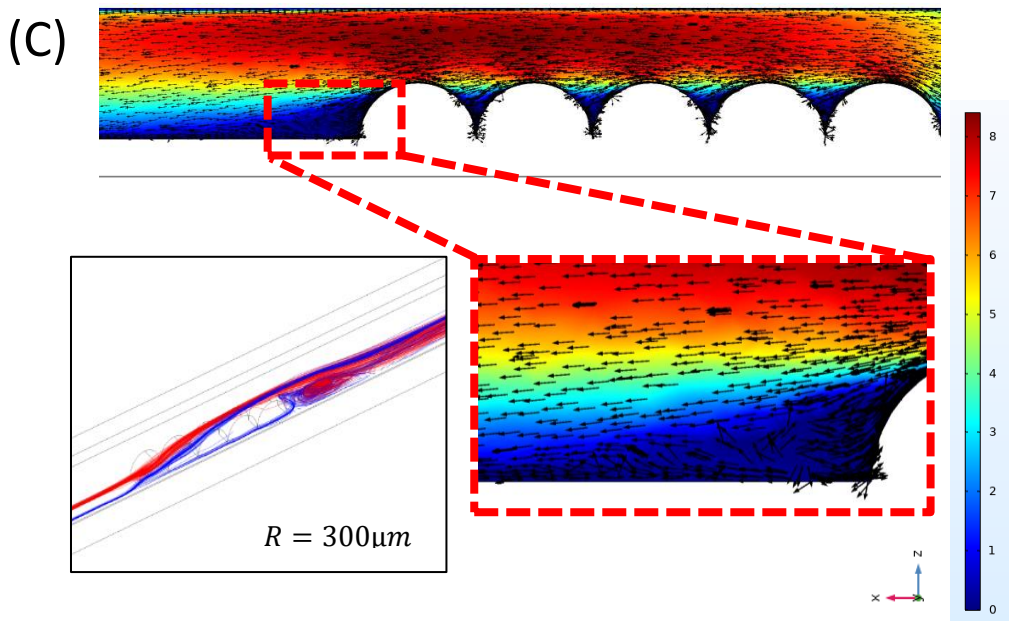
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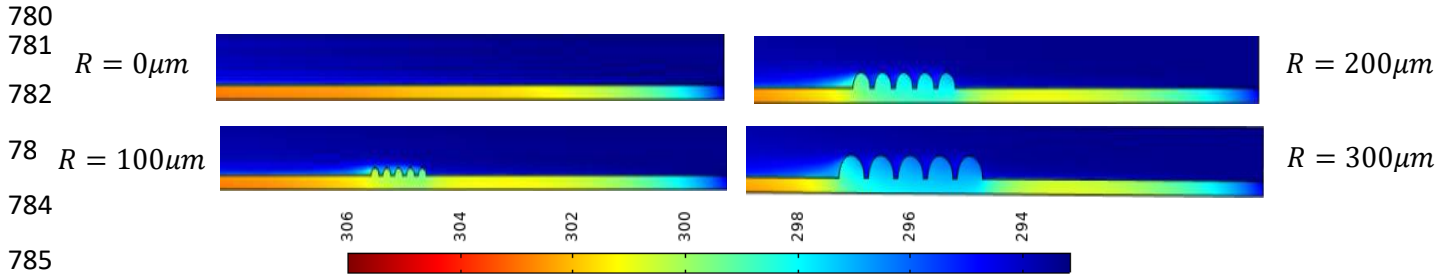
**Figure 5:** Water flow of VGs ( $R=400\mu\text{m}$  and the  $D=0\mu\text{m}$ ) at the back of the channel; (A)  $Re=100$ , (B)  $Re=1900$ .



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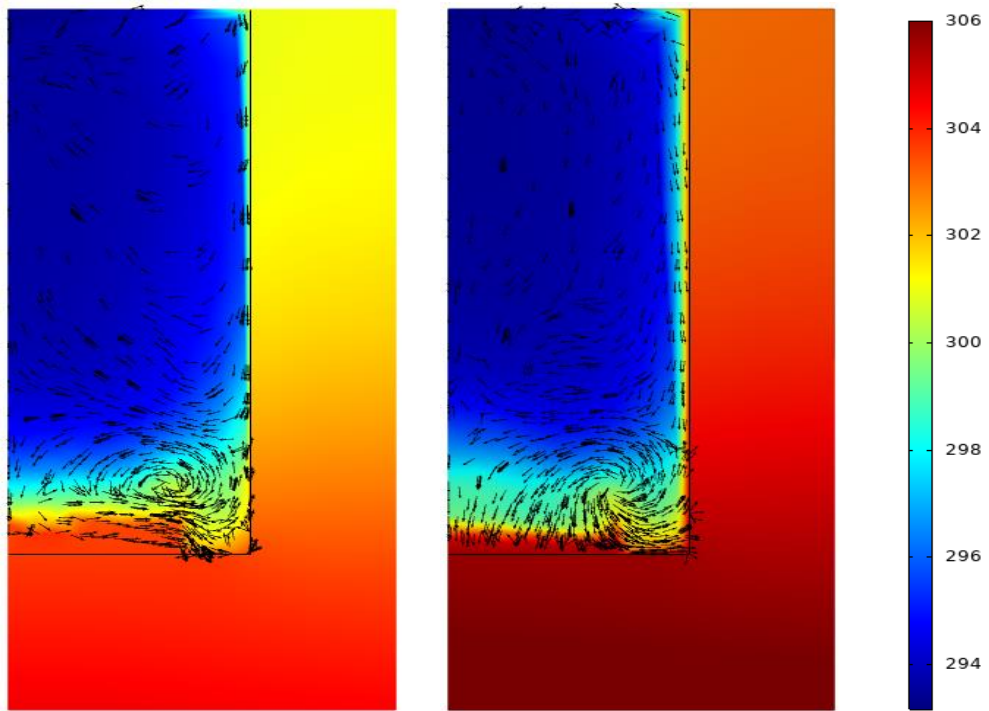
778 **Figure 6:** Particle tracing (red and blue streams) with the corresponding velocity (m/s)  
 779 contours with a front arrangement ( $D=0 \mu\text{m}$ ); (A)  $R=100\mu\text{m}$ , (B)  $R=200\mu\text{m}$ , (C)  $R=300\mu\text{m}$ .



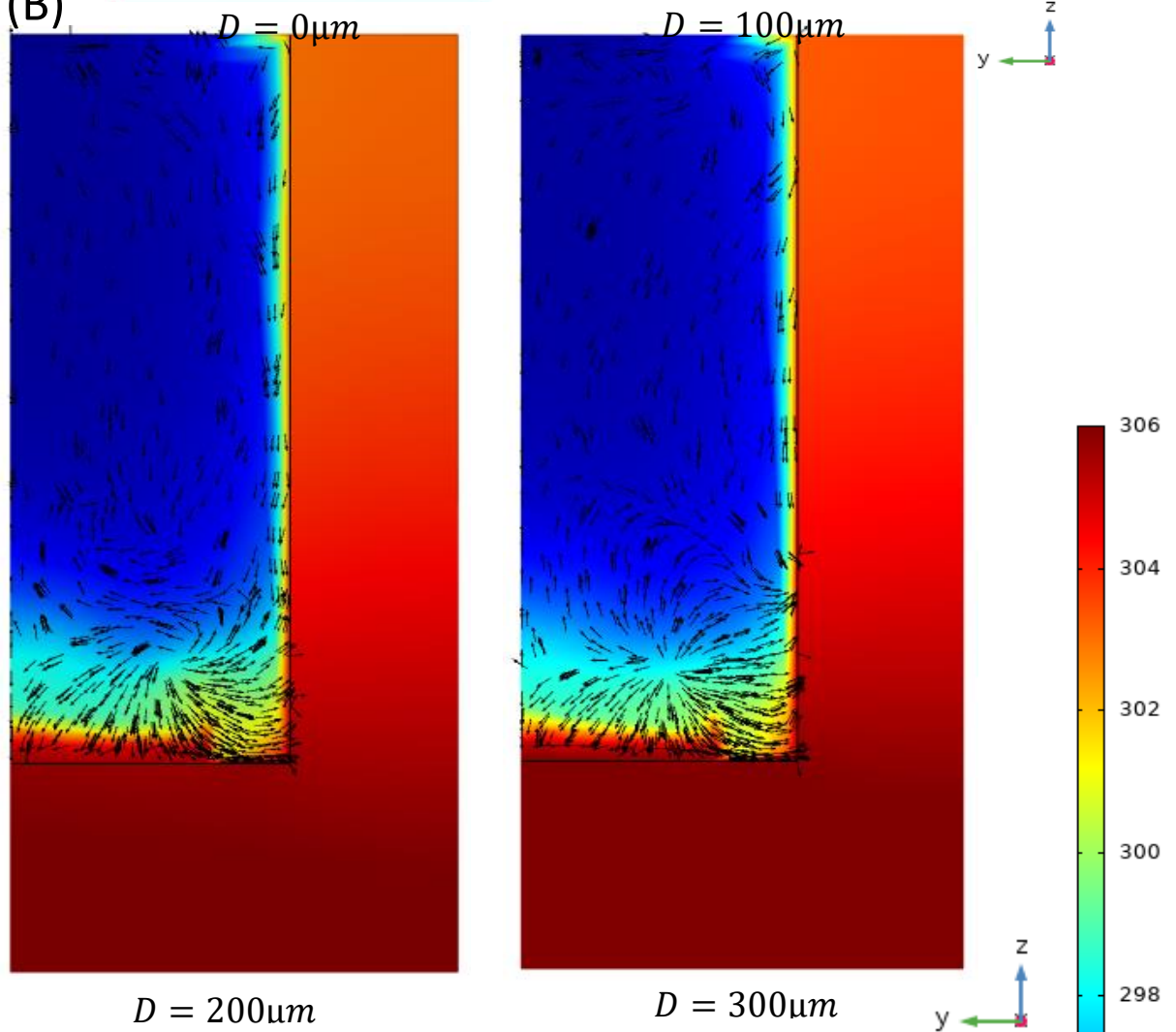
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 786 **Figure 7:** Temperature contours (K) distribution (side-view) for various radii at the front  
 787 position.

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(A)



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$D = 0\mu m$



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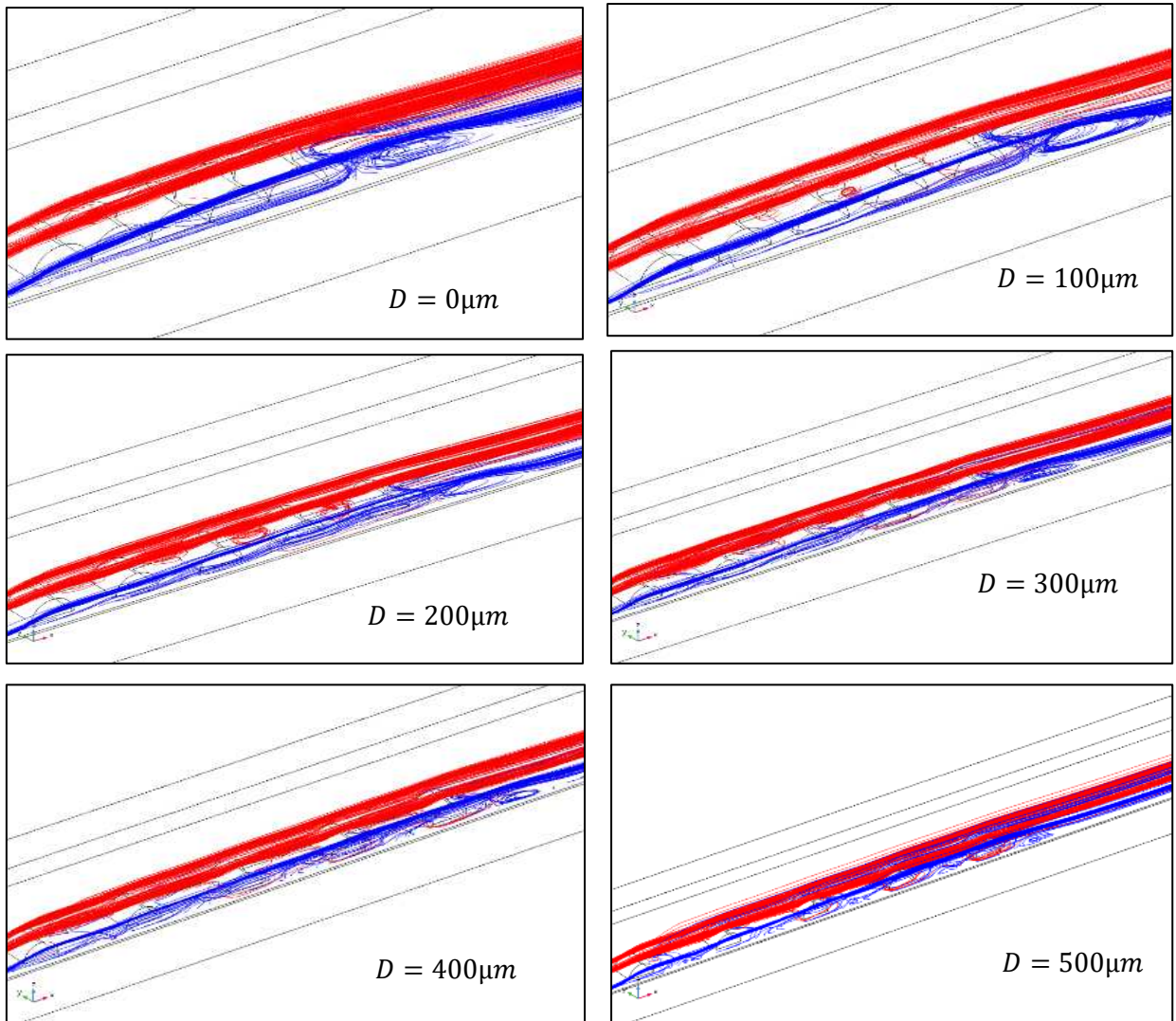
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833 **Figure 8:** Temperature contours (K) with variable distances between VGs from 0  $\mu\text{m}$  to 300  
834  $\mu\text{m}$  at  $\text{Re}=2300$  for VGs in the front arrangement for y-z (front view) and y-z plane (top  
835 view).

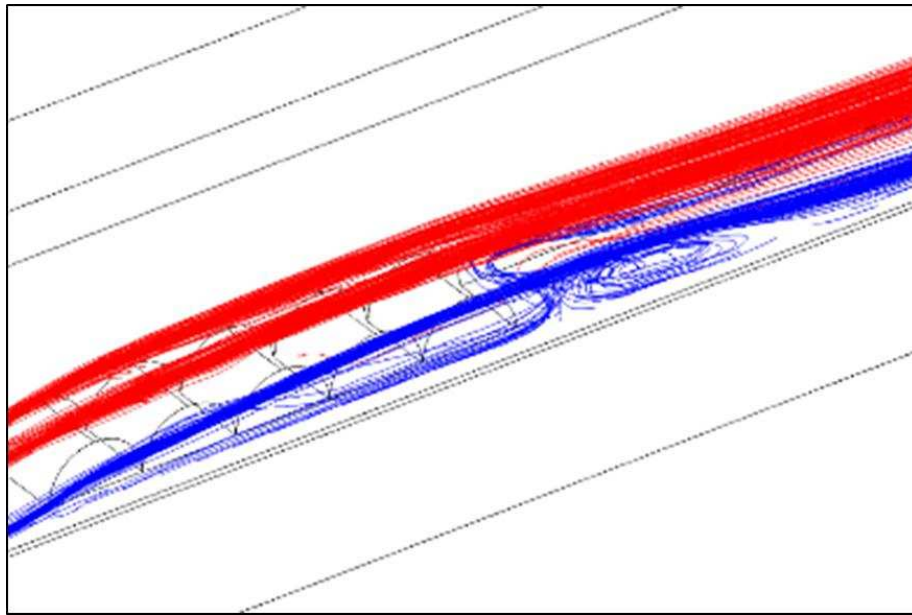
(A)



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(B)

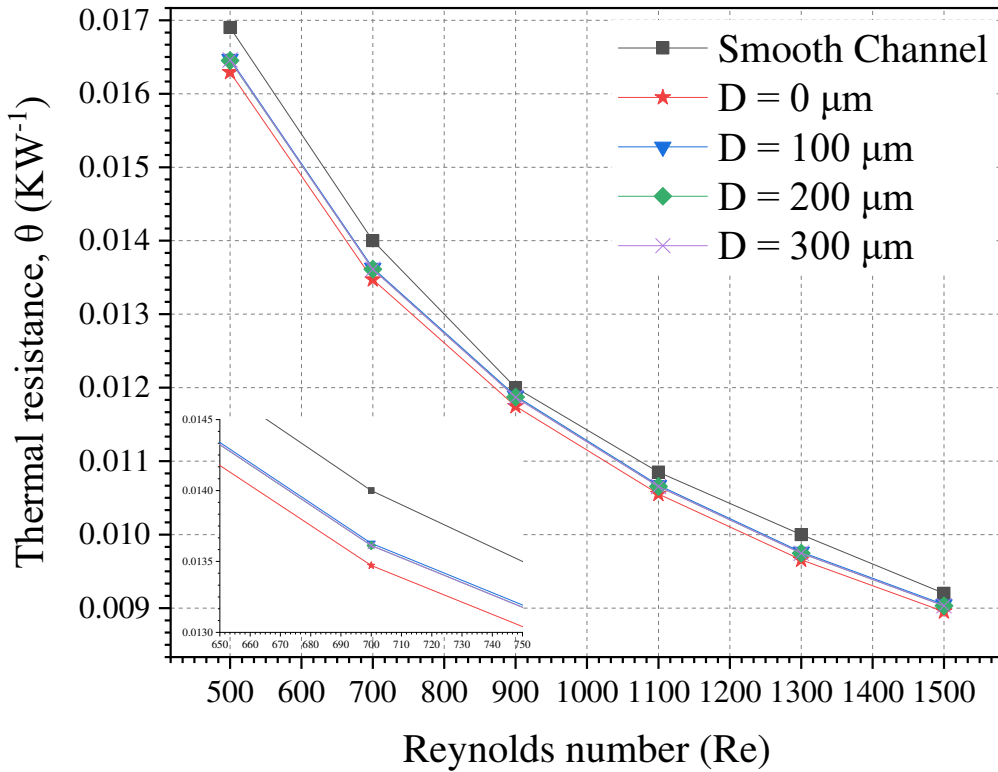


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**Figure 9:** Particle tracing; (A) for different distances ranging from of (0-500)  $\mu\text{m}$  at front position (B) zoomed in view at distance  $0\mu\text{m}$ .



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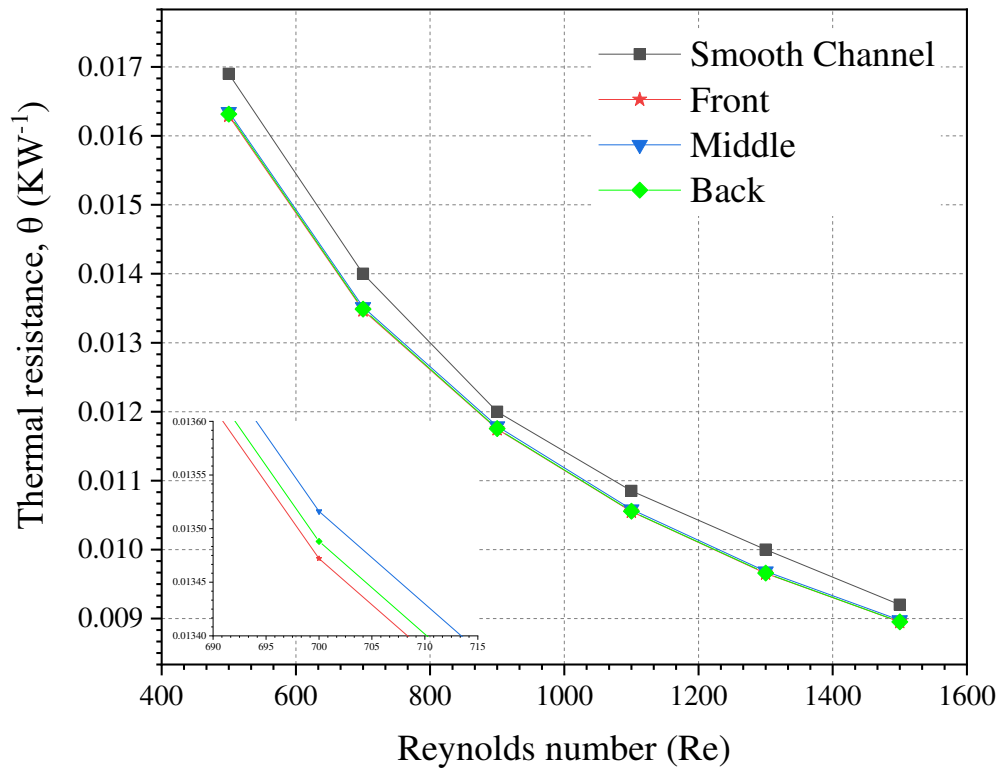
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**Figure 10:** Thermal resistance against Re at difference distances between VGs ( $0\mu\text{m}$ ,  $100\mu\text{m}$ ,  $200\mu\text{m}$  and  $300\mu\text{m}$ ) at the front position.



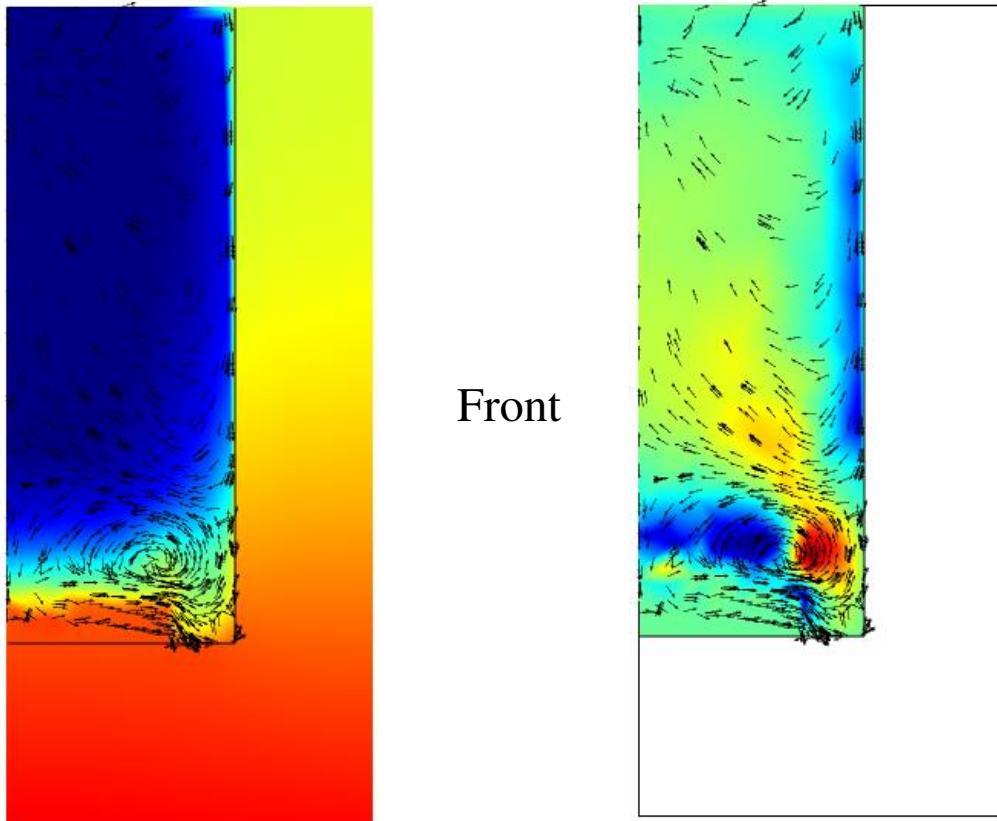
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847 **Figure 11:** Comparison of  $\theta$  at the front, middle and back positions with the uniform channel  
 848 case.

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851 (A)



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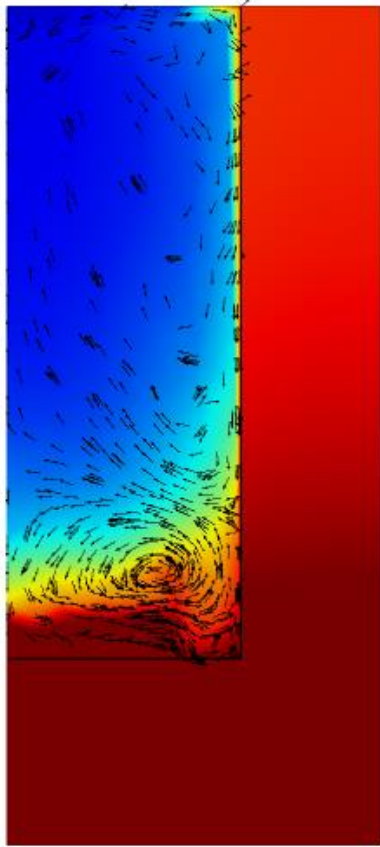
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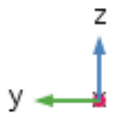
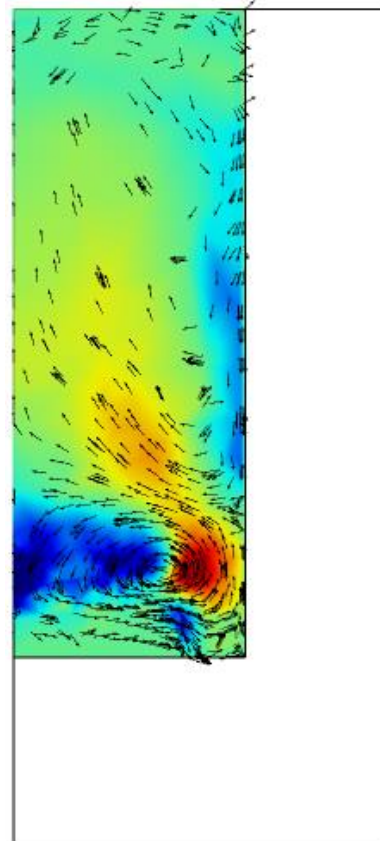
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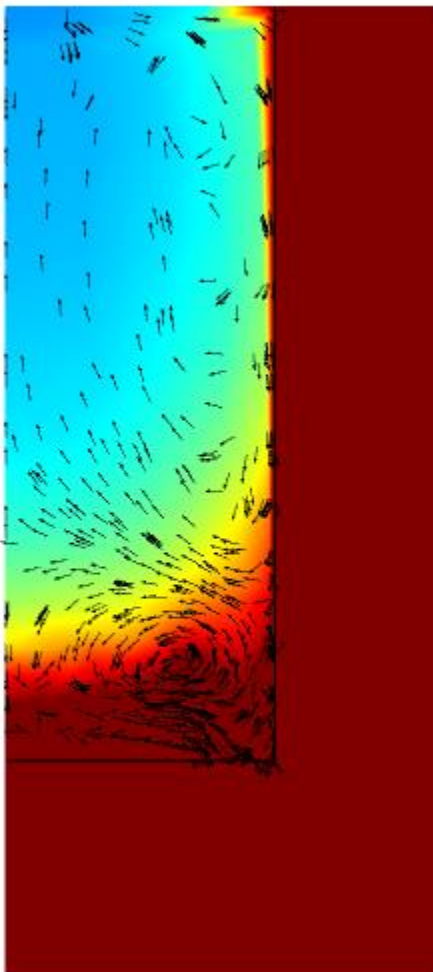
(B)



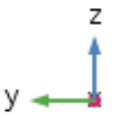
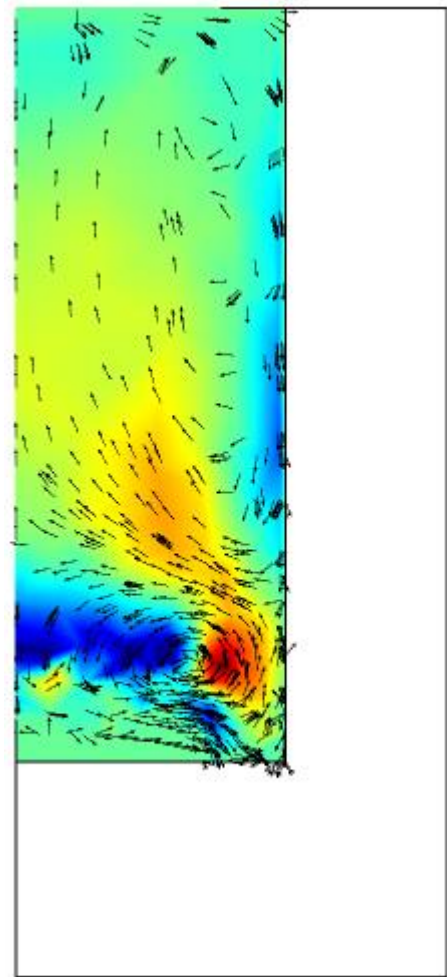
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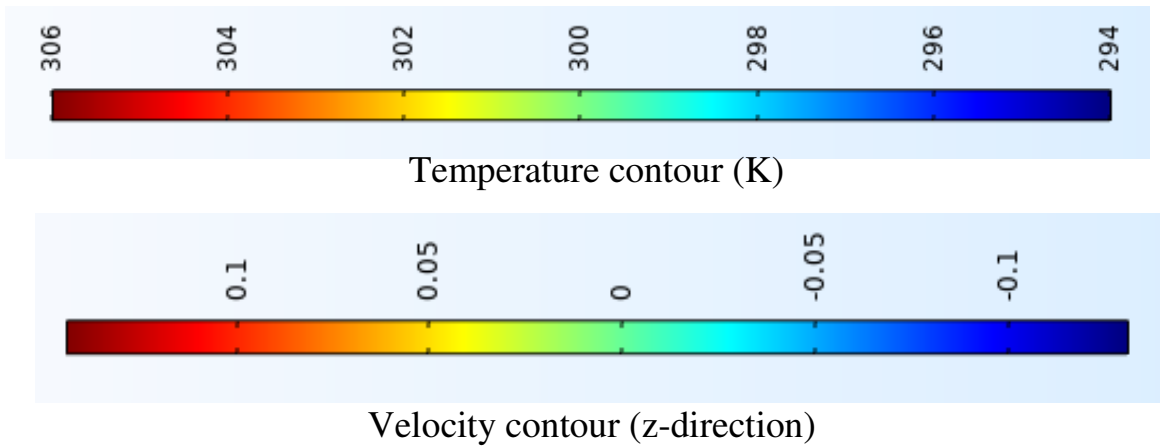
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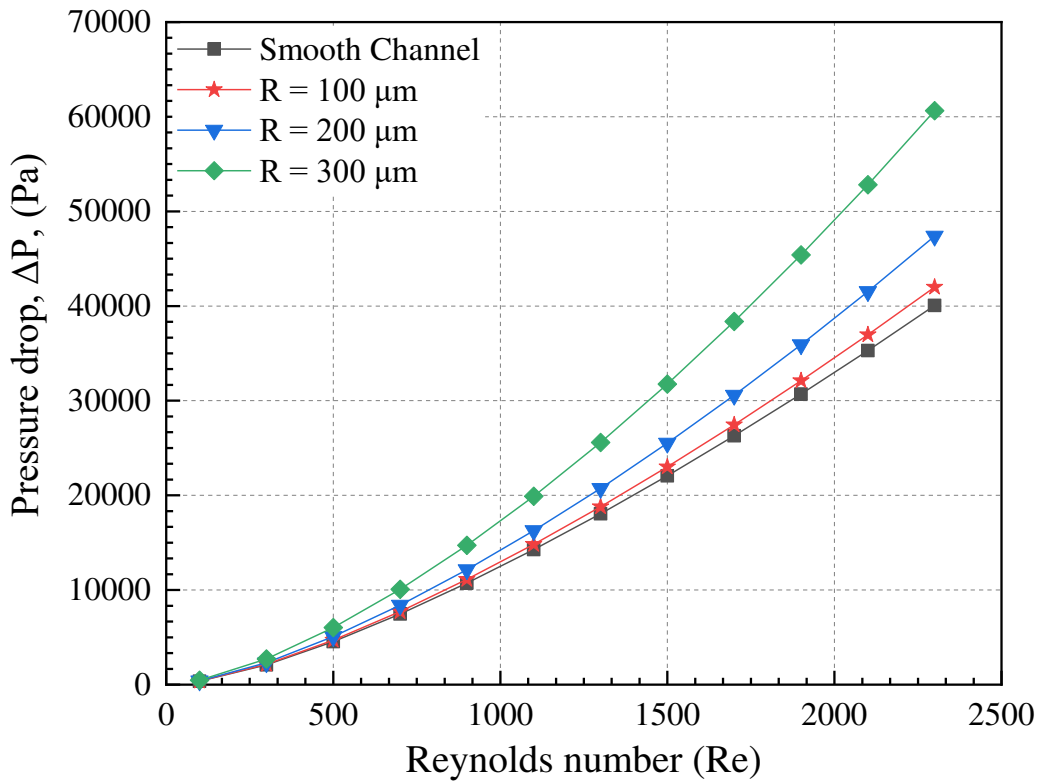
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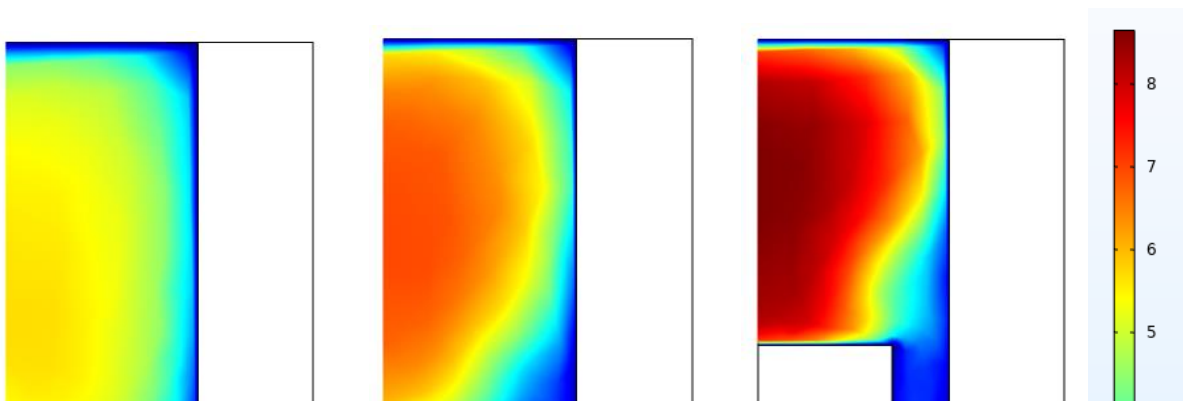


**Figure 12:** Temperature contours (K) (left side plot) and velocity contours ( $\text{ms}^{-1}$ ) in z-direction (right side plot); (A) front (B) middle and (C) back.



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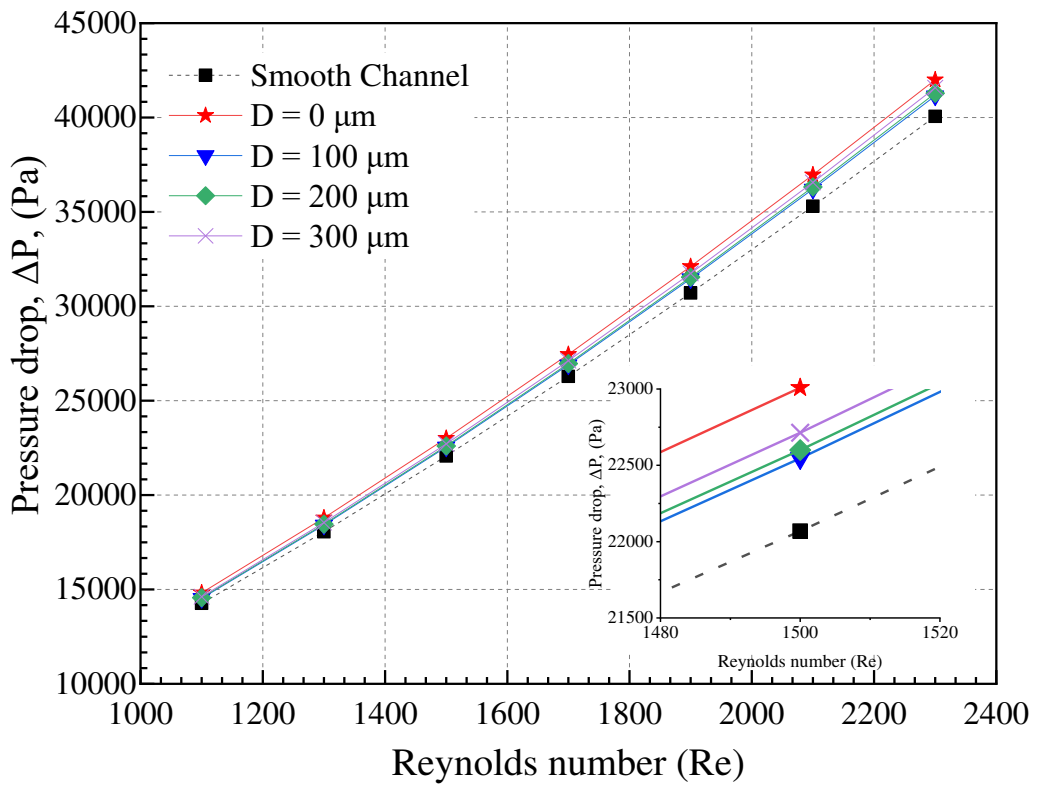
**Figure 13:** Pressure drop against Re from 100 to 2300 and at the front position with the distance between VGs of  $0\mu\text{m}$ .





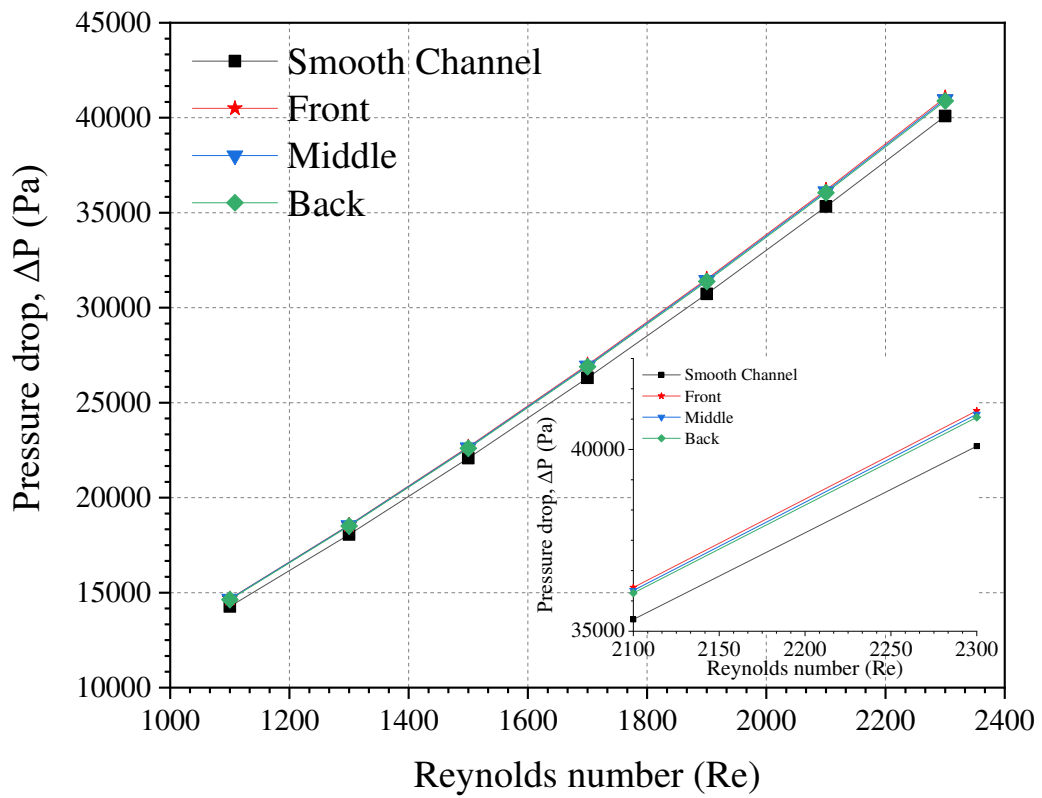
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**Figure 14:** The y-z cross section of the MCHS, with velocity contours (m/s) at different radii of  $100\mu\text{m}$ ,  $200\mu\text{m}$  and  $300\mu\text{m}$  at distance between VGs of  $0\mu\text{m}$  for the front position.



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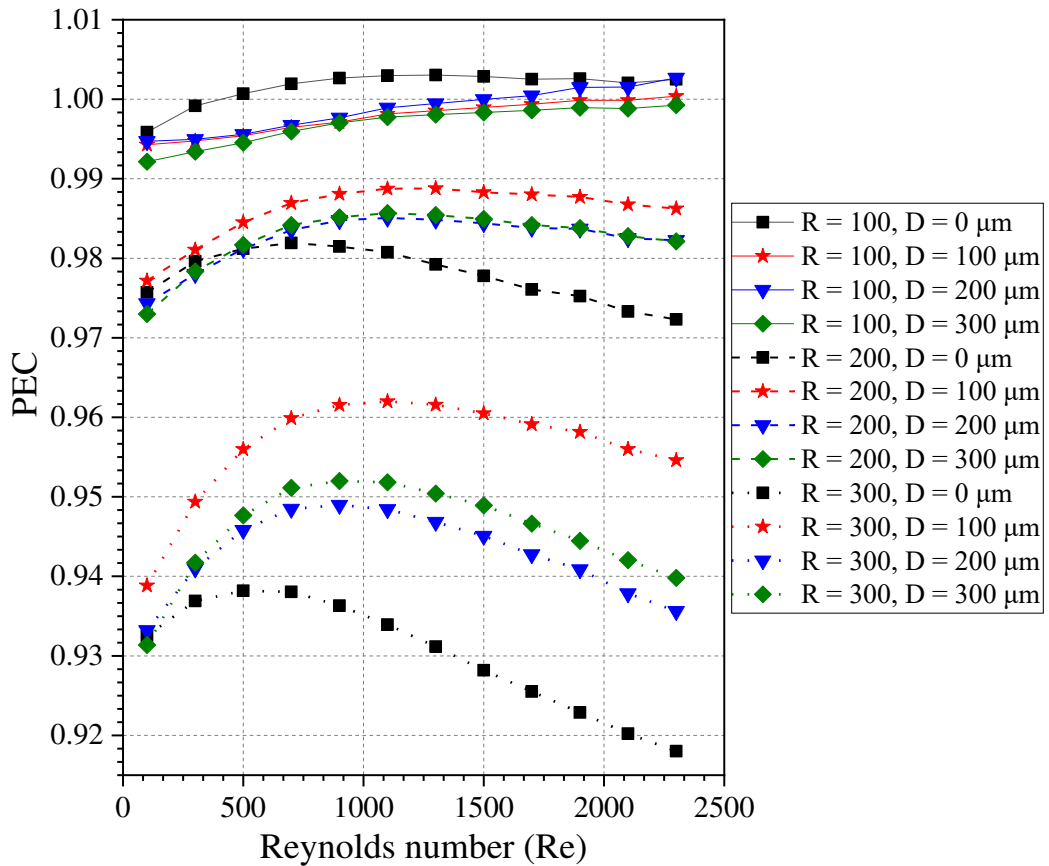
**Figure 15:** Pressure drop against Re at every distance between VGs ranging from (0-300)  $\mu\text{m}$  for the front position at  $R = 100\mu\text{m}$  with zoomed in view.



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**Figure 16:** Pressure drop for VGs placed at the front, middle and back with zoomed in view.

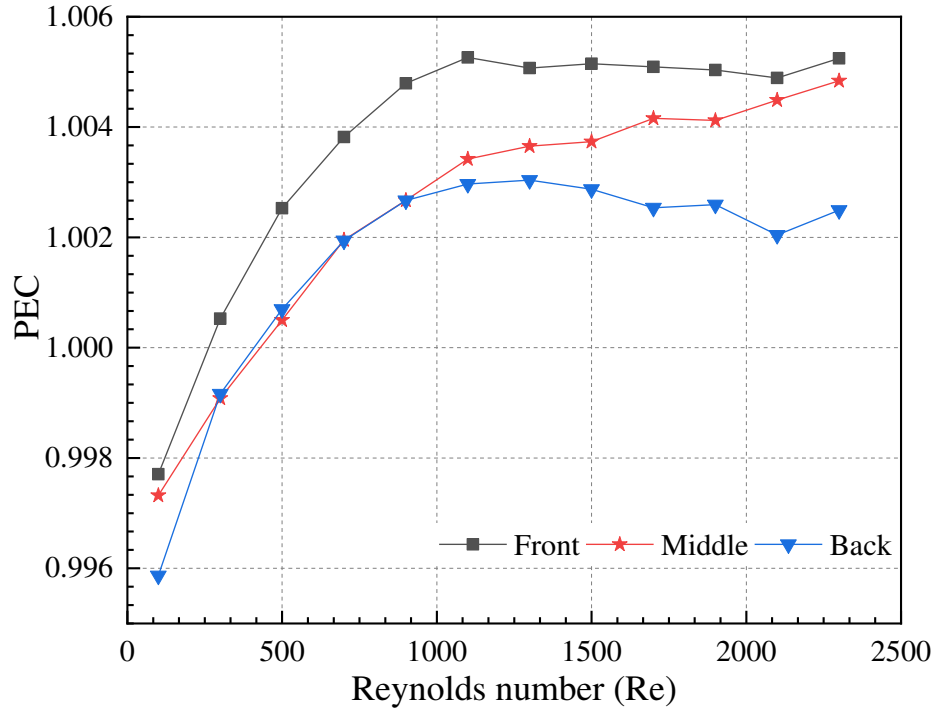


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**Figure 17:** PEC index for different radii and distance between VGs of  $0\mu\text{m}$ ,  $100\mu\text{m}$ ,  $200\mu\text{m}$ , and  $300\mu\text{m}$  at the front position.

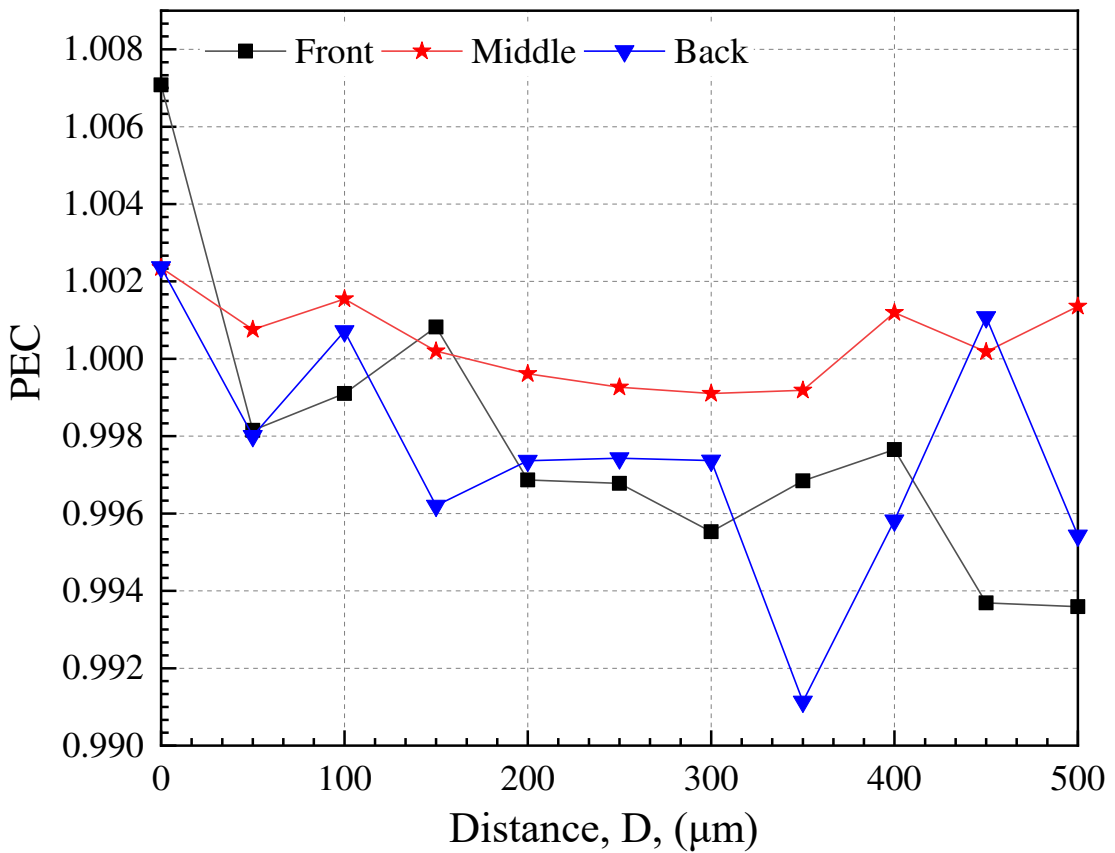


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**Figure 18:** PEC index of different arrangements of VGs (front, middle and back) against Re with the boundary limit set to be 1 for a uniform channel.

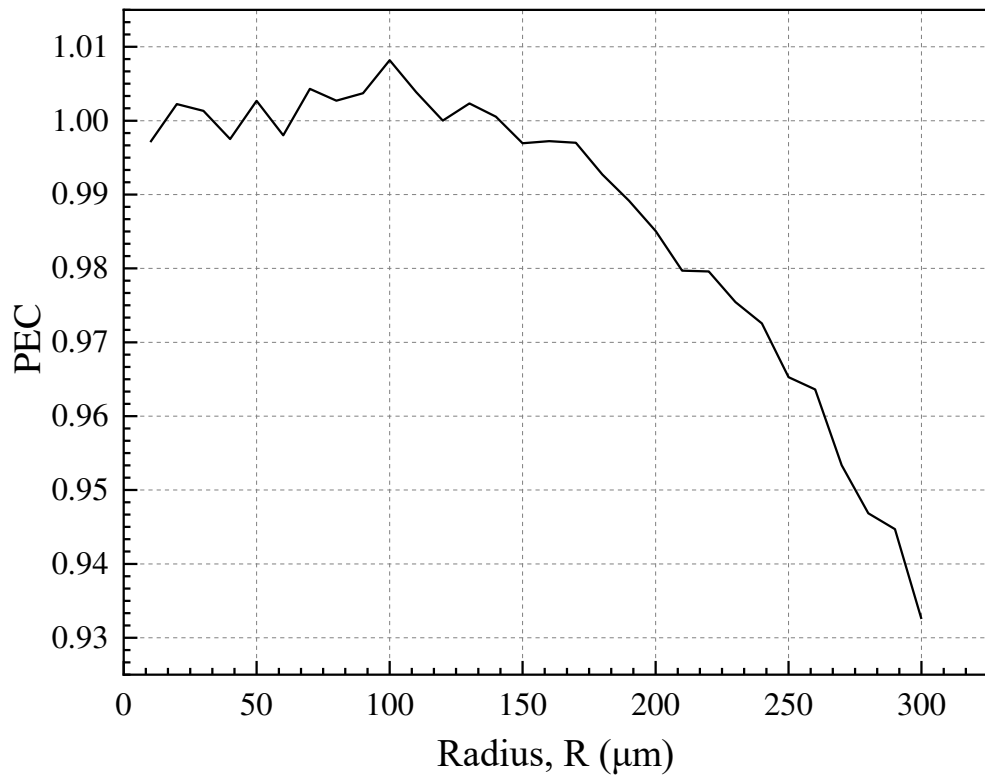


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**Figure 19:** PEC index plot against the distance between VGs at Re= 900 for the three positions.



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**Figure 20:** PEC index for increasing radii at constant Re of 900 with distance,  $D = 0\mu\text{m}$  at the front position.