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Re-tuning an off-tuned tuned mass damper by adjusting temperature
of shape memory alloy: exposed to wind action
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## Abstract

To reduce the wind-induced vibration of building structures, tuned mass damper (TMD) is a widely used approach. However, the off-tune of TMD can cause larger excessive vibration to the structure. In this study, shape memory alloy (SMA) is employed in TMD for retuning. At first, the dynamic properties of SMA-based TMD were characterised by free vibration at between -40°C and 65°C. It is found the stiffness increased and damping reduced with rising temperature. Next, the SMA-based TMD was applied to a steel frame structure under wind excitations. The wind action was generated by autoregressive models method and input by a shaking table. The results present the wind-induced vibration can be attenuated effectively by installing a SMA-based TMD. By changing the main structural mass, the TMD was easy to be off-tuned and the structural response was increased. By means of cooling SMA to retune the TMD, the response of the system can be reduced effectively. However, the effect of heating SMA was relatively small. The increase of damping capacity by combing multiple SMA bars and the applications of SMAs with higher phase transformation temperatures are important to be further investigated in TMD, so as to improve the effectiveness of heating SMA.

# Keywords

Shape memory alloy; wind action; tuned mass damper; retune; off-tuning

# 1. Introduction

Buildings can be affected by wind-induced vibration, and the reliability of structures and comfort level of residents are issues which must be addressed by designers. To reduce the vibration, tuned mass damper (TMD) is a frequently used approach, and is less-complex and space-saving compared with other damping systems. In recent years, TMD is developed fast and has been applied to Taipei 101 in Taipei, the Bloomberg Tower in New York, the Sydney Tower in Sydney, the CN Tower in Toronto and the John Hancock Tower in Boston. The basic principle of TMD is that its natural frequency can be tuned to a particular range, so the damper can resonate with the structure relatively (Connor and Laflamme, 2014). The relative motion of TMD is a way of outputting energy, thus the energy input in the structure can be dissipated and the vibration can be mitigated. TMD can be simulated by consisting of mass  $(m_2)$ , spring  $(k_2)$  and damper  $(c_2)$  as shown in Figure 1 (a). TMD is usually installed in the location where the motion is the greatest such as the top floor (Irwin et al., 2008). Figure 1 (b) presents the idealisation of TMD system into a 2-degree-of-freedom model, where  $m_1$ ,  $k_1$  and  $c_1$  denote the mass, stiffness and damping coefficient of main structure. 

15 The natural frequency of TMD is determined by Equation (1):

$$f_2 = \frac{1}{2\pi} \sqrt{\frac{k_2}{m_2}}$$
(1)

where  $f_2$  denotes the natural frequency of TMD, and  $k_2$  and  $m_2$  imply the stiffness and mass of TMD. The effectiveness of vibration control using TMD can be improved by controlling these parameters: mass ratio and natural frequency ratio between TMD and main structure as well as damping ratio of TMD. The optimal design of TMD parameters was studied, and classical designs can refer to Den Hartog (1956), Sadek et al. (1997), Tsai and Lin (1993) and Warburton (1982). As TMD is a passive vibration control approach, the drawback of using TMD is that TMD could be off-tuned when the main structural condition changes. For instance, the stiffness and mass of buildings usually vary due to climatic events, decoration, repair, and movement of people and facilities (Xue et al., 2009,

Brincker et al., 2004). When the mass and stiffness of the main structure are changed, the tuned condition is influenced and the effectiveness of TMD is degraded (Huang et al., 2017). In off-tuned condition, the structural response subject to vibration may increase greatly (Huang et al., 2017), and the structural safety is threatened.

To overcome this drawback, semi-active TMD (Fisco and Adeli, 2011) is developed as an another passive vibration control approach. In semi-active TMD systems, actively adjustable springs, piezoelectric friction, shape memory alloy (SMA) and other techniques have been employed to adjust the natural frequency of TMD in order to retune it to an expected frequency range (Sun and LI, 2009, Jiang and Hanagan, 2006, Nagarajaiah and Sonmez, 2007). SMA is a smart material with particular thermomechanical properties, and is of potential to be applied to TMD. SMA has two phases: martensite and austenite. As seen in Figure 2 (a), the phase transformation depends on four temperatures:  $M_s$ ,  $M_f$ ,  $A_s$  and  $A_f$  which indicate the start and finish temperature of martensitic and austenitic transformation, respectively. In martensite when in-service temperature is below  $M_f$ , the loading behaviour is shape-memory effect, in which the residual strain can recover to the original point by external heating shown in Figure 2 (b). Martensite has been studied in reinforced concrete and masonry reparation (Soroushian et al., 2001, Indirli et al., 2001). When the working temperature is above  $A_f$ , SMA is austenitic; SMA is superelastic and its loading-unloading curve behaves self-centering as expressed in Figure 2 (c). In a whole, the change of in-service temperature can lead to the change of mechanical behaviours, and stiffness and damping ratio can be varied thereupon (Shaw and Kyriakides, 1995, Araya et al., 2008, Andrawes and DesRoches, 2007). Regarding to fatigue life of SMA, Torra et al. indicated SMA installed in civil structures is expected to withstand a large number of minor oscillations due to the actions of wind (Torra et al., 2009). Our study on SMA material characterisation presents SMA has long fatigue life under small strain level (Huang et al., 2020b). These properties of SMA create the possibility to apply to semi-active TMD.

In mechanical engineering domain, SMA-based tuned mass damper has been developed. Williams et al. (2002) and Aguiar et al. (2013) adjusted the stiffness of SMA by Joule heating so as to change the natural frequency of TMD. Savi et al. (2011), Elahinia et al. (2005) and Williams et al. (2005) conducted numerical studies to investigate the applications of SMA in tuneable mass damper. Most of studies used SMA wires for temperature control in TMD, and heating is mainly from electric current on SMA wires (Rustighi et al., 2005, Aguiar et al., 2013, Mani and Senthilkumar, 2015, Tiseo et al., 2010). Unlike mechanical engineering, effectiveness of using larger size like SMA bars in civil engineering needs to be concerned. Our feasibility study changed the natural frequency of a SMA bar-based TMD attached on a steel cantilever beam through heating and cooling, the excessive free vibration caused by off-tune was effectively attenuated (Huang et al., 2017). Huang and Chang (2018) presented the effectiveness of the SMA-based TMD in reducing the timber floor vibration. More studies regarding the applications of SMA bar to TMD subject to earthquake and wind excitations should be carried out.

The effectiveness of the semi-active TMD in reducing wind-induced structural response has been studied. Yang et al. (2001) investigated the performance of a semi-active magnetorheological TMD in a 76-storey building under wind loading, and considered it to be beneficial. Nagarajaiah and Varadarajan (2005) developed e new semi-active variable stiffness tuned mass damper to reduce the response of wind excited tall buildings. Kang et al. (2011) used a semi-active TMD in which both damping and stiffness can be variable, and the results showed this semi-active TMD could effectively control the vibration of a tall building subject to wind load. Concerning the free vibration testing of SMA-based TMD in our feasibility study (Huang et al., 2017), the vibration can be controlled by varying the natural frequency. It is important the effectiveness of the SMA-based TMD can be examined under wind excitation, as the wind contains wider frequency range unlike machine-induced vibration. To assess the performance of TMD under wind action, theoretical simulation is mostly used. In this study, a new experimental approach is developed, in which shaking table is used

to simulate the wind action. Therefore, a theory of simulating wind action by shaking table is needed,
so as to examine the effectiveness of TMD under the wind.

In this study, a SMA-based variable stiffness and damping TMD was designed and tested, and then applied to a steel frame structure subject to wind loading. By changing the supplementary mass on the main structure to trigger off-tuned situations, the retuning ability of SMA-based TMD was assessed by adjusting the working temperature. The excessive vibration from off-tune is aimed to be reduced by SMA temperature control.

# 2. Dynamic characterisation of the SMA-based TMD and main structural system byfree vibration

In this study, a temperature controlled SMA-based TMD is aimed to be developed and applied to a steel frame structure to reduce the dynamic response subject to wind loading. Therefore, the dynamic properties of the TMD and steel frame structure need to be characterised. Moreover, the effect of temperature on dynamic properties of TMD should be examined. In this section, the variance of stiffness and equivalent viscous damping ratio of TMD under different temperature by free vibration testing are presented, and furthermore the characterisation of the main structure is illustrated.

# 89 2.1 Dynamic characterisation of the SMA-based TMD

SMA used in this study is a Cu-Al-Mn (Cu = 81.84%, Al = 7.43% and Mn = 10.73% by weight) SMA bar. The transformation temperatures  $M_s$ ,  $M_f$ ,  $A_s$  and  $A_f$  were tested by differential scanning calorimetry (DSC), and results show  $M_s = -9^{\circ}$ C,  $M_f = -25^{\circ}$ C,  $A_s = -8^{\circ}$ C and  $A_f = 5^{\circ}$ C. In other word, under cooling process, SMA is martensitic when the in-service temperature is below  $-25^{\circ}$ C. When SMA is heated, SMA completes transformation to austenite after 5°C. The material characterisation of Cu-Al-Mn SMA bars under dynamic bending was performed in our previous material study (Huang et al., 2020b). The material hysteresis, stiffness, damping ratio, and fatigue

97 life were studied under strain levels of 0.5%, 1%, 2%, and 6%. The test results showed Cu-Al-Mn SMA 98 has stable material properties along the dynamic loading and an adequate fatigue life. In this study, 99 dynamic characterisation of SMA-based TMD was carried out at -40, -20, 0, 19, 45, and 65°C, 100 where 19°C is the ambient temperature in laboratory. The the SMA cooling is conducted by spraying 101 Tetrafluoroethane, and heating is implemented by wrapping energised carbon fibre.

In our feasibility studies, the SMA bar was attached to a beam horizontally with pre-stressed load (Huang et al., 2017). In this study, the SMA bar is placed vertically without pre-stress. The free vibration tests are same with our previous study investigating the effectiveness of SMA-based TMD exposed to earthquake excitations (Huang et al., 2020a). As shown in Figure 3 (a), the effective length of SMA bar is 280 mm, and the cross section was machined to 3×12 mm in order to facilitate the unidirectional vibration. As presented in Figure 3 (b), the bottom side of SMA bar was attached with a steel block of 6.4kg, and the top side was fixed rigidly. The free vibration tests were initiated by giving a 10mm displacement at the bottom at different in-service temperatures. The natural frequency and equivalent viscous damping ratio were computed using the linear-prediction singular-value decomposition-based matrix pencil (SVD-MP) method. This approach is able to deal with the approximation for complex exponentials and exhibits high precision in estimating the frequency and damping from measured data. Detailed descriptions can be found in Sarkar and Pereira (1995) and Zieliński and Duda (2011). The SVD-MP approach is based on Equations (2) and (3):

$$y(t) = x(t) + n(t) \approx \sum_{i=1}^{M} R_i \exp(s_i t) + n(t); 0 \le t \le T$$
(2)

115 where y(t) is the observed time response, x(t) is the signal, n(t) is the noise in system, and  $R_i$ 116 denotes the complex amplitudes.  $s_i$  is presented in Equation (3):

$$s_i = -\alpha_i + j\omega_i \tag{3}$$

117 where  $\alpha_i$  and  $\omega_i$  represent the damping factors and the angular frequencies, respectively, and 118  $j = \sqrt{-1}$ . As shown in Equation (2), the objective of SVD-MP is to estimate the frequencies and 119 damping factors from the noise-contaminated data. Thus, solving the parameters is a non-linear 120 problem. According to the equation derivations in Sarkar and Pereira (1995), the matrix pencil is a 121 one-step process for solving a non-linear problem that is computationally efficient. Linear-prediction 122 singular-value decomposition provides a method for decomposing the eigenvectors when using the 123 matrix pencil.

The results show the natural frequency at 19°C is 1.68 Hz. Stiffness was therefore calculated from natural frequency. Figure 4 shows the effect of temperature on stiffness and damping ratio. Stiffness increases and damping ratio decreases with rising temperature from  $-40^{\circ}$ C to  $65^{\circ}$ C. The change of stiffness is dramatic between  $-20^{\circ}$ C and  $0^{\circ}$ C while the damping ratio is sensitive to temperature between  $-40^{\circ}$ C and  $0^{\circ}$ C. As aforementioned about the phase transformation temperatures which are from  $-25^{\circ}$ C to 5°C, the mechanical properties are varied around this temperature range due to the influence of the phase transformation between martensite and austenite. On the whole, the stiffness and damping ratio can be adjusted for up to about 85% and 44% in the testing temperature range, respectively, which presents the potential of using SMA in semi-active TMD.

# 133 2.2 Dynamic characterisation of main structure

The main structure used in this study is the same steel frame which was used in our previous study investigating the performance subject to earthquake loadings as shown in Figure 5 (Huang et al., 2020a). The steel frame is 1.2 m high and 0.6 m wide, and detailed dimensions can be seen in Figure 5 (b). The beam ends were not welded on the columns, and the column-beam connections were built as hinge joints with three paralleled springs to facilitate the rotation. Therefore, the steel framed structure is flexible in the horizontal direction. At the direction perpendicular to the vibration, bracings were added. The detailed descriptions of the steel frame can be referred to Huang et al. (2020a).

The dynamic characterisation of this steel frame with added mass of 10, 25, 30, 35 and 45 kg was done by free vibration. The free vibration was initiated by a shake with a displacement of 5mm from a shaking table shown in Figure 5 (a). The acceleration was measured by accelerometers for 1 minute. When the added mass at the top floor is 30 kg, the natural frequency of the steel frame is 1.78Hz. The optimal design method of TMD can be referred to Warburton (1982). There are two reasons why the Warburton (1982) method was selected as the optimal design method in this study. Firstly, the Warburton method is a classical analytical procedure for designing optimum parameters of TMD under various combinations of excitation and response, which is suitable for the civil engineering application employed in this study. The Warburton method has been widely cited and its effectiveness was demonstrated in previous studies by Hadi and Arfiadi (1998), Miguel et al. (2016) and Islam et al. (2018). Secondly, the Warburton method is a simplified analytical procedure and thus the semi-active vibration control in this study can be eased. By using Warburton (1982)'s optimal design theory presented in Equation (4) and (5):

$$f_{opt} = \sqrt{\frac{(1 - \mu/2)}{1 + \mu}}$$
(4)

$$\zeta_{opt} = \sqrt{\frac{\mu(1 - \mu/4)}{4(1 + \mu)(1 - \mu/2)}}$$
(5)

The natural frequency of TMD should be near 1.66 Hz. In the Equation (4) and (5),  $\mu$  represents the mass ratio between TMD and main structure, and  $f_{opt}$  and  $\zeta_{opt}$  mean optimised natural frequency ratio and damping ratio. The natural frequency of the SMA-based TMD developed in this study is 1.68 Hz as aforementioned in 2.1, which is near the expected value 1.66 Hz. However, the damping ratio of SMA-based TMD is lower than the theoretical expected value calculated by Equation (5).

# 3. Wind input generation

To assess the effectiveness of the SMA-based TMD subject to wind excitation, the method utilised to simulate the wind action is illustrated in this section. In this study, a shaking table test is applied, which represents a new approach for modelling wind excitation.

# 164 3.1 Generation of fluctuating wind force time history

The wind action on a structure can be categorised into the average wind and fluctuating wind. The wind speed and direction of the average wind are constant over time, and it is dependent on the altitude. Fluctuating wind speed time history is a zero-mean Gaussian stochastic process and is characterised by the power spectrum and correlation functions. In this study, the wind action is modelled by fluctuating wind time history. The autoregressive models (AR) method is applied to this study for the purpose of generating fluctuating wind. Wind speed history over time in the AR method can be expressed by Equation (6) (Liang and Liu, 2012):

$$V(t) = \sum_{k=1}^{p} \Psi_k V(t - k\Delta t) + N(t)$$
<sup>(6)</sup>

where *p* is AR model order,  $\Delta t$  is the length of the time step,  $\Psi_k$  is the regression coefficient matrix for the AR model,  $k = 1, 2, \dots, p$  and N(t) is the independent random process vector. Furthermore,  $\Psi_k$  can be derived from Equation (7):

$$R_{\nu}(j\Delta t) = \sum_{k=1}^{p} R_{\nu}[(j-k)\Delta t]\Psi_{k}, j = 1, 2, \cdots p$$
(7)

175 where  $R_v(j\Delta t)$  is correlation matrix, and it is expressed in Equation (8)

$$R_{\nu}(j\Delta t) = \int_{0}^{\infty} S_{\nu}(f) \cos(\omega\Delta t) \, d\omega$$
<sup>(8)</sup>

176 In this study, the Davenport power spectrum  $S_v(f)$  (Davenport, 1961) is used for characterising the 177 stochastic behaviours of fluctuating wind speed, which can be expressed by Equation (9):

$$S_{\nu}(f) = 4K\overline{\nu_{10}}^2 \frac{X^2}{f(1+X^2)^{4/3}}$$
(9)

178 where  $S_{v}(f)$  describes the fluctuating wind velocity spectrum.  $\overline{v_{10}}$  is the mean wind velocity at an 179 altitude of 10 meters,  $X = \frac{1200f}{\overline{v_{10}}}$ , f is the frequency, and K is the surface resistance coefficient. 180 Through the derivations in Equation (7), (8) and (9),  $\Psi_{k}$  can be computed.

181 To acquire N(t):

$$N(t) = Ln(t) \tag{10}$$

n(t) is a normal random process vector within (0,1) and the members in n(t) are independent of 183 each other. The mean value of n(t) is 0, and the variance is 1. If the wind speed time history is 184 required for M points in the space coordinates, *L* would be an M-triangle matrix, which can be 185 decomposed from the M-matrix  $R_N$  by Cholesky decomposition, as shown in Equation (11). 186 Furthermore,  $R_N$  can be solved by Equation (12).

$$R_N = LL^T \tag{11}$$

$$R_{\nu}(0) = \sum_{k=1}^{p} \Psi_k R_{\nu}(k\Delta t) + R_N$$
<sup>(12)</sup>

# 187 The relationship between fluctuating wind pressure and fluctuating wind speed is shown in Equation

188 (13):

$$w(z,t) = \frac{1}{2}\rho[2\overline{v(z)}V(z,t) + v^{2}(z,t)]$$
(13)

189 where  $\bar{v}$  is the mean wind speed at a height of z and  $\rho$  is the air density. w(z, t) is the wind pressure 190 at the height of z. Therefore, the wind force can be calculated by Equation (14), where the *Area* 191 represents the area on the structure subject to wind action.

$$F(t) = w(z, t) \times Area \tag{14}$$

# 3.2 Derivation from wind force to ground motion

193 In this study, the wind motion acting on the structure is modelled by means of inputting ground 194 motion using a shaking table. This is illustrated in Figure 6 (a) and (b), which present a forced 195 vibration system and a base-excited vibration system of a single-degree-of-freedom model, 196 respectively. The dynamic characterisations of forced vibration and base-excited vibration can be 197 described by Equations (15) and (16), respectively. By equating the structural displacement *x* in 198 these two systems, the ground motion *z* in Figure 6 (b) can be derived by the force *F* in Figure 6 (a).

$$m\ddot{x} = F - kx - c\dot{x} \tag{15}$$

$$m\ddot{x} = kz - kx + c\dot{z} - c\dot{x} \tag{16}$$

Through a combination of Equation (15) and (16), the ground motion z(n) can be computed by applying the steps in the flow diagram shown in Figure 7. In Figure 7, n implies the serial number of each time step, and N is the total number of time steps. Figure 7 shows the ground motion computed by the theory demonstrated above, which will be used to model the fluctuating wind action applied via shaking table in the next section.

# 4. Performance of the structure with an off-tuned TMD subject to wind excitation

By varying the mass added on the structure, the natural frequency of the structure would be modified and, as a consequence, the TMD could become off-tuned. In this section, the structural response caused by TMD off-tuning under wind excitation is assessed.

### 4.1 Methods

The non-pre-stressed SMA-based TMD described in Section 2, as shown in Figure 3 (b), was installed on the steel framed structure as shown in Figure 5 vertically. The installation of the SMA-based TMD is presented in Figure 8. The upper section of the SMA bar was rigidly fixed to the second floor. Thus, the stiffness and damping capacity of the TMD were provided by the bending of the SMA. To model the wind action, the ground motion presented in Figure 9 was input using the shaking table. The measurement of acceleration was conducted by accelerometers at a sampling rate of 100 Hz. The testing programme is revealed in Table 1.

# **216**

Table 1 Testing programme of off-tune

Test number	Mass added on the top floor	With or without TMD	Length of measurement (seconds)	Ground motion input
1	10kg	Without TMD	30	Wind excitation
2		With TMD	30	Wind excitation
3	25kg	Without TMD	30	Wind excitation
4		With TMD	30	Wind excitation
5	30kg	Without TMD	30	Wind excitation
6		With TMD	30	Wind excitation
7	35kg	Without TMD	30	Wind excitation
8		With TMD	30	Wind excitation
9	45kg	Without TMD	30	Wind excitation
10		With TMD	30	Wind excitation

# 4.2 Results and discussion

Figure 10 shows the acceleration experienced at the top floor measured from Test Nos. 1-10, and a comparison of the structural responses of the conditions with and without the TMD. It can be observed that the structural response under wind excitation can be reduced by installing the TMD

when the added mass is 25, 30 and 35 kg. However, the structural response actually increased with
10 and 45 kg added mass after installation of the TMD. According to Figures 10 (a) and (e), the offtuning of the TMD induces a greater structural response.

The root mean square (RMS) acceleration for each test is shown in Table 2. The reduction percentage in Table 2 indicates the proportion of the structural response reduced by installing the TMD. When the added mass is 30 kg, the RMS acceleration is the smallest, and the reduction percentage is 30.89%, which indicates that the TMD is approaching its most effective status. This can be explained with reference to the optimal design of TMDs where, if the added mass is 30 kg, the design of the natural frequency of the TMD is near optimal, according to Warburton (1982)'s design theory. In that condition, the TMD is capable of vibrating out of phase with the main structure, thus more energy can be dissipated. However, analysis of the off-tuned conditions reveals that the RMS acceleration becomes larger.

Table 2 RMS acceleration [gal] (Test #)

	10	25	20	25	45
Added mass on top floor (kg)	10	25	30	35	45
With damper	53.0 (2)	33.0 (4)	27.3 (6)	27.4 (8)	30.6 (10)
Without damper	47.7 (1)	46.4 (3)	39.5 (5)	31.4 (7)	28.2 (9)
Reduction percentage	-11.11%	28.88%	30.89%	12.74%	-8.51%

# 5. Retuning the TMD by changing the SMA temperature under wind excitations

Analysis of the scenarios with an off-tuned TMD demonstrated in Section 4 reveal that, by increasing the added mass from 30 kg to 45 kg, the RMS acceleration was increased by 12.09%. The RMS acceleration rose 20.88% when the added mass decreased from 30 kg to 25 kg. It is important to apply temperature control of the SMA for retuning purposes, with the aim of reducing the structural response after adjusting the natural frequency. The control strategy is shown in Figure 11. To adjust

the properties of SMA using temperature control, the cooling process is performed by spraying Tetrafluoroethane while heating is achieved by wrapping the SMA in energised carbon fibre. Experimental testing using these methods shows that SMA can be cooled to  $-20^{\circ}$ C in 1-2 seconds and heated to  $45^{\circ}$ C in a short period (due to the high thermal conductivity of copper).

### 5.1 Retuning methods

According to Warburton (1982)'s design theory, when the structural added mass is increased to 45 kg from 30 kg, the expected natural frequency of the TMD becomes 1.46 Hz, as opposed to 1.66 Hz with 30 kg. In order to retune the main structure, the stiffness of the TMD should be decreased by cooling to -25 or -40°C. By implementing this strategy, the natural frequency of the TMD can be adjusted to achieve a result that is approximate to the theoretical expected value. When the added mass decreases to 25 kg from 30 kg, the expected natural frequency of the TMD is 1.71 Hz. The TMD therefore requires heating to 45°C or 65°C so as to increase the natural frequency of the TMD to approach the expected value. The cooling process is conducted by spraying Tetrafluoroethane, whereas heating is implemented by wrapping the SMA in energised carbon fibre. The testing programme is detailed in Table 3.

## Table 3 Testing programme of retuning

Test number	Mass added on the top floor	With or without TMD	Length of measurement (seconds)	Ground motion input
11	Increase mass to 45kg	Decrease temperature to - 20°C	30	Wind excitation
12		Decrease temperature to - 40°C	30	Wind excitation
13	Decrease mass to 25kg	Increase temperature to 45°C	30	Wind excitation
14		Increase temperature to 65°C	30	Wind excitation

# 259 5.2 Results: Retuning the TMD when the structural mass increases to 45 kg

Figure 12 compares the acceleration time history at the top floor at room temperature conditions and under cooling. Figures 12 (a) and (b) demonstrate that it is feasible to effectively attenuate the excessive structural response caused by off-tuning by cooling the SMA. It should be noted that the structural response at -40°C is relatively small compared with the response at -20°C. With respect to Table 4, the RMS acceleration of 20.0 gal in Test 12 is significantly smaller than the corresponding result in Test 10 of 30.6 gal. Furthermore, 34.64% of the RMS acceleration was reduced through cooling the SMA to -40°C from 19°C.

There are two reasons behind the effective reduction in structural response by cooling. First, the natural frequency of the TMD was retuned to the expected frequency range. Secondly, the damping ratio can be increased by cooling and, in particular, rises significantly from -20°C to -40°C. As the damping ratio of the SMA-based TMD included in this study was not optimally designed and lower than the expected value, the increased damping ratio by cooling to -40°C can partially compensate for this deficiency and, therefore, facilitate the structural response reduction.

Table 4 The structural response with added mass of 45kg after re-tuning the TMD by cooling the SMA

Temperature of damper (°C)	Test number	RMS acceleration (gal)	Reduction Percentage
-40	12	20.0	34.64%
-20	11	21.4	30.07%
19	10	30.6	reference

# 275 5.3 Results: Retuning the TMD when the structural mass decreases to 25 kg

Figures 13 (a) and (b) present the structural response experienced when the SMA-based TMD was heated to 45°C and 65°C (Test 13 and 14), respectively. It can be observed that the structural response was not reduced via heating. According to Table 5, the RMS acceleration was increased by

 3.94% when the heating process was conducted on the SMA. The results demonstrate that the effectiveness of heating the SMA to retune the TMD is non-significant. This could be due to the stiffness of the SMA at a temperature greater than 19°C being insensitive to temperature, which in turn provides a smaller variance. Moreover, heating causes a loss of damping, which degrades the energy dissipation capacity of the TMD.

Table 5 The structural response with added mass of 25kg after re-tuning the TMD by heating the SMA

Temperature of damper (°C)	Test number	RMS acceleration (gal)	Reduction Percentage
65	14	34.3	-3.94%
45	13	34.2	-3.64%
19	4	33.0	reference

# 86 5.4 Discussion

The phase transformation temperature range of the SMA applied during this study is from -25°C to 5°C. The variance of the mechanical properties is large when the SMA is cooled to -20 and -40°C from 19°C, because the SMA transforms to martensite from austenite. If the phase transformation temperature range of the SMA can be adjusted to the higher temperature, the effectiveness of the SMA-based TMD for temperature control at a higher temperature than 19°C, can be improved. In future studies, SMAs with higher phase transformation temperatures should be investigated in terms of their application in semi-active TMDs.

In applications designed to resist wind-induced vibration, the fatigue life of the SMA is particularly important. Therefore, it is essential to study the characteristics of the Cu-Al-Mn SMA under small strain level deformation. As indicated in our previous material studies, which analysed a SMA bar under dynamic bending, the secant stiffness and equivalent viscous damping ratio tend to be smaller in the first 100 cycles in both Cu-Al-Mn and Ni-Ti SMAs. Similar instability of SMAs in the initial cycles

has been previously studied (Eggeler et al., 2004, Soul et al., 2010, Khan et al., 2013). The cause of this instability has been attributed to the dislocation slip between grains, where the internal stress caused by the slip influences the dynamic properties. In order to overcome this problem, Hartl et al. (2010) conducted 100 thermal cycles with a constant stress on the SMA and found the transformation strain become insensitive to the loading cycles. According to previous studies (Shaw and Kyriakides, 1995, Khan et al., 2013, Miyazaki et al., 1986), appropriate annealing treatment can generate stable behaviours in the SMA. Moreover, cyclic loading as a form of 'pre-training' is also an effective method to stabilise the dynamic properties of the SMA. Thus, in future investigations on SMA-based TMDs, the stabilisation of the SMA should be considered. 

When applied to real civil structures, the SMA-based TMD should be of a larger size and thus the efficiency of the temperature control needs to be considered. Copper has a better thermal conductivity than that of other elements comprising SMA, e.g. nickel and titanium, which means that copper-based SMA such Cu-Al-Mn SMA is preferred in real applications. The SMA-based TMD can also employ multiple SMA bars in parallel. Heating and cooling multiple SMA bars can speed up the temperature control and increase its accuracy. This is because, in this combined system, separate bars can be heated and cooled concurrently, enabling the control of both the natural frequency and the damping ratio at a near optimal level of design. The application of multiple SMA bars can be effective in providing an adequate damping ratio in the event of damping loss when heating. The use of multiple SMA bars as a control strategy will be investigated in further studies.

In a future extension of this study, one single SMA-based TMD can be replaced by SMA-based multi-TMD (MTMD) system. MTMD means that more than one TMD is installed on the structure in parallel or in series (Nigdeli and Bekdas, 2019, Arfiadi, 2016). MTMD can distribute natural frequency and can be designed to tune several modes of structural vibration. Consequently, the vibration amplitude can be reduced further in a wider frequency range.

The optimal TMD design method used in this study is the Warburton method (Warburton, 1982), because this study was conducted on a laboratory scale. More precise and effective optimal design methods are required by the full-scale SMA-based tuned mass damper to control large-size structures. Bekdas and Nigdeli (2011), Nigdeli and Bekdas (2013), Bekdas et al. (2017), and Nigdeli and Bekdaş (2017) have developed optimal design methods employing the harmony search algorithm. Optimal design methods employing novel algorithms such as Particle swarm optimisation algorithm (Leung and Zhang, 2009) and machine learning algorithm (Yucel et al., 2019) have recently developed and can be incorporated into the SMA-based TMD to increase the tuning efficiency in future research. Structures not only sustain wind loads; they also suffer seismic loads. Therefore, a reduction in seismic vibration should be taken into consideration in the optimal design procedures employed in further studies of SMA-based TMD (Pourzeynali et al., 2013, Farshidianfar and Soheilia, 2013, Nigdeli and Bekdas, 2014, Bekdaş et al., 2018, Bekdaş et al., 2019).

Wind can cause simultaneous horizontal loadings and vertical loadings on the structure. For tall structures and flexible structures, the vertical stiffness is much larger in comparison to the horizontal stiffness and thus the vertical loads exert only a minimal effect on the vertical axis force on the structure. In such cases, the wind loadings in the calculation can be assumed to be horizontal actions. However, the vertical loads of wind greatly affect the vibration of space structures and long-span structures, and thus should be taken into consideration in the design process. In the tested steel framed structure used in this study, the column-beam connections were built as hinge joints with three parallel springs to facilitate rotation. The steel framed structure was therefore flexible in the horizontal direction. Thus, the wind loads were simplified as horizontal actions. Furthermore, due to the single-degree-of-freedom limitation of the shaking table in the laboratory, the wind loads can only be excited horizontally. For civil engineering applications, both horizontal and vertical wind loadings should be considered in the analytical model to ensure an accurate design.

# 347 6. Conclusion

In this study, SMA was applied to retune an off-tuned TMD to reduce wind-induced vibration. By material characterisation of Cu-Al-Mn SMA, the stiffness increases and damping ratio decreases with rising temperature. The stiffness and damping ratio are sensitive to temperature when the in-service temperature is near the phase transformation temperature range.

The wind excitation in this study was generated through application of the AR method and was imposed by ground motion using a shaking table. The results demonstrate that the wind-induced vibration of the steel framed structure can be attenuated effectively by installing a SMA-based TMD. However, by increasing and decreasing the main structural mass to instigate off-tuning, the structural response became larger. The RMS acceleration shows an increase of up to 20.88% when the TMD is off-tuned. The effectiveness of cooling SMA is significant in terms of retuning the off-tuned TMD, because the stiffness variance is large between -25°C and 5°C and the damping was increased. However, heating the SMA presents limited effectiveness in retuning the TMD, since the stiffness of the SMA is insensitive at temperatures greater than 19°C and damping is reduced. In further studies, SMAs with higher phase transformation temperatures will be applied, and the control theory for multiple SMA bars as well other approaches will be investigated in order to increase the damping capacity of the TMD.

# 364 Acknowledgement

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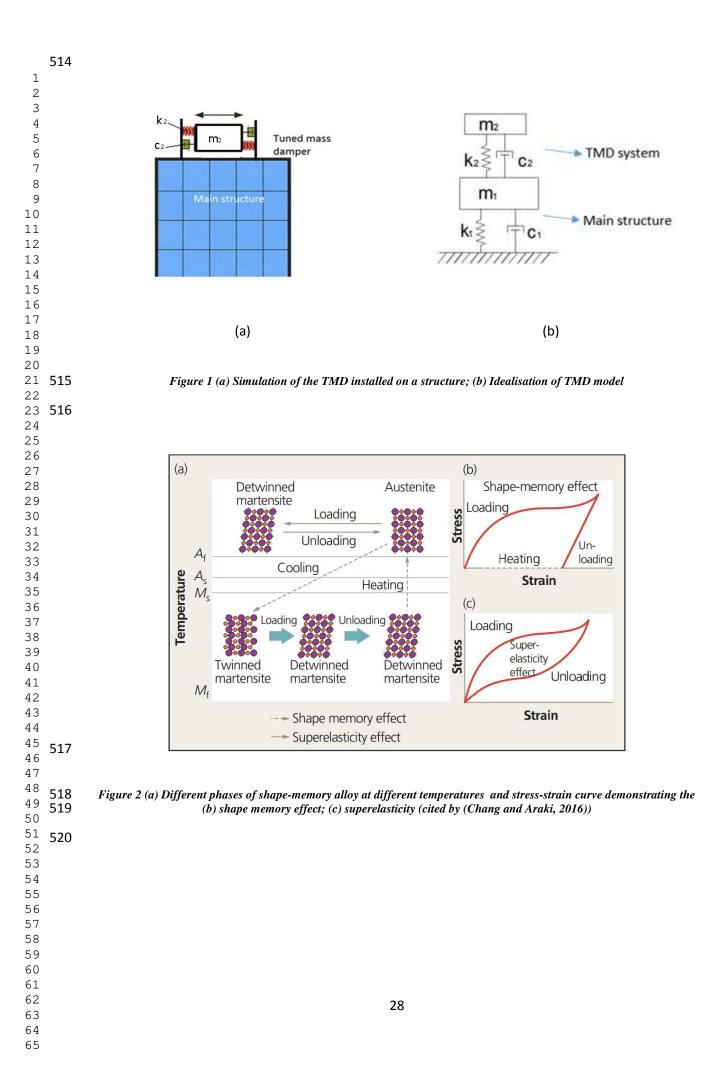
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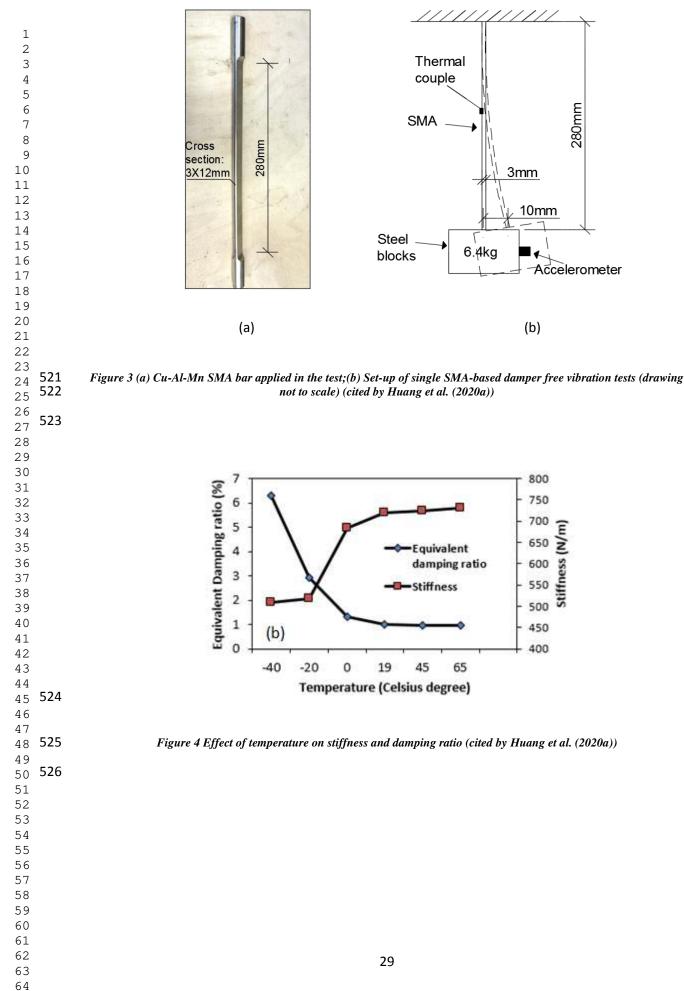
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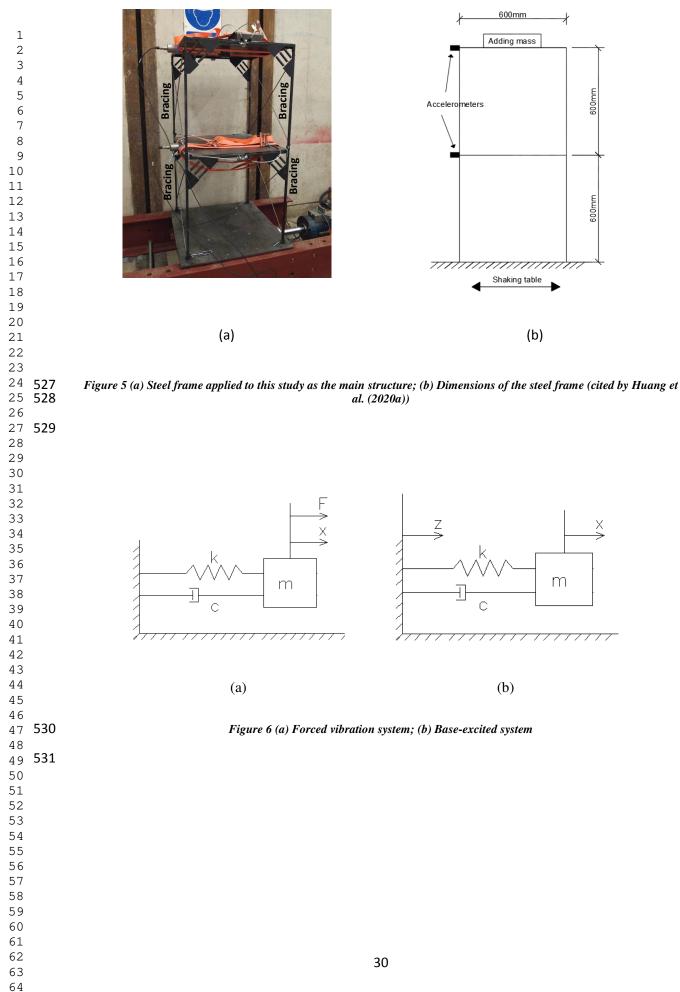
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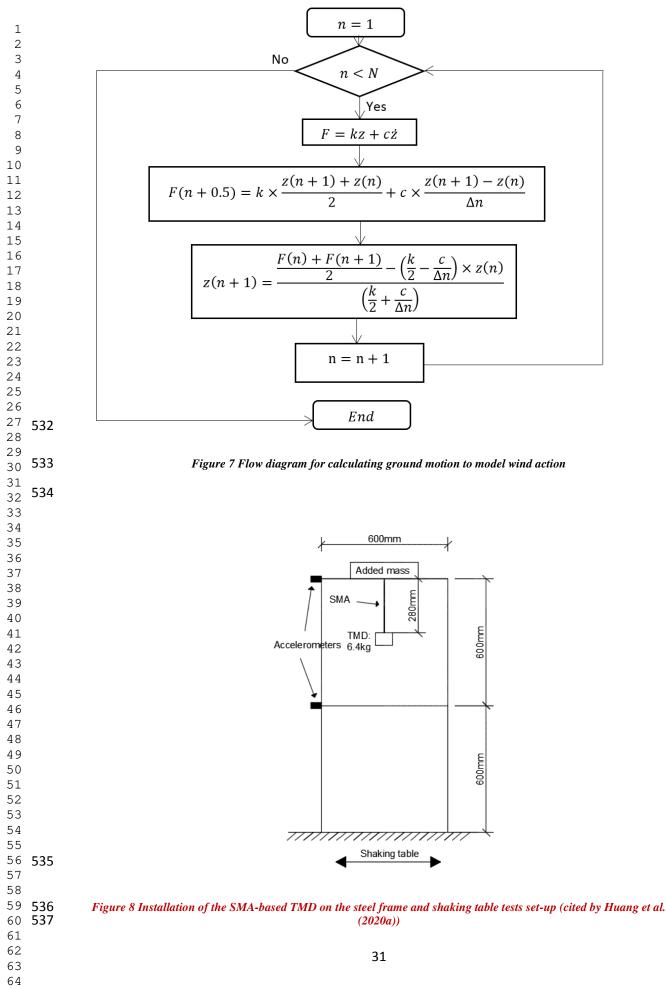
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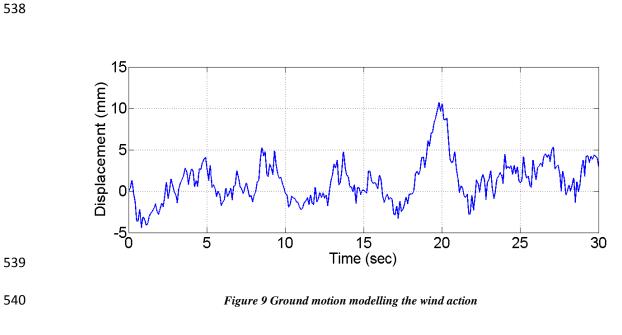
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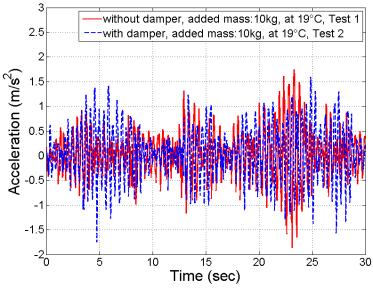






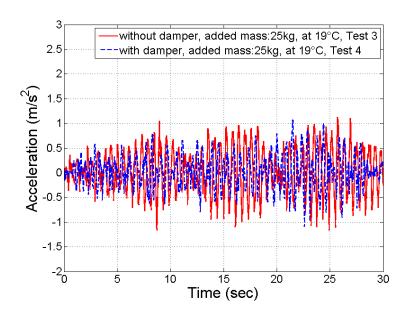




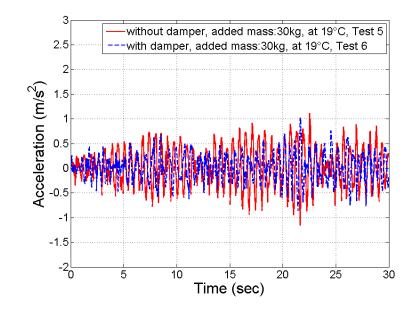


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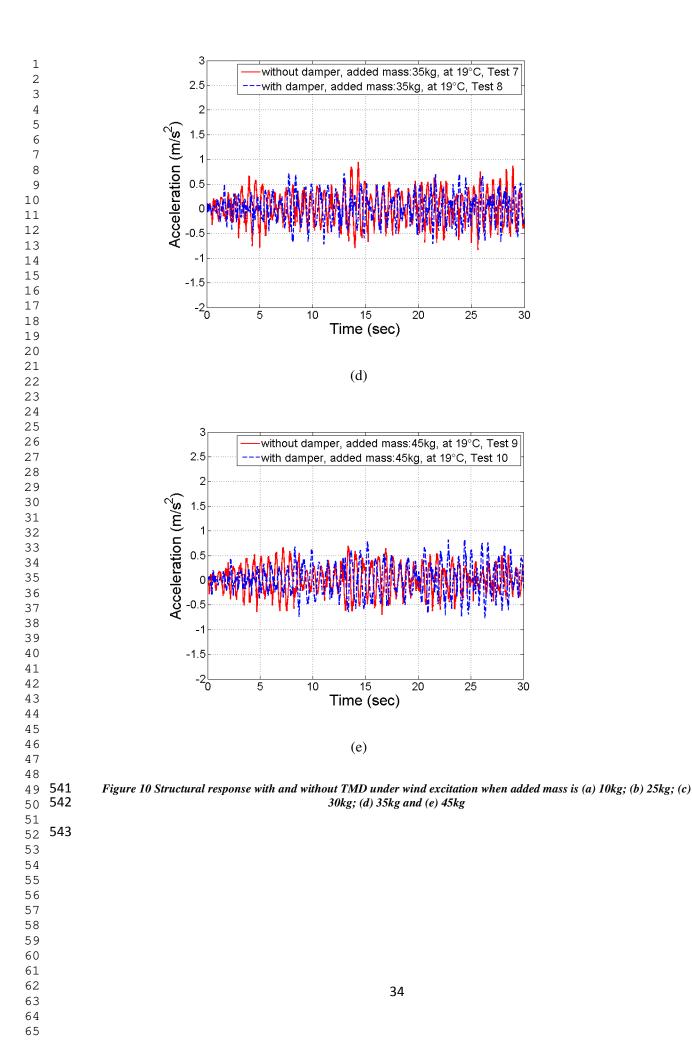
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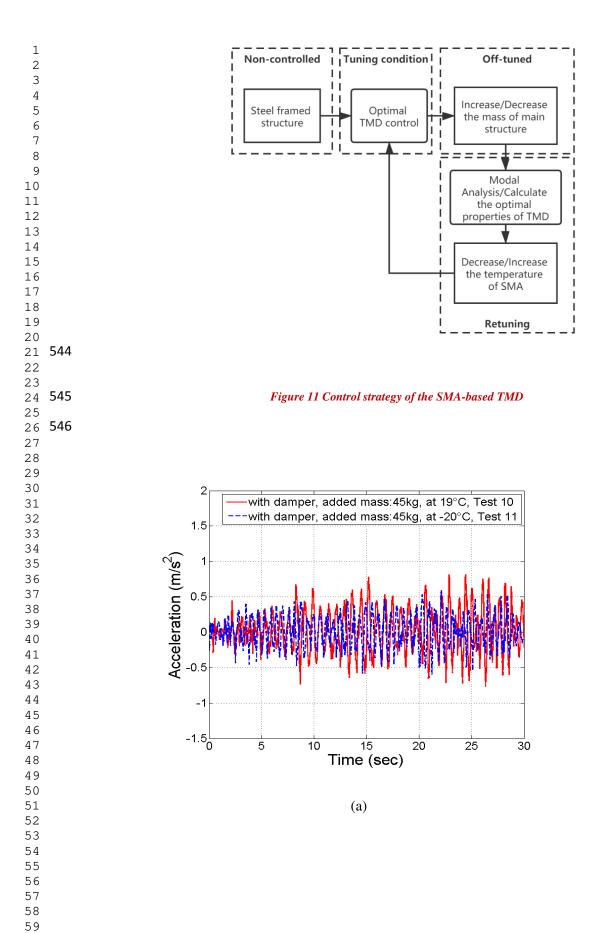






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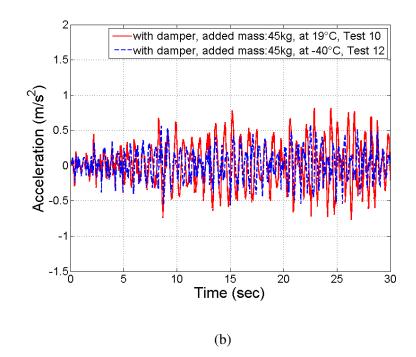
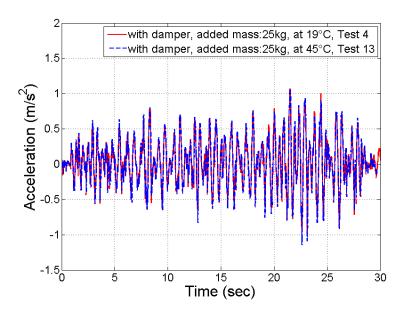
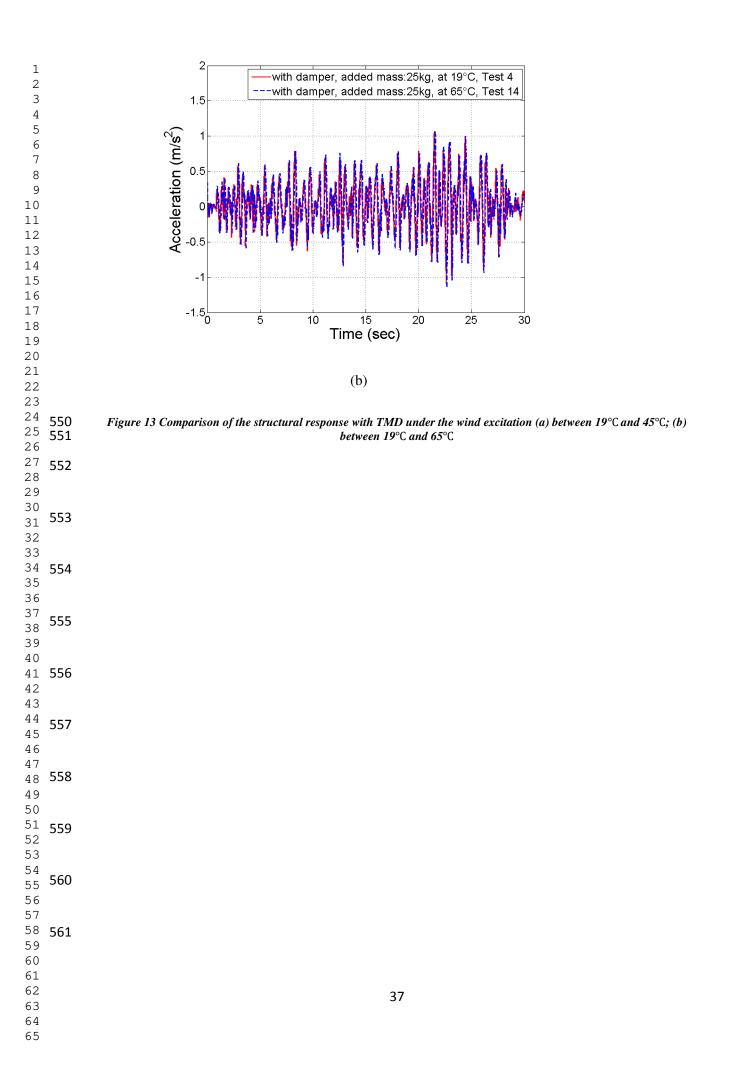


Figure 12 Comparison of the structural response with TMD under the wind excitation (a) at between 19°C and -20°C; (b) at between 19°C and -40°C



(a)



1	562	Figure captions
2 3 4	563	Figure 1 (a) Simulation of the TMD installed on a structure; (b) Idealisation of TMD model
5 6 7	564	Figure 2 (a) Different phases of shape-memory alloy at different temperatures and stress-strain
8 9 10 11 12 13 14 15	565	curve demonstrating the (b) shape memory effect; (c) superelasticity (cited by (Chang and
	566	Araki, 2016))
	567	Figure 3 (a) Cu-Al-Mn SMA bar applied in the test;(b) Set-up of single SMA-based damper free
16 17 18	568	vibration tests (drawing not to scale) (cited by Huang et al. (2020a))
19 20 21 22	569	Figure 4 Effect of temperature on stiffness and damping ratio (cited by Huang et al. (2020a))
23 24 25	570	Figure 5 (a) Steel frame applied to this study as the main structure; (b) Dimensions of the steel
26 27	571	frame (cited by Huang et al. (2020a))
28 29 30 31	572	Figure 6 (a) Forced vibration system; (b) Base-excited system
32 33 34 35	573	Figure 7 Flow diagram for calculating ground motion to model wind action
36 37	574	Figure 8 Installation of the SMA-based TMD on the steel frame and shaking table tests set-up
38 39 40 41	575	(cited by Huang et al. (2020a))
42 43 44	576	Figure 9 Ground motion modelling the wind action
45 46 47	577	Figure 10 Structural response with and without TMD under wind excitation when added mass is
48 49 50	578	(a) 10kg; (b) 25kg; (c) 30kg; (d) 35kg and (e) 45kg
51 52 53	579	Figure 11 Control strategy of the SMA-based TMD
54 55 56	580	Figure 12 Comparison of the structural response with TMD under the wind excitation (a) at
57 58 59 60	581	between 19°C and -20°C; (b) at between 19°C and -40°C
61 62 63 64 65		38

1	582	Figure 13 Comparison of the structural	response	with	TMD	under	the	wind	excitation	(a)
1 2 3	583	between 19°C and 45°C; (b) between	19°C and	65°C						
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Dear Editor,

Please find tables which we respond to all the comments that reviewers have, we have considered comments from reviewers, responded and amended our manuscript as appropriate. The comments from reviewers are very useful to improve the quality of the manuscript, their efforts and time are much appreciated. We are looking forward to working with you during the review process.

Best regards,

Wen-Shao Chang

Reviewer #4:

Reviewer's comments	Response to reviewer
(1) How to use the SMA in TMD, this	The authors agree with the reviewer's comments.
information is lacking. For example, How is	The questions raised are answered in turn below.
the SMA arranged in the TMD device in this	
study? How fast is the shape memory alloy	The non-pre-stressed SMA-based TMD described
heating and cooling? What is the control	in Section 2, as shown in Figure 3 (b), was installed
strategy? Does these affect control	on the steel framed structure as shown in Figure 5
frequency, accuracy, and application of	vertically. The installation of the SMA-based TMD
actual semi-active control?	is presented in Figure 8. The upper section of the
	SMA bar was rigidly fixed to the second floor.
	Thus, the stiffness and damping capacity of the
	TMD were provided by the bending of the SMA.
	Figure 8 has been added in the manuscript to
	show the arrangement of the SMA-based TMD.
	The explanation above has been included in the
	first paragraph in Section 4.1 and is marked in red.
	It is important to apply temperature control of the
	SMA for retuning purposes. The aim is to reduce
	the structural response after adjusting the natural
	frequency. The control strategy is shown in Figure
	11. To adjust the properties of SMA using
	temperature control, the cooling process is
	performed by spraying Tetrafluoroethane while
	heating is achieved by wrapping the SMA in
	energised carbon fibre. Experimental testing using
	these methods shows that SMA can be cooled to -
	20 $^\circ\!\mathrm{C}$ in 1-2 seconds and heated to 45 $^\circ\!\mathrm{C}$ in a short
	period (due to the high thermal conductivity of
	copper). The explanation above has been included
	in the first paragraph of Section 5 and is marked in
	red.
	When applied to real civil structures, the SMA-
	based TMD should be of a larger size and thus the
	efficiency of the temperature control needs to be
	considered. Copper has a better thermal
	conductivity than that of other elements
	comprising SMA, e.g. nickel and titanium, which
	means that copper-based SMA such Cu-Al-Mn
	SMA is preferred in real applications. The SMA-
	based TMD can also employ multiple SMA bars in
	parallel. Heating and cooling multiple SMA bars
	can speed up the temperature control and
	increase its accuracy. This is because, in this
	combined system, separate bars can be heated
	and cooled concurrently, enabling the control of
	both the natural frequency and the damping ratio
	at a near optimal level of design. The application
	of multiple SMA bars can be effective in providing

	an adequate damping ratio in the event of damping loss when heating. The use of multiple SMA bars as a control strategy will be investigated in further studies. The explanation above has been included in the third paragraph of Section 5.4 and is marked in red.
(2) Please provide a full description of linear- prediction singular-value decomposition- based matrix pencil method in section 2.1. How is it calculated and how do the Numbers justify the results?	The authors agree with the reviewer's comments. The natural frequency and equivalent viscous damping ratio were computed using the linear- prediction singular-value decomposition-based matrix pencil (SVD-MP) method. This approach is able to deal with the approximation for complex exponentials and exhibits high precision in estimating the frequency and damping from measured data. Detailed descriptions can be found in Sarkar and Pereira (1995) and Zieliński and Duda (2011). The SVD-MP approach is based on Equations (2) and (3):
	y(t) = x(t) + n(t) $\approx \sum_{i=1}^{M} R_i \exp(s_i t) \qquad (2)$ $+ n(t); 0 \le t \le T$
	where $y(t)$ is the observed time response, $x(t)$ is the signal, $n(t)$ is the noise in system, and $R_i$ denotes the complex amplitudes. $s_i$ is presented in Equation (3):
	$s_i = -\alpha_i + j\omega_i \tag{3}$
	where $\alpha_i$ and $\omega_i$ represent the damping factors and the angular frequencies, respectively, and $j = \sqrt{-1}$ . As shown in Equation (2), the objective of SVD-MP is to estimate the frequencies and damping factors from the noise-contaminated data. Thus, solving the parameters is a non-linear problem. According to the equation derivations in Sarkar and Pereira (1995), the matrix pencil is a one-step process for solving a non-linear problem that is computationally efficient. Linear-prediction singular-value decomposition provides a method for decomposing the eigenvectors when using the matrix pencil. The explanation above has been included in the second paragraph of Section 2.1 and is marked in red.
(3) In general, it takes some time to change the elastic modulus of SMA or to generate the driving force, and the material itself has	The authors agree with the reviewer's comments. The material characterisation of Cu-Al-Mn SMA bars under dynamic bending was performed in our

hysteresis. In this respect, what are the properties of the shape memory alloys used in this study?	previous material study (Huang et al., 2020). The material hysteresis, stiffness, damping ratio, and fatigue life were studied under strain levels of 0.5%, 1%, 2%, and 6%. The test results showed Cu- Al-Mn SMA has stable material properties along the dynamic loading and an adequate fatigue life. The explanation above has been included in the first paragraph of Section 2.1 and is marked in red. For the properties of Cu-Al-Mn SMA, please refer to our paper : HUANG, H., ZHU, YZ. & CHANG, WS. 2020. Comparison of Bending Fatigue of NiTi and CuAlMn Shape Memory Alloy Bars. Advances in
(4) According to the size of start former in	Materials Science and Engineering, 2020, 1-9.
(4) According to the size of steel frame in this paper, the vertical correlation of fluctuating wind load cannot be ignored. However, only one degree of freedom (horizontal) is considered in this paper. Hope the author can consider this factor.	The authors agree with the reviewer's comments. Wind can cause simultaneous horizontal loadings and vertical loadings on the structure. For tall structures and flexible structures, the vertical stiffness is much larger in comparison to the horizontal stiffness and thus the vertical loads exert only a minimal effect on the vertical axis force on the structure. In such cases, the wind loadings in the calculation can be assumed to be horizontal actions. However, the vertical loads of wind greatly affect the vibration of space structures and long-span structures, and thus should be taken into consideration in the design process. In the tested steel framed structure used in this study, the column-beam connections were built as hinge joints with three parallel springs to facilitate rotation. The steel framed structure was therefore flexible in the horizontal direction. Thus, the wind loads were simplified as horizontal actions. Furthermore, due to the single-degree-of- freedom limitation of the shaking table in the laboratory, the wind loads can only be excited horizontally. For civil engineering applications, both horizontal and vertical wind loadings should be considered in the analytical model to ensure an accurate design. The explanation above has been included in the final paragraph of Section 5.4.
(5) When the remarkable period of wind load is close to the natural vibration period of the building structure, the wind-induced	The authors agree with the special case raised by the reviewer, and it is true that the vibration amplitude could be substantially greater when the
vibration will not only cause the structure damage, but also cause the residents' discomfort. Then, whether the ground motion input in this paper takes this special	frequencies of the wind and the structure become equal. This is because the resonance between loading frequency and structural frequency can cause enormous vibration. The SMA-based TMD is

and into account I have the outhor con	designed to us dues the visit of this energial and
case into account. I hope the author can explain.	designed to reduce the risk of this special case occurring. The explanation was presented in our published feasibility study:
	HUANG, H., CHANG, WS. & MOSALAM, K. M. 2017. Feasibility of shape memory alloy in a tuneable mass damper to reduce excessive in- service vibration. Structural Control & Health Monitoring, 24, 1-14.
	The following figure (cited by Huang et al. (2017)) shows the results of our TMD tests. The blue curve denotes the vibration amplitude of the main structure without TMD control. At frequencies of around 4-5 Hz, the amplitude is extremely large, a result attributable to the resonance between loading frequency and structural frequency. The orange curve shows the reduction in vibration amplitude that occurs when employing a SMA- based TMD. The vibration can clearly be reduced in a wider frequency band.
	100 90 80 70 90 90 100 100 100 100 100 100
	In a future extension of this study, one single SMA-based TMD can be replaced by SMA-based multi-TMD (MTMD) system. MTMD means that more than one TMD is installed on the structure in parallel or in series (Nigdeli and Bekdas, 2019, Arfiadi, 2016). MTMD can distribute natural
	frequency and can be designed to tune several modes of structural vibration. Consequently, the vibration amplitude can be reduced further in a wider frequency range. The discussion above has been included in the fourth paragraph in Section 5.4 and is marked in red.

Reviewer #1:

Reviewer's comments	Response to reviewer
(1) In introduction, there are no dates for	The authors thank the reviewers for their efforts
Connor et al. It must be the following study.	in correcting the references. The in-text citation
Connor, J., & Laflamme, S. (2014). Structural	and the corresponding reference have now been
motion engineering (Vol. 476). New York:	corrected.
Springer.	
So. Give it as Connor and Laflamme (2014)	
and correct it in references.	
<ul> <li>(2) In the paper, the optimum tuning method of Warburton was used. Why this method is choosen? The other methods must be also mentioned. In future studies, I suggest to use other methods, espacially the curve fitting formulations given in Yucel et al. 2019.</li> <li>Yucel, M., Bekdaş, G., Nigdeli, S. M., &amp; Sevgen, S. (2019). Estimation of optimum tuned mass damper parameters via machine learning. Journal of Building Engineering, 26, 100847.</li> </ul>	There are two reasons why the Warburton (1982) method was selected as the optimal design method in this study. Firstly, the Warburton method is a classical analytical procedure for designing optimum parameters of TMD under various combinations of excitation and response, which is suitable for the civil engineering application employed in this study. The Warburton method has been widely cited and its effectiveness was demonstrated in previous studies by Hadi and Arfiadi (1998), Miguel et al. (2016) and Islam et al. (2018). Secondly, the Warburton method is a simplified analytical procedure and thus the semi-active vibration control in this study can be eased. The explanation
Louggest montioning the following studios	<ul> <li>above has been included in the second paragraph in Section 2.2 and is marked in red.</li> <li>The authors thank the reviewer for their recommendation. Machine learning provides a more effective analytical method for the optimal design of TMD parameters. The authors will strongly consider using the method proposed by Yucel et al. (2019), which has been cited in the fifth paragraph of Section 5.4.</li> </ul>
I suggest mentioning the following studies. Yucel, M., Bekdaş, G., Nigdeli, S. M., & Sevgen, S. (2019). Estimation of optimum tuned mass damper parameters via machine	The authors thank the reviewer for recommending studies on the optimal design of TMD. We have cited all the studies suggested in the fourth and fifth paragraphs of Section 5.4.
learning. Journal of Building Engineering, 26,	A discussion on the optimal design of TMD has
100847.	been included in the fifth paragraph and is marked
Leung, A.Y.T., Zhang, H., 2009, Particle	in red. This reads as follows:
swarm optimization of tuned mass dampers,	"The optimal TMD design method used in this
Engineering structures, 31 (3), 715-728.	study is the Warburton method (Warburton,
Pourzeynali, S., Salimi, S., Kalesar, H. E.,	1982), because this study was conducted on a
2013, Robust multi-objective optimization	laboratory scale. More precise and effective
design of tmd control device to reduce tall	optimal design methods are required by the full-
building responses against earthquake	scale SMA-based tuned mass damper to control
excitations using genetic algorithms, Scientia	large-size structures. Bekdaş and Nigdeli (2011),
iranica, 20 (2), 207-221.	Nigdeli and Bekdas (2013), Bekdaş et al. (2017),

Arfiadi, Y., 2016, Reducing response of structures by using optimum composite tuned mass dampers, Procedia engineering, 161, 67-72.

Farshidianfar, A., Soheili, S. 2013, ABC optimization of tmd parameters for tall buildings with soil structure interaction, Interaction and multiscale mechanics, 6 (4), 339-356.

Bekdaş G, Nigdeli SM, Yang X-S, Metaheuristic Based Optimization for Tuned Mass Dampers Using Frequency Domain Responses. In: Harmony Search Algorithm. Advances in Intelligent Systems and Computing, vol 514, Del Ser J. (eds) Springer, pp. 271-279, 2017.

Bekdaş, G., & Nigdeli, S. M. (2011). Estimating optimum parameters of tuned mass dampers using harmony search. Engineering Structures, 33(9), 2716-2723. Nigdeli, S.M. and Bekdaş, G. (2017), "Optimum tuned mass damper design in frequency domain for structures", KSCE Journal of Civil Engineering, 21(3), 912-922. Nigdeli, S. M., & Bekdas, G. (2014). Optimum tuned mass damper approaches for adjacent structures. Earthquakes and Structures, 7(6), 1071-1091.

Bekdaş G., Nigdeli SM, Yang X-S. A novel bat algorithm based optimum tuning of mass dampers for improving the seismic safety of structures. Engineering Structures 2018; 159: 89-98.

Nigdeli, S. M., & Bekdaş, G. (2019). Optimum design of multiple positioned tuned mass dampers for structures constrained with axial force capacity. The Structural Design of Tall and Special Buildings, e1593.

Bekdaş, G., Kayabekir, A. E., Nigdeli, S. M., & Toklu, Y. C. (2019). Transfer function amplitude minimization for structures with tuned mass dampers considering soilstructure interaction. Soil Dynamics and Earthquake Engineering, 116, 552-562. Nigdeli, S. M., & Bekdas, G. (2013). Optimum tuned mass damper design for preventing brittle fracture of RC buildings. Smart Structures and Systems, 12(2), 137-155. and Nigdeli and Bekdaş (2017) have developed optimal design methods employing the harmony search algorithm. Optimal design methods employing novel algorithms such as Particle swarm optimisation algorithm (Leung and Zhang, 2009) and machine learning algorithm (Yucel et al., 2019) have recently developed and can be incorporated into the SMA-based TMD to increase the tuning efficiency in future research. Structures not only sustain wind loads; they also suffer seismic loads. Therefore, a reduction in seismic vibration should be taken into consideration in the optimal design procedures employed in further studies of SMA-based TMD (Pourzeynali et al., 2013, Farshidianfar and Soheilia, 2013, Nigdeli and Bekdas, 2014, Bekdas et al., 2018, Bekdas et al., 2019)."

We wish to draw the attention of the Editor to the following facts which may be considered as potential conflicts of interest and to significant financial contributions to this work. [OR] We wish to confirm that there are no known conflicts of interest associated with this publication and there has been no significant financial support for this work that could have influenced its outcome.

We confirm that the manuscript has been read and approved by all named authors and that there are no other persons who satisfied the criteria for authorship but are not listed. We further confirm that the order of authors listed in the manuscript has been approved by all of us.

We confirm that we have given due consideration to the protection of intellectual property associated with this work and that there are no impediments to publication, including the timing of publication, with respect to intellectual property. In so doing we confirm that we have followed the regulations of our institutions concerning intellectual property.

We understand that the Corresponding Author is the sole contact for the Editorial process (including Editorial Manager and direct communications with the office). He/she is responsible for communicating with the other authors about progress, submissions of revisions and final approval of proofs. We confirm that we have provided a current, correct email address which is accessible by the Corresponding Author and which has been configured to accept email from w.chang@sheffield.ac.uk

Signed by all authors as follows:

Hange Hercury

Haoyu Huang

Wen-Shao Chang

## **Declaration of interests**

 $\boxtimes$  The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

□The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: