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1 **Vibration Annoyance Assessment of Train Induced Excitations from Tunnels Embedded in**
2 **Rock**

3 Onur Avci¹, Ashish Bhargava², Nikolaos Nikitas³, Daniel J Inman⁴

4
5 ¹ Guest Lecturer, School of Civil Engineering, University of Leeds, Leeds, United Kingdom
6 Email: oavci@vt.edu (Corresponding Author).

7 ² Project Engineer, AECOM USA, Inc., New York City, NY, USA.
8 Email: ashish.bhargava@aecom.com

9 ³ Associate Professor, School of Civil Engineering, University of Leeds, Leeds, United Kingdom
10 Email: n.nikitas@leeds.ac.uk

11 ⁴ Professor, Department of Aerospace Engineering, University of Michigan, Ann Arbor, MI, USA.
12 Email: daninman@umich.edu
13

14 **Abstract**

15 **Train movements generate** oscillations that are transmitted as waves through the track support system into
16 its surroundings. The vibration waves propagate through the soil layers and reach to nearby buildings
17 creating distractions for human activities and causing equipment malfunctioning. Not only the train
18 components and the rails, but also the surrounding tunnel, soil and rock strata have dynamic
19 characteristics that play significant roles in the vibration levels felt in a nearby structure. This paper
20 presents a finite element study conducted to investigate the vibrations resulting from train movements in
21 nearby subway tunnels. The subway line is located at an average horizontal distance of 50 ft (15.2 m)
22 from the structure in assessment, which is a six-story office building. **The main goal of the work is to**
23 **assess the train-induced vibrations at the ground level of the building through a case study and sensitivity**
24 **analysis.** A plane strain finite element model is built to represent the railroad tunnel embedded in the rock
25 and the soil stratum above it. The one train loading function is applied to the model as a point source at
26 the track level and compared to the two-train scenario. Other simulations are undertaken for sensitivity
27 analysis involving increased loading, decreased damping and decreased distance to tunnels. Even though
28 there are several numerical studies on the propagation of train induced vibrations in the literature; a finite
29 element model accompanied with a sensitivity analysis has not been discussed in detail in a technical
30 publication before. The paper not only presents the finite element modeling but also compares the results
31 with the criteria of *Transit Noise and Vibration Impact Assessment Manual*, which was published by the
32 Federal Transit Administration (FTA) of the U.S. Department of Transportation.

33
34 **Keywords:** **Vibrations disturbance**; train vibrations; **ground-borne vibrations**; railroad tunnels; tunnels
35 embedded in rock; ANSYS; finite element modelling
36

37 1. Introduction

38

39 Occupants in buildings are sensitive to vibrations. While most perceptible indoor vibrations are originated
40 from sources within the buildings (human movement, mechanical units, etc.), there are also outdoor
41 sources of vibrations (trains, construction equipment, vehicle traffic, etc.) propagating through the
42 ground, penetrating the building and creating vibratory distractions for building occupants (Sanayei et al.
43 2014; Xia et al. 2010). The vibrations generated due to vehicles on tires are generally observed to be less
44 than the vibrations caused by train excitations. Among the outdoor sources of vibrations, even though
45 construction blasting and pile-driving (Grizi et al. 2016) have been reported to result in damage on
46 buildings, the train vibrations seldom result in building damage. However, there are cases where
47 excessive train vibrations cause extensive distractions to building occupants such as decreasing work
48 focus in office environments during day time and negatively affecting sleep quality during night time. In
49 addition, such vibrations might result in malfunctioning of vibration sensitive equipment. Meanwhile, the
50 train vibrations can be felt by people standing outdoors, however it is seldom that people that are outside
51 complain about outdoor vibrations.

52

53 Train induced noise and vibration have been an area of research over the decades (Degrande and
54 Schillemans 2001; Kephelopoulos et al. 2014; Yang et al. 2019; Zou et al. 2017). Regardless of the train
55 being at the ground level or in a tunnel, ground-borne vibration is a predominant concern for the building
56 occupants especially in the close vicinity of transit system routes (Kouroussis et al. 2016; Licitra et al.
57 2016; Ngamkhanong and Kaewunruen 2018; Peris et al. 2014, 2016). Vibration levels generated by trains
58 are dependent on several factors (Connolly et al. 2016; Lee et al. 2014; Zou et al. 2015). While the
59 material and dynamic properties of the train components, tunnels and surrounding geological conditions
60 are one set of factors (Cai et al. 2010; Galvín and Domínguez 2007; Sheng et al. 2006); wheel
61 smoothness, rail smoothness, vehicle suspension system, track support system are another set (Fiala et al.
62 2007; Metrikine and Vrouwenvelder 2000; Sheng et al. 2004; Triepaischajonsak et al. 2011). For
63 instance, dynamic characteristics of the soil stratum and the depth of the bedrock are important
64 parameters affecting wave propagation (Avillez et al. 2013; Yang and Hsu 2006). While the wave
65 propagation is more effective in stiff clays, when the depth to bedrock is 30ft (9.1 m) or less, it is known
66 that vibration energy is more pronounced near at-grade track. This would most probably result in
67 vibration problems even at large distances from the railway tracks (Bian et al. 2015; Hanson et al. 2018).
68 Also, for the tunnels embedded in rock the train vibrations do not attenuate as rapidly as in soils. It is also
69 observed that the buildings with heavier foundation and superstructure tend to experience relatively
70 smaller vibrations than the lighter structures. The maximum response of the structure will mainly depend

71 on the level of vibrations reaching the building foundations, modal characteristics of the building, and the
72 coupling of the building foundation to the soil (soil-structure interaction).

73
74 As the steel wheels of the trains roll on the rails, vibratory forces are generated. As the wheel meets a
75 discontinuity like a joint, a reactive force is exerted on the wheel and hence on the train. When the
76 vibration of the transit structure generates oscillatory waves propagating away within the soil layers,
77 vibrational energy moves through the surrounding media in a variety of wave forms (shear, compression
78 and Rayleigh waves). The Rayleigh waves carry considerable amount of vibrational energy. In the
79 presence of multi-layered soils, the mathematical modeling of vibration is even more complicated;
80 therefore, FE modeling appears as a reasonable way to model such conditions in a relatively easier and
81 practical way (Andersen and Jones 2006). Yet, vibration propagation from the railways to the structure
82 foundations is complex and requires extensive FE modeling. On a different note, the interaction between
83 the soil and the foundation is significantly important for vibration assessment with FE models (Galvín et
84 al. 2010; Galvín and Domínguez 2009; Hall 2003; Ju and Lin 2004; Yaseri et al. 2014). Once the
85 oscillations propagate through the structure, based on the intensity levels, the vibration can be felt by
86 occupants and/or cause malfunctioning on sensitive equipment. The propagation of oscillations from the
87 foundation to the upper levels of the structure is also complex and has been researched in detail. The
88 propagation within the building depends on the type of the building and the structural design.

89 Since railway induced vibration propagation involves many parameters, it is difficult to estimate the
90 resulting vibrations at a specific location (Park et al. 2008a; b). Therefore, the majority of assessment
91 techniques utilized for transit projects are based on empirical data. For more project specific estimations,
92 where vibration impact is probable, detailed FE models are utilized by researchers and engineers for
93 estimating the vibration levels. While the DVA method typically assumes a steel-wheel/rail system, it is
94 based on frequency domain information typically in terms of one-third octave-band spectrum.

95

96 **2. Vibration analysis levels per the Transit Noise and Vibration Impact Assessment Manual**

97

98 The United States Department of Transportation's Federal Transit Administration (FTA) released an
99 updated version of the Transit Noise and Vibration Impact Assessment Manual (Hanson et al. 2018),
100 which outlines means and methods for prediction and assessment of vibration (and noise) impacts of
101 transit projects as part of FTA's environmental review process. The manual includes clarifications to
102 existing policy and updates to outdated references, where applicable, but does not change the existing
103 assessment procedures of previous versions of the document.

104 In the FTA Transit Noise and Vibration Impact Assessment Manual (Hanson et al. 2018), there are three
105 levels of procedure presented to assess the potential ground-borne vibration impacts resulting from a train
106 line. The appropriate level of analysis is a function of the project specifics such as environmental settings,
107 scale and type of the transit project. According to the FTA manual, there are three levels of analysis:

- 108 • Vibration Screening Procedure (VSP)
- 109 • General Vibration Assessment (GVA)
- 110 • Detailed Vibration Analysis (DVA).

111

112 In order to determine which level of procedure to apply, the primary item to consider is the presence of
113 any vibration sensitive land use through the VSP. This screening procedure determines the work area of
114 any vibration assessment process. **In other words, if there is not any vibration-sensitive equipment present**
115 **within the defined screening distance, then there is no need for further vibration assessment.** When the
116 major project details are known relatively early in the project development stage, the GVA procedure is
117 implemented. The GVA procedure is conducted if there is any potential for considerable vibration levels.
118 For this, vibration levels at receiving locations are determined by predicting the overall vibration velocity
119 level as a function of distance from the rail-tracks. This process also includes adjustments to consider
120 factors like the building type, track and wheel conditions, vehicle speed and track support systems. The
121 GVA is adequate for the environmental review of standard projects where transit modal alternatives are
122 considered for a potential relocation or any other project modification. The GVA is considered adequate
123 when there is a commitment to mitigate vibration impacts, such as a change in transit mode or alignment.
124 **However, if the impact is identified through the GVA procedures and not mitigated, a DVA must be**
125 **conducted.** The DVA is conducted to determine the severity and extent of the impact especially for
126 sensitive buildings, i.e., in the close vicinity of train routes. If needed, vibration mitigation measures
127 would also be implemented after a DVA procedure. **On another note, a DVA may be warranted earlier in**
128 **the environmental review process if there are impact indications regarding the closeness of vibration-**
129 **sensitive structures. This type of assessment task requires experienced professionals to perform tests and**
130 **post-process data.**

131 On another note, a DVA may not be necessary for all segments of a project. Generalized prediction
132 curves from the GVA procedures may be sufficient for most of the alignment, and the DVA procedure
133 may only need to be applied to particularly sensitive receivers. Furthermore, a DVA is typically required
134 for special type of track-support systems (e.g., ballast mats, floating slabs). Costly vibration mitigation
135 techniques can only be called following a DVA in the design stage.

136 The type of work conducted in this paper is a typical example of a DVA procedure where the vibration
137 impact of twin tunnels embedded in rock are researched in detail to make sure that the occupants of an
138 existing nearby six story office building do not get affected by the vibrations generated by the trains
139 passing by. The railway line is an additional line to an existing subway system of a relatively large city
140 located in North America. The proposed alignment of the railway tunnels is passing adjacent to a six story
141 office building and right underneath a six story parking garage. A detailed finite element (FE) model is
142 built and train excitations are simulated to observe the vibration responses at the base of the existing
143 building.

144 The criteria for the DVA and the interpretation of vibration criteria are summarized in Figure 1 and Table
145 1 which are both adapted from the FTA Assessment Manual (Hanson et al. 2018). On Figure 1, the x-axis
146 is one-third octave band center frequency while the y-axis is the vibration velocity level. The DVA
147 criteria of Figure 1 and Table 1 are based on international standards for the effects of vibration on people
148 related to annoyance and interference with activities in buildings (Hanson et al. 2005). The criteria also
149 covers the extensively used standards for vibration-sensitive equipment (Nelson et al. 1982). Specifically,
150 these criteria define limits for acceptable vibration velocity levels with a one-second averaging time at the
151 floor of the building under consideration. For this, the x-axis representation requires to be based on one-
152 third octave band frequency spectrum. For the band levels exceeding a particular criterion curve,
153 mitigation options should be introduced considering the specific range of frequency where the mitigation
154 is expected to be the most efficient. Interpretations of each criterion are defined in Table 1. It must be
155 emphasized that both criteria are on a frequency spectrum since vibration-related problems are dependent
156 on the resonant conditions of the structure and the sensitive equipment. With that, a DVA run is expected
157 to provide an assessment on the criterion limits. The DVA criterion is based on generic cases when people
158 are standing or equipment is mounted on the building floor (Hanson et al. 2018). Therefore, the criterion
159 is less stringent at relatively lower frequencies (less than 8 Hz) as observed in Figure 1. It should be noted
160 that the first bending mode of elevated building floors are almost always less than 8 Hz. For the special
161 case of vibration isolation, the Figure 1 curves may be considered as flat also at lower frequencies.

162
163 For the detailed vibration analysis of this paper, the VC-A category curve is appropriate for the vibration
164 impact criterion of the six story office building. The VC-A curve is defined applicable for healthy
165 functioning of optical balances, microbalances, medium-to high-power optical microscopes (400X) and
166 similar specialized equipment. Therefore, the DVA results of this study are to be compared to this curve.

167
168
169

170 3. Assessment of the office building

171 The building in assessment is the office building right next to the parking garage. The proposed alignment
172 of the new railway tunnels passing adjacent to the six story office building and right underneath the six
173 story parking garage is shown in Figure 2. The train line is an additional line to an existing subway
174 system of a relatively large city located in North America. The closest edge of the building is about 25 ft
175 (7.6 m) away from the East Bound (EB) tunnel horizontally and the farthest horizontal distance from the
176 building to the tunnel is about 90 ft (27.4 m), as shown in Figure 3.

177 The office building has a pile foundation system where the piles are bearing on bedrock at 70 ft (21.3 m)
178 below the ground level. It has been reported in the literature that the piles tend to attenuate the motion at
179 the base of the superstructure as shown in seismic problems (Anoyatis et al. 2013; Di Laora and de
180 Sanctis 2013). The tunnel is located within the bedrock at about 97 ft (29.6 m) below the ground. Figure 4
181 shows the geologic profile in the vicinity of the building in assessment.

182 The main goal of the project is to assess the vibrations that are be transmitted from the rail tracks and the
183 tunnel walls, through the bedrock and soil layers, then to the piles and the ground level. The approach
184 adapted for the assessment is to build a FE model to assess the vibrations generated from the trains in the
185 twin tunnels. The primary assumption in the modeling is to use a plane strain approach and treat the train
186 loading as a harmonic line source.

187 Many problems in elasticity have been treated satisfactorily by the two-dimensional plane theory. In plane
188 strain approach, the out of plane strain is assumed to be zero and the plane strain model is applicable for
189 the cases where the strain state of a point has non-zero components lying in one plane only. As will be
190 discussed in the next section, the plane strain approach is efficient since the simulations are run in a single
191 plane and the plane strain refers to the type of element used to discretize the soil domain.

192

193 4. Finite element model

194 A multi-purpose FE software, ANSYS (ANSYS 2009) is used for the study. Train vibrations and wave
195 propagation have been effectively analyzed and studied with FE models in similar studies (Guo et al.
196 2018; Wang et al. 2005). For the vibration nuisance assessment presented in this paper, the major features
197 of the FE model are shown in Figure 5. The ground surface vibrations at the foundation level of the
198 building are analyzed in the FE model (the elevated floors of the building are not modeled). The soil fill
199 extends to a depth of 70 ft (21.3 m) and the tunnels are located in the rock layer where the top of tunnel is
200 located at 97 ft (29.6 m) from the ground surface. A plane strain FE model is built to represent the soil

201 and the rock layers. The foundation slabs of the office building are not included in the FE model. The
202 piles however, are included in the model as discrete beam elements extending from the ground surface
203 down to the bed rock. For the 2D model, it is assumed that the next row of piles is far away to affect the
204 results at this 2D section. The foundation slab and the piles of the parking garage are not included in the
205 model.

206 In the FE model, the boundaries are placed far away from the excitation source to avoid corner/ 3D
207 effects (Figure 5). Also, absorbing boundary conditions based on Lysmer dampers (Lysmer and
208 Kuhlemeyer 1969) are placed on the model boundaries to avoid reflections. These boundaries have been
209 used by various researchers in FE models for eliminating the waves reflecting from the boundaries (Bao
210 et al. 2012; Mott and Wang 2011; Nielsen 2006; Shen and Giurgiutiu 2015; Volpini et al. 2019; Zhang
211 and Tang 2007).

212 Rayleigh damping model is used in the ANSYS model for the analysis, in which the damping ratio is
213 frequency dependent (Figure 6). Since the frequency range of 2 Hz - 30 Hz was observed to be more
214 critical than higher frequencies in this study, to be conservative in the FE model analysis, smaller
215 damping values are chosen for this critical range of frequency. The smaller damping ratios would result in
216 higher vibration levels, which is basically being on the safe side for an assessment study like this. It can
217 also be argued that reducing the damping ratio compensates for the linearity in the surrounding soil. As
218 such, based on the frequency dependent characteristics of the Rayleigh damping model, the damping ratio
219 varied from 3% to 5% for the 2 Hz - 30 Hz range. For higher frequencies, the damping is higher than 5%
220 based on the curve trend shown in Figure 6. On a related note, linear material properties are used for the
221 analysis. For the soil, the elastic properties are based on shear wave velocity of about 400 ft/s (122 m/s).
222 For the rock, a shear wave velocity of about 13000 ft/s (3963 m/s) is used (Table 2).

223 The train loading is introduced as a harmonic line source in the FE model. Properties of Flexity Swift
224 M5000 LRV train car are used for the analysis; elevations and plan view of which are shown in Figure 7.
225 The empty train car weight is about 80,000 lbs (36,288 kg) and the car length is about 95 ft (29 m).
226 Assuming a total of 100 people with an average weight of about 150 lb (68 kg), the total load is about
227 95000 lbs (43,091 kg). The load is spread over the train length of 95 ft (29 m), i.e., a uniform load of
228 about 1kip/ft (14.6 kN/m). The load is distributed on the two rail tracks and each track has a load of about
229 0.5 kip/ft (7.3 kN/m). Based on this, the source of vibration is a line harmonic source with frequency
230 varying from 0 to 200 Hz and amplitude of 0.5 kip/ft (7.3 kN/m) for each rail track. One train loading
231 condition assumes that there is a train only in the East Bound (EB) tunnel and two train loading condition
232 assumes trains in both EB and WB tunnels at the same time.

233 As mentioned earlier, a plane strain FE model is used for the vibration assessment work in this paper. The
 234 plane strain model is applicable for the cases where the strain state of a point has non-zero components
 235 lying in one plane only (Boresi et al. 1993). This approach of using a plane strain model with harmonic
 236 line load to assess ground vibration due to underground tunnels is consistent with the work by Yang et al.
 237 (Yang et al. 2007). The ANSYS simulations run in a single plane and the plane strain refers to the type of
 238 element used to discretize the soil domain. As such, based on the standard 2-D plane strain assumption,
 239 the strains in the direction normal to the plane of Figure 5 are considered to be zero. In two-dimensional
 240 elasticity, the governing partial differential equations for the plane stress model incorporating body forces
 241 and inertia forces can be written as (Przemieniecki, J. 1968; Sokolnikoff 1956):

$$G \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) + \frac{G(1+\nu)}{(1-\nu)} \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + X = \rho \frac{\partial^2 u}{\partial t^2} \quad (1)$$

$$G \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) + \frac{G(1+\nu)}{(1-\nu)} \frac{\partial}{\partial y} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + Y = \rho \frac{\partial^2 v}{\partial t^2} \quad (2)$$

$$G = \frac{E}{2(1+\nu)} \quad (3)$$

242 Where,

243 ρ = density of the material

244 X, Y = body forces in x and y directions respectively, per unit volume

245 E = modulus of elasticity

246 ν = Poisson's ratio

247 G = shear modulus

248 Similarly, the governing partial differential equations for the plane strain model incorporating body forces
 249 and inertia forces can be simplified as:

$$G \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) + \frac{G}{(1-2\nu)} \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + X = \rho \frac{\partial^2 u}{\partial t^2} \quad (4)$$

$$G \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) + \frac{G}{(1-2\nu)} \frac{\partial}{\partial y} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + Y = \rho \frac{\partial^2 v}{\partial t^2} \quad (5)$$

250 **4.1 Generalized Loading**

251 From pure analytical approach, the loading function created by a train can be presented as a moving
 252 harmonic load with frequency, f_0 . As shown by Yang et al. (Yang and Hung 2008), for the train travelling

253 with speed c on the z -axis with the coordinate origin at the train railway contact point, the loading
 254 function is:

$$f(x, y, z, t) = \psi(x, y)\phi(z - ct)e^{-i2\pi f_0 t} \quad (6)$$

255 On the x - y plane, the influence function of moving loads is written as:

$$\psi(x, y) = \delta(x)\delta(y) \quad (7)$$

256 Where;

257 $\phi(z)$ = load distribution function for the train travelling on the z -axis.

258 $\delta(x)$ = influence function component of the moving load in x -direction

259 $\delta(y)$ = influence function component of the moving load in y -direction

260 $\psi(x, y)$ = the influence function of the moving loads on the tunnel cross sectional plane (x - y
 261 plane)

262 f_0 = moving load excitation frequency

263 c = train speed

264 The external loading in time domain $f(x, y, z, t)$ is represented as the component summation of a series of
 265 harmonic loads (Yang and Hung 2008):

$$f(x, y, z, t) = \int_{-\infty}^{\infty} \frac{1}{c} \delta(x)\delta(y)\tilde{\phi}(-k)e^{-ikz}e^{-i\omega t}d\omega \quad (8)$$

266 Where;

267 $\tilde{\phi}(k)$ = Fourier transform of the function $\phi(z)$

$$k = (\omega - 2\pi f_0)/c$$

268 The steady-state response in the time domain for a linear system is determined by the superposition of
 269 responses created by the series of harmonic load components. For the location (x', y') assuming the
 270 response created by a harmonic load, $\delta(x)\delta(y)e^{-ikz}e^{-i\omega t}$ is represented as $H(i\omega)$. With that, again in
 271 the time domain, the final response is presented as (Yang et al. 2003; Yang and Hung 2008):

$$d(x', y', z, t) = \int_{-\infty}^{\infty} \frac{1}{c} \tilde{\phi}(-k)H(i\omega)e^{-ikz}e^{-i\omega t}d\omega \quad (9)$$

272 Meanwhile, in the frequency domain, the equation of motion is:

$$([K] - \omega^2[M] + i\omega[C])\{D\} = \{F\} \quad (10)$$

273

274 Where $[K]$ is the global stiffness matrix; $[M]$ is the global mass matrix; $\{D\}$ is the vector of nodal
 275 displacements; and $\{F\}$ is the vector of applied loads. The displacements $\{D\}$ in the frequency domain
 276 become:

$$\{D\} = ([K] - \omega^2[M] + i\omega[C])^{-1}\{F\} \quad (11)$$

277

278 When $\{D\}$ of Eq.(12) is inserted for representing the function $H(i\omega)$, a time domain response can be
 279 achieved (Yang and Hung 2008).

280

281 However, the various unknowns regarding the design of the train tunnels and the surrounding media are
 282 only a few of many set of factors making the use of Equations (9-10) unreasonable at instances. The
 283 tunnels mentioned in this paper are still in the design stage which means the material and geometrical
 284 properties are always subject to change. In addition, due to the complex dynamic interaction among the
 285 subgrades, train car, bogie, wheelset, rail-pads, rails, ballast, sleepers and unevenness in the soil layers,
 286 Equations (9-10) acquire a further degree of uncertainty, hence cannot be used with full confidence. On
 287 top of all this, the modal properties like stiffness and inherent damping are also unknown with potential
 288 nonlinearity (Avci 2016, 2017).

289

290 **4.2 Adapted Loading Function**

291 The uncertainties in the complex response function $H(i\omega)$; the oscillation of train car suspension system;
 292 unevenness of the rails; the complicated interaction between the rails and wheels; geometric and material
 293 irregularities of the soil layers and radiation damping phenomenon are other important factors resulting in
 294 a need to create a FE model to determine the vibrations at the surface. A detailed FE model would result
 295 in vibration levels to be compared to the FTA criterion. For the FE analysis, a model is developed in
 296 ANSYS. The train load is simplified to a sinusoidal excitation:

297 $P\sin(\omega t)$ = harmonic force function generated by the train pass

298 P = harmonic force amplitude

299 ω = frequency range 0-200 Hz

300

301 Vibration velocity level in decibels is formulated as:

$$L_{vel} = 20 \log \left(\frac{vel}{vel_{ref}} \right) \quad (12)$$

302 where:

303 L_{vel} = velocity level, VdB

304 vel = RMS velocity amplitude

305 $vel_{ref} = 10^{-6}$ in/sec in the USA

306 $= 10^{-8}$ m/sec internationally

307
308 Since the reference quantities vary in the literature (Hanson et al. 2018), it is crucial to report the
309 reference quantity when specifying velocity levels. In this paper, all the vibration levels are referenced to
310 1×10^{-6} inches/second. A sinusoidal excitation is applied at the tunnel location of the 2D model, and the
311 response at the bottom of the building at 50 ft (15.2 m) horizontal distance from the train excitation
312 location is calculated. The ANSYS run is based on the sinusoidal excitations being applied with the
313 harmonic sweep (sine sweep) function which cycles through a range of frequencies in a single run. The
314 results are post-processed at specific frequency values. These specific frequencies at which results are
315 extracted are based on the FTA manual criteria (One-Third Octave Band Frequency). The peak responses
316 at the critical frequencies are automatically recorded and printed out at each of the corresponding
317 frequencies. The results of the harmonic sweep analysis are discussed in the following section.

318

319 **5. Analysis results and sensitivity analysis**

320 The surface vibrations at a horizontal distance of about 50 ft (15.2 m) from the tunnel are shown in Figure
321 8. The Federal Transit Authority (FTA) VC-A criterion is also plotted in the figure. The vibrations from
322 the railway tunnel peak in the frequency ranges of 8 Hz to 12 Hz and 20 Hz to 30 Hz. In these ranges the
323 peak RMS VdB for the one train loading condition is about 60 VdB and for the two train loading
324 condition is about 64 VdB. These peaks are lower than the VC-A criteria therefore no adverse impact is
325 expected on the building.

326 When there is uncertainty in the output of a task, the input items (independent variables) of the same task
327 can be sub-grouped and/or assigned to various sources of uncertainty within reasonable boundaries. This
328 is the simplistic description of the sensitivity analysis which is also used in the context of this paper. The
329 harmonic loading of the one-train condition, damping ratios and the horizontal distance from the
330 harmonic load to the tunnel are the sensitivity analysis items focused on within this study. While
331 increasing the loading, decreasing the damping ratio and decreasing the distance to harmonic loads are all
332 independent inputs, they would all result in an increased vibration response at the building foundations.
333 This makes the analyses conservative which serves the purpose of the sensitivity analyses.

334 In order to assess the sensitivity of the results three additional sets of analyses are conducted with the
335 following variations from the above baseline model:

- 336 1. One train loading condition with 20% load amplitude increase.
- 337 2. Lower the damping ratio from 3% - 5% range (see Figure 6) to 1% - 2% range.

338 3. Decrease the horizontal distance from the loading to the building from 50 ft (15.2 m) to 25 ft (7.6
339 m).

340 The analysis result for one train condition with 20% load amplitude increase is shown in Figure 9. For
341 20% increase in the load the VdB values are found to increase by about 1.6 VdB. Therefore, for the most
342 critical frequency of one train condition, the peak increases from 60 VdB to about 61.6 VdB (an increase
343 of 2.7%), still remaining below the FTA VC-A limit (66 VdB).

344 Considering the frequency dependency of the damping ratios in Rayleigh damping model (Figure 6), the
345 second run to check for the sensitivity analysis was conducted by using lower damping ratios than the
346 original range of 3% to 5% in the FE model runs. The damping ratios were lowered to 1% to 2% in the
347 critical frequency range of 2 Hz - 30 Hz considering the fact that lower damping ratios would result in
348 higher vibration peaks. In other words, lowering the damping ratios makes the analysis more
349 conservative, hence complying with the sensitivity analysis. With that, the analysis result for one train
350 condition with lower damping is shown in Figure 10. For lower damping, VdB values are found to
351 increase by about 1.6 VdB. Therefore for one train condition, the peak increases from 60 VdB to about
352 61.6 VdB (an increase of 2.7%), staying below the VC-A criteria limit of FTA (66 VdB).

353 For the third sensitivity analysis, the horizontal distance from the load to the building is decreased from
354 50 ft (15.2 m) to 25 ft (7.6 m). The analysis results are shown in Figure 11. The results show that for
355 relatively low frequencies (less than 50 Hz) the ground surface vibrations are not sensitive to the tunnel
356 location, at least for the two locations compared against each other. For regions closer to the tunnel, the
357 higher frequency (greater than 50 Hz) vibrations are not attenuated, and consequently at higher
358 frequencies the vibration levels are higher as shown in the figure. For 25 ft (7.6 m) distance, at the most
359 critical frequency value of 25 Hz, the vibrations are found to increase by about 1.0 VdB. The peak
360 increases from 60 VdB to about 61 VdB (an increase of 1.7%), staying below the VC-A criteria limit of
361 FTA (66 VdB).

362

363 **6. Other components of nuisance**

364 **6.1 Vibration nuisance in the existing building**

365 Floor vibrations are unwanted in a building since the oscillations irritate the occupants and cause
366 discomfort. In the last couple of decades, slender structural members and modern construction
367 technologies have resulted in more vulnerable floor systems against vibrations (Avci 2015; Bhargava et
368 al. 2013; Muhammad et al. 2018; Younis et al. 2017). As such, the vibration serviceability of the floors

369 has become a standard design parameter that needs to be checked by the designers to ensure human
370 comfort on building floors (Avei 2005). The vibrations on building floors can be caused not only by
371 human activities such as walking, running, dancing, and aerobics; but also by the train traffic nearby the
372 building (Alabbasi et al. 2019).

373
374 There are several methods for the assessment of floor vibrations serviceability, ranging from probabilistic
375 methods to simplified methods (Abdeljaber et al. 2018, 2019). There are four well established floor
376 vibration evaluation methods extensively used over the world. These are the American Institute of Steel
377 Construction (AISC) Design Guide 11 Chapter 4 method (Murray et al. 2016); Steel Construction
378 Institute (SCI) P354 Simplified Method (Smith et al. 2009); Steel Construction Institute (SCI) P354
379 Vibration Dose Values Method (Smith et al. 2009); and Human Induced Vibration of Steel Structures
380 (HIVOSS) Method (RFCS 2009). While all of these methods are very useful for human-induced
381 excitations, none of them are covering the vibrations serviceability and human comfort levels due to train-
382 induced excitations.

383
384 Transmission of train vibrations from the ground into the building and propagation within the building
385 towards the upper floors have been researched by various researchers. It has been reported that
386 developing a methodology to predict vibration levels at the upper floors based on the vibrations at the
387 foundation level is not very straightforward (Sanayei et al. 2014). For human response to vibrations, the
388 FTA Assessment Manual (Hanson et al. 2018) recommends an attenuation of -2 dB per floor for the first
389 five stories of the building; and a -1 dB per floor for the next five stories of the building (floor five to
390 floor ten). However, there is also an amplification component due to the resonances of walls, floors and
391 ceilings which may potentially increase the vibration levels +6 db for light-weight and timber-frame
392 structures. Since the existing building of this study is a steel-framed building, this amplification is not
393 applicable (summarized in Table 3).

394
395 Moreover, for the detailed vibration analysis of this paper, the VC-A category curve of the FTA
396 Assessment Manual is used for the vibration impact criterion of the six story office building which is
397 applicable for healthy functioning of optical balances, microbalances, medium-to high-power optical
398 microscopes (400X) and similar specialized equipment. This criterion is compared with the ground
399 surface vibrations (at the foundation level of the building) with the results of detailed FE model
400 investigation and the accompanying sensitivity analysis. As discussed earlier, the peak RMS VdB for the
401 one train loading condition is about 60 VdB and for the two train loading condition is about 64 VdB.
402 Similarly, as the one train loading amplitude is increased 20%, the RMS peak was found to be 61.6 VdB;

403 and with lower damping ratio, the RMS peak was found to be 61.6 VdB. Even with the decreased
404 distance to the train line, the RMS peak was at 61 VdB. While all these peak values are below the 66 VdB
405 limit of the VC-A criteria, they are all calculated at the foundation level of the existing building which is
406 fairly conservative. This conservatism is due to the fact that the vibrations will attenuate as the waves are
407 propagating upwards within the building. The FTS suggested attenuation of -2 dB per floor for the first
408 five stories of the building; and a -1 dB per floor for the next five stories of the building would further
409 decrease the already acceptable RMS VdB peaks. As a result of this, no adverse impact is expected for
410 occupants located on the elevated floors of the existing building.

411
412 On another note, there are simplified impedance-based analytical models available in the literature for
413 train-induced vibration predictions (Sanayei et al. 2011). In these models, the vibrations propagate
414 through the axial waves in the columns of the building. The impedance of columns and slabs representing
415 the stiffness, mass and damping properties are the predominant components of the model where each
416 finite portion of the column is modeled according to the impedances at the top and bottom of each
417 column. With that, the displacements and forces at the ends of the columns are represented in the dynamic
418 stiffness matrices.

419

420 **6.2 Noise nuisance**

421 Like vibration, noise may also cause annoyance to building occupants. Not only trains but also other
422 transit sources create noise in various levels based on the type of the transit and operating conditions.
423 Between the source and the receiver, the level of noise can be attenuated along the path depending on the
424 obstacles in the way, ground type, damping components and several other factors. Generally, the noise
425 metrics are expressed in terms of “A-Weighted Decibels” (dBA) which is the basic noise unit in transit
426 noise terminology. Also known as “A-Weighted Sound Level”, this term represents the overall noise at a
427 receiver location that is adjusted in frequency to approximate typical human hearing sensitivity. The letter
428 "A" indicates that the sound has been filtered to reduce the strength of very low and very high-frequency
429 content to represent the human response to sound levels (Hanson et al. 2018).

430

431 In transit noise impact assessment, another important parameter is the “Sound Exposure Level” (SEL).
432 This term is defined as the cumulative noise exposure from a single noise event, normalized to one
433 second. The louder events have a larger SEL value than the quieter events. Similarly, the shorter events
434 have a smaller SEL value than the longer events. Basically, the SEL value represents the identical overall

435 sound energy as the actual varying sound energy during the single noise event. Being a primary metric for
436 the measurement of transit vehicle noise emissions, it is also an “A-Weighted” cumulative measure.

437
438 In transit noise terminology, another common term is the “Maximum Sound Level” (L_{max}) which is also
439 known as the “Maximum Noise Level”. This measure represents the maximum level of sound generated
440 during a single noise event, and it is considered as “A-Weighted Maximum Noise Level” in various
441 references. This metric is predominantly used in vehicle noise specifications and typically calculated for
442 individual vehicles.

443
444 The equation for computing L_{max} for a single locomotive pass-by per FTA Assessment Manual (Hanson
445 et al. 2018) is:

$$L_{max} = SEL_{ref} - 10\log\left(\frac{L_{meas}}{50}\right) - 10\log\left(\frac{D_{meas}}{50}\right) + 10\log(2\alpha) - C_{consist} - C_{emissions} - 3.3 \quad (13)$$

446 Where;

447 SEL_{ref} = Source Reference Level (Reference SEL)

448 L_{meas} = total length of measured group of locomotives or rail cars (ft)

449 D_{meas} = closest distance between measurement position and source (ft)

450 $\alpha = \arctan\left(\frac{L_{meas}}{2D_{meas}}\right)$ in radians

451 $C_{consist} = -10\log(N_{cars})$ for locomotives and rail cars where N_{cars} is the number of locomotives in the
452 measured group

453 $C_{emissions} = 0$ for $T < 6$ for locomotives

454 $C_{emissions} = -2(T - 5)$ for $T \geq 6$ for locomotives where T is average throttle setting of the locomotives.

455 While the sound nuisance of the train excitations was not intended to be discussed in this manuscript, the
456 train noise calculations are briefly shown here for the sake of completeness. The train-induced noise
457 calculations were also not run nor discussed as the presented FE model was used only to investigate the
458 vibrations resulting from the train movements, at the foundation level of the existing building.

459 7. Conclusions

460 In this paper, ground surface vibrations are investigated due to trains passing through proposed
461 underground tunnels in the vicinity of an office building. A 2D finite element model is created reflecting

462 the railroad tunnels embedded in the rock and the soil stratum above it. Also, a train loading function is
463 applied to the model as a point source at the track level. Various simulations are undertaken followed by a
464 sensitivity analysis. Taking the plane strain assumption within the finite element model simulations, the
465 vibrations from the railway tunnel were determined to have peaks in the frequency ranges of 8 Hz to 12
466 Hz and 20 Hz to 30 Hz. In these ranges the peak RMS VdB for one train loading condition is about 60
467 VdB and for two train loading condition the peak RMS is about 64 VdB. Meanwhile, for the sensitivity
468 analyses, when the one train loading amplitude is increased 20%, the RMS peak was found to be 61.6
469 VdB. On another run, when lower damping values are used, the RMS peak was found to be 61.6 VdB.
470 For the last sensitivity analysis run, the distance from the building to the loading is decreased to 25 ft (7.6
471 m) which resulted in an RMS peak of 61 VdB. The results are compared to the criteria of Transit Noise
472 and Vibration Impact Assessment Manual, which was published by Federal Transit Administration (FTA)
473 of the U.S. Department of Transportation. Since all of the peaks are observed to be lower than the FTA
474 VC-A criteria (66 VdB); no adverse impact is expected on the building.

475 The predominant limitations of the study presented in this paper could be listed as the use of 2D analysis
476 and material linearity. While a 2D model is relatively easier to build and processed faster, a 3D model
477 would have allowed a more realistic modeling of the harmonic force function and would have produced
478 more information on wave propagation. Yet, a 3D model would also have the same material and
479 geometrical unknowns as a 2D model for the tunnels, surrounding media, and complex dynamic
480 interaction among the train car and wheel components. In addition, while the material and dynamic
481 properties of the structural members and the soil layers are known to be non-linear in reality, the model
482 used in the study assumes a linear behavior.

483
484

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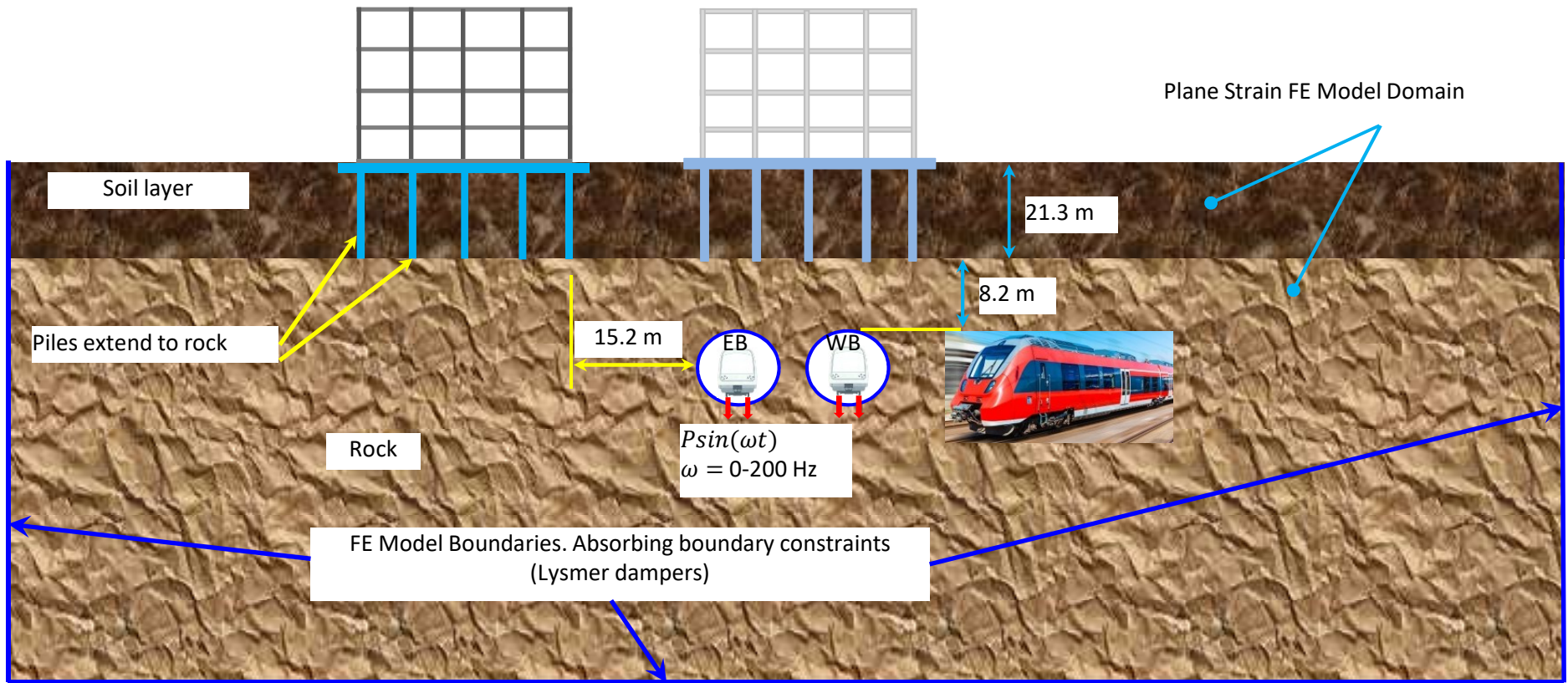
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640



Vibration Annoyance Assessment of Train Induced Excitations from Tunnels Embedded in Rock

Onur Avci¹, Ashish Bhargava², Nikolaos Nikitas³, Daniel J Inman⁴

¹ Guest Lecturer, School of Civil Engineering, University of Leeds, Leeds, United Kingdom
Email: oavci@vt.edu (Corresponding Author).

² Project Engineer, AECOM USA, Inc., New York City, NY, USA.
Email: ashish.bhargava@aecom.com

³ Associate Professor, School of Civil Engineering, University of Leeds, Leeds, United Kingdom
Email: n.nikitas@leeds.ac.uk

⁴ Professor, Department of Aerospace Engineering, University of Michigan, Ann Arbor, MI, USA.
Email: daninman@umich.edu

Highlights

- This paper presents a study conducted to assess vibrations of trains to nearby buildings through a case study.
- A plane strain finite element model is built for the railroad tunnel and the surrounding media.
- Various simulations are undertaken for sensitivity analysis.
- The results are compared to the *Transit Noise and Vibration Impact Assessment Manual*.
- All peaks are found to be lower than the criteria, no adverse impact is expected.

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2 **Rock**

3 Onur Avci¹, Ashish Bhargava², Nikolaos Nikitas³, Daniel J Inman⁴

4
5 ¹ Guest Lecturer, School of Civil Engineering, University of Leeds, Leeds, United Kingdom
6 Email: oavci@vt.edu (Corresponding Author).

7 ² Project Engineer, AECOM USA, Inc., New York City, NY, USA.
8 Email: ashish.bhargava@aecom.com

9 ³ Associate Professor, School of Civil Engineering, University of Leeds, Leeds, United Kingdom
10 Email: n.nikitas@leeds.ac.uk

11 ⁴ Professor, Department of Aerospace Engineering, University of Michigan, Ann Arbor, MI, USA.
12 Email: daninman@umich.edu

13

14 **Abstract**

15 Train movements generate oscillations that are transmitted as waves through the track support system into
16 its surroundings. The vibration waves propagate through the soil layers and reach to nearby buildings
17 creating distractions for human activities and causing equipment malfunctioning. Not only the train
18 components and the rails, but also the surrounding tunnel, soil and rock strata have dynamic
19 characteristics that play significant roles in the vibration levels felt in a nearby structure. This paper
20 presents a finite element study conducted to investigate the vibrations resulting from train movements in
21 nearby subway tunnels. The subway line is located at an average horizontal distance of 50 ft (15.2 m)
22 from the structure in assessment, which is a six-story office building. The main goal of the work is to
23 assess the train-induced vibrations at the ground level of the building through a case study and sensitivity
24 analysis. A plane strain finite element model is built to represent the railroad tunnel embedded in the rock
25 and the soil stratum above it. The one train loading function is applied to the model as a point source at
26 the track level and compared to the two-train scenario. Other simulations are undertaken for sensitivity
27 analysis involving increased loading, decreased damping and decreased distance to tunnels. Even though
28 there are several numerical studies on the propagation of train induced vibrations in the literature; a finite
29 element model accompanied with a sensitivity analysis has not been discussed in detail in a technical
30 publication before. The paper not only presents the finite element modeling but also compares the results
31 with the criteria of *Transit Noise and Vibration Impact Assessment Manual*, which was published by the
32 Federal Transit Administration (FTA) of the U.S. Department of Transportation.

33

34 **Keywords:** Vibrations disturbance; train vibrations; ground-borne vibrations; railroad tunnels; tunnels
35 embedded in rock; ANSYS; finite element modelling

36

37 **1. Introduction**

38

39 Occupants in buildings are sensitive to vibrations. While most perceptible indoor vibrations are originated
40 from sources within the buildings (human movement, mechanical units, etc.), there are also outdoor
41 sources of vibrations (trains, construction equipment, vehicle traffic, etc.) propagating through the
42 ground, penetrating the building and creating vibratory distractions for building occupants (Sanayei et al.
43 2014; Xia et al. 2010). The vibrations generated due to vehicles on tires are generally observed to be less
44 than the vibrations caused by train excitations. Among the outdoor sources of vibrations, even though
45 construction blasting and pile-driving (Grizi et al. 2016) have been reported to result in damage on
46 buildings, the train vibrations seldom result in building damage. However, there are cases where
47 excessive train vibrations cause extensive distractions to building occupants such as decreasing work
48 focus in office environments during day time and negatively affecting sleep quality during night time. In
49 addition, such vibrations might result in malfunctioning of vibration sensitive equipment. Meanwhile, the
50 train vibrations can be felt by people standing outdoors, however it is seldom that people that are outside
51 complain about outdoor vibrations.

52

53 Train induced noise and vibration have been an area of research over the decades (Degrande and
54 Schillemans 2001; Kephelopoulos et al. 2014; Yang et al. 2019; Zou et al. 2017). Regardless of the train
55 being at the ground level or in a tunnel, ground-borne vibration is a predominant concern for the building
56 occupants especially in the close vicinity of transit system routes (Kouroussis et al. 2016; Licitra et al.
57 2016; Ngamkhanong and Kaewunruen 2018; Peris et al. 2014, 2016). Vibration levels generated by trains
58 are dependent on several factors (Connolly et al. 2016; Lee et al. 2014; Zou et al. 2015). While the
59 material and dynamic properties of the train components, tunnels and surrounding geological conditions
60 are one set of factors (Cai et al. 2010; Galvín and Domínguez 2007; Sheng et al. 2006); wheel
61 smoothness, rail smoothness, vehicle suspension system, track support system are another set (Fiala et al.
62 2007; Metrikine and Vrouwenvelder 2000; Sheng et al. 2004; Triepaischajonsak et al. 2011). For
63 instance, dynamic characteristics of the soil stratum and the depth of the bedrock are important
64 parameters affecting wave propagation (Avillez et al. 2013; Yang and Hsu 2006). While the wave
65 propagation is more effective in stiff clays, when the depth to bedrock is 30ft (9.1 m) or less, it is known
66 that vibration energy is more pronounced near at-grade track. This would most probably result in
67 vibration problems even at large distances from the railway tracks (Bian et al. 2015; Hanson et al. 2018).
68 Also, for the tunnels embedded in rock the train vibrations do not attenuate as rapidly as in soils. It is also
69 observed that the buildings with heavier foundation and superstructure tend to experience relatively
70 smaller vibrations than the lighter structures. The maximum response of the structure will mainly depend

71 on the level of vibrations reaching the building foundations, modal characteristics of the building, and the
72 coupling of the building foundation to the soil (soil-structure interaction).

73

74 As the steel wheels of the trains roll on the rails, vibratory forces are generated. As the wheel meets a
75 discontinuity like a joint, a reactive force is exerted on the wheel and hence on the train. When the
76 vibration of the transit structure generates oscillatory waves propagating away within the soil layers,
77 vibrational energy moves through the surrounding media in a variety of wave forms (shear, compression
78 and Rayleigh waves). The Rayleigh waves carry considerable amount of vibrational energy. In the
79 presence of multi-layered soils, the mathematical modeling of vibration is even more complicated;
80 therefore, FE modeling appears as a reasonable way to model such conditions in a relatively easier and
81 practical way (Andersen and Jones 2006). Yet, vibration propagation from the railways to the structure
82 foundations is complex and requires extensive FE modeling. On a different note, the interaction between
83 the soil and the foundation is significantly important for vibration assessment with FE models (Galvín et
84 al. 2010; Galvín and Domínguez 2009; Hall 2003; Ju and Lin 2004; Yaseri et al. 2014). Once the
85 oscillations propagate through the structure, based on the intensity levels, the vibration can be felt by
86 occupants and/or cause malfunctioning on sensitive equipment. The propagation of oscillations from the
87 foundation to the upper levels of the structure is also complex and has been researched in detail. The
88 propagation within the building depends on the type of the building and the structural design.

89 Since railway induced vibration propagation involves many parameters, it is difficult to estimate the
90 resulting vibrations at a specific location (Park et al. 2008a; b). Therefore, the majority of assessment
91 techniques utilized for transit projects are based on empirical data. For more project specific estimations,
92 where vibration impact is probable, detailed FE models are utilized by researchers and engineers for
93 estimating the vibration levels. While the DVA method typically assumes a steel-wheel/rail system, it is
94 based on frequency domain information typically in terms of one-third octave-band spectrum.

95

96 **2. Vibration analysis levels per the Transit Noise and Vibration Impact Assessment Manual**

97

98 The United States Department of Transportation's Federal Transit Administration (FTA) released an
99 updated version of the Transit Noise and Vibration Impact Assessment Manual (Hanson et al. 2018),
100 which outlines means and methods for prediction and assessment of vibration (and noise) impacts of
101 transit projects as part of FTA's environmental review process. The manual includes clarifications to
102 existing policy and updates to outdated references, where applicable, but does not change the existing
103 assessment procedures of previous versions of the document.

104 In the FTA Transit Noise and Vibration Impact Assessment Manual (Hanson et al. 2018), there are three
105 levels of procedure presented to assess the potential ground-borne vibration impacts resulting from a train
106 line. The appropriate level of analysis is a function of the project specifics such as environmental settings,
107 scale and type of the transit project. According to the FTA manual, there are three levels of analysis:

- 108 • Vibration Screening Procedure (VSP)
- 109 • General Vibration Assessment (GVA)
- 110 • Detailed Vibration Analysis (DVA).

111

112 In order to determine which level of procedure to apply, the primary item to consider is the presence of
113 any vibration sensitive land use through the VSP. This screening procedure determines the work area of
114 any vibration assessment process. In other words, if there is not any vibration-sensitive equipment present
115 within the defined screening distance, then there is no need for further vibration assessment. When the
116 major project details are known relatively early in the project development stage, the GVA procedure is
117 implemented. The GVA procedure is conducted if there is any potential for considerable vibration levels.
118 For this, vibration levels at receiving locations are determined by predicting the overall vibration velocity
119 level as a function of distance from the rail-tracks. This process also includes adjustments to consider
120 factors like the building type, track and wheel conditions, vehicle speed and track support systems. The
121 GVA is adequate for the environmental review of standard projects where transit modal alternatives are
122 considered for a potential relocation or any other project modification. The GVA is considered adequate
123 when there is a commitment to mitigate vibration impacts, such as a change in transit mode or alignment.
124 However, if the impact is identified through the GVA procedures and not mitigated, a DVA must be
125 conducted. The DVA is conducted to determine the severity and extent of the impact especially for
126 sensitive buildings, i.e., in the close vicinity of train routes. If needed, vibration mitigation measures
127 would also be implemented after a DVA procedure. On another note, a DVA may be warranted earlier in
128 the environmental review process if there are impact indications regarding the closeness of vibration-
129 sensitive structures. This type of assessment task requires experienced professionals to perform tests and
130 post-process data.

131 On another note, a DVA may not be necessary for all segments of a project. Generalized prediction
132 curves from the GVA procedures may be sufficient for most of the alignment, and the DVA procedure
133 may only need to be applied to particularly sensitive receivers. Furthermore, a DVA is typically required
134 for special type of track-support systems (e.g., ballast mats, floating slabs). Costly vibration mitigation
135 techniques can only be called following a DVA in the design stage.

136 The type of work conducted in this paper is a typical example of a DVA procedure where the vibration
137 impact of twin tunnels embedded in rock are researched in detail to make sure that the occupants of an
138 existing nearby six story office building do not get affected by the vibrations generated by the trains
139 passing by. The railway line is an additional line to an existing subway system of a relatively large city
140 located in North America. The proposed alignment of the railway tunnels is passing adjacent to a six story
141 office building and right underneath a six story parking garage. A detailed finite element (FE) model is
142 built and train excitations are simulated to observe the vibration responses at the base of the existing
143 building.

144 The criteria for the DVA and the interpretation of vibration criteria are summarized in Figure 1 and Table
145 1 which are both adapted from the FTA Assessment Manual (Hanson et al. 2018). On Figure 1, the x-axis
146 is one-third octave band center frequency while the y-axis is the vibration velocity level. The DVA
147 criteria of Figure 1 and Table 1 are based on international standards for the effects of vibration on people
148 related to annoyance and interference with activities in buildings (Hanson et al. 2005). The criteria also
149 covers the extensively used standards for vibration-sensitive equipment (Nelson et al. 1982). Specifically,
150 these criteria define limits for acceptable vibration velocity levels with a one-second averaging time at the
151 floor of the building under consideration. For this, the x-axis representation requires to be based on one-
152 third octave band frequency spectrum. For the band levels exceeding a particular criterion curve,
153 mitigation options should be introduced considering the specific range of frequency where the mitigation
154 is expected to be the most efficient. Interpretations of each criterion are defined in Table 1. It must be
155 emphasized that both criteria are on a frequency spectrum since vibration-related problems are dependent
156 on the resonant conditions of the structure and the sensitive equipment. With that, a DVA run is expected
157 to provide an assessment on the criterion limits. The DVA criterion is based on generic cases when people
158 are standing or equipment is mounted on the building floor (Hanson et al. 2018). Therefore, the criterion
159 is less stringent at relatively lower frequencies (less than 8 Hz) as observed in Figure 1. It should be noted
160 that the first bending mode of elevated building floors are almost always less than 8 Hz. For the special
161 case of vibration isolation, the Figure 1 curves may be considered as flat also at lower frequencies.

162
163 For the detailed vibration analysis of this paper, the VC-A category curve is appropriate for the vibration
164 impact criterion of the six story office building. The VC-A curve is defined applicable for healthy
165 functioning of optical balances, microbalances, medium-to high-power optical microscopes (400X) and
166 similar specialized equipment. Therefore, the DVA results of this study are to be compared to this curve.

167
168
169

170 **3. Assessment of the office building**

171 The building in assessment is the office building right next to the parking garage. The proposed alignment
172 of the new railway tunnels passing adjacent to the six story office building and right underneath the six
173 story parking garage is shown in Figure 2. The train line is an additional line to an existing subway
174 system of a relatively large city located in North America. The closest edge of the building is about 25 ft
175 (7.6 m) away from the East Bound (EB) tunnel horizontally and the farthest horizontal distance from the
176 building to the tunnel is about 90 ft (27.4 m), as shown in Figure 3.

177 The office building has a pile foundation system where the piles are bearing on bedrock at 70 ft (21.3 m)
178 below the ground level. It has been reported in the literature that the piles tend to attenuate the motion at
179 the base of the superstructure as shown in seismic problems (Anoyatis et al. 2013; Di Laora and de
180 Sanctis 2013). The tunnel is located within the bedrock at about 97 ft (29.6 m) below the ground. Figure 4
181 shows the geologic profile in the vicinity of the building in assessment.

182 The main goal of the project is to assess the vibrations that are be transmitted from the rail tracks and the
183 tunnel walls, through the bedrock and soil layers, then to the piles and the ground level. The approach
184 adapted for the assessment is to build a FE model to assess the vibrations generated from the trains in the
185 twin tunnels. The primary assumption in the modeling is to use a plane strain approach and treat the train
186 loading as a harmonic line source.

187 Many problems in elasticity have been treated satisfactorily by the two-dimensional plane theory. In plane
188 strain approach, the out of plane strain is assumed to be zero and the plane strain model is applicable for
189 the cases where the strain state of a point has non-zero components lying in one plane only. As will be
190 discussed in the next section, the plane strain approach is efficient since the simulations are run in a single
191 plane and the plane strain refers to the type of element used to discretize the soil domain.

192

193 **4. Finite element model**

194 A multi-purpose FE software, ANSYS (ANSYS 2009) is used for the study. Train vibrations and wave
195 propagation have been effectively analyzed and studied with FE models in similar studies (Guo et al.
196 2018; Wang et al. 2005). For the vibration nuisance assessment presented in this paper, the major features
197 of the FE model are shown in Figure 5. The ground surface vibrations at the foundation level of the
198 building are analyzed in the FE model (the elevated floors of the building are not modeled). The soil fill
199 extends to a depth of 70 ft (21.3 m) and the tunnels are located in the rock layer where the top of tunnel is
200 located at 97 ft (29.6 m) from the ground surface. A plane strain FE model is built to represent the soil

201 and the rock layers. The foundation slabs of the office building are not included in the FE model. The
202 piles however, are included in the model as discrete beam elements extending from the ground surface
203 down to the bed rock. For the 2D model, it is assumed that the next row of piles is far away to affect the
204 results at this 2D section. The foundation slab and the piles of the parking garage are not included in the
205 model.

206 In the FE model, the boundaries are placed far away from the excitation source to avoid corner/ 3D
207 effects (Figure 5). Also, absorbing boundary conditions based on Lysmer dampers (Lysmer and
208 Kuhlemeyer 1969) are placed on the model boundaries to avoid reflections. These boundaries have been
209 used by various researchers in FE models for eliminating the waves reflecting from the boundaries (Bao
210 et al. 2012; Mott and Wang 2011; Nielsen 2006; Shen and Giurgiutiu 2015; Volpini et al. 2019; Zhang
211 and Tang 2007).

212 Rayleigh damping model is used in the ANSYS model for the analysis, in which the damping ratio is
213 frequency dependent (Figure 6). Since the frequency range of 2 Hz - 30 Hz was observed to be more
214 critical than higher frequencies in this study, to be conservative in the FE model analysis, smaller
215 damping values are chosen for this critical range of frequency. The smaller damping ratios would result in
216 higher vibration levels, which is basically being on the safe side for an assessment study like this. It can
217 also be argued that reducing the damping ratio compensates for the linearity in the surrounding soil. As
218 such, based on the frequency dependent characteristics of the Rayleigh damping model, the damping ratio
219 varied from 3% to 5% for the 2 Hz - 30 Hz range. For higher frequencies, the damping is higher than 5%
220 based on the curve trend shown in Figure 6. On a related note, linear material properties are used for the
221 analysis. For the soil, the elastic properties are based on shear wave velocity of about 400 ft/s (122 m/s).
222 For the rock, a shear wave velocity of about 13000 ft/s (3963 m/s) is used (Table 2).

223 The train loading is introduced as a harmonic line source in the FE model. Properties of Flexity Swift
224 M5000 LRV train car are used for the analysis; elevations and plan view of which are shown in Figure 7.
225 The empty train car weight is about 80,000 lbs (36,288 kg) and the car length is about 95 ft (29 m).
226 Assuming a total of 100 people with an average weight of about 150 lb (68 kg), the total load is about
227 95000 lbs (43,091 kg). The load is spread over the train length of 95 ft (29 m), i.e., a uniform load of
228 about 1kip/ft (14.6 kN/m). The load is distributed on the two rail tracks and each track has a load of about
229 0.5 kip/ft (7.3 kN/m). Based on this, the source of vibration is a line harmonic source with frequency
230 varying from 0 to 200 Hz and amplitude of 0.5 kip/ft (7.3 kN/m) for each rail track. One train loading
231 condition assumes that there is a train only in the East Bound (EB) tunnel and two train loading condition
232 assumes trains in both EB and WB tunnels at the same time.

233 As mentioned earlier, a plane strain FE model is used for the vibration assessment work in this paper. The
 234 plane strain model is applicable for the cases where the strain state of a point has non-zero components
 235 lying in one plane only (Boresi et al. 1993). This approach of using a plane strain model with harmonic
 236 line load to assess ground vibration due to underground tunnels is consistent with the work by Yang et al.
 237 (Yang et al. 2007). The ANSYS simulations run in a single plane and the plane strain refers to the type of
 238 element used to discretize the soil domain. As such, based on the standard 2-D plane strain assumption,
 239 the strains in the direction normal to the plane of Figure 5 are considered to be zero. In two-dimensional
 240 elasticity, the governing partial differential equations for the plane stress model incorporating body forces
 241 and inertia forces can be written as (Przemieniecki, J. 1968; Sokolnikoff 1956):

$$G \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) + \frac{G(1+\nu)}{(1-\nu)} \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + X = \rho \frac{\partial^2 u}{\partial t^2} \quad (1)$$

$$G \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) + \frac{G(1+\nu)}{(1-\nu)} \frac{\partial}{\partial y} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + Y = \rho \frac{\partial^2 v}{\partial t^2} \quad (2)$$

$$G = \frac{E}{2(1+\nu)} \quad (3)$$

242 Where,

243 ρ = density of the material

244 X, Y = body forces in x and y directions respectively, per unit volume

245 E = modulus of elasticity

246 ν = Poisson's ratio

247 G = shear modulus

248 Similarly, the governing partial differential equations for the plane strain model incorporating body forces
 249 and inertia forces can be simplified as:

$$G \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) + \frac{G}{(1-2\nu)} \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + X = \rho \frac{\partial^2 u}{\partial t^2} \quad (4)$$

$$G \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) + \frac{G}{(1-2\nu)} \frac{\partial}{\partial y} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + Y = \rho \frac{\partial^2 v}{\partial t^2} \quad (5)$$

250 4.1 Generalized Loading

251 From pure analytical approach, the loading function created by a train can be presented as a moving
 252 harmonic load with frequency, f_0 . As shown by Yang et al. (Yang and Hung 2008), for the train travelling

253 with speed c on the z -axis with the coordinate origin at the train railway contact point, the loading
 254 function is:

$$f(x, y, z, t) = \psi(x, y)\phi(z - ct)e^{-i2\pi f_0 t} \quad (6)$$

255 On the x - y plane, the influence function of moving loads is written as:

$$\psi(x, y) = \delta(x)\delta(y) \quad (7)$$

256 Where;

257 $\phi(z)$ = load distribution function for the train travelling on the z -axis.

258 $\delta(x)$ = influence function component of the moving load in x -direction

259 $\delta(y)$ = influence function component of the moving load in y -direction

260 $\psi(x, y)$ = the influence function of the moving loads on the tunnel cross sectional plane (x - y
 261 plane)

262 f_0 = moving load excitation frequency

263 c = train speed

264 The external loading in time domain $f(x, y, z, t)$ is represented as the component summation of a series of
 265 harmonic loads (Yang and Hung 2008):

$$f(x, y, z, t) = \int_{-\infty}^{\infty} \frac{1}{c} \delta(x)\delta(y)\tilde{\phi}(-k)e^{-ikz}e^{-i\omega t}d\omega \quad (8)$$

266 Where;

267 $\tilde{\phi}(k)$ = Fourier transform of the function $\phi(z)$

$$k = (\omega - 2\pi f_0)/c$$

268 The steady-state response in the time domain for a linear system is determined by the superposition of
 269 responses created by the series of harmonic load components. For the location (x', y') assuming the
 270 response created by a harmonic load, $\delta(x)\delta(y)e^{-ikz}e^{-i\omega t}$ is represented as $H(i\omega)$. With that, again in
 271 the time domain, the final response is presented as (Yang et al. 2003; Yang and Hung 2008):

$$d(x', y', z, t) = \int_{-\infty}^{\infty} \frac{1}{c} \tilde{\phi}(-k)H(i\omega)e^{-ikz}e^{-i\omega t}d\omega \quad (9)$$

272 Meanwhile, in the frequency domain, the equation of motion is:

$$([K] - \omega^2[M] + i\omega[C])\{D\} = \{F\} \quad (10)$$

273

274 Where $[K]$ is the global stiffness matrix; $[M]$ is the global mass matrix; $\{D\}$ is the vector of nodal
 275 displacements; and $\{F\}$ is the vector of applied loads. The displacements $\{D\}$ in the frequency domain
 276 become:

$$\{D\} = ([K] - \omega^2[M] + i\omega[C])^{-1}\{F\} \quad (11)$$

277

278 When $\{D\}$ of Eq.(12) is inserted for representing the function $H(i\omega)$, a time domain response can be
 279 achieved (Yang and Hung 2008).

280

281 However, the various unknowns regarding the design of the train tunnels and the surrounding media are
 282 only a few of many set of factors making the use of Equations (9-10) unreasonable at instances. The
 283 tunnels mentioned in this paper are still in the design stage which means the material and geometrical
 284 properties are always subject to change. In addition, due to the complex dynamic interaction among the
 285 subgrades, train car, bogie, wheelset, rail-pads, rails, ballast, sleepers and unevenness in the soil layers,
 286 Equations (9-10) acquire a further degree of uncertainty, hence cannot be used with full confidence. On
 287 top of all this, the modal properties like stiffness and inherent damping are also unknown with potential
 288 nonlinearity (Avci 2016, 2017).

289

290 **4.2 Adapted Loading Function**

291 The uncertainties in the complex response function $H(i\omega)$; the oscillation of train car suspension system;
 292 unevenness of the rails; the complicated interaction between the rails and wheels; geometric and material
 293 irregularities of the soil layers and radiation damping phenomenon are other important factors resulting in
 294 a need to create a FE model to determine the vibrations at the surface. A detailed FE model would result
 295 in vibration levels to be compared to the FTA criterion. For the FE analysis, a model is developed in
 296 ANSYS. The train load is simplified to a sinusoidal excitation:

297 $P\sin(\omega t)$ = harmonic force function generated by the train pass

298 P = harmonic force amplitude

299 ω = frequency range 0-200 Hz

300

301 Vibration velocity level in decibels is formulated as:

$$L_{vel} = 20 \log \left(\frac{vel}{vel_{ref}} \right) \quad (12)$$

302 where:

303 L_{vel} = velocity level, VdB

304 vel = RMS velocity amplitude

305 $vel_{ref} = 10^{-6}$ in/sec in the USA

306 $= 10^{-8}$ m/sec internationally

307

308 Since the reference quantities vary in the literature (Hanson et al. 2018), it is crucial to report the
309 reference quantity when specifying velocity levels. In this paper, all the vibration levels are referenced to
310 1×10^{-6} inches/second. A sinusoidal excitation is applied at the tunnel location of the 2D model, and the
311 response at the bottom of the building at 50 ft (15.2 m) horizontal distance from the train excitation
312 location is calculated. The ANSYS run is based on the sinusoidal excitations being applied with the
313 harmonic sweep (sine sweep) function which cycles through a range of frequencies in a single run. The
314 results are post-processed at specific frequency values. These specific frequencies at which results are
315 extracted are based on the FTA manual criteria (One-Third Octave Band Frequency). The peak responses
316 at the critical frequencies are automatically recorded and printed out at each of the corresponding
317 frequencies. The results of the harmonic sweep analysis are discussed in the following section.

318

319 **5. Analysis results and sensitivity analysis**

320 The surface vibrations at a horizontal distance of about 50 ft (15.2 m) from the tunnel are shown in Figure
321 8. The Federal Transit Authority (FTA) VC-A criterion is also plotted in the figure. The vibrations from
322 the railway tunnel peak in the frequency ranges of 8 Hz to 12 Hz and 20 Hz to 30 Hz. In these ranges the
323 peak RMS VdB for the one train loading condition is about 60 VdB and for the two train loading
324 condition is about 64 VdB. These peaks are lower than the VC-A criteria therefore no adverse impact is
325 expected on the building.

326 When there is uncertainty in the output of a task, the input items (independent variables) of the same task
327 can be sub-grouped and/or assigned to various sources of uncertainty within reasonable boundaries. This
328 is the simplistic description of the sensitivity analysis which is also used in the context of this paper. The
329 harmonic loading of the one-train condition, damping ratios and the horizontal distance from the
330 harmonic load to the tunnel are the sensitivity analysis items focused on within this study. While
331 increasing the loading, decreasing the damping ratio and decreasing the distance to harmonic loads are all
332 independent inputs, they would all result in an increased vibration response at the building foundations.
333 This makes the analyses conservative which serves the purpose of the sensitivity analyses.

334 In order to assess the sensitivity of the results three additional sets of analyses are conducted with the
335 following variations from the above baseline model:

- 336 1. One train loading condition with 20% load amplitude increase.
- 337 2. Lower the damping ratio from 3% - 5% range (see Figure 6) to 1% - 2% range.

338 3. Decrease the horizontal distance from the loading to the building from 50 ft (15.2 m) to 25 ft (7.6
339 m).

340 The analysis result for one train condition with 20% load amplitude increase is shown in Figure 9. For
341 20% increase in the load the VdB values are found to increase by about 1.6 VdB. Therefore, for the most
342 critical frequency of one train condition, the peak increases from 60 VdB to about 61.6 VdB (an increase
343 of 2.7%), still remaining below the FTA VC-A limit (66 VdB).

344 Considering the frequency dependency of the damping ratios in Rayleigh damping model (Figure 6), the
345 second run to check for the sensitivity analysis was conducted by using lower damping ratios than the
346 original range of 3% to 5% in the FE model runs. The damping ratios were lowered to 1% to 2% in the
347 critical frequency range of 2 Hz - 30 Hz considering the fact that lower damping ratios would result in
348 higher vibration peaks. In other words, lowering the damping ratios makes the analysis more
349 conservative, hence complying with the sensitivity analysis. With that, the analysis result for one train
350 condition with lower damping is shown in Figure 10. For lower damping, VdB values are found to
351 increase by about 1.6 VdB. Therefore for one train condition, the peak increases from 60 VdB to about
352 61.6 VdB (an increase of 2.7%), staying below the VC-A criteria limit of FTA (66 VdB).

353 For the third sensitivity analysis, the horizontal distance from the load to the building is decreased from
354 50 ft (15.2 m) to 25 ft (7.6 m). The analysis results are shown in Figure 11. The results show that for
355 relatively low frequencies (less than 50 Hz) the ground surface vibrations are not sensitive to the tunnel
356 location, at least for the two locations compared against each other. For regions closer to the tunnel, the
357 higher frequency (greater than 50 Hz) vibrations are not attenuated, and consequently at higher
358 frequencies the vibration levels are higher as shown in the figure. For 25 ft (7.6 m) distance, at the most
359 critical frequency value of 25 Hz, the vibrations are found to increase by about 1.0 VdB. The peak
360 increases from 60 VdB to about 61 VdB (an increase of 1.7%), staying below the VC-A criteria limit of
361 FTA (66 VdB).

362

363 **6. Other components of nuisance**

364 **6.1 Vibration nuisance in the existing building**

365 Floor vibrations are unwanted in a building since the oscillations irritate the occupants and cause
366 discomfort. In the last couple of decades, slender structural members and modern construction
367 technologies have resulted in more vulnerable floor systems against vibrations (Avci 2015; Bhargava et
368 al. 2013; Muhammad et al. 2018; Younis et al. 2017). As such, the vibration serviceability of the floors

369 has become a standard design parameter that needs to be checked by the designers to ensure human
370 comfort on building floors (Avei 2005). The vibrations on building floors can be caused not only by
371 human activities such as walking, running, dancing, and aerobics; but also by the train traffic nearby the
372 building (Alabbasi et al. 2019).

373
374 There are several methods for the assessment of floor vibrations serviceability, ranging from probabilistic
375 methods to simplified methods (Abdeljaber et al. 2018, 2019). There are four well established floor
376 vibration evaluation methods extensively used over the world. These are the American Institute of Steel
377 Construction (AISC) Design Guide 11 Chapter 4 method (Murray et al. 2016); Steel Construction
378 Institute (SCI) P354 Simplified Method (Smith et al. 2009); Steel Construction Institute (SCI) P354
379 Vibration Dose Values Method (Smith et al. 2009); and Human Induced Vibration of Steel Structures
380 (HIVOSS) Method (RFCS 2009). While all of these methods are very useful for human-induced
381 excitations, none of them are covering the vibrations serviceability and human comfort levels due to train-
382 induced excitations.

383
384 Transmission of train vibrations from the ground into the building and propagation within the building
385 towards the upper floors have been researched by various researchers. It has been reported that
386 developing a methodology to predict vibration levels at the upper floors based on the vibrations at the
387 foundation level is not very straightforward (Sanayei et al. 2014). For human response to vibrations, the
388 FTA Assessment Manual (Hanson et al. 2018) recommends an attenuation of -2 dB per floor for the first
389 five stories of the building; and a -1 dB per floor for the next five stories of the building (floor five to
390 floor ten). However, there is also an amplification component due to the resonances of walls, floors and
391 ceilings which may potentially increase the vibration levels +6 db for light-weight and timber-frame
392 structures. Since the existing building of this study is a steel-framed building, this amplification is not
393 applicable (summarized in Table 3).

394
395 Moreover, for the detailed vibration analysis of this paper, the VC-A category curve of the FTA
396 Assessment Manual is used for the vibration impact criterion of the six story office building which is
397 applicable for healthy functioning of optical balances, microbalances, medium-to high-power optical
398 microscopes (400X) and similar specialized equipment. This criterion is compared with the ground
399 surface vibrations (at the foundation level of the building) with the results of detailed FE model
400 investigation and the accompanying sensitivity analysis. As discussed earlier, the peak RMS VdB for the
401 one train loading condition is about 60 VdB and for the two train loading condition is about 64 VdB.
402 Similarly, as the one train loading amplitude is increased 20%, the RMS peak was found to be 61.6 VdB;

403 and with lower damping ratio, the RMS peak was found to be 61.6 VdB. Even with the decreased
404 distance to the train line, the RMS peak was at 61 VdB. While all these peak values are below the 66 VdB
405 limit of the VC-A criteria, they are all calculated at the foundation level of the existing building which is
406 fairly conservative. This conservatism is due to the fact that the vibrations will attenuate as the waves are
407 propagating upwards within the building. The FTS suggested attenuation of -2 dB per floor for the first
408 five stories of the building; and a -1 dB per floor for the next five stories of the building would further
409 decrease the already acceptable RMS VdB peaks. As a result of this, no adverse impact is expected for
410 occupants located on the elevated floors of the existing building.

411
412 On another note, there are simplified impedance-based analytical models available in the literature for
413 train-induced vibration predictions (Sanayei et al. 2011). In these models, the vibrations propagate
414 through the axial waves in the columns of the building. The impedance of columns and slabs representing
415 the stiffness, mass and damping properties are the predominant components of the model where each
416 finite portion of the column is modeled according to the impedances at the top and bottom of each
417 column. With that, the displacements and forces at the ends of the columns are represented in the dynamic
418 stiffness matrices.

419

420 **6.2 Noise nuisance**

421 Like vibration, noise may also cause annoyance to building occupants. Not only trains but also other
422 transit sources create noise in various levels based on the type of the transit and operating conditions.
423 Between the source and the receiver, the level of noise can be attenuated along the path depending on the
424 obstacles in the way, ground type, damping components and several other factors. Generally, the noise
425 metrics are expressed in terms of “A-Weighted Decibels” (dBA) which is the basic noise unit in transit
426 noise terminology. Also known as “A-Weighted Sound Level”, this term represents the overall noise at a
427 receiver location that is adjusted in frequency to approximate typical human hearing sensitivity. The letter
428 "A" indicates that the sound has been filtered to reduce the strength of very low and very high-frequency
429 content to represent the human response to sound levels (Hanson et al. 2018).

430

431 In transit noise impact assessment, another important parameter is the “Sound Exposure Level” (SEL).
432 This term is defined as the cumulative noise exposure from a single noise event, normalized to one
433 second. The louder events have a larger SEL value than the quieter events. Similarly, the shorter events
434 have a smaller SEL value than the longer events. Basically, the SEL value represents the identical overall

435 sound energy as the actual varying sound energy during the single noise event. Being a primary metric for
436 the measurement of transit vehicle noise emissions, it is also an “A-Weighted” cumulative measure.

437
438 In transit noise terminology, another common term is the “Maximum Sound Level” (L_{max}) which is also
439 known as the “Maximum Noise Level”. This measure represents the maximum level of sound generated
440 during a single noise event, and it is considered as “A-Weighted Maximum Noise Level” in various
441 references. This metric is predominantly used in vehicle noise specifications and typically calculated for
442 individual vehicles.

443
444 The equation for computing L_{max} for a single locomotive pass-by per FTA Assessment Manual (Hanson
445 et al. 2018) is:

$$L_{max} = SEL_{ref} - 10\log\left(\frac{L_{meas}}{50}\right) - 10\log\left(\frac{D_{meas}}{50}\right) + 10\log(2\alpha) - C_{consist} - C_{emissions} - 3.3 \quad (13)$$

446 Where;

447 SEL_{ref} = Source Reference Level (Reference SEL)

448 L_{meas} = total length of measured group of locomotives or rail cars (ft)

449 D_{meas} = closest distance between measurement position and source (ft)

450 $\alpha = \arctan\left(\frac{L_{meas}}{2D_{meas}}\right)$ in radians

451 $C_{consist} = -10\log(N_{cars})$ for locomotives and rail cars where N_{cars} is the number of locomotives in the
452 measured group

453 $C_{emissions} = 0$ for $T < 6$ for locomotives

454 $C_{emissions} = -2(T - 5)$ for $T \geq 6$ for locomotives where T is average throttle setting of the locomotives.

455 While the sound nuisance of the train excitations was not intended to be discussed in this manuscript, the
456 train noise calculations are briefly shown here for the sake of completeness. The train-induced noise
457 calculations were also not run nor discussed as the presented FE model was used only to investigate the
458 vibrations resulting from the train movements, at the foundation level of the existing building.

459 **7. Conclusions**

460 In this paper, ground surface vibrations are investigated due to trains passing through proposed
461 underground tunnels in the vicinity of an office building. A 2D finite element model is created reflecting

462 the railroad tunnels embedded in the rock and the soil stratum above it. Also, a train loading function is
463 applied to the model as a point source at the track level. Various simulations are undertaken followed by a
464 sensitivity analysis. Taking the plane strain assumption within the finite element model simulations, the
465 vibrations from the railway tunnel were determined to have peaks in the frequency ranges of 8 Hz to 12
466 Hz and 20 Hz to 30 Hz. In these ranges the peak RMS VdB for one train loading condition is about 60
467 VdB and for two train loading condition the peak RMS is about 64 VdB. Meanwhile, for the sensitivity
468 analyses, when the one train loading amplitude is increased 20%, the RMS peak was found to be 61.6
469 VdB. On another run, when lower damping values are used, the RMS peak was found to be 61.6 VdB.
470 For the last sensitivity analysis run, the distance from the building to the loading is decreased to 25 ft (7.6
471 m) which resulted in an RMS peak of 61 VdB. The results are compared to the criteria of Transit Noise
472 and Vibration Impact Assessment Manual, which was published by Federal Transit Administration (FTA)
473 of the U.S. Department of Transportation. Since all of the peaks are observed to be lower than the FTA
474 VC-A criteria (66 VdB); no adverse impact is expected on the building.

475 The predominant limitations of the study presented in this paper could be listed as the use of 2D analysis
476 and material linearity. While a 2D model is relatively easier to build and processed faster, a 3D model
477 would have allowed a more realistic modeling of the harmonic force function and would have produced
478 more information on wave propagation. Yet, a 3D model would also have the same material and
479 geometrical unknowns as a 2D model for the tunnels, surrounding media, and complex dynamic
480 interaction among the train car and wheel components. In addition, while the material and dynamic
481 properties of the structural members and the soil layers are known to be non-linear in reality, the model
482 used in the study assumes a linear behavior.

483

484

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- 640

Table 1 - Interpretation of Vibration Criteria for Detailed Vibration Analysis (adapted from Table 6-6 of the FTA Assessment Manual)

Criterion Curve	Max Lv, VdB	Description
Workshop (ISO)	90	Vibration that is distinctly felt. Appropriate for workshops and similar areas not as sensitive to vibration.
Office (ISO)	84	Vibration that can be felt. Appropriate for offices and similar areas not as sensitive to vibration.
Residential Day (ISO)	78	Vibration that is barely felt. Adequate for computer equipment and low-power optical microscopes (up to 20X).
Residential Night, Operating Rooms (ISO)	72	Vibration is not felt, but ground-borne noise may be audible inside quiet rooms. Suitable for medium-power optical microscopes (100X) and other equipment of low sensitivity.
VC-A	66	Adequate for medium-to high-power optical microscopes (400X), microbalances, optical balances, and similar specialized equipment.
VC-B	60	Adequate for high-power optical microscopes (1000X) and inspection and lithography equipment to 3-micron line widths.
VC-C	54	Appropriate for most lithography and inspection equipment to 1-micron detail size.
VC-D	48	Suitable in most instances for the most demanding equipment, including electron microscopes operating to the limits of their capabilities.
VC-E	42	The most demanding criterion for extremely vibration-sensitive equipment.

Table 2[Click here to download Table: Table 2.docx](#)

Table 2 – Shear wave velocities used in the FE model

Material	Property	Symbol	US Customary units	SI units
Soil	Shear Wave Velocity	V_s	400 ft/s	122 m/s
Rock	Shear Wave Velocity	V_s	13,000 ft/s	3963 m/s

Table 3[Click here to download Table: Table 3.docx](#)

Table 3 – Receiver Adjustment Factors for Ground Borne Vibration Propagation (adapted from Table 6-13 of the FTA Assessment Manual)

Receiver Factor	Adjustment to Propagation Curve		Description
Floor to floor attenuation	1 to 5 stories above grade	-2 dB per story	This adjustment is intended to address the dispersion and attenuation of vibration energy as it propagates through a structure with the first starting with elevated floor.
	5 to 10 stories above grade	-1 dB per story	
Amplification due to resonances of floors, walls, and ceilings.	+6 dB		The amplification will depend on the type of the existing structure (wood frame, masonry, reinforced concrete, steel).

List of Figures

Figure 1 – Criteria for detailed vibration analysis (adapted from Figure 6-2 of FTA Assessment Manual)

Figure 2 – Building in assessment (a) North view, (b) South view. (Railway tunnel size and locations not to scale).

Figure 3 – Plan view of building in assessment and the railway tunnels

Figure 4 – Geologic profile in the vicinity of the building in assessment

Figure 5 – Extents of the FE model

Figure 6 – Rayleigh damping model

Figure 7 – Flexity Swift M5000 train car (all dimensions in mm)

Figure 8 - Surface vibrations at 50 ft (15.2 m) from the tunnel

Figure 9 - Surface vibrations at 50 ft (15.2 m) from the tunnel with 20% load increase

Figure 10 - Surface vibrations at 50 ft (15.2 m) from the tunnel with lower damping

Figure 11 - Surface vibrations at 25 ft (7.6 m) from the tunnel

Figure 1

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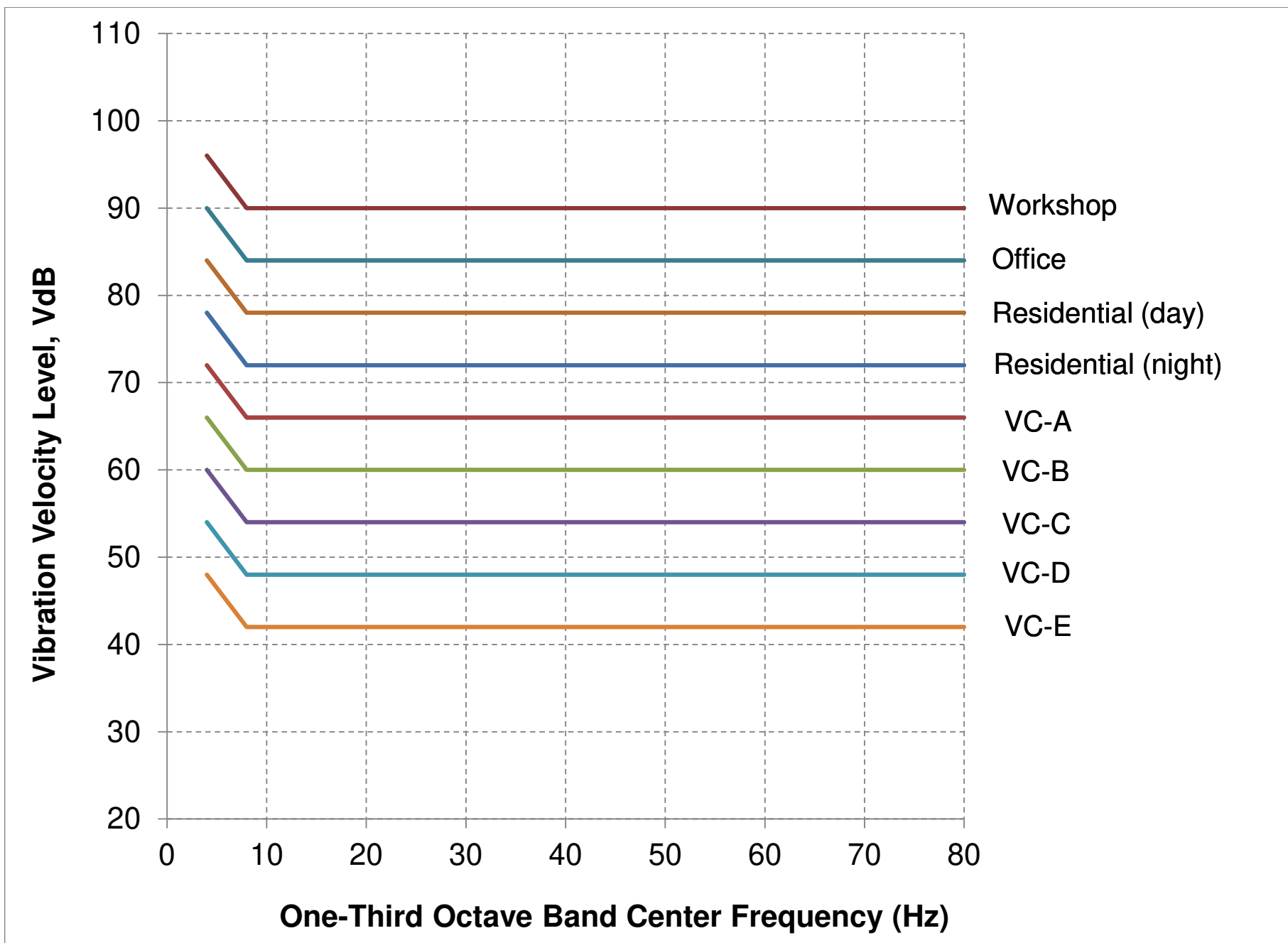


Figure 2a
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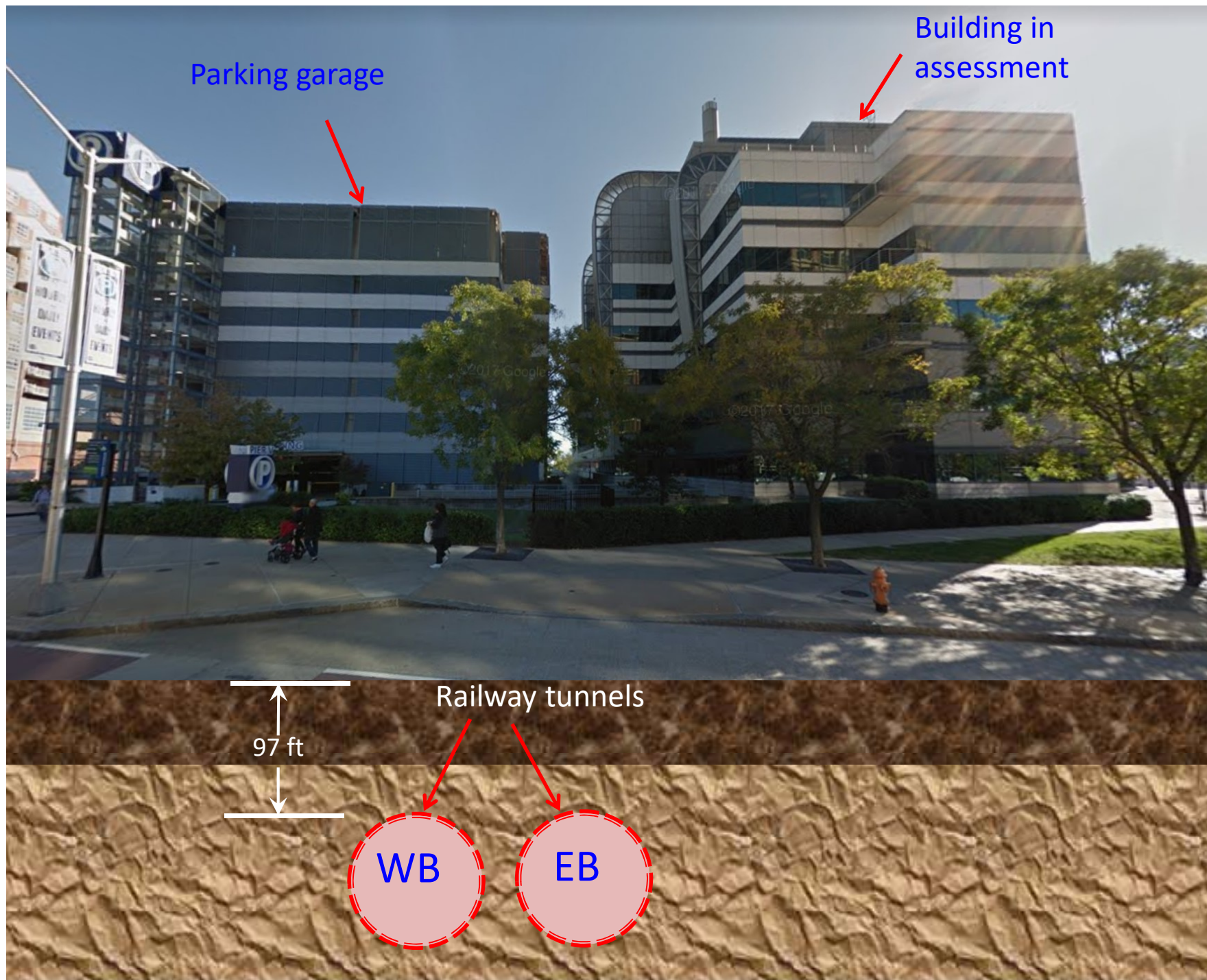


Figure 2b
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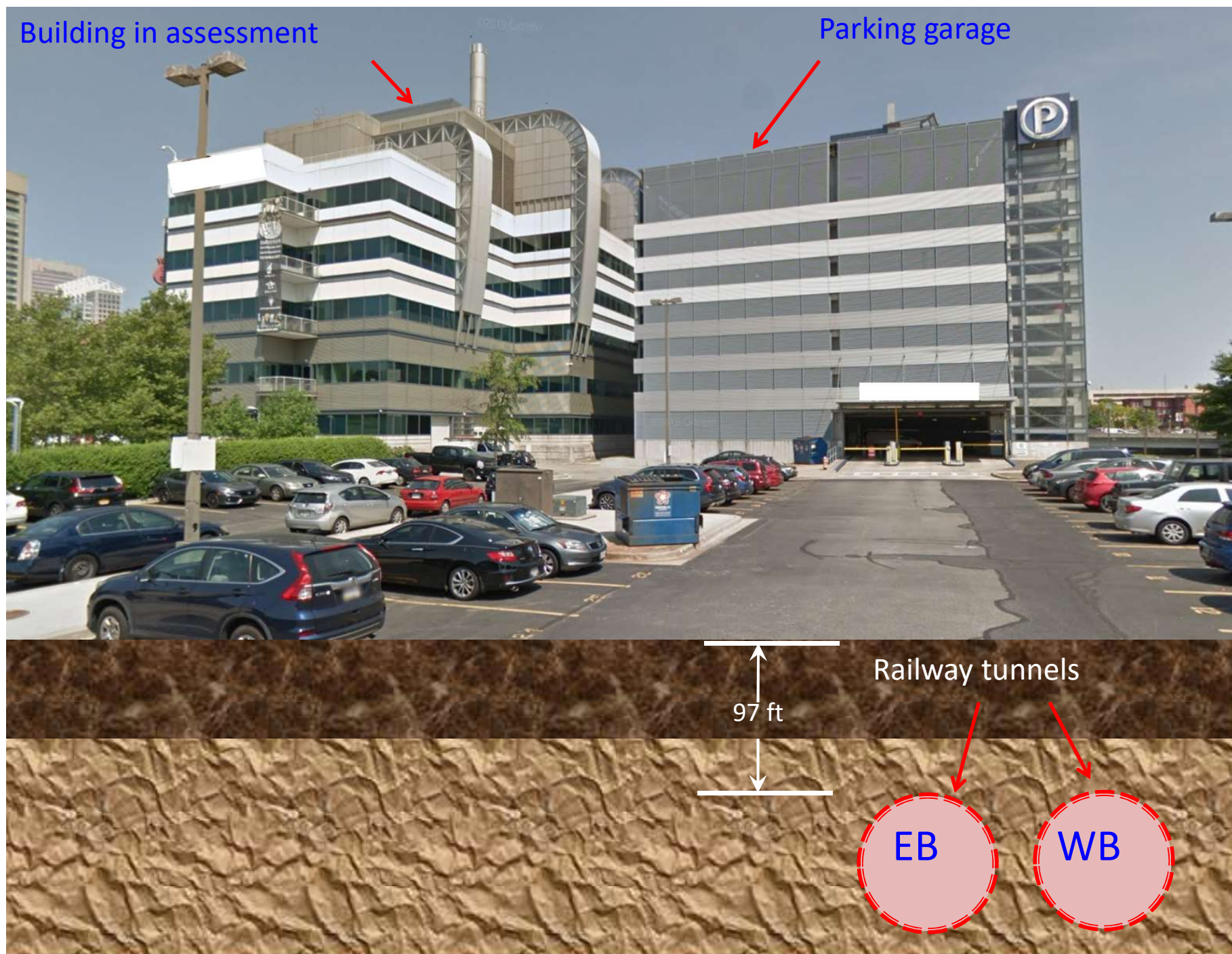


Figure 3
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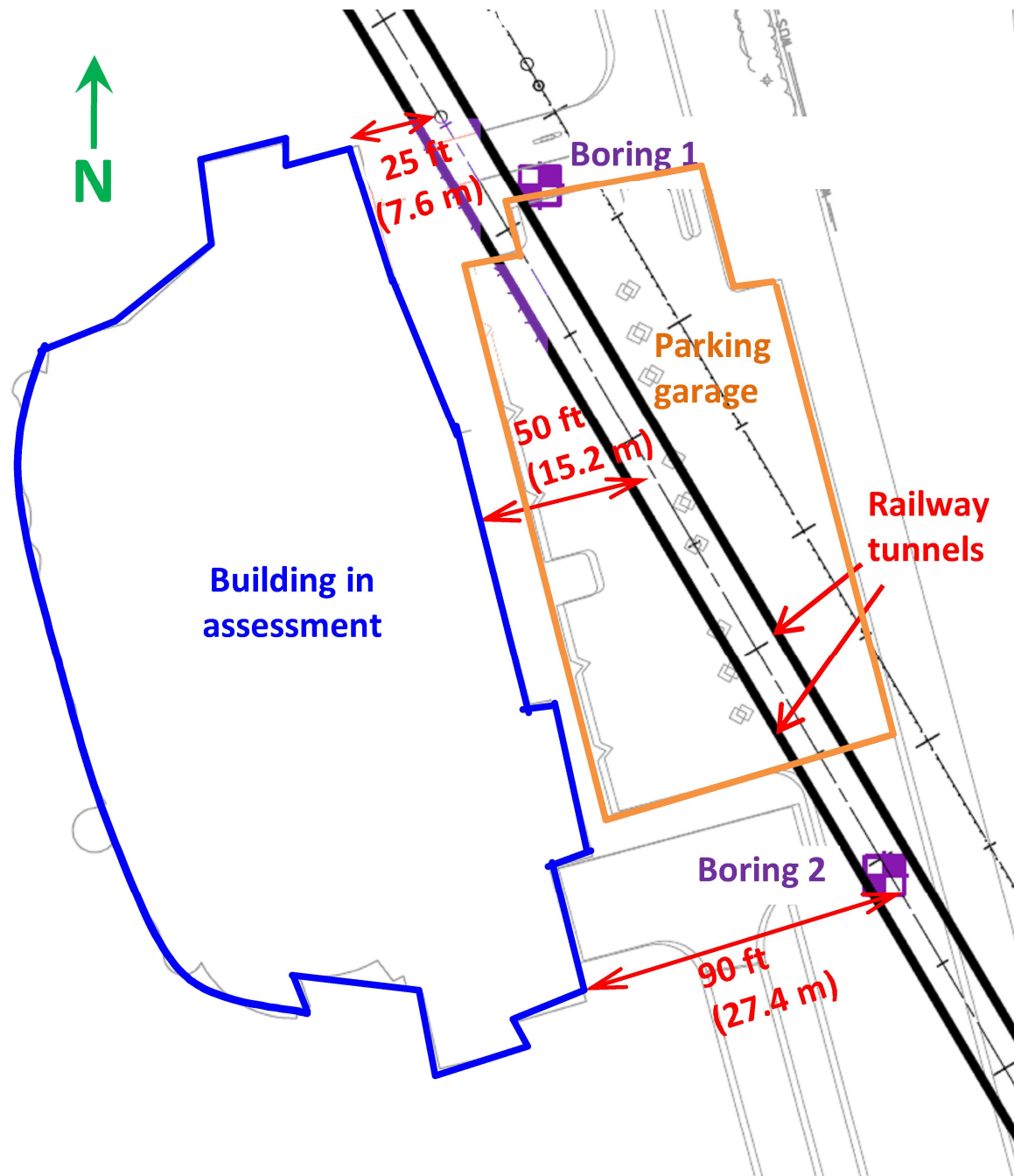


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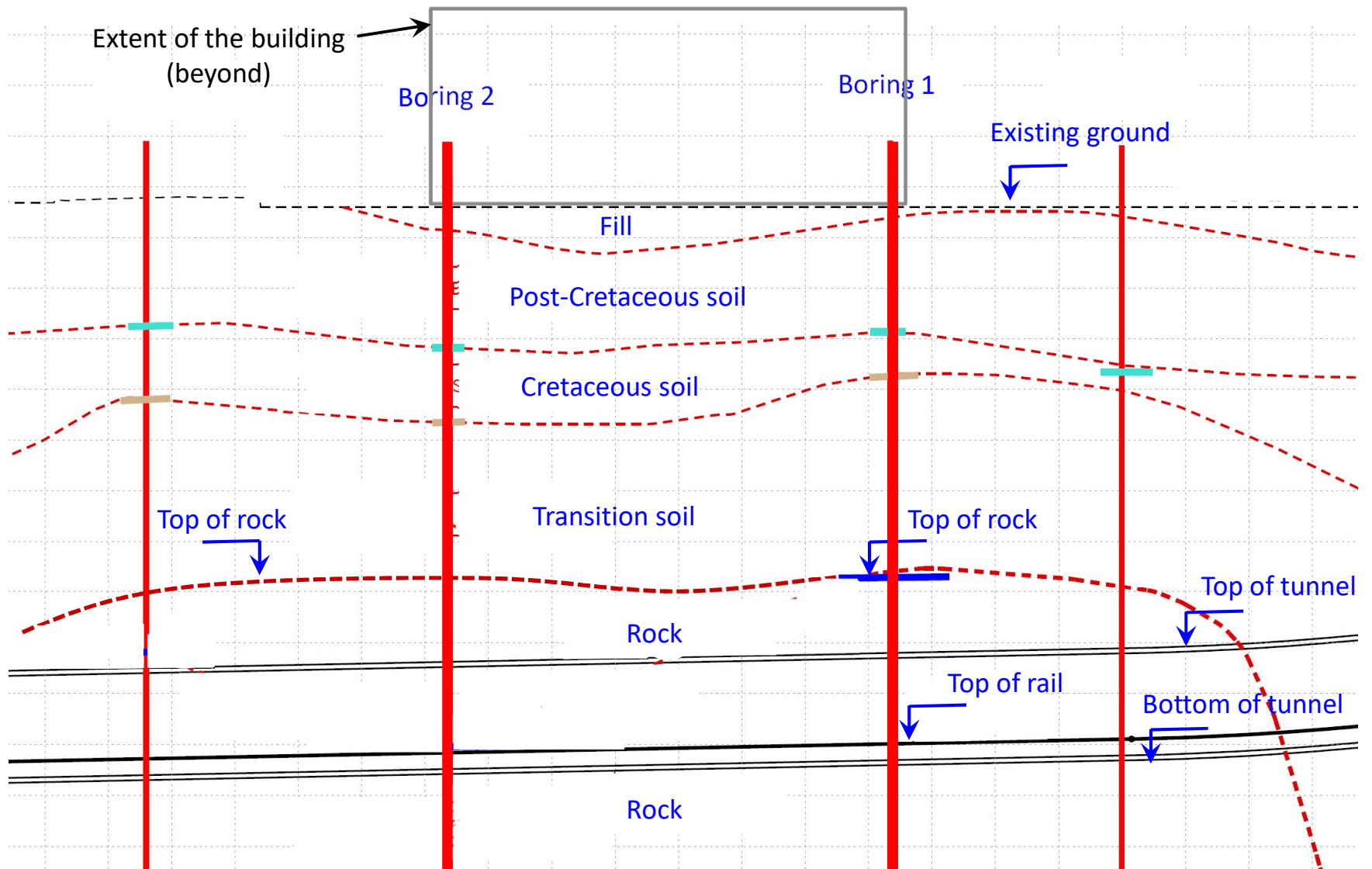


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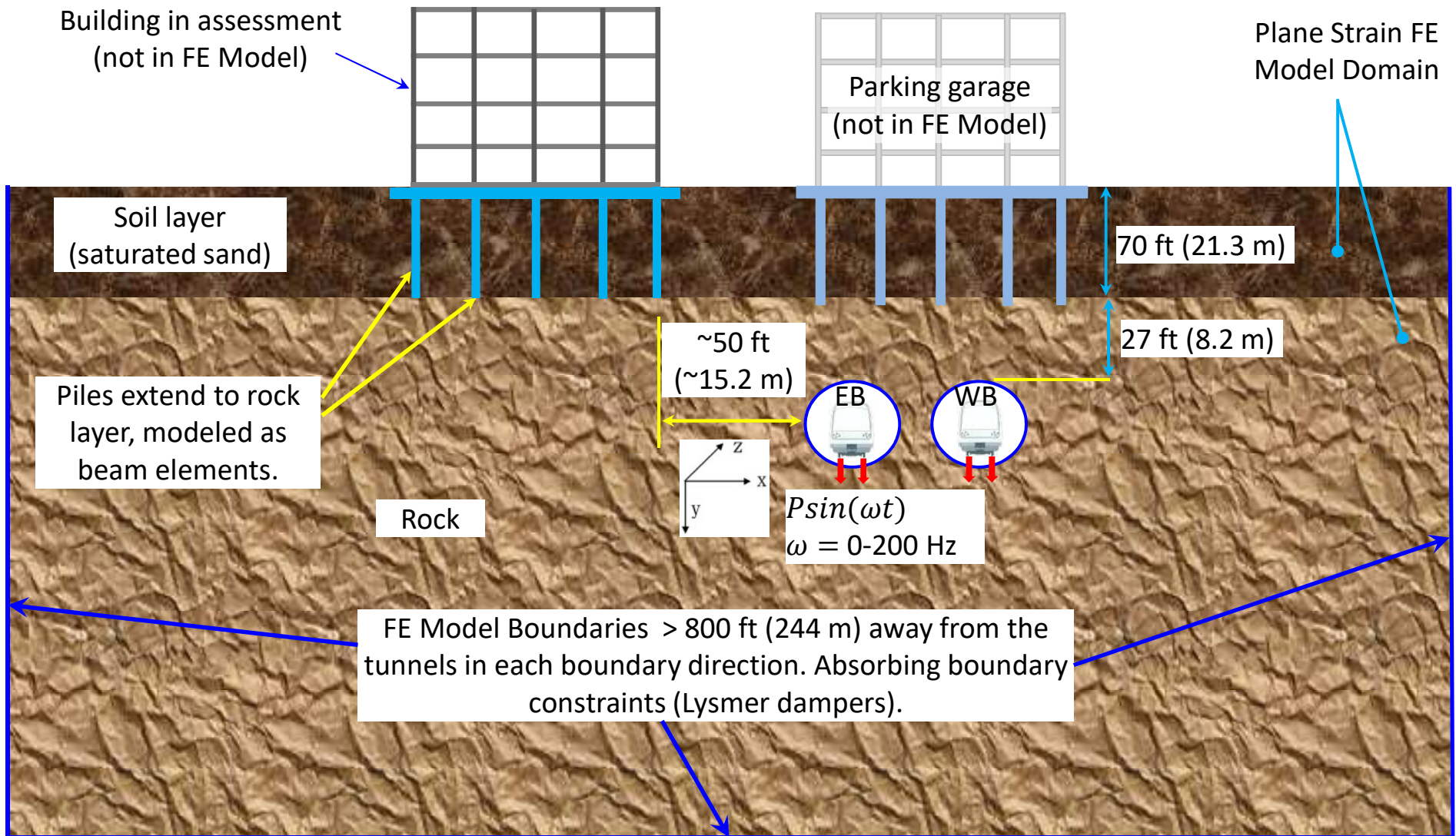


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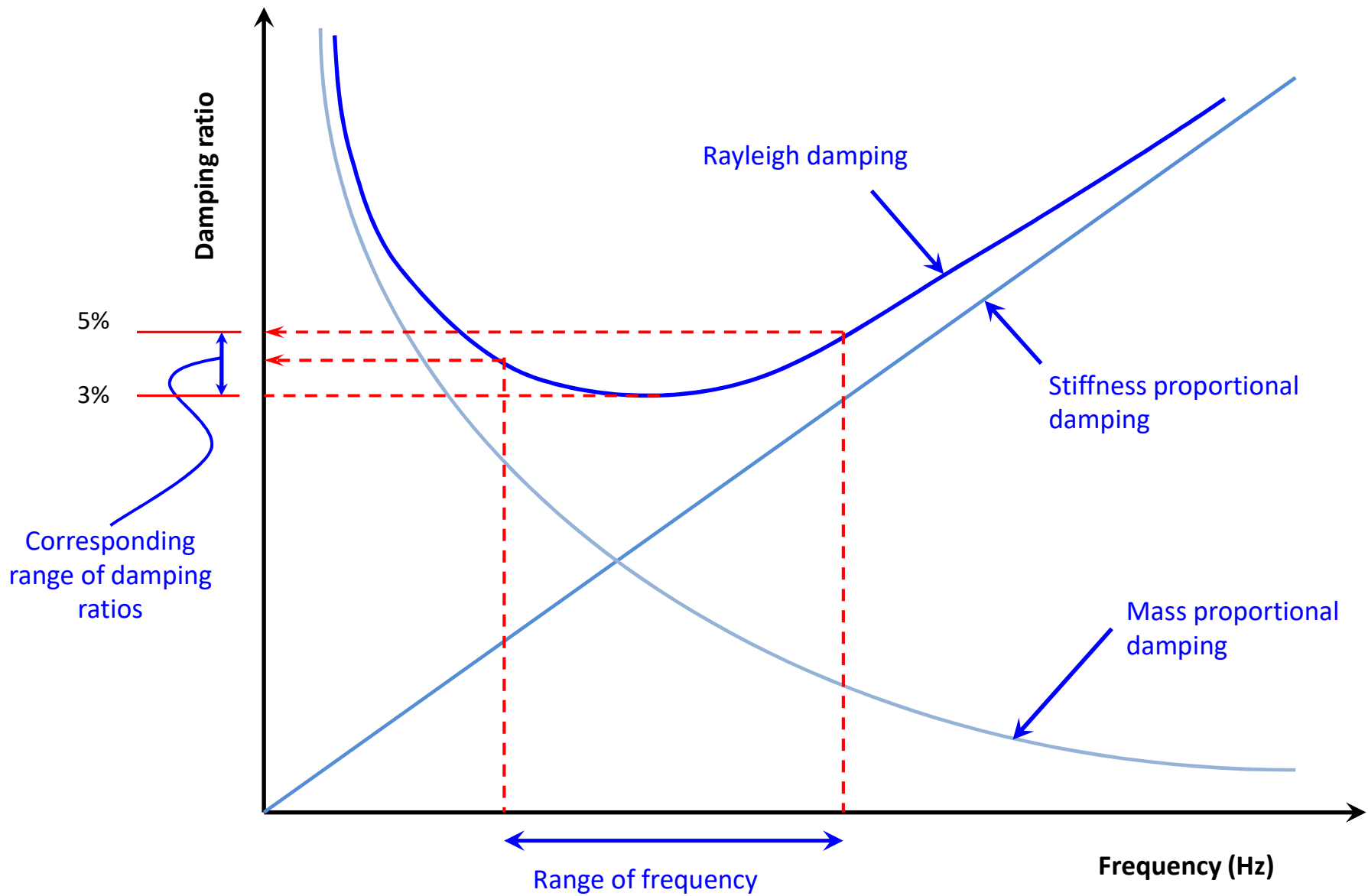


Figure 7
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Figure 8

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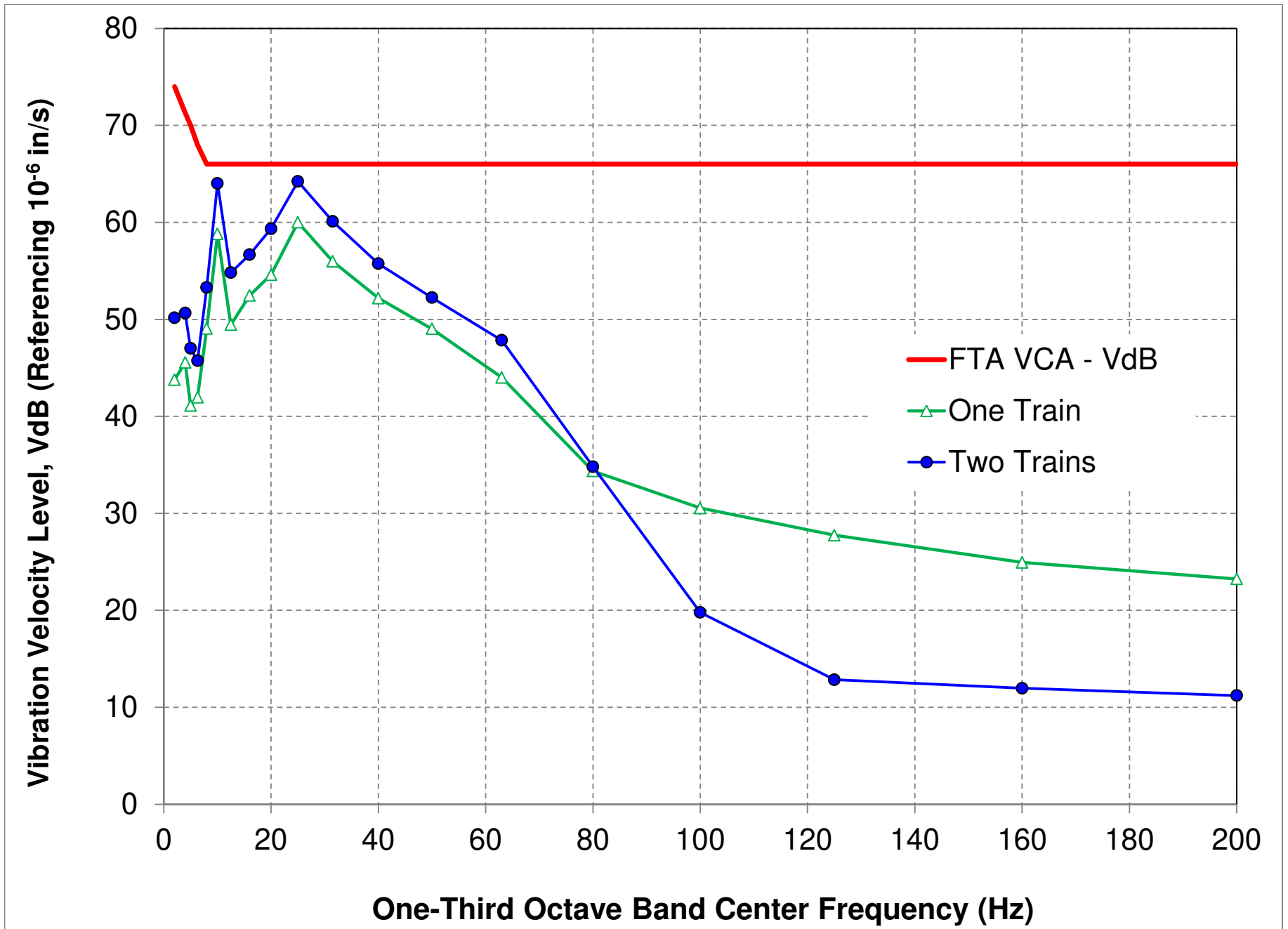


Figure 9
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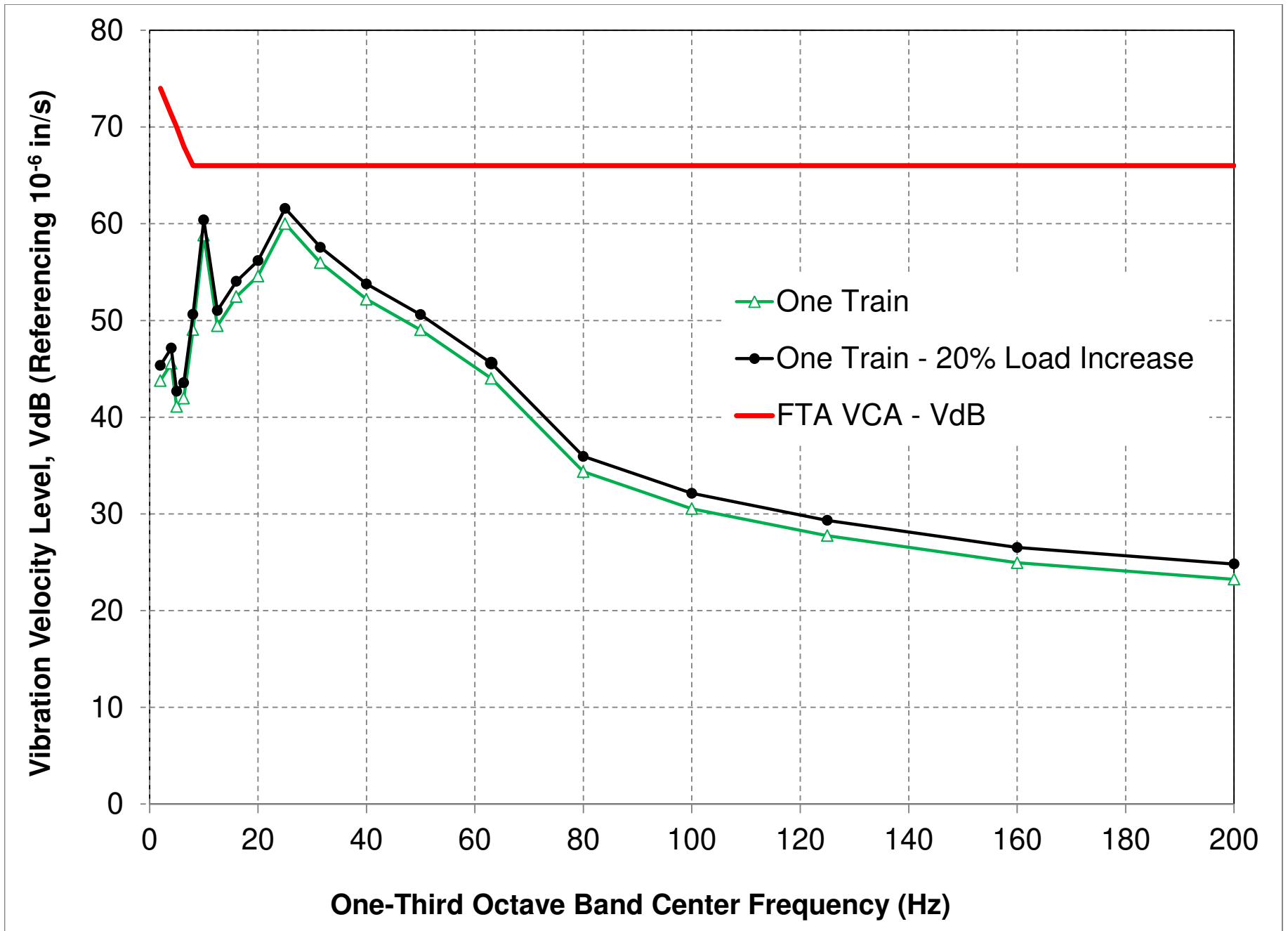


Figure 10

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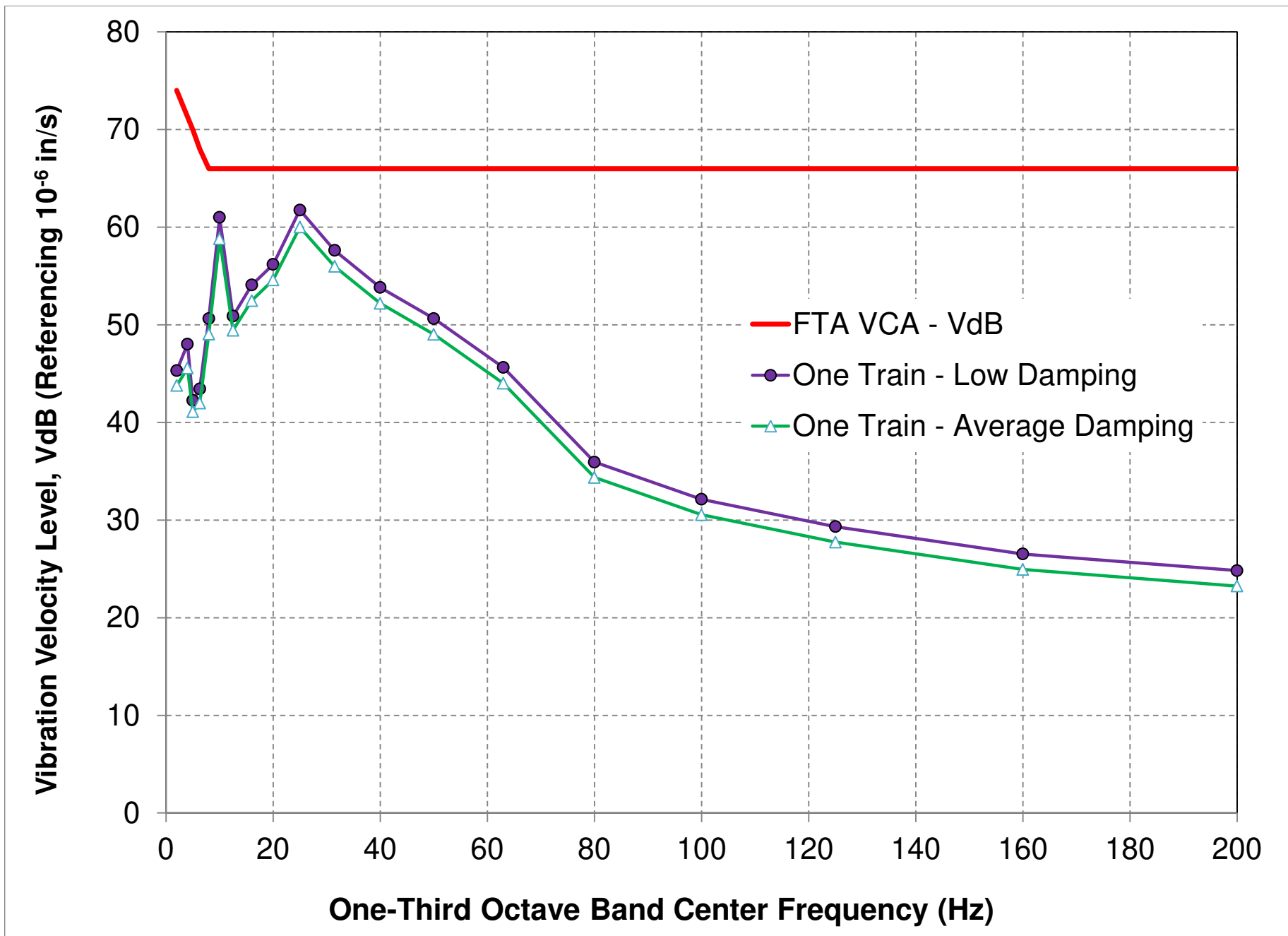


Figure 11

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