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Liquid–liquid phase separation morphologies in ultra-white beetle scales and a synthetic equivalent

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Cyphochilus beetle scales are amongst the brightest structural whites in nature, being highly opacifying whilst extremely thin. However, the formation mechanism for the voided intra-scale structure is unknown. Here we report 3D x-ray nanotomography data for the voided chitin networks of intact white scales of *Cyphochilus* and *Lepidiota stigma*. Chitin-filling fractions are found to be 31 ± 2% for *Cyphochilus* and 34 ± 1% for *Lepidiota stigma*, indicating previous measurements overestimated their density. Optical simulations using finite-difference time domain for the chitin morphologies and simulated Cahn-Hilliard spinodal structures show excellent agreement. Reflectance curves spanning filling fraction of 5-95% for simulated spinodal structures, pinpoint optimal whiteness for 25% chitin filling. We make a simulacrum from a polymer undergoing a strong solvent quench, resulting in highly reflective (~94%) white films. In-situ X-ray scattering confirms the nanostructure is formed through spinodal decomposition phase separation. We conclude that the ultra-white beetle scale nanostructure is made via liquid–liquid phase separation.

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White surfaces are ubiquitous. Conventional white paint comprises a film-forming polymer latex dispersion loaded with high refractive index ($n \sim 2.6$) nanoparticles of Titanium dioxide (TiO_2). In biology, however, whiteness is usually conferred by voided structures made of a continuous biopolymer phase and air. These biological "structural whites"[1,2] have been studied with a view to characterising their nanostructure and explaining their optical properties on the basis of their structure. The important question of how these structures arise in vivo, and the pathways by which they have evolved towards optimum optical properties, remains largely open[3,4].

For the case of highly ordered crystalline photonic structures in beetle and butterfly scales, the structure formation has been postulated to be via pre-patterning and partitioning into intra- and extra-cellular space, followed by chitin deposition[5–8]. Alternatively the patterning and deposition stages could possibly occur simultaneously[9], although this process has not yet been seen in situ to fully understand the stages of photonic nanostructure development. The 3D photonic structures observed to date are ordered crystal grain structures that are highly faceted and strongly break up and segment the internal scale volume. These structures are proposed to be patterned using the physics of hydrophobic–hydrophilic interactions[8] to control morphology (gyroid, cubic, hexagonal, sphere, lamellar etc.) akin to the structural diversity seen in photonic block copolymers[10–12]. These highly ordered 3D biological photonic structures exhibit multiple higher order X-ray scattering peaks due to their structural uniformity and order[8]. However, previously published scattering data show that these higher order X-ray scattering peaks are not observed for the white beetles[8].

Isotropic structural colour, that is independent of viewing angle, is widely found for pseudo-photonic crystals, which exhibit a degree of disorder. Here the optical properties are due to coherent light scattering from a two-phase (air and biopolymer) nanostructure. These are frequently observed in bird feathers[13], and was first documented by Prum et al.[14]. The size of the well-defined length scale in these pseudo-photonic crystals directly affects the observed colour. This is clearly illustrated in Parnell et al.[15], where Eurasian Jay feathers have a periodic gradient in colour from white to blue to black. Pseudo-photonic materials, which have a degree of disorder can be optically modelled using Bragg type reflecting structures, with a distribution of length scales in the layers and their spacings[16]. However, while such models may capture the optical properties well, they do not inform us as to the process by which these optically active nanomaterials form. It has been reported previously that blue structural colour in bird feathers and beetles is probably a result of biopolymer[15,17,18] phase separation[19] via spinodal decomposition with drying[8] and chitin crystallisation[20,21] being potential arrest mechanisms of phase separation[19] within arthropod scales.

In this work, we show a complete ultra-structural characterisation of two intensely opaque biological systems—the white scales of the beetles[22,23] *Lepidiota stigma (L. stigma)* and *Cyphochilus*. We compare these structures[24] with those found in the late stage[25] of the generic process of spinodal decomposition[26], and show by numerical solution of Maxwell's equation for these nanostructures that such spinodal structures can quantitatively reproduce the optical properties of the biological systems. This allows us to confirm that the beetle scales have close to the optimum combination of volume fraction and characteristic length scale to maximise their whiteness and fabricate a synthetic mimic using phase separation by spinodal decomposition.

Results

Non-destructive X-ray nanotomography of ultra-white scales. The beetles, *L. stigma* and *Cyphochilus*, are covered with highly
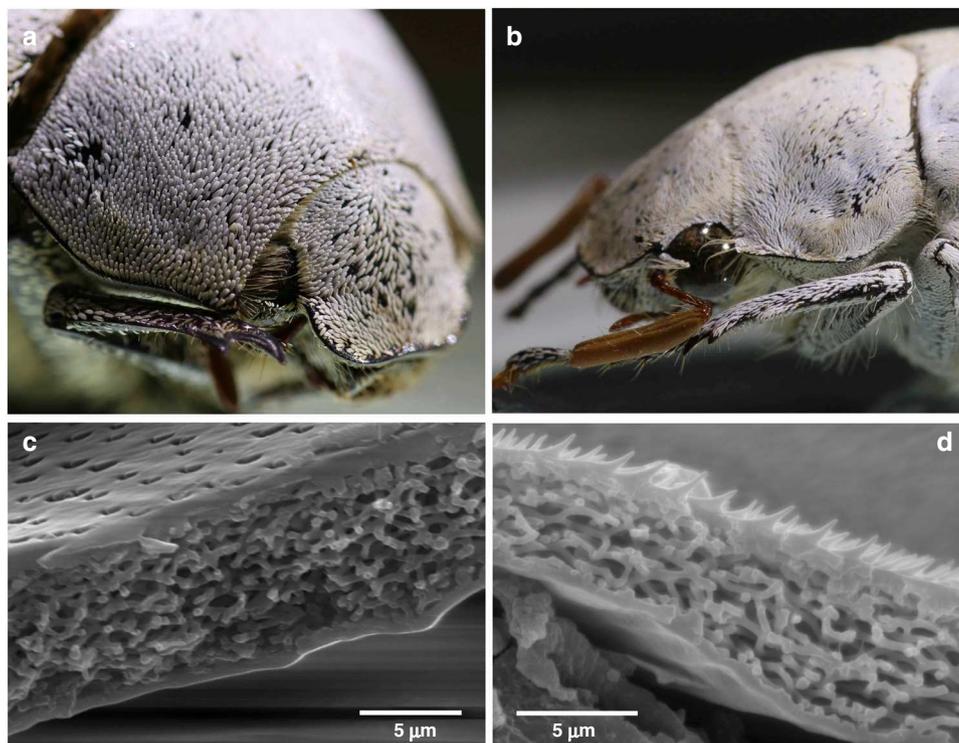
Fig. 1 Microscopy images of the ultra-white beetle scales. **a** An *L. stigma* beetle; the scales are ~350 μm long and 120 μm wide. **b** An image of *a Cyphochilus* beetle; the *Cyphochilus* scales are ~220 μm long and 60 μm wide. The underlying black cuticle can be observed where there are no scales. **c**, **d** Cross-sectional scanning electron microscopy (SEM) images of individual scales for *L. stigma* and *Cyphochilus,* respectively
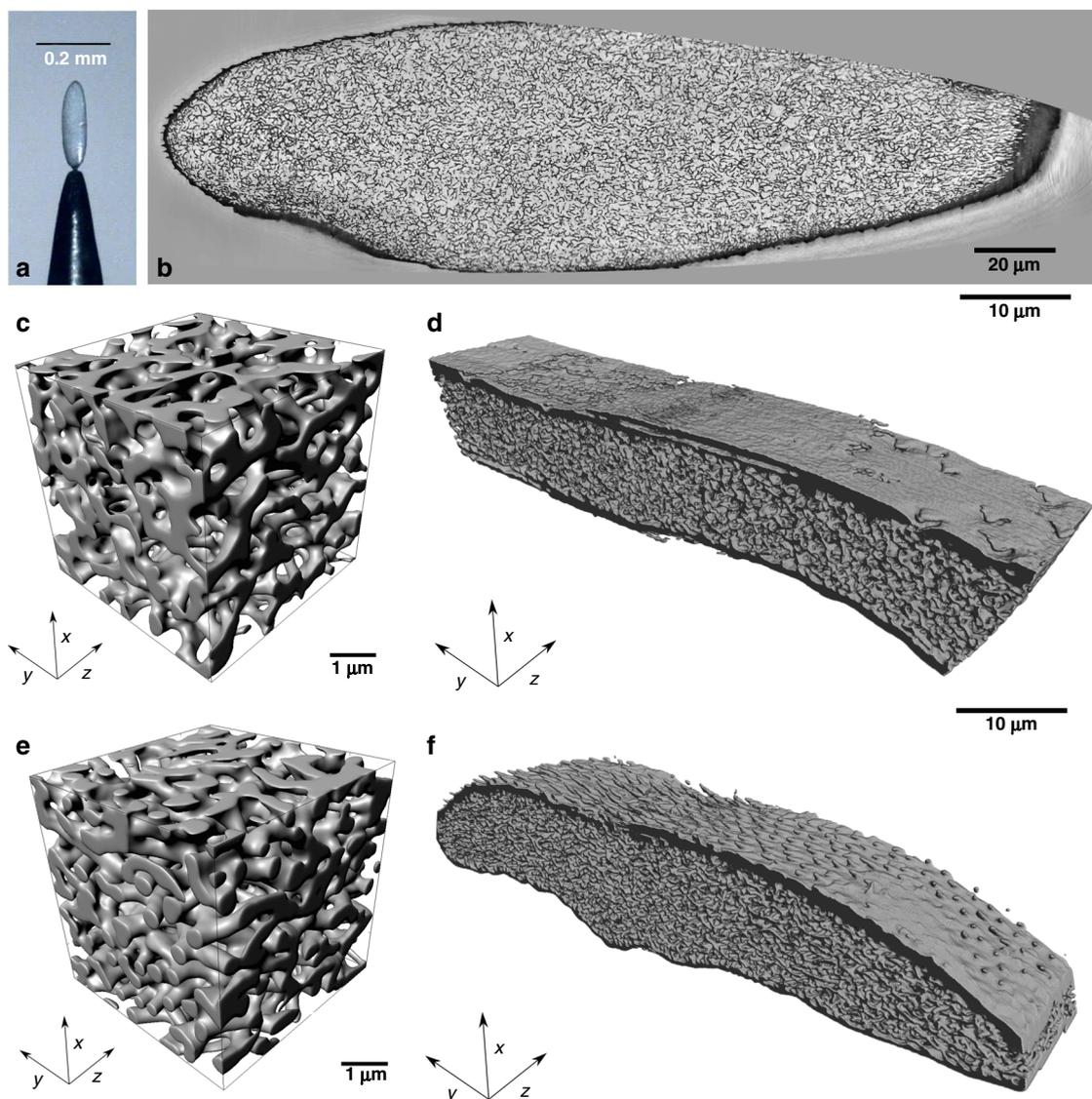
Fig. 2 X-ray nanotomography of intact ultra-white beetle scales. **a** Image showing a single intact Cyphochilus scale mounted to allow a full nanotomography scan. **b** Representative longitudinal slice (*y–z* plane) through the optical structure of an entire *Cyphochilus* scale. **c** Representative optical structure inside an *L. stigma* scale, based on the correlation analysis of 275 individual 5 μm cubes. **d** A larger volume of *L. stigma* showing the extent and filling of the scale interior, and the surface features on the cuticle. **e**, **f** A typical cube and larger cross section, respectively, for the scale of *a Cyphochilus* beetle

opaque, white scales (Fig. 1a, b). Their opacity arises from strong scattering throughout the internal structure of the scales. This inner scale space comprises an interconnected network of α-chitin (Supplementary Fig. 1) with a complementary inter-connected network of air voids[22]. The internal structure of these white beetle scales was studied by scanning and transmission electron microscopy (SEM and TEM) revealing a "foam-like" structure of chitin fibrils (Fig. 1c, d), similar to that previously reported[22]. We found that the sectioning of whole intact scales, even using focused ion beam (FIB) sectioning, resulted in severe scale distortion (Supplementary Figs. 2–4). The substantial warping and curving of the scales when they are cut open could be the result of the voided inner scale nanostructure having an inherent mechanical tension, which is relieved when the outer scale membrane becomes compromised. Therefore, in order to accurately model the optical properties of the scales, structural characterisation of intact scales is needed.

Imaging directly through the outer scale cuticle using X-ray nanotomography[27] for individual *Cyphochilus* and *L. stigma*

scales (Fig. 2) enabled the measurement of the full 3D internal morphology of complete intact scales (Fig. 2a). A cross section through the entire scale (Fig. 2b) shows that the internal structure is continuous, with no evidence of grain boundaries. This indicates that the process used to pattern the white beetles occurs at the same time point in time throughout the entire scale volume.

Representative 5 μm cubes of the internal structure of the *Cyphochilus* and *L. stigma* are shown in Fig. 2c, e, respectively. These cubes were chosen from the 275 cubes cut from each full 3D dataset and had the minimum mean squared error compared with the average correlation functions shown later in Fig. 3a, b. Figure 2d, f shows scale cross sections; with thicknesses of ~12 μm for both species (Supplementary Figs. 5 and 6). The intra-scale nanostructure is a highly continuous and interconnected air-voided network with a characteristic length scale, reminiscent of morphologies observed for phase separating polymer blends[28], which have undergone phase separation via spinodal decomposition[29–31].
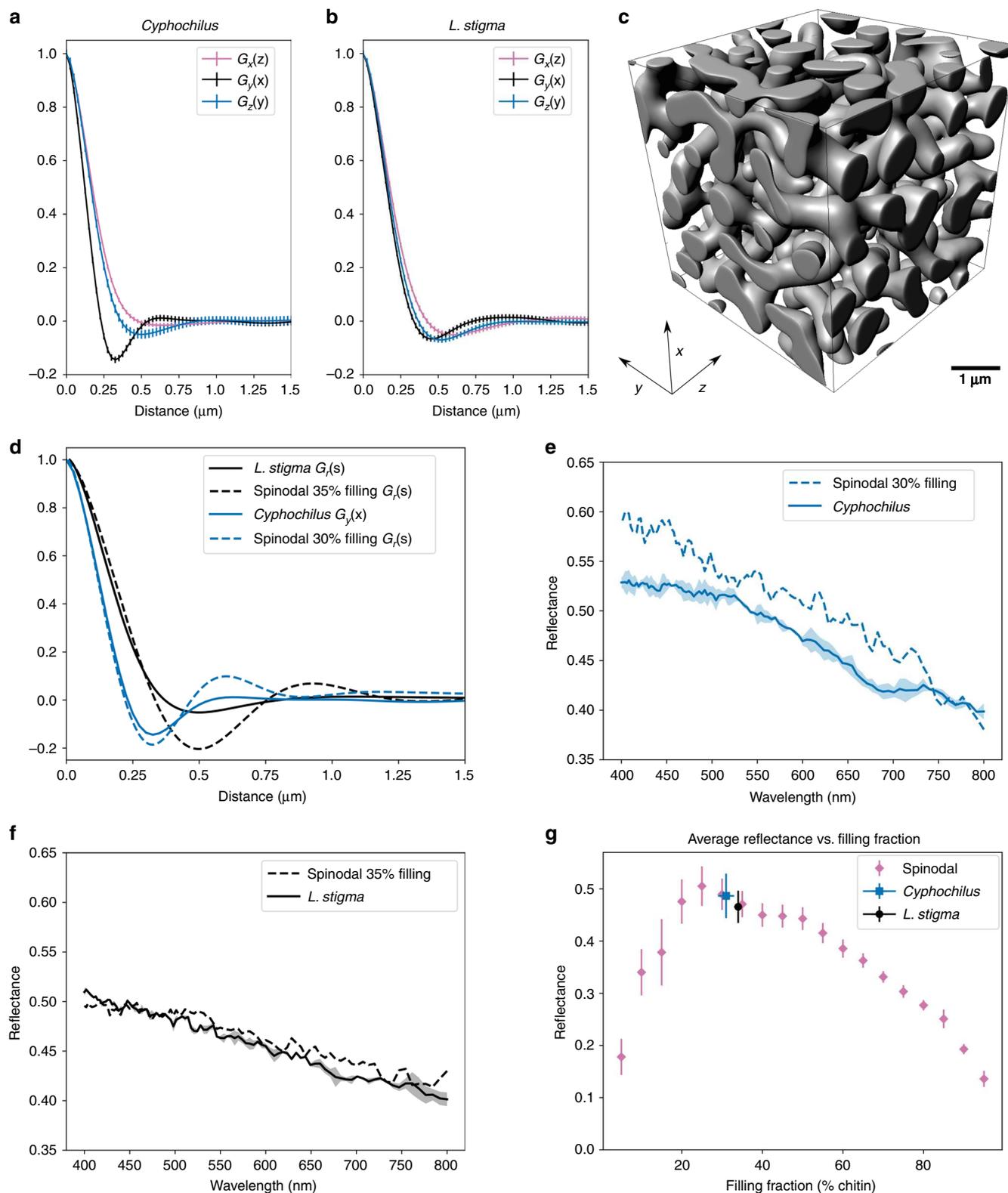
Fig. 3 Comparison of beetle scales and simulated spinodal whites. **a**, **b** Projections of the correlation function in three orientations for the *Cyphochilus* and *L. stigma* intra-scale structures, respectively. Error bars represent the standard deviation at each point across the 275 averaged cubes. **c** A simulated late-stage spinodal phase separated volume with a 30% volume-filling fraction, comparable to the *Cyphochilus* beetle scale-filling fraction. **d** Comparison of the correlation function projections for the measured beetle intra-scale morphologies and the (self-similar) spinodal simulations scaled to the same length scale. **e** *Cyphochilus* FDTD x-reflectance simulation for a slab of measured *Cyphochilus* intra-scale nanostructure and a simulated 30% filling-fraction spinodal with a Gr(s) scaled to 325 nm and **f** FDTD modelling showing theoretical x-reflectance comparison for a 35% filling-fraction spinodal scaled to 500 nm and the structure measured using X-ray nanotomography for *L. stigma* scales. **g** Average reflectance across the visible spectrum as a function of chitin-filling fraction from FDTD optical modelling. The confidence levels show the standard deviation of the reflectance across the sampled wavelengths (400–800 nm) for each filling fraction

From the whole-scale nanotomography data we were able to determine the mean scale-filling fraction, based on entire scales, measured to be $31 \pm 2\%$ for the *Cyphochilus* and $34 \pm 1\%$ for the *L. stigma*. These values are lower than previously reported[4,23,32], and lower than the values we measured using the FIB electron microscopy (Supplementary Tables 1 and 2). We attribute these differences to distortions arising from the use of sectioned scales in electron microscopy studies. Interestingly, our tomography results show only a very small difference of 3% in filling fraction between the two species, suggesting that there may be something special or limiting about a scale-filling fraction of 30%, since the intra-scale structure of both species have converged towards this value.

Analysis of the X-ray nanotomography measured intra-scale structure provides insight into two important issues; the dominant length scale of the intra-scale structures, and the degree to which the structures are isotropic (Supplementary Note 1 and Supplementary Eqs. (1)–(9)). In the case of *Cyphochilus*, a degree of anisotropy is perceptible in Fig. 2e (and Supplementary Movie 1), where the *x–y* plane contains significantly more small round fibril cross sections than the other two planes, indicating that fibrils preferentially lie in the *y-z* plane (the plane parallel to the scale's largest surface). This is quantitatively shown in the average projections of the correlation function (Fig. 3a) along each axis for the 275 individual 5 μm cubes for the *Cyphochilus* data. In the *x*-direction, shown by $G_y(x)$, the correlations are reduced when compared with the other two orientations. This is consistent with the literature[33] and shows that the intra-scale structure for *Cyphochilus* is anisotropic, resulting in differences in the magnitude of the reflected wavelengths for the different axes (Supplementary Fig. 7), with light reflected strongest for the *x*-axis, but at the expense of the *y*- and *z*-axes. In the *x*-direction the correlation function has a much deeper minimum, indicating a prominent length scale in that direction. In addition, the location of the correlation minimum at 325 nm is somewhat smaller compared with the other two orientations, both of which occur at 500 nm. In contrast to *Cyphochilus*, the correlation projections for *L. stigma* in Fig. 3b have similar correlation functions for each orientation, indicating that *L. stigma* scales have an isotropic internal structure (Supplementary Movie 2). This appears to be in contrast to previous studies[23]. Within error, the correlation minimum corresponds to a length scale of 500 nm.

3D Cahn–Hilliard liquid–liquid phase separation simulations. To test if the optical properties of the ultra-white beetle scales could be replicated with a spinodal structure, we simulated a number of structures using numerical solutions in 3D, of the Cahn–Hilliard equations for polymer systems in the long-time limit[25]. We simulated effective chitin-filling fraction in the range between 5 and 95%. These simulated structures capture the mechanism of length-scale selection present in spinodal decomposition, which leads to a structure that is random and isotropic, but with a characteristic length scale, together with the coarsening of that structure at late stages to a pattern obeying dynamic self-similarity[34] (Fig. 3c). In this regime, for a given filling fraction, the statistical characteristics of the patterns (pair correlation functions) are identical when scaled by a single characteristic length scale, which physically is determined by the length of time the system has had for domains to grow in size, known as coarsening[25].

It was possible to set the characteristic length scale of the simulated late-stage spinodal structures to match the correlation functions of the measured beetle intra-scale structures (Fig. 3d). This was accomplished by adjusting the pixel to real-space

conversion up and down in order to virtually zoom in and out of the structure. To match the *Cyphochilus* structure, a 30% filling-fraction spinodal simulation was matched to the length scale in the *x*-axis *Cyphochilus* correlations. For the isotropic *L. stigma* structure, a 35% filling-fraction spinodal simulation was matched to the radially averaged *L. stigma* correlations.

Finite-difference time-domain optical modelling. To explore the optical properties of the reconstructed beetle intra-scale nanostructures, and the corresponding simulated spinodal structures, we needed to calculate reflection coefficients as a function of wavelength. This is a difficult regime in which to carry out such calculations—the presence of many strongly scattering interfaces separated by length scales comparable with optical wavelengths mean that many optical approximations are invalid, such as ray tracing[35] or matrix methods[36]. Hence we used the full numerical solution of Maxwell's equations for the 3D structures using finite-difference time-domain methods (FDTD)[37], this allowed us to calculate the broadband reflectance for any arbitrary structure.

To simulate the geometry of a scale lying on a beetle elytrum, 5 μm × 20 μm × 25 μm (*x*, *y*, *z*) slabs of each beetle structure were cut from the tomography data, and FDTD was used to calculate the reflectance of the top of the slab in the *x*-direction. The same was done for slabs of the spinodal simulations with equivalent length scales and filling fractions to the intra-scale X-ray tomography data. The results for the 35% filling-fraction spinodal slab show excellent agreement with the reflectance results from the actual *L. stigma* structure (Fig. 3d). The *Cyphochilus* results were complicated by anisotropy in the intra-scale structure; however, the isotropic equivalent spinodal simulation was still able to capture the general trend of the *Cyphochilus* reflectance, by virtue of it exhibiting a higher reflectance for smaller incident wavelengths. It is important to stress that these results are not fits to the experimental data, but rather are FDTD simulations in which only the characteristic length scale and the filling fraction of the structure have been matched to the appropriate values for each beetle's measured intra-scale nanostructure, i.e. the reflectance of the beetles scales is predicted by a spinodal phase separation structure.

To investigate the effect of filling fraction for a fixed length scale, FDTD reflectance was calculated for slabs of Cahn–Hilliard spinodal structures with filling fractions covering the range of 5–95%. The first minimum in correlations for all the slabs was set to 500 nm, this being the length scale for the intra-scale structure of *L. stigma* measured via X-ray nanotomography. The results plotted as average scattering intensity over wavelengths 400–800nm are presented in Fig. 3g. The reflectance from the measured beetle scale structures *L. stigma* (green point) and *Cyphochilus* (blue point) is also plotted to enable comparison, these both lie very close to their spinodal equivalents, the spinodal simulations reach maximum reflectance at ~25% chitin-filling fraction. This important result, that filling fractions well below previously reported chitin scale-filling fractions result in superior reflectance, has very recently been reported for a naive simple branching random walk model[38] despite being highly anisotropic. However, as the isotropic 30% filling-fraction spinodal simulation had a higher reflectance than the *Cyphochilus* structure (Supplementary Fig. 8). This shows that anisotropy is not crucial to achieving highly reflective materials, since the simulated isotropic spinodal structure is capable of superior reflectance. There has been an on-going debate[39] in the field of opacifying layers as to whether "a flat" compressed nanofoam of air bubbles can outperform TiO_2-based opacifying coatings. On the basis of these FDTD simulations we can see that this is not necessary and

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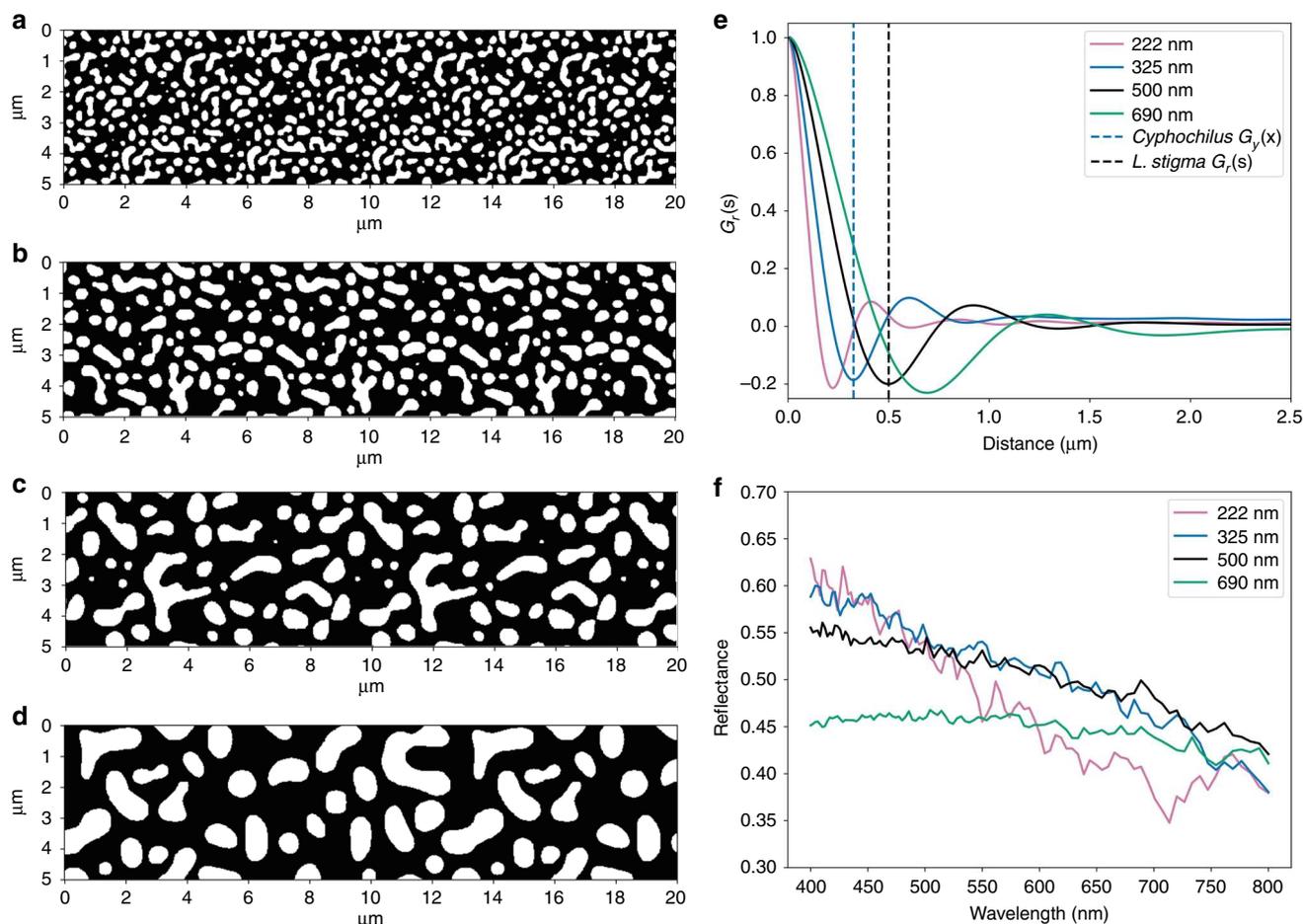
Fig. 4 Spectral response versus spinodal characteristic length scale. Representative 2D cross sections in the *xy* plane for a series of spinodal slabs of varying characteristic length scale **a** 222 nm, **b** 325 nm, **c** 500 nm and **d** 690 nm. Each slice, regardless of length scale is 5 μm × 20 μm and has a filling fraction of 30% white pixels. **e** Gr(x) results for the 30:70 spinodal filling fraction for four different characteristic length scales. The dashed lines show the length scales of the *Cyphochilus* and the *L. stigma* beetles. **f** FDTD reflectance results for 5μm × 20 μm 30:70 spinodal optical structures having different characteristic correlation lengths

indeed the isotropic spinodal scale structure for both beetle length scales gives a higher level of reflectance, than the anisotropic equivalent.

The effect of length scale on the simulated reflectance for a fixed filling fraction is shown in Fig. 4. This was accomplished by altering the characteristic length scale of a 30% spinodal slab to four different values (Fig. 4a–d). The values were chosen such that two of the slabs matched the length scale of the *Cyphochilus* and *L. stigma* structures, one slab was smaller and one was larger (Fig. 4e). The FDTD reflectance results in Fig. 4f show a clear trend of increasing reflectance at low wavelengths with decreasing feature size at the cost of decreased reflectance at higher wavelengths. With its flat spectrum, the largest length scale (690 nm) would be the most white in colour, while the smallest length scale (222 nm) would be the most blue. If the aim of these structures is to maximise reflectance across all wavelengths (i.e. make the brightest white), and then a 500-nm length scale provides a suitable compromise between maximising reflectance, without losing reflected intensity at higher wavelengths and producing a more "blue-white" as observed for smaller length scales.

Based on the FDTD optical modelling we suggest that any synthetic route to create opacifying structures[40] via spinodal phase separation should aim for a filling fraction of 25% and a

length scale of 500 nm. While this optimal filling fraction is much lower than measured and reported for the beetle scales[4,23,32] over the last 10 years, we propose that the high filling fraction values are an artefact of the assay, as the sample preparation causes densification as demonstrated by our comparative FIB SEM and X-ray nanotomography results.

Nanostructured ultra-white cellulose acetate polymer film. Our deep structural understanding of the *L. stigma* and *Cyphochilus* intra-scale structures and their optical equivalence to structures formed by spinodal decomposition led us to develop a synthetic analogue. This was achieved using a commercially available bio-derived polymer, cellulose acetate (CA). CA was dissolved in acetone, which underwent a solvent quench in the presence of a salt, calcium chloride ($CaCl_2$). The CA was molecularly dissolved in acetone to make a solution with a concentration of 0.1 g/mL and mixed together with a methanol/salt solution such that the solvent ratio of acetone to methanol was 5:3 by volume. The solution was then drawn into a film and allowed to phase separate and vitrify, this process was fast ~40 s. The mass ratio of CA to salt was optimised to produce a film with the target filling fraction by control of the solvent quality. The optimum ratio was found to be 2:1 CA to salt by mass.
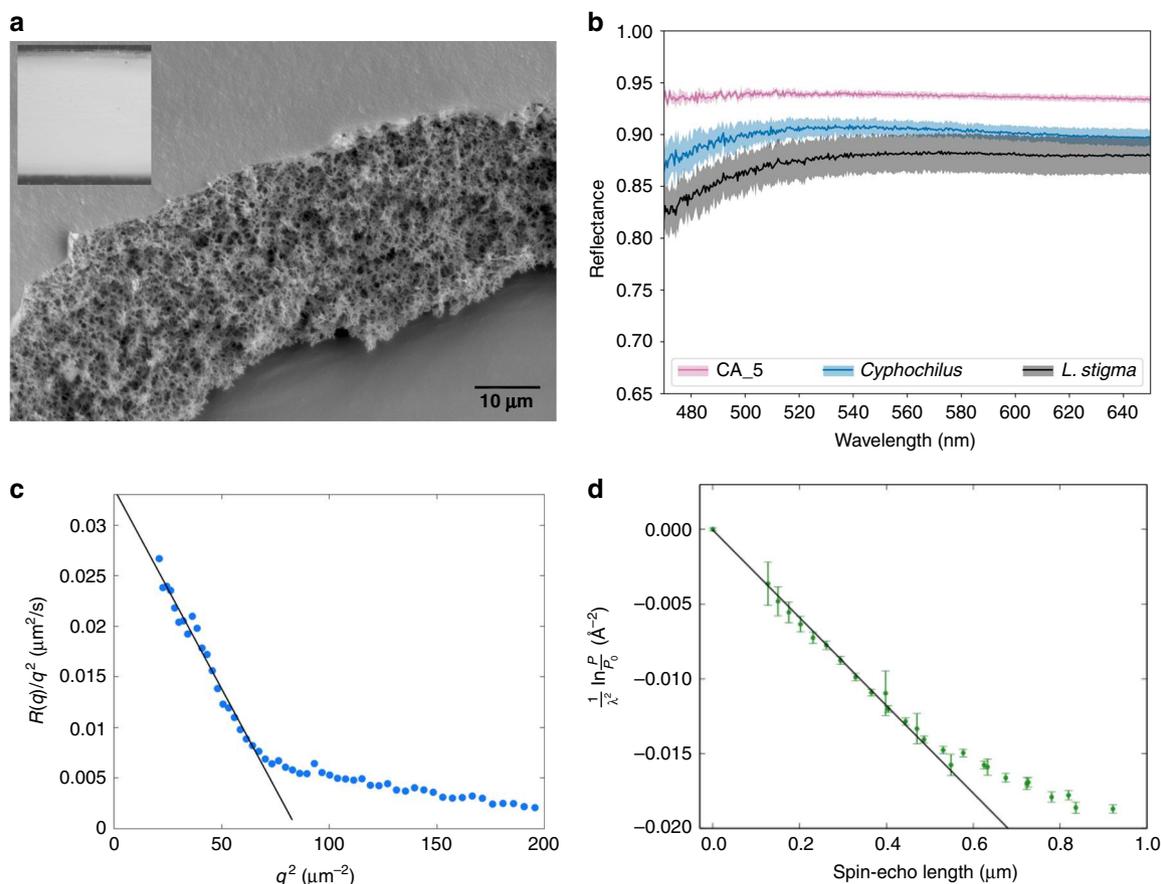
Fig. 5 Structure formation and characterisation of synthetic whites **a** SEM image of a porous white cellulose acetate film, with an inset showing the appearance of the white synthetic film. **b** Optical reflectance comparison for scales of *L. stigma, Cyphochilus* and an optimum cellulose acetate white film (12.8 ± 1.6 μm in thickness) The shaded area represents the confidence levels calculated as the standard deviation across all measurements collected. **c** Amplification factor R(q), measured by ultra small-angle X-ray scattering (USAXS) plotted as R(q)/q^2 versus q^2, showing a linear region typical of spinodal decomposition. **d** Linear fit to the initial slope of the wavelength normalised spin-echo small-angle neutron scattering (SESANS) $G_x(y)$ signal, used to measure the density and therefore the filling fraction of the synthetic white films.The error bars are calculated based on the neutron counting statistics

The resulting CA films were white, highly voided (Fig. 5a), and exceedingly reflective as verified by reflectance measurements (Fig. 5b). Comparing the reflectivity of the CA film to scales from *L. stigma* and *Cyphochilus* for which reflectance is 90% and 88%, respectively, the synthetic film had consistently higher reflectance, at ~94% for a 12.8 μm film (Supplementary Fig. 9), compared with both beetle species' scale thicknesses of 12 μm at their thickest point.

To understand the structure formation mechanism we used time resolved, in situ, ultra small-angle X-ray scattering (USAXS). The fast data acquisition and unique USAXS length scale range at ID02 (European Synchrotron Radiation Facility (ESRF)) made it possible to follow the structural evolution and phase separation dynamics as a function of momentum transfer q, where $q = \frac{2\pi}{d}$, d being length scale. The early time information allowed us to measure the length-scale-dependent amplification factor R(q) at early times[29,30] for our CA films. For longer length scales, a linear relationship between R(q)/q^2 and q^2 was found (Fig. 5c), confirming spinodal decomposition as the phase separation structuring mechanism.

Using spin-echo small-angle neutron scattering[41,42] (SESANS) we were able to measure the correlation function directly for a large area of the synthetic structural white. This was performed in three orientations to confirm the isotropic nature of the CA films (Supplementary Fig. 10). The data showed a discontinuity

(Fig. 5d) at ~470 nm, close to the dominant length scale found for the ultra-white beetle internal scale structure. The density of the films could be determined from the slope of the correlation function and was found to be 21.5 ± 4% (Fig. 5d, Supplementary Note 2 and Supplementary Eq. (10)).

Therefore, the improvement in the film's reflectance over the beetle scales is most likely the result of its filling fraction being close to the filling fraction required to achieve optimal reflectance, 25%, determined using the filling fraction phase diagram (Fig. 3g). However, some of the increase in reflectance could be due to the specular component from the surface of the films and the slightly thicker voided layer, as the beetle scales possess a dense cuticle layer ~1 μm thick.

Discussion
In the case of the anisotropic network within the *Cyphochilus*, the internal α-chitin optical structure is highly interconnected and prone to distortion on sectioning, meaning that anisotropy must be imparted to the optical structure before it fully solidifies. We envision that the anisotropy is imparted in the late stage of liquid–liquid phase separation when the chitin precursors are transitioning to become mechanically stable crystalline α-chitin, vitrifying the internal scale nanostructure. The anisotropy is probably caused by the liquid flow that removes the aqueous fluid from the narrow stalk opening back to the socket cell, leaving a

dry desiccated α-chitin air network. The effect of flow on phase separation is well known in spin-coated thin polymer blend films, where a radial flow provides a strong position dependent radial shear which alters the phase separation length scales and breaks the symmetry, due to advective flow[43,44]. There are several reasons this effect could be observed in the *Cyphochilus* and not the *L. stigma* such as differences in the liquid removal dynamics (shear flow) due to geometrical considerations (scale size) or the crystallisation of α-chitin (reaction rate). In addition, the *Cyphochilus* nanostructure network has a small difference in filling fraction making it different mechanically and therefore possibly more susceptible to advective flow.

In summary, using FDTD optical modelling of the intact 3D intra-scale structures for *L. stigma* and *Cyphochilus* and simulated spinodal phase separated structures, we were able to establish design rules for producing highly reflective synthetic structural whites based on biological optical design. We then optimised the optical and structural properties of our cellulose acetate polymer films (controlling length-scale, filling fraction) and fabricated a synthetic mimic capable of producing a higher reflectance than the beetle scales for a comparable thickness. Given that we are able to replicate the morphology and optical reflectance of the beetle scales using structures that form via spinodal decomposition, using both optical simulations and the formation of a simulacrum, it seems nature uses the same liquid–liquid phase separation mechanism[45] to create ultra-white structural colour.

The large existing body of work on structural colour has found a range of interesting and diverse structural colour architectures in biological systems. What has proved elusive has been the understanding of how these structures are made in vivo. Our insight into the optical structure of white beetle scales and our synthetic equivalent implicates liquid–liquid phase separation. This is increasingly seen as an important way to understand the process by which cell biology[45,46] provides order, organisation and segregation in cells across many different length scales. Our work confirms that some biological cells exhibiting structural colour use liquid–liquid phase separation to drive the formation of a highly interconnected bicontinuous nanonetwork in a single scale cell.

Methods

Fourier transform infrared attenuated total reflection. The beetle scales infrared (FTIR ATR) data were collected using a Thermo Scientific Nicolet iS10 Fourier transform infrared (FTIR) instrument equipped with a diamond attenuated total reflection (ATR). A background was collected; the sample was then placed in contact with the diamond ATR surface. A resolution of $2\,cm^{-1}$ was used and a total of 128 acquisitions.

Scanning electron microscopy. SEM Beetle scales and the synthetic cellulose acetate samples were mounted using conductive carbon discs AGG3357N (Agar Ltd) on conductive metal stubs (Agar Ltd). These were sputtered with ~10 nm of gold (Agar Ltd) and imaged on a JEOL JSM-6010LA using the InTouchScope data acquisition software.

Transmission electron microscopy. Scales from both the *L. stigma* and the *Cyphochilus* beetles were mounted in a 1:1 mixture of 1,2epoxypropane: Araldite resin and left overnight in a rotating mixer. The solvents were then replaced with fresh Araldite CY212 resin (Agar Scientific Ltd) and the samples were imbedded in 'coffin moulds'. The samples were allowed to cure at 60 °C for 48–72 h before 500 nm sections were cut using an ultramicrotome (Reichert-Jung Ultracut E). The sections were subsequently stained with 1% toluidine blue in 1% borax. The sections were then washed with deionized water, dried and mounted using DPX (Agar Scientific). Finally, again using the ultramicrotome, sections were cut on 200 mesh copper grids and imaged using a TEM (FEI Tecnai). The thickness of the TEM sections was estimated at about 85–90 nm. In order to determine the filling fraction of chitin within the scales the images needed were thresholded into binary images so the number of pixels corresponding to chitin in the images could be quantified.

Focused ion beam scanning electron microscopy. An FEI Nova 600 DualBeam FIB field emission gun scanning electron microscope from the Loughborough

Materials Characterisation Centre, was used for imaging. The gallium ion source ion in this instrument allowed regions to be milled away from the scale to reveal the internal network of chitin filaments. The probe current was kept between 3–7 pA. The Dual-Beam FIB was used to extensively study the internal structures and mill away and open the scales, slice layers from the samples (Supplementary Figs. 2–4).

X-ray nanotomography. The X-ray nanotomography on individual scales was performed at the ID16B beamline ESRF using holotomographic scheme with a high flux (10^{12} ph/s) monochromatic beam ($\Delta E/E = 10^{-2}$) with an energy of 17.5 keV. The use of a 25 nm pixel size limits the field of view available to $54 \times 64 \times 64\,\mu m^3$. According to the sample geometry and dimensions, we mounted the samples in the vertical direction (Supplementary Figs. 11 and 12) in order to have the cross section fully in the horizontal field of view, and then performed multiple overlapping scans in the vertical direction. The *Cyphochilus* and the *L. stigma* scales were ~250 and 350 μm, respectively, in length, which corresponded to six scans and eight scans in the vertical with 10 μm overlap between the scans. For each acquisition, 2998 projections were acquired over 360° with a counting time of 150 ms per projection. To avoid artefacts on the reconstructed images and keep the highest 3D resolution, the sample was mounted to give an unobstructed 360° field of view. Beam damage was not observed. The reconstructed scans were then assembled and thresholded to separate the chitin and air pixels and produce the final 3D data sets (Supplementary Movies 3 and 4).

Finite-difference time-domain optical modelling. The FDTD simulations were performed using the commercial software, Lumerical (Lumerical Inc. Canada), which is a 2D- and 3D-solver for Maxwell's equations. For each simulation a 3D matrix containing a structure of interest represented as a binary matrix, where 1 was material and 0 was air. The material in every instance was taken to be chitin, which has a refractive index of 1.54. Each matrix contained a slab of material that had a real-space size of $5\,\mu m \times 20\,\mu m \times 25\,\mu m$. To study how light propagated along each principle axis, the slabs were divided into 20 cubes, each $5\,\mu m \times 5\,\mu m \times 5\,\mu m$, and a polarised Gaussian source of width 1 μm was directed into different faces of the cubes individually. Monitors collected the light, which exited the cubes, and the results were averaged across all of the cubes for a given slab. To study just the reflectance from a slab of material, an unpolarised Gaussian beam of width 6 μm was directed parallel to the shortest axis of the matrix and monitors collected the light, which was reflected back to the source. In all instances perfectly matched layers surrounded the region of interest, outside of the light monitors, to prevent light that had been scattered outside the region of interest from re-entering the simulation.

Synthetic films. To prepare the polymer solutions, cellulose acetate sheets (Clarifoil®) were cut and weighted into a glass vial. Acetone (Sigma-Aldrich UK) was then added to the vial to achieve a target concentration of 0.1 g/mL. A stirrer flea was added and the vial was left to stir overnight at room temperature, to ensure the cellulose acetate was completely dissolved. In a separate vial, $CaCl_2$ (Sigma-Aldrich) was dissolved in methanol (Sigma-Aldrich). The mass of $CaCl_2$ was varied to the desired ratio by mass to cellulose acetate, the volume of methanol was set such that ratio between the acetone and methanol was 5:3 by volume. Finally, the $CaCl_2$/methanol solution was added to the cellulose acetate/acetone solution and left to stir at room temperature until homogeneous.

Once the solutions were prepared they were drawn into films of varying thicknesses. In order to accomplish this, an automated system was developed capable of achieving consistent and repeatable drawdowns. The system consisted of three main components, a drawdown cube, a drawdown guide to hold the cubes and substrate and a linear actuator to move the cubes across the substrate at constant speed.

Ultra small-angle X-ray scattering. The USAXS measurements were performed at the ESRF, beamline ID02[47,48]. X-rays with a wavelength of 1 Å (12.4 keV) were used. The beam size was 20 μm × 20 μm, and sample-to-detector distance of 30.68 m (q range 0.002–0.2 nm^{-1}). A set of rails was made to accommodate the drawdown cubes. The rails were on a moving platform that could rotate. The drawdown cube was positioned over the sample on the moving platform, maintaining the platform horizontal. As the cube finished a drawdown, the platform rotates into a vertical position, necessary for transmission USAXS (Supplementary Fig. 13).

Neutron reflectivity. Neutron Reflectivity (NR) was performed on a thin film of spin-coated cellulose acetate, spun from a 2 wt% acetonitrile (Sigma-Aldrich UK) solution. The substrate was a large diameter (50.8 mm) circular silicon wafer (Prolog Semicor, Ukraine). The NR data were measured at the ISIS pulsed Neutron and Muon Source (Oxfordshire, UK) using the instrument OFFSPEC with neutron wavelengths 2–12 Å. Three incident angles were collected (0.5°, 1.5° and 2.5°) to cover the momentum transfer range 0.008–0.238 Å^{-1}, using a resolution of 2.5%. The data were reduced using Mantid[49] and Offspec specific routines to stitch the three angles and subsequently rebin the data into one dataset. The data were then modelled using routines based on the scheme of Névot and Croce[50]

(Supplementary Fig. 14). From modelling a thin film of cellulose acetate has a measured scattering length density value of 1.64×10^{-6} Å^{-2}.

Spectroscopic ellipsometry. Spectroscopic ellipsometry (M2000V, J.A. Woollam) was used to determine the refractive index and absorption of a cellulose acetate thin film. A Cauchy[51] model (Supplementary Eq. (11)) was used to fit Ψ, the ratio of the amplitude of the incident and reflected light beams and Δ, the ratio of the phase lag of the incident and reflected light beams, over the wavelength range 375–1000 nm. The model-derived optical constants are plotted in Supplementary Fig. 15, which shows that the absorption is negligible in the entire visible range.

Micro-spectroscopy measurements. The transmission/reflectance was measured using a bespoke microscope setup, we measured the light transmission for regions of individual beetle scales and the synthetic structured cellulose acetate films. The light source was a Tungsten light source, focused onto the sample using a long working lens (100 mm), the light was collected using a ×50 objective (Mitutoyo Plan Apo SL infinity corrected) with a numerical aperture (NA) = 0.42 and passed to an imaging spectrograph (Andor Shamrock SR193i). The data capture was performed using the Andor Solis software. A background without the lamp impinging on the spectrometer was collected to account for the electrical dark current. The optical transmission (T) through the glass substrate was collected for each sample measurement followed by the beetle scale/synthetic cellulose acetate region of interest. The field of view for each image entirely filled by a region of the beetle scale; a number of measurements were collected for *Cyphochilus* and *L. stigma*, as well as the cellulose acetate films. Reflectance was calculated as 1−T, which can be considered appropriate due to the negligible absorption of chitin[52] and cellulose acetate (Supplementary Fig. 13) in the visible range and the excitation NA (~0.08) being much smaller than collection NA (0.42).

Spin-echo small-angle neutron scattering. The beetle scale samples were prepared using a scalpel blade to remove elytra from *Cyphochilus* beetles. Individual elytra were stacked together and wrapped in Aluminium foil, which is transparent to thermal neutrons. The SESANS data for the *Cyphochilus* scales on the elytra were collected on the dedicated SESANS instrument at TU Delft in Holland. The number of wings required was determined through trial and error by increasing the number of wings in the beam until sufficient depolarisation of the beam was observed. The final number of elytra used was 28. By estimating the number of scales inside a known area of the wing, an approximate scale density was calculated to be ~9.7×10^{-5} scales/μm^2, making a grand total of ~3.7×10^5 scales for 28 elytra. The SESANS data for the CA films were taken on Larmor at the ISIS Spallation Neutron and Muon Source. A total of 30 films were sufficient for depolarisation of the beam. The films were measured in three different orientations with the films mounted vertically, horizontally and at an angle of ~36°. The films were measured with neutrons with a wavelength range of 2–10 Å, a radio frequency of 1 MHz and a beam size of about 5 mm × 5 mm. The data were collected with a count time of 30 min for magnetic field angles of 20, 50 and 75° giving a spin echo range out to 7 μm.

Data availability
All relevant data for this manuscript are available from the authors.

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Author contributions

A.J.P., D.M., R.A.L.J. and J.P.A.F. conceived the study. A.P. selected from a cross section of opacifying structures from the NHM. A.J.P performed SEM of Beetle scales, optical microscopy and reflectance measurements with C.V. FIBSEM work and analysis was carried out by S.J.M., S.D. and M.H. TEM of the Beetle scales by C.H. S.B., A.W., A.D. and J.V. performed the X-ray tomography at the ESRF. S.B. reconstructed the data, and calculated the structural parameters from this data. M.C. and W.F. provided access to high-performance computing resources and expertise on research software, methods and workflow. N.C. performed the 3D late stage liquid–liquid phase separation simulations for a series of different volume fractions. D.M.C. undertook the FDTD analysis for the X-ray intra-scale structures and the computer simulated Cahn–Hilliard probe structures. D. M.C. also built the micro-optical setup used to measure the reflectance and the transmission of the beetle scales. S.B., A.B., A.W., S.P., R.D., O.O.M. and A.J.P. conducted the kinetic SAXS measurements on the synthetic system and A.J.R. helped analyse the early stage USAXS data for the synthetic CA system. S.B., S.R.P., R.M.D, A.W. and A.J.P measured the SESANS signals from the biological and synthetic samples. A.J.P. wrote the initial draft of the manuscript with input and revisions from all authors.

Additional information