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Why are fiscal multipliers asymmetric? The role of credit constraints*

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Abstract

Recent empirical evidence strongly points to the state-dependence of fiscal multipliers which are larger in recessions than in expansions. Yet, standard business cycle models face great difficulty in producing such asymmetric fiscal policy effects. By incorporating endogenously binding collateral constraints into a medium scale DSGE model, we find that fiscal effectiveness can vary substantially across the business cycle. The key to our framework is the state-dependent nature of collateral constraints; binding in bad times while slack in good times, amplifying the effectiveness of fiscal policy and hence generating fiscal multipliers that are larger during recessions.

Key words: fiscal policy; fiscal multipliers; housing market; collateral constraints; recessions.

JEL Classification: E21, E62, H31.

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1 Introduction

Substantial fiscal stimulus packages adopted in response to the 2008-09 global financial crisis revived the interest in the effectiveness of fiscal policy, particularly in downturns. A key finding from the ensuing empirical work has been that fiscal multipliers are state-dependent: larger in recessions when there is spare capacity in the economy, and smaller in upturns. For example, Auerbach & Gorodnichenko (2012), Auerbach & Gorodnichenko (2013), Baum & Koester (2011) and Fazzari et al. (2015), find government spending multipliers range from near zero at the peak of the business cycle to 1.6 or greater during recessions. Similarly, Tagkalakis (2008) shows that fiscal policy has been more effective in expanding private investment during recessions compared to expansions in OECD countries. Bachmann & Sims (2012) document the non-linearity in government spending multipliers and show that this is due to different types of policy governments pursue in upturns versus in downturns. Although other papers find smaller variation (see for example Owyang et al. 2013, Ramey & Zubairy 2018) there is now significant empirical support for fiscal multipliers that vary across the cycle.

Despite such widespread evidence, formal work on the state-dependence of fiscal effectiveness seriously lags behind. That is perhaps not surprising given the difficulty standard business cycle models face in generating asymmetries in dynamics. To the best of our knowledge, there are only two attempts in the existing literature to formally answer the question of why fiscal policy is more effective in bad times. In the first, Michailat (2014) demonstrates that the effect of fiscal expansion varies across the stages of the business cycle by utilizing a simple New Keynesian framework with search and matching employment frictions. An increase in public employment increases the tightness of the labour market and crowds out private employment; this effect is stronger in expansions (when employment is already high and the labour market tight) than in recessions, leading to the public employment multiplier doubling (from 0.24 to 0.49) when the unemployment rate rises from 5 per cent to 8 per cent.

The second formal explanation for the asymmetric effects of fiscal policy is provided by Canzoneri et al. (2016) who base their state-dependent multipliers on costly financial intermediation. By incorporating countercyclical variation in bank intermediation costs into the model of Curdia & Woodford (2010), Canzoneri et al. arrive at fiscal multipliers that are state-dependent. In the presence of financial frictions that are aggravated in recessions, an expansionary fiscal action facilitates more borrowing by reducing the interest rate spread, which is itself countercyclical.¹ This, in turn, allows fiscal policy to be more effective in

¹ Similarly, the countercyclical nature of financial intermediation and its role on the state-dependence of

expanding output in bad times than in good times. While Canzoneri et al. (2016) get a significant state-dependence in the short run (the impact multiplier during expansions is approximately 1, as opposed to 2 during recessions), the difference disappears in the medium horizon.

In this paper, we propose an alternative explanation for the asymmetric effects of fiscal policy by developing a tractable model based on endogenously binding borrowing constraints. Building on Guerrieri & Iacoviello (2017), we incorporate collateral constraints that are tied to the value of housing wealth into a medium scale dynamic stochastic general equilibrium (DSGE) model. In this framework, a share of households face borrowing constraints which are binding in normal times and recessions but become ‘slack’ during expansions when their consumption is high. As a result, during recessions any additional income from fiscal expansion and associated loosening of their borrowing constraint is spent on consumption; however, during expansions the borrowing constraint is slack, and the marginal utility of consumption is lower, and additional income is smoothed across time, which results in lower output increases. Therefore, fiscal policies which raise household income when the marginal propensity to consume is higher (when the borrowing constraint is binding) will have a larger impact than when this is not the case.

While the fact that models with credit-constrained consumers produce higher fiscal multipliers is well-understood, these agents are permanently constrained in much of the existing work, at odds with state-dependency of responses to fiscal policy (see, for example, Galí et al. 2007, Kaplan & Violante 2014). A key advantage of our framework is the endogenous nature of the slackness in the credit constraint in our model, which allow us to establish the state-dependence of multipliers. In order to examine the potential asymmetries in fiscal policy, we construct a medium-scale New Keynesian DSGE model with eight fiscal instruments. Our model economy is populated by two types of households: patient (lenders) and impatient (borrowers). Both households supply labour to firms and the government, consume the final good and accumulate housing; however, impatient households discount the future at a higher rate and, as a result, borrow from patient households who also lend to the government and accumulate physical capital. Central to our framework is the explicit treatment of housing wealth, which has a key role in determining the value of the collateral constraints for impatient agents, and therefore the implications of the fiscal shocks. The model features nominal rigidities in price and wage setting and real frictions of adjustment costs, monopolistic competition in the non-residential good sector and capital utilisation

fiscal policy is also explored by Faria-e Castro (2017) in a paper studying the effectiveness of the US fiscal policy during the global financial crisis. It is shown that following the global financial crisis the fall in private consumption would have been worse by a third in the absence of the fiscal stimulus in the US.

costs.

We find that fiscal policy is indeed state-dependent and fiscal effectiveness varies substantially across the cycle. Moreover, the rich fiscal structure we employ in our framework allows us to calculate the state dependence of fiscal policy for a large number of fiscal instruments. For example, we find four quarter cumulative spending multipliers to be, on average, 49 per cent lower during consumption booms compared to when the borrowing constraint is always binding; tax multipliers are on average 33 per cent lower in booms. We find clear heterogeneity across fiscal instruments; multipliers in targeted transfers vary the most between downturns relative to normal times, as these policies strongly rely on the consumption dynamics of impatient households. Our consideration of such an extensive set of fiscal instruments allows us to generalize our results and identify new outcomes such as in the case of capital taxes, where expansionary policy (a cut in taxes) leads to a substitution from labour to capital, and subsequently lower incomes for credit-constrained agents. Under this scenario, having more access to borrowing in the boom allows these households to mitigate the impact of the policy, increasing their consumption in addition to the expansionary effects from the policy of increasing the productive capacity of the economy. Our results further suggest that it is the credit conditions of agents which determine the asymmetry of fiscal multipliers and not the fiscal action itself, as the size and direction of the latter plays a limited role in the former. That is, only shocks to transfers and labour taxes can have a substantial effect on access to credit for impatient agents and therefore, for the majority of policies, the size and expansionary/contractionary nature of the fiscal action does not lead to asymmetries itself. The implication of this is that it is the underlying economic environment that determines the impact of fiscal policy, not the size or the direction of fiscal action.

Moreover, the asymmetries in the effectiveness of fiscal policy persist in the long-run, in contrast to Canzoneri et al. (2016) who find the non-linearity of their state-dependent multipliers diminishing beyond ten quarters; this persistence better matches the empirical results which typically look at multipliers over the medium term (for example Auerbach & Gorodnichenko 2012, measure output multipliers over five years). Furthermore, our modelling assumptions mean that higher fiscal multipliers are present in both normal times as well as in downturns, making them the rule rather than the exception; consistent with the empirical estimates from Tagkalakis (2008) and Fazzari et al. (2015).

An additional advantage of our framework with its rich set of policy instruments is that we can explore the state-dependence of fiscal multipliers in nine separate cases: five government spending policies (government consumption, government investment, transfers, targeted transfers and public employment) and four tax instruments (employer social security contributions and labour, consumption and capital taxes). Given that the existing two

theoretical studies employ one type of fiscal multiplier each - public employment in Michailat (2014) and government consumption in Canzoneri et al. (2016) - it is important to establish whether the state-dependence of fiscal multipliers is limited to certain instruments or applies generally. Doing so also allows us to map our results to the estimated fiscal multipliers which varies substantially across different types of public spending (see, for example, Auerbach & Gorodnichenko 2013). More importantly, our findings on the state-dependency of individual fiscal multipliers enable us to present policy prescriptions for disaggregated fiscal policy, with crucial implications for policy design, particularly in downturns.

The rest of the paper is organized as follows. Section 2 presents a detailed description of our model economy and the policy-making structure. Section 3 provides a number of fiscal experiments towards uncovering the state-dependent nature of fiscal policy effectiveness. Further extensions and robustness checks are presented in Section 4. Section 5 assesses the empirical relevance of our framework with occasionally binding constraints by using Simulated Method of moments and discusses our results within the context of the existing empirical literature. Finally, Section 6 concludes.

2 The model

Our model builds upon that of Guerrieri & Iacoviello (2017) in two clear ways: first, we endogenise the production of the residential (durable) good; and second, we develop a full fiscal sector with eight policy instruments and nine policy experiments.² In what follows, we present the key features of the model structure; the rest of the model description is presented in a supplementary technical Appendix.

2.1 Households

As in Iacoviello & Neri (2010) there is a continuum of measure 1 of households in each of the two groups: ‘patient’ and ‘impatient’. Both types of household consume residential and non-residential goods and supply labour to production. The key difference between the two types of households is that the patient discounts the future at a lower rate than the impatient and hence the former are lenders to the latter; the value of housing stock of the impatient agents acts as collateral against their borrowing, as in Iacoviello (2005).

²The endogenised production of housing brings the model closer to that of Iacoviello & Neri (2010) and Alpanda & Zubairy (2016) (among others) and provides a more realistic framework of the economy whereby the housing stock can vary with the macroeconomic climate and can further have a feedback effect on the economy. We perform sensitivity of our results to this assumption which are discussed in Section 4.3.

Patient Households

The utility function for each patient household is given by:

$$E_0 \sum_{t=0}^{\infty} \beta^t \varepsilon_t^B \left(\Gamma_c^P \ln (C_t^P(i) - h^P C_{t-1}^{P*}(i)) + \varepsilon_t^H \sigma_h \ln (H_t^P(i)) - \frac{1}{1 + \sigma_l} (L_t^P(i))^{1+\sigma_l} \right) \quad (1)$$

where superscript P is used for patient agents, i indicates a particular household, and t represents time; β is a subjective discount factor; σ_l is the inverse elasticity of labour (L); σ_h denotes a weight on housing in utility; ε_t^B , and ε_t^H denote shocks to intertemporal preferences and housing preferences as in Iacoviello & Neri (2010); C^P and H^P represent consumption of the final good and housing, respectively; h^P denotes the external habit parameter, C^{P*} denotes average consumption of Patient households, and Γ_c^P is a scaling factor as in Iacoviello & Neri (2010).³ Each patient household receives income from the following sources: their after tax labour income $(1 - \tau_t^l)(w_t^P(i)L_t^P(i))$, where τ_t^l and w_t^P denote the labour tax and wage rate; the after tax capital income $(1 - \tau_t^k)[r_{n,k,t}u_{n,t}(i)\bar{K}_{n,t-1}(i)]$, where τ_t^k denotes the capital tax rate, and \bar{K}_n , u_n and $r_{n,k}$ ($n \in \{c, h\}$) denote the physical stock of capital, the utilisation and rental rate of capital used in the production of the consumption ($n = c$) and the housing good ($n = h$); the after tax dividend income $(1 - \tau_t^k)div_t(i)$; interest income from holdings of government bonds (B) and loans to the impatient agents (LO), $((R_{t-1} - 1)/\pi_t)(B_{t-1}(i) + LO_{t-1}(i))$, where R_{t-1} is the gross nominal interest rate on one period bonds and $\pi_t = P_t/P_{t-1}$ is gross inflation; and, lump sum transfers from the government $\mu \Gamma R_t$, where μ is the share of government transfers received by patient households.

Each patient household i spends: $(1 + \tau_t^c) C_t^P(i)$ on the final consumption good where τ_t^c denotes the consumption tax rate; $\sum_{n=c,h} I_{n,t}(i) = I_{c,t}(i) + I_{h,t}(i)$ on investment in physical capital in the consumption and the housing producing sectors, respectively; $q_t[H_t^P(i) - (1 - \delta_h)H_{t-1}^P(i)]$ on residential property where $q_t = P_{h,t}/P_t$ denotes relative price of housing and δ_h the depreciation of housing; $(LO_t(i) - LO_{t-1}(i)/\pi_t)$ and $(B_t(i) - B_{t-1}(i)/\pi_t)$ on loans to impatient households and purchases of government's bonds; and on costs arising from changes in the level of the capital utilisation rate in both the consumption and housing sectors, $a(u_{n,t})\bar{K}_{n,t-1}(i)$.⁴ Investment increases the stock of physical capital according to:

³The scaling factor $\Gamma_c^P = (1 - h^P)/(1 - \beta h^P)$ ensures, as in Iacoviello & Neri (2010), that the steady-state is not affected by habit persistence. The utility function does not allow for habit persistence in housing; in a model similar to ours, Iacoviello & Neri (2010) estimate habit persistence in housing and find estimates insignificant from zero.

⁴Note that when combining the net purchases of government bonds $(B_t - B_{t-1}/\pi_t)$ with the income from these bonds as presented above $[(R_{t-1} - 1)/\pi_t]B_{t-1}$, the net result would simply be to have B_t on one side of the budget constraint and $R_{t-1}B_{t-1}/\pi_t$ on the other (with a similar condition for loans), as presented in

$$\bar{K}_{n,t}(i) = (1 - \delta_{n,k})\bar{K}_{n,t-1}(i) + \left[1 - S\left(\frac{I_{n,t}(i)}{I_{n,t-1}(i)}\right)\right] \varepsilon_t^I I_{n,t}(i) \quad (2)$$

where ε_t^I as in Smets & Wouters (2007) denotes a shock to the price of investment relative to consumption goods. The flow budget constraint of the patient household can then be represented in real terms by:

$$\begin{aligned} & \sum_{n=c,h} I_{n,t}(i) + (1 + \tau_t^c) C_t^P(i) + q_t [H_t^P(i) - (1 - \delta_h)H_{t-1}^P(i)] + LO_t(i) + B_t(i) \\ &= (1 - \tau_t^l) (w_t^P(i)L_t^P(i)) + \mu TR_t + A_t^P(i) + \frac{R_{t-1}}{\pi_t} (B_{t-1}(i) + LO_{t-1}(i)) \\ &+ (1 - \tau_t^k) \left[\sum_{n=c,h} r_{n,k,t} u_{n,t}(i) \bar{K}_{n,t-1}(i) + div_t(i) \right] - \sum_{n=c,h} a(u_{n,t}(i)) \bar{K}_{n,t-1}(i) \quad (3) \end{aligned}$$

where A_t^P denote state contingent securities, the presence of which implies that households are homogeneous with respect to consumption and assets choices; households are assumed to supply differentiated labour, and as such, without these securities would otherwise receive different income and have different expenditure allocations.⁵ Each patient household maximizes utility subject to the budget constraint, the capital accumulation equations and the demand for labour. Wages are set subject to Calvo (1983) frictions.

Impatient Households

The utility of impatient households evolves according to:

$$E_0 \sum_{t=0}^{\infty} \gamma^t \varepsilon_t^B \left(\Gamma_c^I \ln (C_t^I(i) - h^I C_{t-1}^{I*}(i)) + \varepsilon_t^H \sigma_h \ln (H_t^I(i)) - \frac{1}{1 + \sigma_l} (L_t^I(i))^{1+\sigma_l} \right) \quad (4)$$

Each impatient household i faces a flow budget constraint which states that net labour income $(1 - \tau_t^l)(w_t^I(i)L_t^I(i))$, transfers $(1 - \mu)TR_t$, and the net acquisition of new loans $LO_t(i) - (LO_{t-1}(i)/\pi_t)$ should match total expenditure made up of: interest payments on

equation (3).

⁵Note that in this specification, taxes on capital income are applied to dividends and income on physical capital and not on income generated from holdings in government debt. This is in line with much of the existing literature (see for example Leeper, Walker & Yang 2010, Leeper, Plante & Traum 2010, Trabandt & Uhlig 2011, Drautzburg & Uhlig 2015); we test and discuss the importance of our results to this assumption in Section 4.3.

outstanding loans $((R_t - 1)/\pi_t)LO_{t-1}(i)$; the expenditure on consumption $(1 + \tau_t^c)C_t^I(i)$; and the net acquisition of housing $q_t(H_t^I(i) - (1 - \delta_h)H_{t-1}^I(i))$. The impatient agents' budget constraint is therefore given by:

$$\begin{aligned} \frac{(R_{t-1} - 1)LO_{t-1}(i)}{\pi_t} + (1 + \tau_t^c)C_t^I(i) + q_t(H_t^I(i) - (1 - \delta_h)H_{t-1}^I(i)) \\ = LO_t(i) - \frac{LO_{t-1}(i)}{\pi_t} + (1 - \tau_t^l)w_t^I(i)L_t^I(i) + (1 - \mu)TR_t + A_t^I(i) \end{aligned} \quad (5)$$

The maximum that an impatient agent can borrow is defined by the constraint:

$$LO_t(i) \leq (1 - \tau)q_tH_t^I(i) \quad (6)$$

where τ denotes the ratio of the down-payment to the value of housing. This constraint states that the value of the loan has to be less than or equal to the value of housing, adjusted by the down-payment $(1 - \tau)q_tH_t^I(i)$. Each impatient household maximizes utility subject to the budget constraint, the borrowing constraint and the demand for labour.

2.2 Non-residential good sector

Final good sector

The final good Y is produced by combining differentiated intermediate products using CES technology, $Y_t = [\int_0^1 Y_t(j)^{(v_p-1)/v_p} dj]^{v_p/(v_p-1)}$, where $v_p \geq 1$ denotes the elasticity of substitution among the differentiated outputs of intermediate firms and $Y_t(j)$ denotes output of j^{th} producer. The retail firm chooses $Y_t(j)$ and maximises profit of the form:

$$Prof_t = P_t Y_t - \int_0^1 P_t(j) Y_t(j) dj \quad (7)$$

where P_t is the price of the composite good and $P_t(j)$ denotes the price of the intermediate firm j . The first order condition results in the demand equation for the output of intermediate producer j , $Y_t(j) = (P_t/P_t(j))^{v_p} Y_t$, and the zero profit condition implies a price index of $P_t = \int_0^1 P_t(j)^{1-v_p} dj^{1/(1-v_p)}$.

Intermediate good sector

The production technology of the monopolistically competitive intermediate good producers is given by the Cobb-Douglas function:

$$Y_t(j) = \varepsilon_t^{A,c} K_{c,t-1}^\alpha \left[(N_{c,t}^P(j))^{b_1} (N_{c,t}^I(j))^{1-b_1} \right]^{1-\alpha} K_{g,t-1}^{\sigma_g} - \Phi \quad (8)$$

where $\varepsilon_t^{A,c}$ denotes a productivity shock, $K_{g,t-1}$ and $K_{c,t-1}(j)$ denotes public and private capital services, respectively; $N_{c,t}^P(j)$ and $N_{c,t}^I(j)$ denote labour supplied by the patient and impatient households, respectively; α denotes the share of capital in production; b_1 stands for the share of patient households in total labour used in production; Φ is a fixed cost; and σ_g denotes the elasticity of output with respect to public capital. Monopolistic producers choose $K_{c,t-1}(j)$, $N_{c,t}^P(j)$, and $N_{c,t}^I(j)$ to minimise total real costs of production subject to the available technology, where all prices of inputs are taken as given. Monopolistic producers are also price setters, and prices are subject to Calvo (1983) frictions. In particular, in each period a share of firms, θ_p , are unable to re-optimize their prices and they simply increase prices by the central bank's target rate of inflation.

2.3 Residential good sector

The competitive residential good producers use capital, K_h , and labour of patient and impatient households, N_h^P and N_h^I , to produce the residential output (HI) using Cobb-Douglas production function of the form:

$$HI_t = \varepsilon_t^{A,h} K_{h,t-1}^{\alpha_h} \left[(N_{h,t}^P)^{b_1} (N_{h,t}^I)^{1-b_1} \right]^{1-\alpha_h} K_{g,t-1}^{\sigma_g} \quad (9)$$

where $\varepsilon_t^{A,h}$ denotes a housing sector-specific productivity shock and α_h is the capital share in the production of housing. Both producers of the non-residential and residential good are subject to employers' social security contributions (τ^{er}) which adds a tax proportional to the total labour costs of the firm. Note that public capital $K_{g,t}$ enters the production function of both the immediate goods producer (8) and the residential good producer (9) in the same way, in this respect, government capital is a public good as it is non-excludable and non-rivalrous.

2.4 Monetary Policy

We adopt a standard formulation of monetary policy where policy-makers follow a Taylor rule through which the nominal interest rate responds to movements in both output and inflation with some persistence (ρ):

$$R_t = \max \left\{ 1, R \left(\frac{R_{t-1}}{R} \right)^\rho \left[\left(\frac{(\pi_t^A)^{0.25}}{\bar{\pi}} \right)^{\rho_\pi} \left(\frac{GDP_t}{GDP} \right)^{\rho_y} \right]^{1-\rho} \varepsilon_t^R \right\} \quad (10)$$

where ε_t^R is a monetary shock; GDP represents gross domestic product which is given by $GDP_t = Y_t + qHI_t + (1 + \tau_t^{er})(w_t^P N_{g,t}^P + w_t^I N_{g,t}^I)$ where $N_{g,t}^P = \vartheta_g N_t^P$ and $N_{g,t}^I = \vartheta_g N_t^I$ represent public employment of patient and impatient agents; $\bar{\pi}$ is the central bank's target rate of inflation and $\pi_t^A = P_t/P_{t-4}$ is annual inflation rate; ρ_π and ρ_y , denote respectively, the policy maker's aversion to deviations of inflation and output from their respective steady-state values.⁶ Variables with no time subscript represent steady-state values. As in Iacoviello & Neri (2010), the formulation in (10) maintains that the nominal interest rate does not respond directly to variation in house prices.

2.5 Fiscal policy

The government budget constraint requires that spending on consumption (G_c), investment (I_g), transfers (TR) and public employment (N_g^P and N_g^I), as well as the repayment of previous period debt, is equal to tax receipts from the four revenue sources and issuance of new government debt.⁷ As such, the government budget constraint is given by:

$$\begin{aligned} & \left(\frac{R_{t-1}}{\pi_t} \right) B_{t-1} + G_t + I_{g,t} + TR_t \\ & = \tau_t^c (C_t^P + C_t^I) + \tau_t^l (w_t^P L_t^P + w_t^I L_t^I) + \tau_t^{er} (w_t^P N_t^P + w_t^I N_t^I) \\ & \quad + \tau_t^k (r_{k,c,t} u_{c,t} \bar{K}_{c,t-1} + r_{k,h,t} u_{h,t} \bar{K}_{h,t-1} + div_t) + B_t \end{aligned} \quad (11)$$

where $G_t = G_{c,t} + (1 + \tau_t^{er})(w_t^P N_{g,t}^P + w_t^I N_{g,t}^I)$. For transfers, we adopt two scenarios: one where transfers are spread evenly across patient and impatient households ($\mu = b_1$, where b_1 is the share of patient households in total labour used in production); and another where transfers are targeted to impatient agents who both have lower incomes and who respond more to changes in transfers ($\mu = 0$).⁸ In total, therefore, there are eight fiscal instruments and nine fiscal experiments at the disposal of the government (including both targeted and general transfers).

Public investment augments public capital according to:

$$K_{g,t} = (1 - \delta_{k,g})K_{g,t-1} + I_{g,t} \quad (12)$$

⁶Note that this formulation of GDP has three components: the total demand for the non-residential good (Y_t); investment in housing (qHI_t); and the wage cost of public sector employment $(1 + \tau_t^{er})(w_t^P N_{g,t}^P + w_t^I N_{g,t}^I)$ which is equal to the output of public sector.

⁷We model employment by the government to be unproductive in that the output from such employment neither enters the utility functions of agents nor the production functions of producers. The monetary value of government employment, through the payments of wages, is added to the gross domestic product of the economy.

⁸This characterisation is increasingly common in the literature, see for example Coenen et al. (2012).

where $\delta_{k,g}$ denotes the depreciation of public capital. Consistent with Ratto et al. (2009), Leeper, Walker & Yang (2010), Traum & Yang (2015) we assume no adjustment costs or utilisation rates for government capital; we test the sensitivity of our results to this in Section 4.1. Fiscal policy rules are set similar to those used by Leeper, Plante & Traum (2010). We assume that fiscal policy responds countercyclically to the movements in debt, which implies that:

$$\begin{aligned}\frac{X_t}{X} &= \left(\frac{B_t}{B}\right)^{\phi_{B,x}} \varepsilon_t^x \\ \varepsilon_t^x &= 1 + \eta_{x,t} + \eta_{x,t-1} + \eta_{x,t-2} + \eta_{x,t-3}\end{aligned}\tag{13}$$

where $x = \{\tau^c, \tau^k, \tau^l, \tau^{er}, G_c, I_g, N_g^P, N_g^I, TR\}$ is the set of fiscal instruments, and where $\eta_{x,t} \sim N(0, \sigma_x^2)$ are *i.i.d.* normally distributed errors. Shocks to fiscal instruments, therefore, last for only four quarters, with no persistence (as is adopted in Coenen et al. 2012); extensions to these shocks is conducted in Section 4.1.

2.6 Equilibrium in residential and non-residential markets

The homogeneous output of the residential good producer is purchased by patient and impatient households:

$$HI_t = H_t^P + H_t^I - (1 - \delta_h)(H_{t-1}^P + H_{t-1}^I)\tag{14}$$

The final goods market is in equilibrium when the aggregate supply equals the aggregate public and private demand in the final consumption good, investment and housing. The resource constraint is given by:

$$\begin{aligned}K_{c,t-1}^\alpha \left[(N_{c,t}^P)^{b_1} (N_{c,t}^I)^{(1-b_1)} \right]^{1-\alpha} K_{g,t-1}^{\sigma_g} - \Phi \\ = s_{1,t} [I_{c,t} + I_{h,t} + C_t^P + C_t^I + G_{c,t} + I_{g,t} + a(u_{h,t})\bar{K}_{h,t-1} + a(u_{c,t})\bar{K}_{c,t-1}]\end{aligned}\tag{15}$$

where

$$s_{1,t} = (1 - \theta_p)(\tilde{p}_t)^{-v_p} + \theta_p \left(\frac{\bar{\pi}}{\pi_t}\right)^{-v_p} s_{1,t-1}\tag{16}$$

where $s_{1,t}$ is a term denoting price dispersion.

3 Are the effects of fiscal policy state-dependent?

3.1 Time preference, borrowing constraints and consumption

To explore the asymmetries in the model, a full understanding of the consumption decisions of impatient households is crucial given that it is through the impatient agents that the non-linear effects of the policy are transmitted into the economy. The first order conditions for impatient and patient households with respect to consumption are presented in the following Euler equations:

$$(1 - \lambda_t^b) \left\{ \frac{U_{c,t}^I}{P_t(1 + \tau_t^c)} \right\} = \gamma R_t E_t \frac{U_{c,t+1}^I}{P_{t+1}(1 + \tau_{t+1}^c)} \quad (17)$$

$$\left\{ \frac{U_{c,t}^P}{P_t(1 + \tau_t^c)} \right\} = \beta R_t E_t \frac{U_{c,t+1}^P}{P_{t+1}(1 + \tau_{t+1}^c)} \quad (18)$$

where λ^b is the price of borrowing (the ratio of the Lagrange multiplier on the borrowing constraint to the Lagrange multiplier on the budget constraint), and $U_{c,t}^m = \Gamma_c^m[(\varepsilon_t^B / (C_t^m - h^m C_{t-1}^m)) - (h^m \beta \varepsilon_{t+1}^B / (C_{t+1}^m - h^m C_t^m))]$ denotes marginal utility of consumption for $m \in \{P, I\}$.

Using equation (17), it is straightforward to show that when $\lambda_t^b > 0$ the following holds:

$$\frac{U_{c,t}^I}{P_t(1 + \tau_t^c)} - \gamma R_t E_t \frac{U_{c,t+1}^I}{P_{t+1}(1 + \tau_{t+1}^c)} > 0 \quad (19)$$

Put differently, when the constraint on borrowing is binding (when the left-hand of (19) is greater than the right-hand side) impatient agents would rather borrow more than they are permitted. This, in turn, is when the marginal utility of additional consumption ($U_{c,t}^I / (P_t(1 + \tau_t^c))$) is greater than the expected cost of this borrowing ($\gamma R_t E_t U_{c,t+1}^I / (P_{t+1}(1 + \tau_{t+1}^c))$) to the impatient agent. In this situation, any additional income in the current period (including any extra borrowings from the loosening of the borrowing constraint) is used for contemporaneous consumption. This suggests that when impatient consumption in the current period is sufficiently high the constraint on their borrowing is no longer binding ($\lambda_t^b = 0$) and the two Euler equations of patient and impatient households become similar. Intuitively, this is when the marginal utility of additional consumption from extra borrowing is equal to the expected cost of this borrowing. Put differently, when $\lambda_t^b = 0$ impatient agents smooth any additional increase in income over the period in which they expect the borrowing constraint to be slack. In doing so, they reduce interest payments and this allows for a slightly higher

consumption profile in the longer horizon.⁹

Iterating forward the Euler equations in (17) and (18) provides:

$$U_{c,t}^I = \prod_{l=0}^{i=\infty} E_t \left\{ \frac{\gamma}{1 - \lambda_{t+l}^b} \frac{R_{t+l}}{\pi_{t+1+l}} \frac{1 + \tau_{t+l}^c}{1 + \tau_{t+1+l}^c} \right\} \quad (20)$$

$$U_{c,t}^P = \prod_{l=0}^{i=\infty} E_t \left\{ \beta \frac{R_{t+l}}{\pi_{t+1+l}} \frac{1 + \tau_{t+l}^c}{1 + \tau_{t+1+l}^c} \right\} \quad (21)$$

which confirms the intuition from above. When $\lambda_t^b = 0$ the two equations become similar, where the difference in discount rates mean that the impatient bring more consumption forward than the patient. In this situation, impatient households smooth any additional income over the horizon in which the borrowing constraint is slack ($\lambda_t^b = 0$) and their borrowing is lower than the constraint permits. The presence of λ_t^b in (17) implies that any loosening of the borrowing constraint results in higher consumption today, whereas a tightening of the constraint has the reverse effect.

3.2 Policy experiments

Provided that the constraint on borrowing for impatient agents is always binding ($\lambda^b > 0$) these agents borrow all that is permitted and there are no asymmetries in the dynamics from the model; that is, the impact of shocks in the model is symmetric. Therefore, in order to identify non-linear effects of fiscal policy, this borrowing constraint needs to not bind for some time interval; this will happen when consumption today is so high that the marginal utility gained from further borrowing (and therefore further consumption) is equal to the marginal cost of borrowing, as stipulated by (19). In this environment, shocks of the same magnitude will have different effects depending on how long the borrowing constraint on impatient households does not bind, or is ‘slack’. In order to get the constraint to not bind, as in Guerrieri & Iacoviello (2017) we use a housing preference shock (ε^H in (1) and (4) such that the stock and value of housing increases for impatient and patient agents, therefore increasing the borrowing potential of these households and thus consumption; we then increase the size of this shock in order to increase the number of periods in which the

⁹Note that in the steady-state the borrowing constraint of impatient households is binding: $\lambda^b = 1 - \gamma/\beta > 0$ as $\gamma < \beta$. We impose the restriction $\lambda_t^b \geq 0$ implying that impatient agents either wish to borrow ($\lambda_t^b > 0$) or are indifferent between borrowing and saving ($\lambda_t^b = 0$); a similar restriction is also adopted in Guerrieri & Iacoviello (2017).

constraint does not bind.¹⁰

To calculate the size of fiscal multipliers, we include a small fiscal shock on top of the housing preference shock such that the length of the period in which the borrowing constraint does not bind is not altered; this fiscal shock is spread equally over four quarters before it subsequently dies (as specified in (13)). We then calculate multipliers by looking at the difference in variables with the additional fiscal shock compared to the counterfactual of only including the housing preference shock in the economy. In this respect, we find what Erceg & Lindé (2014) call a ‘marginal’ multiplier as the fiscal intervention is not of sufficient size to change the state the economy. In Section 4.1 we present extensions to these fiscal experiments including where we allow for sizeable fiscal shocks such that policy can alter the time horizon over which the borrowing constraint on impatient households is not binding. The benchmark results from using the experiments as outlined above are consistent with these further extensions. Note, finally, that the period when the borrowing constraint on impatient agents binds can be considered as the multiplier corresponding to both ‘normal’ and recessionary times, whilst when it does not bind the economy is experiencing good times or a ‘boom’; the longer the constraint does not bind, the longer the boom.

In order to quantify the impact of policy on output, we employ the following metric to calculate cumulative fiscal multipliers (M):

$$M_T = \frac{\sum_{j=0}^T (Y_{t+T} - Y_0)}{\sum_{j=0}^T (x_{t+T} - x_0)} \quad (22)$$

where T is the time horizon over which the multiplier is measured, x is the respective fiscal instrument, and variables with a subscript zero are outcomes corresponding to the counterfactual of no fiscal policy change. When x is a government spending instrument, we use the monetary value of the change in spending as the denominator (throughout the paper, we use the expression ‘government spending’ to represent the four spending instruments in the model in total). To ensure consistency, for tax multipliers we use the change in tax revenues were all other variables (with the exception of the relevant tax rate) to remain the same.¹¹ In solving the model, we apply the toolkit for solving dynamic models with

¹⁰In order to get the borrowing constraint not binding for an increasing period of time, we increase the size of the housing preference shock. A two (eight) quarter period of slack in the borrowing constraint requires a shock leading to an on impact increase in the house price of 0.5 (2.3) per cent. Given that an estimated one standard deviation housing preference shock leads to an approximate increase of 2 per cent in the house price in Guerrieri & Iacoviello (2017), it is clear that the magnitude of the required shock to ensure the slackness of the borrowing constraint is well within the range observed in the data. Guerrieri & Iacoviello (2017), for example, in an estimated version of their model, find the borrowing constraint on impatient agents to have been slack between 1998 and 2006.

¹¹For government spending instruments (G_C, I_G, N_g, TR) we set each shock such that the change is equal to 0.01% of steady-state output. To ensure comparability of multipliers across fiscal instruments, we shock

occasionally binding constraints developed in Guerrieri & Iacoviello (2015).

3.3 Calibration

We calibrate the model using the values adopted in the previous literature and data from the US between 1985 and 2016, as outlined in Table 1. We set the ratio of government consumption, investment, transfers to output and the share of public employment to total employment to match the averages in the data for the period 1985-2016 (we take 1985 as the starting point to be consistent with Guerrieri & Iacoviello 2017).¹² The calibration is in line with Trabandt & Uhlig (2011), Drautzburg & Uhlig (2015) and Alpanda & Zubairy (2016) who calibrate government consumption to GDP to 18%, 15.3% and 18% respectively, and Drautzburg & Uhlig (2015) who calibrate government investment to GDP to 4%.¹³ In setting the tax rates we rely on the dataset and methods used in Trabandt & Uhlig (2011). For the purpose of this paper we modify their work in two dimensions: first, we recalculate the tax rates so that our starting point is 1985 (their average tax rates are calculated for the period from 1995); and second, we include both labour income taxes and employers' social security contributions (whereas Trabandt & Uhlig 2011, combine both in one tax rate.)¹⁴

For the majority of the remaining parameters, we follow the calibration in Guerrieri & Iacoviello (2017), as outlined in Table 1. The exception to this is that our capital utilisation cost and investment adjustment cost are based on the estimated values in Iacoviello & Neri (2010). The elasticity of fiscal instruments to debt ($\phi_{B,x}$) is set to 0.2 which means that all instruments are used to ensure government solvency and respond slowly to bring debt to its steady-state; debt as a result of fiscal shocks is halved after 34 quarters, and sensitivity to this parameter is performed in Section 4.1. We set the elasticity of output with respect to public capital equal to 0.02 which is in line with the range of estimates discussed in Leeper, Walker & Yang (2010). We then set the depreciation rate of public capital to 0.015 to match the ratio of public capital to GDP in the data. The estimates of habit

tax rates such that the change in the steady-state tax revenue is also equal to 0.01% of steady-state output. This size of shock ensures that the horizon over which the borrowing constraint on impatient agents is not binding is unaffected.

¹²All the data used to calculate the steady-state shares are taken from the Bureau of Economic Analysis. Data on private consumption expenditure, non-residential investment, and residential investment are from Table 1.1.5. Data on public consumption, investment and transfers are taken from Table 3.1. Data on public capital, private residential and non-residential capital are from Table 1.1. Data on physical capital in the residential production sector are taken from Table 3.1ESI. Data used to calculate the share of employees working in the public sector are taken from Table 6.4B.

¹³None of these models include public employment, and in all three the level of transfers is fixed through the calibration of other parameters.

¹⁴The inclusion of either employers' social security contributions or public employment (and, to a lesser extent, government investment) are uncommon assumptions in the literature. Therefore we test the sensitivity of our results to a model which do not include these; see Appendix A for further details.

persistence in non-residential consumption for patient and impatient agents is taken from Iacoviello & Neri (2010) for the period 1989-2006 who also estimated habit persistence in housing to be indiscernible from zero. We calibrate the weight of housing in the utility function and the depreciation of housing to match the ratio of housing wealth to GDP and of residential investment to GDP; this implies a utility weight of 0.093 and a depreciation rate of 0.0101, values very close to the ones used in Iacoviello & Neri (2010). Since Guerrieri & Iacoviello (2017) do not use housing production, we use the share of physical capital in production from Iacoviello & Neri (2010). Given the shares of capital in production, the capital income tax rate and the patient households' discount rate, we set the depreciation of both residential and non-residential capital to match the investment and capital to GDP ratios in the data. The depreciation rate of non-residential capital is set at 0.0145, similar to those used in Drautzburg & Uhlig (2015) and Alpanda & Zubairy (2016) and depreciation rate of residential capital (0.03) is in line with Iacoviello & Neri (2010).

To assess the reliability of our calibration, we compare four quarter output multipliers from our benchmark model specification (where borrowing constraints are always binding) to those presented in Coenen et al. (2012).¹⁵ In general, our multipliers fit within the range of estimates from the different models utilised in Coenen et al. (2012). The one exception is for consumption taxes, where we get higher multipliers; this is driven by the fact that our benchmark calibration for habit formation in consumption (for which we used the estimated results from Iacoviello & Neri 2010) are lower. As is seen in Section 4.3, calibrating higher levels of habit persistence in consumption brings our consumption tax multipliers in line with those presented in Coenen et al. (2012) and has a limited effect on the key findings in our analysis.

3.4 Dynamics

In order to explore the transmission mechanism through which fiscal policy impacts upon impatient agents' consumption (and subsequently the broader economy), we present dynamics from two fiscal experiments involving a shock to transfers (Figure 1) and government consumption (Figure 2). In these plots the period over which the borrowing constraint on impatient agents is slack varies between zero and 18 quarters.¹⁶ As discussed in Section 3.2,

¹⁵Coenen et al. (2012) compute fiscal multipliers across seven instruments for a number of models used by policy institutions. Following their work, we also distinguish between targeted and general transfers, where targeted transfers go only to impatient agents and general transfers are spread evenly across the two types of households.

¹⁶This is in line with Guerrieri & Iacoviello (2017) who show that the borrowing constraints were slack in the USA between 1998 and 2006 and the subsequent housing collapse lead to tightening of borrowing constraints which exacerbated the recession of 2008-2009.

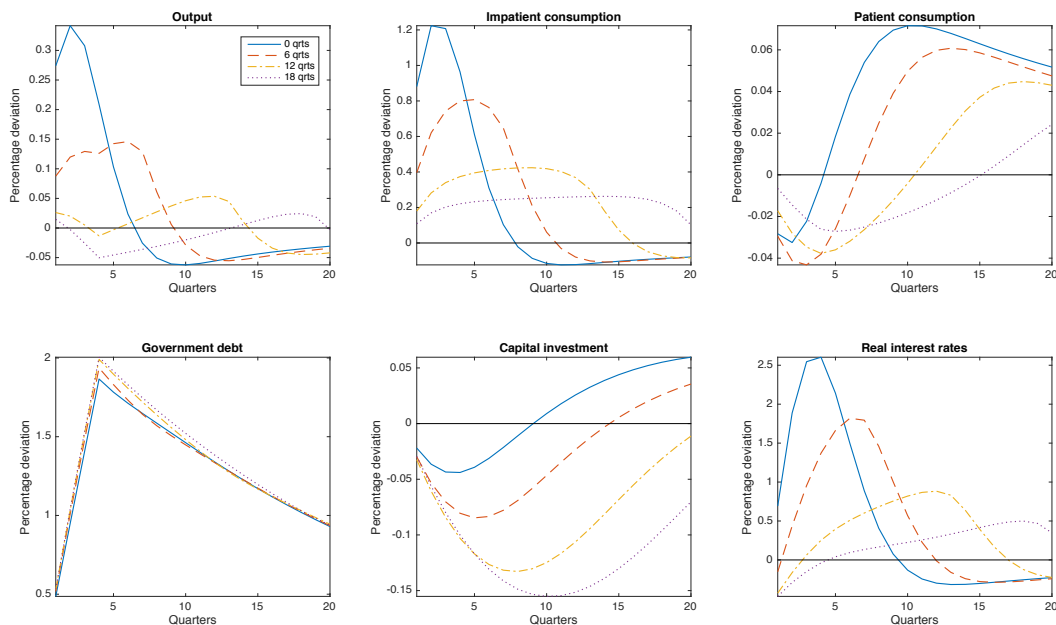
Table 1: Calibration

Parameter	Description	Value	Data/ Source
Preferences			
σ_h	Utility share of housing	0.093	*
σ_l	Frisch elasticity of labour	1	GI
h^P	Patient habit persistence	0.40	IN
h^I	Impatient habit persistence	0.61	IN
β	Patient discount factor	0.995	GI
γ	Impatient discount factor	0.9922	GI
b_1	Share of patient agents	0.5013	GI
τ	Down-payment ratio	0.1	GI
ρ_B	Persistence in housing shock	0.9835	GI
Technology			
α_c	Share of capital in non-residential production	0.3	IN
α_h	Share of capital in residential production	0.1	IN
$\delta_{k,c}$	Depreciation of non-residential capital	0.0145	*
$\delta_{k,h}$	Depreciation of residential capital	0.03	*
δ_h	Depreciation of housing	0.0101	*
$\delta_{k,g}$	Depreciation of public capital	0.0151	*
σ_g	Elasticity of output w.r.t. public capital	0.02	*
ϕ_k	Investment adjustment cost parameters	14.25	IN
κ	Capital utilisation adjustment parameter	2.2258	IN
θ_p	Price stickiness	0.9182	GI
θ_w	Wage stickiness	0.9163	GI
v_p	Steady-state price markup	0.2	GI
v_w	Steady-state wage markup	0.2	GI
Monetary policy			
ρ	Monetary policy persistence	0.5509	GI
ρ_π	Inflation Taylor rule weight	1.7196	GI
ρ_y	Output Taylor rule weight	0.0944	GI
Fiscal policy			
$\phi_{B,x}$	Response of fiscal instruments to debt	0.2	
τ^c	Consumption tax rate	0.05	TU
τ^l	Labour tax rate	0.2	TU
τ^k	Capital tax rate	0.36	TU
τ^{er}	Employers social security contributions rate	0.07	TU
G/GDP	Public consumption and employment to GDP	0.149	0.149
IG/GDP	Public investment to GDP	0.041	0.041
TR/GDP	Transfers to GDP	0.114	0.114
$\vartheta_g = N_g^I/N^I = N_g^P/N^P$	Share of public employment	0.147	0.147
Other ratios matched			
$(C_P + C_I)/GDP$	Consumption to GDP	0.645	0.645
$(I_h + I_c)/GDP$	Non-residential investment to GDP	0.123	0.123
qHI/GDP	Residential investment to GDP	0.042	0.042
$(Kc + Kh)/(4 \times GDP)$	Business capital to GDP	2.107	2.239
$q(H_I + H_P)/(4 \times GDP)$	Housing value to GDP	1.038	1.033
$Kg/(4 \times GDP)$	Public capital to GDP	0.679	0.678
$Kh/(Kc + Kh)$	Share of residential capital in total capital	0.009	0.007

The abbreviations ‘GI’, ‘IN’ and ‘TU’ refers to Guerrieri & Iacoviello (2017), Iacoviello & Neri (2010) and Trabandt & Uhlig (2011) respectively. The symbol * represents a value implied by other calibrations to fix steady-state shares to empirical values.

we get this borrowing constraint to not bind by shocking housing preferences (ε^H) and then consider the impact of policy by including a further shock to the relevant fiscal instrument.

Figure 1: Dynamics from a transfer shock



Dynamics from fiscal experiments where the borrowing constraint on impatient agents is slack for 0, 6, 12 and 18 quarters, as illustrated by the legend. In each instance, the results have been normalised to present the dynamics as a result of a shock to fiscal policy equal to one per cent of output; dynamics for each variable are presented as percentage deviations from the steady-state. The results present marginal impacts as the length of time the borrowing constraint is not binding is unaffected by the policy; the normalisation is performed on shocks equal to one-one-hundredth of this and is done for ease of presentation.

An increase in transfers increases both the income for impatient households and the level of government debt. In normal times, when $\lambda^b > 0$, impatient households convert increased incomes into increased consumption for the four quarters whilst the policy shock is active (this includes any additional borrowing arising from an increase in the value of the borrowing constraint). This is because the marginal utility of additional consumption for these households is higher than the marginal cost of borrowing, as discussed in Section 3.1. Higher demand from impatient agents brings about higher output, and inflationary pressures lead to an increase in the real interest rate which subsequently leads to a fall in consumption of patient households, as indicated in equation (21).

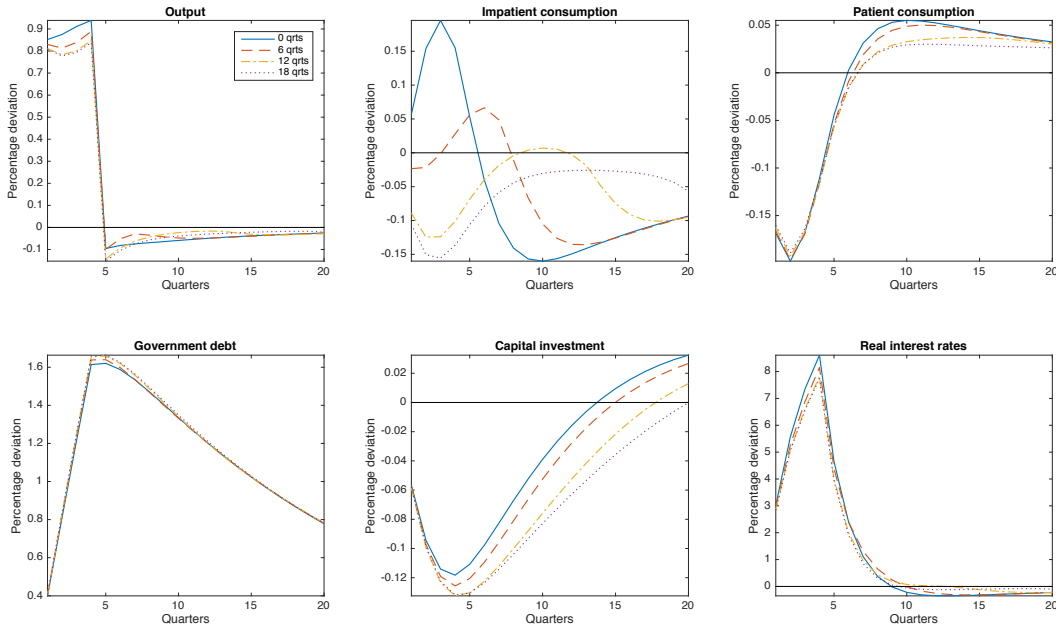
When the borrowing constraint on impatient agents is not binding, on the other hand, these agents smooth any additional income over the period in which they expect their borrowing constraint to be slack, where changes in consumption are also driven by habit persistence

(thus explaining the hump in impatient consumption over this smoothing period). This is when the marginal utility of additional consumption for these households is equal to the marginal cost of this consumption. This implies a smaller increase in impatient households' consumption in the short run, and therefore a smaller increase in output. This can be seen in the first and second panels of Figure 1 (for output and impatient agents' consumption, respectively) for differing periods over which the borrowing constraint is slack; a smoothing of impatient income leads to a smoothing of the effects of policy on output.

The smoothing actions of impatient households impacts the dynamics of patient agents in two ways: first, when the impatient borrowing constraint is not binding for a period of time, their smoothing of consumption leads to more persistent levels of inflation and subsequently higher real interest rates following the fiscal shock; and second, a smoothing of consumption by impatient agents leads to a smaller response to output arising from the fiscal action, and as such lower tax revenue and higher debt. The combination of anticipated higher interest rates and taxes (the latter needed to repay higher debt) lead patient agents' to crowd out the expenditure more when impatient agents' smooth their response to the policy, as is clear from (21). Therefore, the response of output to fiscal stimulus in the short run is determined by the actions of impatient agents which is influenced by whether they are constrained in their borrowing; over the medium-run, however, the dynamics of output are determined by the action of patient agents responding to the wealth outcomes of the policy.

Figure 2 presents dynamics as a result of a government spending shock, for differing horizons over which the constraint on impatient borrowing is not binding; as is illustrated in the first panel, output multipliers tend to be lower than one, suggesting a net crowding out of private expenditure to the policy. Similar to above, an increase in government consumption leads to both increases in impatient incomes and government debt. Higher output and inflation result in an increase in the real interest rate which crowds out expenditure of patient households on impact, as indicated in equation (21). In normal and recessionary times, when $\lambda^b > 0$, impatient agents increase their consumption in the short run when government consumption is increased, as extra aggregate demand increases labour demand and subsequently income for these agents. When the borrowing constraint on the impatient is not binding, on the other hand, these agents smooth the additional expenditure over the period in which they expect the borrowing constraint to be slack. Therefore, the mechanism determining the consumption path of impatient households is the same as in the case of transfers. The main difference between the two policy experiments, however, is the fact that transfers impact directly the income of impatient households, whereas government consumption does indirectly through higher labour income. Therefore, the increase in income and consumption is smaller in the case of government consumption (as shown in Figure 2), and

Figure 2: Dynamics from a government consumption shock



Dynamics from fiscal experiments where the borrowing constraint on impatient agents is slack for 0, 6, 12 and 18 quarters, as illustrated by the legend. In each instance, the results have been normalised to present the dynamics as a result of a shock to fiscal policy equal to one per cent of output; dynamics for each variable are presented as percentage deviations from the steady-state. The results present marginal impacts as the length of time the borrowing constraint is not binding is unaffected by the policy; the normalisation is performed on shocks equal to one-one-hundredth of this and is done for ease of presentation.

the output effects of this policy come from public (and not private) demand. As the income being smoothed is smaller, the impact on the real economy resulting from this smoothing process is also smaller and therefore the difference in response of output between expansions and recessions is not as large as in the case of transfers. Given this, the subsequent influence of consumption smoothing of impatient agents on patient households expenditure via the channels discussed above (expected real interest rates and taxes) is also smaller, as can be seen in Figure 2.

3.5 Fiscal multipliers

To extend the analysis to all nine fiscal experiments, the first column of Figure 3 presents four quarter cumulative output multipliers (y -axis) for differing periods for which the constraint on impatient households' borrowing does not bind (x -axis); note that the plots present step functions as dynamics will only be altered with discrete changes in the time horizon over

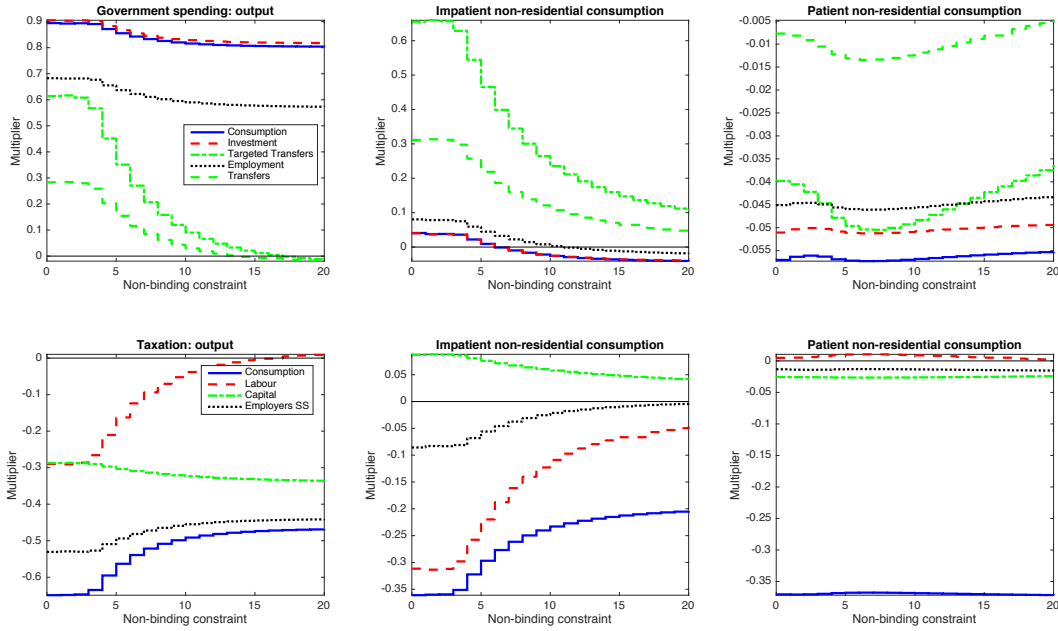
which this borrowing constraint is not binding. The intuition from above, that the longer the slack in the borrowing constraint the smaller the fiscal policy effect on output is maintained.¹⁷ As discussed above, in periods of slack, impatient agents are already consuming enough to not use their full credit capacity and increases in their incomes during these periods lead to a lower consumption response of impatient agents compared to when their borrowing constraint binds. For example, average government spending multipliers are 49% lower when there is slack in the impatient borrowing constraint for 20 quarters compared to when this is always binding; similarly, taxation multipliers are lower by (on average) 33% between the two benchmarks. The largest non-linearity in multipliers are for targeted and general transfers and labour taxes which are 0.61, 0.28 and -0.29, respectively, in normal and recessionary times when the borrowing constraint binds, and approximately zero when there is slack for 20 quarters.

The one exception to the main result is for capital taxes which have a higher impact on the economy when the impatient borrowing constraint is not binding. In normal and recessionary times ($\lambda^b > 0$), a cut in capital taxes leads to a substitution from labour to capital, lowering labour income and therefore impatient consumption. In this situation, impatient households would prefer to borrow more (λ^b increases) which they can do if the borrowing constraint is not binding. Therefore a decrease in capital taxes has a smaller negative effect on the consumption of impatient households during an expansion and as a result, there is an additional improvement in output resulting in a higher multiplier. The distortionary nature of taxes can lead to the general intuition to brake, but only in our model for taxes on capital; for all other instruments, expansionary policy leads to higher incomes for impatient agents and as such, if their borrowing constraint is not binding at the time of the policy, output multipliers are lower.

The degree to which the effects of fiscal policy are non-linear is determined by the degree to which the effectiveness of policy is influenced by the consumption movements of impatient agents. If these movements are small when the borrowing constraint binds (for example, when the government increases spending on consumption, investment and employment or when it decreases employers social security contributions or taxes on capital), the non-linearity of the response to fiscal policy is smaller. Cumulative four quarter consumption

¹⁷At the margin, there is some non-monotonicity in the movements of multipliers as the borrowing constraint on impatient does not bind for longer horizons; that is, for some fiscal instruments, we see a slight increase in multipliers when the borrowing constraint is not binding for two quarters versus to when it is always binding. This non-monotonicity is negligible (observed at the third decimal point or higher) and is due to the fiscal experiments in (13) being fixed for four quarters. When the constraint on impatient agents is not binding for two quarters (say) half of the fiscal shock is in this period, and half not. When this occurs, impatient agents can increase their consumption by more in periods three and four, due to lower interest payments in period two, when the households were not borrowing as much as they could have.

Figure 3: Four-quarter cumulative multipliers

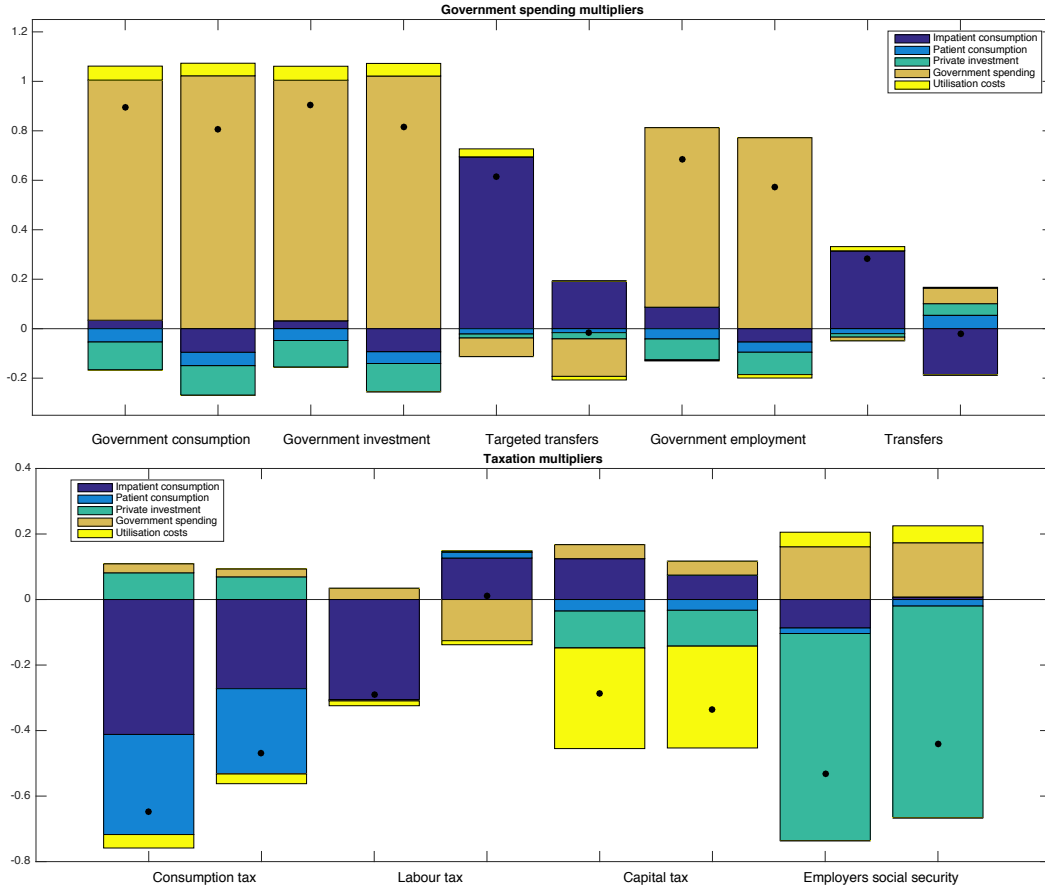


Cumulative multipliers for the nine fiscal experiments for differing horizons over which the borrowing constraint on impatient households does not bind; the first column presents output multipliers, the second column impatient non-residential consumption multipliers; and the final column patient non-residential consumption multipliers. The first row represents results for government spending instruments and the second row taxation instruments.

multipliers presented in the second and third column of Figure 3 demonstrate that impatient consumption multipliers are largest when their borrowing constraint is binding for targeted and general government transfers, and labour and consumption taxes. As such, these instruments lead to the most non-linear of outcomes in both impatient consumption and output; note that the consumption of patient agents is largely unaffected by the actions of the impatient in the four-quarter horizon. Patient agents have higher discount factors and their consumption is influenced by the path of expected future real interest rates and consumption taxes (as demonstrated in (21)); although the actions of the impatient influence these, the effects come over the medium term and as a result four quarter consumption multipliers are not as volatile as for impatient households.

To examine further the role of binding versus non-binding borrowing constraints on fiscal outcomes, Figure 4 presents a decomposition of four quarter cumulative output multipliers for each of the nine fiscal experiments, separated between government spending and tax instruments. The movement of each component of GDP were examined to determine what was contributing to the movement in total output over the first four quarters of the fiscal

Figure 4: Four-quarter cumulative output multipliers decomposition



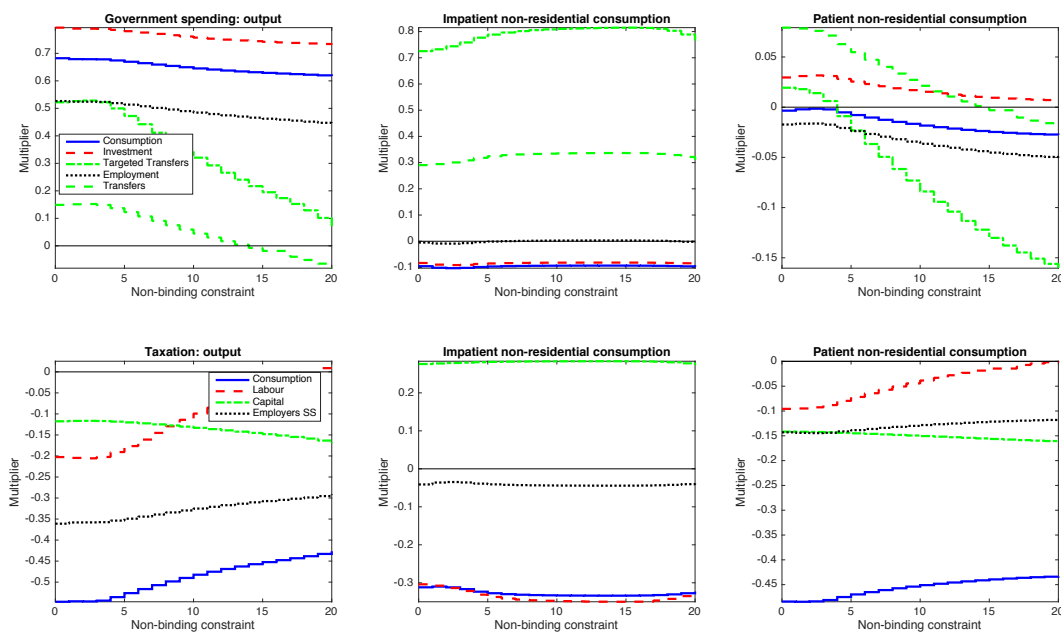
A decomposition of output multipliers for each instrument (along the x -axis) where each instrument has two bars, representing a pair of values: in the left-hand bar the borrowing constraint on impatient agents is always binding; in the right hand bar it is slack for 20 quarters. The decompositions separate between those elements which contribute negatively and positively to the four-quarter cumulative output multiplier, with the circle-point in each bar representing the value of the multiplier (the net of the positive and negative effects).

intervention; for each fiscal experiment a pair of results are presented side-by-side to each other, one where the borrowing constraint on impatient agents is always binding (left-hand bar) and another where it is slack for 20 quarters (right-hand bar). These results illustrate that it is the movements in impatient agents' consumption which is the biggest source of non-linearity in these multipliers; the bars which represent impatient spending are those which vary the most between the different scenarios. It follows, therefore, that when impatient spending is not a large contributor to the output multiplier, the difference in results relative to when the borrowing constraint is not binding is not as quantitatively large; that is, for those policies which do not require movements in impatient households' consumption to

change output, fiscal effects are less non-linear.

As highlighted in Figures 1 and 2, although the smoothing actions of impatient agents reduce the output response of policy in the short term, when their borrowing constraint is slack, over a longer period it improves output as consumption is spread over the longer horizon. This smoothing of actions by the impatient agents leads to less non-linearity in multipliers when measured over a long horizon; this is confirmed in the first column of Figure 5 which plots twenty quarter cumulative output multipliers. Non-linearity is still observed, and although the percentage changes in output multipliers are similar, the absolute range of these values is smaller. Targeted and general transfers continue to be the most non-linear spending instruments and twenty quarter cumulative multipliers are negative for general transfers when there is slack in the impatient borrowing constraint. These negative multipliers result from the rise in distortionary taxes to pay for the expansionary policy, and from the behaviour of patient households, as discussed in Section 3.4.

Figure 5: Twenty-quarter cumulative multipliers



Cumulative multipliers for the nine fiscal experiments for differing horizons over which the borrowing constraint does not bind; the first column presents output multipliers, the second column impatient non-residential consumption multipliers; and the final column patient non-residential consumption multipliers. The first row represents results for government spending instruments and the second row taxation instruments.

Over short time horizons, the non-linear response of fiscal multipliers is determined by the consumption of impatient agents; however, evaluating a period which nests the entire

time in which borrowing constraints are slack (and therefore the period over which impatient consumption is smoothed), it is the response of patient agents which becomes more important. This can be seen in the second and third columns of Figure 5 which presents twenty quarter cumulative consumption multipliers for the two types of household for differing periods over which credit constraints are slack. Whereas in Figure 3 the non-linearity in four quarter cumulative consumption multipliers is driven by impatient agents, when the whole period over which these agents can smooth their consumption is considered, as in Figure 5, the non-linearity is driven by patient households.

As discussed above, the difference in the four quarter output multipliers between expansions and recessions stems from the consumption smoothing of impatient households during expansions. Over the 20-quarter period the entire smoothing exercise is completed therefore there is limited volatility in the impatient households' consumption multiplier. On the other hand, the smoothing process of impatient households results in more persistent real interest rates and larger increases in the present discounted value of taxes, which leads to greater crowding out of patients' consumption and therefore a lower consumption multiplier for these households. There is therefore both a short and long run non-linearity to fiscal policy. In this respect our results differ from those presented in Canzoneri et al. (2016) who use costly financial intermediation to produce asymmetric fiscal multipliers; in their paper, although the short run multipliers are different in recessions and expansions, there is limited non-linearity over a longer time horizon (beyond ten quarters).

4 Further extensions

4.1 Further fiscal experiments

As discussed in Section 3.2, the fiscal experiments in our benchmark specification featured small temporary shocks spread over four quarters. To examine the non-linear effects of policy further, we now consider larger shocks which can generate substantial changes in macroeconomic outcomes. In this respect, these shocks can influence the time horizon over which the borrowing constraint on impatient households is not binding, and therefore we now present average multipliers compared with the 'marginal' effects analysed above.

We apply housing preference shocks of different values to change the underlying conditions of the economy; the first column of Table 2 presents the change in output in the first quarter as a result of the different values for these shocks, conditional on there being no fiscal intervention and borrowing constraints always binding. We then allow a fiscal expansion of one per cent of quarterly GDP over four quarters (therefore a stimulus of 0.25 per cent of

annual GDP per quarter) and record the average multipliers as a result of this intervention across the nine fiscal instruments; these multipliers are presented in the remaining columns of Table 2.

Now consider the results of targeted transfers (the third column in Table 2). When output is higher than in steady-state, targeted transfers have a lower multiplier compared to when the economy is in a recession. This result follows from the intuition presented above; when output and incomes are high, house prices are elevated and the borrowing constraint on impatient agents does not bind, leading to lower marginal propensities to consume for these agents and lower fiscal multipliers. The bigger the boom in the economy, the longer the horizon over which the borrowing constraint will be slack. When output is below that of steady-state, incomes are lower, and therefore impatient agents have a higher marginal propensity to consume, thus leading to higher multipliers as a result of any fiscal intervention. Four quarter cumulative multipliers for targeted transfers range from near zero in a boom, and 0.7 in recessions. Two components influence this variability: the underlying economy which influences the borrowing conditions of impatient agents; and the impact of the fiscal policy itself, further changing the horizon over which borrowing constraints are slack.

Table 2: Four quarter cumulative average fiscal multipliers

ΔGDP_t	G	I^G	TR'	N_g	TR	τ^c	τ^l	τ^k	τ^{er}
4	0.805	0.819	0.003	0.576	-0.013	-0.472	0.004	-0.333	-0.443
3	0.808	0.821	0.020	0.579	-0.004	-0.476	-0.005	-0.330	-0.446
2	0.813	0.826	0.052	0.586	0.012	-0.485	-0.021	-0.324	-0.452
1	0.830	0.842	0.119	0.605	0.053	-0.511	-0.062	-0.311	-0.469
0	0.889	0.900	0.315	0.670	0.199	-0.617	-0.207	-0.287	-0.527
-1	0.894	0.905	0.486	0.683	0.272	-0.648	-0.279	-0.287	-0.531
-2	0.894	0.905	0.552	0.683	0.283	-0.649	-0.290	-0.287	-0.531
-3	0.894	0.905	0.580	0.683	0.283	-0.649	-0.290	-0.287	-0.531
-4	0.894	0.905	0.604	0.683	0.283	-0.649	-0.290	-0.287	-0.531

Average four quarter multipliers where house price shocks of different sizes are used to change output to the values presented in the first column of the table. Then the economy is subsequently subjected to a fiscal expansion of one percentage point of annual GDP spread over four quarters.

Note that the variability in fiscal multipliers in Table 2 in the other instruments is lower, especially when the economy is at the steady-state levels of output or below. When this is true, the borrowing constraint on impatient households always binds, and therefore the only change in multipliers comes from the fiscal intervention itself influencing impatient agents' borrowing conditions, giving some slack in their constraint. Those fiscal instruments which have a smaller impact on impatient incomes and house prices will, therefore, demonstrate

lower levels of volatility in Table 2; indeed, the variability of multipliers in Table 2 is correlated with those from Figure 3. Therefore, it can be concluded that even though fiscal multipliers are state-dependent, the policy itself has a limited impact upon its own effectiveness. The implication of this is that it is the underlying economic climate - in our model the credit conditions - that determines the impact of fiscal intervention not the direction of the fiscal action.

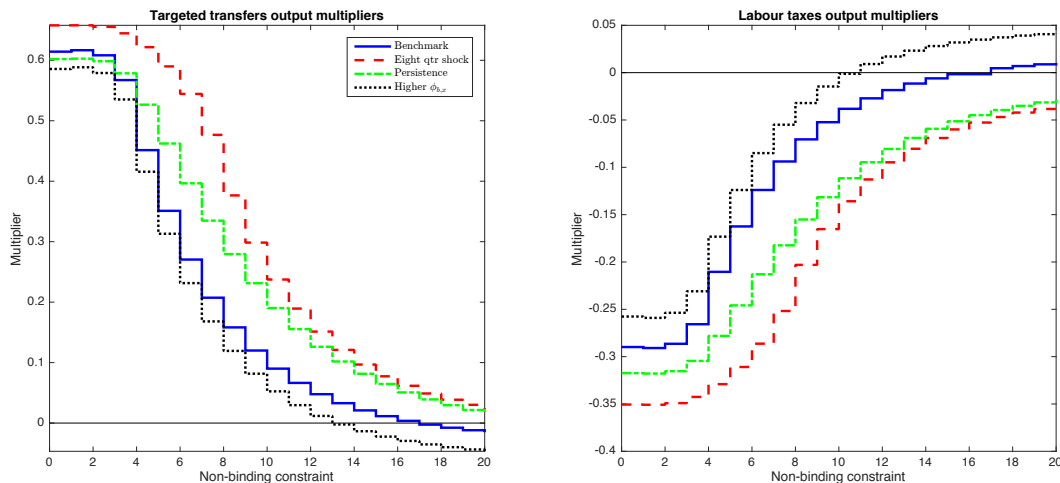
We have performed experiments similar to those in Table 2 using different shocks to change the underlying conditions of the economy; the results from above are maintained such that multipliers are higher during a recession than in a boom, and the impact of policy itself can change the macroeconomic climate to influence the borrowing constraints on impatient agents. We have also considered different sizes of fiscal shocks than those present in Table 2, and again the intuition is maintained; the larger the fiscal shock in these experiments, the more scope this policy has on influencing the borrowing conditions of households.¹⁸

We further consider experiments similar to those above in Section 3.5 but now including fiscal shocks: lasting eight quarters (compared with four in the benchmark); lasting for four quarters (as in (13)) and then followed with persistence after this period (of value 0.8); and with higher levels of debt aversion ($\phi_{b,x}$ in (13)). Figure 6 presents results for both targeted transfers and labour taxes; results are not sensitive to which fiscal instruments are considered and these two are chosen for ease of presentation. Although fiscal multipliers in these two extensions vary from those in the benchmark, the difference is limited. In the above two cases, longer lasting shocks lead to higher short-run multipliers as impatient agents play an important role in the transmission mechanism in the case of labour income taxes and transfers.¹⁹ Higher levels of debt aversion lead to lower multipliers as the government are now more aggressively responding to debt by lowering spending and raising taxes thus reducing demand. Despite these changes in the size of multipliers, however, the asymmetry and the state-dependence are maintained.

¹⁸We also consider two further extensions to those results in Table 2, that of contractionary fiscal shocks, and when expansionary shocks respond with a lag of one quarter. A negative shock can weaken a boom in the economy, and therefore lead to a shorter horizon over which the borrowing constraint on impatient agents is not binding, thus increasing multipliers during output expansions; the impact to which this occurs is conditional on the extent to which the fiscal policy can influence impatient incomes and house prices. A shock that responds to the change in output with a lag influences the economy as it returns to steady-state values when the borrowing constraint on impatient agents is always binding. As such, multipliers are higher with shocks that increase output and smaller for shocks that decrease output; however, both of these extensions have only small effects at the margin, and the main intuition is retained (results available on request).

¹⁹For the remaining fiscal instruments, where impatient households play a relatively less significant role in the transmission mechanism, the negative wealth effect dominates and the more persistent action of the fiscal authority results in smaller multipliers, and the impact on the variability of these over the business cycle is very limited.

Figure 6: Four quarter cumulative multipliers: fiscal policy extensions



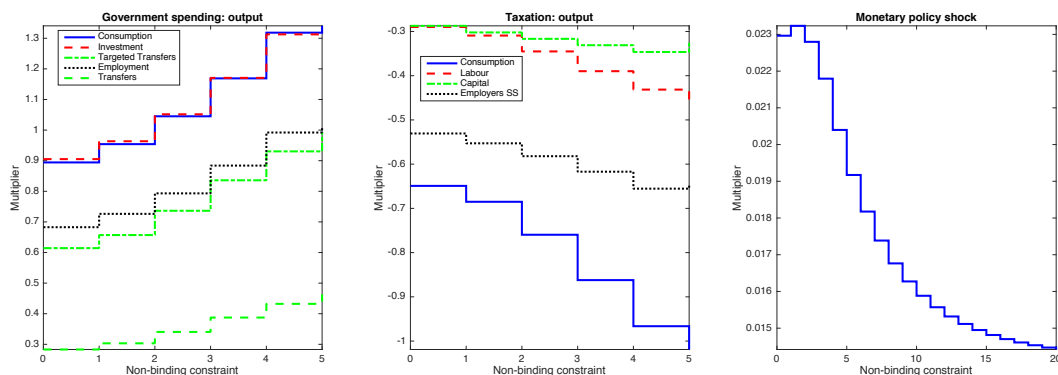
Four quarter cumulative multipliers for targeted transfers and labour taxes under a number of different extensions as labelled in the legend: ‘Benchmark’ represents the benchmark results above; ‘8 qtr shock’ represents where fiscal shocks last for eight quarters (in benchmark, fiscal shocks last for four quarters); ‘persistence’ where there is a four quarter shock as in the benchmark, and after this there is persistence of 0.8, such that the value of the shock decays over time; and ‘Higher $\phi_{b,x}$ ’ refers to $\phi_{b,x} = 0.4$ (as opposed to 0.2 in the benchmark), this change leads to debt being halved in 18 quarters on average instead of 34 quarters in the benchmark scenario.

4.2 Monetary policy

In order to put the results on the non-linearity of fiscal policy into context, in this section we extend our analysis in two dimensions: first, we consider another source of non-linearity, that of monetary policy being at its ‘zero lower bound’ (ZLB); and second, similar to the framework above, we consider whether the impact of monetary policy shocks on the general economy are non-linear by varying the time over which the borrowing constraint on impatient agents is slack. In order to consider the former, we use a preference shock to get the nominal interest rate to be at its ZLB for up to five quarters and then apply the small fiscal shocks from above to get multiplier values, as in Section 3.5. To investigate potential non-linearities in monetary policy we use a framework similar to that of above, but now instead of applying a small fiscal shock for when the impatient borrowing constraint is slack for up to 20 quarters, we apply a small one-quarter monetary policy shock, reducing nominal interest rates. The results are normalised to show a percentage change in output over a four-quarter horizon to a one-quarter change in the interest rate of 100 basis points. Results from these extensions are presented in Figure 7.

The first panel of Figure 7 demonstrates that fiscal policy multipliers are more non-linear

Figure 7: Monetary policy extensions



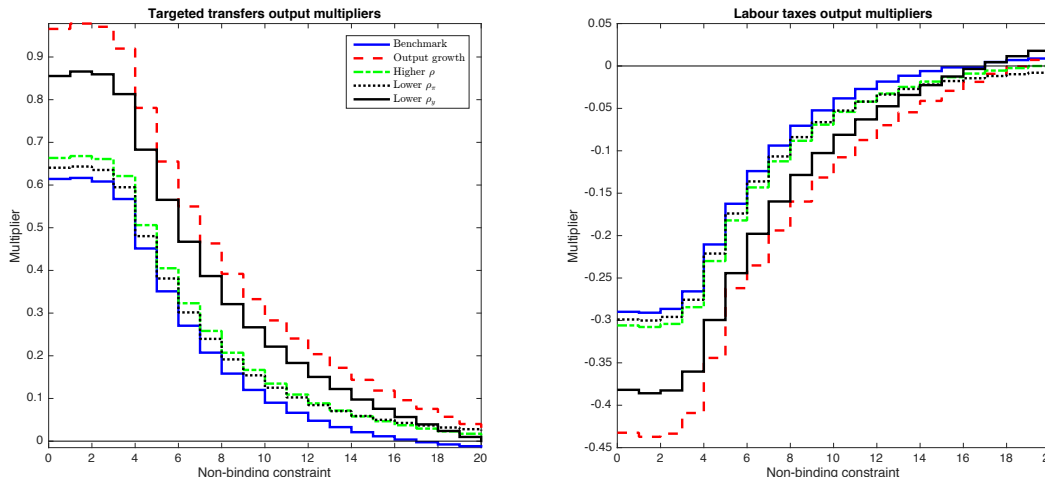
The first two panels present fiscal multipliers for spending and tax instruments, respectively, for periods over which the ZLB is binding for between zero and five quarters. The third panel presents results from a one-quarter monetary policy shock where the change in the interest rate lasts for one quarter and is equal to 100 basis points.

with changes in the ZLB length than with the borrowing conditions of impatient households: for example, government spending (tax) multipliers are 54% (38%) larger than normal times with a ZLB length of five quarters. This is intuitive given that the non-linearity in the results presented in Section 3.5 derive from the actions of impatient households (which account for half the economy in our benchmark calibration), whereas the ZLB has an impact on the whole economy. Fiscal expansions can have an inflationary effect which, when combined with the ZLB, lowers real interest rates encouraging spending by both impatient and patient households. A period where the monetary ZLB is binding is likely to also be one of where the borrowing constraint on impatient households is also binding, as it is unlikely for the former to occur in a consumption boom. As such, the co-existence of the ZLB and a recession would yield even greater state-dependence and hence greater asymmetries in fiscal multipliers than those presented above. That is, the ZLB provides one end of the spectrum where fiscal multipliers are high and the impatient borrowing constraint is always binding; whereas the other end of the spectrum is where the borrowing constraint on the impatient is expected to be slack for a long time horizon.

Weise (1999) and Lo & Piger (2005) find that monetary shocks have a bigger impact on output in a recession than in a boom, whereas Tenreyro & Thwaites (2016) show the reverse finding i.e. business investment and consumption on durables are less responsive to interest rate shocks during downturns. Our results (as illustrated in the third panel of Figure 7) are consistent with the former and suggest that monetary policy is less effective in expansions than in recessions. From the perspective of impatient households, monetary policy stimulus

leads to higher labour income, lower interest payments and higher transfers (as the government budget constraint is relaxed with lower interest). In normal times and in recessions all this additional income is spent instantly, whereas in an expansion the expenditure is smoothed over the period in which borrowing constraints are expected to be slack, hence rendering monetary policy less effective in upturns.

Figure 8: Four quarter cumulative multipliers: Taylor rule extensions



Four quarter cumulative multipliers for targeted transfers and labour taxes under a number of different extensions as labelled in the legend: ‘Benchmark’ represents the benchmark results from above; ‘Output growth’ represents where output growth, as opposed to the deviation of output from steady-state, is in the Taylor rule (10); ‘Lower ρ_π ’ when the calibration of this parameter is 1 (1.7196 in the benchmark); ‘Lower ρ_y ’ when the calibration of this parameter is 0.01 (0.0944 in the benchmark); ‘Higher ρ ’ when the calibration of this parameter is 0.85 (0.5509 in the benchmark).

We also consider different forms for the Taylor rule and different calibrations of its parameters. Figure 8 presents results for general transfers and labour tax multipliers under various Taylor rule specifications, where again these instruments are used as examples and the results are not sensitive to which fiscal instruments considered. In general, the results presented in Section 3.5 are robust with asymmetric responses to fiscal policy depending on the conditions of the impatient agents’ borrowing constraint. The non-linearity of fiscal policy is greater under two scenarios: first, when the response of the monetary authority to higher output is muted ($\rho_y = 0.01$); and second, where the Taylor rule responds to output growth (GDP_t/GDP_{t-1}) instead of movements in output from the steady-state. When the Taylor rule responds to output growth, multipliers are 54% and 38% smaller for government spending and taxation instruments, respectively, when the borrowing constraint is slack for 20 quarters compared to when it is always binding (the corresponding differences were 49%

and 33% in the benchmark results). In both scenarios, four quarter multipliers increase significantly (with respect to the benchmark) when the borrowing constraint is binding, or not binding for a relatively short period of time. When this is the case there is a significant initial increase in output and a monetary policy that is unresponsive to output ($\rho_y = 0.01$) means that the increase in the interest rate is smaller, leading to a smaller crowding out of patient households' consumption and as a result a greater multiplier. A similar profile emerges when the Taylor rule responds to output growth, where changes in the interest rate occur only in the period of growth, whereas there is no change when output is steadily above the steady-state value. With respect to the benchmark, this also implies a smaller response of interest rates and a lower crowding out of patients' consumption. For other changes analysed in Figure 8, there are small variations in the size of multipliers under different calibrations, but not to the variability of these multipliers as a result of slack in the impatient borrowing constraint.

4.3 Further sensitivity

In addition to the above, we also performed sensitivity tests to other parameter values, including (but not limited to): price and wage stickiness; the proportion of impatient households in the economy; the exclusion of employers' social security contributions, public employment and productive public capital in the model; and higher levels of habit persistence. Despite quantitative shifts in the size of multipliers, the non-linearity of fiscal impacts remains similar to those presented above; the results are robust to further sensitivity tests. Further results can be found in Appendix A which presents results from changes in other assumptions: allowing for a fixed housing stock (as in Guerrieri & Iacoviello 2017, Figure 13 in Appendix A); including capital income tax on interest from government debt and loans (Figure 14 in the Appendix A); and incorporating an adjustment cost to public investment similar to that of private investment (Figure 15 in the Appendix A). The changes in these assumptions lead to changes in the underlying size of multiplier but have a limited effect on the variability of the effects of fiscal multipliers (results available on request).

5 Empirical evidence and discussion

Having explored the results from our theoretical model above in detail, we now present a discussion of these findings in the context of the broader empirical literature. In what follows, we first provide support for the key mechanism deriving our asymmetric multipliers before subsequently framing our findings in the context of existing empirical findings.

5.1 The case for occasionally binding borrowing constraints

The asymmetries in fiscal multipliers in our model derive from variation in the marginal propensity to consume (MPC) of impatient agents depending on the nature of their credit constraints. Bunn et al. (2018) demonstrate that the MPC of UK household's is higher in the face of negative income shocks than those of positive ones. Importantly, Bunn et al. (2018) demonstrate that this variation can be explained by balance sheet characteristics concerning debt, liquidity and credit market access; it is concluded that a model with occasionally binding borrowing constraints replicates these results. Bunn et al. (2018) estimate that MPCs for those with mortgages (similar to the 'impatient' in our model) are higher than those in owner-occupied properties (similar to the 'patient' in our model), especially in the case of negative income shocks, where it is more likely for borrowing constraints to be binding.²⁰ Christelis et al. (2017) found similar results using survey responses from Dutch households to demonstrate that the MPC of households is bigger from negative income shocks compared to positive ones. Again, Christelis et al. (2017) demonstrate that this behaviour can be explained with a model incorporating occasionally binding credit constraints.

The theoretical literature introducing collateral constraints - which are sometimes occasionally binding - also provides support for the transmission mechanisms that drive our asymmetric fiscal multipliers. Iacoviello (2005) develops a model with collateral constraints tied to housing wealth to provide better estimates of the response of aggregate demand to house price shocks. Iacoviello & Neri (2010) further develop this model to allow the housing stock to be produced in its own sector and demonstrate that spillover effects from this sector to the macroeconomy between 1965 and 2006 are non-negligible. Guerrieri & Iacoviello (2017) extend these models to allow collateral constraints to be occasionally binding, introducing an asymmetry in the response of consumption to shocks, which better explains the US economy during the great moderation and the Great Recession.

Models with asymmetries are able to better explain skewness in macroeconomic observations. For example, Jensen et al. (2017) document a negative skewness in business cycles and further, that this skewness has been increasing over time in the US. Jensen et al. (2017) then estimate a model with occasionally binding borrowing constraints on both households and firms to show that such a model can explain these dynamics when combined with the observation that leverage has been increasing over time.²¹ The intuition is that agents respond differently to positive shocks than negative shocks (as outlined above), and when leverage

²⁰Further, these MPCs are higher for those who are credit constrained, those who do not have a buffer of savings, and those who have higher debt-to-income ratios, all reconciling with the characteristics of the impatient in our model.

²¹This is further supported in Jensen et al. (2017) through illustrating that both the state level variance of the Great Recession and the skewness of output is correlated with state-level debt-to-income ratios.

is higher, the response to adverse outcomes is amplified as debt reduction becomes more burdensome. Abbritti & Fahr (2013) use downward nominal wage rigidity in an otherwise standard New Keynesian model to explain positive skewness in the growth rates of wages and unemployment and a negative skewness in output.

Panel A of Table 3 presents skewness statistics for real output, real consumption, real investment (in both the residential and non-residential sector and in the consumption of housing) and house prices for HP filtered data and quarter-on-quarter growth rates. The one variable for which there is clear evidence of a negative skewness is house prices; this is resulting from many periods of low growth in prices, with short sharp episodes of relatively higher falls in prices. Intuitively, this could be replicated with our model using occasionally binding borrowing constraints as conditions are different for when house prices are rising compared to when they are falling.

To formally test whether our model with occasionally binding constraints can better explain these asymmetries in the data, we use Simulated Method of Moments (SMM) to estimate the size and persistence of non-fiscal shocks in the model (ε^B , ε^H , ε^I , $\varepsilon^{A,c}$, $\varepsilon^{A,h}$) by minimising the difference between standard deviations and the skewness of the four variables in Table 3, between the data and that resulting from the model with the estimated shock parameters.²² That is, we estimate shock parameters which best match the data for these moments.²³ We perform this estimation twice for two versions of the model, one where borrowing constraints are occasionally binding (as in our above model) and one where they are always binding. By comparing the ability of the two models to match the data, we assess the importance of allowing for occasionally binding borrowing constraints in the model, the mechanism which drives the results in our paper. The results are presented in Table 3.

When looking at the standard deviations of macroeconomic variables (Panel B of Table 3), the model with occasionally binding borrowing constraints better matches the data, even when the algorithm is minimising the differences for the model with always binding constraints. The model with occasionally binding borrowing constraints also does substantially better in matching the skewness in macroeconomic data; for all variables in both treatments,

²²Jensen et al. (2017) discuss how SMM estimation is particularly useful for DSGE models with non-binding borrowing constraints.

²³Following Abbritti & Fahr (2013) we use the standard deviations from Hodrick Prescott detrended data and the skew from growth rates (as in Jensen et al. 2017); results are not sensitive to this and are robust to different definitions. We apply the Matlab function `fminsearchbnd` to perform the optimisation. To calculate moments we used the following data: the logarithm of GDP, consumption, private investment, residential investment where all the data are from NIPA Table 1.1.5 and are firstly divided by civilian non-institutional population over 16 (LNU00000000Q, Bureau of Labor Statistics) and the GDP deflator (NIPA Table 1.1.4); relative house prices, where house price is All-Transactions House Price Index for the United States [USSTHPI], U.S. Federal Housing Finance Agency divided by the GDP deflator; inflation is given by log difference of GDP deflator.

Table 3: Model estimation and empirical skewness

	A. Skew in data		B. Standard deviation			C. Skewness		
	HP Filter	Growth	Data	Occas.	Always	Data	Occas.	Always
	Estimation on occasionally binding							
Output	0.135	-1.184*	1.037	1.037	1.225	-1.184	-0.280	-0.145
Consumption	0.310	-1.620*	0.903	1.187	1.557	-1.620	-1.008	-0.276
Investment	0.569*	-1.493*	4.471	3.281	3.224	-1.493	0.139	0.172
House prices	-0.698*	-1.140*	1.986	1.986	2.062	-1.140	-0.252	-0.089
	Estimation on always binding							
Output			1.037	1.004	1.225	-1.184	-0.230	-0.095
Consumption			0.903	0.937	1.176	-1.620	-0.700	-0.276
Investment			4.471	3.006	2.996	-1.493	0.209	0.215
House prices			1.986	1.159	1.185	-1.140	-0.330	-0.170

Panel A present skewness statistics for the four variables on data detrended using the Hodrick Prescott filter (column ‘HP Filter’) and on quarterly growth of the variables (‘Growth’); the notation ‘*’ represents a skewness statistic which is statistically significant from zero with at least 99% confidence. Comparisons of results from the estimated versions of the model with the data are presented in Panels B and C where the first column represents statistics from the ‘Data’, the second column statistics from the model with occasionally binding borrowing constraints (‘Occas.’) and the third column from a model where these are always binding (‘Always’). These results are split into two for the two treatments of the estimation of the model, and the corresponding values for the size and persistence of the shock processes. The top set of results come from models applying the estimations of these shock parameters on the occasionally binding borrowing constraint version of the model, and the bottom set of results from the estimations in the model when the constraint is always binding.

the skewness is better estimated in the model with occasionally binding borrowing constraints (Panel C of Table 3). The model predicts less skewness than is present in the data for all of the variables; however, our model only allows for one source of non-linearity and further, the estimation only uses the size and persistence of shocks in the optimisation. On average, the model with occasionally binding borrowing constraints obtains twice as much skewness in the four macroeconomic variables compared to the model where constraints are always binding; this is true across a number of different iterations of the SMM exercise, where the estimation is optimising over different moments from the data. These experiments provide further support for the use of models with occasionally binding borrowing constraints, consistent with the existing literature (Iacoviello 2005, Iacoviello & Neri 2010, Guerrieri & Iacoviello 2017).

5.2 Existing evidence on asymmetric fiscal multipliers

It is not possible to directly compare our results to those in the empirical literature for two main reasons: first, this literature typically only looks at a broad category of government spending and not at the full nine experiments we consider in our theoretical model; and second, the empirical literature generally considers the change of multipliers over the business cycle, and not credit constraints directly. There is also some disagreement over the degree of asymmetry in fiscal multipliers. While Owyang et al. (2013) and Ramey & Zubairy (2018) find limited asymmetries in government spending multipliers with respect to slack in the economy, Baum & Koester (2011) find more volatility in spending multipliers using a threshold VAR to estimate a range between 0.36 in good times and 1.04 during recessions. Auerbach & Gorodnichenko (2013), Auerbach & Gorodnichenko (2012) and Fazzari et al. (2015), on the other hand, find the greatest range in results with government spending multipliers statistically insignificant from zero at the peak of the business cycle, and 1.6 or greater during recessions.²⁴

Our estimates are in the middle of the range of findings in this literature, with differences in fiscal multipliers varying by approximately 40%. It should be noted, though, that we present one mechanism of potentially many in which multipliers may be non-linear. Indeed, we have shown that through combining non-linearities in the form of the ZLB on interest rates and occasionally binding borrowing constraints, one can get a larger variation in multipliers. Importantly, our modelling assumptions mean that higher multiplier values are observed during ‘normal’ times when the borrowing constraint on impatient households always binds;

²⁴Ramey & Zubairy (2018) suggest that the results from Auerbach & Gorodnichenko (2013) are sensitive to the way in which impulse response functions are derived, something which is less straightforward in non-linear models. When using a different method to derive these impulse responses, lower levels of asymmetries are found in Ramey & Zubairy (2018).

that is, it is not rare to have more effective policy, and this is not limited to times of crisis. This is indeed documented by Tagkalakis (2008) and Fazzari et al. (2015); the latter finds that the US experienced high multipliers in most periods between 1967 and 2012, and the former present evidence for heightened effects of fiscal policy for 19 OECD countries between 1970 and 2001 for half of this period.

Although we cannot directly compare our theoretical results to the empirical literature for each fiscal instrument in turn, there are a handful of papers which look at both government spending and tax multipliers collectively, and the variation in estimates between the two can provide support for our results. We find more asymmetry in government spending multipliers compared with tax instruments, but only if transfers (targeted or otherwise) are included in the analysis. For example, our results suggest average government spending multipliers are 49% lower with 20 quarters of slack in the impatient borrowing constraint, compared with 33% lower for taxation instruments.

In a model considering the liquidity constraints on households (proxied by the loan to value of ratios in residential lending) Tagkalakis (2008) finds similar results utilizing data from 19 OECD countries. Spending and taxation multipliers are 95% and 65% lower, respectively, during booms (periods of high loan-to-value ratios) compared to recessions. Baum & Koester (2011) apply a threshold structural VAR to data from Germany between 1976 and 2009 and find reductions in government spending multipliers of 43.8% from recessions to expansions with the results for changes in tax revenue multipliers are not statistically significant. Baum et al. (2012) apply a threshold vector autoregression to data from G7 countries (excluding Italy); however, they do not include transfers in their measure of government spending. They find tax multipliers to be more responsive to the business cycle than government spending multipliers (consistent with our results if we remove transfers from the analysis). On average across the G7 countries, spending multipliers are 40.9% lower during expansions than recessions, whereas tax multipliers are 111.4% smaller (going from negative multipliers in recessions to mildly positive multipliers in expansions).

6 Conclusions

This paper has shown that fiscal effectiveness can vary substantially across the cycle by developing and presenting a tractable and carefully calibrated DSGE model based on endogenously binding borrowing constraints. The key to our framework has been the state-dependent nature of the collateral constraints that are tied to the value of housing-wealth - binding in bad times while slack in good times - which, in turn, create state-dependence in fiscal multipliers. Moreover, we find that such fiscal asymmetries persist in the long-run,

better matching the empirical estimates.

Another key aspect of our work has been the rich fiscal structure we used in our setting, enabling us to explore the state-dependence of fiscal policy across a large number of fiscal instruments. The high degree of heterogeneity on the impact of slack in the borrowing constraint on fiscal multipliers across instruments has important interpretations when considering potential non-linearities and subsequent policy recommendations. In our results, transfers (and especially targeted transfers) can have a large non-linear effect depending on the presence of slack in the impatient's borrowing constraint as it is these agents who respond to movements in transfers. On the other hand, direct government spending and investment have lower non-linear effects as impatient consumption has less influence on the effectiveness of these policies. The degree and source of state-dependent multipliers are important because they offer more scope for countercyclical fiscal policy; stimulus in a downturn would be less costly in terms of output relative to contractionary policy during booms when multipliers are smaller. This provides an additional dimension to policy making, with crucial implications for the optimal policy design.

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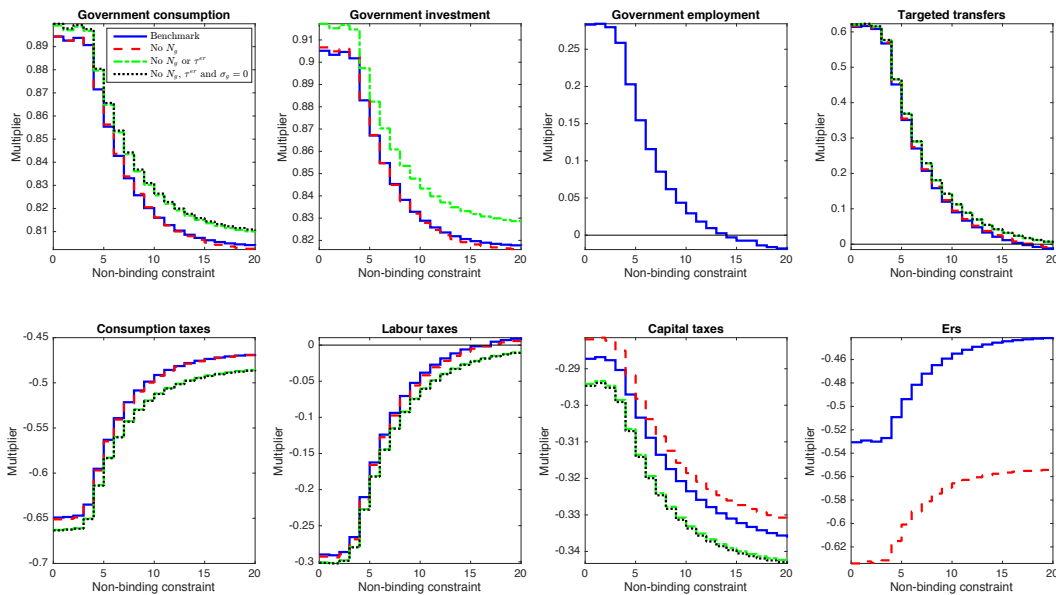
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A Appendix: further robustness tests

A.1 Model without public employment and employers social security contributions

As highlighted in Section 3.3 it is uncommon for DSGE models to contain both employers' social security contributions and public employment, especially one calibrated to the US economy. This subsection presents results from two separate iterations from the benchmark model above: one with public employment but without social security contributions; and another without both public employment and employer social security contributions. Figure 9 presents results for the eight remaining fiscal instruments.

Figure 9: Four quarter cumulative output multipliers: models without public employment and social security contributions



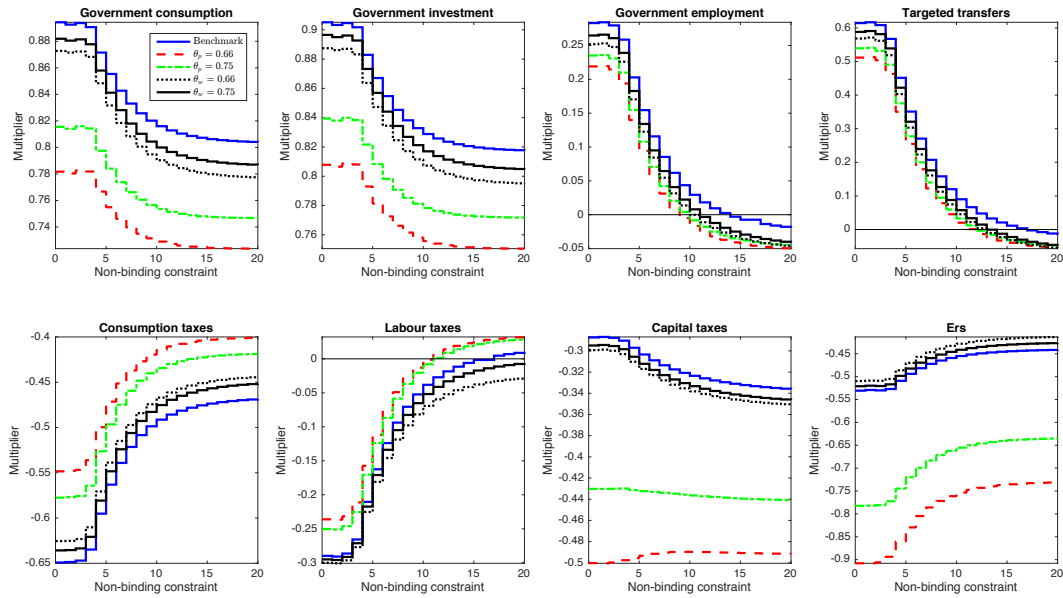
Four quarter cumulative output multipliers for eight fiscal instruments with models which include: the benchmark from above; the benchmark without public employment; the benchmark without public employment and employers social security contributions; and, the benchmark without either employment or employers social security contributions and where public capital is not productive ($\sigma_g = 0$).

A.2 Further sensitivity checks

Figures 10, 11, 12 13, 14 and 15 presents results from a set of further sensitivity checks changing: calibrations of price and wage stickiness; other parameter calibrations; habit

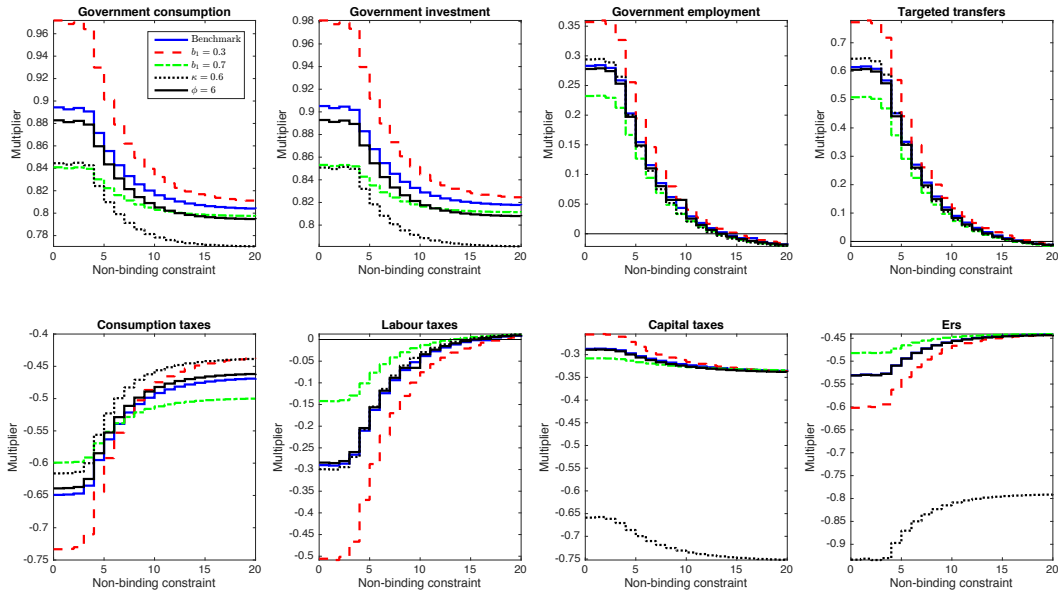
persistence; fixing the stock of housing; charging capital income tax on interest from loans and government debt; and adding adjustment costs to government investment.

Figure 10: Robustness checks: price and wage stickiness



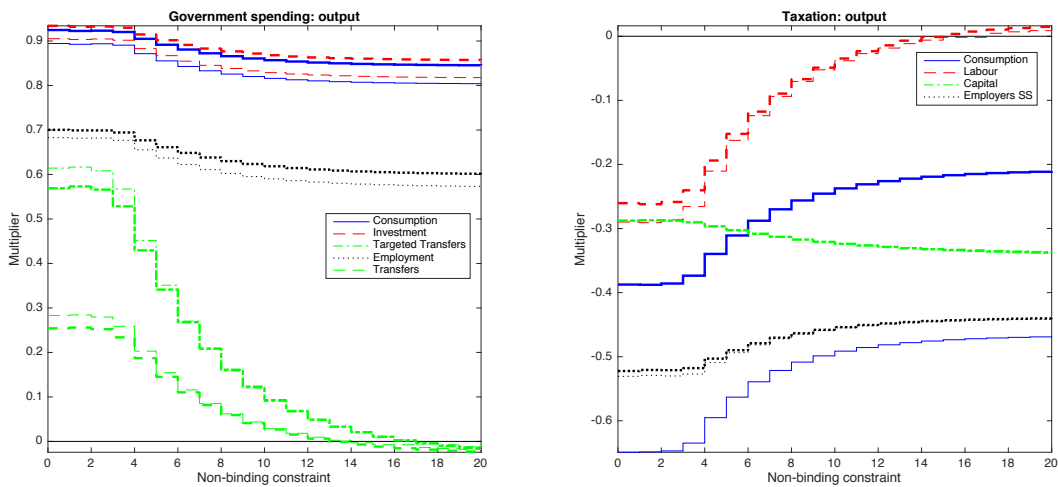
Four quarter cumulative multipliers for the eight fiscal experiments under a number of different extensions as labelled in the legend.

Figure 11: Robustness checks: other parameters



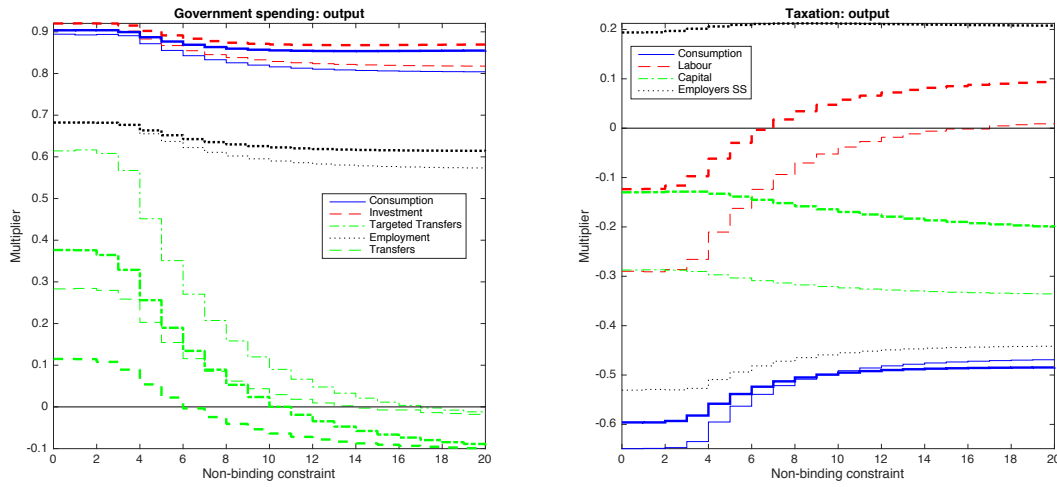
Four quarter cumulative multipliers for the eight fiscal experiments under a number of different extensions as labelled in the legend.

Figure 12: Robustness checks: habit persistence



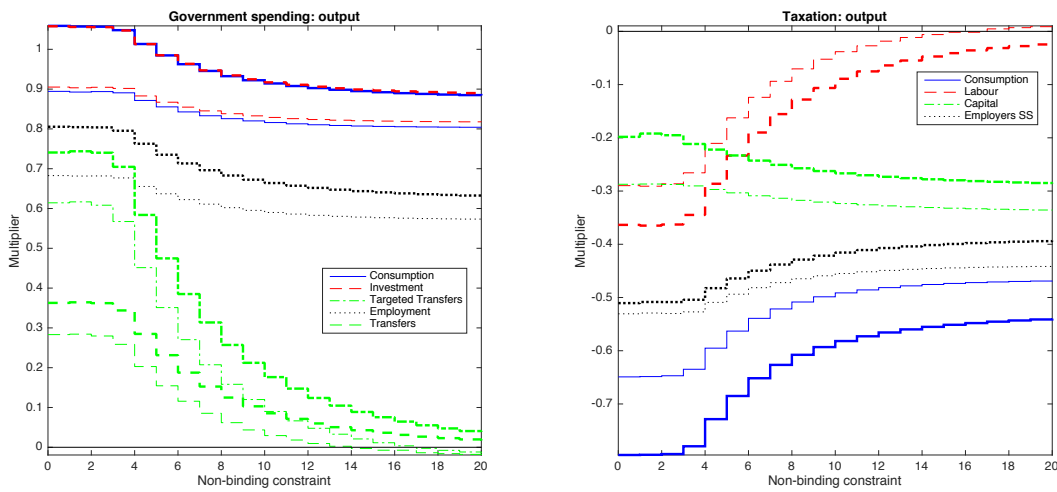
Four quarter cumulative multipliers in nine fiscal experiments for differing horizons over which the borrowing constraint on impatient household does not bind. For each experiment, two sets of results are presented: those with thinner lines are those from the benchmark; those with thicker lines are those where agents' utility functions feature habit persistence with parameter 0.7.

Figure 13: Fixed housing stock



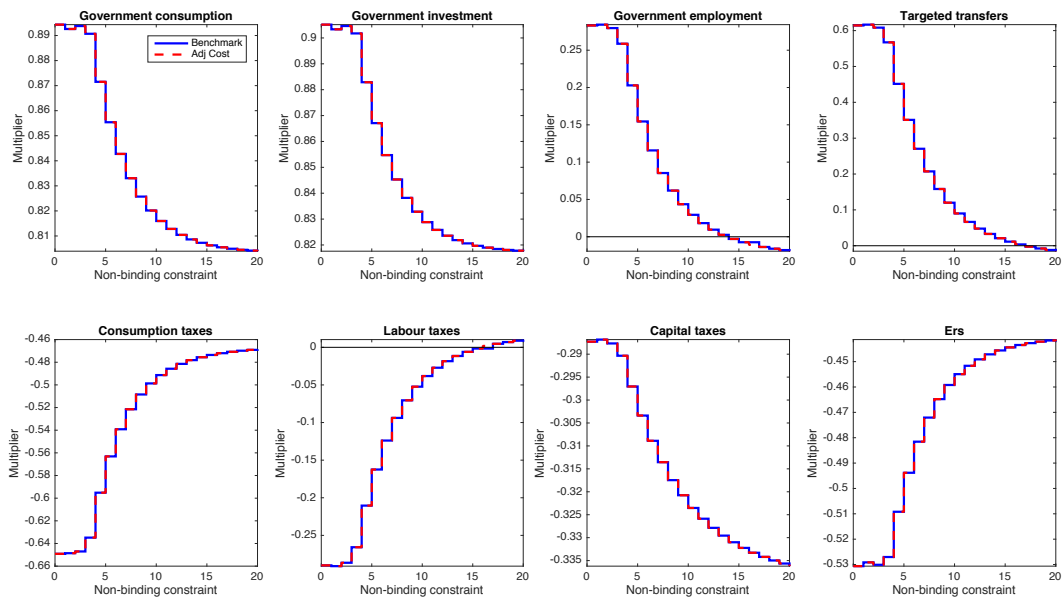
Four quarter cumulative multipliers in nine fiscal experiments for differing horizons over which the borrowing constraint on impatient household does not bind. For each experiment, two sets of results are presented: those with thinner lines are those from the benchmark above; those with thicker lines are those where a fixed housing stock is assumed.

Figure 14: Capital tax on interest income



Four quarter cumulative multipliers in nine fiscal experiments for differing horizons over which the borrowing constraint on impatient household does not bind. For each experiment, two sets of results are presented: those with thinner lines are those from the benchmark above; those with thicker lines are those where a capital tax is charged on interest income from government debt and loans.

Figure 15: Adjustment costs on government investment



Four quarter cumulative multipliers for the eight fiscal experiments for differing horizons over which the borrowing constraint on impatient household does not bind. For each experiment, two sets of results are presented: the benchmark above and where an adjustment cost to government investment is imposed, similar to that on private investment (with the same calibration).