A global correlation linking young stars, clouds, and galaxies

Towards a unified view of star formation

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ABSTRACT

Context. The star formation rate (SFR) linearly correlates with the amount of dense gas mass (M_{dg}) involved in the formation of stars both for distant galaxies and clouds in our Galaxy. Similarly, the mass accretion rate ($\dot{M}_{acc}$) and the disk mass (M_{disk}) of young, Class II stars are also linearly correlated.
Aims. We aim to explore the conditions under which the previous relations could be unified.
Methods. Observational values of SFR, M_{dg}, $\dot{M}_{acc}$, and M_{disk} for a representative sample of galaxies, star forming clouds, and young stars have been compiled from the literature. Data were plotted together in order to analyze how the rate of gas transformed into stars and the mass of dense gas directly involved in this transformation relate to each other over vastly different physical systems.
Results. A statistically significant correlation is found spanning ∼ 16 orders of magnitude in each axis, but with large scatter. This probably represents one of the widest ranges of any empirical correlation known, encompassing galaxies that are several kiloparsec in size, parsec-size star-forming clouds within our Galaxy, down to young, pre-main sequence stars with astronomical unit-size protoplanetary disks. Assuming that this global correlation has an underlying physical reason, we propose a bottom-up hypothesis suggesting that a relation between $\dot{M}_{acc}$ and the total circumstellar mass surrounding Class 0/I sources (M_{cs}; disk+envelope) drives the correlation in clouds that host protostars and galaxies that host clouds. This hypothesis is consistent with the fact that the SFRs derived for clouds over a timescale of 2 Myr can be roughly recovered from the sum of instantaneous accretion rates of the protostars embedded within them, implying that galactic SFRs averaged over ∼ 10-100 Myr should be constant over this period too. Moreover, the sum of the circumstellar masses directly participating in the formation of the protostellar population in a cloud likely represents a non-negligible fraction of the dense gas mass within the cloud.
Conclusions. If the fraction of gas directly participating in the formation of stars is ∼ 1-35% of the dense gas mass associated with star-forming clouds and galaxies, then the global correlation for all scales has a near unity slope and an intercept consistent with the (proto-)stellar accretion timescale, $M_{cs}/\dot{M}_{acc}$. Therefore, an additional critical test of our hypothesis is that the $\dot{M}_{acc}$-M_{disk} correlation for Class II stars should also be observed between $\dot{M}_{acc}$ and M_{cs} for Class 0/I sources with similar slope and intercept.

Key words. Galaxies: star formation – ISM: clouds – Circumstellar matter – Stars: pre-main sequence – Accretion, accretion disks

1. Introduction

Star formation encompasses a broad range of physical regimes that account for the collapse of gas to form smaller structures: from star-forming galaxies to individual young stars surrounded by accreting envelopes and disks, passing through intermediate scales including giant molecular clouds, clumps, and dense cores.

Almost 60 years ago, Schmidt (1959) proposed that the star formation rate (SFR) is a power-law function of the total gas density (atomic and molecular), $\sum_{SFR} = K\sum_{gas}^{N}$ (Kennicutt 1998), with $\sum_{SFR}$ and $\sum_{gas}$ the SFR and the total gas mass (M_{gas}) per unit surface area, and K and N the appropriate constants. The Schmidt-Kennicutt law has been observationally confirmed many times when spanning different types of galaxies, revealing a nonlinear correlation with typical values $1 < N < 2$ and significant scatter. Using the HCN molecule to trace dense gas mass (M_{dg}; $n(H_2) > 10^4$ cm^{-3}), Gao & Solomon (2004) found a roughly linear ($N \sim 1$) correlation between the spatially in-

tegrated SFR and M_{dg} for a wide range of galaxies including normal spirals, luminous, and ultra-luminous infrared galaxies (LIRGs and ULIRGs, respectively). Wu et al. (2005) then found that the spatially integrated SFR in distant star-forming clouds in our Galaxy also correlates linearly with the amount of HCN-emitting gas (see also Jackson et al. 2013; Stephens et al. 2016), showing that this correlation also connected smoothly with the one previously found for galaxies. On this basis, Wu et al. (2005) suggested that the formation of stars in other galaxies may be understood in terms of the basic units of star formation in the Milky Way (MW), which they identified as the clouds massive enough to fully sample the initial mass function (IMF) by hosting massive young stars. The measurements were extended to nearby molecular clouds with and without massive stars using dust extinction to more accurately trace dense gas masses and direct counts of young stars to more robustly measure the SFRs (Lada et al. 2010, 2012). These measurements confirm that the correlation is linear and spreads approximately ten orders of magnitude in each axis. In summary, strong lines of evidence support the

linearity of the SFR-M_{dg} correlation and that this connects individual Galactic clouds and the various types of star-forming galaxies (see also the recent works in Shimajiri et al. 2017; Tan et al. 2018).

The previous view somewhat neglects the role of the actual units in star formation, which are the individual, forming stars. This can be partly attributed to the fact that the SFR, defined as the rate at which gas transforms into stars (in units of $M_\odot$ yr^{-1}), characterizes physical systems that typically include $\sim 10\text{-}10^{11}$ objects. However, there is an equivalent parameter for individual stars that also accounts for the gas-to-star transformation by measuring the rate at which gas falls from the circumstellar environment onto the stellar surface: the stellar mass accretion rate ($\dot{M}_{acc}$, in units of $M_\odot$ yr^{-1} too). Direct estimates of $\dot{M}_{acc}$ are only available for optically visible pre-main sequence objects. These are young stars in a relatively advanced stage of early stellar evolution (Class II from the classification of Lada 1987), when the optically thick envelope has dissipated and direct observations of the remaining circumstellar disks and the stellar accretion shocks are possible. Their gas disk masses (M_{disk}; $n(H_2) > 10^5$ cm^{-3}) are in turn inferred either from observations of different molecules or from submillimeter and millimeter dust continuum emission and an assumed gas-to-dust ratio. Different works indicate that so far the latter method provides more accurate measurements of M_{disk} (Manara et al. 2016; Rosotti et al. 2017). In fact, $\dot{M}_{acc}$ and dust-based M_{disk} measurements are also linearly correlated for large samples of optically visible young stars (Najita et al. 2007; Mendigutía et al. 2012; Najita et al. 2015), a result that has been unambiguously confirmed from recent Atacama Large Millimeter/submillimeter Array (ALMA) data at least for the star-forming regions Lupus and Cha I, despite the large scatter (Manara et al. 2016; Mulders et al. 2017). Although one could be tempted to interpret the $\dot{M}_{acc}$-M_{disk} correlation of stars only in terms of small-scale physical processes in the circumstellar disks, this correlation resembles a scaled-down version of the above-mentioned linear correlation linking local clouds and other galaxies.

This paper shows that the linear correlation that links galaxies and star-forming clouds within our Galaxy (through SFR and M_{dg}) can indeed be connected down to individual, forming stars when physically equivalent measurements ($\dot{M}_{acc}$ and M_{disk}) are used for the latter objects. We propose that such global correlation has an underlying explanation that may ultimately contribute to a unified view of star formation across an enormous range of astronomical scale. Section 2 shows that the correlations for young stars and clouds in the MW can be connected. We discuss the origin of such a single correlation under the hypothesis that the relation observed in clouds is driven by the individual (mainly Class 0/I) stars that form them. Section 3 extends the previous finding and discussion, including data for other galaxies. Finally, Sect. 4 summarizes the main conclusions.

2. Correlation between stars and clouds

Figure 1 shows the SFR versus M_{dg} for 39 distant (a few *Kpc*) and nearby (a few hundred *pc*) star-forming clouds in the Galaxy. Only the 28 distant clouds with log $M_{dg} > 2.50$ (log $L_{HCN} > 1.50$) from the original sample in Wu et al. (2010) have been considered (see Appendices A and B), and most contain HII regions and high-mass young stars. The nearby Galactic clouds are from Lada et al. (2010). The bottom left region shows the $\dot{M}_{acc}$ and M_{disk} values for the nearly complete sample of 62 Class II, optically visible, low-mass young stars in the Lupus I and III star-forming clouds (~ 150 *pc*) from Manara et al. (2016). The
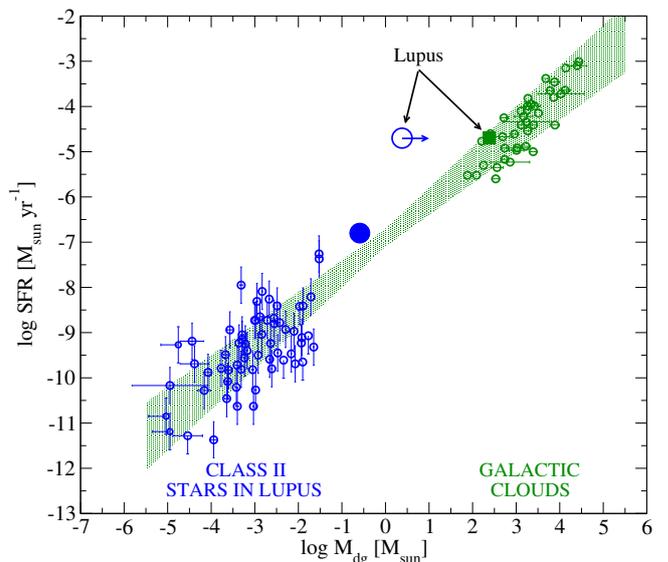

Fig. 1. Star formation rate versus dense gas mass for distant and nearby Galactic star-forming clouds (green circles with and without horizontal error bars, respectively; Wu et al. 2010; Lada et al. 2010) and mass accretion rate versus disk mass in Class II stars in Lupus (blue circles, upper limits as one-sided bars; Manara et al. 2016). Error bars are indicated when provided in the original works. The 3σ linear fit for stars and clouds is indicated with the green dotted region. The green solid square is the direct measurement of SFR and M_{dg} in Lupus. The blue solid circle is the sum of the accretion rates and disk masses of the Class II stars in Lupus, and the blue open circle includes 20 Class 0/I stars in that cloud with an average accretion rate of 1×10^{-6} $M_\odot$ yr^{-1} and a minimum circumstellar mass of $0.1M_\odot$, that is, a maximum displacement in the x-axis given by $f = 1\%$ of the total dense gas mass in Lupus (see text).

axes are labeled in terms of SFR and M_{dg} for all sources, as often used in studies of star formation scaling laws. The original conversion factors between the observations and the physical parameters compared have been kept and the data considered are representative of each regime, which is enough for our purposes. Appendix A describes how the parameters were derived, and Appendix C shows data for additional samples.

The overall trend in Fig. 1 is confirmed from the Spearman's probability of false correlation using the partial correlation technique (e.g., Wall & Jenkins 2003), which accounts for the fact that the plotted values were computed from a squared-distance factor that depends on the stars and clouds. Its small value ($p = 9.5\times10^{-23} << 0.05$) implies that the correlation is statistically significant and not driven by the d^2 factor. Least-squares fitting including 3σ errors provides log SFR = -6.9($\pm$0.2) + 0.80($\pm$0.1)log M_{dg}, with a correlation coefficient of 0.95. That the slope for the whole sample is not exactly unity is mainly due to the fact that the intercepts for stars and clouds are different. Also relevant is that the y-axis scatter is maximum for stars ($\sim \pm 1.5$ dex) and decreases for clouds ($\sim \pm 0.75$ dex). Both topics are discussed in Sects. 2.2 and 3.

In order to understand the correlation, we propose the hypothesis that the trend in clouds is driven by a relation between the mass accretion rate onto the central object and the total circumstellar gas mass (M_{cs} hereafter) surrounding the individual stars in each cloud. The total circumstellar gas mass refers to M_{disk} for Class II objects, and to M_{disk} plus physically associated material in a surrounding dense core for Class 0/I objects. In the latter case, M_{disk} is usually insignificant compared to M_{cs}, but both M_{cs} and M_{disk} refer to the surrounding dense gas mass that

is directly participating in the formation of Class 0/I and Class II stars, respectively. To develop this idea in detail we need to consider the extent to which the numbers plotted in Fig. 1 are comparable (see Appendix A). In particular, if our bottom-up hypothesis is correct, the SFR and M_{dg} of a given cloud should scale with the sum of the individual $\dot{M}_{acc}$ and M_{cs} values of all stars in that cloud.

2.1. Link between SFR and $\dot{M}_{acc}$

The $\dot{M}_{acc}$ and SFR estimates in the vertical axis of Fig. 1 are compared in the following. The sum of the accretion rates of all Class II stars in Lupus from Manara et al. (2016) is $\sim 1.7 \times 10^{-7}$ $M_\odot$ yr^{-1} (log $(\Sigma \dot{M}_{acc}) \sim -6.8$), which is more than an order of magnitude smaller than the SFR directly estimated for that cloud (log SFR ~ -4.7; Lada et al. 2010). This difference is not only caused by the fact that Class 0/I sources are not included in the sample of Manara et al. (2016), but also because of the different timescales involved in the calculation of SFR and $\dot{M}_{acc}$: the averaged one during the past ~ 2 Myr for the clouds, and the actual (virtually instantaneous) conversion of gas into individual young stars. The amount of gas (per time unit) transformed into a given star during its age (t_*) is given by $(1/t_*) \times \int_0^{t_*} \dot{M}_{acc}(t)$ dt = $(1/t_*) \times \int_0^{t_*} \dot{M}_{acc}^0$ e^{-t/τ_*} dt = $(\dot{M}_{acc}^0 \tau_*/t_*) \times (1 - e^{-t_*/\tau_*})$, $\dot{M}_{acc}^0$ being the initial mass accretion rate and τ_* the dissipation timescale.[1] Neglecting possible "FUOr" and "EXOr" events of episodic accretion (Audard et al. 2014) and focusing on the overall, smooth decrease, an exponential decay with τ_* typically between 1 and 3 Myr is estimated from observations of Class II stars (Fedele et al. 2010; Mendigutía et al. 2012), and at least one order of magnitude smaller for Class 0/I sources (Bontemps et al. 1996). The SFR of a cloud during the past few Myr would then be the sum of the previous expression for all stars in that cloud, which is dominated by the term $\dot{M}_{acc}^0$.

Direct observational estimates of $\dot{M}_{acc}^0$ are difficult because of the embedded nature of the stars at their initial stages. The empirically based value consistent with most star-forming regions and commonly adopted is $10^{-4} < \dot{M}_{acc}^0$ ($M_\odot$ yr^{-1}) $< 10^{-6}$ (e.g., Palla & Stahler 2000; Padoan et al. 2014), for which -3 < log SFR < -6. This range is in rough agreement with direct estimates for the clouds. Indeed, within a cloud the actual SFR derived from the sum of the individual $\dot{M}_{acc}$ values is dominated by the high accretion rate of the Class 0/I sources. This is also expected to be of the order of $\dot{M}_{acc}^0$ for individual protostars and, in sum, matches the direct estimates of the SFR. For instance, the typical accretion rate of a Class 0/I star with an IMF stellar mass of ~ 0.3 $M_\odot$ and age of ~ 0.3 Myr (e.g., Padoan et al. 2014) is given by the ratio between both values, 1×10^{-6} $M_\odot$ yr^{-1}. Given that Lupus has ~ 20 Class 0/I sources (Merín et al. 2008; Benedettini et al. 2012), the aggregate value $\Sigma \dot{M}_{acc}$ is $\sim 2 \times 10^{-5}$ $M_\odot$ yr^{-1} (log$(\Sigma \dot{M}_{acc}) \sim -4.7$), which coincides with the direct estimate of the total SFR for that region averaged over 2 Myr (Lada et al. 2010). Moreover, for three molecular clouds for which low-mass protostars have been reasonably well sampled, we find 329, 139, and 43 Class 0/I sources in Orion A, Perseus, and California (Megeath et al. 2012; Carney et al. 2016; Lewis & Lada 2016; Lada et al. 2017). This gives $\Sigma \dot{M}_{acc} = 3.3 \times 10^{-4}$, 1.4×10^{-4}, and 4.3×10^{-5} $M_\odot$ yr^{-1}, which are within a factor $\leq$

2 the SFRs of the same clouds estimated considering all young stars and a 2 Myr timescale: 7.1×10^{-4}, 1.5×10^{-4} and 7.0×10^{-5} $M_\odot$ yr^{-1}, respectively (Lada et al. 2010). This close agreement again supports the idea that the SFRs directly estimated for entire populations and averaged over 2 Myr are recovered from the sum of the "instantaneous" (0.3 Myr) accretion rates when those are dominated by Class 0/I stars, that is, $<SFR>_{2Myr} = \Sigma \dot{M}_{acc}^0 \equiv SFR_0$. In other words, the SFR is essentially constant over timescales of 2 Myrs, approximately ten times the typical protostellar lifetime.

2.2. Link between M_{dg} and M_{cs}

Next we consider the gas mass estimates on the horizontal axis of Fig. 1. The sum of all individual disk masses in Lupus from Manara et al. (2016) is ~ 0.25 $M_\odot$ (log $(\Sigma M_{disk}) \sim -0.6$), which is again orders of magnitude smaller than the M_{dg} value typically estimated for Lupus (log $M_{dg} \sim 2.4$; Lada et al. 2010). However, the sample in Manara et al. (2016) refers to evolved Class II stars that are associated with relatively small amounts of gas. For a more complete accounting of gas associated with young stars in a forming cloud, we need to include the contribution from protostellar (Class 0/I) objects to the dense gas budget (similar to the situation with the SFRs discussed above). Being embedded in dense cores and surrounded by infalling material, Class 0/I sources are associated with significantly higher amounts of dense gas. Indeed, protostellar objects are almost exclusively located in regions where the extinction exceeds 0.8 magnitudes at K band (e.g., Lombardi et al. 2014; Zari et al. 2016; Lada et al. 2017), which is the defining lower limit used by Lada et al. (2010) for their measurements of M_{dg} in nearby clouds.

Still, circumstellar dense cores likely only account for some fraction of the dense gas in a cloud, $\Sigma M_{cs} = f M_{dg}$. Because the boundary between a dense core and the surrounding dense gas in which it is embedded is difficult to determine or even define, the value of f is uncertain. Assuming that the bottom-up hypothesis is correct, we can extrapolate the roughly linear relation for the Lupus Class II sources to match the observed (total) SFR for the Lupus cloud and then predict the value of $\Sigma M_{cs} \sim$ SFR $\times \tau$, where τ is the accretion timescale of the Class II stars, $M_{disk}/\dot{M}_{acc}$. For SFR = 2×10^{-5} $M_\odot$ yr^{-1} (Lada et al. 2010) and τ ranging between ~ 0.15 and 4.25 Myr (Manara et al. 2016, see also Fig. 3 and the discussion in the next section), we find $3 < \Sigma M_{cs}/M_\odot < 85$ (i.e., $0.012 < \Sigma M_{cs}/M_{dg} < 0.34$), which for the ~ 20 Class 0/I sources in the cloud would mean $0.15 < <M_{cs}>/M_\odot < 4.2$. That is, the total mass of circumstellar gas directly participating in star formation in Lupus appears to represent between 1.2% and $\sim 34\%$ of the total dense gas reservoir measured in the cloud, and the gas mass around a protostar directly associated with accretion typically contains between $0.15 M_\odot$ and $4.2 M_\odot$. Direct measurements of some Class 0/I stars in Lupus indicate that a lower limit for $<M_{cs}>$ is $\sim 0.15 M_\odot$ (Mowat et al. 2017). This and additional Herschel measurements of M_{cs} in Lupus and other star-forming regions (Rygl et al. 2013; Könyves et al. 2015) may be suggesting that f is closer to 1% than to 35%.

Generally speaking, the gas mass of protostellar and prestellar dense cores typically ranges between 0.1 and 10 $M_\odot$ (e.g., Enoch et al. 2008); assuming that $3 < <M_{cs}>/M_\odot < 5$ and that $f \sim N_{protostars} \times <M_{cs}>/M_{dg}$, the recent extinction maps of local molecular clouds in Lombardi et al. (2014), Zari et al. (2016), and Lada et al. (2017) indicate that 7% < f(OrionA) < 12%, 22% < f(Perseus) < 33%, and 4% < f(California) < 7%. Therefore, a f value ranging between $\sim 1\%$ and 35% is reasonable. Such a

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[1] Three different timescales are used in this work: the "dissipation timescale" τ_*, as introduced here for Class 0/I and Class II stars; the "accretion timescale" $\tau = M_{cs}/\dot{M}_{acc}$ (which is $M_{disk}/\dot{M}_{acc}$ for Class II stars); and the "depletion timescale" M_{dg}/SFR, for clouds and galaxies.

range means that the corresponding log ($\Sigma\dot{M}_{acc}$)-log(ΣM_{cs}) values for the clouds should be shifted between 0.5 dex (f = 35%) and 2 dex (f = 1%) to the left from their log SFR-log M_{dg} values in Fig. 1 (the values for the vertical axis would remain practically equal, as previously argued). This change of intercept would not break the correlation and fits even better with the trend shown by stars (see Sect. 3). It is noted that a value of f closer to the upper limit of 35% is obtained if the prestellar cores are considered. Indeed, Herchel surveys indicate that the mass around these sources can dominate over the circumstellar mass around protostars (Könyves et al. 2015). In addition, inflow motions have been detected at least in some prestellar cores at large, sub-parsec scales (e.g., Tafalla et al. 1998).

In summary, the numbers provided should be taken as a first order approach, not only because of the uncertainties involved, but also because it has been assumed that the accretion timescale for Class 0/I sources is similar to that for Class II stars (as discussed below). In any case, our arguments strongly suggest that the sum of individual M_{cs} measurements of Class 0/I sources represents a non-negligible contribution to the total M_{dg} estimates for clouds from extinction maps, in agreement with the bottom-up hypothesis.

2.3. Some observational and theoretical implications

Given that the $\dot{M}_{acc}$ and M_{cs} values of Class 0/I sources dominate over more evolved stars, a major consequence is that the observed correlation between $\dot{M}_{acc}$ and M_{disk} in Class II stars could be the tip of the iceberg; our hypothesis implies that the correlation should continue with similar slope and intercept to $\dot{M}_{acc}$ and M_{cs} in earlier Class 0/I stages, filling the gap between the Class II stars and the clouds in Fig. 1. This means that the accretion timescale for Class 0/I stars, $M_{cs}/\dot{M}_{acc}$, should be roughly similar (~ within ± 1 dex) to that for Class II objects, $M_{disk}/\dot{M}_{acc}$. In other words, the decline of the accretion rate must occur at a pace comparable to that for the dissipation of the circumstellar material in order to keep a similar accretion timescale along the different stages of star formation. The latter has been observed in Class II stars (apart from the Lupus data studied here, see, e.g., Fedele et al. 2010), and has been suggested by observations (Bontemps et al. 1996) and modeling (see below) for Class 0/I sources independently. In fact, assuming a direct proportionality between accretion and ejection, a linear relation between $\dot{M}_{acc}$ and M_{cs} was inferred based on a comparative study of outflow activity in Class0/I objects (Bontemps et al. 1996).

However, a direct comparison between the Class II and Class 0/I accretion timescales is not feasible so far not only because of the observed scatter in the correlation for the Class II stars in the couple of star-forming regions that have been reliably probed (Manara et al. 2016; Mulders et al. 2017), but especially because such correlation has not been reported for Class 0/I sources, apart from indirect suggestions like the one mentioned above (Bontemps et al. 1996). Indeed, accurate $\dot{M}_{acc}$ and M_{cs} values for complete samples of Class 0/I sources are generally lacking. The extrapolation of line-luminosity to accretion-luminosity correlations (Mendigutía et al. 2015) to embedded objects are providing promising results (Pomohaci et al. 2017). In particular, mid-infrared (IR) emission lines could be useful to provide $\dot{M}_{acc}$ estimates of highly embedded stars (Rigliaco et al. 2015), for which the spectroscopic capabilities of the James Webb Space Telescope will be ideally suited. Ongoing submillimeter surveys devoted to characterize the accretion properties of Class 0 sources (Herczeg et al. 2017) will also be of great value. Regarding M_{cs},

ALMA should be able to make an improved census of the protostellar envelope masses in several star-forming regions.

Similarly, our hypothesis suggests that a relevant theoretical framework must be able to predict a $\dot{M}_{acc}$-M_{cs} correlation at the initial Class 0/I stages. Such type of theories have already been proposed, for example, predicting the $\dot{M}_{acc}$-M_{disk} correlation in Class II stars from the imprint of the parent, turbulent core, either from its rotational properties (Dullemond et al. 2006) or/and from gravitational instabilities and density perturbations (Vorobyov & Basu 2008). Alternatively, similar correlations for Class 0/I sources have also been reproduced in models that do not assume ad-hoc initial and boundary conditions for the cores, but emphasize the importance of the turbulent medium considering the cloud as a whole (Padoan et al. 2014). According to this view, the observed $\dot{M}_{acc}$-M_{disk} correlation in Class II stars would not be caused by the disk physics but would be evidence of an underlying $\dot{M}_{acc}$-M_{cs} correlation in previous Class 0/I stages. In other words, if our hypothesis is confirmed, viscous disk evolution should be dominant only when the envelopes have dissipated, but its influence on the location of Class II stars in the $\dot{M}_{acc}$-M_{disk} plane – and thus on the corresponding accretion timescale $M_{disk}/\dot{M}_{acc}$ – would be less relevant as this would have been mainly determined at earlier, embedded stages.

3. The global correlation

As introduced in Sect. 1, strong lines of evidence show that the SFR and M_{dg} values of Galactic clouds and whole galaxies are connected through a linear relation. Figure 2 extends Fig. 1, adding the SFR and M_{dg} values of the 65 normal spiral galaxies, LIRGS, and ULIRGS at distances between a few and a few hundred Mpc from Gao & Solomon (2004). The global correlation including all sources overlaps with that for clouds and stars derived in the previous section is also statistically significant (p = 2.6×10^{-36}), and has a slope N close to (but still different from) unity (the 3σ fit is log SFR = -6.8(±0.2) + 0.88(±0.06)log M_{dg}; correlation coefficient = 0.99). As in the previous section, the values for the probability of false correlation and the linear correlation coefficient have been derived from the partial correlation technique (e.g., Wall & Jenkins 2003), indicating that the global correlation is not driven by the wide range of distances to the sources. Therefore, from the statistical perspective the SFR-M_{dg} correlation can be extended from galaxies and clouds to young stars when $\dot{M}_{acc}$ and M_{disk} are used for the latter objects. Once again the inclusion of additional data or the use of different scaling factors between the observations and the physical parameters compared would not have a significant effect on our discussion (Appendices A and C). Moreover, one may still think that any stellar parameter could appear to be similarly correlated on a log-log diagram when such a huge range in both axes is considered, but Appendix C shows that this is not the case.

Wu et al. (2005) proposed that the correlation in galaxies can be understood from the sum of basic units within each galaxy, concluding that these are clumps that host high-mass young stars. However, Appendix B shows that distance dependencies and the fact that the correlation extends to local clouds that do not generally form massive stars (Lada et al. 2010, 2012) makes this conclusion less robust (see also Stephens et al. 2016). Recently, Shimajiri et al. (2017) proposed that the relation between kiloparsec-size galaxies and parsec-size clouds may be governed by the "microphysics" of core and star formation along filaments within the clouds. Following these lines of reasoning and based on Fig. 2 and our results in the previous section, we propose that, as basic products of star formation, the (sub-)parsec-size in-
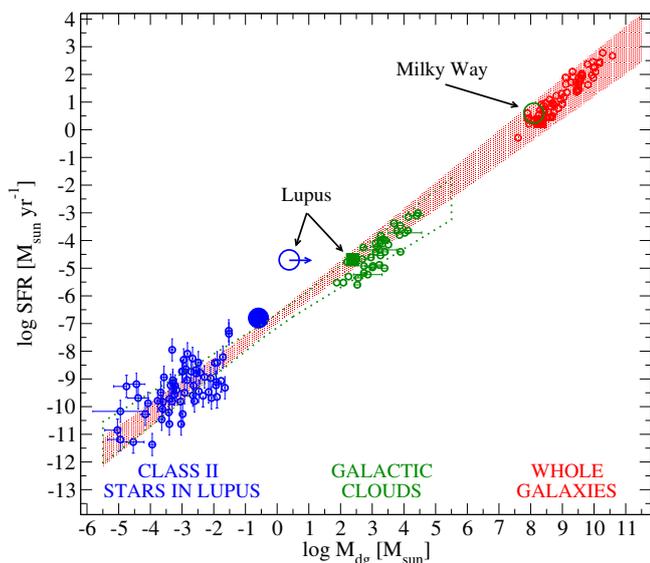
Fig. 2. Figure 1 including galaxies (red circles; Gao & Solomon 2004). The fit for the stars and clouds is now indicated by the region enclosed within the green dotted line. The red dotted region is the 3σ global fit for all sources. The green open circle is the sum of 4×10^4 clouds with a typical SFR and M_{dg}, and the red solid square is the direct measurement of SFR and M_{dg} in the MW (see text).

Fig. 3. Accretion timescales $M_{cs}/\dot{M}_{acc} = 0.1, 1, 5$, and 10 Myr are indicated from top to bottom with the dashed lines. The original data for the clouds and the galaxies in Fig. 2 (green and red open circles) are shifted -1.3 dex in the x-axis (green and red filled circles), corresponding to a fraction of gas directly associated with star formation of 5% the total dense gas mass measured in those systems.

dividual protostellar systems may ultimately drive the observed correlation not only for protostellar-hosting clouds but also for cloud-hosting galaxies.

Our Galaxy follows the global correlation showing log SFR ~ 0.3 (Chomiuk & Povich 2011; Kennicutt & Evans 2012) and log $M_{dg} \sim 8.3$ (e.g., Stephens et al. 2016, and references therein). These values can be roughly recovered, for example, by summing up a reasonable value of $\sim 4\times10^4$ clouds with a typical log SFR = -4 and log M_{dg} = 3.5. Regardless of the exact numbers, the bottom line is that the SFR and M_{dg} estimates for the MW or any other galaxy could in principle be derived also from the sum of the accreting stellar population within each galaxy, since we have shown in the previous section that the SFR and M_{dg} values for the clouds scale with the sum of the $\dot{M}_{acc}$ and M_{cs} values of the stars hosted by them. For the same reason argued when the SFRs of the clouds and the instantaneous accretion rates of the stars were compared, if our bottom-up hypothesis can be extended to whole galaxies, then their SFRs should be roughly constant along a timescale of 10-100 Myr, given that such a timescale is the one usually considered to estimate galactic SFRs (Appendix A).

In addition, because estimates for clouds and galaxies are averaged over the entire systems, we show in Appendix D that our bottom-up hypothesis firstly implies that the intercepts in the linear relations derived for stars, clouds, and galaxies individually should be roughly similar, and secondly that the scatter should decrease from stars to galaxies. The second consequence is clearly observed in our data (the y-axis dispersion in galaxies decreases again to $\sim \pm 0.5$ dex, see also Sect. 2), in the more complete sample of clouds and galaxies studied by Stephens et al. (2016), or in the very recent work by Tan et al. (2018) (but see also Lada et al. 2012; Shimajiri et al. 2017). The first consequence presents some caveats. As discussed in Appendix D, the least-squares intercepts should be similar at least if all stars have comparable $\dot{M}_{acc}/M_{cs}$ ratios (see Sect. 2.3) and if the fraction of dense gas directly involved in star formation is $f \sim 100\%$. Under these assumptions, the gas depletion timescale derived for galax-
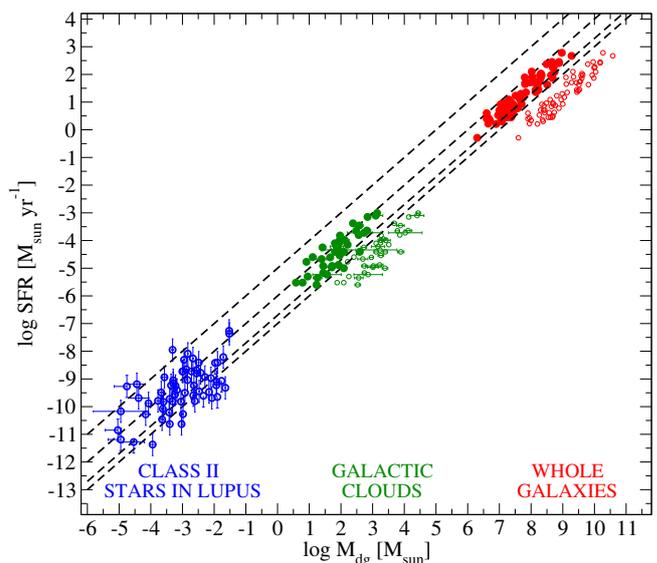
ies and clouds from least-squares fitting (M_{dg}/SFR) should be the same as the accretion timescale of the stars ($M_{cs}/\dot{M}_{acc}$), but the former should be larger than the latter if $f < 100\%$. Indeed, Fig. 3 shows that whereas an accretion timescale ranging between ~ 0.1 and 10 Myr matches the Class II stars, the original data for the clouds and the galaxies fall displaced to the right, consistent with larger timescales. Shifting the clouds and galaxies between ~ -0.5 and -2 dex in the x-axis provides a better match with the stars, finally resulting in a global correlation with near unity slope and an intercept more consistent with the stellar accretion timescale (e.g., for the shift shown in Fig. 3, log SFR = -6.3(± 0.1) + 0.98(± 0.02)log M_{dg}). Given that $\Sigma M_{cs} = fM_{dg}$, the previous shift range corresponds to $0.01 < f < 0.35$, suggesting that the amount of gas directly participating in star formation should be roughly between 1% and 35% the total dense gas mass measured in clouds and galaxies, in agreement with the observational data discussed in the previous section. Once again the underlying assumption is that the dominating Class 0/I sources have a similar accretion timescale as observed for Class II stars, for which we remark that accurate measurements of $\dot{M}_{acc}$ and M_{cs} for Class 0/I stars are the most critical observations needed to test the bottom-up hypothesis.

4. Summary and conclusions

The gas-to-star transformation rate and the dense gas mass available for star formation show a statistically significant correlation that has been extended from galaxies and Galactic clouds to individual young stars. The correlation spreads ~ 16 orders of magnitude, covering spatial scales from distant (hundreds of Mpc) galaxies with sizes of a few Kpc, to nearby (~ 150 *pc*) proto-planetary disks with sizes of hundreds of au. Given the difference between the intercepts of the individual linear fits determined for protoplanetary disks, star-forming clouds, and galaxies, it is not clear how physically meaningful the global correlation is. Here we have proposed and explored one possible unifying hypothesis that could explain the global correlation.

Our bottom-up hypothesis is that the correlation between the mass accretion rate and the total circumstellar gas mass surrounding young – mainly Class 0/I – stars is the underlying cause of the global correlation on all scales. Two main lines of evidence supporting this scenario have been provided. First, the SFRs of molecular clouds are recovered from the sum of empirically based stellar accretion rates. Second, the sum of the individual circumstellar gas masses appears to represent a relevant fraction of the total dense gas mass within such clouds. If that fraction is between $\sim$ 1% and 35 % of the dense gas mass in clouds and galaxies, then the global correlation has a near unity slope and intercept consistent with the stellar accretion timescale, $M_{cs}/\dot{M}_{acc}$. Indeed, a crucial test of our hypothesis is that the $\dot{M}_{acc}$-M_{disk} linear correlation on astronomical unit scales for Class II stars should also be observed between $\dot{M}_{acc}$ and M_{cs} on (sub-)parsec scales for Class 0/I sources. Our hypothesis also explains that the scatter in the correlation decreases from stars to galaxies, and implies that the average SFR of galaxies remains constant on a timescale of $\sim$ 10-100 Myr.

The $\dot{M}_{acc}$-M_{disk} and SFR-M_{dg} correlations in stars, clouds, and galaxies have been independently studied from physical contexts relatively isolated from each other. Our result suggests a global approach and that theoretical efforts should consider all scales and physical systems involved in a single correlation.

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Appendix A: Estimates of the different parameters for stars, clouds, and galaxies

This appendix refers to the different ways that the parameters compared in Figs. 1 and 2 were derived.

Stars: Values of $\dot{M}_{acc}$ refer to the instantaneous disk-to-star accretion rates, which were derived by fitting an accretion shock model to the extinction-corrected near-ultraviolet (UV) excess. Values of M_{disk} were calculated from ALMA submillimeter continuum data using typical assumptions of a single dust grain opacity $\kappa(890 \ \mu m) = 3.37 \ cm^2 \ g^{-1}$, a single dust temperature $T_{dust} = 20$ K, and a gas-to-dust ratio of 100. Further details can be found in Manara et al. (2016) and references therein. The typical densities of protoplanetary disks are $n(H_2) > 10^5 \ cm^{-3}$, which can be as high as $> 10^8 \ cm^{-3}$ in the innermost, densest regions (see, e.g., Bergin et al. 2007, and references therein).

Nearby clouds: The SFRs were derived by counting the number of young stars within each cloud (N_{stars}), assuming a typical IMF mass ($M_* = 0.5 M_\odot$), and a common age for all sources ($t_* = 2$ Myr). Then $SFR(M_\odot \ yr^{-1}) = N_{stars} \times M_*/ t_* = 0.25 \times 10^{-6} \ N_{stars}$[2]. In turn, M_{dg} was calculated from Two Micron All Sky Survey (2MASS) extinction maps of the clouds with $A_K > 0.8$ magnitudes and a gas-to-dust ratio of 100, which involves gas densities $n(H_2) > 10^4 \ cm^{-3}$. Further details can be found in Lada et al. (2010).

Distant clouds: SFR and M_{dg} values were derived from the IR luminosities (L_{IR}, from 8 to 1000 μm) and the HCN (1–0) luminosities (L_{HCN}) listed in Wu et al. (2010), following the same procedure as for the galaxies in Gao & Solomon (2004), described in the following.

Galaxies: SFRs were derived from unresolved measurements of L_{IR}, assuming that this is produced primarily from dust heating by O, B, and A stars, a typical Salpeter IMF, and applying $SFR \ (M_\odot \ yr^{-1}) = 2 \times 10^{-10} \times (L_{IR}/L_\odot)$. This methodology implicitly assumes that the SFR is constant along a timescale of ~ 100 Myr. Values of M_{dg} were estimated from unresolved measurements of L_{HCN} by applying $M_{dg} = \alpha_{HCN} \times L_{HCN}$, with $\alpha_{HCN} = 10 \ M_\odot$ (K km s^{-1} pc^2)$^{-1}$ a constant derived assuming that L_{HCN} is emitted by the gravitationally bound cloud cores with a brightness temperature of 35 K. The gas densities involved are also $n(H_2) > 10^4 \ cm^{-3}$. Further details can be found in Gao & Solomon (2004). It is noted that recent works claim that HCN (1–0) traces densities an order of magnitude smaller (Pety et al. 2017; Kauffmann et al. 2017b). However, Kauffmann et al. (2017b) show that even in this case the M_{dg} values derived from L_{HCN} would differ from those in Gao & Solomon (2004) by less than a factor of two, which would not have a significant effect on our results.

Despite the fact that there are differences in the methodologies, spatial, and temporal scales involved to derive the parameters, all are referred to the same two physical concepts: the rate at which gas is transformed into stars, and the mass of dense gas related to stellar formation. Thus, the comparison between them can and should be carried out. Lada et al. (2012) compared the SFRs and M_{dg} values in clouds and galaxies, as estimated from the different methodologies summarized above (see also, e.g., Shimajiri et al. 2017). Therefore, in our work we have mainly focused on the comparison between $\dot{M}_{acc}$-SFR and M_{disk}-M_{dg} in stars and clouds, when the latter were derived from direct counts of stars and extinction maps, respectively.

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[2] That is, the SFR derived in this way implicitly assumes that the individual stars are actually the basic units driving the correlation, in agreement with the bottom-up hypothesis of this work

Appendix B: Re-analysis of the Wu et al. (2005) sample of distant Galactic clouds

Figures 1 and 2 do not include the distant Galactic clouds from Wu et al. (2010) with log $M_{dg} < 2.50$ (log $L_{HCN} < 1.50$). As shown in Wu et al. (2005), these clouds do not follow the linear correlation but have a super-linear slope. In other words, for a given M_{dg} below that limit, distant Galactic clouds have a smaller SFR than predicted from the trend followed by the remaining Galactic clouds and the galaxies. Figure B.1 (left) shows that the ratio SFR/M_{dg} of the clouds from Wu et al. (2010) actually increases with M_{dg} up to the mentioned limit, remaining roughly constant from that point. Based on this change of slope, Wu et al. (2005) proposed the existence of a basic unit in star formation: if M_{dg} is below the mass of that unit, SFR/M_{dg} rises with M_{dg} because clouds with low M_{dg} do not sample the IMF completely by excluding high-mass stars. If M_{dg} is above the mass of that unit, then the IMF is completely sampled and additional increases of M_{dg} produce more units but not further increases in SFR/M_{dg}. In short, Wu et al. (2005) proposed that the star formation correlation in other galaxies can be understood from the sum of basic units within each galaxy, these units being clouds with high-mass young stars. However, Fig. B.1 (right) shows that the ratio SFR/M_{dg} also follows a trend with the distance to the clouds that is very similar to that with M_{dg}. The SFR/M_{dg} ratio also increases for d < 2.5 kpc, remaining roughly constant from that point. The Spearman's probability of false correlation accounting for the distances from the partial correlation technique (e.g., Wall & Jenkins 2003) is 0.1 when only the 22 clouds with log $M_{dg} < 2.50$ from Wu et al. (2010) are plotted in the SFR-M_{dg} plane. This high p-value (> 0.05) indicates that the SFR-M_{dg} correlation for those sources is spurious since this is mainly driven by the d^2 factor used to compute both parameters compared. Therefore, it cannot be concluded that the change of the SFR/M_{dg} ratio is caused by a physical limit in M_{dg} because the influence of the distance cannot be ruled out. In conclusion, the proposal of high-mass star-forming clouds as the basic units driving the linear correlation cannot be supported from that data.

In addition, the break of the SFR-M_{dg} linear relation for clouds with low M_{dg} could be explained from the fact that L_{IR} was used as a tracer to measure the SFR. Most of the IR is emitted by high-mass stars and as soon as they are missing L_{IR} could no longer be a good proxy of the SFR. In either case, by using different tracers for M_{dg} and SFR Lada et al. (2010, 2012) already showed that the linear correlation is also valid for nearby clouds that do not necessarily host massive stars.

Appendix C: Is the global correlation just the result of a large-scale, log-log diagram?

One may wonder if the enormous extent covered by the axes in Fig. 2 somewhat hides the scatter and washes out significant trends within the data or, in other words, if any parameter could appear correlated simply because we are zooming out. Whereas the scale considered certainly has an effect on whether this or any other empirical trend is identified or not, not all data fit within the global correlation analyzed in this work.

We have compiled additional data on top of that analyzed in Fig. 2, which is plotted in Fig. C.1 (references included in the caption). First, recent ALMA measurements of Class II stars in the Cha I star-forming region (blue crosses) have been added to the Lupus sources, both constituting the only complete data for Class II stars available to date. Even when the origin of the large scatter in $\dot{M}_{acc}$ is subject to debate (accretion variability,
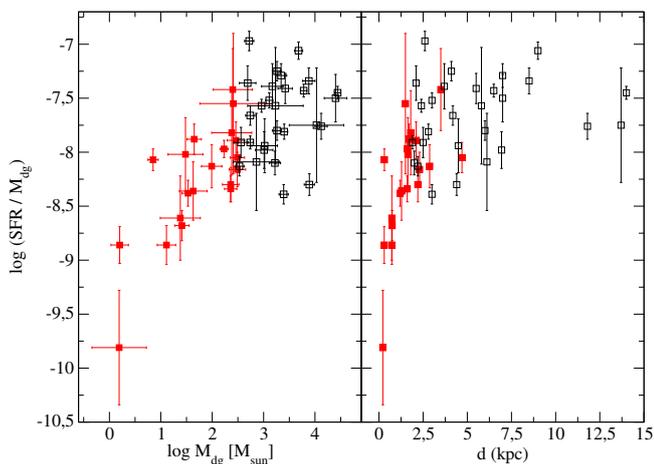
Fig. B.1. SFR/M_{dg} ratio versus the dense gas mass (left) and the distance (right) for all distant Galactic clouds from Wu et al. (2010). Red-filled and open squares correspond to log M_{dg} < and > 2.50, respectively (log L_{HCN} < and > 1.50).

observational limits, sample selection effects, different evolutionary stages and initial conditions in previous phases; see, e.g., Mendigutía et al. 2015; Manara et al. 2016; Mulders et al. 2017, and references therein), it has been shown that there is a statistically significant, roughly linear correlation in each star-forming region separately (Manara et al. 2016; Mulders et al. 2017). Indeed, considering the Lupus and Cha I samples together, we derive a slope ∼ 0.9 ± 0.2. Concerning the rest of the new data in Fig. C.1, the samples are selected because they have been reported to show deviations with respect to the linear scaling relation. For instance, the additional sample of (U)LIRGS (red crosses) shows a slightly super-linear slope. On the contrary, pointings of specific regions in disks of other galaxies (orange circles, see also, e.g., Bigiel et al. 2016) show a sub-linear slope, as well as clouds close to the Galactic center (green triangles with error bars) when these are considered alone. These sub-trends are relatively washed out under the axes range considered here and are roughly incorporated to the global correlation. In addition, the central molecular zone (orange squares) and some massive clumps in our Galaxy from the Millimetre Astronomy Legacy Team 90 GHz (MALT90) survey (green crosses with ∼ log M_{dg} < 4) appear displaced from the global correlation even when such a large axes range is used. Despite the fact that the tracers and methodology used to derive the SFR and M_{dg} values in many of the samples included in Fig. C.1 are the same as those described in Appendix A, different approaches have also been used (see, e.g., Longmore et al. 2013; Kauffmann et al. 2017a). The recent work by Shimajiri et al. (2017) may solve most apparent deviations with respect to the global correlation from a careful determination of the conversion factors between the observables and the physical parameters involved (see also, e.g., Lada et al. 2012; Tan et al. 2018), which have not been considered in this work. However, even if the correlation changes in certain environments, the scope of this paper is not to explain the possible sub-trends within the global correlation but to point out that the individual stars could eventually play a role in such an explanation by means of the bottom-up hypothesis.

In contrast, Fig. C.1 also shows that when the stellar masses are plotted instead of the disk masses (black circles and crosses), the well known $\dot{M}_{acc}$-M_* correlation (e.g., Mendigutía et al. 2015; Mulders et al. 2017, and references therein) shows up with a very different slope and intercept, and can be clearly distin-
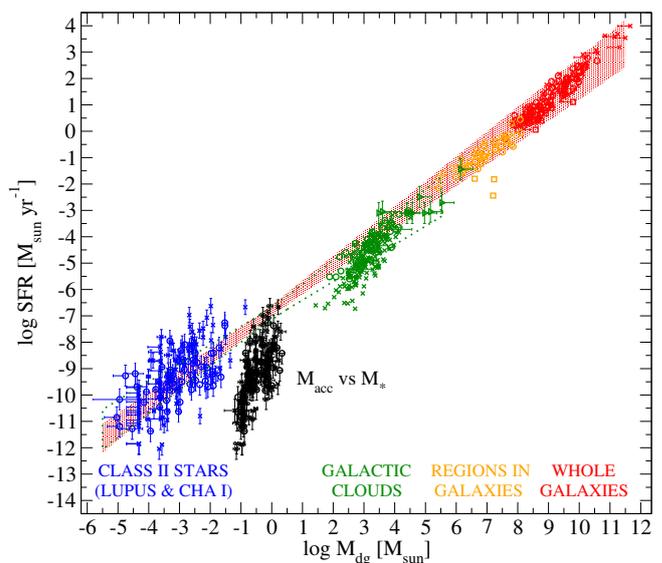
Fig. C.1. Data and linear fits shown in Fig. 2 including additional samples: Class II stars in the Cha I star-forming region (blue crosses; Mulders et al. 2017); massive Galactic clumps from the MALT90 survey (green crosses; Stephens et al. 2016); molecular clouds close to the Galactic center (green triangles; Kauffmann et al. 2017a); the central molecular zone (CMZ) in our Galaxy (orange squares; Longmore et al. 2013), regions within disks of other galaxies (orange circles; Usero et al. 2015), (U)LIRGS and star-forming galaxies (red crosses and red squares; García-Burillo et al. 2012; Usero et al. 2015). On the other hand, the accretion rates in Lupus and Cha I are plotted versus the stellar masses instead of the disk masses (black circles and crosses; Manara et al. 2016; Mulders et al. 2017).

guished from the global correlation linking stars, clouds, and galaxies. This simple modification in one of the axes demonstrates that not any single stellar parameter appears to be correlated in a logarithmic scale plot spanning over a huge axes range.

Appendix D: Relation between least-squares intercepts for stars, clouds, and galaxies

The $\dot{M}_{acc}$-M_{disk} linear relation observed in Class II stars can be generalized to also include the total circumstellar gas mass in Class 0/I sources. For a sample of young stars in a given cloud, this is expressed as log $\dot{M}_{acc}$ = log K_s + log M_{cs}. If least-squares linear regression is used, by definition the intercept is given by log K_s = <log $\dot{M}_{acc}$> - <log M_{cs}>, where the arithmetic means refer to the total number of stars in the cloud (N_s). The value of K_s can then be expressed as

$$K_s = \left(\prod_{i=1}^{N_s} \frac{\dot{M}_{acc_i}}{M_{cs_i}} \right)^{1/N_s} = \left(\prod_{i=1}^{N_s} k_{s_i} \right)^{1/N_s} , \quad (D.1)$$

with $k_{si} = \dot{M}_{acc_i}/M_{csi}$ the ratio between the accretion rate and the circumstellar gas mass for each star. Therefore, K_s is the geometric mean of the individual k_{si} ratios for each star. Similarly, the least-squares intercept derived for a sample of N_c clouds provides a K_c value that is the geometric mean of the individual SFR$_j$/$M_{dg\,j}$ ratios of each cloud, and equivalently for a sample of galaxies. Under the hypothesis proposed in this work, the SFR of a given cloud is given by the sum of the individual accretion rates of the stars within that cloud. Similarly, the M_{dg} values are given by the sum of the total circumstellar gas masses of the stars

within that cloud, divided by a factor f that accounts for the fraction of dense gas mass that is directly involved in star formation (i.e., for a given cloud $\Sigma M_{cs} = f M_{dg}$). Therefore,

$$K_c = \left(\prod_{j=1}^{N_c} \frac{f_j < \dot{M}_{\mathrm{acc}} >_j}{< M_{cs} >_j} \right)^{1/N_c} = \left(\prod_{j=1}^{N_c} f_j k_{c_j} \right)^{1/N_c}. \qquad (D.2)$$

Similarly, for a sample of N_g galaxies,

$$K_g = \left(\prod_{k=1}^{N_g} \frac{f_k < \dot{M}_{\mathrm{acc}} >_k}{< M_{cs} >_k} \right)^{1/N_g} = \left(\prod_{k=1}^{N_g} f_k k_{g_k} \right)^{1/N_g}. \qquad (D.3)$$

Equations D.1, D.2, and D.3 show that the intercepts of clouds and galaxies are determined mainly by the ratio between the accretion rate and the circumstellar gas mass of the young stars hosted by them. The simplest scenario occurs when this ratio is the same for all stars, that is, $k_{si} = k_s = \dot{M}_{\mathrm{acc}}/M_{cs}$, and the fraction of dense gas directly participating in stellar accretion is the same for all clouds and galaxies. In this case $f K_s = K_c = K_g$, that is, the intercepts of clouds and galaxies are the same as for the stars only if the amount of gas directly participating in star formation is 100% of the dense gas in clouds and galaxies ($f = 1$), and smaller than the stars otherwise ($0 < f < 1$). From a physical perspective, $\tau_s = k_s^{-1}$ is the accretion timescale on which all M_{cs} would fall onto a given star for a constant mass accretion rate $\dot{M}_{\mathrm{acc}}$. Under the assumption of equal accretion to circumstellar gas ratios and f-factors, $\tau_s/f = \tau_c = \tau_g$, which means the gas depletion timescales for clouds and galaxies are the same as the accretion timescales for the stars only if the amount of gas directly participating in star formation is 100% of the dense gas in clouds and galaxies ($f = 1$), and larger than the stars otherwise ($0 < f < 1$).

Finally, when a single cloud is considered, Eq. D.2 reduces to $K_c = f k_c = f <\dot{M}_{\mathrm{acc}}>/<M_{cs}> = \sum_{i=1}^{N_s} f k_{si} M_{csi}/\sum_{i=1}^{N_s} M_{csi}$. For a given M_{cs} value, the scatter in $\dot{M}_{\mathrm{acc}}$ for the stars can be quantified through a fixed value $\sigma k_{si} = \sigma k_s$, which translates to

$$\sigma k_c = \sigma k_s \times \left(\frac{\sum_{i=1}^{N_s} M_{cs_i}^2}{\left(\sum_{i=1}^{N_s} M_{cs_i} \right)^2} \right)^{1/2} < \sigma k_s. \qquad (D.4)$$

Consequently, for the galaxies, $\sigma k_g < \sigma k_c$. Therefore, the y-axis scatter in the global correlation should be maximum for stars and decreases from clouds to galaxies.