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## 1 **Wall shear stress at the initiation site of cerebral aneurysms**

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4  
5 Received: date / Accepted: date

6 **Abstract** Hemodynamics are believed to play an important role in the initiation of  
7 cerebral aneurysms. In particular, studies have focused on wall shear stress (WSS),  
8 which is a key regulator of vascular biology and pathology. In line with the obser-  
9 vation that aneurysms predominantly occur at regions of high WSS, such as bifurca-  
10 tion apices or outer walls of vascular bends, correlations have been found between  
11 the aneurysm initiation site and high WSS. The aim of our study was to analyze  
12 the WSS field at an aneurysm initiation site that was neither a bifurcation apex nor  
13 the outer wall of a vascular bend. Ten cases with aneurysms on the A1 segment of  
14 the anterior cerebral artery (ACA) were analyzed and compared with ten controls.  
15 Aneurysms were virtually removed from the vascular models of the cases to mimic  
16 the pre-aneurysm geometry. Computational fluid dynamics (CFD) simulations were  
17 created to assess the magnitude, gradient, multidirectionality, and pulsatility of the  
18 WSS. To aid the inter-subject comparison of hemodynamic variables, we mapped  
19 the branch surfaces onto a two-dimensional parametric space. This approach made it

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Preliminary findings from this study were presented at the International Symposium on Biomechanics in Vascular Biology and Cardiovascular Disease, Montreal, QC, Canada, 28–29 April 2014 and at the European Solid Mechanics Conference, Madrid, Spain, 6–10 July 2015.

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possible to view the whole branch at once for qualitative evaluation. It also allowed us to define a patch for quantitative analysis, which was consistent among subjects and encapsulated all aneurysm initiation sites. To test the reproducibility of our results, CFD simulations were repeated with a second independent observer virtually removing the aneurysms and with a 20 % higher flow rate at the inlet. We found that branches harboring aneurysms were characterized by high WSS and high WSS gradients. Among all assessed variables, the aneurysm initiation site most consistently coincided with peaks of temporal variation in the WSS magnitude.

**Keywords** aneurysm initiation · cerebral aneurysms · computational fluid dynamics · hemodynamics · image-based modeling · flow pulsatility · wall shear stress

## 1 Introduction

Cerebral aneurysms are localized, pathological dilatations of cerebral arteries. Their rupture causes subarachnoid hemorrhage and is associated with high rates of morbidity and mortality (Hop et al, 1997). Better understanding of the mechanisms underlying aneurysm initiation is crucial for the development of new preventive and therapeutic strategies (Jamous et al, 2005).

While systemic risk factors such as hypertension and connective tissue disorders may weaken the cerebral arteries' ability to maintain homeostasis, hemodynamic stress appear to be a necessary trigger for the pathological remodeling leading to aneurysm formation (Brown et al, 1990; Stehbens, 1989; Nixon et al, 2010; Penn et al, 2011; Dolan et al, 2013; Sadasivan et al, 2013; Meng et al, 2014; Frösen, 2014; Turjman et al, 2014). In vivo measurements of these stresses are limited by the low spatial and temporal resolution of current imaging techniques (Markl et al, 2012) and the rarity of imaging a patient prior to aneurysm formation. Instead, computational fluid dynamics (CFD) techniques have been employed to simulate the hemodynamics in vascular geometries with the aneurysm virtually removed to approximate the pre-aneurysm condition (Mantha et al, 2006; Baek et al, 2009; Ford et al, 2009; Shmogonya et al, 2009; Singh et al, 2010; Castro et al, 2011; Chen et al, 2013; Kono and Terada, 2013; Lauric et al, 2014) and in vascular geometries derived from rare pre-aneurysm images (Doenitz et al, 2010; Kulcsar et al, 2011; Kono and Terada, 2013; Kono et al, 2014). CFD simulations have also been used to complement histological analyses of aneurysm formation in animal models (Meng et al, 2007; Metaxa et al, 2010).

Hemodynamic studies have strongly focused on wall shear stress (WSS), which is a key regulator of vascular biology and pathology (Dolan et al, 2013). In line with the observation that aneurysms predominantly occur at high WSS regions such as bifurcation apices or outer walls of vascular bends (Kondo et al, 1997; Alnaes et al, 2007; Piccinelli et al, 2011; Alfano et al, 2013), many studies have found correlations between the aneurysm initiation site and high WSS (Castro et al, 2011; Singh et al, 2010; Chen et al, 2013), especially in combination with high positive WSS gradients (WSSG) (Meng et al, 2007; Metaxa et al, 2010; Kulcsar et al, 2011; Kono and Terada, 2013; Kono et al, 2014). Other studies have found correlations with low WSS (Mantha et al, 2006; Doenitz et al, 2010), WSS patterns involving both high and low

WSS (Baek et al, 2009; Lauric et al, 2014), or indices describing the oscillatory nature of the WSS and WSSG (Mantha et al, 2006; Ford et al, 2009; Shimogonya et al, 2009; Chen et al, 2013). These apparent inconsistencies among CFD-based studies can be attributed to the small datasets, variety of aneurysm locations, and subjectivity of data analyses, as pointed out by Chen et al. (Chen et al, 2013), but also to missing patient-specific information about boundary conditions and properties of the arterial wall.

The aim of our study was to analyze the WSS field at the aneurysm initiation site. All included aneurysms were from a single location, which was neither a bifurcation apex nor the outer wall of a vascular bend. Vascular geometries with the aneurysm removed were matched to controls that never formed an aneurysm at that particular location but elsewhere. To standardize the data analysis and simplify the comparison of cases, branches of interest were mapped onto the same parametric space. Tests were performed to measure the reproducibility of the computed WSS field with respect to the observer virtually removing the aneurysm and the flow rate imposed at the inlet.

## 2 Methods

### 2.1 Case selection

Twenty patients, ten cases and ten controls, were drawn from a large multicenter database created within the EU-funded project @neurIST (Villa-Uriol et al, 2011). The data collection protocol was approved by individual local ethics committees, and written consent was obtained from patients or, where appropriate, next of kin. The cases were all the patients in the database with an aneurysm on the A1 segment of the anterior cerebral artery (ACA). They were selected because of their remarkable consistency in aneurysm location: all aneurysms were just distal to the internal carotid artery (ICA) bifurcation with nine cases directed posteriorly (cases 1 to 9) and one case directed anteriorly (case 10). Moreover, the location was neither a bifurcation apex nor the outer wall of a vascular bend, which – attributed to being high WSS regions – are the most common aneurysm locations (Kondo et al, 1997; Alnaes et al, 2007; Piccinelli et al, 2011; Alfano et al, 2013). The controls were patients with an aneurysm at the middle cerebral artery (MCA) bifurcation, hence predisposed to having aneurysms, that did not form an aneurysm at the studied location on the A1 segment of the ACA. They were selected to match cases by patient age (within 2 years) and aneurysm hemisphere (left or right). No other information was considered during the selection process.

### 2.2 Vascular modeling

Patient-specific vascular models, represented by triangular surface meshes, were constructed by segmenting three-dimensional rotational angiography (3DRA) images using a geodesic active regions approach (Bogunović et al, 2011). The ophthalmic

102 artery, anterior choroidal artery, and posterior communicating artery branching off  
103 the ICA were preserved if successfully segmented. Touching vessels were removed.  
104 Models were smoothed using a geometry-preserving smoothing algorithm (Nealen  
105 et al, 2006). To ensure consistency in the extent of the vascular models, inlet and  
106 outlet branches were clipped at the same location for all cases and controls. Inlet  
107 branches were clipped at a manually selected location at the start of the cavernous  
108 segment of the ICA and then extruded 10 mm to allow for flow to develop. Outlet  
109 branches were automatically clipped 10 mm from their proximal bifurcation; those  
110 shorter than 10 mm were first extruded. The ACA had to be extruded only for control  
111 6. Figure 1 shows the vascular models of all cases and controls.

112 Aneurysms were virtually removed from the vascular models of the cases to  
113 mimic the pre-aneurysm geometry (Figure 1). Triangle removal and hole filling op-  
114 erations were iteratively applied to reconstruct the ACA without aneurysm. Subse-  
115 quently, the vascular model was smoothed and inlet and outlet branches were clipped  
116 as described in the previous paragraph. To assess the reproducibility of the computed  
117 WSS field with respect to this manual procedure, two observers independently re-  
118 moved the aneurysm for all cases.

119 The automatic selection of outlet locations made use of centerlines and bifurca-  
120 tion origins generated with the Vascular Modeling Toolkit (VMTK) (Antiga et al,  
121 2008; Piccinelli et al, 2009). Manual mesh editing operations were performed in  
122 @neuFuse (B3C, Bologna, Italy) (Villa-Uriol et al, 2011), a software application de-  
123 veloped within @neurIST.

## 124 2.3 Blood flow modeling

125 Unstructured volumetric meshes were created with ICEM CFD 13.0 (ANSYS, Canons-  
126 burg, PA, USA) using an octree approach. Meshes were composed of tetrahedral el-  
127 ements with a side length of 0.2 mm and three prism layers with a total height of  
128 0.07 mm and a side length of 0.1 mm. The total number of elements ranged from 2.3  
129 to 6.7 million, the density from 3124 to 4076 elements per  $\text{mm}^3$ , depending on the  
130 surface-area-to-volume ratio of the computational domain. This mesh resolution was  
131 chosen following previously performed mesh dependency tests (Geers et al, 2014).

132 CFD simulations were created with CFX 13.0 (ANSYS), which is a commercial  
133 vertex-centered finite volume solver. We used a second-order advection scheme and a  
134 second-order backward Euler transient scheme. Solutions converged until the normal-  
135 ized residual of the WSS everywhere in the computational domain was  $< 5 \times 10^{-4}$ .

136 Blood was modeled as an incompressible Newtonian fluid with density  $\rho = 1060 \text{ kg/m}^3$   
137 and viscosity  $\mu = 4 \text{ mPa s}$ . Although blood is a non-Newtonian fluid, assuming con-  
138 stant viscosity is appropriate for our problem (Morales et al, 2013). Vessel walls were  
139 assumed rigid with a no-slip boundary condition. A parabolic velocity profile was im-  
140 posed at the inlet.

141 Since patient-specific flow information was unavailable, we estimated the flow  
142 rate waveform at the inlet and imposed zero-pressure boundary conditions at all out-  
143 lets. The shape of the flow rate waveform was obtained from Ford et al. who aver-  
144 aged the waveform shapes of 17 young, normal volunteers (Ford et al, 2005). The

145 time-averaged flow rate,  $Q$ , was obtained using the relationship from Cebal et al.:  
 146  $Q = 48.21 A^{1.84} T^{-1}$  where  $Q$  is in ml/s,  $A$  is the inlet's cross-sectional area in  $\text{cm}^2$ ,  
 147 and  $T$  is the period of the cardiac cycle in s. This relationship was obtained by fitting  
 148 a power-law function through measurements of  $Q$  and  $A$  of the ICAs and vertebral  
 149 arteries of 11 normal volunteers (Cebal et al, 2008). Reynolds numbers at the inlets  
 150 ranged from 62 to 441 with an average of 152. To assess the reproducibility of the  
 151 computed WSS field with respect to boundary conditions, we repeated the simula-  
 152 tions for all cases and controls with a 20 % higher flow rate at the inlet.

153 The cardiac cycle was discretized in 200 uniformly distributed time steps and, to  
 154 reduce the effect of initial transients, the second of two simulated cardiac cycles was  
 155 analyzed. These settings were chosen following previously performed time step and  
 156 cycle dependency tests (Geers et al, 2014).

157 A total of 50 CFD simulations were created: 10 cases and 10 controls under 'nor-  
 158 mal' inflow conditions, 10 cases and 10 controls under 'high' inflow conditions, and  
 159 10 cases under 'normal' inflow conditions with the aneurysm removed by the second  
 160 observer.

## 161 2.4 Hemodynamic variables

162 As mentioned in the Introduction (Section 1), different aspects of the WSS field are  
 163 deemed relevant to the initiation of aneurysms. Specifically, we assessed the magni-  
 164 tude, gradient, multidirectionality, and pulsatility of the WSS, according to the defi-  
 165 nitions below.

166 Given WSS vector  $\tau_w = \tau_w(x, t)$  at surface point  $x$  and time  $t$ , the time-averaged  
 167 WSS magnitude (TAWSS) is defined as

$$\text{TAWSS} = \frac{1}{T} \int_0^T |\tau_w| dt \quad (1)$$

168 where  $T$  is the period of the cardiac cycle.

169 For use in the definition of other WSS-related variables, we defined unit vectors  
 170 in the direction of and perpendicular to the time-averaged WSS vector, respectively  
 171  $\hat{p}$  and  $\hat{q}$ , as

$$\hat{p} = \frac{\int_0^T \tau_w dt}{\left| \int_0^T \tau_w dt \right|}, \quad \hat{q} = \hat{p} \times \hat{n} \quad (2)$$

172 where  $\hat{n}$  is the surface normal.

173 For the gradient of TAWSS (TAWSSG), we used the definition proposed by Meng  
 174 and colleagues (Tremmel et al, 2010; Dolan et al, 2013), which differentiates between  
 175 positive and negative gradients with respect to  $\hat{p}$ , namely,

$$\text{TAWSSG} = \nabla_S (\text{TAWSS}) \cdot \hat{p} \quad (3)$$

176 where  $\nabla_S$  is the gradient on the vessel wall surface.

177 Throughout the cardiac cycle, the WSS vector may change direction and not re-  
 178 main parallel to  $\hat{p}$ . The changing WSS direction is associated with the concept of

179 ‘disturbed’ flow. To quantify the multidirectionality of disturbed flow, we used the  
 180 transverse WSS (transWSS), which was recently proposed by Peiffer et al. in the  
 181 context of atherosclerosis (Peiffer et al, 2013a). The transWSS is defined as the time-  
 182 averaged absolute value of the  $q$ -component of the WSS vector, that is,

$$\text{transWSS} = \frac{1}{T} \int_0^T |\tau_w \cdot \hat{q}| dt \quad (4)$$

183 We quantified the temporal variation in the WSS magnitude during the cardiac  
 184 cycle by calculating the WSS pulsatility index (WSSPI) (Gosling and King, 1974),  
 185 given by

$$\text{WSSPI} = \frac{\max_{t \in [0, T]} \tau_w - \min_{t \in [0, T]} \tau_w}{\text{TAWSS}} \quad (5)$$

186 As the WSS *magnitude* may vary substantially between CFD simulations us-  
 187 ing either patient-specific or estimated boundary conditions, caution in interpretation  
 188 must be exercised (Karmonik et al, 2010; Marzo et al, 2011; Jansen et al, 2014; Mc-  
 189 Gah et al, 2014). We chose to focus on the WSS *distribution* by normalizing TAWSS  
 190 by the space-averaged TAWSS on the branch ( $\overline{\text{TAWSS}}_B$ ). For aneurysms, normalized  
 191 WSS distributions have been shown to remain relatively unchanged across a range  
 192 of physiological boundary conditions (Marzo et al, 2011). TAWSSG and transWSS  
 193 were similarly normalized by  $\overline{\text{TAWSS}}_B$ . Unless stated otherwise, we will report on  
 194 normalized values.

## 195 2.5 Geometric variables

196 Vascular geometry has a major impact on hemodynamics (Geers et al, 2011) and  
 197 indeed bifurcations harboring aneurysms tend to more strongly deviate from the op-  
 198 timality principle (Baharoglu et al, 2014). To complement the hemodynamic analysis  
 199 in our study, we characterized the vascular geometry using the framework presented  
 200 by Piccinelli et al. (Piccinelli et al, 2009), which is available as part of VMTK. We  
 201 will briefly outline the procedure. Some of the processing steps are illustrated in Fig-  
 202 ure 2. For more details, refer to (Piccinelli et al, 2009).

203 Two centerlines were created: one from the inlet to the MCA outlet and another  
 204 from the inlet to the ACA outlet. At the ICA bifurcation, the two centerlines diverged  
 205 into their respective branches and the corresponding bifurcation origin and plane were  
 206 identified. The normal to the bifurcation plane was set to point posteriorly. Center-  
 207 lines were split into branches corresponding to the ICA, MCA, and ACA.

208 For each branch, a representative cross sectional area  $A$  was defined as the mean  
 209 surface area of two cross sections. These two sections were created one and two  
 210 maximally inscribed sphere radii away from the bifurcation. The bifurcation’s area  
 211 ratio (Ingebrigtsen et al, 2004) was given by

$$\text{area ratio} = \frac{A_{ACA} + A_{MCA}}{A_{ICA}} \quad (6)$$

212 Vectors pointing in the direction of the branches were created and then projected  
213 onto the bifurcation plane. The in-plane ICA-ACA and ICA-MCA angles were cal-  
214 culated.

215 To quantify the tortuosity of the ACA, we used the definition

$$\text{tortuosity} = \frac{L}{D} - 1 \quad (7)$$

216 where  $L$  is the length along the centerline and  $D$  is the Euclidean distance between its  
217 endpoints.

## 218 2.6 Branch extraction and parametrization

219 To aid the inter-subject comparison of hemodynamic variables on the surface of the  
220 ACA, we used the approach proposed by Antiga et al. (Antiga and Steinman, 2004),  
221 which is also available as part of VMTK. Briefly, the vessel wall surface was split into  
222 branches corresponding to the previously split centerlines (Figure 2). As branches  
223 are topologically equivalent to cylinders, the ACA could be mapped onto a two-  
224 dimensional (2D) parametric space with a longitudinal coordinate,  $u$ , and a periodic  
225 circumferential coordinate,  $v$ . Coordinate  $u$  ranged from 0 to 10 mm, increasing in the  
226 direction of the flow. Coordinate  $v$  ranged from  $-\pi$  to  $\pi$  rad. The position of  $v = 0$   
227 was determined by the bifurcation normal parallel transported along the centerline  
228 and  $v > 0$  was set to correspond to the superior side of the ACA.

## 229 2.7 Data visualization

230 Contour plots were created to visualize the distribution of hemodynamic variables  
231 on the surface of the ACA. Using the 2D parametrization, the branch surface was  
232 flattened onto a rectangle such that  $u$  and  $v$  corresponded to the vertical and horizontal  
233 axes of the plots, respectively (Figure 2). This approach made it possible to view  
234 the whole branch at once and more easily compare between subjects. Because the  
235 circumferential coordinate is periodic, we slightly extended the plot to range from  $-4$   
236 to  $4$  rad, thus maintaining a visual continuity of the variable distributions. To indicate  
237 the location of the aneurysm neck, we calculated the distance from the surface with  
238 aneurysm to the surface without aneurysm and plotted a contour line at 0.1 mm. The  
239 region enclosed by the aneurysm neck will be referred to as ‘aneurysm initiation site’.

## 240 2.8 Statistical analysis

241 In this study, we assessed the reproducibility of the computed WSS field with respect  
242 to the observer virtually removing the aneurysm and to the flow rate imposed at the  
243 inlet. Differences between solutions were quantified by calculating the root-mean-  
244 square deviation (RMSD) between TAWSS fields, after linearly interpolating them  
245 onto a uniformly remeshed branch surface with a nominal node spacing of 0.05 mm.  
246 Solutions of observer 2 were projected onto the remeshed branch surface of observer



1. Since normalized TAWSS fields were considered, for which  $\overline{\text{TAWSS}}_B = 1$ , the RMSD was equal to the coefficient of variation of the RMSD (CVRMSD). CVRMSD will be expressed as a percentage.

Space-averaged values of variables were calculated for quantitative analysis. Besides analyzing the whole branch, we defined a ‘patch’ that encapsulated all aneurysm initiation sites. This patch was bound by  $u \in [0, 5]$  and  $v \in [-\pi/2, \pi/2]$ , see Figure 2. For case 10, with the aneurysm directed anteriorly, and its matching control, the patch was defined at the opposite side of the branch, bound by  $u \in [0, 5]$  and  $v \in [-\pi, -\pi/2) \cup (\pi/2, \pi]$ . Variables were averaged over the branch, patch, and non-patch (branch minus patch).

To test the significance of the differences between regions and between cases and controls, we used the Wilcoxon signed-rank test for paired samples and the Wilcoxon rank-sum test for unpaired samples. Differences were considered statistically significant for  $p < 0.05$ . The following samples were compared: I. patch vs. non-patch for the cases (paired), II. patch vs. non-patch for the controls (paired), III. patches of the cases vs. patches of the controls (unpaired), and IV. branches of the cases vs. branches of the controls (unpaired).

The Wilcoxon rank-sum test was also used to compare geometric variables between cases and controls. Again, differences were considered statistically significant for  $p < 0.05$ .

### 3 Results

#### 3.1 Geometry

As mentioned in Section 2.1, cases in this study were remarkably consistent in location, which is also confirmed by the location of the aneurysm initiation site in Figure 3. For cases 1 to 9, the circumferential coordinate of the center of the initiation site was on average  $2^\circ$  (range:  $-24$  to  $13^\circ$ ). For case 10, it was  $119^\circ$ . In other words, most aneurysms were approximately aligned with the transported bifurcation normal.

Table 1 reports on the statistical analysis of geometric variables. Bifurcation angles were very similar among cases and controls. Cross sectional areas of branches tended to be larger for cases, but only for the MCA branch these differences were statistically significant. Area ratios were not significantly different. The tortuosity of ACAs showed a non-significant trend of being larger for cases than for controls.

#### 3.2 Hemodynamics

Figure 3 shows for all cases and controls the non-normalized TAWSS on the ACA. There were large variations in space-averaged TAWSS with values ranging from 1.0 to 11.2 Pa (mean: 3.5 Pa; standard deviation: 2.2 Pa). Figure 4 shows the normalized TAWSS, highlighting the distribution rather than the magnitude. Overall, cases appeared to have a larger spatial variation in TAWSS, covering a wider range of TAWSS

285 values. Close to the apex of the bifurcation and on the superior side of the ACA (Fig-  
286 ure 2), TAWSS was relatively high for cases. However, some controls showed sim-  
287 ilar patterns, e.g. control 3 and control 5, whereas some cases, e.g. case 6, did not.  
288 Aneurysm initiation sites partly overlapped with regions of high TAWSS, yet tended  
289 to be near the edge of them. Statistical analysis revealed no significant differences  
290 between the patch and the rest of the branch (non-patch) for controls, but did show  
291 significant differences between those regions for cases (Table 2). Also, patches of  
292 cases experienced significantly higher TAWSS than those of controls. By definition,  
293 normalization removed differences in TAWSS between branches.

294 Figure 5 shows the distribution of TAWSSG. Cases' larger spatial variation in  
295 TAWSS was reflected by higher positive and negative gradients. Correspondingly,  
296 the absolute value of TAWSSG was significantly higher, both for the whole branch  
297 and for the patch (Table 2). Although magnitudes varied, distributions were found to  
298 be similar for cases and controls: patches experienced significantly higher absolute  
299 TAWSSG than the rest of the branch. However, there was no clear correlation between  
300 either positive or negative gradients and the aneurysm initiation site.

301 Figure 6 shows the distribution of transWSS. Concentrated regions of high trans-  
302 sWSS were observed. WSS vectors changed direction more strongly closer to the ICA  
303 bifurcation, which is also reflected by patches having significantly higher transWSS  
304 than non-patches (Table 2). On average, transWSS was higher for cases than controls,  
305 but only for the whole branch these differences were significant. No clear correlations  
306 were found between regions of high transWSS and the aneurysm initiation site.

307 Animations of the WSS field during the cardiac cycle showed that, although the  
308 WSS magnitude obviously changed over time, the distribution remained relatively  
309 unchanged. Please refer to (Geers et al, 2015a) to view the animations online. This  
310 means that at each point on the branch the WSS magnitude over time resembled the  
311 shape of a typical flow rate waveform, which motivated our choice for describing  
312 the temporal variation with the pulsatility index. Figure 7 shows the distribution of  
313 WSSPI. Similar patterns could be observed among cases and controls. Near the bifur-  
314 cation, regions of relatively high WSSPI were located on the posterior and anterior  
315 side of the ACA and regions of relatively low WSSPI were located on the superior  
316 and inferior side (See Figure 2C for a location guide). Further downstream, WSSPI  
317 was also relatively low. As a result, we found significant differences between patches  
318 and non-patches (Table 2). The main difference between cases and controls was that  
319 WSSPI was on average higher for cases, a significant difference for branches but not  
320 for patches. Judging from the contour plots, however, we did observe a clear corre-  
321 lation between WSSPI peaks and the aneurysm initiation site. Additional statistical  
322 analysis confirmed this observation by revealing that WSSPI was significantly higher  
323 for just the initiation site than for the whole patch (1.61 vs. 1.52,  $p = 0.007$ ), which  
324 was not true for any of the other variables. In other words, among the assessed hemo-  
325 dynamic variables, WSSPI most consistently correlated with the aneurysm initiation  
326 site.

327 No pattern was found explaining the deviating aneurysm orientation of case 10.  
328 Removing the case and its matching control from analysis did not alter the observed  
329 trends.

### 330 3.3 Reproducibility analysis

331 Figure 8 shows the differences in TAWSS distribution between the observers manu-  
332 ally removing the aneurysm and between ‘normal’ and ‘high’ flow rates at the inlet.  
333 For each comparison, we chose three representative cases or controls, corresponding  
334 to minimum, closest-to-mean and maximum CVRMSD. Good reproducibility was  
335 found between observers and, although increasing the flow rate by 20 % increased the  
336 average TAWSS magnitude by 28 %, the TAWSS distribution remained relatively un-  
337 changed. CVRMSD between observers was  $6.17 \pm 0.07$  % (mean  $\pm$  standard error),  
338 range: 3.57 to 8.05 %. CVRMSD between flow rates was  $3.96 \pm 0.04$  %, range: 2.73  
339 to 5.21 %.

## 340 4 Discussion

### 341 4.1 Main contributions and findings

342 In summary, the main contributions of this study are: 1. the dataset was drawn from a  
343 multicenter database and was composed of cases with aneurysms at a single location,  
344 which was not in a known region of high WSS, and a matching set of controls, 2.  
345 objective comparison of variable distributions was made possible by automatic ex-  
346 traction and parametrization of the branch, 3. to our knowledge, this is the first study  
347 to evaluate the transWSS and WSSPI in the context of aneurysm initiation; and 4.  
348 tests were performed to assess the reproducibility of the computed WSS field with  
349 respect to the observer virtually removing the aneurysm and the flow rate imposed at  
350 the inlet.

351 The main findings of this study are: 1. aneurysms form on branches with large  
352 spatial variations in TAWSS, as also reflected by the presence of high TAWSSG gra-  
353 dients; 2. aneurysms form on branches with large temporal variations in WSS direc-  
354 tion (i.e. transWSS); 3. aneurysms form at regions of high TAWSS; and 4. aneurysms  
355 form at focal regions with large temporal variations in WSS magnitude (i.e. WSSPI).

### 356 4.2 Aneurysm location

357 The majority of aneurysms are found at the apex of bifurcations or the outer wall of  
358 vascular bends, which has long established the importance of hemodynamic stress in  
359 the initiation of cerebral aneurysms (Kayembe et al, 1984; Stehbens, 1989; Gonzalez  
360 et al, 1992; Kondo et al, 1997; Foutarakis et al, 1999). At the bifurcation apex, blood  
361 impinges the wall and rapidly accelerates and then decelerates as it diverts into the  
362 branches. The associated WSS is low at the impingement region and high further  
363 downstream, with, along the branch, first high positive and then high negative gra-  
364 dients (Dolan et al, 2013). By complementing animal studies with CFD simulations,  
365 Meng and colleagues have gathered evidence indicating that the combination of high  
366 WSS and positive WSSG triggers the pathological remodeling leading to aneurysm  
367 formation (Meng et al, 2007; Metaxa et al, 2010; Dolan et al, 2013). Other CFD stud-  
368 ies, using pre-aneurysm images, have corroborated this finding (Kulcsar et al, 2011;

369 [Kono and Terada, 2013](#); [Kono et al, 2014](#)). With respect to the rest of the branch and  
370 the controls, we also found aneurysms to form in regions of relatively high WSS and  
371 WSSG. However, although regions of positive WSSG were found close to the bifur-  
372 cation apex, aneurysms were located further downstream in regions of mixed positive  
373 and negative WSSG.

374 Aneurysms also occur at locations with lesser-known hemodynamic conditions.  
375 Studying these locations can provide great insight into the hemodynamic mecha-  
376 nisms underlying aneurysm initiation. For instance, finding high WSS and WSSG in  
377 regions that are not commonly dominated by those WSS characteristics, which can  
378 be confirmed with controls, would provide stronger evidence in support of their role  
379 in aneurysm initiation. Recently, [Lauric et al.](#) reported on a study of 10 aneurysms  
380 located at the inner wall of the carotid siphon and 25 control ICAs ([Lauric et al,](#)  
381 [2014](#)). The location was of particular interest as little was known about the hemo-  
382 dynamic conditions, except that the WSS was expected to be low. They found that  
383 aneurysms had formed in regions of low WSS flanked by peaks of high WSS and  
384 WSSG; WSS peaks correlated with the aneurysm necks; and controls were charac-  
385 terized by low, almost constant, WSS and WSSG. Similarly, in our study, comparing  
386 ACAs harboring aneurysms to ACAs that never formed an aneurysm allowed us to  
387 differentiate between hemodynamic stress patterns common to ACAs and those spe-  
388 cific to aneurysm formation.

#### 389 4.3 Temporal variation in WSS direction

390 Apart from their magnitudes, research has also focused on the oscillatory nature of  
391 the WSS and WSSG vectors. The most commonly used variable in this regard is the  
392 oscillatory shear index (OSI), which was introduced in the context of atherosclerosis  
393 ([Ku et al, 1985](#)) but later also used to study aneurysm initiation ([Shimogonya et al,](#)  
394 [2009](#); [Singh et al, 2010](#); [Kono et al, 2014](#)) and rupture ([Xiang et al, 2011](#); [Miura et al,](#)  
395 [2013](#)). Two other variables were introduced specifically to study aneurysm initiation:  
396 the (potential) aneurysm formation indicator (AFI) ([Mantha et al, 2006](#)) and the gra-  
397 dient oscillatory number (GON) ([Shimogonya et al, 2009](#)). Variable definitions and  
398 results for these variables are presented in the appendix (Section 6)

399 [Peiffer et al.](#) recently proposed the transWSS and showed that it captures different  
400 flow features than OSI ([Peiffer et al, 2013a](#)). Preliminary results indicated strong  
401 correlations with atherosclerotic lesion. Other than OSI and AFI, which give more  
402 weight to flow reversal, transWSS focuses solely on the multidirectional (vs. uniaxial)  
403 nature of disturbed flow. Given these unique properties, we considered it a relevant  
404 new variable to assess in the context of aneurysm initiation.

405 For both cases and controls, regions of high transWSS were concentrated, sug-  
406 gesting that flow disturbances remained in the same location throughout the cardiac  
407 cycle. As expected, flow was more disturbed closer to the ICA bifurcation, leading to  
408 higher transWSS values in that region. Averaged over the whole, cases were found to  
409 have significantly higher transWSS values, but there were no clear correlations with  
410 the aneurysm initiation site.

#### 411 4.4 Temporal variation in WSS magnitude

412 Among the assessed hemodynamic variables, WSSPI most consistently coincided  
413 with the aneurysm initiation site. The variable was introduced as a simple metric  
414 to quantify the temporal variation of the WSS magnitude without using noise-prone  
415 temporal gradients (Lee et al, 2009). Besides the spatial variation in the WSS mag-  
416 nitude, related to the WSSG, and the temporal variation in the WSS direction, our  
417 results suggest that the temporal variation in the WSS magnitude is also an important  
418 factor to consider when investigating the role of hemodynamic stress in aneurysm ini-  
419 tiation. This is in line with the observation that endothelial cells respond differently  
420 to temporal vs. spatial variations in WSS (White et al, 2001, 2005) and to different  
421 types of pulsatile flow (Helmlinger et al, 1991; Himburg et al, 2007; Feaver et al,  
422 2013).

#### 423 4.5 Limitations and future directions

424 Aneurysms were virtually removed to approximate the pre-aneurysm vascular geom-  
425 etry. This approach has two main limitations. First, manual removal of aneurysms  
426 is observer-dependent. We addressed this by repeating the analysis with a second  
427 observer and found good agreement (Figure 8). Other studies employed automatic  
428 removal methods (Ford et al, 2009; Shimogonya et al, 2009; Chen et al, 2013), but  
429 these preserve less of the vascular geometry and still rely on manually set parameters.  
430 Second, aneurysm removal does not account for possible changes in parent vessel  
431 geometry due to interaction with the perianeurysmal environment during aneurysm  
432 growth (Sforza et al, 2012). Since ICA bifurcations are not near bone structures, sub-  
433 stantial changes were unlikely to have occurred. However, prospective studies are  
434 needed for confirmation.

435 Discrepancies between estimated and patient-specific flow rate waveforms at the  
436 inlet have been shown to strongly affect the WSS magnitude (Karmonik et al, 2010;  
437 Marzo et al, 2011; Jansen et al, 2014; McGah et al, 2014), but not the WSS distri-  
438 bution (Marzo et al, 2011). Therefore, we focused on the distribution by normalizing  
439 appropriate variables by the average WSS on the branch. We also repeated the anal-  
440 ysis with a 20 % higher inflow rate to confirm that the WSS distribution remained  
441 relatively unchanged. The influence of the waveform shape on the WSSPI should be  
442 investigated. Regarding the outlets, despite the simplification of zero-pressure bound-  
443 ary conditions, the resulting ACA:MCA flow split of 34:66 closely matched the in  
444 vivo measurements (36:64) reported in (Zhao et al, 2007). Although much can be  
445 learned from WSS distributions, we wish to stress that CFD studies scrutinizing the  
446 role of hemodynamics in aneurysm initiation and rupture would greatly benefit from  
447 patient-specific boundary conditions. Ideally, a range of possible boundary condi-  
448 tions, covering all the patient's levels of exercise, should be considered to obtain a  
449 complete picture of the shear stresses exerted on the arterial wall.

450 Pathogenesis of cerebral aneurysms involves the interplay between mechanical  
451 stimuli, vascular biology, and vascular geometry (Meng et al, 2014). Therefore, aneurysm  
452 initiation is likely caused by a combination of biochemical and biomechanical fac-

453 tors ([Sadasivan et al, 2013](#)). Although hemodynamic stresses appear to be important,  
454 their effect on the vascular biology, i.e. the mechanobiology, should also be modeled  
455 to gain a deeper understanding of the underlying mechanisms ([Humphrey and Taylor,](#)  
456 [2008](#); [Watton et al, 2009, 2010](#)). Moreover, among hemodynamic stresses, not only  
457 the WSS but also pressure-induced tensile stresses are known regulators of vascular  
458 biology and should be analyzed ([Meng et al, 2014](#)).

## 459 5 Conclusions

460 The aim of this study was to analyze the WSS field at the aneurysm initiation site.  
461 Ten cases with aneurysms at a single location were analyzed and compared with  
462 ten controls. We found that the general region in which aneurysms had formed was  
463 characterized by high TAWSS and high TAWSSG. The aneurysm initiation site partly  
464 overlapped with regions of high TAWSS and, among all assessed variables, most  
465 consistently coincided with peaks of WSSPI.

## 466 6 Open data

467 To promote the future use of the dataset, surface meshes of all cases (with and without  
468 aneurysm) and controls have been made available online at ([Geers et al, 2015b](#)).

## 469 Conflict of interest

470 None.

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## 485 Appendix: Additional hemodynamic variables

486 This appendix presents variable definitions and results for three additional hemody-  
487 namic variables describing the oscillatory nature of the WSS and WSSG vectors.

488 The oscillatory shear index (OSI) was introduced by Ku et al. (Ku et al, 1985) and  
489 later redefined by He and Ku (He and Ku, 1996). It describes the oscillatory nature  
490 of the WSS vector,  $\tau_w$ , during the cardiac cycle and has been used extensively in the  
491 context of atherosclerosis (Peiffer et al, 2013b) and aneurysm initiation (Singh et al,  
492 2010; Shimogonya et al, 2009; Kono et al, 2014). It is given by

$$\text{OSI} = \frac{1}{2} \left( 1 - \frac{\left| \int_0^T \tau_w dt \right|}{\int_0^T |\tau_w| dt} \right), \quad \text{OSI} \in [0, \frac{1}{2}] \quad (8)$$

493 where  $t$  is time and  $T$  is the cardiac period.

494 The (potential) aneurysm formation indicator (AFI) was proposed by Mantha et  
495 al. (Mantha et al, 2006) to identify flow stagnation zones, which in their study of  
496 three sidewall aneurysms coincided with the aneurysm initiation site. It measures the  
497 cosine of angle  $\theta$  between the instantaneous WSS vector and the time-averaged WSS  
498 vector, that is,

$$\text{AFI} = \cos \theta = \frac{\tau_w}{|\tau_w|} \cdot \hat{p}, \quad \text{AFI} \in [-1, 1] \quad (9)$$

499 AFI was obtained at time point H1 of Ford et al.'s flow rate waveform (Ford et al,  
500 2005), corresponding to midsystolic deceleration during which flow is least stable  
501 (Fung, 1997, p. 137).

502 The gradient oscillatory number (GON) was proposed by Shimogonya et al. (Shi-  
503 mogonya et al, 2009) to quantify the degree of oscillating tension/compression forces  
504 at the aneurysm initiation site. It is given by

$$\text{GON} = 1 - \frac{\left| \int_0^T G dt \right|}{\int_0^T |G| dt}, \quad \text{GON} \in [0, 1] \quad (10)$$

505 where

$$G = \begin{pmatrix} \nabla_S (\tau_w \cdot \hat{p}) \cdot \hat{p} \\ \nabla_S (\tau_w \cdot \hat{q}) \cdot \hat{q} \end{pmatrix} \quad (11)$$

506 Contour plots of the three variables are in Figures 9 (OSI), 10 (AFI), and 11  
507 (GON).

508 We found strong correlations between variables, implying that they capture the  
509 same flow features: AFI correlated with OSI, GON correlated with absolute TAWSSG.  
510 This is in accordance with previous studies (Lee et al, 2009; Peiffer et al, 2013a). The  
511 distribution of GON was very noisy, which can largely be attributed to it being the  
512 temporal variation in the second-order derivative of the velocity (Chen et al, 2013).  
513 No clear correlations were found between the variable distributions and the aneurysm  
514 initiation site.

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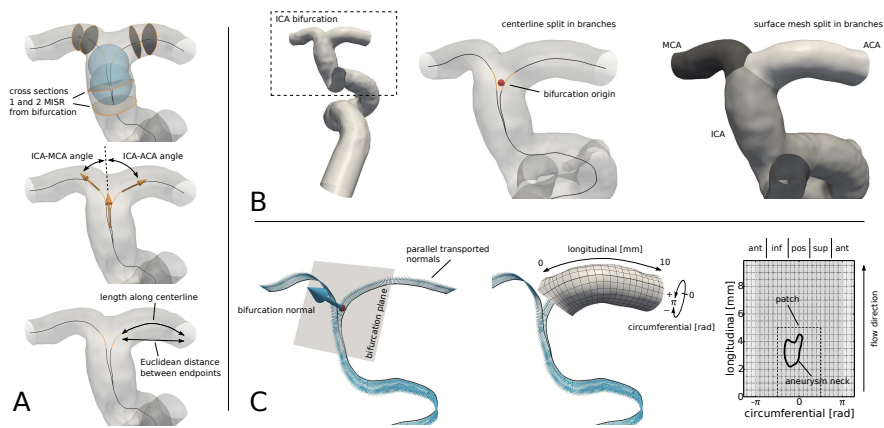
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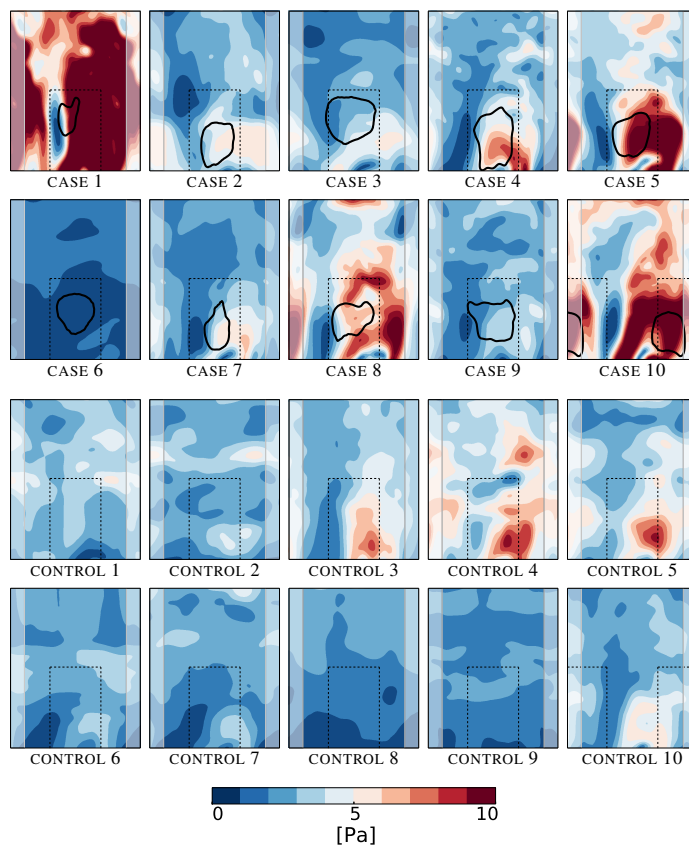
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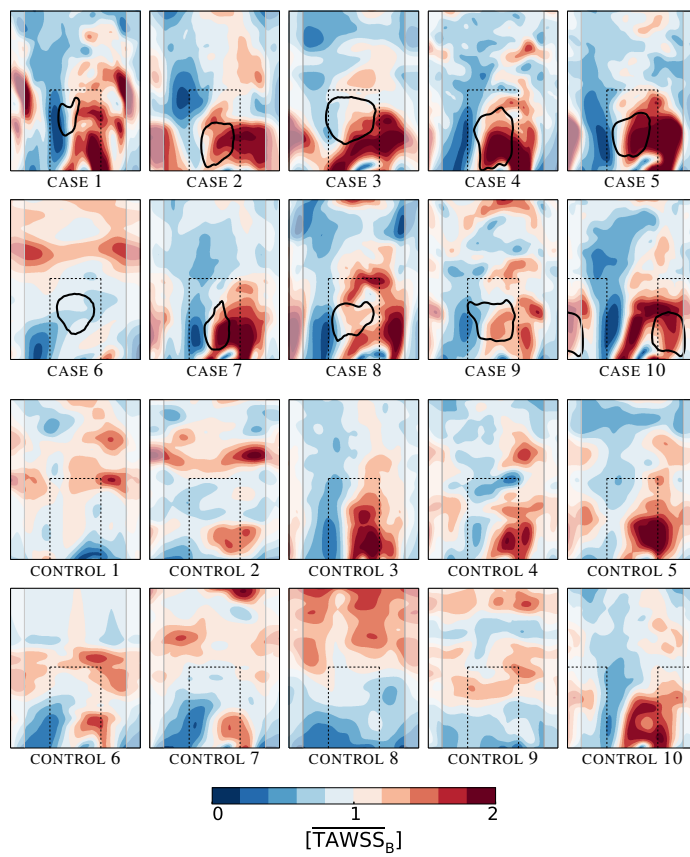
**Fig. 1** Vascular models of cases with aneurysm (top), cases with the aneurysm virtually removed (middle), and controls (bottom). The ACA is colored red. View points were selected to best visualize the vascular model, so images are not necessarily at the same scale.



**Fig. 2** Post-processing steps. A. Bifurcation sections were created one and two maximally inscribed sphere radii (MISR) away from the bifurcation to obtain representative cross sectional areas for the ICA, ACA and MCA. Bifurcation vectors projected onto the bifurcation plane (panel C) were used to calculate the bifurcation angles. The tortuosity was defined by Eq. (7) using the branch length along the centerline and the Euclidean distance between its endpoints. B. Centerlines from inlet to ACA outlet and inlet to MCA outlet diverged at the ICA bifurcation and were split into branches. Correspondingly, the vessel wall surface was also split into branches. C. The posteriorly directed normal to the bifurcation plane was parallel transported along the centerline. The ACA was mapped onto a 2D parametric space with a longitudinal and a circumferential coordinate. To view the distribution of hemodynamic variables on the whole branch at once, it was flattened onto a rectangle. Plots of the flattened branch indicate the location of the aneurysm neck and the patch. They also indicate the location of the posterior (pos), anterior (ant), superior (sup) and inferior (inf) sides of the branch. The plot range of the circumferential coordinate was slightly extended to show the continuity of the variable distribution. Duplicated regions were grayed out.

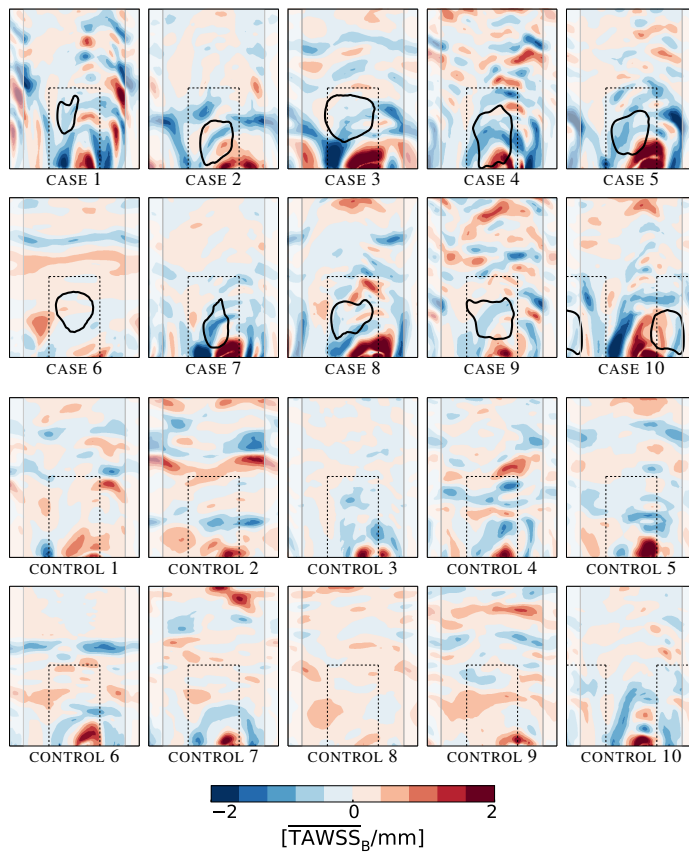


**Fig. 3** Time-averaged WSS (TAWSS) under 'normal' inflow conditions. The same colormap range was used for all cases and controls. Plot properties are explained in Figure 2C.

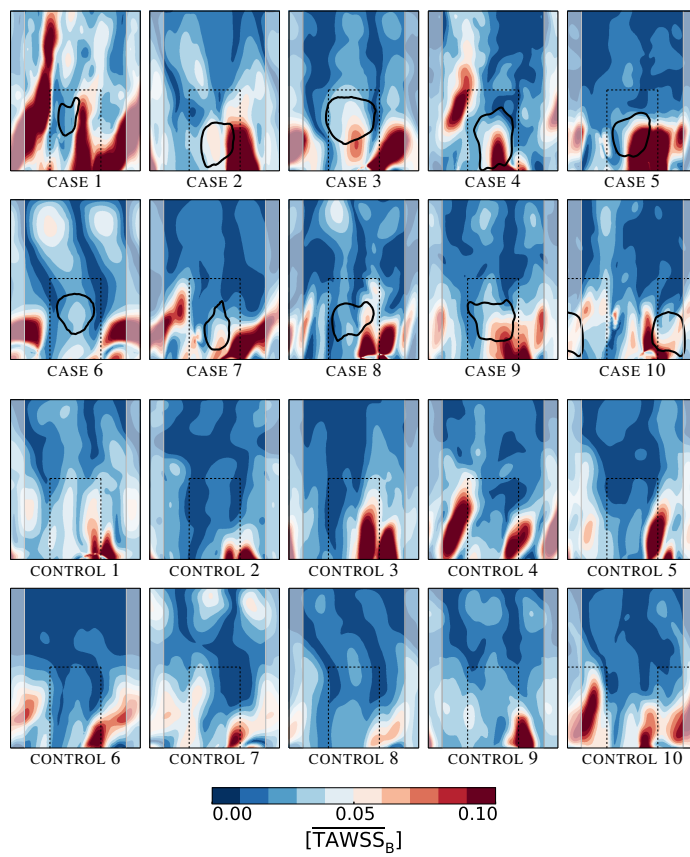


**Fig. 4** Time-averaged WSS (TAWSS) under 'normal' inflow conditions. Colormaps were normalized by using  $\overline{\text{TAWSS}}_B$  as unit. Plot properties are explained in Figure 2C.

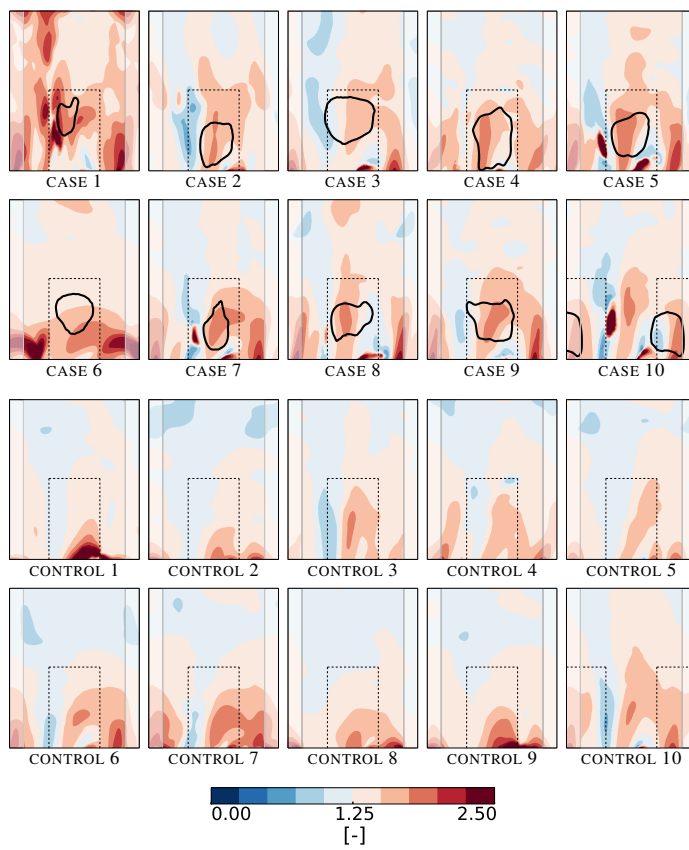




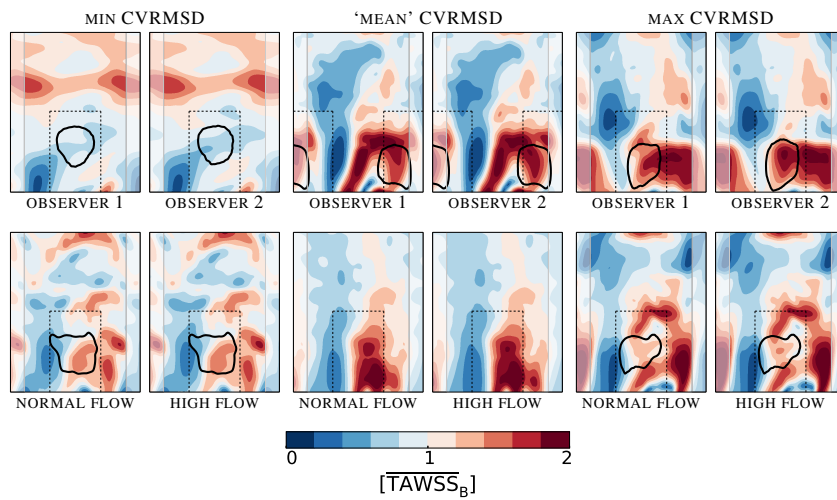
**Fig. 5** Gradient of the time-averaged WSS (TAWSSG) under 'normal' inflow conditions. Colormaps were normalized by using  $\overline{\text{TAWSS}}_B/\text{mm}$  as unit. Plot properties are explained in Figure 2C.



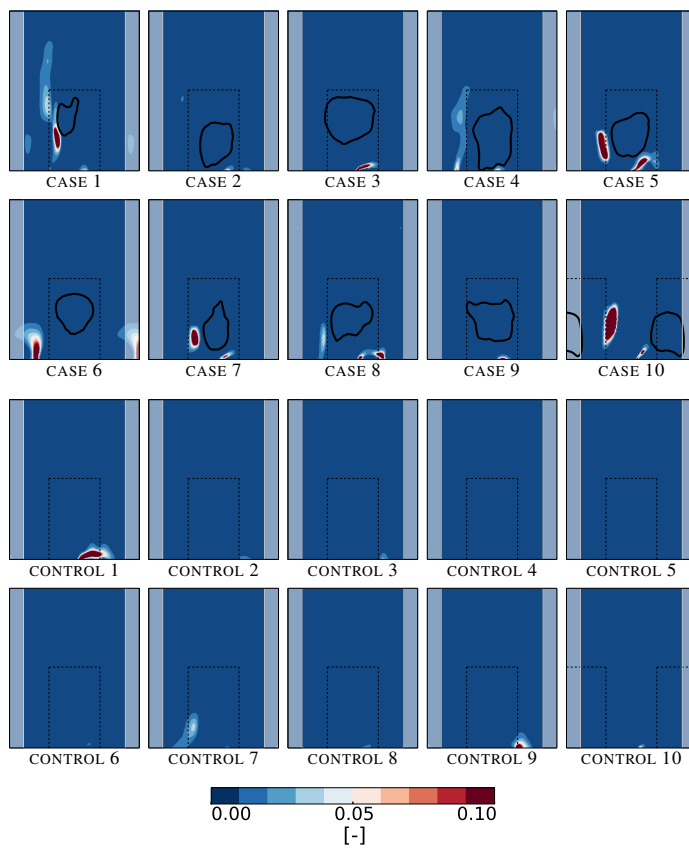
**Fig. 6** Transverse WSS (transWSS) under 'normal' inflow conditions. Colormaps were normalized by using  $\overline{\text{TAWSS}}_B$  as unit. Plot properties are explained in Figure 2C.



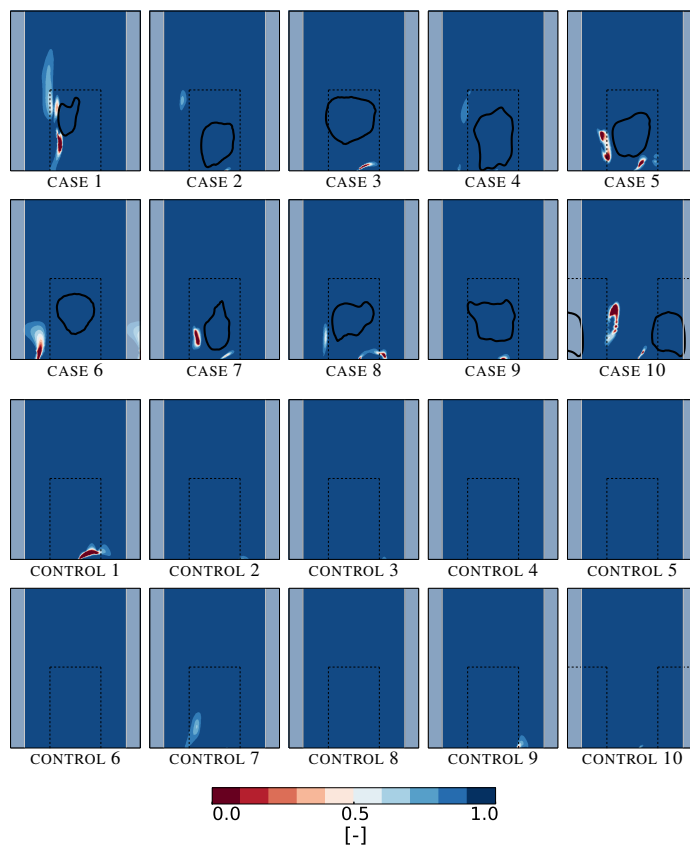
**Fig. 7** WSS pulsatility index under 'normal' inflow conditions. The same colormap range was used for all cases and controls. Plot properties are explained in Figure 2C.



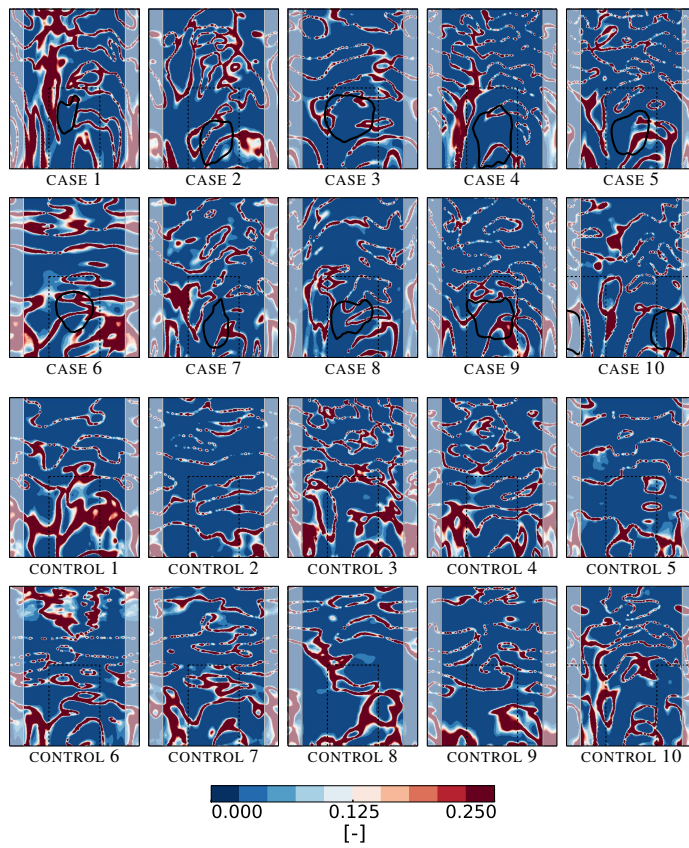
**Fig. 8** Comparison of TAWSS distributions between observers removing the aneurysm and between 'normal' and 'high' flow rates at the inlet. Displayed are three cases or controls representing minimum, closest-to-mean and maximum CVRMSD. Colormaps were normalized by using  $\overline{TAWSS}_B$  as unit. Plot properties are explained in Figure 2C.



**Fig. 9** Oscillatory shear index (OSI). Plot properties are explained in Figure 2C.



**Fig. 10** Aneurysm formation indicator (AFI). Plot properties are explained in Figure 2C.



**Fig. 11** Gradient oscillatory number (GON). Plot properties are explained in Figure 2C.

**Table 1** Statistical analysis of geometric variables.

Variable	Unit	Mean and standard error		<i>p</i> -value <sup>a</sup>
		Cases	Controls	
ICA-ACA angle	[°]	77.8 ± 2.7	77.8 ± 3.1	.880
ICA-MCA angle	[°]	40.3 ± 2.5	39.4 ± 3.0	.940
ICA cross sectional area	[mm <sup>2</sup> ]	10.7 ± 0.8	9.5 ± 1.0	.364
ACA cross sectional area	[mm <sup>2</sup> ]	5.2 ± 0.6	3.8 ± 0.3	.059
MCA cross sectional area	[mm <sup>2</sup> ]	6.0 ± 0.3	5.1 ± 0.3	<b>.049</b>
ICA bifurcation area ratio	[-]	1.05 ± 0.05	0.98 ± 0.05	.545
ACA tortuosity	[-]	0.12 ± 0.03	0.06 ± 0.01	.059

<sup>a</sup> *p*-values were calculated with the Wilcoxon rank-sum test; values highlighted in bold face correspond to statistically significant differences with *p* < 0.05.



**Table 2** Statistical analysis of hemodynamic variables.

Variable	Unit	Mean and standard error of space-averaged variable values						<i>p</i> -value <sup>b</sup>			
		Cases			Controls			I	II	III	IV
		Patch	Non-patch	Branch	Patch	Non-patch	Branch				
TAWSS	[TAWSS <sub>B</sub> ]	1.18±0.05	0.94±0.02	1.00±0.00	1.01±0.05	1.00±0.02	1.00±0.00	<b>.022</b>	.959	<b>.034</b>	1.00
TAWSSG <sup>a</sup>	[TAWSS <sub>B</sub> /mm]	0.53±0.05	0.34±0.02	0.39±0.02	0.35±0.03	0.26±0.02	0.28±0.02	<b>.017</b>	<b>.013</b>	<b>.010</b>	<b>.003</b>
transWSS	[10 <sup>-3</sup> TAWSS <sub>B</sub> ]	42.7±3.9	26.1±3.0	30.4±2.7	31.4±3.2	21.4±1.1	23.7±1.3	<b>.007</b>	<b>.005</b>	.059	<b>.028</b>
WSSPI	[-]	1.52±0.03	1.38±0.03	1.41±0.03	1.45±0.02	1.27±0.02	1.32±0.02	<b>.005</b>	<b>.005</b>	.082	<b>.003</b>

<sup>a</sup> TAWSSG differentiates between positive and negative gradients, so we space-averaged the absolute TAWSSG.

<sup>b</sup> *p*-values were calculated with the Wilcoxon rank-sum test; the following samples were compared: I. patch vs. non-patch for the cases (paired), II. patch vs. non-patch for the controls (paired), III. patches of the cases vs. patches of the controls (unpaired), and IV. branches of the cases vs. branches of the controls (unpaired); values highlighted in bold face correspond to statistically significant differences with  $p < 0.05$ .