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# 1 Geological discontinuity persistence: Implications and quantification

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## 9 **Abstract**

10 Persistence of geological discontinuities is of great importance for many rock-related  
11 applications in earth sciences, both in terms of mechanical and hydraulic properties  
12 of individual discontinuities and fractured rock masses. Although the importance of  
13 persistence has been identified by academics and practitioners over the past  
14 decades, quantification of areal persistence remains extremely difficult; in practice,  
15 trace length from finite outcrop is still often used as an approximation for persistence.  
16 This paper reviews the mechanical behaviour of individual discontinuities that are not  
17 fully persistent, and the implications of persistence on the strength and stability of  
18 rock masses. Current techniques to quantify discontinuity persistence are then  
19 examined. This review will facilitate application of the most applicable methods to  
20 measure or predict persistence in rock engineering projects, and recommended  
21 approaches for the quantification of discontinuity persistence. Furthermore, it  
22 demonstrates that further research should focus on the development of persistence

23 quantification standards to promote our understanding of rock mass behaviours  
24 including strength, stability and permeability.

25 **Keywords:** Discontinuity persistence; incipient discontinuity; rock bridges;  
26 geophysics; rock mass strength

## 27 **1. Introduction**

28 Geological discontinuities are of great importance for strength, deformability and  
29 permeability of rock masses. Characterisation of discontinuity geometry (i.e.  
30 aperture, persistence, length and spatial connectivity) is the first step to  
31 understanding the overall behaviour of rock masses. Early references to  
32 discontinuity persistence include those of Jennings (1970) and Einstein et al. (1983),  
33 and the summary publication by the International Society for Rock Mechanics and  
34 Rock Engineering (ISRM, 1978).

35 It is difficult to quantify true persistence due to the intrinsic three-dimensional nature  
36 of discontinuities within rock masses and the number of studies that have attempted  
37 to quantify this parameter has been relatively small. Some techniques have been  
38 developed in recent years, for example, geophysical detection (e.g. Heike et al.,  
39 2008; Deparis et al., 2011), surface terrestrial laser scanning (e.g. Sturzenegger and  
40 Stead, 2009a; Tuckey and Stead, 2016) and the forensic excavation of rock masses  
41 (e.g. Shang et al., 2017a). Modelling the inevitable uncertainty in the fracture  
42 network is addressed in FracMan by Diershowitz and colleagues at Golder  
43 Associates and by Monte-Carlo simulation (e.g. Wang et al., 2016)

44 The purpose of this paper is to consider the implications of discontinuity persistence  
45 on the mechanical properties of individual discontinuities, strength and stability of

46 rock masses and to review the available techniques to quantify this parameter.  
47 Several recommendations for future research are included in this paper.

## 48 **2. Definition**

### 49 **2.1 Incipient and mechanical geological discontinuities**

50 Geological discontinuity is normally recognised as a general term to describe any  
51 mechanical break (lacking significant tensile strength) within rock masses, including  
52 most joints, weak bedding planes, weakness zones and faults (ISRM, 1978). This  
53 definition however does not apply to incipient traces, regardless of strength, although  
54 such traces are often recorded during discontinuity logging in the outcrop (Hencher,  
55 2014 and 2015). This common practice leads to underestimation of strength of rock  
56 masses, and overestimation of permeability. It can considerably increase  
57 expenditure on rock support systems and also influence reliable prediction of water,  
58 oil and gas extraction. As a first step, it is therefore practically and theoretically  
59 important to differentiate the degree of incipency of discontinuities in terms of their  
60 tensile strength (Hencher, 2014; Shang et al., 2016).

61 Incipient discontinuities may have considerable tensile strength as a result of their  
62 partial development, secondary mineralization or cementation. This concept is  
63 illustrated by Fig. 1, in which a sub-vertical incipient rock joint terminates in rock.  
64 Characterising the horizontal traces, would generally be disregarded in rock mass  
65 characterisation, but these clearly represent a weakness.

66 Incipient rock discontinuities often develop over geological time into full mechanical  
67 discontinuities (Hencher, 2014) with zero tensile strength as defined by ISRM (1978).

68 Fig. 2 shows rock cores with strong incipient traces and zero-tensile strength  
69 mechanical joints; these discontinuities can be differentiated on the basis of relative

70 tensile strength of the parent rock (Hencher, 2014; Shang et al., 2015, 2016). Fig. 3  
71 shows different development stages of incipient joints on a face cut by a diamond  
72 wire saw. Joints can be seen as linear traces stained with iron oxides. These joints  
73 were evidently formed from brittle fracture propagation at a late stage during  
74 cooling/emplacement of this granite, as can be interpreted from cross-cutting  
75 relationships and the geometrical association of some joints with mineral  
76 differentiation (as indicated by 1, in an area washed clean with water). Note that  
77 some of the joint traces terminate as visible features, as indicated at 2. Note that one  
78 of the shallowly dipping joints, has an open aperture locally (indicated by 3) allowing  
79 seepage of groundwater, indicating partial development to a full mechanical  
80 discontinuity. Hence, it is proposed that the incipient joint pattern represents a  
81 'blueprint' that, given time and appropriate conditions, will develop as interconnecting  
82 true, mechanical discontinuities in the sense defined by ISRM (1978).

## 83 **2.2 Rock bridge and discontinuity persistence**

84 The term 'rock bridge' is defined as an area of intact/strong rock material separating  
85 coplanar or non-coplanar discontinuities in rock masses (Kim et al., 2007b; Zheng et  
86 al., 2015). Rock bridges usually occupy a part of the planar joint plane (Dershowitz  
87 and Einstein 1988); such rock bridges in coplanar joints are the focus of this review.

88 True discontinuity persistence is the areal extent of a rock discontinuity. Fig. 4a  
89 illustrates the areal discontinuity persistence ( $K$ ), which is defined as the fraction of  
90 continuous discontinuity area (Einstein et al., 1983) whereby:

$$91 \quad K = \sum[(A_D - A_{Bi}) / A_D] \quad (1)$$

92 where  $\sum A_{Bi}$  is the total area of scattered rock bridges and  $A_D$  is reference gross  
93 area including rock bridges and continuous joint segments.

94 The above definition implies that a planar discontinuity follows a predefined  
95 weakness plane. For this type of geometry, the effects of the incipient parts of the  
96 discontinuity represented by rock bridges have been investigated in stability analysis.  
97 For example in a recent work reported by Viviana et al. (2015), effects of the spatially  
98 distributed rock bridges along a preferential sliding plane was investigated. In reality,  
99 however, linear persistence ( $K_L$ ), see Fig. 4b, is often used as an approximation of  
100 areal persistence (Einstein et al., 1983); this is defined as a linear ratio of sum of  
101 joint segments ( $\sum J_i$ ) and the total length of coplanar given line  $\sum(J_i + B_i)$ :

$$102 \quad K_L = \sum [J_i / (J_i + B_i)] \quad (2)$$

103 This definition has been widely used in experimental, analytical and numerical  
104 studies (e.g. Lajtai, 1969a,b; Jennings, 1970; Zhang et al., 2006; Prudencio and Van  
105 Sint Jan, 2007; Ghazvinian et al., 2012; Bahaaddini et al., 2013; Shang et al., 2013;  
106 Jiang et al., 2015).

107 ISRM (1978) suggested a classification scheme for persistence by measuring length  
108 ( $L$ ) of joint trace formed by the intersection of a joint within an exposure. In that  
109 scheme, five categories comprising very low persistence ( $L < 1$  m), low persistence  
110 ( $1 \text{ m} < L < 3$  m), medium persistence ( $3 \text{ m} < L < 10$  m), high persistence ( $10 \text{ m} < L <$   
111  $20$  m) and very high persistence ( $20 \text{ m} < L$ ) were provided. That scheme however  
112 only provides a description of discontinuities on a finite rock exposure (Norbury,  
113 2010) and ignores the problem of joint sections that maintain strength.

114 The above definitions (based on coplanar discontinuities) mainly focus on the  
115 geometrical properties of single discontinuities without consideration of stress  
116 concentration around fracture tips (Kevin, 1980; Wasantha et al., 2014). Some  
117 studies considered the stress influence on degree of discontinuity persistence:

118 Wasantha et al. (2014) is an example in which a new parameter was developed to  
119 define persistence, considering stress distributions, however it is still difficult for the  
120 practical application in rock engineering. It is noted that there is also a difference (in  
121 definitions of persistence) between industries and universities (for example, nearly  
122 four decades ago, the term “joint continuity”, rather than “persistence”, was used in  
123 the joint survey in the Feitsui Reservoir Project, Taiwan, which is probably due to its  
124 simplicity). In this review, the term “areal persistence” (Eq. 1), reflecting the three  
125 dimensional nature of discontinuities, is recommended to be used to describe  
126 discontinuity which is the best measure of persistence.

### 127 **3. Mechanical properties of individual discontinuities**

128 Tensile or shear failure of incipient discontinuities is often the ‘final straw’ leading to  
129 instability of rock masses, which usually occurs in response to a number of triggers  
130 including temperature and insolation (Brian and Greg, 2016), precipitation  
131 (Wieczorek and Jager, 1996), weathering (Borrelli et al., 2007; Tating et al., 2013;  
132 Goudie, 2016) and seismic loading (Cravero and Labichino, 2004). In exposures and  
133 tunnel roofs, many overhanging and threatening rock blocks or slabs (Fig. 5) only  
134 remain in place because of the strength of incipient discontinuities mainly arising  
135 from rock bridges (Paolo et al., 2016). The area of rock bridge can only be viewed  
136 after collapse (see for example in Fig. 6) when strength of revealed bridges can be  
137 back analysed (Paronuzzi and Serafini, 2009).

138 Shang et al. (2016 and 2017c) investigated the tensile strength of incipient rock  
139 discontinuities in the laboratory. They demonstrated that incipient traces can have  
140 considerable tensile strength, and can be differentiated using relative tensile strength  
141 to that of parent rock, as originally proposed by Hencher (2014). Based on the

142 laboratory findings by Shang et al. (2015 and 2016), a further numerical investigation  
143 of the direct tensile behaviour of laminated and transversely isotropic rocks was  
144 recently presented by Shang et al. 2017b, in which the incipency of bedding planes  
145 (relative tensile strength to that of parent rock) was considered.

146 Many investigations have been undertaken to measure the shear strength of  
147 discontinuities, mostly focusing on mechanical discontinuities with zero true cohesion  
148 (Barton, 1976). For non-filled and non-persistent rock joints, shear strength is  
149 however controlled by four components including fundamental shear strength of rock  
150 bridges (Shang and Zhao, 2017), internal friction in solid bridges (after rock bridges  
151 are mobilized), friction from the persistent joint segments (Lajtai, 1969b) as well as  
152 geometry and location of bridges (Ghazvinian et al., 2007). An equivalent shear  
153 strength calculation method was developed based on the Mohr-Coulomb failure  
154 criterion, in which strength contributions from rock bridges and persistent joint areas  
155 are linearly combined (Lajtai, 1969a; Hudson and Harrison, 2000) as expressed by  
156 the following equation:

$$157 \quad \tau = c_i + \sigma \cdot \tan\varphi_i = [K_L \cdot c_p + (1 - K_L) \cdot c_B] + \sigma[K_L \cdot \tan\varphi_p + (1 - K_L)\tan\varphi_B] \quad (3)$$

158 where  $\tau$  and  $\sigma$  are shear strength of incipient rock joints and normal stress;  $c_i$  and  
159  $\varphi_i$  are the equivalent cohesion and internal friction angle of incipient rock joints;  $c_p$   
160 and  $\varphi_p$  are the cohesion and internal friction angle of persistent joint;  $c_B$  and  $\varphi_B$  are  
161 the cohesion and internal friction angle of intact rock bridges;  $K_L$  is the linear  
162 persistence in the direction of shearing.

163 This equation tends to overestimate the shear strength as it assumes that rock  
164 bridges and friction of persistent joint areas are mobilized simultaneously, that is at  
165 the same deformation (Lajtai 1969a). In addition, the Mohr-Coulomb criterion is only



166 applicable to smooth joint surfaces; it only describes rough joints under relatively low  
167 normal stress level; Eq. (3) thus has limited usefulness in practice.

168 Rock bridges significantly increase the shear strength of individual incipient rock  
169 discontinuities (Shang and Zhao. 2017), especially under constant normal stiffness  
170 boundary conditions (Shang et al., 2018). They effectively produce a strength  
171 reserve and that is mobilised prior to failure occurring along the incipient joint plane  
172 (Jennings, 1970; Stimpson, 1978; Gehle and Kutter, 2003; Paolo et al., 2016).  
173 Hencher (1984) by undertaking a direct shear test on an incipient tuff joint at the core  
174 scale (54 mm in diameter) with an areal persistence of around 86% found that the  
175 rock bridge on the incipient joint plane produced a cohesion of 750 kPa. At a larger  
176 scale, a rock bridge having a size of about 150 mm X 300 mm was identified by  
177 Paolo et al. (2016) after collapse of a limestone wedge (tetrahedral block with a  
178 volume of around 28 m<sup>3</sup>) at the Rosandra valley, north-eastern Italy. Cohesion of the  
179 bridge was back-calculated to be around 2.4 MPa (cohesion of the intact rock is 25  
180 MPa). It is however rare to see laboratory shear testing on natural incipient rock  
181 discontinuity as it is not straightforward to secure and prepare groups of natural rock  
182 samples containing incipient discontinuities.

183 Numerical analysis has been used as an alternative to examine the shear strength of  
184 non-persistent rock joints, for example, using Itasca Particle Flow Code (e.g.  
185 Cundall, 1999; Park and Song, 2009; Ghazvinian et al., 2012; Shang et al., 2018)  
186 and Rock Failure Process Analysis code (e.g. Zhang et al., 2006). In numerical  
187 analysis, non-persistent rock joints containing rock bridges with different geometrical  
188 parameters are readily analysed (Shang and Zhao, 2017); the brittle failure of rock  
189 bridges often lead to a dramatic drop in shear strength (Fig. 7). Shear strength of  
190 incipient rock joints generally increases when persistence value decreases, and it

191 also varies with spatial scale of rock bridges, as illustrated by Fig. 8 in which  
192 numerically simulated shear strength of three incipient rock joints with the same  
193 areal persistence ( $K=0.5$ ) varied. Such scale dependent of strength arises from  
194 variations in the stress distribution (Rao et al., 2006) and therefore mode of fracture  
195 initiation and propagation.

#### 196 **4. Implications for the strength and stability of rock masses**

##### 197 **4.1 Block size and volume for rock masses with non-persistent joint**

198 The intersections of discontinuities in rock masses leads to discrete blocks with  
199 variable geometries (Mauldon, 1994; Kalenchuk et al., 2006), especially when  
200 discontinuities are not fully persistent. Publications accounting for discontinuity  
201 persistence and its influence on the rock block size and volume are discussed below.

202 Assessing rock block size and volume can be roughly categorized into three groups  
203 such as index evaluation (e.g. ISRM, 1978; Sen and Eissa, 1992), image-based  
204 measurement (e.g. Panek, 1981; Maerz, 1996), and model dissection (e.g.  
205 Goodman and Shi, 1985).

206 For rock masses containing several sets of persistent rock joints, rock block volume  
207 ( $V$ ) within a representative rock mass can be empirically calculated by:

$$208 \quad V = \frac{S_1 \cdot S_2 \cdot S_3 \cdots S_i}{\sin\alpha_1 \cdot \sin\alpha_2 \cdot \sin\alpha_3 \cdots \sin\alpha_i} \quad (4)$$

209 where  $S_i$  and  $\alpha_i$  are joint spacing and angle of inclination for each joint set,  
210 respectively (Cai et al., 2004; Palmström, 2005).

211 Block volume calculated by Eq. (4) is an estimation of real rock block volume on the  
212 assumption that discontinuities are fully persistent. This approximation tends to be

213 more problematic when the scale of rock mass increases (Lu and Latham, 1999).  
 214 Rock bridges in fractured rock masses lead to irregular rock block shapes and larger  
 215 rock block size (Longoni et al., 2012). An equivalent spacing  $S_i'$  for incipient rock  
 216 joints can be defined as (Cai and Horri, 1992):

$$217 \quad S_i' = \frac{S_i}{\sqrt[3]{K_i}} \quad (5)$$

218 where  $K_i$  is joint persistence for each joint set  $i$ .

219 Thus the equivalent rock block volume can be expressed by the following equation:

$$220 \quad V = \frac{S_1 \cdot S_2 \cdot S_3 \cdots S_i}{\sqrt[3]{K_1 \cdot K_2 \cdot K_3 \cdots K_i} \cdot \sin\alpha_1 \cdot \sin\alpha_2 \cdot \sin\alpha_3 \cdots \sin\alpha_i} \quad (6)$$

221 It has been accepted that block size and volume are sensitive to discontinuity  
 222 persistence (Rogers et al., 2007; Elmouttie and Poropat, 2012) and block volume  
 223 increases when persistence decreases (Kalenchuk et al., 2006). Numerical  
 224 modelling allows the sensitivity of block volume to persistence to be investigated  
 225 quantitatively (Kim, 2007b; Palleske et al., 2014). Fig. 9 shows an reciprocal  
 226 relationship between discontinuity persistence and rock block size (including 294  
 227 cases analysed by UDEC), and volume (including 144 cases analysed by 3DEC)  
 228 with parametric analysis using the discrete element method (Kim et al., 2007b and  
 229 2007c). In Fig.9a, Groups 1-3 represent simulation cases that the standard deviation  
 230 (SD) of joint angle between each joint set is  $5^\circ$ , and the SDs of spacing and trace  
 231 length are 10, 20 and 30% of the mean values, respectively. Groups 4-6 (Fig. 9a)  
 232 represent simulation cases that the standard deviation (SD) of joint angle between  
 233 each joint set is  $10^\circ$ , and the SDs of spacing and trace length are 10, 20 and 30% of  
 234 the mean values, respectively. In Fig. 9b, S represents simulation cases that the SDs  
 235 of joint spacing and angle are within 30% of the mean value.

236 Normalised rock block size (Fig. 9a) and volume (Fig. 9b) decreased when  
237 discontinuity persistence increased, asymptotically approaching unity for fully  
238 persistent discontinuities. However it should be noted that the reciprocal  
239 relationships shown in Fig. 9 depended on the specific discontinuity orientations and  
240 number of joint sets (two sets) used in the simulation. In real projects, lithology and  
241 geological conditions should also be considered in the assessment of rock mass  
242 properties.

## 243 **4.2 Mechanical properties and deformability of non-persistently jointed rock** 244 **masses**

### 245 **4.2.1 Influence of persistence on rock mass behaviour**

246 Many factors control the overall mechanical properties of a rock mass which include  
247 intact rock matrix strength (Hu et al., 2012a), geometrical and mechanical properties  
248 of discontinuities, discontinuity intersections (stress distribution varies with the  
249 number and arrangement of discontinuities, Mughieda, 1997) and the interactions  
250 between discontinuities and rock matrix (such as block interlocking). There have  
251 been several classic rock mass classification schemes, for example, RMR  
252 (Bieniawski 1973, 1989), Q system (Barton et al., 1975) and GSI (Hoek et al., 1995),  
253 to assess the strength of rock masses. Generally, these classification schemes are  
254 empirically developed to provide a guidance for engineering support (except for GSI,  
255 which was semi-empirically designed for rock mass strength estimation) based on  
256 engineering projects and laboratory data (Hu et al., 2012b). A specific value  
257 considering different influential factors is assessed and calculated to reflect the  
258 quality of rock masses. Nevertheless, these schemes fail to explicitly consider the  
259 influence of persistence in the mass strength determination. For example, in GSI  
260 system, discontinuity persistence is only indirectly considered by the interlocking

261 descriptor (Cai et al., 2004); essentially discontinuities are assumed fully persistent.  
262 GSI therefore tends to underestimate the overall strength of a rock mass, especially  
263 at high confinement where interlocking effects are strong (Bharani and Kaiser 2013).  
264 Rock quality designation (RQD), originally introduced by Deere (1963) for the use in  
265 core logging, is one of the key parameters used in RMR and Q system. Sound core  
266 pieces greater than 100 mm in length are summed and expressed as a percentage  
267 of total core run. RQD however was devised to include only fully development  
268 discontinuities with zero tensile strength, so when incipient joint traces (which have  
269 considerable tensile strength) are also included in the assessment, rock mass  
270 strength is underestimated (Hencher 2014, 2015; Pells et al., 2017).

271 Prudencio and Van Sint Jan (2007) conducted laboratory tests on physical models of  
272 non-persistently jointed rock mass under biaxial loading condition. A set of non-  
273 persistent rock joints was made by inserting steel sheets into the mortar mixture  
274 during sample preparation. One of the key findings is that rock mass failure modes  
275 and compressive strength depended on the geometry of the discontinuity, loading  
276 stresses, and ratios of principle and intermediate stresses. Three basic failure modes  
277 were identified (i.e. failure through incipient joint plane, stepped failure and rotational  
278 failure of rock blocks).

279 Numerical modelling has been used to investigate the influence of persistence on  
280 overall mechanical properties of jointed rock masses. Kim et al. (2007a, b and c)  
281 examined how the incipient discontinuities with varying persistence values affect the  
282 mechanical properties of jointed rock mass. UDEC and 3DEC codes combined with  
283 experimental approaches were used in their study. Shear and compressive strengths  
284 of a jointed rock mass with and without considering persistence (represented as  $t$ ,  $t_0$ ,  
285  $\sigma_c$  and  $\sigma_{c0}$  respectively, with the zero subscript indicating fully persistent case) were

286 studied, while GSI values with and without considering persistence were calculated  
287 using the quantitative approach proposed by Cai et al. (2004). Normalised ratios  
288 found from Kim et al. (2007a, b) including  $t / t_0$ ,  $\sigma_c / \sigma_{c0}$  and  $GSI / GSI_0$  are plotted  
289 against discontinuity persistence (see Fig. 10). It can be seen that normalised  
290 shear strength (red curve) of jointed rock masses dramatically decreases when  
291 persistence increases. The analysis shows that the shear strength of rocks can be  
292 underestimated dramatically if persistence is ignored in the rock mass strength  
293 assessment. The normalised compressive strength (blue curve) and normalised GSI  
294 value (green curve) against persistence also show that the assumption of full  
295 persistence leads to strength underestimation but by a smaller extent, i.e., by about  
296 up to 1.5 times for each case.

297 Following their laboratory investigation of discontinuity geometry (Prudencio and Van  
298 Sint Jan 2007), the PFC3D code was used to investigate the effect of discontinuity  
299 persistence on the failure mechanism of jointed rock masses (Bahaaddini et al.,  
300 2013). Compressive strength and elastic modulus of rock masses with multiple  
301 layers of coplanar non-persistent discontinuities were examined (Fig. 11). In their  
302 study, persistence varied from 0.5 to 0.8 while other geometrical parameters were  
303 set to be constant except for the dip angle  $\beta$ , which varied from  $0^\circ$  to  $90^\circ$ . Their  
304 numerical results are reproduced in Fig. 12, with corresponding failure modes of  
305 samples when  $K=0.5$  and  $\beta=90^\circ$ . Compressive strength and elastic modulus of the  
306 rock mass decreased when persistence increased, for the same dip angle relative to  
307 the loading axis. Tensile cracks dominated at low persistence but decreased  
308 dramatically when persistence increased from 0.5 to 0.8 (see the insert diagrams of  
309  $\beta=90^\circ$ , Fig. 12a.). This phenomenon can be attributed to the reduction of the number

310 of joint tips. A further investigation was reported by Bahaaddini et al. (2016); a similar  
311 methodology was used and similar results were arrived at to those plotted in Fig. 12.

#### 312 **4.2.2 Rock slope stability considering non-persistent discontinuities**

313  
314 Non-persistent rock discontinuities have significant influence on the mechanical  
315 properties and deformability of rock masses and therefore on the stability of rock  
316 engineering projects such as engineered rock slopes. Large rock volumes  
317 (compared with joint spacing) can contain many discontinuities and therefore  
318 complex stress distributions, especially where discontinuities are randomly  
319 distributed. A challenging difficulty confronting practitioners is how to consider the  
320 incipency of discontinuities in large-scale stability analysis. In addition, the gradual  
321 development and coalescence of discontinuities over engineering time may have  
322 profound effects on stability. An illustrative example was presented by Hencher  
323 (2006), in which progressive development of sheeting joints over a period of many  
324 years was observed prior to the detachment of a large landslide in Hong Kong.

325 Einstein et al. (1983) proposed a probabilistic criterion for failure that was related to  
326 discontinuity data, to examine the effect of discontinuity persistence on rock slope  
327 stability. Only one set of parallel discontinuities with varying persistence was  
328 examined in their study. The “critical path” for a given discontinuity geometry  
329 (including coplanar and non-coplanar joint planes, such as an en echelon) was defined  
330 to consider strength contributions from discontinuities and intervening rock bridges  
331 as well as the spatial variability of discontinuity geometry. For this “critical path” they  
332 defined a minimum safety margin, SM, as the ratio of available resisting force to  
333 driving force. The SLOPESIM code was utilized to find the paths of minimum SM and

334 achieve probabilistic failure analysis of a jointed rock slope. In addition, the effect of  
335 probabilistic distribution of persistence was investigated using a parametric method.

336 The notion of representative volume element (RVE) of jointed rock masses was  
337 proposed by Pariseau et al. (2008) aiming to simultaneously enhance the reliability  
338 of large-scale rock mass stability analysis and dramatically reduce computer run  
339 time, from hundreds of hours to several hours. The RVE of a non-persistently jointed  
340 rock mass represents the smallest volume over which a measurement can be made  
341 that will yield a value representative of the whole. In this study, the stability of  
342 engineered open pit slopes was investigated by utilizing a finite element modelling  
343 technique in which RVE were recognised for a given discontinuity geometry, rather  
344 than modelling individual discontinuities. Equivalent discontinuity properties  
345 (Pariseau et al., 2008) were calculated for a given persistence for each set of  
346 discontinuities within the RVE, and then employed in the slope stability analysis. The  
347 main contribution of RVE approach is that numerous non-persistent discontinuities  
348 within a rock mass at project scale can be effectively dealt with.

349 In another study of the effect of incipency on rock mass strength behaviour, Viviana  
350 et al. (2015) proposed a method combining a probabilistic approach (assuming the  
351 distribution of the rock bridges along the sliding plane follows a fractal distribution  
352 law) using the discrete element method (DEM), to investigate translational sliding  
353 failure along a single incipient discontinuity within rock slopes. Three different sliding  
354 block geometries were investigated, that is, with block centres of gravity located in  
355 the upper part (Fig.13a), lower part (Fig.13b) and middle of sliding block (Fig.13c),  
356 respectively. For each situation, three different dip angles ( $30^\circ$ ,  $50^\circ$ , and  $70^\circ$ ) were  
357 used. The dominant slope failure mode (indicated by extent of shear versus tensile  
358 crack development) was found to be dependent on the slope geometry (dip of slope



359 and centre of gravity) and discontinuity persistence (Fig.13). For all situations, tensile  
360 and shear cracking increased dramatically when persistence decreased which  
361 confirms the finding by Bahaaddini et al. (2013) that higher tensile cracking arises  
362 from lower discontinuity persistence. For configurations where centres of gravity  
363 were located in the upper (see the schematic diagram in Fig.13a) and middle section  
364 of the sliding block (see the schematic diagram Fig.13c), shear cracks predominate,  
365 especially for a small dip angles i.e.,  $30^\circ$  where pure shear failure occurred. For  
366 higher dip angles, rock slopes often fail in by both tensile and shear cracking.

## 367 **5. Quantification of rock discontinuity persistence**

368 As discussed earlier, the influence of persistence on rock mass mechanical  
369 behaviour has long been known but generally has been dealt with crudely. Currently,  
370 there are no recommended methods to measure or predict discontinuity persistence.  
371 An approximation to real discontinuity size can be derived from measured trace  
372 length from rock exposures after correcting the sampling bias (e.g. Baecher et al.,  
373 1977; Priest and Hudson 1981; Mauldon 1998; Zhang et al., 2002; Latham et al.,  
374 2006) but with inherent limitations.

### 375 **5.1 Discontinuity data collection and size estimation**

376 Data acquisition of discontinuities from exposed rock faces, can be grouped into two  
377 categories: manual methods (i.e. scanline sampling and window sampling) and  
378 computer-aided methods.

#### 379 **5.1.1 Scanline and window sampling methods**

380 At planar or nearly planar rock exposures, statistical sampling methods including  
381 scanline and window approaches have been widely used to measure the extent of  
382 discontinuities intersected.

383 In straight scanlines, a tape is laid along rock face, and the joint traces intersecting  
384 the line in a scanline survey are recorded. In practice, surveys including between  
385 150 and 350 discontinuities are suggested and colour photos of exposed rock faces  
386 and scale makers are useful (Hudson and Priest, 1979). Scanline surveys may be  
387 grouped into two categories: quick scanline and detailed scanline. For a quick  
388 scanline survey, only the location of the scanline, the chainage of each intersection,  
389 plunge and azimuth of joint traces are recorded. Detailed scanline surveys normally  
390 also include, discontinuity types (e.g. joints, bedding, foliation, lamination and  
391 cleavage), trace length, aperture and infilling condition, planarity, waviness,  
392 termination and water condition (any evidence of seepage). A good example  
393 template of detailed scanline survey is produced by Hencher (2015), in which relative  
394 strength to parent rock was additionally suggested to be considered.

395 Fig. 14 diagrammatically shows a scanline survey on a planar rock face of limited  
396 extent. This survey is subject to some drawbacks, for example, sampling biases,  
397 orientation bias and censoring bias, which have been noted by many researchers  
398 (e.g. Cruden 1977). These biases are summarised as follows:

399 (1) Size bias. Scanlines will preferentially identify those discontinuities with a  
400 longer trace length, and small traces on exposures are missed (Priest and  
401 Hudson 1981)

402 (2) Orientation bias. Discontinuities striking roughly parallel to the scanline will be  
403 under-represented and excluded from the sampling results. This will lead to a  
404 serious misinterpretation of discontinuity extent as some critical information is  
405 omitted. Park and West (2002) verified and emphasised the orientation bias  
406 based on the examination of the differences in results from vertical borehole  
407 fracture mapping method and horizontal scanline sampling. Selection of

408 several scanline directions in the measurement of trace length can, to some  
409 extent, eliminate the orientation bias and it is recommended that scanlines  
410 should be measured in each orthogonal direction (Priest 1993; Hencher 2015)

411 (3) Censoring bias. Rock exposures are limited and relatively small compared  
412 with major joints. Inevitably for large discontinuities, one end or both ends,  
413 may extend beyond the visible exposure, therefore they are censored to some  
414 degree depending on discontinuity size (Cruden 1977). The censoring bias  
415 should be considered in the inference of discontinuity size (Baecher 1980).

416 Window sampling, another manual data acquisition technique, has also been used  
417 for sampling the discontinuities exposed at a given rock face. The preliminaries and  
418 measurement techniques are similar to scanline survey except that all discontinuities  
419 are measured in a finite area, rather than the intersection of the scanline. For setting  
420 up window sampling, a rectangle or circular area is defined on the outcrop. The  
421 window should be sufficiently large to reduce the sampling bias, with each side  
422 intersecting between 30 and 100 discontinuities. Discontinuities are counted and  
423 classified into three classes (Pahl 1981; Zhang and Einstein 2000):

424 (1) Discontinuities contained in the window: both ends of discontinuities are  
425 visible in the sampling domain.

426 (2) Discontinuities that transect the window: both ends of discontinuities are  
427 invisible in the sampling domain, this is, ends beyond the limits of window.

428 (3) Discontinuities that intersect the window: only one end is visible in the window  
429 and another one beyond the limits of sampling area.

430 Although window sampling still suffers from the censoring issue, this method  
431 normally is able to eliminate size and orientation biases (Mauldon et al., 2001). In

432 addition, discontinuity termination characteristics can also be logged by using  
433 window sampling (Dershowitz and Einstein 1988), but it does not provide any  
434 information about discontinuity orientation or surface geometry (Priest 1993).

435 Manual data acquisition methods suffer from some limitations. The first is that they  
436 are labour and time consuming. In order to minimise the sampling bias, sampling  
437 should be conducted at many different locations. The operator's safety during  
438 sampling is another issue. The second is that unbiased discontinuity characterisation  
439 requires a skilled interpretation (rock engineer or geologist). The third limitation is  
440 that manual methods cannot collect data from rock exposures that are not  
441 accessible. So researchers have paid a lot attention to producing alternative ways to  
442 obtain discontinuity data from outcrop.

### 443 **5.1.2 Computer aided sampling**

444 Computer aided sampling methods for discontinuity characterisation have made  
445 significant advances over the last 25 years. An image analysis technique, perhaps  
446 the pioneer work towards this topic, was proposed by Ord and Cheung (1991) to  
447 describe discontinuities in outcrop automatically. Since then, computer-aided  
448 techniques have been developed. Roberts and Poropat (2000) proposed a digital  
449 photogrammetric technique to investigate three dimensional models of rock faces.  
450 Feng et al. (2001) proposed a portal system, in which a laser range finder was used,  
451 to identify discontinuities in outcrop. Several computer aided techniques including  
452 digital photogrammetry (e.g. Tuckey and Stead 2016), ground-based LiDAR (e.g.  
453 Mattew and Malte 2012), and digital trace mapping (Tuckey et al., 2012) have been  
454 applied to develop a standardized and adaptable methodology for assessing  
455 discontinuity persistence. An example among these techniques is shown in Fig. 15

456 (Tuckey et al., 2012), in which the image processing code Image-J was used to trace  
457 discontinuities and infer rock bridges. The results of the study were used to  
458 supplement field window sampling. Umili et al. (2013) developed an automatic  
459 method to map and identify discontinuity traces based on a digital surface model  
460 (DSM), which consists of a triangulated point cloud that approximates the true  
461 surface. Terrestrial Laser Scanner (TLS) and Terrestrial digital photogrammetry  
462 (TDP) have also been widely used in characterising discontinuities and rock face  
463 morphology (e.g. Rosser et al., 2005; Sturzenegger and Stead 2009 a, b; Slob 2010;  
464 Sturzenegger et al., 2011; Brideau et al., 2012). Abellan et al., (2014)  
465 comprehensively reviewed the application of TLS technique to rock exposure  
466 characterization. These methods are generally based on the segmentation of the  
467 rock exposures, and discontinuity characteristics are obtained from the boundaries  
468 and orientations of the identified planes (Umili et al., 2013). Data collected is  
469 statistically examined and is used for the rock mass characterisation.

### 470 **5.1.3 Discontinuity size estimation from censored measurements**

471 Discontinuity size is often estimated based on censored sampling measurements  
472 using the aforementioned techniques. As visible trace length does not equal to true  
473 persistence, probability distributions of trace lengths need to be corrected for  
474 sampling biases to provide an estimate of the true discontinuity size (or trace length)  
475 distribution. Well formulated probability sampling planes should be used otherwise  
476 errors will occur (Baecher and Lanney 1977). Table 1 presents a selection of key  
477 publications advancing these approaches highlighting the methods used, sampling  
478 techniques they are applicable, and major assumptions.

## 479 **5.2 Discontinuity persistence in the subsurface**

480 Geophysical techniques have been used to investigate discontinuities in the  
481 subsurface (e.g. Grandjean and Gourry 1996; Willenberg et al., 2008; Kana et al.,  
482 2013). The paper by Longoni et al. (2012) provided illustrating insights into the  
483 application of radar in the investigation of subsurface discontinuity persistence. In  
484 their work, ground penetrating radar surveys were conducted to image the 3D  
485 discontinuity planes inside rock mass, thereafter discontinuity persistence was  
486 calculated. Geological discontinuities in the subsurface are usually complex thus  
487 sometimes will frustrate geophysical sampling, geophysical approaches requires a  
488 high resolution to be able to sample discontinuities as these are relatively thin, and  
489 an experienced operator is also needed to process and interpret discontinuities  
490 within radar datasets.

## 491 **5.3 Forensic excavation of rock masses**

492 In a recent work reported by Shang et al. (2017a), a new technique, termed forensic  
493 excavation of rock masses (FERM), was introduced as an approach for investigating  
494 discontinuity areal persistence. Fig. 16 shows the FERM testing procedures. This  
495 technique involves non-explosive excavation of rock masses by injecting an  
496 expansive grout along incipient discontinuities. The agent causes the incipient rock  
497 discontinuity traces to open as open joints, thus allows the observation of areal joint  
498 surfaces and determination of areal persistence. Laboratory and field tests has been  
499 conducted on two lithologies (Midgley Grit Sandstone and Horton Formation  
500 Siltstone) by the authors, which demonstrated that FERM allows measurement of  
501 areal persistence at laboratory scale and field scale over the range of a few meters.  
502 Project scale tests will hopefully to be conducted to verify the capability of FERM at  
503 larger scales.

## 504 **6. Summary, conclusion and recommendations for future research**

### 505 **6.1 Summary and conclusion**

506 It has been nearly four decades since awareness of the importance of discontinuity  
507 persistence in earth science applications (Cruden 1977; ISRM 1978). Some  
508 endeavours have been made to consider persistence during the measurement of  
509 discontinuities (e.g. ISRM 1978; Priest and Hudson 1981; Latham et al., 2006) and in  
510 the assessment of rock mass stability (e.g. Einstein 1983; Pariseau et al., 2008).  
511 These endeavours however have not led to standard methods to quantify real  
512 persistence. This review has described the fundamentals of this topic e.g. definitions  
513 (incipient, mechanical discontinuities and persistence), mechanical properties of  
514 individual rock discontinuities, and those of rock masses containing non-persistent  
515 joints. State-of-the-art methodologies in the description and quantification of  
516 discontinuity persistence were summarised and reviewed.

517 Areal persistence, reflecting the three dimensional nature of geological  
518 discontinuities, is the best measure of persistence. Studies aiming at quantification of  
519 discontinuity persistence have been relatively few in number. In rock engineering  
520 practice, “geological judgements” are often used, but these can fail to represent the  
521 three dimensional nature of discontinuities, for example where linear persistence is  
522 used to represent areal persistence.

523 The size and volume of rock blocks within rock masses are sensitive to discontinuity  
524 persistence and will be underestimated if 100% persistence is assumed. Geometrical  
525 considerations based on uniform joint spacing imply a reciprocal cube-root  
526 relationship between discontinuity persistence and block size / block volume (Eq. 6),  
527 whereas previous studies using more realistic spacing distributions suggest a

528 reciprocal relationship i.e.  $V_b/V_0 \sim K^{-1}$ . However, the specific lithology and geological  
529 conditions should be considered in the assessment of rock mass properties based  
530 on persistence values.

531 Failure modes of a rock mass are generally controlled by the discontinuities. Studies  
532 show that discontinuity persistence, orientation and number of discontinuities  
533 overshadow the efficacy of other factors. Potential for sliding failure of rock slopes  
534 along planar discontinuities is mainly controlled by the persistence and orientation of  
535 discontinuities. In addition, the spatial distributions and geometries of intact rock  
536 bridges as well as mineral infills influence the mechanical properties of incipient  
537 discontinuities (Shang et al., 2016).

## 538 **6.2 Recommendations for future research**

539 The authors recommend some topics that might be taken up for future research.

540 These are as follows:

541 (1) Current definitions of persistence (i.e., Eqs. 1 and 2) only apply to planar  
542 discontinuities. Engineering applications based on the definitions will unavoidably  
543 have some limitations, as some discontinuities are not planar in shape (e.g., 'zig-zag'  
544 and 'en-echelon' fractures). Thus, there is a need to define persistence for non-  
545 planar discontinuities; thereafter a full spectrum of discontinuity persistence is able to  
546 be quantified and implemented into engineering applications such as discrete  
547 fracture network modelling.

548 (2) Up to date, rock engineering practise lacks standard methods to deal with the  
549 incipency of some discontinuities, i.e. those that are not fully developed mechanical  
550 break with some tensile strength. The degree of incipency of discontinuities can be  
551 described by their tensile strengths relative to that of parent rock. Tensile strength is



552 suggested because incipient discontinuity shear strength is complicated by other  
553 factors, including roughness and asperities of the persistent sections. A classification  
554 scheme differentiating incipient discontinuities has been conceptually proposed  
555 by Hencher (2014) with different bands including open fracture, weak, moderate and  
556 high. Direct tensile tests on incipient rock discontinuities have been conducted by  
557 Shang (2016) in the laboratory to follow up that topic. However, limited tests were  
558 involved due to the difficulty of the natural sample collection and preparation. It is  
559 therefore suggested that more tests need to be performed to facilitate the production  
560 of the classification scheme of discontinuity incipient.

561 (3) In a recent study by Shang et al. (2017a), the quantification of areal persistence  
562 was attempted by “forensic excavation of rock masses (at block sale)”; this technique  
563 needs proof of concept at larger scales.

564 (4) Non-invasive quantification of persistence might also be achieved using  
565 geophysics, which if successful will improve the ability to predict rock mass  
566 properties.

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888 **Figure Captions**

889 **Fig 1** Partially developed discontinuities that are incipient (non-persistent), Horton-in-  
890 Ribblesdale, Yorkshire, England.

891 **Fig 2 a** Section of andesitic tuff cores (Hong Kong) with incipient and mechanical  
892 discontinuities and **b** Same core (disassembled). Relative tensile strength, i.e.,  
893 high, moderate and weak strength relative to the strength of the parent rock, is  
894 proposed to differentiate these discontinuities. Adapted from Hencher (2014).

895 **Fig 3** A Face cut by a diamond wire saw in dimension stone quarry in granite near  
896 Tui, Galicia, Spain. Joints 1 and 2 are in earlier incipient stages (which are  
897 always poorly defined by current standards). Joint 3 is in later incipient stage  
898 and it has a persistent area partially, allowing seepage of fluid. After Shang et  
899 al. (2016)

900 **Fig 4** Definitions of rock discontinuity persistence. **a** Areal extent of a discontinuity  
901 plane (true persistence) and **b** Linear extent definition (approximation of  
902 persistence).

903 **Fig 5** Slope with daylighting rock slabs threatening highway in central Taiwan. The  
904 incipient nature of the discontinuities contributes tensile and shear strength and  
905 allows temporary stability.

906 **Fig 6** General view of a collapsed overhanging limestone slab located at northern  
907 part of Cellina Valley gorge on January 26th, 1999. A rock bridge (red-hatched  
908 area) was exposed after failure. The average tensile strength of this rock bridge  
909 was calculated as 5.19 MPa through back-analysis. After Paronuzzi and  
910 Serafini (2009).

911 **Fig 7** Relationship between shear displacement and horizontal shear force for  
912 various numerical models containing non-persistent rock joint with different  
913 geometrical parameters. Adapted from Zhang (2006).

914 **Fig 8** Stress and strain curves of Midgley Grit Sandstone joints with the same areal  
915 persistence ( $K=0.5$ ) in numerical direct shear tests under constant normal  
916 stresses of 4 and 6 MPa. Three samples showing the spatial distribution of rock  
917 bridges (Rb) and persistent joints (Pj) are shown. Particles representing rock  
918 matrix (within the top and bottom shear boxes) are not shown for clarity. After  
919 Shang and Zhao (2017).

920 **Fig 9** Relationship between joint persistence and normalized block size (**a**) and block  
921 volume (**b**). Raw data from Kim et al. (2007b and 2007c).

922 **Fig 10** Relationship between relative rock mass strengths and persistence. Raw  
923 data from Kim et al. (2007b and 2007b).

924 **Fig 11** Discontinuity geometrical parameters used in the numerical modelling by  
925 Bahaaddini et al. (2013). Reproduced from Bahaaddini et al. (2013).

926 **Fig 12** Effects of discontinuity persistence on relative compressive strength of rock  
927 masses (**a**) and on relative elastic modulus of rock masses (**b**). Note that yellow  
928 is rock matrix in PFC model; green is non-persistent rock joint; red is tension  
929 crack and blue is shear crack (rarely can be seen). K refers to linear  
930 persistence. Adapted from Bahaaddini et al. (2013).



931 **Fig 13** DEM study results of the relationship between number of micro-cracks and  
932 discontinuity areal persistence. Schematic diagrams of simulated slopes with  
933 three different geometries are included (cracks are not shown): Centres of  
934 gravity were located in the upper part (**a**), lower part (**b**) and the middle (**c**),  
935 respectively. Shear cracks dominated when centres of gravity were located in  
936 the upper part (**a**) and middle (**c**) of sliding block. Both tensile and shear cracks  
937 occurred when centre of gravity was in the lower part of block. The dashed lines  
938 correspond to tensile crack while continuous lines represent shear crack.  
939 Adapted from Viviana et al. (2015)

940 **Fig 14** Diagrammatic representation of discontinuity traces intersecting a scanline  
941 set up on a planar exposure of limited extent. For small size discontinuities or  
942 those that are roughly parallel to scanline or concealed, bias will occur when  
943 sampling. Adapted from Latham et al. (2006).

944 **Fig 15 a** Digital trace mapping of incipient discontinuities and blast-induced fractures  
945 on local part of the Stawamus Chief (granite), British Columbia, Canada; **b**  
946 Discontinuity traces were analysed after tracing. Irregular blast-induced  
947 fractures were traced in red, bedding planes traced in green and scattered  
948 joints traced in cyan and orange. After Tuckey et al. (2012).

949 **Fig 16** Schematic diagram showing the testing procedures for the forensic  
950 excavation of rock masses (FERM). After Shang et al. 2017a

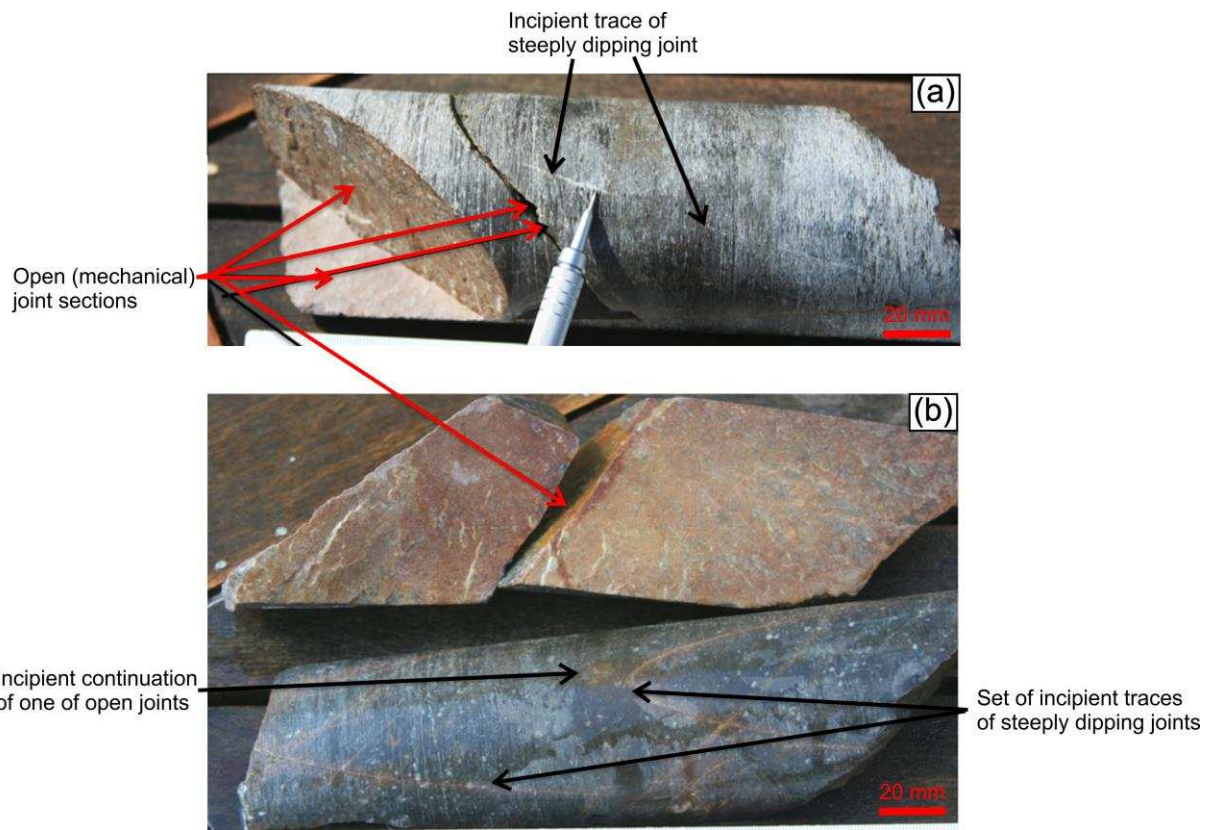


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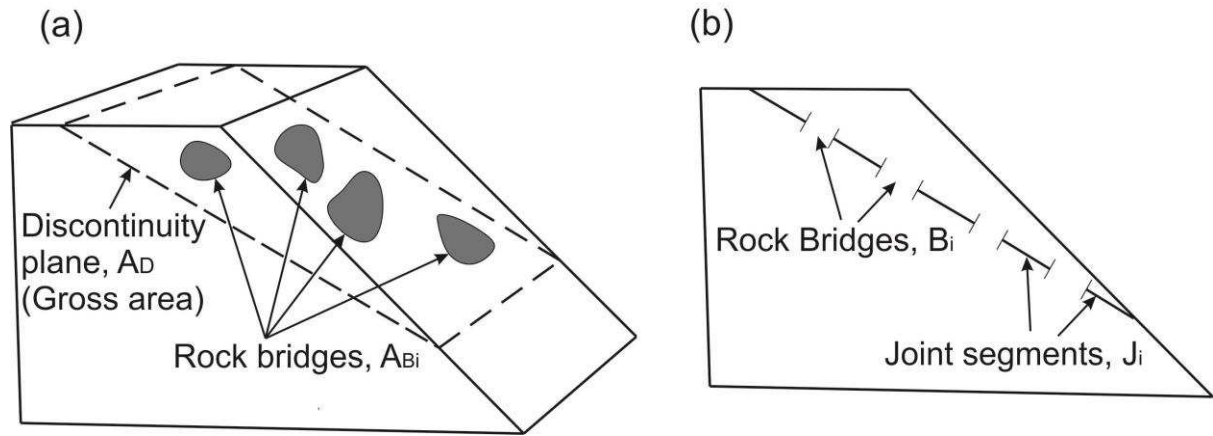
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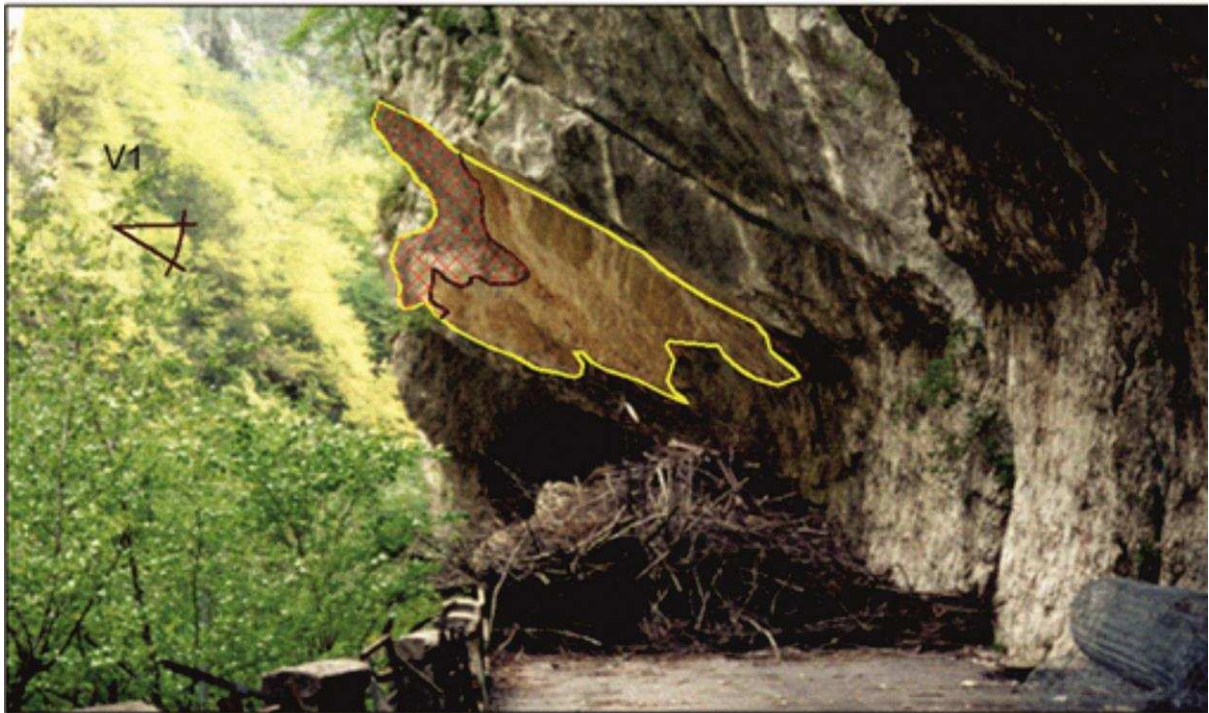
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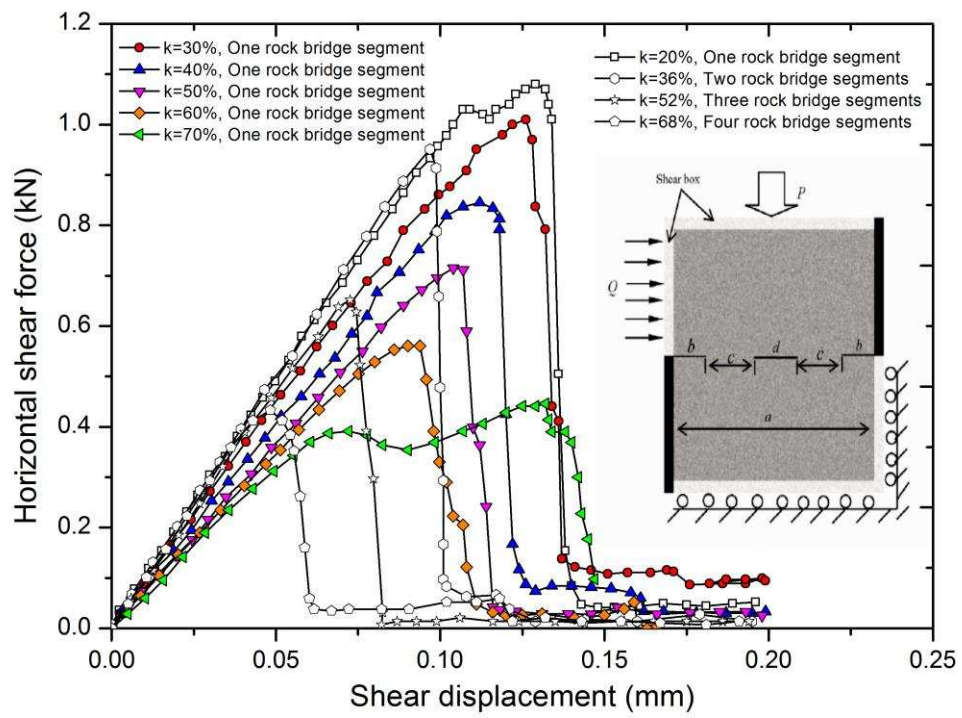
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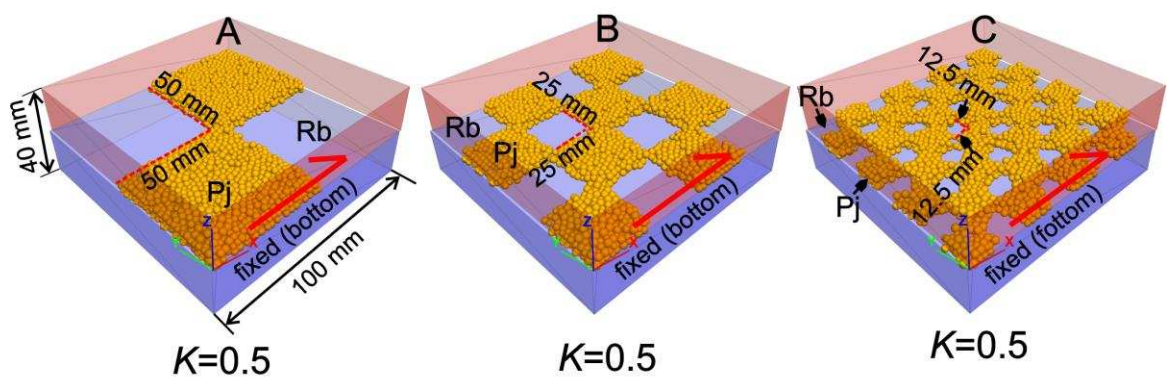
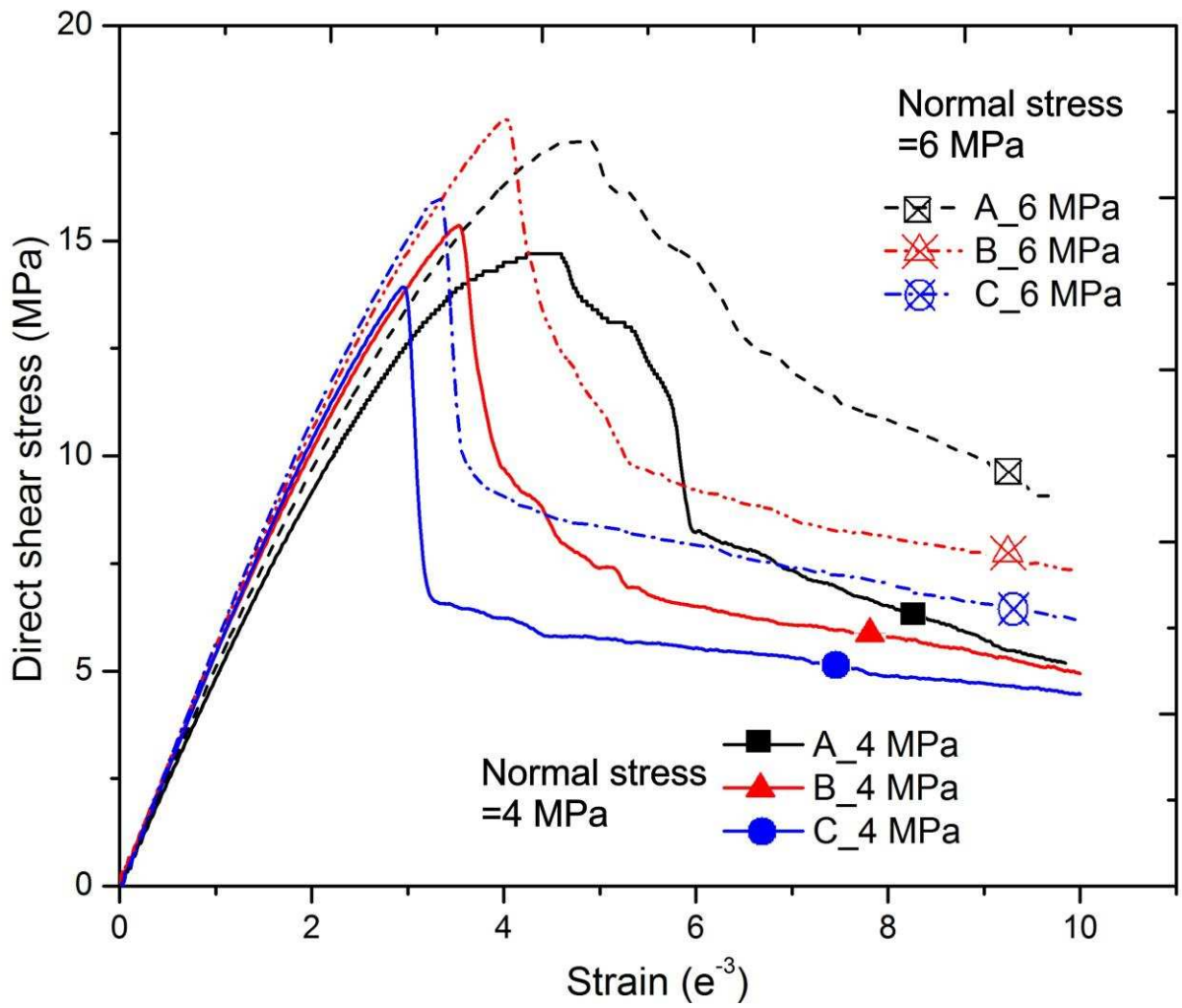
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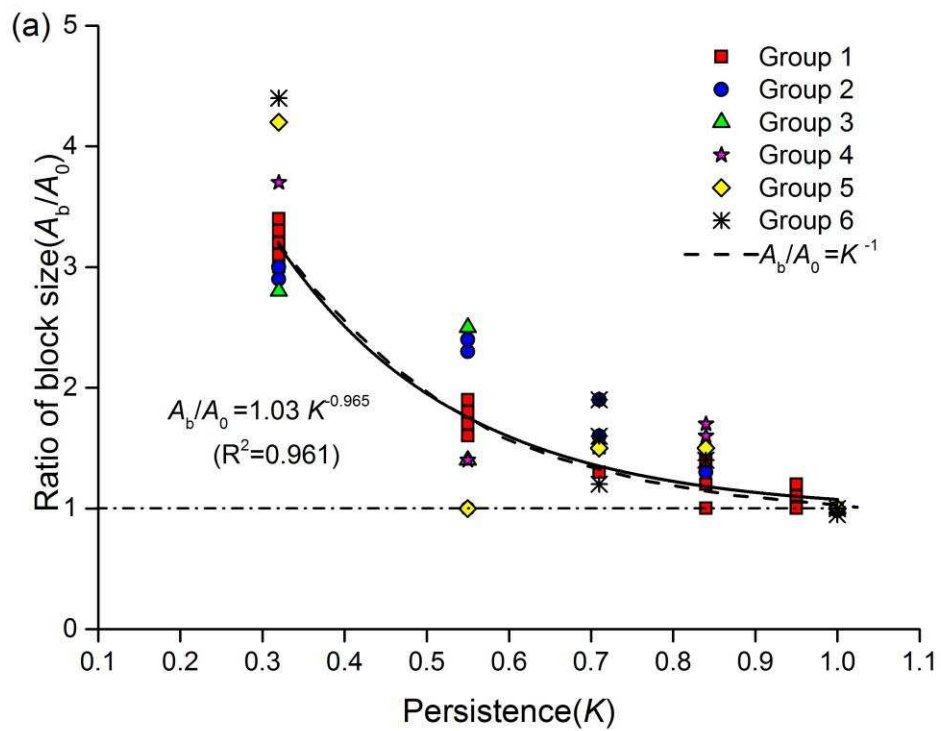
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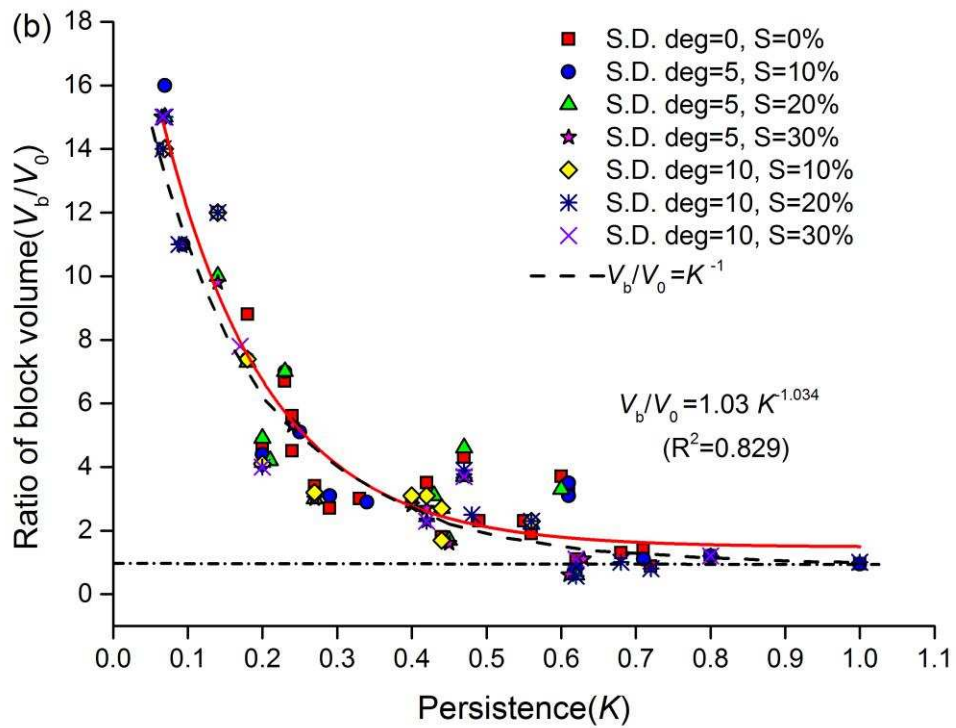
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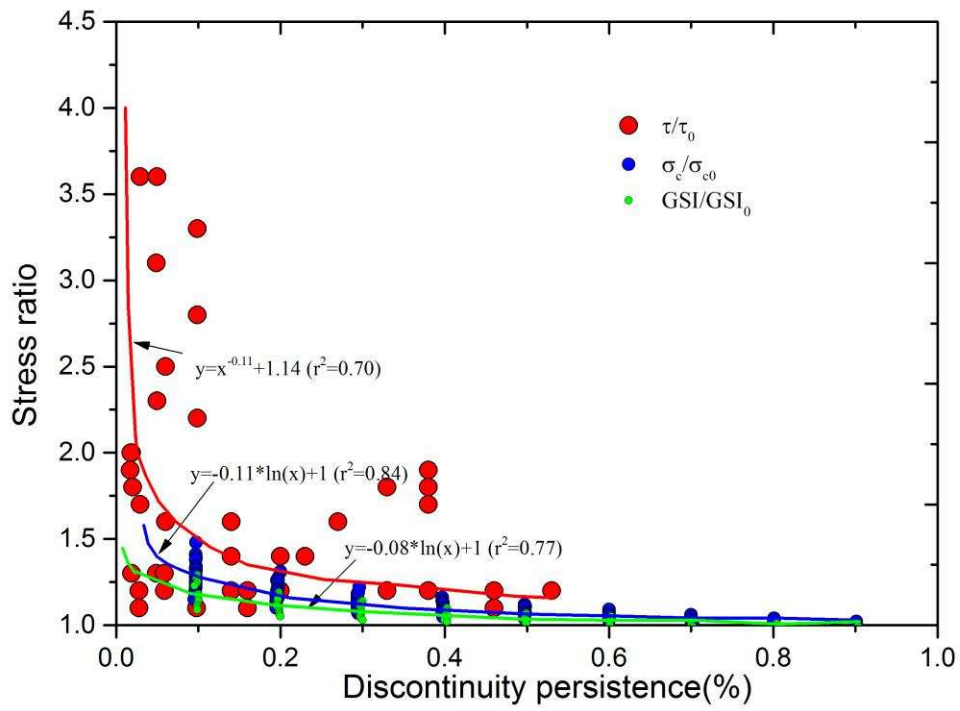


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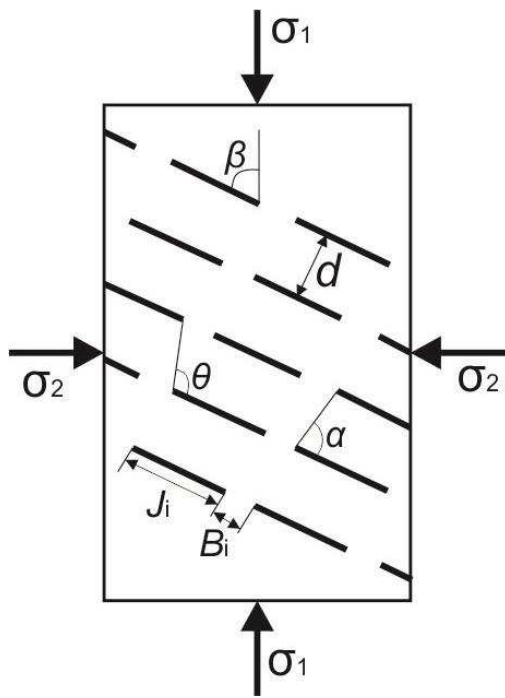
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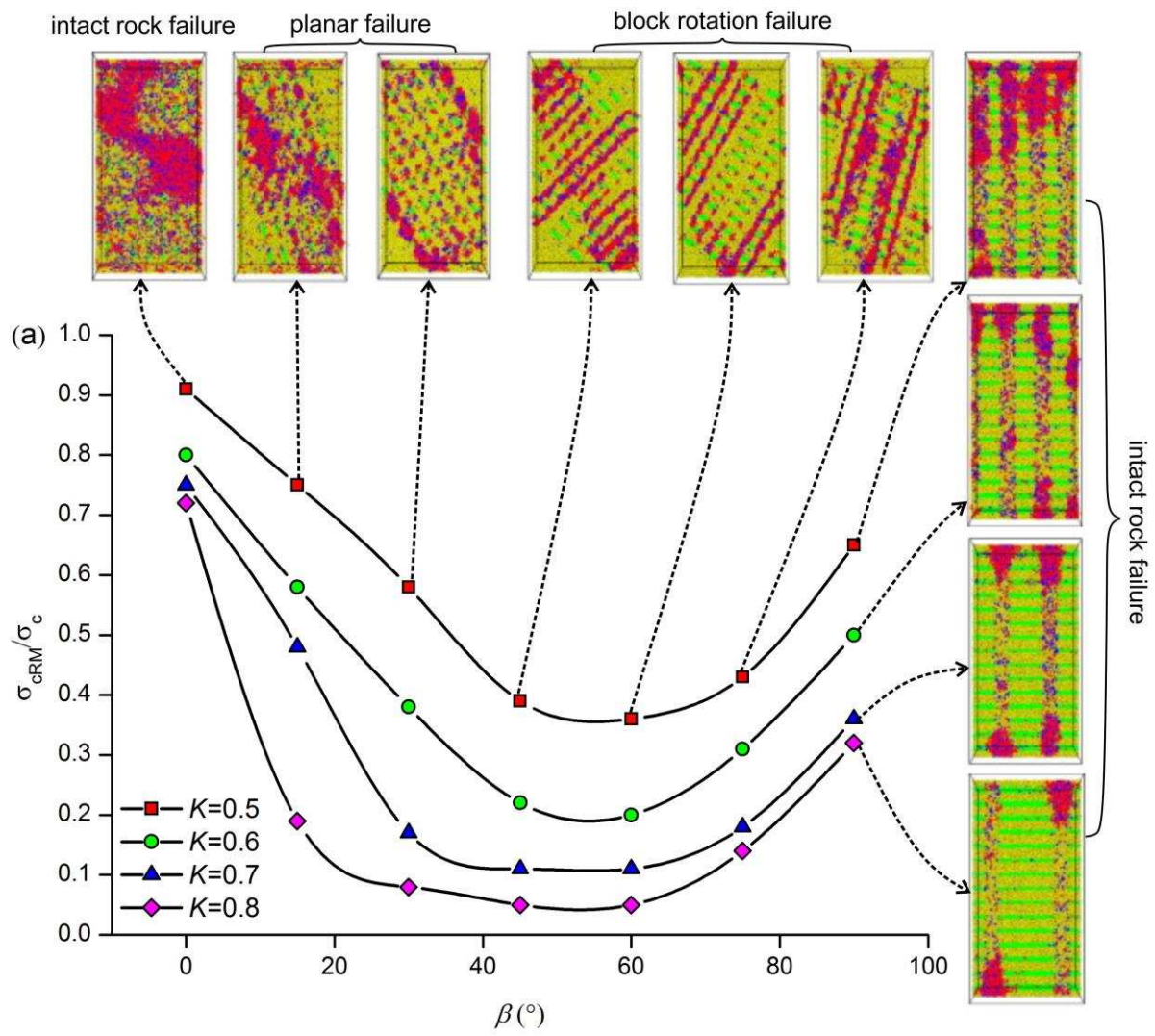
Parameter keys

- $\beta$  Joint orientation relative to loading axis
- $\theta$  Joint step angle
- $\alpha$  Joint tip to tip angle
- $d$  spacing
- $J_i$  Persistent joint segment
- $B_i$  Rock bridge segment
- $\sigma_1$  Principle stress
- $\sigma_2$  Intermediate stress

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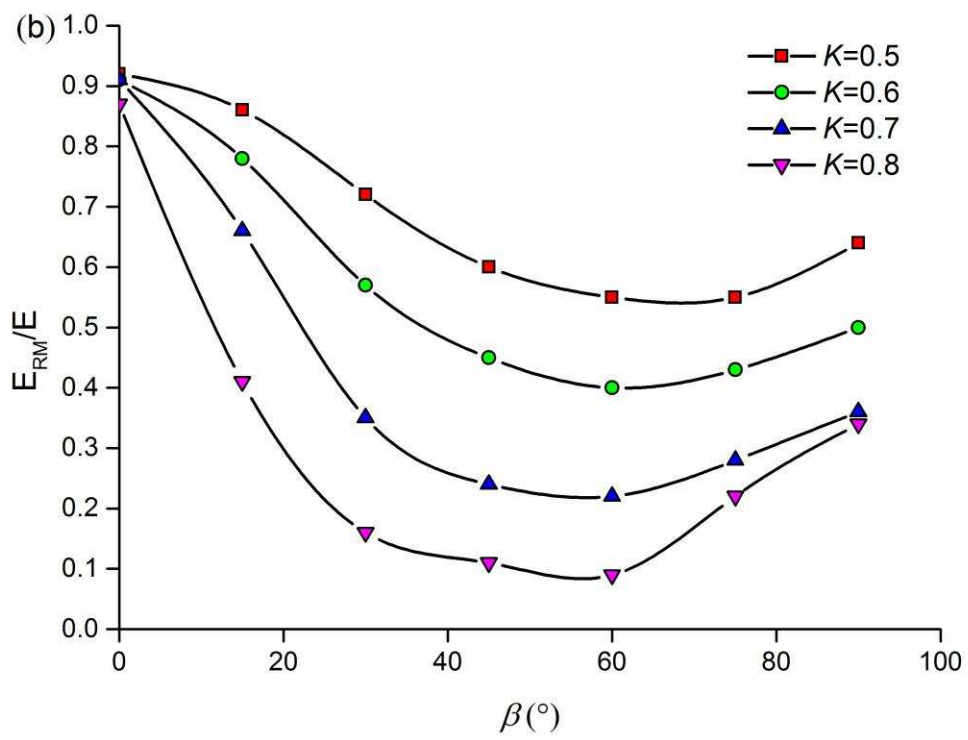
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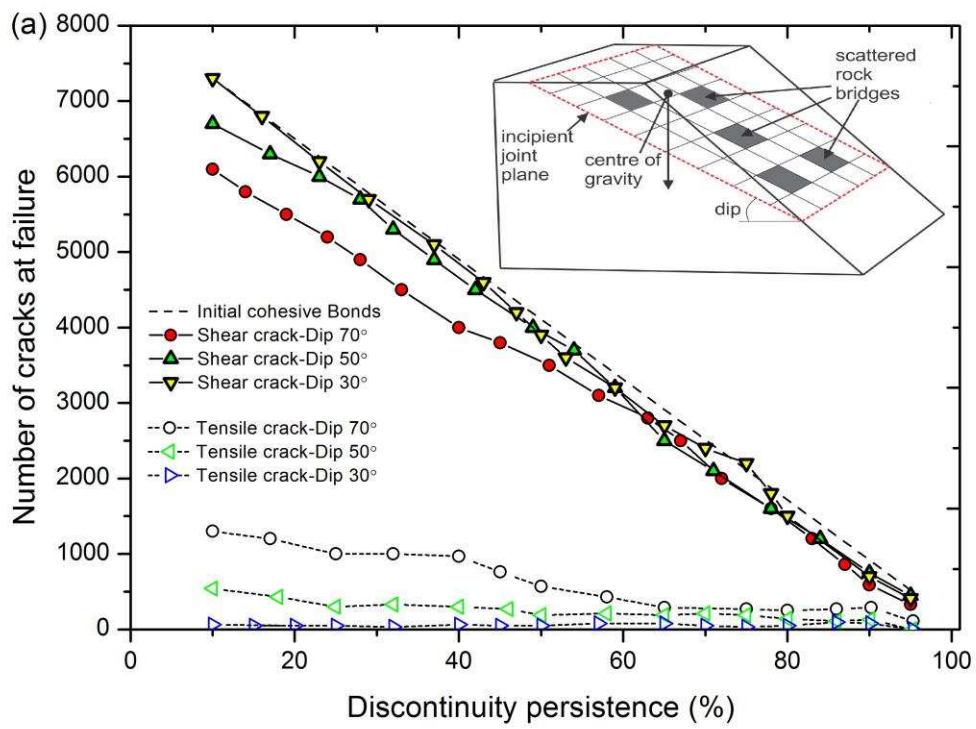
1053 Fig 12a



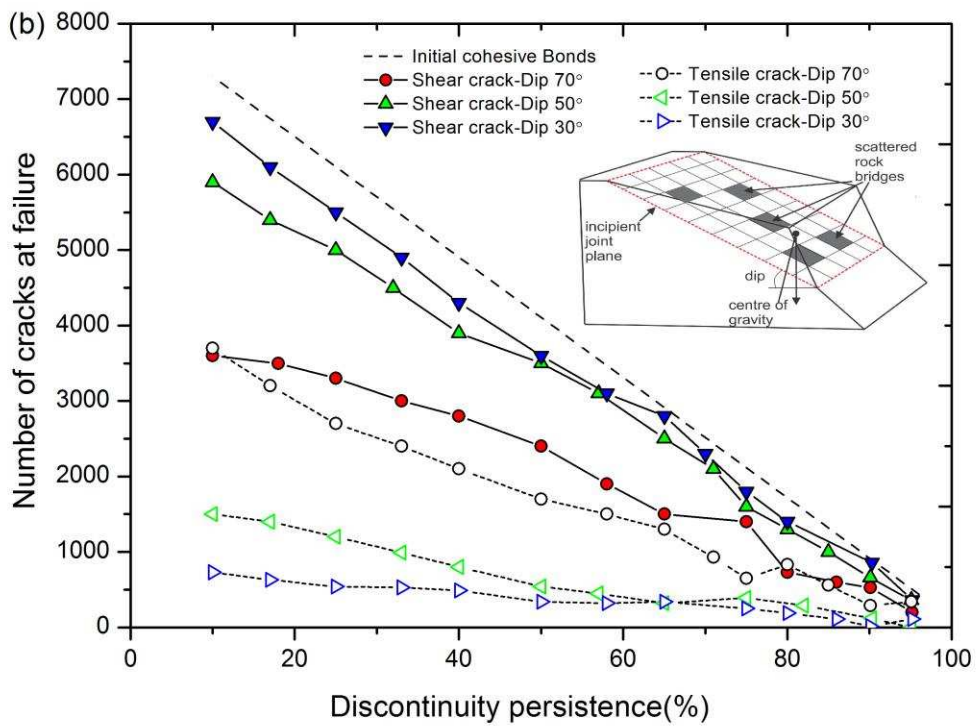
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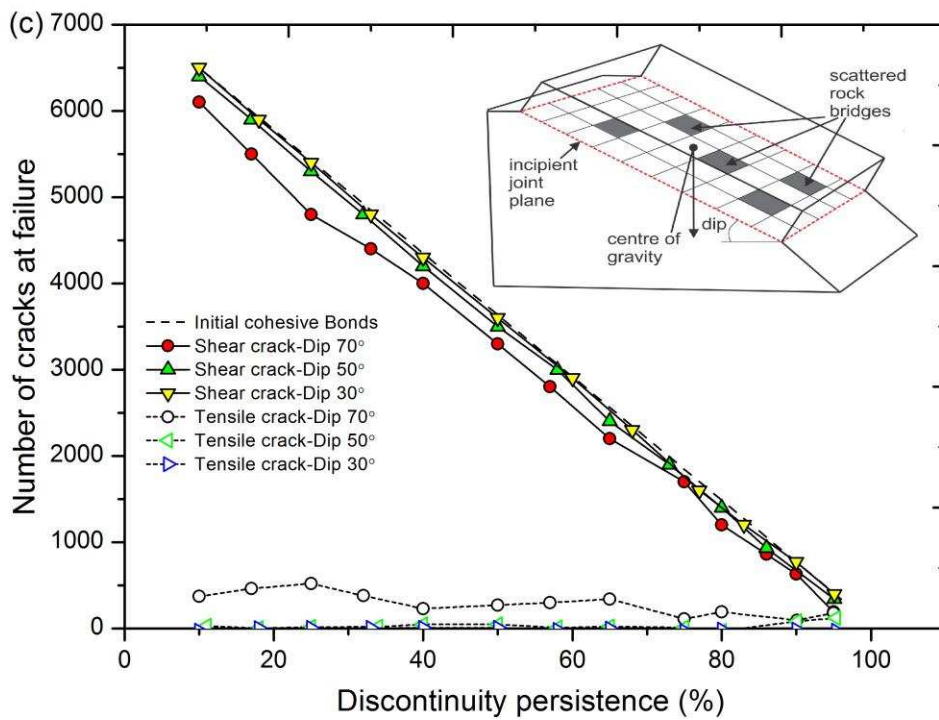
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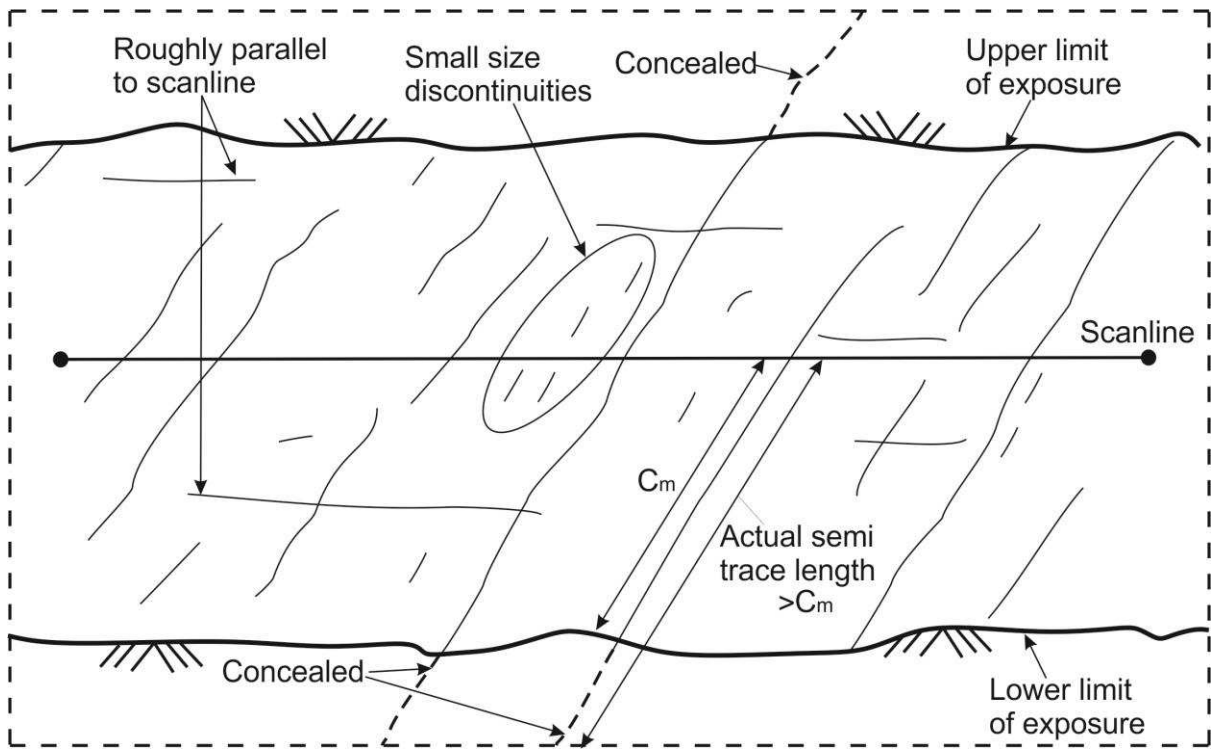
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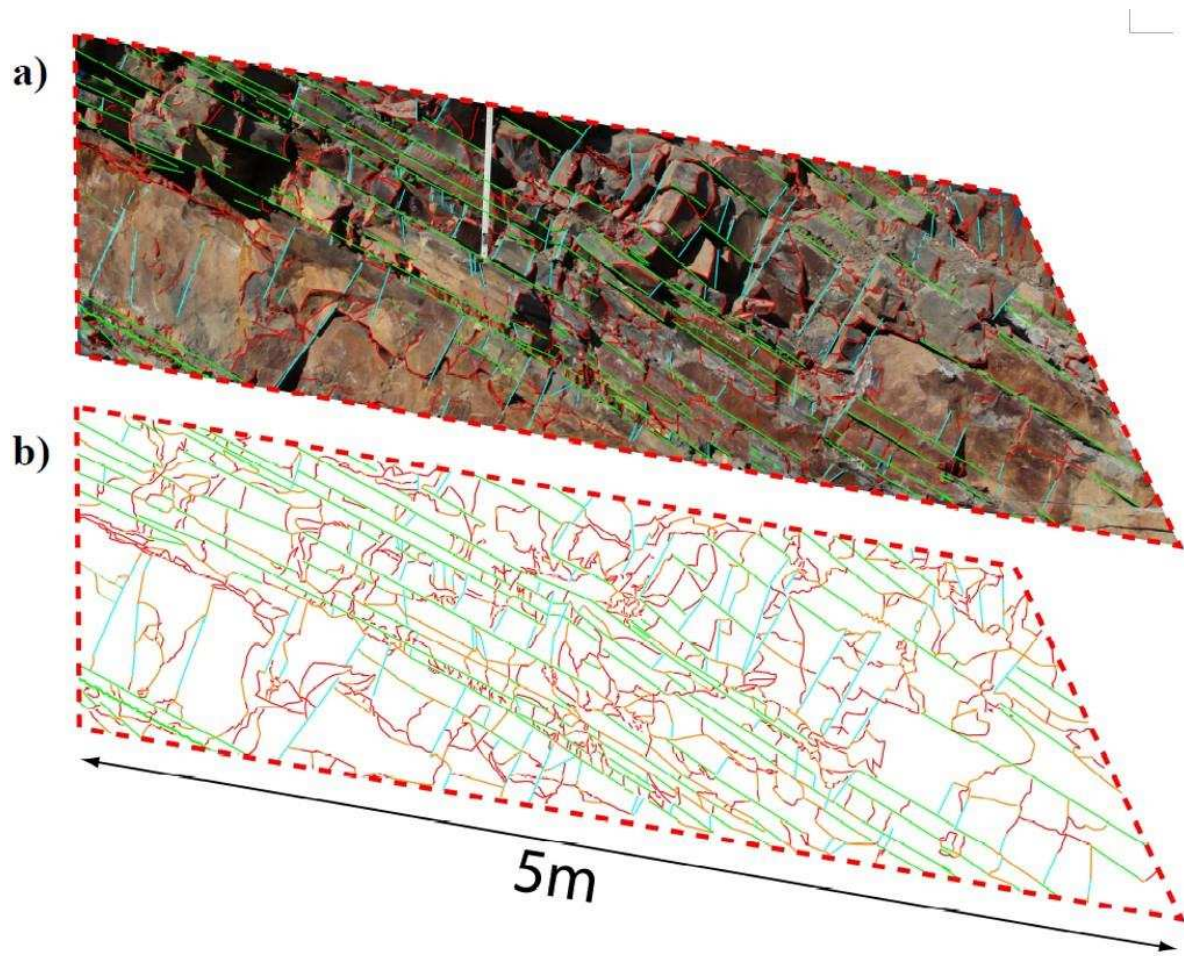


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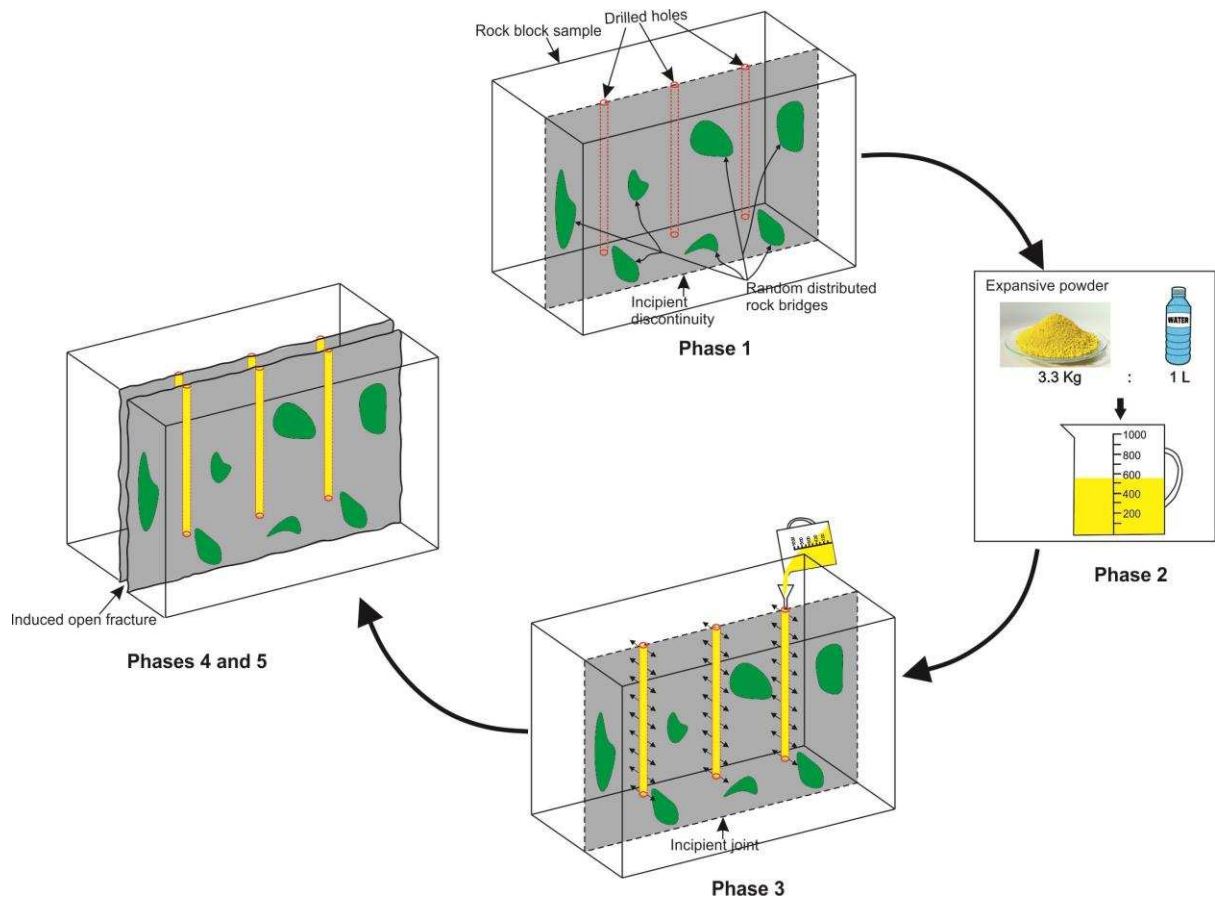
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**Table 1** Representative contributions to discontinuity size (trace length) estimation from censored measurements.

<b>Methodologies</b>	<b>Major contributions</b>	<b>Remarks</b>	<b>Sampling methods</b>	<b>References</b>
Censored exponential distribution	Field procedure was devised to provide a method for characterizing and estimating trace length. Data requirements dramatically reduced.	The analysis does not consider type of discontinuity termination and tends to overestimate larger trace length.	SS	Cruden 1977
Moment estimate	Moment estimation of unconditional radius distribution of joints was presented.	Reliability of results depends on the probability function assumed.	SS	Baecher and Lanney (1978)
Probability distribution analysis	Four simple probability distributions were used to study bias in scanline sampling. The relations between these distributions provide analytical methods of estimating mean discontinuity trace length.	Reliability of results depends on the probability function assumed.	SS	Priest and Hudson (1981)
Probability distribution function	A technique was proposed for estimating mean trace length on infinite exposures. Does not require lengths and density function of observed traces.	Only applicable to discontinuities whose orientation is described by a probability distribution function.	WS	Kulatilake and Wu (1984)
Distribution-free methods	Simple estimators were developed for the estimation of variably oriented fracture trace length as well as trace density.	Reliability of results depend on the probability function assumed; underlying distribution of trace length is generally unknown.	WS	Mauldon (1998)
Probability analysis, numerical and analytical methods	Joint trace length distribution was estimated for the Poisson disc joint model. Joint diameter distribution was also numerically and analytically investigated	Relies on the assumption that joint lengths are similar in strike and dip directions.	WS	Song and Lee (2001)
Stereological relation analysis	Stereological analysis used to estimate size distributions of elliptical discontinuity from true trace length distribution.	Discontinuity assumed planar and elliptical in shape.	SS and WS	Zhang and Einstein (2002)
Maximum likelihood method	Extends previous methods to include arbitrary joint set and sampling plane orientations.	Derived results only apply for joint traces normal to top and bottom of sampling window.	WS	Lyman (2003)
Statistical graphical approach	A flexible method for inference of trace length using statistical graphical model based on observations at rock outcrops.	--	WS	Jimenez-Rodriguez and Sitar (2006)

Probability weighted moments (PWM) and L-moments	A distribution-free method to estimate fracture trace length distributions in the light of the estimation of PWM and L-moments of true trace length.	--	WS	Li et al. (2014)
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SS: Scanline Sampling; WS: Window Sampling

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