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Research Article

Statistical analysis of coverage error in simple global temperature estimators

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Abstract

Background. Global mean surface temperature is widely used in the climate literature as a measure of the impact of human activity on the climate system. While the concept of a spatial average is simple, the estimation of that average from spatially incomplete data is not. Correlation between nearby map grid cells means that missing data cannot simply be ignored. Estimators that (often implicitly) assume uncorrelated observations can be biased when naively applied to the observed data, and in particular, the commonly used area weighted average is a biased estimator under these circumstances. Some surface temperature products use different forms of infilling or imputation to estimate temperatures for regions distant from the nearest observation, however the impacts of such methods on estimation of the global mean are not necessarily obvious or themselves unbiased. This issue was addressed in the 1970s by Ruvim Kagan, however his work has not been widely adopted, possibly due to its complexity and dependence on subjective choices in estimating the dependence between geographically proximate observations.

Objectives. The aim of this work is to present a simple estimator for global mean surface temperature from spatially incomplete data which retains many of the benefits of the work of Kagan, while being fully specified by two equations and a single parameter. The main purpose of the simplified estimator is to better explain to users of temperature data the problems associated with estimating an unbiased global mean from spatially incomplete data, however the estimator may also be useful for problems with specific requirements for reproducibility and performance.

Methods. The new estimator is based on generalized least squares, and uses the correlation matrix of the observations to weight each observation in accordance with the independent information it contributes. It can be implemented in fewer than 20 lines of computer code. The performance of the estimator is evaluated for different levels of observational coverage using reanalysis data with artificial noise.

Results. For recent decades the generalized least squares estimator mitigates most of the error associated with the use of a naive area weighted average. The improvement arises from the fact

that coverage bias in the historical temperature record does not arise from an absolute shortage of observations (at least for recent decades), but rather from spatial heterogeneity in the distribution of observations, with some regions being relatively undersampled and others oversampled. The estimator addresses this problem by reducing the weight of the oversampled regions, in contrast to some existing global temperature datasets which extrapolate temperatures into the unobserved regions. The results are almost identical to the use of kriging (Gaussian process interpolation) to impute missing data to global coverage, followed by an area weighted average of the resulting field. However, the new formulation allows direct diagnosis of the contribution of individual observations and sources of error.

Conclusions. More sophisticated solutions to the problem of missing data in global temperature estimation already exist. However the simple estimator presented here, and the error analysis that it enables, demonstrate why such solutions are necessary. The 2013 Fifth Assessment Report of the Intergovernmental Panel on Climate Change discussed a slowdown in warming for the period 1998–2012, quoting the trend in the HadCRUT4 historical temperature dataset from the United Kingdom Meteorological Office in collaboration with the Climatic Research Unit of the University of East Anglia, along with other records. Use of the new estimator for global mean surface temperature would have reduced the apparent slowdown in warming of the early 21st century by one third in the spatially incomplete HadCRUT4 product.

Key words: Climate change, historical temperature record, observational coverage.

1. Introduction

Global mean surface temperature change is a key metric in the quantification of global warming (Stocker *et al.*, 2013). Surface air temperature is significantly influenced by local and seasonal factors, such as altitude, exposure and surface type, so the metric is usually expressed in the form of a global mean surface temperature anomaly, which is the areal average of the temperature deviation from an average over some reference period of the temperatures for that location and month of the year (Jones *et al.*, 1999). The global mean surface temperature anomaly is then defined as the areal average of these local temperature anomalies over the whole of the surface of the planet (Equation 1), where T_{gl} is the global mean surface temperature anomaly for a given month, $T(\lambda, \phi)$ is the anomaly at a given latitude λ and longitude ϕ and A is the area element.

$$T_{\text{gl}} = \frac{\iint T(\lambda, \phi) dA}{\iint dA} \quad (1)$$

For numerical purposes, temperature fields are commonly represented on a grid, most frequently a rectangular array on the latitude and longitude coordinates, although sometimes equal area grids, which feature fewer cells per latitude band at higher latitudes, are used. When we have complete data (i.e. no missing grid cells), the global mean surface temperature anomaly can be calculated from the gridded temperature anomalies under the assumption that the grid cells are small enough to accurately represent the spatial variation in the surface temperature anomaly (or that the grid cell values are themselves representative of the average temperature in the region spanned by the grid cell). The global mean is given by Equation 2, where T_i is the temperature in a given grid cell and a_i is the area of the grid cell denoted by the index i :

$$T_{\text{gl}} \approx \frac{\sum_i a_i T_i}{\sum_i a_i} = \mathbf{w}_{\text{gl}}^T \mathbf{T} \quad (2)$$

where \mathbf{w}_{gl} is the vector of normalized weights $a_i/\sum_i a_i$, and \mathbf{T} is the vector of temperatures T_i .

However, observational data typically do not have global coverage, i.e. there are grid cells for which the measurements are missing. In the simple case where all the grid cells are uncorrelated, we could view the partial coverage as a random sample from a population. Then the best estimator of the global mean would be the sample mean (i.e. the

mean of the available grid cells weighted by the cell areas), and this will be an unbiased estimator of the global mean surface temperature anomaly.

In practice, the observations (or more strictly the deviations from the global mean) are spatially correlated (Vinnikov *et al.*, 1990), which complicates matters. It is useful here to introduce terminology from the statistics literature (Little and Rubin, 2002; Graham, 2009), where a distinction is made between data that are missing completely at random (MCAR), missing at random (MAR) and missing not at random (MNAR). Missing data are MCAR if the missingness mechanism is independent of other information, in our case, if the probability a grid cell record is missing does not depend upon a cell's location or the temperature anomaly. The data are MAR if the missingness depends upon the covariates, but not the quantity of interest, i.e. the probability a cell record is missing can depend upon its latitude and longitude but not the temperature anomaly. MNAR data occur when the missing mechanism depends on the quantity of interest, for example, if a temperature observation was censored for being too high or low. Only MCAR data can be analysed using complete data techniques by simply ignoring the missing values. In particular, the use of the sample mean as an estimator for the global mean is contingent on the assumptions of ordinary least squares, namely that observations are a random sample from the population and that the errors are uncorrelated, or in other words that the missing data are MCAR. When applied to MAR and MNAR data, the sample mean can lead to biased estimates. For the temperature data, missingness is strongly correlated with longitude and latitude, with, for example, data at high latitudes more likely to be missing. The observations are, therefore, at best missing *conditionally* at random (MAR), so that unless we control for the influence of longitude and latitude, statistical estimators based on the data will be biased. The observations could also be MNAR due to manual station selection or outlier rejection; however, the resulting biases would not be detectable or correctable without reference to a larger set of weather station data such as that of Rohde *et al.* (2013) or Rennie *et al.* (2014).

Historical temperature records based on gridded observations include the HadCRUT4 record from the UK Meteorological Office and University of East Anglia (Morice *et al.*, 2012) and the weather station contribution to the Japan Meteorological Agency record (Japan Meteorological Agency, 2017); however, in both cases, the global mean is determined from the mean of the grid cells for which values are available (with an additional step to equalize the weight of the hemispheres in the case of Morice *et al.*). More sophisticated methods developed for dealing with missing temperature data assume a MAR mechanism, and then try to compensate for the missing data either by using a more sophisticated estimator for the global mean or by imputing the missing data before using complete data techniques. For example, the variance-covariance matrix of observations is used directly in the optimal estimation of global mean surface temperature by Kagan (1979, 1997) and has also been employed by Vinnikov *et al.* (1990), Gandin (1993), Smith *et al.* (1994) and Weber and Madden (1995). In contrast, Hansen *et al.* (2010), Vose *et al.* (2012), Rohde *et al.* (2013) and Cowtan and Way (2014) use interpolation methods to reconstruct temperature estimates for the unobserved regions, although in the case of Vose *et al.*, polar regions are not interpolated. Even in interpolated records, coverage is typically incomplete prior to the mid-20th century because many interpolation techniques only infill within a specified distance of the available observational constraint, and that constraint is very sparse prior to the beginning of the 20th century.

Reconstruction of the global temperature field based on empirical orthogonal functions (EOFs) is an alternative approach which introduces empirical information about the underlying physical processes through the identification of common spatial patterns of temperature variation in the historical data (Shen *et al.*, 1994; Kaplan *et al.*, 1997; Folland *et al.*, 2001). However, EOF-based methods are either limited to reconstructing temperatures in regions for which observations are available for at least part of the record or must use and become contingent on reanalyses or climate models to infer global patterns. While this may lead to superior temperature reconstructions when teleconnections are correctly diagnosed, it carries additional costs in terms of complexity and reproducibility when compared to optimal averaging and may lead to worse results if the reanalysis or model behaviour differs substantively from reality.

Why is optimal averaging not used in the historical temperature record products? Optimal averaging brings a cost in terms of complexity. Complex methods are harder to debug, harder to maintain, harder for other researchers to reproduce and less transparent to users of the data. In the absence of evidence that a simple statistic is inadequate for a particular purpose, there are, therefore, good reasons to favour a simple statistic over a complex one, subject to the simple statistic being a sufficiently good estimator to support the conclusions drawn from it.

The early part of the 21st century provides evidence that the simple area average of the observed regions may lead to incorrect conclusions. In the context of an evaluation of climate models, the IPCC Fifth Assessment Report (Flato *et al.*, 2013) discusses a 'hiatus' in warming for the period 1998–2012, quoting a trend of 0.04°C/decade in the HadCRUT4 record over that period. This hiatus has been the subject of numerous research papers (Medhaug *et al.*,

2017), many of which overlooked the already documented contribution of incomplete spatial coverage. Hansen *et al.* (2006) reported that limited coverage of the Arctic in the HadCRUT3 record led to differing conclusions concerning whether 2005 was the hottest year on record to that point. Vose *et al.* (2005) and Hansen *et al.* (2010) noted that most of the differences between HadCRUT3 and their own infilled record arose from differences in spatial coverage. Simmons *et al.* (2010) found evidence for the underestimation of temperature trends in the UKMO HadCRUT3 observational record in comparison to the ERA-interim reanalysis due to incomplete coverage. Cowtan and Way (2014) and Karl *et al.* (2015) found that infilling temperatures in the unobserved regions led to higher trends for the hiatus period, consistent with the ERA-interim reanalysis (Simmons *et al.*, 2017).

The aim of this work is to demonstrate an estimator for global mean surface temperature which better satisfies the competing criteria of simplicity and statistical validity. The goal is to identify the simplest function that yields a substantially better estimate than the area weighted mean of the observed cells, without interpolating temperatures into the unobserved regions. For the purposes of this analysis, grid cell values will be treated as observations, although in practice gridded values are the average of multiple measurements, with daily temperatures from one or more weather stations contributing to the monthly mean for the cell. The estimator for the global mean of the observations will be evaluated using reanalysis data with simulated errors. The historical precedents for the resulting method and the implications for the assessment of the hiatus will be examined.

2. Generalized Least Squares Averaging

Linear models are commonly used statistical models for describing trends in data. The models are expressed in terms of a linear trend and a random error:

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\epsilon} \quad (3)$$

where \mathbf{y} is the vector of observations ($\mathbf{y} = (y_1, \dots, y_n)^\top$), \mathbf{X} is a design matrix of covariates, $\boldsymbol{\beta}$ is an unknown parameter vector, and $\boldsymbol{\epsilon}$ a vector of random errors. If the random errors are uncorrelated and homoscedastic (i.e. $\text{Var}(\epsilon_i) = \sigma^2$ and $\text{Cov}(\epsilon_i, \epsilon_j) = 0$ if $i \neq j$), then we can use ordinary least squares to fit the model (estimate $\boldsymbol{\beta}$). If a single constant is fitted to the data (i.e. $y_i = \mu + \epsilon_i$), then the result is mathematically identical to the calculation of the arithmetic mean of the data (i.e., $\hat{\mu} = \bar{y}$). In this case, the arithmetic mean (\bar{y}) of the sample is an unbiased estimator of the population mean (μ).

However, temperature observations show significant correlation between observations which are geographically proximate (Vinnikov *et al.*, 1990). For linear models where the random errors are correlated or heteroscedastic, generalized least squares must be used instead of ordinary least squares to fit the model. If the variance-covariance matrix of the random errors is $\text{Var}(\boldsymbol{\epsilon}) = \mathbf{C}$, the generalized least squares estimate for the coefficients $\boldsymbol{\beta}$ is:

$$\boldsymbol{\beta} = (\mathbf{X}^\top \mathbf{C}^{-1} \mathbf{X})^{-1} \mathbf{X}^\top \mathbf{C}^{-1} \mathbf{y}. \quad (4)$$

For the simple analysis presented here, we will ignore measurement errors except for their role in reducing the correlation between nearby observations, which will be approximated through the functional form of \mathbf{C} as outlined below and in Section 3.

When calculating the global mean anomaly, there is a single constant predictor variable, so $\mathbf{X} = \mathbf{1}_n$, a column vector of ones of length n . To calculate an estimate of global mean surface temperature anomaly, the response variable becomes the vector of temperature anomalies for those grid cells for which values are available. Equation 4 then simplifies to:

$$\hat{T} = \frac{\sum_i \sum_j C_{ij}^{-1} y_j}{\sum_i \sum_j C_{ij}^{-1}} \quad (5)$$

where C_{ij}^{-1} is the i, j element of the matrix \mathbf{C}^{-1} .

The covariance matrix can be estimated from the observations for regions where observations are plentiful. Here for simplicity we take a different approach, and model the covariance between two temperature observations using a simple exponential function applied to the distance between the two grid cell centres d_{ij} , calculated assuming a spherical Earth of radius 6371 km. The covariance function can be replaced by a correlation (Equation 6), because the covariance appears in both the numerator and denominator of Equation 5 and so the scale factor cancels.

$$C_{ij} = \exp(-d_{ij}/d_0) \quad (6)$$

The range of the correlation is controlled by a single parameter, which is the *length-scale* or *e*-folding distance of the exponential, d_0 . The range parameter d_0 may be estimated from the *correlogram*, which is the correlation over time between every pair of cells in the temperature field as a function of distance between those cells. The value of d_0 is then determined which best fits the decline in correlation with distance.

The resulting temperature averaging method is fully specified by Equations 5 and 6 which contain a single adjustable parameter—the length-scale of the correlation function. The weights applied to each grid cell in the calculation of the global mean are a function of the coverage mask for that month, the length-scale parameter and nothing else. A necessary consequence of this simplicity is that factors like surface type, topography and internal modes of variability are ignored, so benchmarking will be required to assess the utility of the method.

The variance of the estimator \hat{T} can also be determined using the covariance matrix. From Equation 5, we can see that \hat{T} is a weighted average of the observed cells ($\hat{T} = \mathbf{w}_{\text{GLS}}^T \mathbf{y}$) with weights \mathbf{w}_{GLS} given by Equation 7, where $\mathbf{X} = \mathbf{1}_n$.

$$\mathbf{w}_{\text{GLS}}^T = (\mathbf{X}^T \mathbf{C}^{-1} \mathbf{X})^{-1} \mathbf{X}^T \mathbf{C}^{-1} \quad (7)$$

The true weights for an area weighted mean of spatially complete data are the vector of cell areas as a fraction of the area of the globe, \mathbf{w}_{gl} , from Equation 2. The error is the difference between the GLS weighted and true weighted means, which is equal to the difference in the weights multiplied by the spatially complete temperature field. If the true covariance matrix of the spatially complete observations is \mathbf{C}_t , the variance of the resulting error is, therefore, given by Equation 8, where \mathbf{w}_{GLS} is zero for missing observations.

$$\text{Var}(\hat{T}) = (\mathbf{w}_{\text{GLS}} - \mathbf{w}_{\text{gl}})^T \mathbf{C}_t (\mathbf{w}_{\text{GLS}} - \mathbf{w}_{\text{gl}}) \quad (8)$$

The scale of the covariance matrix is generally treated as unknown and estimated from the residuals of the GLS model by applying a correction factor $\sigma_{\text{GLS}}^2 = (\mathbf{y} - \hat{\mathbf{y}})^T \mathbf{C}^{-1} (\mathbf{y} - \hat{\mathbf{y}}) / N_{\text{df}}$, where N_{df} is the number of degrees of freedom—in this case, one less than the number of observations. If \mathbf{C}_s is an arbitrarily scaled estimate of the covariance matrix of the spatially complete observations, then the variance of \hat{T} is given by Equation 9.

$$\text{Var}(\hat{T}) = \sigma_{\text{GLS}}^2 (\mathbf{w}_{\text{GLS}} - \mathbf{w}_{\text{gl}})^T \mathbf{C}_s (\mathbf{w}_{\text{GLS}} - \mathbf{w}_{\text{gl}}) \quad (9)$$

This result is compared to the standard result for the uncertainty of a GLS estimator in the [Supplementary Data](#).

We describe the estimator \hat{T} as a Generalized Temperature Average with 1 parameter, abbreviated to GTA1 and parameterized by the length-scale in kilometers. A GTA1 temperature series using a 1000 km length-scale will be referred to by the symbol $T_{\text{GTA1}(1000)}$.

The GTA1 estimator is almost identical to infilling by ordinary kriging (Cowtan and Way, 2014) followed by calculating the area weighted mean of the resulting spatially complete field, however the intermediate step of determining the infilled field is omitted. The two approaches provide complementary insights: while kriging enables diagnosis of the spatial contributions to coverage bias (for example the contribution of rapid Arctic warming noted by Cowtan and Way), the GLS weights enable the contribution of individual grid cells to the global mean to be evaluated, providing insight into the interaction of different sources of error and how the GTA1 estimator improves over naive area weighting.

2.1. Relationship to Kagan (1979)

The generalized least squares average in Equation 5 is a simplification of the method described by Kagan (1979, 1997), Vinnikov *et al.* (1990), Smith *et al.* (1994) and Weber and Madden (1995). Kagan uses the covariance matrix of observations to optimally weight the observations; however, Kagan also allows for errors in the observations, different covariance functions for different latitude bands and variations in the covariance of the observations in any grid cell with the global mean. While the covariance function undoubtedly does vary with latitude at least (Vinnikov *et al.*, 1990), determining that variation increases the number of parameters and subjective parameter choices. Furthermore, the covariance matrix of the observations and covariances of the observations with the global mean must be determined in a self consistent manner, otherwise the resulting averaging method will not reduce to an areal average in the case of geographically complete data.

The complexity and dependence on non-observational sources may have contributed to the lack of adoption of the optimal averaging framework. We will, therefore, pursue the simpler form in Equation 5 and use synthetic, but nevertheless realistic, data to evaluate whether the resulting approximation provides a significant improvement over the simple averages employed currently. Equation 5 of this paper may be obtained from Equation 6 of Weber and Madden (1995) when the vector of covariances with the global mean (Ω) is a vector of ones, leading to $w = w' = w''$ in Equation 13 of Weber and Madden, or corresponding equations in Kagan (1979).

3. Implementation and testing

The GTA1 estimator has been implemented in the Python and R programming languages as a pair of functions implementing Equations 5 and 6. The first function uses Equation 6 to calculate the correlation matrix for the globally complete grid. For each month in the record, the second function extracts a subset of the correlation matrix corresponding to a given coverage mask, and Equation 5 is used to calculate the mean of the temperature field for that month. Each step requires no more than 10 lines of computer code. Minimal implementations in the Python and R computer languages are given in the Supplementary Data. The costliest part of the calculation is inverting the correlation matrix. This is performed using the Python ‘Numpy’ library (Dubois *et al.*, 1996), which uses the Moore-Penrose implementation in the LAPACK library (Anderson *et al.*, 1999). The calculation is practical on a modern desktop computer (e.g. with 8 GB of RAM) for data sampled on grids as fine as 2 degrees: for more finely sampled data, additional memory or regridding will be required. For faster results, it is possible to solve the GLS equations rather than inverting the correlation matrix.

The correlation between grid cell values as a function of distance was determined by the following steps: Monthly gridded temperature anomalies were used for grid cells and months of the year where at least 10 values are available over the period 1981–2010. The values were detrended to remove any climate signal and normalized to zero mean and unit variance, giving a detrended anomaly for each grid cell and month of the year. Squared differences between cells were then accumulated as a function of the distance between the cells. The resulting function is well described by an exponential function with only a single parameter—the length-scale (Fig. 1). A preliminary value for the length-scale d_0 in Equation 6 was determined by least squares optimization to fit the predicted to the observed correlation for pairs of observations within 4000 km, giving a best estimate for d_0 of ≈ 1000 km. However, the range over which temperatures are correlated varies with latitude (Vinnikov *et al.*, 1990; Rohde *et al.*, 2013) as well as surface type and topography, so the optimum length-scale for averaging a *specific* temperature field can vary depending on the distribution of unobserved cells and will be determined later by simulation.

The correlation between observations is influenced both by the distance between the observations and by the noise in the individual observations. To isolate the effect of noise, correlograms were also determined for surface temperature fields from the MERRA2 reanalysis (Gelaro *et al.*, 2017), a recently developed atmospheric reanalysis spanning 1980 to the present. Figure 1 also shows how correlation changes with distance for the MERRA2 reanalysis data with

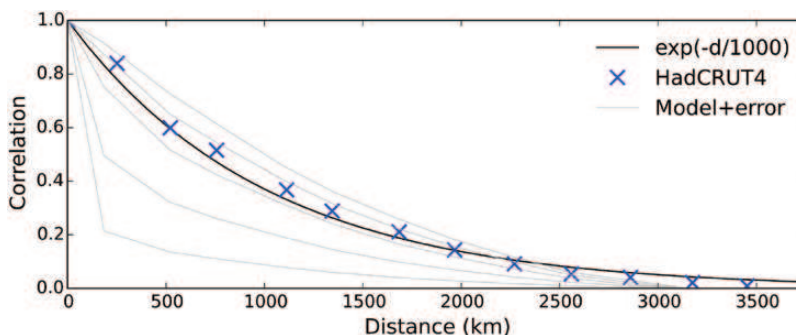


Figure 1. Correlation as a function of distance estimated from pairwise comparison of cells from the HadCRUT4 blended land/ocean data. Crosses indicate binned averages. The thick line is the least squares fit of an exponential function against every individual cell difference. Thin lines show the correlation with distance for the MERRA2 reanalysis with spatially constant geographical noise of 0.25°C (top line), 0.5°C, 1.0°C, 2.0°C and 5.0°C (bottom line).

different amounts of geographically constant noise. When the noise signal is small, the correlogram has a bell curve shape. Increasing noise scales the correlations for all distances greater than zero, and so the fit to the exponential model is somewhat contingent on the magnitude of the noise contribution. The observed correlogram falls between the reanalysis correlograms for a noise contribution of between 0.5°C and 1.0°C, consistent with estimates from [Morice *et al.* \(2012\)](#) for the size of this term in real world data.

The GTA1 method includes several simplifications which might impact the efficiency of the estimator. The method will, therefore, be tested by reconstructing temperature fields from incomplete and noisy data where the correct answer is known. The MERRA2 reanalysis was used for this purpose; however, the ERA-interim reanalysis ([Dee *et al.*, 2011](#)), which shows faster Arctic warming over recent years ([Simmons and Poli, 2015](#); [Simmons *et al.*, 2017](#)), leads to similar conclusions.

The validation method follows a similar approach to that used in the estimation of coverage uncertainty in the HadCRUT family of temperature products ([Jones *et al.*, 1997](#); [Brohan *et al.*, 2006](#); [Morice *et al.*, 2012](#)):

- The reanalysis 2m air temperature is converted to an air temperature anomaly using a 30-year baseline period and converted to the same grid as the observational record.
- A 'true' global mean surface temperature anomaly is calculated from the spatially complete reanalysis field.
- Coverage is reduced to match a month from the observational record, and random noise is added to each grid cell in the reanalysis field. A global mean surface temperature estimate is then constructed from the coverage reduced noisy data using the estimator to be tested. The root-mean-square (RMS) error between the estimate and the true value, evaluated using multiple months of data from the reanalysis, is used to evaluate the estimator.

Each month in the observational record produces a coverage mask. This mask is used in conjunction with the corresponding month from every year in the reanalysis to produce an error estimate for a given estimator. For example, for the observational coverage from January 1940, the reanalysis fields for the 37 Januaries between 1980 and 2016 are used in estimating the errors. This assumes that the spatial scale of variability is invariant under transient climate change; this assumption will be tested later using a longer reanalysis.

The validation method is contingent on the use of realistic estimates of the noise to be added to each grid cell in the reanalysis data. While the HadCRUT4 dataset provides uncertainty estimates for each individual grid cell ([Morice *et al.*, 2012](#)), these estimates do not include contributions from temporally and spatially correlated biases in the land and sea surface temperature observations, which are instead provided through an ensemble of reconstructions and covariance matrices ([Kennedy *et al.*, 2011](#); [Morice *et al.*, 2012](#)).

An independent estimate for the cell noise including all of the relevant contributions was, therefore, determined from the temperature data themselves. A 3 × 3 block of grid cells was omitted from the map, and the value for the centre cell of the omitted region restored by kriging using the method of [Cowtan and Way \(2014\)](#). The error in the cell value was then estimated from the difference between the observed and reconstructed values. The calculation was repeated for each cell in turn. The RMS error for a given cell was then estimated from the RMS of the errors (over time) in that cell, for those cells with at least 60 months of differences over the period 1981–2010.

The errors in isolated Antarctic observations are overestimated because there are no nearby stations, and the noise estimate, therefore, contains a significant contribution from the geographical differences between stations. The maximum value for the cell noise was, therefore, capped at the 99th percentile of the values obtained over the whole map, with the result that the inland Antarctic cells were given a similar error to cells in the Arctic. The resulting noise map is shown in [Figure 2](#). For cells where insufficient data were available to estimate the error, RMS error values were extrapolated by kriging.

The noise estimates show a similar spatial pattern to uncorrelated error estimates from [Morice *et al.* \(2012\)](#) for both land and ocean data but are about 50% larger in size: this reflects the facts that some of the error sources identified by [Morice *et al.*](#) are not included in the comparison, and that our estimates are inflated by interpolation error. Noise will be larger for earlier periods because there are often fewer observations per grid cell; however, when identifying climatic contributions to coverage, bias annual and decadal error estimates are more relevant than the monthly estimates used here. On this basis, the noise estimates are likely to be conservative for recent decades but may be underestimated for the early record. Our noise estimates do not include the effects of long range spatial correlated biases which are represented in the HadCRUT4 by an ensemble of temperature realizations, because while these

contribute to the total uncertainty in the global mean temperature anomaly, they have comparatively little impact on the contribution of incomplete coverage to that uncertainty.

The noise map was used to add uncorrelated noise series to each cell in the reanalysis data from a normal distribution with mean of zero and standard deviation equal to the estimated RMS error for that cell. This does not account for the partial correlation of the errors in the sea surface temperature data, which may lead to the impact of noise in the data being slightly underestimated.

To determine the optimum value of the length-scale d_0 , the errors in the GTA1 estimator were evaluated for length-scales in the range 500–1500 km. The RMS error in the GTA1 estimate as a function of length-scale is shown in Figure 3. The results from reconstructing the reanalysis data support a value of between 800 and 900 km for d_0 , similar to but slightly lower than the value determined from the observations.

The GTA1 method was then tested to ensure that the weighting of the data reduces to simple area weighting (i.e. Equation 2) in the case where the temperature field is spatially complete. The weights given to grid cells as a function of latitude are in good agreement between the two methods (Fig. 4). This result holds for values of the length-scale d_0 which are similar to or greater than the cell spacing; values of d_0 which are significantly less than the cell spacing lead to cell weights which diverge from the cell areas, approaching uniform (i.e. non-area) weighting as d_0 tends to zero. The equivalence to area weighting is also contingent on the use of the correlation matrix rather than the covariance matrix in Equation 5, otherwise regions with noisier observations are systematically downweighted.

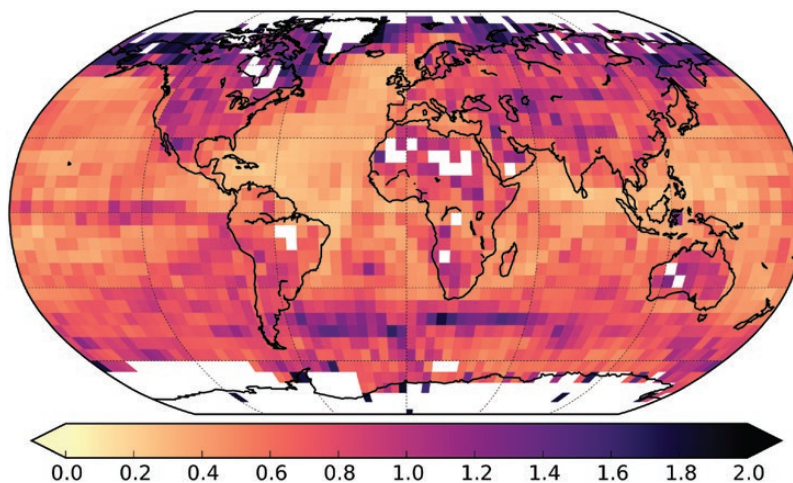


Figure 2. RMS error in degree Celsius in the HadCRUT4 data estimated from the difference between the value of a cell and a value inferred from nearby (but non-neighbouring) cells by kriging. Data are for the period 1981–2010.

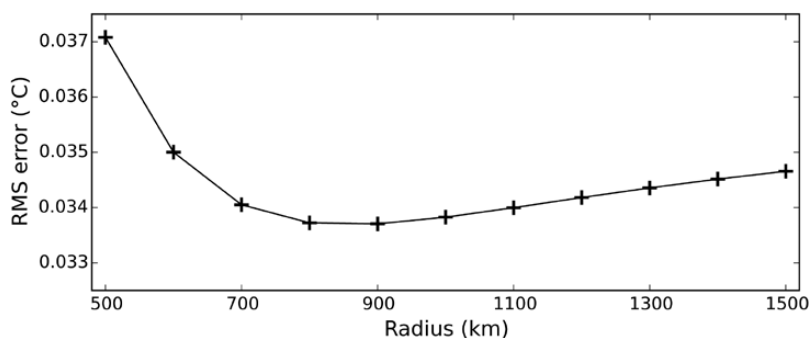


Figure 3. RMS error in global mean surface temperature estimates as a function of length-scale d_0 for the GTA1 estimator. The error is evaluated by reducing the coverage of every year of the MERRA2 reanalysis data to match the coverage of the HadCRUT4 observations for the years 1981–2010.

4. Results

Four estimators were evaluated on the basis of their skill in reconstructing the global mean of the MERRA2 fields from the noise-added data using historical coverage masks:

1. The global mean of the observed cells, which is the method used in combination with different levels of infilling by [Vose et al. \(2012\)](#), [Hansen et al. \(2010\)](#) and [Japan Meteorological Agency \(2017\)](#).
2. The mean of the hemispheric means of the observed cells, which is the method used by [Morice et al. \(2012\)](#).
3. The mean of the zonal means, which has been used for radiosonde data by [Thorne et al. \(2005\)](#) and for surface temperature data by [Gleisner et al. \(2015\)](#) under the assumption that temperature anomalies are primarily correlated with other temperature anomalies at the same latitude.
4. The generalized least squares estimator GTA1 described by Equations 5 and 6, with the length-scale d_0 set to 800 km.

The RMS errors for the four different global mean estimators are plotted for the coverage of each month in the HadCRUT4 record in [Figure 5](#). The global mean of the observed cells and the mean of the hemispheric means lead to very similar RMS errors, with the mean of the hemispheric means performing slightly better during the mid-20th century but worse during the 19th century. The mean of the zonal means performs substantially better than the global

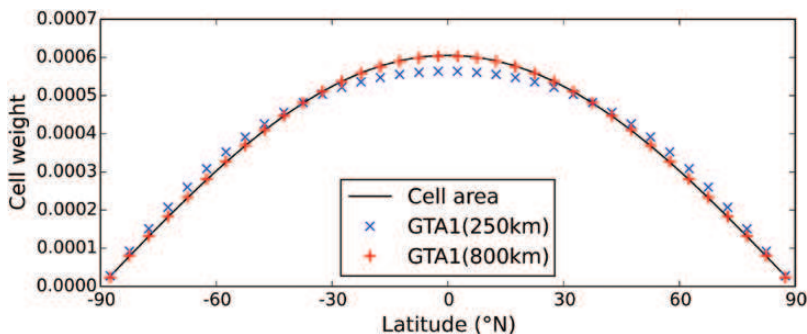


Figure 4. Weights given to grid cells as a function of latitude in the case of a spatially complete field by a simple weighted average based on cell area, and by the GTA1 estimator with e -folding radius d_0 of 250 or 800 km.

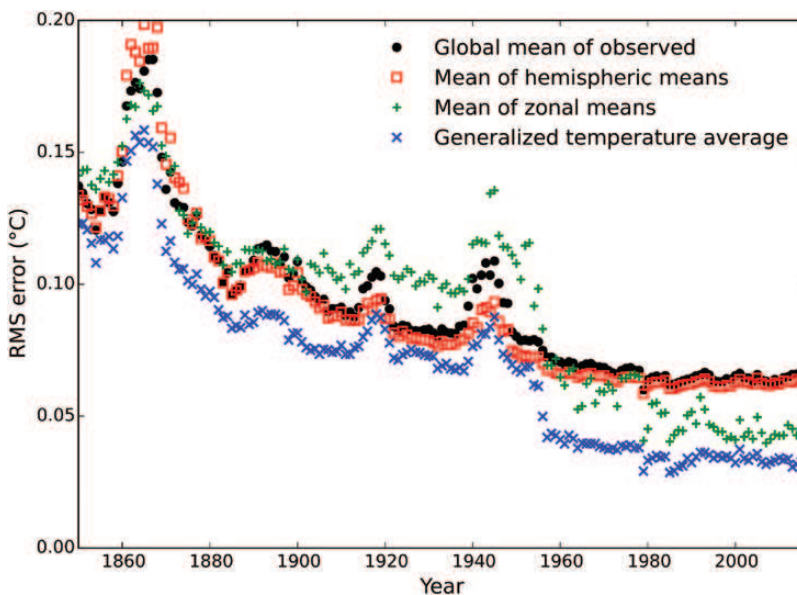


Figure 5. RMS error in global mean surface temperature estimates as a function of coverage. The four estimators are compared on the basis of the error in reconstructing coverage reduced MERRA2 data, where coverage is determined by each of 12 months of a given year in the HadCRUT4 data.

or hemispheric means for the period since 1950; however, it performs worse than these methods prior to that date. The GTA1 estimator performs better than all the other estimators over the whole of the record, and in particular leads to RMS errors which are about half of the error from the global or hemispheric means for recent years. Since errors combine as variances, this implies that use of the GTA1 estimator mitigates three quarters of the error variance from sampling and measurement errors in the global or hemispheric means.

The difference between the generalized least squares average and the simple area weighted average may be understood by examining the weights given under the GTA1 approach to different cells, illustrated using the data from January 1920 of the CRUTEM4 land temperature dataset (Jones *et al.*, 2012), normalized such that the largest weight is equal to one (Fig. 6). Isolated observations are given unit weight. Isolated pairs of adjacent observations are given just over half weight. Densely sampled observations are further downweighted inversely with the density of observations, to produce an effective area weighting.

The weighting scheme serves to minimize the combined effect of sample noise (arising from there being insufficient observations) and sample bias (arising from some areas of the planet being over-represented)—the latter will be referred to as coverage error. When observations are sparse, all observations are given equal weight to minimize the impact of the error in any individual observation (i.e. assuming homoscedasticity). When observations are plentiful, observations are weighted in inverse proportion to the density of observations to avoid the over-representation of densely sampled regions. The large reduction in error after 1950 (Fig. 5) shows that coverage error is the dominant problem post-1950, and therefore downweighting the densely sampled regions leads to a better estimate of global mean temperature. This benefit is realized despite the fact that the errors are in reality heteroscedastic (Morice *et al.*, 2012).

A theoretical estimate of the expected coverage error can be obtained from Equation 9. However, this estimate does not include the contribution of sample noise arising from errors in the observations, which is present even when coverage is complete and so $\text{Var}(\hat{T})$ is zero. The contribution of sample noise to the error in \hat{T} can be estimated using Equation 10 from the cell weights w_{GLS} and the diagonal matrix Σ whose diagonal elements are the estimated noise variances for each grid cell, determined empirically from the observations as described in Section 3 (Kagan, 1997, equation 3.1.5).

$$\text{Var}_{\text{noise}}(\hat{T}) = w_{\text{GLS}}^T \Sigma w_{\text{GLS}} \quad (10)$$

The total error variance of the GTA1 estimator should be given by the sum of $\text{Var}(\hat{T})$ and $\text{Var}_{\text{noise}}(\hat{T})$. This estimate of the uncertainty in the GTA1 estimator, along with the contributory terms, is compared to the empirical RMS error in Figure 7a. The theoretical estimate of the uncertainty in the estimator agrees well with the empirical values for the period from the late 1950s when Antarctic observations are available, but underestimates the uncertainty for the earlier periods, which suggests that the correlation model is too simple to produce optimal results for the early part of the record.

The correlation matrix C can be converted into a covariance matrix by multiplying each row and column by the standard deviations of the temperature anomalies for the corresponding grid cells. However, if the covariance matrix is used in Equation 5, the resulting weights do not tend towards the cell areas as coverage improves. Correct determination of the weights from the covariance matrix requires the more complex normalization procedure of

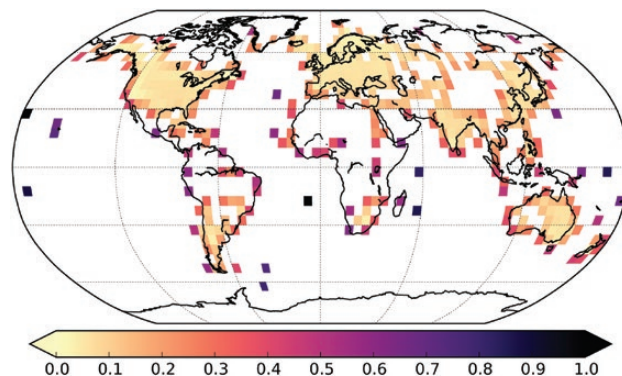


Figure 6. Weights given under the GTA1 approach to each grid cell for a map with the coverage of the CRUTEM4 data in January 1920, scaled such that the greatest weight is equal to 1. The weights are dimensionless.

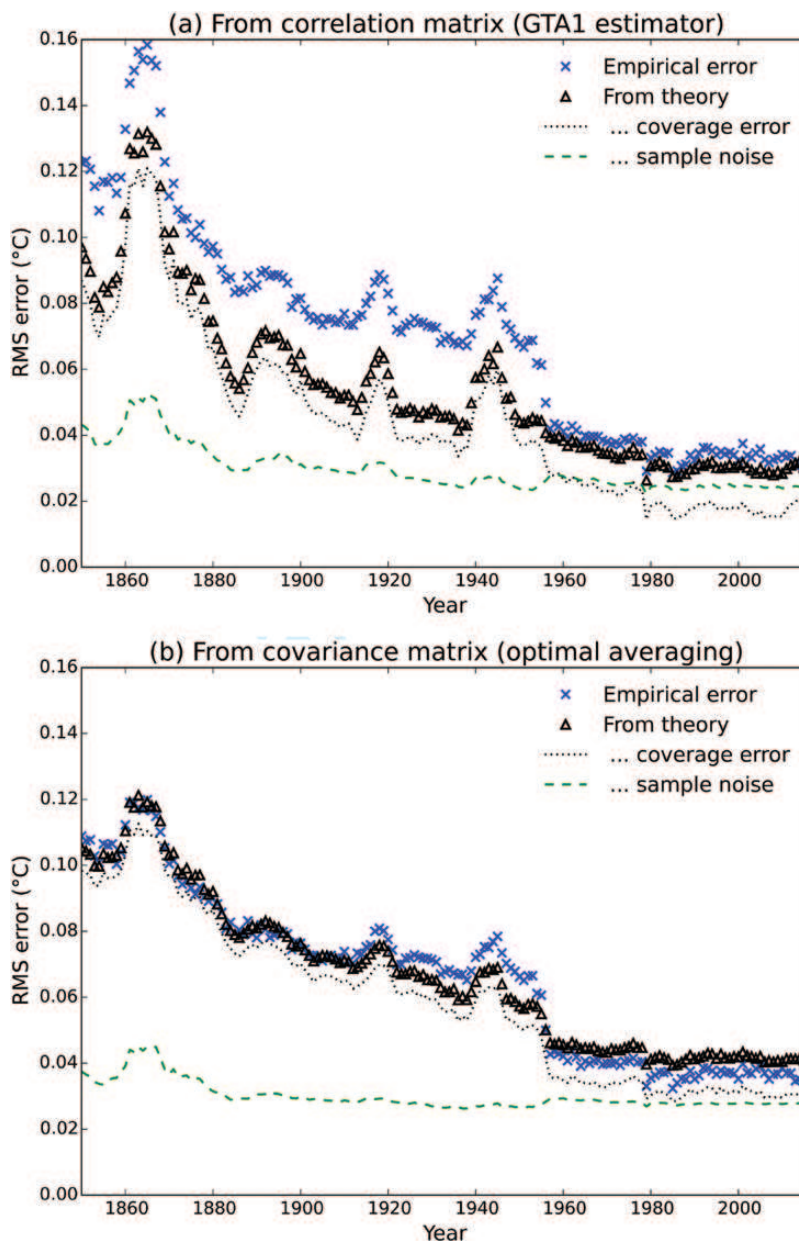


Figure 7. Comparison of the theoretical and empirical estimates of RMS error in the temperature estimates as a function of coverage. (a) Error contributions using the GTA1 estimator; (b) error contributions using the covariance matrix instead of the correlation matrix, with the appropriate normalization. The empirical estimate from Figure 5 is compared to the theoretical estimate from the sum in quadrature of Equations 9 and 10. The individual contributions of the coverage error and sample noise terms are also shown.

Kagan (1997, equation 3.3.7) or Weber and Madden (1995, equation 13) (the additional normalization has no effect if applied to the correlation matrix). Figure 7b shows the theoretical and empirical uncertainties estimates obtained when using the covariance matrix, which now show good agreement over the whole period. While performance of the correlation and covariance calculations is similar for recent decades, use of the covariance matrix noticeably reduces the errors in the early period. If coverage is poor and complexity is not an issue, the full optimal averaging method of Kagan should, therefore, be used in preference to the simpler GTA1 estimator.

The same approach can be used to analyse the errors for the other estimators by substituting the effective cell weights for that estimator in place of wGLS. The coverage error and sample noise for the global mean of the observed cells and the GTA1 estimator are shown in Figure 8. The GTA1 estimator reduces the coverage error compared to the global mean of the observed cells at a cost of increasing the sample noise. The coverage error is the dominant source of error for the global mean of the observed cells for the whole of the record, and so this provides a net reduction in the error of the estimator. Sample noise is minimized by using equal weights (or when allowing for heteroscedasticity by weighting according to the inverse variance for that grid cell), to avoid inflating the noise contribution of any individual observation. Coverage error is minimized by weighting the data to reflect the true population. The improved performance of the GTA1 estimator over the global mean of the observed cells arises from a better compromise between these two sources of error.

In contrast to Kagan (1979), the noise contribution of individual cell values to the global mean is not handled explicitly in the GTA1 estimator, rather the global scale of the noise contribution is handled through the length-scale of the correlogram d_0 , although the fit of the exponential model becomes poorer with lower or higher noise levels than those in the HadCRUT4 observations (Fig. 1). In the absence of noise, inclusion of an isolated cell observation reduces the uncertainty in the resulting global mean in proportion to the area of the planet for which that observation is informative, which is controlled by the length-scale. Since uncertainties sum in quadrature, they are dominated by the larger source of error, thus when the noise is less than the bias which is mitigated by including that cell, the cell noise has little effect on the correlogram. If the cell noise exceeds the bias mitigated by including that cell, the optimal range for the correlogram drops rapidly, with the effect that multiple observed cells are required to provide an informative temperature estimate for the same area.

4.1. Contributions to coverage uncertainty

Coverage uncertainty in a global mean temperature estimate from spatially incomplete data arises from two sources: changes in the temperature of the unobserved region relative to the observed region and changes in coverage. Let T_{gl} be the true global mean surface temperature, T_{obs} be the mean temperature of the observed region, T_{unobs} be the mean temperature of the unobserved region and f_{unobs} be the fraction of the surface which is unobserved, then:

$$T_{gl} = T_{obs}(1-f_{unobs}) + T_{unobs}f_{unobs}. \quad (11)$$

If the mean temperature is estimated from the average of the observed region alone, the error in the resulting estimate will be $\epsilon = T_{obs} - T_{gl}$. Let the difference between the means of the unobserved and observed regions be $D_{unobs} = T_{obs} - T_{unobs}$, then:

$$\epsilon = D_{unobs}f_{unobs}. \quad (12)$$

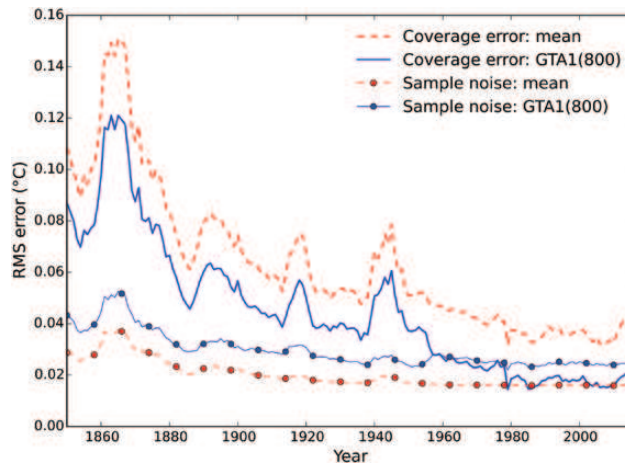


Figure 8. Comparison of the coverage error and sample noise contributions for both the global mean of the observed cells and the GTA1 estimators.

When using temperature anomalies, the absolute value of the bias is irrelevant; however, changes in bias over time will lead to an error in temperature trends spanning the change in bias. The change in bias obeys a product rule:

$$\delta\epsilon \approx D_{unobs}\delta f_{unobs} + f_{unobs}\delta D_{unobs}. \quad (13)$$

Therefore, a change in coverage bias may arise from a change in the difference between the temperatures of observed and unobserved regions, or from a change in coverage subject to D_{unobs} being non-zero.

Changes in D_{unobs} may be noise-like, for example due to weather systems moving into or out of the unobserved region, or bias-like, for example due to relative changes in climate between the observed and unobserved regions relative to the baseline period. The rapid warming of the incompletely observed Arctic is an example of the latter (Cowtan and Way, 2014), although decadal scale regional climate change due to internal variability has been shown to occur elsewhere as well (Xie *et al.*, 2015).

To separate the effects of changes in climate and changes in coverage, additional validation tests were performed in which the coverage for a given month was used to calculate the error due to limited coverage in a historical reanalysis temperature field for the corresponding month only. The ERA 20th Century Reanalysis (ERA20C) was used for this experiment (Poli *et al.*, 2013) and provides a spatially complete temperature field covering the period 1900–2010. The reanalysis is based on temperature, pressure and wind observations from the oceans, and pressure and wind observations from land weather stations. However, for unsampled regions (such as Antarctica in the early 20th century), the reanalysis temperatures are determined solely by the atmospheric model and boundary conditions and may also be impacted by observational biases. No noise was added to ERA20C reanalysis data.

Figure 9 shows the decadal distributions of monthly temperature errors using either the global mean of the observed cells or the GTA1 estimator to reconstruct the mean of the ERA20C temperature field using the observational coverage from the years 1860, 1910, 1960 and 2010 for the corresponding month. With 1860 coverage, the range of errors is large for both the global mean and GTA1 estimators. With 1910 coverage, the GTA1 estimator tends to reduce the decadal bias and provides a slight reduction in the spread of the errors (in particular the outliers). With 1960 coverage, bias is substantially reduced and the spread of the errors reduced. With 2010 coverage, bias is almost eliminated and the spread of the errors substantially reduced.

Bias is expected to be lower during the 1961–90 baseline period because D_{unobs} should be close to zero, but in practice only the 1970s temperature estimates show little bias when using the global mean estimator. The spread in the errors due to the weather contribution to coverage error is large compared to the persistent climatic contribution; however, there is a centennial trend from a warm to a cool bias in the global mean estimator for all coverages, and in the GTA1 estimator for 1860 and 1910 coverage due to the faster warming of the unobserved regions (Simmons *et al.*, 2010). The global mean consistently underestimates the warming in the reanalysis data for any historical coverage. The GTA1 estimator provides a good estimate of the rate of warming for 1960 or 2010 coverage but underestimates the rate of warming when limited to 1860 or 1910 coverage.

Figure 10 shows the same experiment but using the historical coverage for the corresponding month as the basis for temperature reconstruction. For the period since the 1950s, bias is near zero and noise is dramatically reduced by the GTA1 estimator. For earlier decades, the GTA1 estimator provides a modest reduction in bias but little reduction in noise. The bias tends to be undercorrected suggesting that the GTA1 estimator is conservative with respect to the magnitude of the bias correction.

Changes in bias when using fixed coverage (Fig. 9) arise from changes in temperature anomaly in the unobserved region relative to the observed region, while the changes in bias when using historical coverage include the additional contribution from changes in coverage. The most notable change in the 1950s is the establishment of the Antarctic weather stations. The GTA1 estimator leads to consistently low noise and bias with 2010 coverage; however, it does not significantly reduce noise and only mitigates some bias with pre-1950 coverage. The actual bias estimates are, however, contingent on the reanalysis producing realistic temperatures in regions where no weather station observations are present.

4. 2. Impact of temperature estimators on the global warming ‘hiatus’

Numerous research papers have discussed a possible ‘hiatus’ in global warming at the start of the 21st century (Lewandowsky *et al.*, 2015; Medhaug *et al.*, 2017). The IPCC Fifth Assessment Report noted a trend in the HadCRUT4 temperature record of 0.04°C/decade for the period 1998–2012 (Hartmann *et al.*, 2013). This trend is substantially

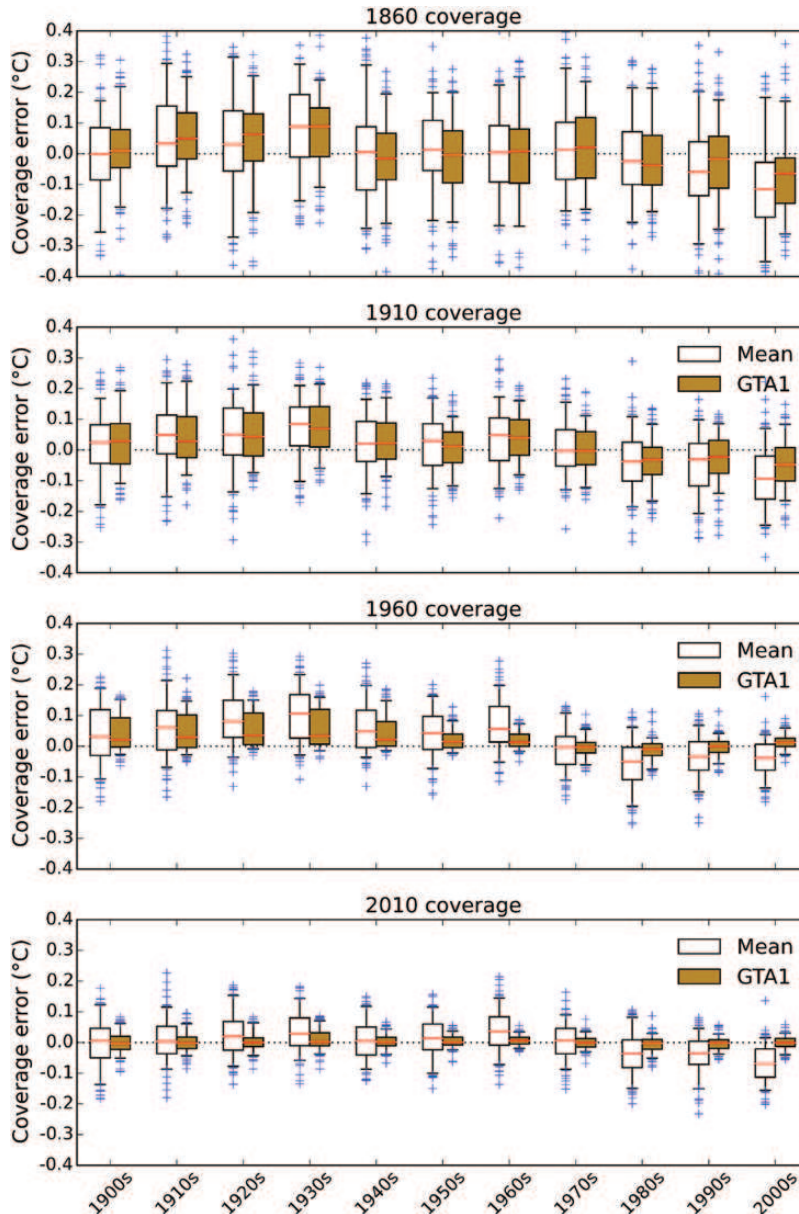


Figure 9. Error in the global mean of the observed cells and the GTA1 estimators of global mean surface temperature, grouped by decade when reconstructing months of the ERA20C reanalysis data reconstructed. Boxes show the interquartile range and whiskers the 5–95% range of errors for individual months in the decade. The line bisecting each box is the median, which provides an estimate of the decadal bias. The four panels show reconstructions using the HadCRUT4 observational coverage for the years 1860, 1910, 1960 and 2010.

below the 32-year trend of about $0.17^{\circ}\text{C}/\text{decade}$ (Foster and Rahmstorf, 2011) after removal of El Niño and other effects. Infilled temperature records from NASA and NOAA showed trends which were only slightly higher; however, these records did not at the time correct for a known bias due to the transition from ship to buoy measurements of sea surface temperature (Smith *et al.*, 2008; Kennedy *et al.*, 2011). The trend over the hiatus period is also influenced by a residual uncorrected bias in the ship data (Huang *et al.*, 2015; Hausfather *et al.*, 2017), and a trend from El Niño to La Niña conditions over the period.

Temperature trends for HadCRUT4 version 4.1.1, which was the current version at the time of preparation of Hartmann *et al.*, and for the now current version 4.6.0, were determined using the four estimators outlined earlier to determine the sensitivity of the trend to the temperature averaging method. The results are shown in Table 1.

The global mean of the observed cells and the mean of the hemispheric means both produce values consistent with Hartmann *et al.* (2013). The generalized least squares (GTA1) method produces a trend which is more than twice that of HadCRUT4.1.1 over the same period, while the mean of the zonal means method of Gleisner *et al.* (2015) produces an intermediate trend which is still closer to the GTA1 value. The use of the GTA1 method accounts for more than a third of the difference in trend between the hiatus period and the 32-year trend from Foster and Rahmstorf (2011). This increase in warming over the supposed hiatus period is also observed in records which use infilling to improve coverage (Cowtan and Way, 2014; Karl *et al.*, 2015).

5. Discussion

Historical temperature record products are utilized for multiple purposes, sometimes with conflicting requirements. Gridded temperature data are used to evaluate the performance of climate models and to identify spatial signatures associated with different climatic influences. The gridded data are also summarized by a global mean surface temperature estimate which may be used to quantify change in global climate for public and policy purposes, and to estimate climate sensitivity in simple energy balance calculations (e.g. Otto *et al.*, 2013).

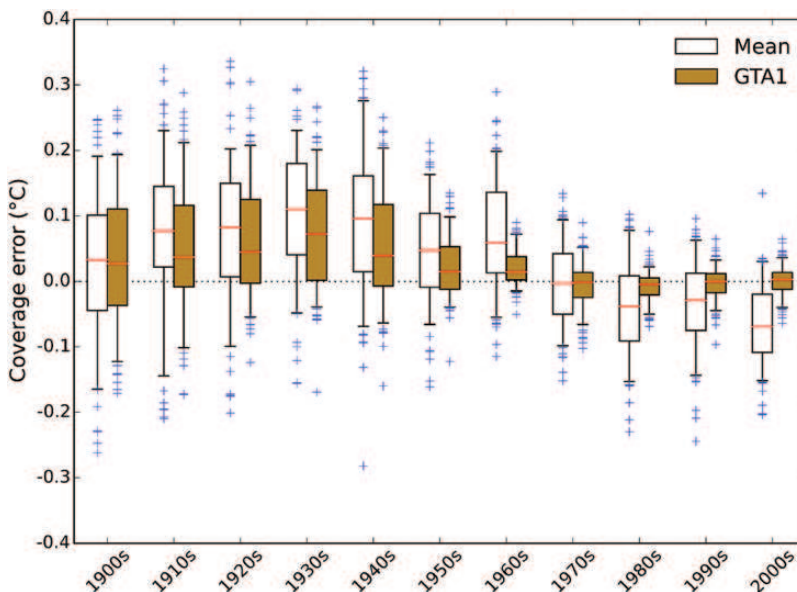


Figure 10. Error in the global mean of the observed cells and the GTA1 estimators of global mean surface temperature, grouped by decade when reconstructing months of the ERA20C reanalysis data reconstructed using the HadCRUT4 observational coverage from the corresponding year of the observational record.

Table 1. Temperature trends in degree Celsius per decade for the period 1998–2012 (Hartmann *et al.*, 2013) using the four different estimators of global mean surface temperature

Method	HadCRUT4.1.1	HadCRUT4.6.0
Global mean of observed cells	0.040	0.054
Mean of hemispheric means	0.040	0.052
Mean of zonal means	0.074	0.086
GTA1(800)	0.088	0.098

Trends are given for the HadCRUT4.1.1 data, which were current at the time of Hartmann *et al.*, and for the most recent version.

The HadCRUT4 record provides a monthly record of gridded temperature observations, with each observation contributing to only a single map grid cell. The Japan Meteorological Agency record (Japan Meteorological Agency, 2017) adopts a similar approach for land-based weather stations. In contrast, records from Hansen *et al.* (2010), Rohde *et al.* (2013) and Cowtan and Way (2014) use infilling to produce a temperature field with near global coverage, which may be averaged by conventional methods. The errors in the resulting averages are contingent on the effectiveness of the infilling method.

The non-infilled temperature products have an important benefit for the evaluation of climate models. The gridded temperature record can be compared to the climate model outputs after reducing coverage to match the observational record. The benefit of using a non-infilled product in this case is that differences between the models and observations must arise from either the models or the observations. By contrast when using an infilled record, differences may arise from the models, the observations or from artefacts of the infilling method.

The simplicity of the gridded observational record leads to a product which is easier for temperature record users to understand, and if necessary to reproduce. Simple methods are easier to debug and maintain, which is important for products which must be maintained over many years by changing personnel. There are, therefore, multiple reasons to maintain non-infilled gridded observational records. A simple average of the resulting gridded data, however, can produce misleading results, with the temperature trends during the hiatus period being a notable example.

We have proposed a less biased estimator for determining the global mean surface temperature from spatially incomplete observations. For recent years, this estimator mitigates the larger part of the error associated with the use of the naive area weighted mean. The estimator is almost identical to the use of kriging to infill to global coverage and then averaging the resulting field; however, it is simpler to implement and analyse. Implementation requires around 20 lines of computer code, and the results are determined solely by the temperature field (including the coverage mask) and a single parameter which describes the range of spatial autocorrelation in the temperature field. The estimator is also less biased than the mean of the zonal means which has been used with radiosonde data.

A number of more sophisticated approaches to averaging temperature data have been proposed, from Kagan (1979) to the recent works of Ilyas *et al.* (2017) and Huang *et al.* (2017). We do not intend the simple estimator proposed here to be a replacement for such methods; however, it does provide an easily understood and easily analyzed demonstration of why more naive averages are inadequate. Ideally, global temperature estimation would be performed using the optimal averaging method of Kagan or more modern methods; however, where simplicity of implementation and reproducibility are concerns, the GTA1 estimator can still substantially reduce the coverage error contribution to temperatures estimates for recent decades. The impact on temperature trends during the apparent ‘hiatus’ period provides an illustration of why good statistical estimators of global mean temperature are required for use in the evaluation of both historical temperature change and current temperature trends.

Supplementary material

Data and methods for this paper are available at <https://doi.org/10.15124/c47f6da3-2430-4f0e-973e-6f6597c6da42> with updates at <http://www-users.york.ac.uk/~kdc3/papers/coverage2018>.

Supplementary material is available at *Dynamics and Statistics of the Climate System* online.

Declaration

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Conflict of interest: none.

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