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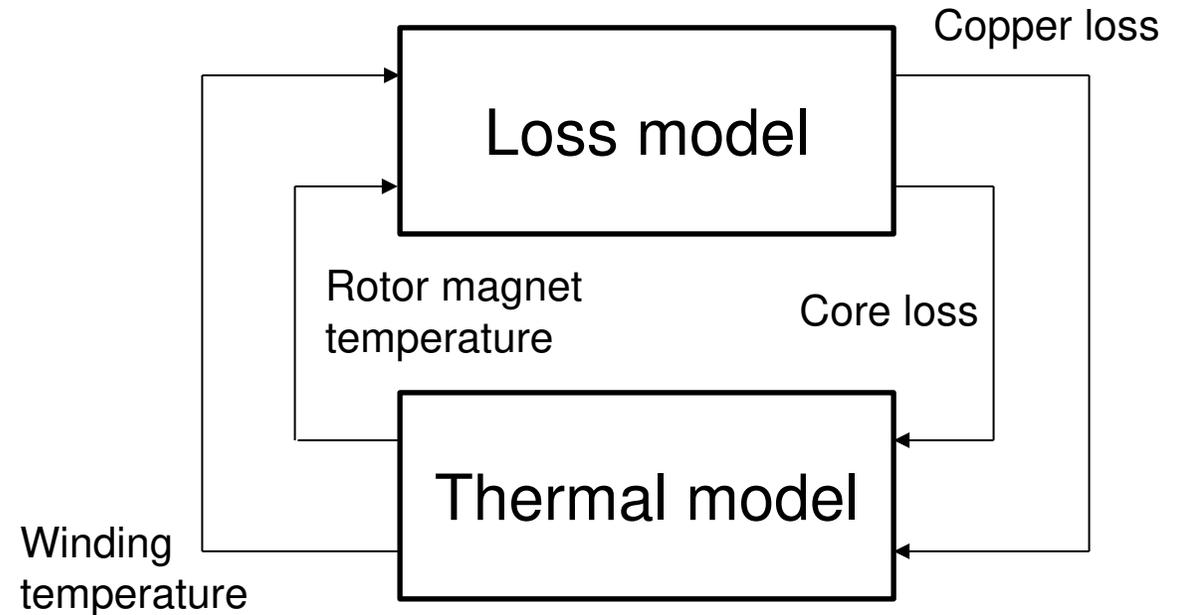
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# COMPUTATIONALLY EFFICIENT, ELECTRO-THERMALLY COUPLED MODEL FOR PERMANENT MAGNET MACHINES IN ELECTRIC VEHICLE TRACTION APPLICATIONS

Liang Chen, Xiao Chen, Jiabin Wang and Antonio Griffo,  
University of Sheffield, UK

- **Research Motivation**
- **Methodology (Equivalent d-axis current representing temperature effect)**
- **Electro-thermally Coupled Model**
- **FE Validation**
- **Simulation Results**
- **Experimental Validation**

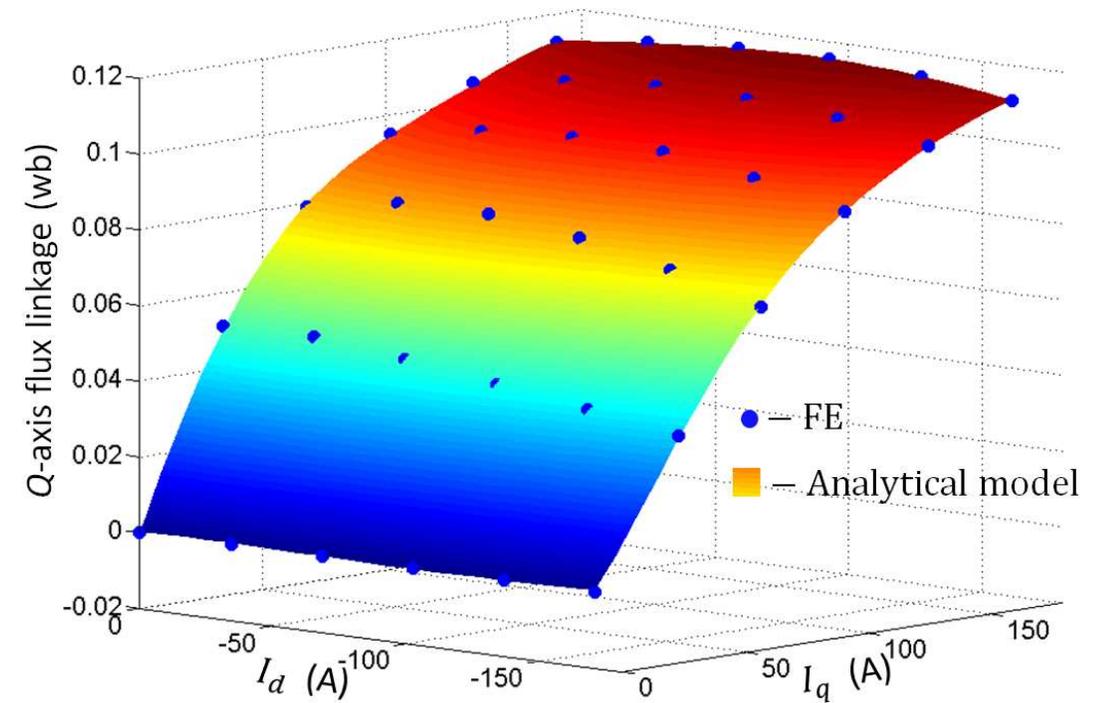
- ❑ **Electrical machine temperatures are subject to its copper loss, core loss, etc.**
- ❑ **Machine copper loss and core loss are largely affected by machine temperatures**
  - a) Winding resistance increases by 39% for every 100°C temperature rise;
  - b) Magnet remanence reduces by 12% for every 100°C temperature rise (for NdFeB);
  - c) High nonlinearity in the machine flux linkage map due to core saturation



# Research Motivation

- ❑ Electrical machine temperatures are subject to its copper loss, core loss, etc.
- ❑ Machine copper loss and core loss are largely affected by machine temperatures
  - a) Winding resistance increases by 39% for every 100°C temperature rise;
  - b) Magnet remanence reduces by 12% for every 100°C temperature rise (for NdFeB);
  - c) High nonlinearity in the machine flux linkage map due to core saturation

**Essential to accurately model the electro-thermally coupling effect in the electrical machine, in order to accurately simulate the waste heat recovery in the vehicle powertrain system.**



10kW 18-slot 8-pole IPM machine

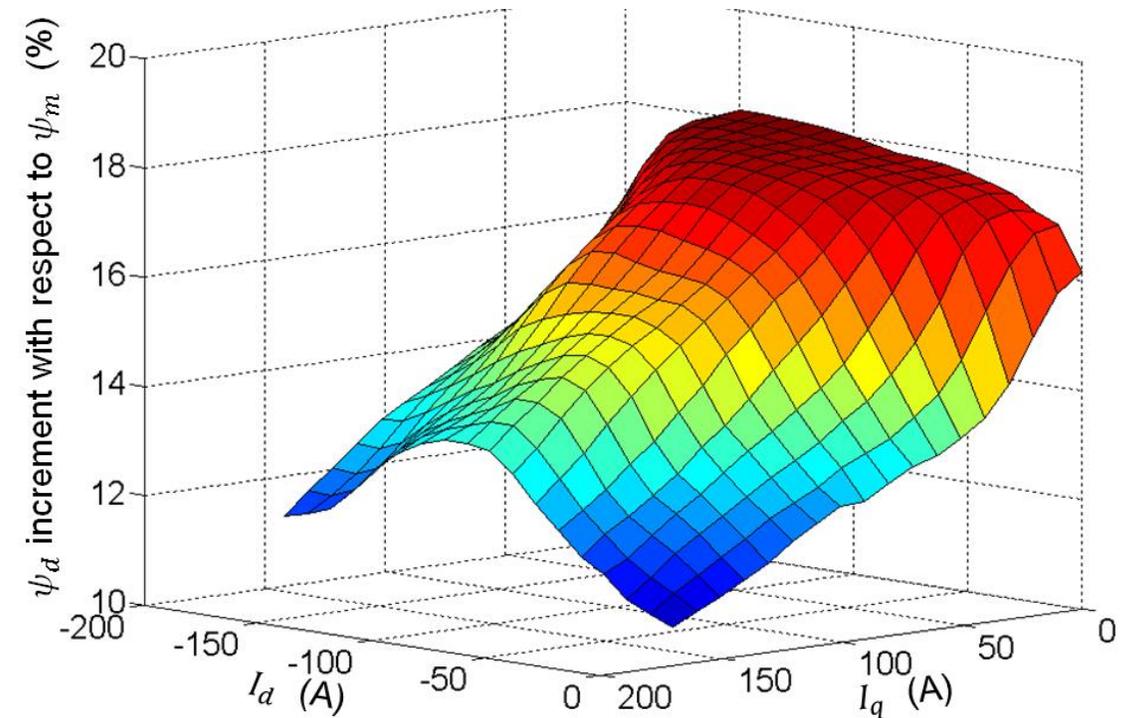
# Temperature Effects on Flux Linkages

$$B_{r2}(T_2) = B_r(T_1) \times [1 + \alpha \times (T_2 - T_1)]$$

where  $\alpha$  is temperature coefficient,  $B_{r2}$  and  $B_{r1}$  represent the remanence at temperature of  $T_2$  and  $T_1$ , respectively.

$d$ -axis flux linkage increment over  $d$ -,  $q$ -axis current ranges when temperature decreases from 100°C to 20°C (normalized to the flux-linkage due to permanent magnets at 120°C)

The increment can be up to 18%;  
The increment is non-uniform in the range of  $d$ - and  $q$ -axis currents



10kW 18-slot 8-pole IPM machine

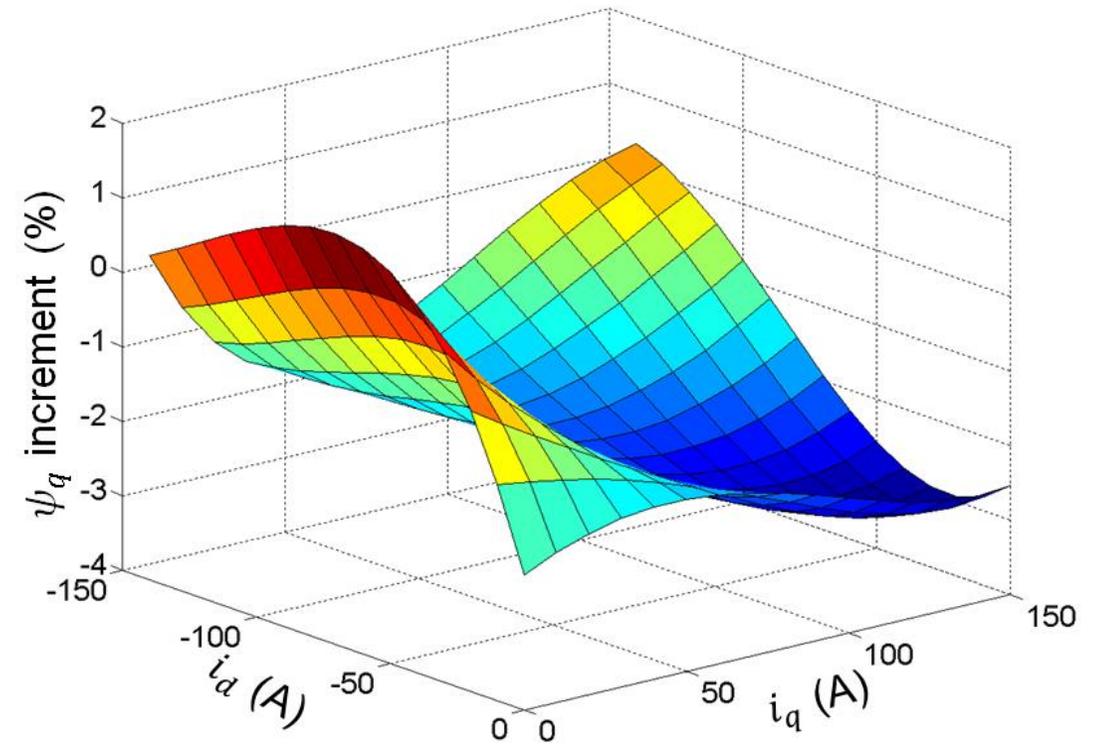
# Temperature Effects on Flux Linkages

$$B_{r2}(T_2) = B_r(T_1) \times [1 + \alpha \times (T_2 - T_1)]$$

where  $\alpha$  is temperature coefficient,  $B_{r2}$  and  $B_{r1}$  represent the remanence at temperature of  $T_2$  and  $T_1$ , respectively.

$q$ -axis flux linkage increment over  $d$ -,  $q$ -axis current ranges when temperature decreases from 100°C to 20°C (normalized to the flux-linkage due to permanent magnets at 120°C)

Neglecting the temperature effect on the  $q$ -axis flux linkage does not incur large error



10kW 18-slot 8-pole IPM machine

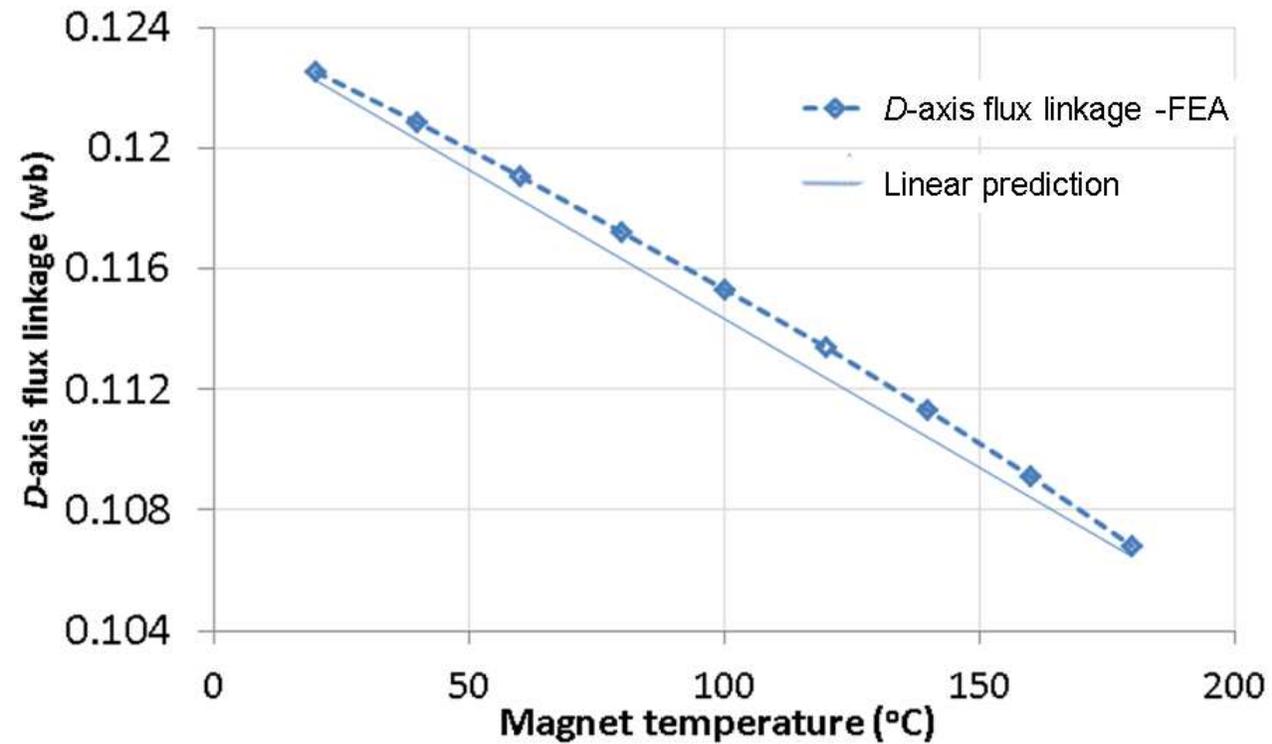
# Temperature Effects on Flux Linkages

$$B_{r2}(T_2) = B_r(T_1) \times [1 + \alpha \times (T_2 - T_1)]$$

where  $\alpha$  is temperature coefficient,  $B_{r2}$  and  $B_{r1}$  represent the remanence at temperature of  $T_2$  and  $T_1$ , respectively.

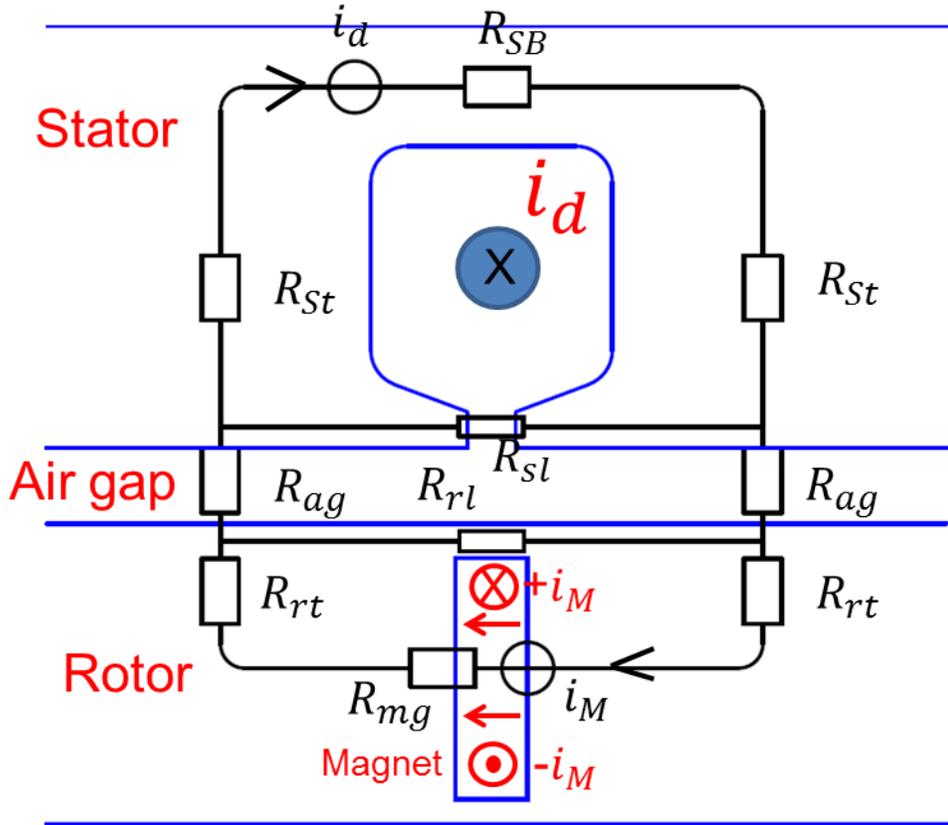
FE predicted open-circuit  $d$ -axis flux linkage  $\psi_d$  variation with magnet temperature.

Due to saturation effect,  $\psi_d$  varies not strictly linear with temperature

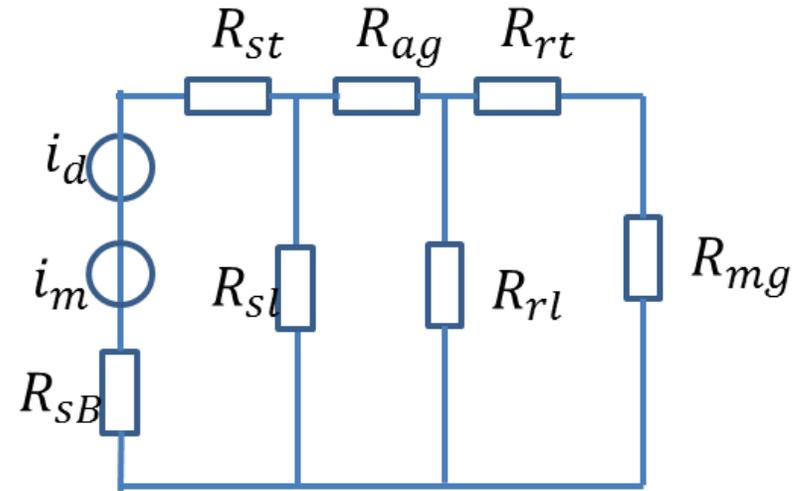


# Equivalent $d$ -axis Current Representing Temperature Effects

Magnetic flux path



Equivalent magnetic circuit

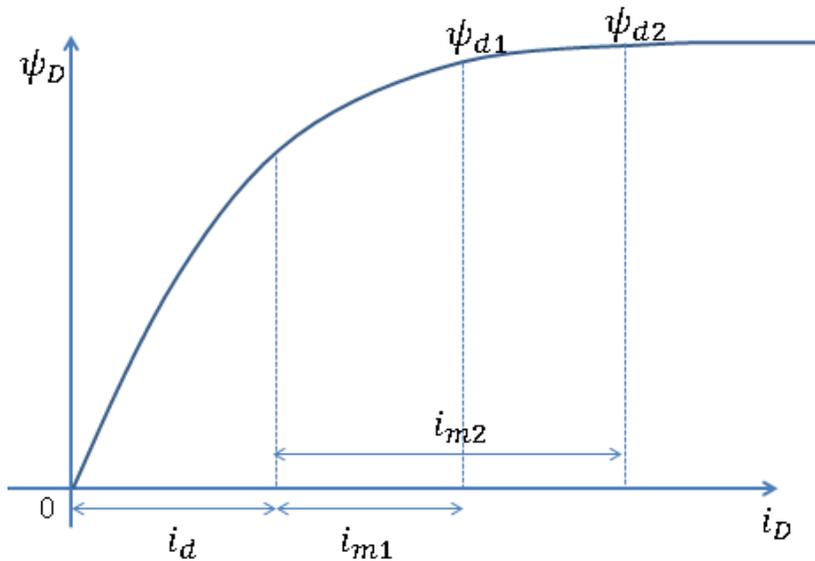


Therefore the total equivalent excitation current in the  $d$ -axis seen by the stator windings is  $i_d + i_m$

$i_m$  changes proportionally to the temperature variation

# Equivalent $d$ -axis Current Representing Temperature Effects

Therefore, when temperature changes,



$$\psi_d(i_d, i_q, T_1) = \psi_D(i_d + i_{m1}, i_q)$$

$$\psi_d(i_d, i_q, T_2) = \psi_D(i_d + i_{m2}, i_q)$$

$$\begin{aligned}\psi_d(i_d, i_q, T_2) &= \psi_D(i_d + i_{m1} + i_{m2} - i_{m1}, i_q) \\ &= \psi_d(i_d + (i_{m2} - i_{m1}), i_q, T_1) \\ &= \psi_d(i_d + i_{mc}, i_q, T_1)\end{aligned}$$

$$\text{where } i_{mc} = i_{m2} - i_{m1}$$

Therefore the flux linkages at a new temperature  $T_2$  can be predicted using the model at the reference temperature  $T_1$  with its  $d$ -axis current displaced by a constant  $i_{mc}$ , which is equal to the magnet equivalent current difference between the two temperatures.

# Equivalent $d$ -axis Current Representing Temperature Effects

Considering the flux linkage variation due to different rotor position:

$$\psi_d(i_d, i_q, \theta, T_2) = \psi_d(i_d + i_{mc}, i_q, \theta, T_1)$$

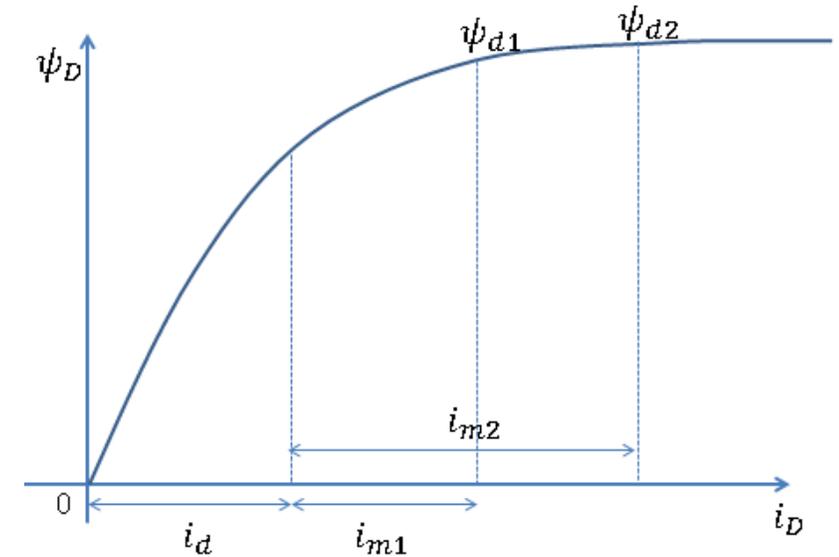
$$\psi_q(i_d, i_q, \theta, T_2) = \psi_q(i_d + i_{mc}, i_q, \theta, T_1)$$

Neglecting the saturation effect in the rotor bridge region:

$$i_{mc} = i_{m2} - i_{m1} = i_{m1} \times \alpha \times (T_2 - T_1)$$

$i_{m1}$  can be calculated using the short-circuit condition:

$$\psi_D(i_{d-sc1} + i_{m1}, 0) = \psi_d(i_{d-sc1}, 0, T_1) = 0$$

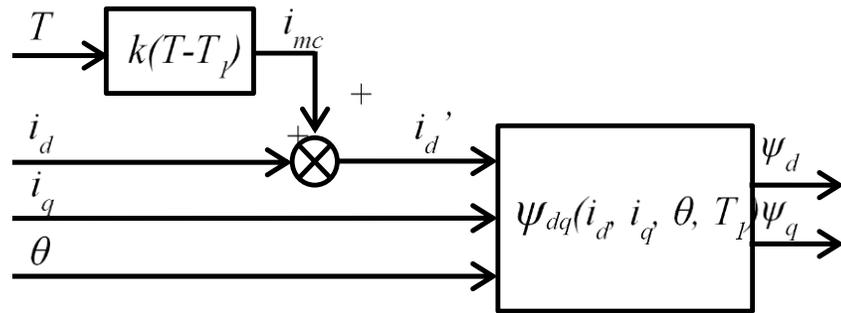


Once  $i_{m1}$  has been determined from the FE simulation of the short-circuit condition at the reference temperature  $T_1$ , the  $i_{mc}$  at any given temperature  $T_2$  can be obtained.

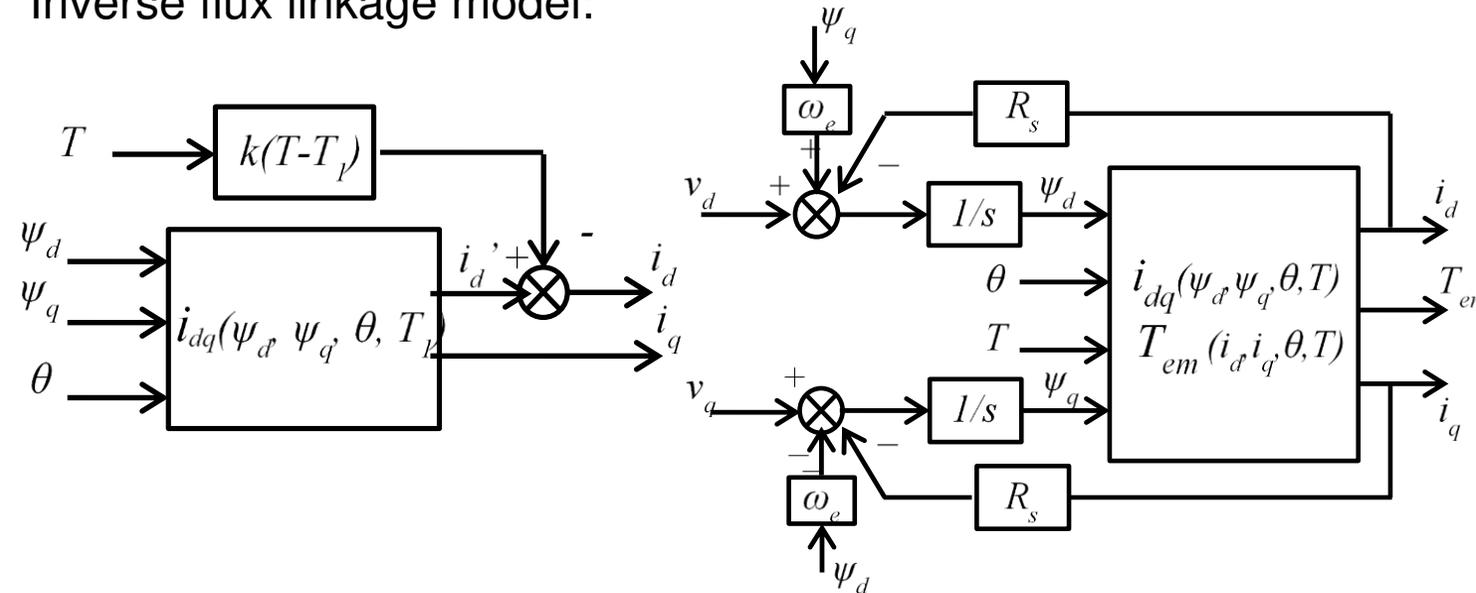
Then, use the modified  $d$ -axis current  $i_d + i_{mc}$  to calculate the flux linkages and torque at any temperature.

# Inverse Flux Linkage Model with Temperature Effects

Conventional flux linkage model:



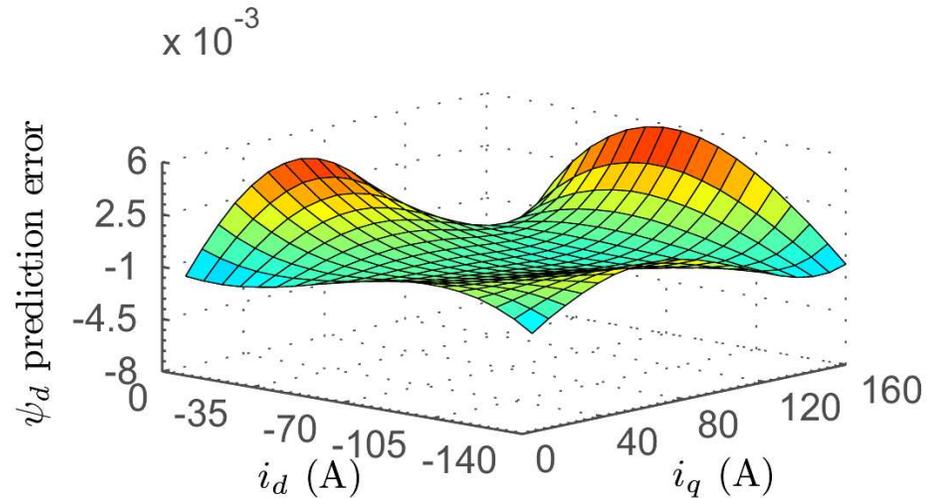
Inverse flux linkage model:



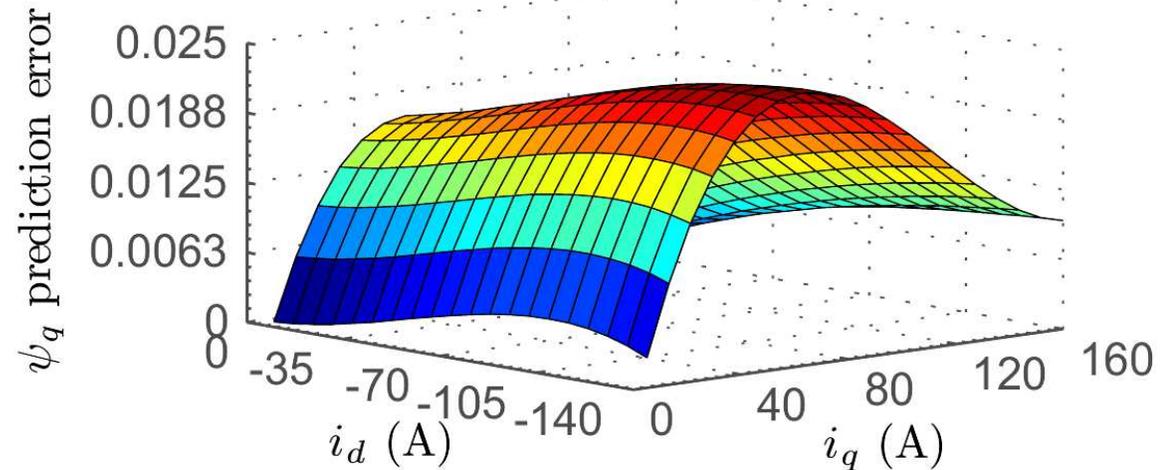
$$i_d(\psi_d, \psi_q, \theta, T) = i_{d1}(\psi_d, \psi_q, \theta, T_1) - k(T - T_1)$$

$$i_q(\psi_d, \psi_q, \theta, T) = i_{q1}(\psi_d, \psi_q, \theta, T_1)$$

$d$ -axis flux linkage error



$q$ -axis flux linkage error

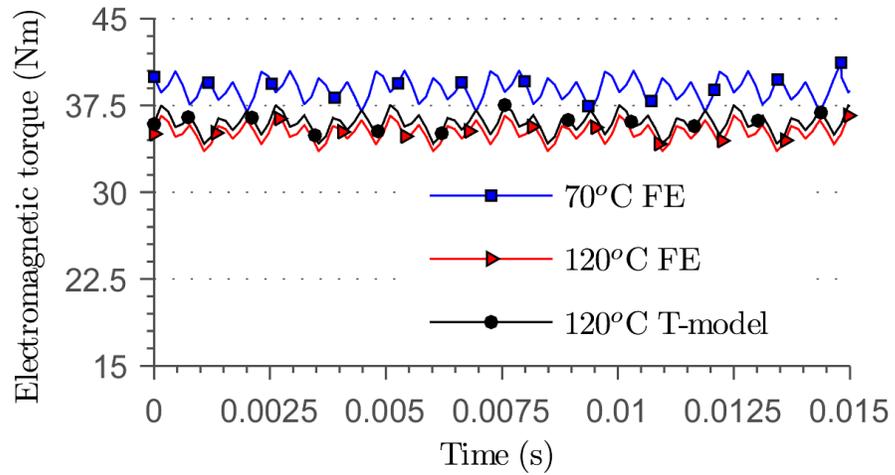


RMS error over  $i_d$  and  $i_q$  ranges:

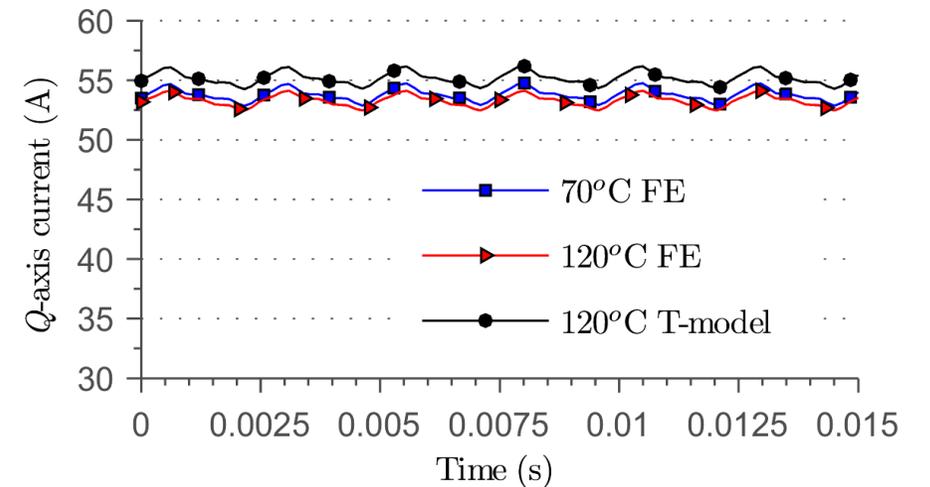
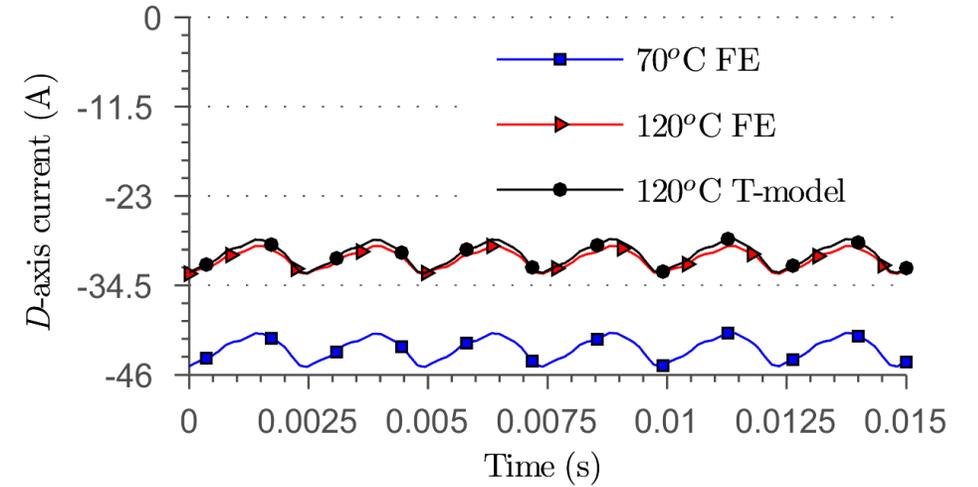
Variables	% change (from 100 °C to 20 °C)	Relative error of proposed model
$\psi_d$	10.82%	1.41%
$\psi_q$	1.45%	1.51%
$\psi_m$	8.98%	1.28%
$T_q$	4.66%	0.98%

# Time Domain Simulation

Rated torque and base speed (35Nm and 1350r/min)

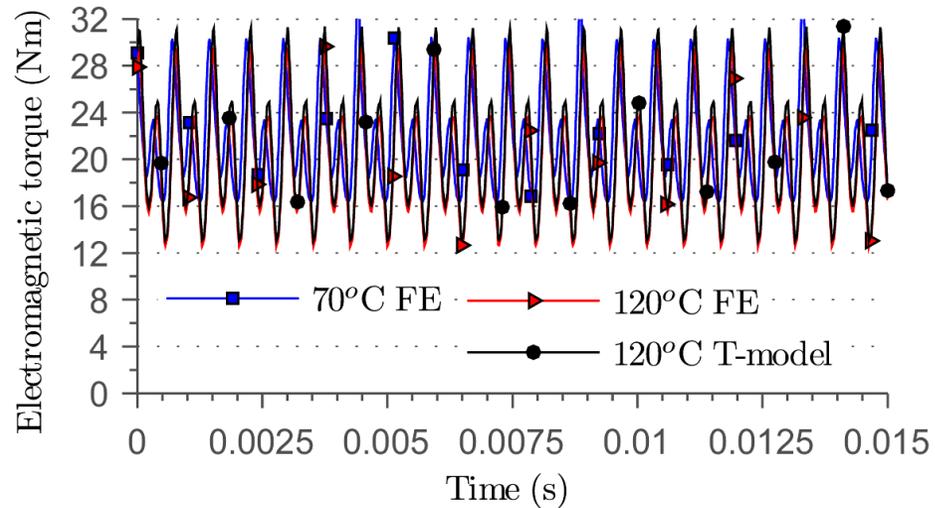


Good agreement achieved

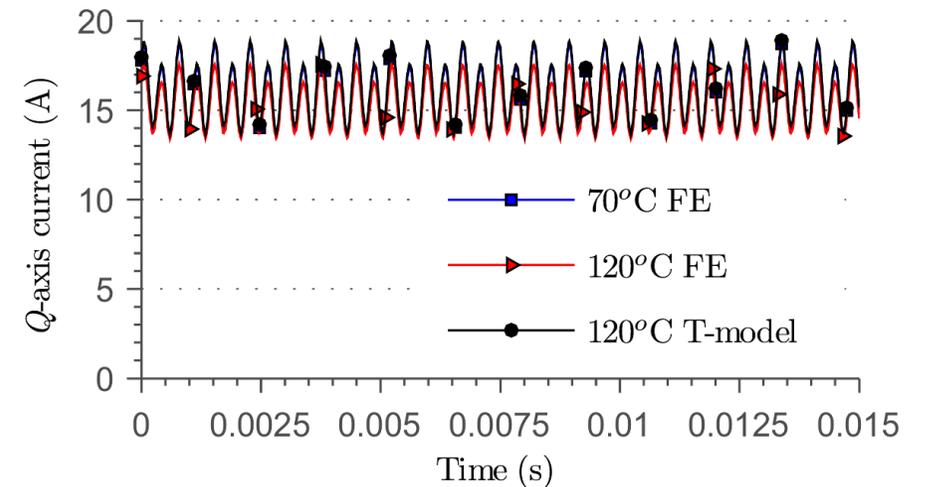
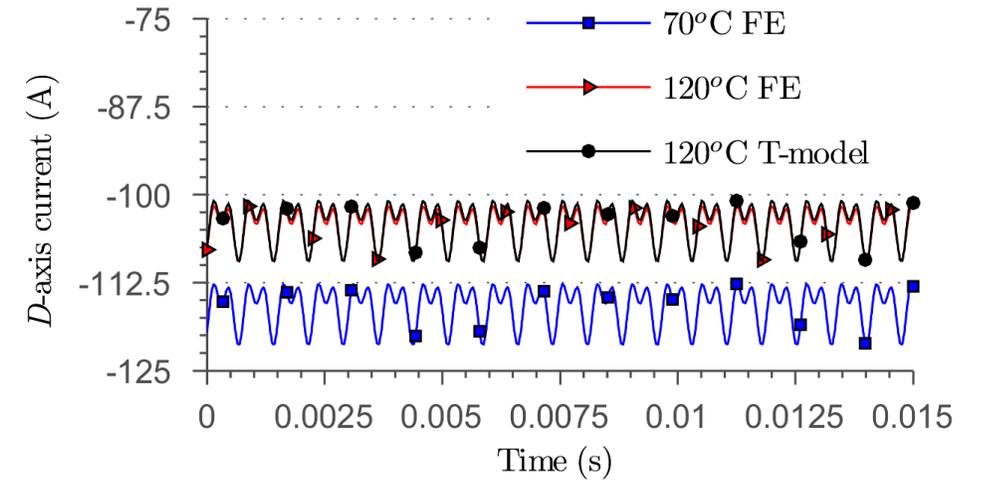


# Time Domain Simulation

Field weakening operation (20Nm and 4500r/min)

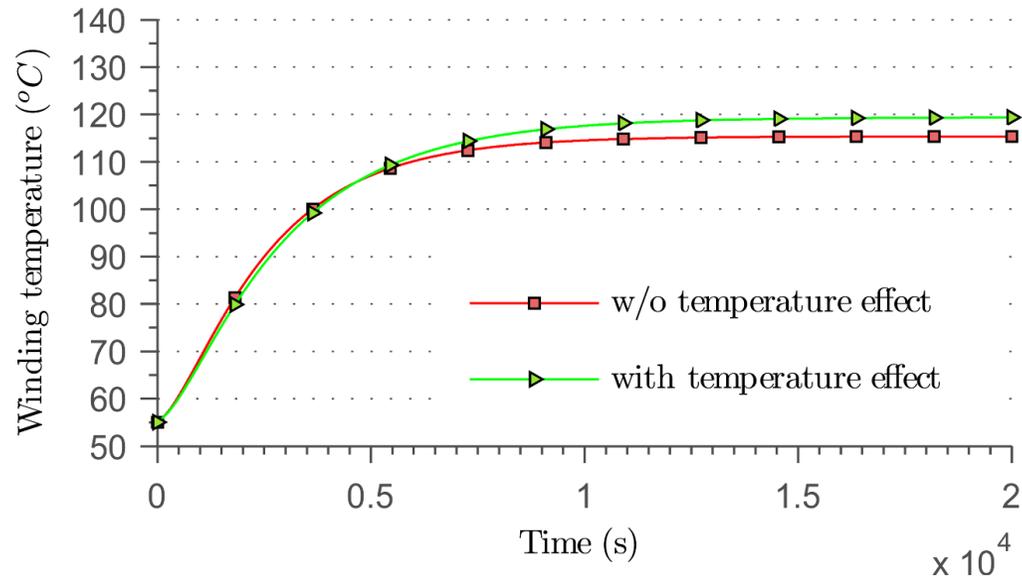


Good agreement achieved

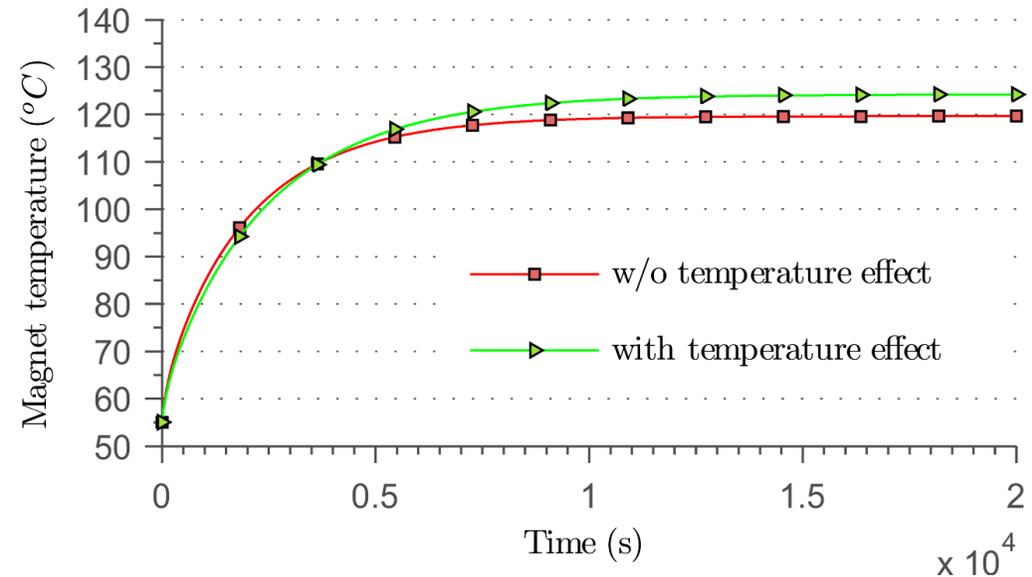


# Electro-thermally Coupled Simulation

Winding temperature:



Magnet temperature:



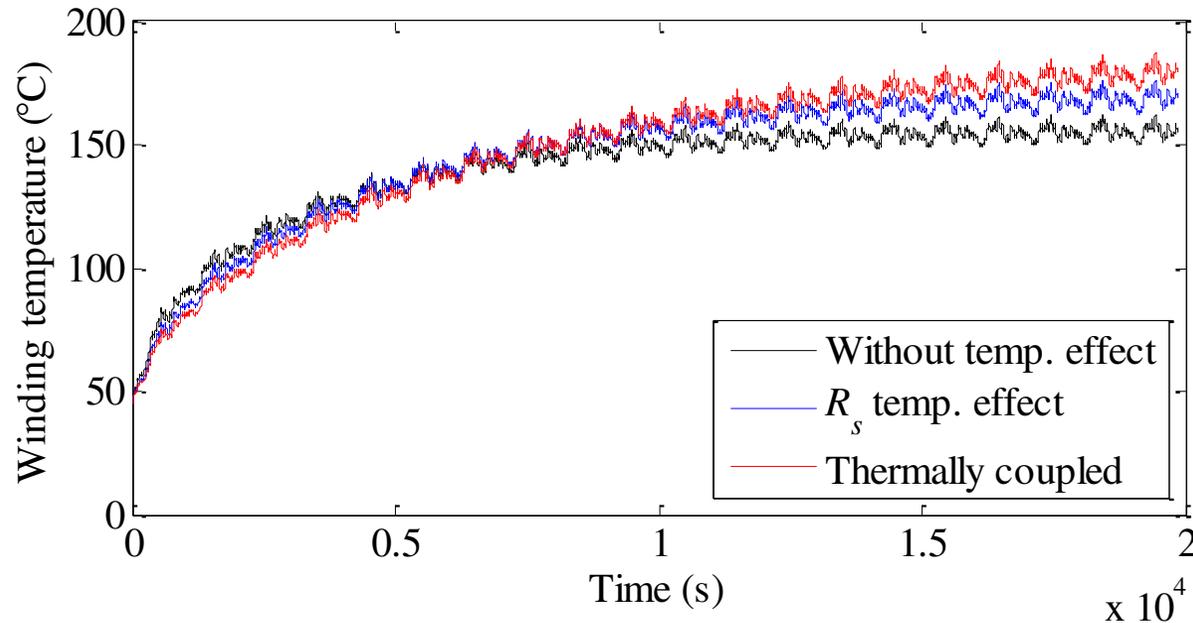
Rated torque and base speed operation

'w/o temperature effect' refers to assuming the machine temperature is fixed at 100°C

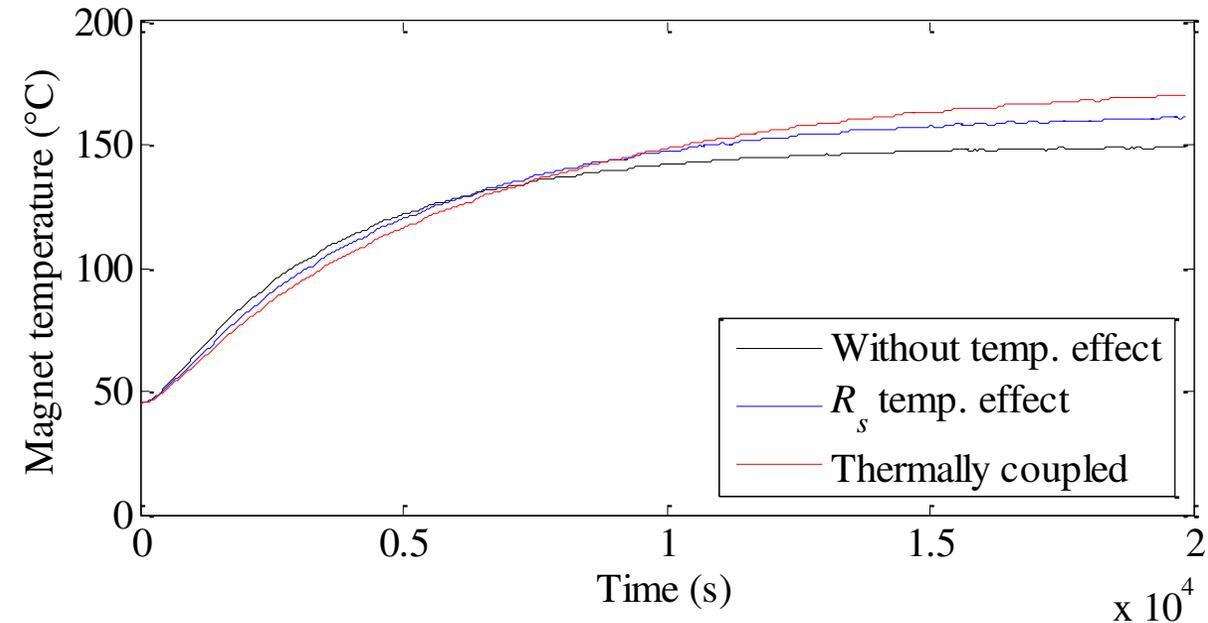
With the temperature effect considered, the winding and magnet temperatures are ~5°C higher than the results calculated using the conventional method when the machine gets into thermal steady state.

# 20 Artemis Urban Driving Cycles, 10° gradient

Winding temperature:



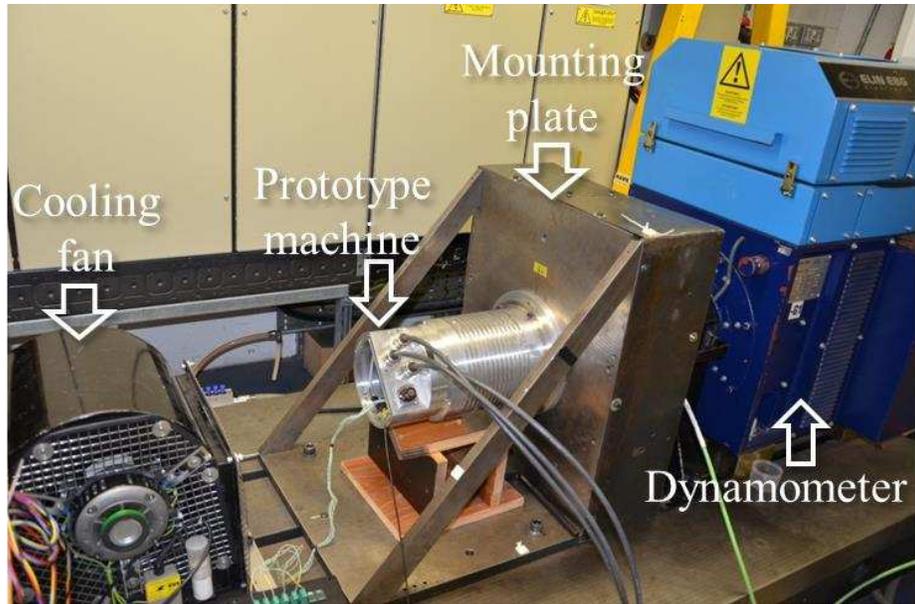
Magnet temperature:



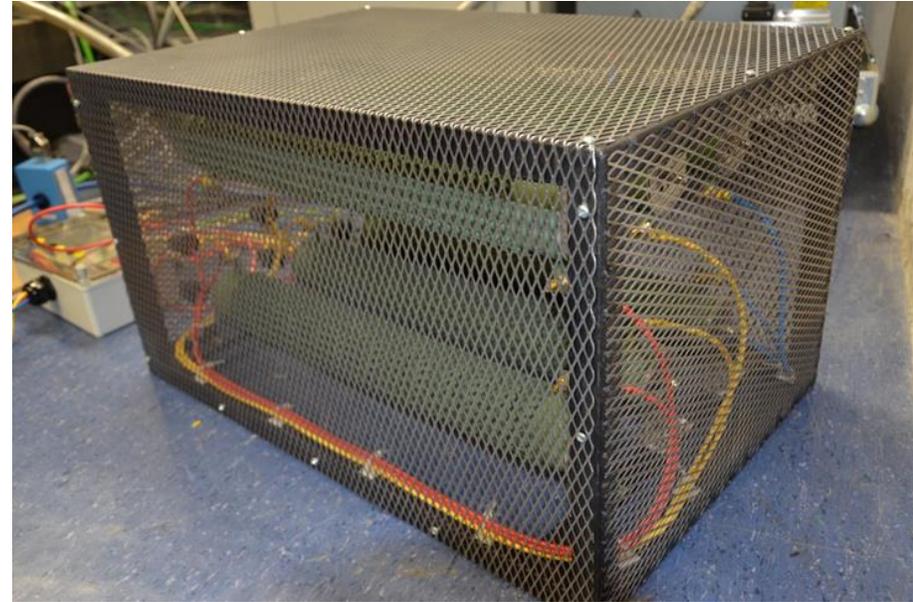
With the temperature effect considered, the winding and magnet temperatures are ~20°C higher than the results calculated using the conventional method and ~10°C higher than the results considering only the temperature effects on winding resistance.

# Experimental validation

Test rig

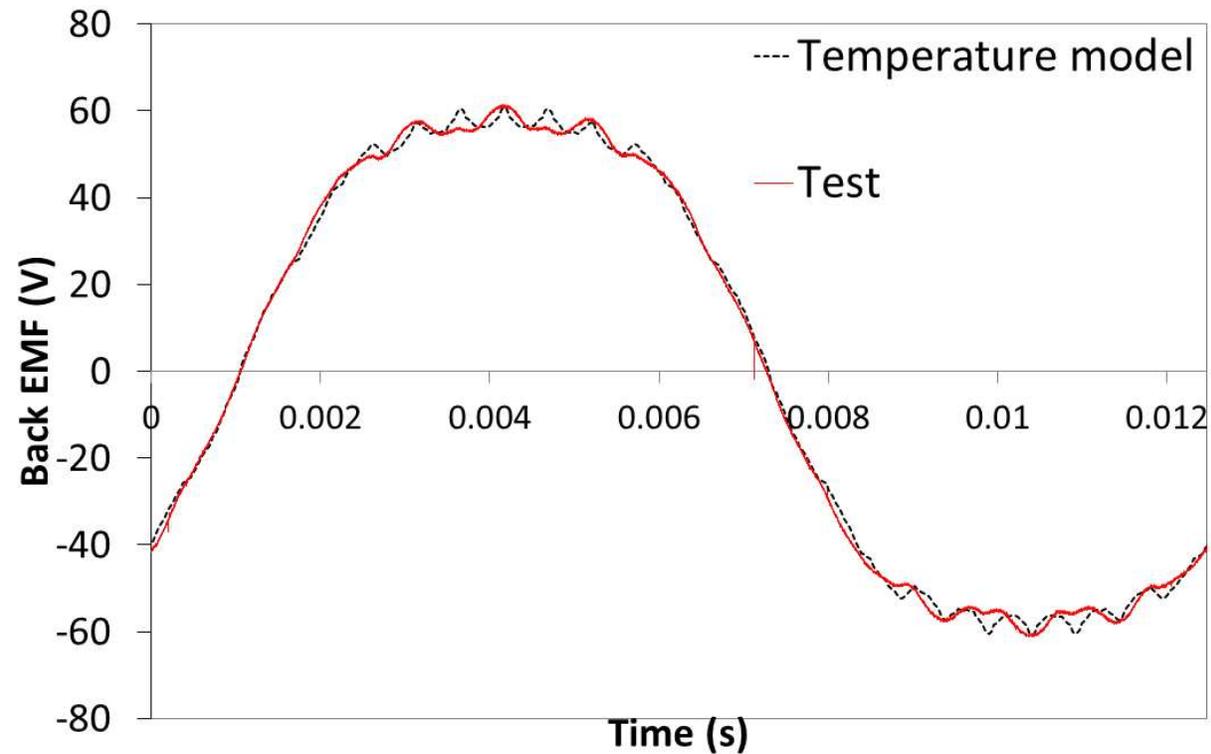


Power resistors:



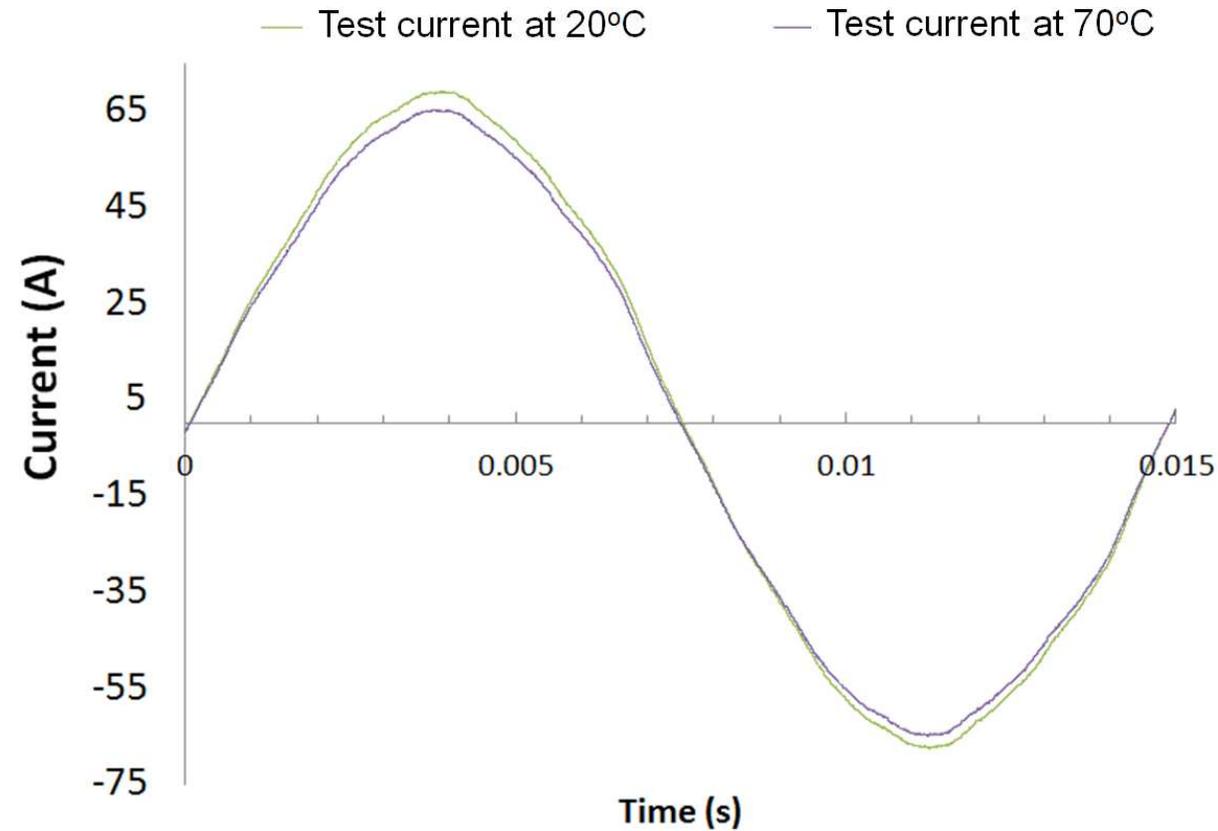
A prototype machine of the 36-slot 6-pole IPM is driven by a dynamometer in the generator mode with a resistive load at different temperatures.

## Back-EMF



With the calibrated remanence, the predicted open-circuit back EMFs at 20°C have good agreements with the measure ones.

## Current Measurements

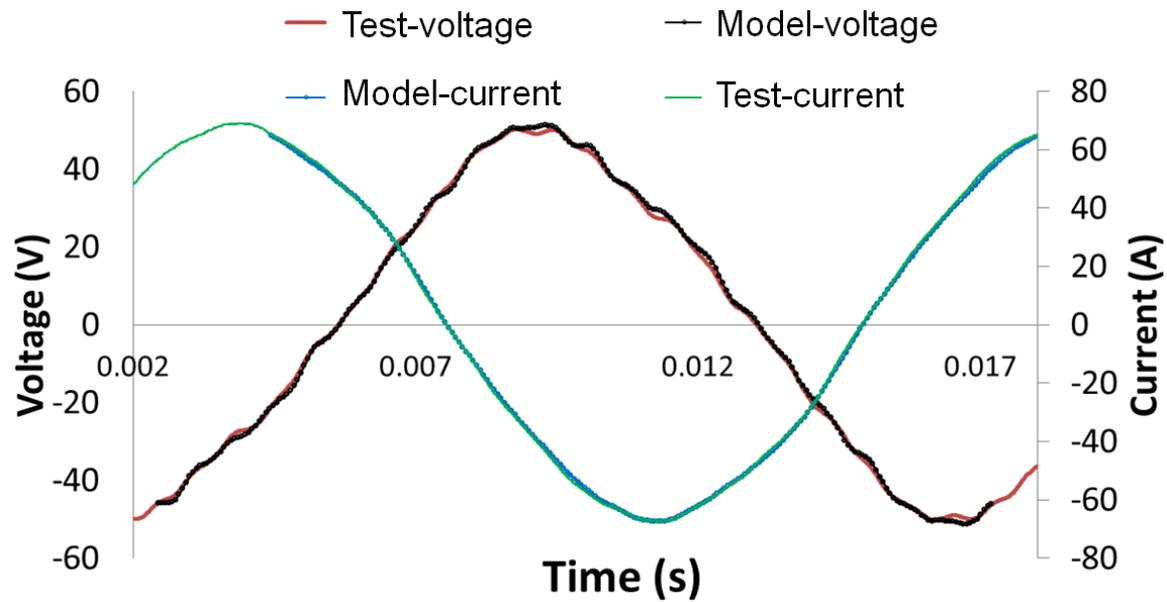


6% reduction in fundamental current when temperature rises from 20°C to 70°C

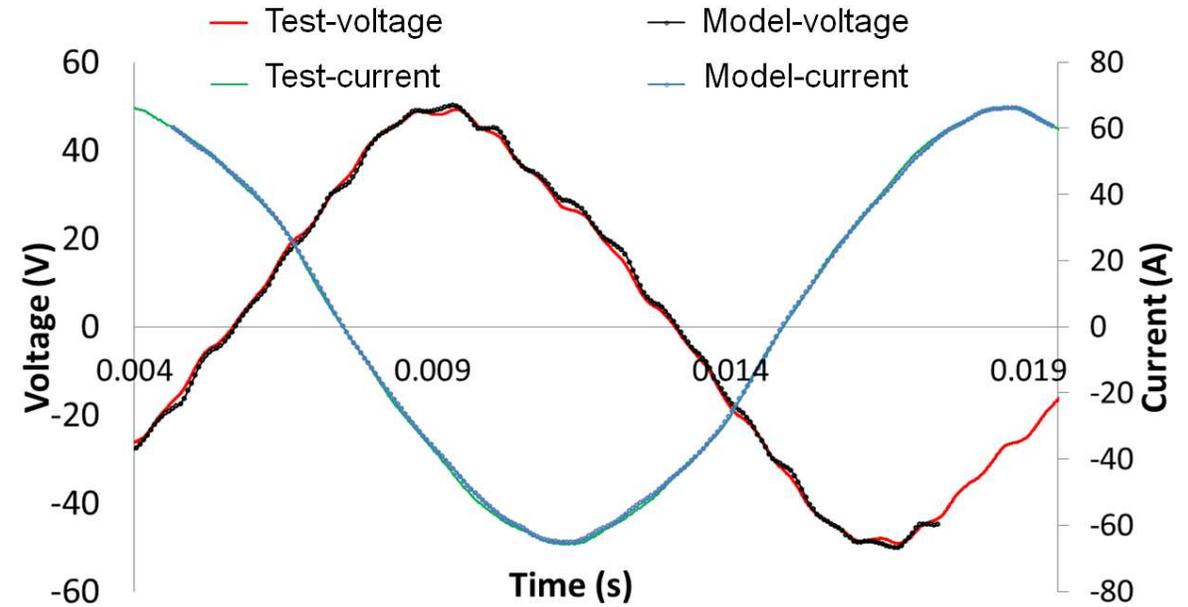
# Experimental validation

## Comparison

20°C



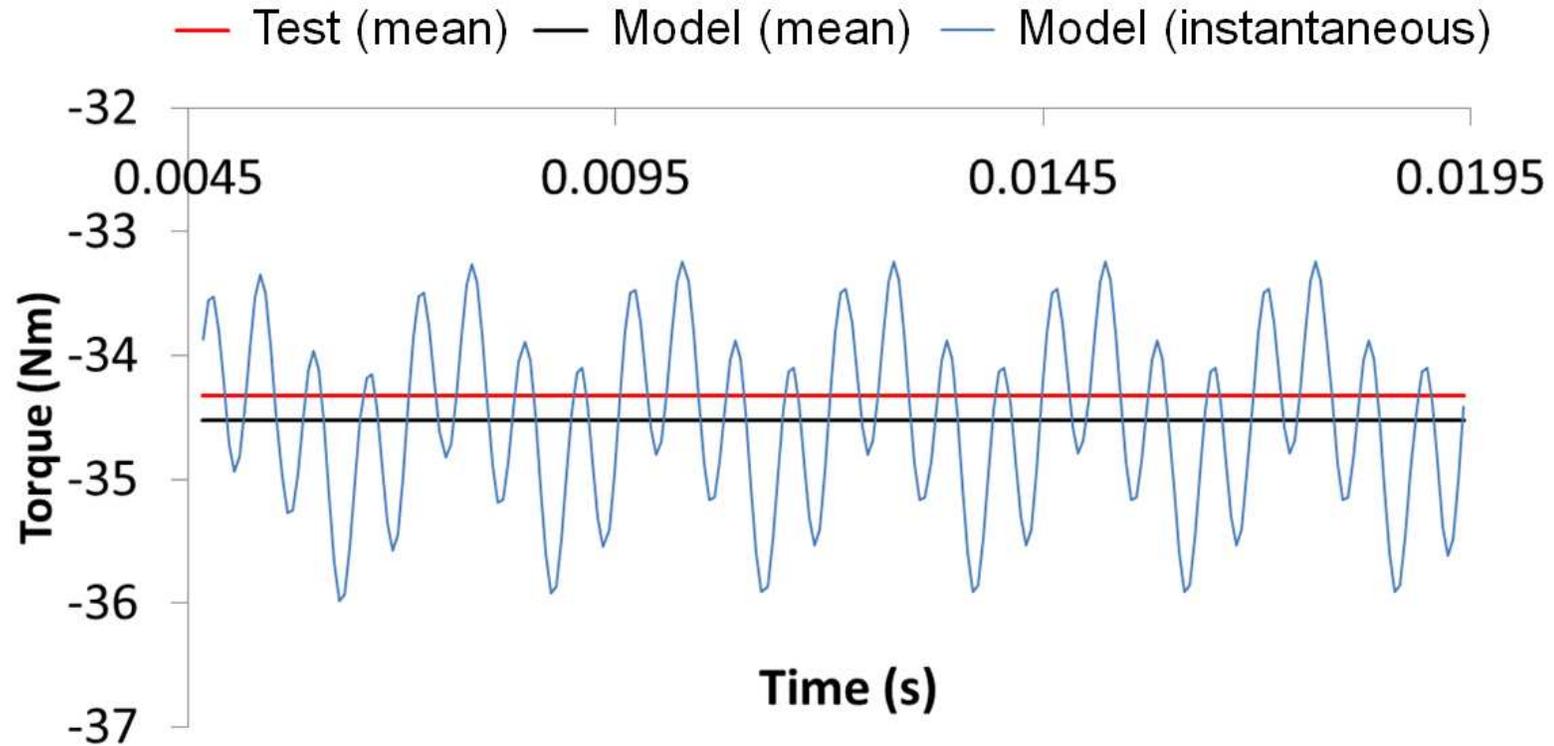
70°C



Good agreement achieved

# Experimental validation

## Measured torque



Mean torque error: 0.58%

# Conclusions

- This paper proposed a high fidelity, computationally efficient method for representing the temperature effect of magnets on the machine behaviors.
- It employs an equivalent d-axis current proportional to the temperature variations in the machine flux linkage maps characterized at a reference temperature and expressed as functions of d- and q-axis currents and rotor position.
- The method can greatly reduce simulation time for performance evaluation under driving cycles various driving conditions.
- The effectiveness of the method has been validated by finite element analysis and tests on a prototype machine.

**Thank you for your attention!**