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1 Centrifuge modelling of cone penetration tests in layered soils

2

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16 Figures

2 Tables

3 **Abstract**

4 Penetration problems are important in many areas of geotechnical engineering, such as the
5 prediction of pile capacity and interpretation of in-situ test data. **[Reply 3-1] The cone**
6 **penetration test is a proven method for evaluating soil properties, yet relatively**
7 **little research has been conducted to understand the effect of soil layering on pen-**
8 **etrometer readings. This paper focuses on the penetration of a probe within lay-**
9 **ered soils and investigates the layered soil effects on both penetration resistance**
10 **and soil deformation.** A series of centrifuge tests was performed in layered configurations
11 of silica sand with varying relative density in a 180° axisymmetric model container. The tests
12 allowed for the use of a half-probe for observation of the induced soil deformation through a
13 Perspex window **[Reply 3-2] as well as a full-probe for measurement of penetration**
14 **resistance within the central area of the container.** The variations of penetration re-
15 sistance and soil deformation characteristics as they relate to penetration depth, soil density,
16 and soil layering are examined. The results of deformation are also compared with previous
17 experimental data to examine the effect of the axisymmetric condition. The effects of soil
18 layering on both resistance and soil deformation are shown to be dependent on the relative
19 properties between soil layers.

20
21 Keywords: cone penetration test, layered soils, centrifuge modelling.

22
23 List of notations provided at end of paper.
24

1 Introduction

It is increasingly important for geotechnical engineers to cost-effectively determine engineering properties of soil using in-situ test methods, which avoid the difficulties in retrieving undisturbed samples. The cone penetration test (CPT) is one of the most versatile devices for in-situ soil testing and has been widely used in geotechnical engineering practice. The CPT can provide reliable and repeatable data which can be used to evaluate soil properties and to delineate between layers of different soil types and states (IRTP, 1994). The analogues between a penetrometer and a displacement pile in both geometry and installation method make the study of penetration problems relevant to a wide range of foundation problems. CPT-based design methods have been developed for piles (Jardine and Chow, 1996; Lehane et al., 2005; White and Bolton, 2005) and for the evaluation of liquefaction potential of soils (Robertson, 1982; Tseng, 1989; Moss et al., 2006).

The interpretation of CPT data tends to rely on empirical relationships, of which many have been developed over the years for soil identification and classification. Numerical modelling has many advantages compared to empirical methods and can provide insights into the relationship between soil characteristics and probe response. However analysis of penetration problems using numerical models is difficult due to the large strains that are induced within the ground in the localised area around the probe. The detailed soil stress/strain history associated with pile/probe installation and the relationship to the distribution of the load on the probe are still not well understood. A review of the methods that have been developed for CPT data analysis was provided by Yu and Mitchell (1998).

One of the complicating factors in the interpretation of CPT data (e.g. cone tip resistance, q_c , and sleeve friction, f_s) is that readings are influenced not only by the soil at the location of the cone tip but also by the soil within an influence zone extending some distance beneath and above the tip. There has been relatively little research done on the effect of soil layering on CPT measurements. A small number of experiments have been carried out that provide observations of the transition of penetration resistance through layered soils (e.g. Treadwell, 1976; Silva and Bolton, 2004; Xu, 2007). There have also been some numerical simulations conducted for the analysis of layered effects and the definition of the influence zones around soil interfaces (e.g. van den Berg et al., 1996; Ahmadi and Robertson, 2005; Xu and Lehane, 2008; Walker and Yu, 2010). The first analytical solution for penetration in layered soils was proposed by Vreugdenhil et al. (1994), which is an approximate solution for simple linear-elastic media. Elastic-plastic solutions for expanding cavities embedded in two different cohesive-frictional materials were proposed by Mo et al. (2014b), which were shown to provide an effective method for the interpretation of CPT data in layered soils in Mo et al. (2014a).

Geotechnical centrifuge testing provides an effective experimental method for the study of pene-

63 tration problems and allows replication of full-scale stress levels and gradients within small-scale
64 models. Previous CPT-based centrifuge tests have provided useful information relating to the
65 effects of boundaries, stress level, and grain size ratio (Lee, 1990; Bolton et al., 1993; Gui et al.,
66 1998). A new test methodology for CPT modelling within a geotechnical centrifuge has been
67 developed in this research, using a 180° axisymmetric model so that image-based methods (White
68 et al., 2003) could be used to acquire sub-surface displacements around a cylindrical probe. The
69 decision to use an axisymmetric model, rather than a fully 3D or plane-strain one, was based on
70 the desire to see and measure the mechanisms of deformation that occur within the soils around
71 a representative cylindrical probe. The axisymmetric condition provides this ability, but involves
72 additional experimental complications which are discussed in the paper.

73

74 This paper presents an experimental study of the CPT response in layered soils using geotech-
75 nical centrifuge testing. The aim of the work is to investigate the relationship between layered
76 soil properties and penetrometer response. A full description of the experimental equipment and
77 methodology is first provided. This is followed by experimental results **including the transition**
78 **of penetration resistance ratio to illustrate the effect of layered soil properties on**
79 **penetrometer response (2-layer and 3-layer profiles are considered), as well as com-**
80 **parison with previous numerical and analytical studies.** Soil displacement profiles and
81 trajectories as well as strain paths are then provided to illustrate the observed penetration mech-
82 anisms in both uniform and layered soils. The paper ends with an appropriate set of conclusions.

83

84 2 Centrifuge Modelling Methodology

85 2.1 Experimental apparatus

86 The centrifuge tests focused on the use of an axisymmetric model (rather than plane-strain) in or-
87 der to obtain measurements of sub-surface displacements yet still be consistent with the geometric
88 and stress/strain conditions around a cylindrical penetrometer. The centrifuge container, illus-
89 trated in Fig. 1, has an inner diameter (D) of 500 mm and a 75 mm thick transparent Perspex wall
90 installed at the centre of the container as a plane of symmetry. A vertical load actuator capable of
91 providing a maximum load of 10 kN was used to drive probes into the soil to a maximum displace-
92 ment of 220 mm . **[Reply 3-15] Sub-surface soil displacements were measured using the**
93 **particle image velocimetry (PIV) and photogrammetry method of White et al. (2003)**
94 **on images obtained from two Canon Powershot G10 digital cameras mounted in front**
95 **of the Perspex wall.** The PSRemote Multi-Camera software was used to simultaneously capture
96 images from the two cameras every 5 seconds. An array of 16 control points was painted onto the
97 Perspex window within each camera's field-of-view (FOV) for use within the White et al. (2003)
98 geoPIV analysis method.

[Fig. 1 about here.]

101 2.2 Model penetrometers

102 Aluminium alloy probes with a 12 mm diameter (B), a smooth un-coated shaft, and an apex angle
 103 of 60° were used for the centrifuge tests (Fig. 2). For the half-probe, the ratio of the container
 104 to the probe diameter ($D/B = 42$) and the ratio of the probe diameter to the mean grain size of
 105 the soil ($B/d_{50} = 86$) were greater than that suggested by Gui et al. (1998) in order to reduce
 106 the boundary and grain size effects. Full-probe tests were also performed in the same samples
 107 to provide a more conventional (and reliable) measure of penetration resistance away from the
 108 container boundaries. **[Reply 3-16] The distance from the full-probe to the container**
 109 **boundaries was just under the $10B = 127\text{ mm}$ value (see Fig. 1b) recommended by Gui**
 110 **et al. (1998) to limit boundary effects on penetrometer readings.**

111

112 Attempts have been made by previous researchers to accurately model half-probes in the cen-
 113 trifuge (Liu, 2010; Marshall and Mair, 2011). However, any intrusion of sand particles between
 114 the half-probe and the window forces the probe to deviate from the window, causing bending of
 115 the probe and the inability to track its position using image analysis. This problem, which is not
 116 such an issue for plane-strain tests (e.g. White, 2002), is one of the main challenges when using a
 117 180° axisymmetric model for these types of tests. In order to maintain contact between the probe
 118 and the window in this project, a new method was developed which used a guide bar and channel
 119 system (Fig. 2a). The guide bar was connected to the half-probe along its length so that the sep-
 120 aration between the bar and the probe was fixed. During testing, the probe was pushed with its
 121 flat edge down the plane of symmetry of the Perspex wall and the bar slid into the channel (8 mm
 122 wide by 8 mm depth) which was fixed within the Perspex wall such that it was flush with the
 123 plane of symmetry. This method ensured that the probe followed the exact same vertical path in
 124 each test and prevented soil from getting between the probe and the Perspex. To minimise friction
 125 along the back of the probe and the guide bar, the contacting surfaces were coated with silicon
 126 grease. The gap within the channel was sealed with silicone sealant to prevent sand ingress; the
 127 screws connecting the half-probe to the guide bar cut through the sealant relatively easily during
 128 a test. The guide bar system provided an effective method to conduct consistent experiments.
 129 However one disadvantage was the loss of soil deformation data in an 8 mm wide zone (4 mm on
 130 either side of probe axis) ahead of the probe tip where the channel blocked the view of the soil
 131 through the Perspex.

132

133 Penetration loads were measured using a load cell at the top of the probes as well as strain gauges
 134 installed on the probes. **[Reply 3-18] As shown in Fig. 2a, a hemispherical loading cap**
 135 **was attached to the upper part of the load cell. The cap was greased to encourage**

136 **sliding to occur between the actuator loading plate and the upper part of the pile**
137 **in the event that there was some misalignment between the pile and the actuator**
138 **which would induce unwanted bending strains within the pile.** The probe was hung from
139 the actuator assembly using steel wires to prevent it from penetrating the soil during centrifuge
140 spin-up. Three strain gauges ('SG1', 'SG2' and 'SG3') were embedded inside the body of the half-
141 probe in order to measure tip resistance and shaft friction. Unfortunately, the data obtained from
142 these gauges proved to be unreliable, most likely due to the effect of probe bending and difficulty
143 calibrating the half-probe. For this reason, analysis of cone tip resistance in this paper focuses
144 on data from the full-probe. The full-probe had a similar size and length as the half-probe. As
145 illustrated in Fig. 2b, it was manufactured from aluminium tubing with an outer and inner diam-
146 eter of 12.7 mm and 9.5 mm , respectively. Rather than the single strain gauge in the half-probe
147 tip, a pair of strain gauges ('SG45') were installed on the tip of the full-probe with a Wheatstone
148 half-bridge in order to compensate for bending.

149

[Fig. 2 about here.]

150

151 **2.3 Centrifuge tests**

152 Table 1 provides details of the six centrifuge tests presented in this paper. All of the centrifuge
153 tests were carried out on the Nottingham centre for Geomechanics (NCG) 2 m radius geotechnical
154 centrifuge at $50g$. Penetration was done at a constant speed of approximately 1 mm/s , corre-
155 sponding to a quasi-static penetration process.

156

157 The main focus of this project was the study of penetration within layered soils, which was achieved
158 by varying the relative density of the sand at distinct levels within the soil, as summarised in Ta-
159 ble 1. The layered tests included 2-layer soil samples of loose over dense (T04) and dense over
160 loose (T05) sands. These tests intended to reach a 'steady-state' penetration condition within
161 each layer. Two 'sandwich' soil tests (T06 and T07) were also conducted to examine the thin-layer
162 effects during penetration. The results of the two uniform soil tests (T02 and T03) served as a
163 reference for the layered sample tests.

164

165 For a particular test, the half-probe test would be done first, then the centrifuge would be spun
166 down and the load actuator moved and fitted with the full-probe before spinning up again to
167 conduct the full-probe test. The test layout is shown in Fig. 1, where the full-probe tests were
168 located to try to reduce the boundary and interaction effects.

169

170 **[Reply 3-21] Fraction E silica sand, supplied by David Ball Ltd UK, was used for**
171 **the centrifuge tests due to its appropriate grain size of $d_{50} = 0.14\text{ mm}$, providing a**
172 **B/d_{50} ratio greater than 20 as suggested by Gui et al. (1998) as well as its high grain**

173 **strength, thereby avoiding significant effects of particle breakage.** The properties of
174 Fraction E sand as reported by Tan (1990) are listed in Table 2. The mechanical behaviour of
175 Fraction E sand has been investigated by many previous researchers (e.g. Tan, 1990; Bui, 2009).
176 To achieve uniform samples, the multiple-sieving air pluviation method (Miura and Toki, 1982;
177 Zhao, 2008) was employed, with an achievable range of relative density between 50 % and 90 %.
178 A single-holed sand pourer, consisting of a hopper with a nozzle containing multiple sieves, was
179 hung from a hoist for vertical position adjustment and was manoeuvred horizontally by hand in
180 order to fill the centrifuge container. The nozzle of the hopper contains a plate with a single hole,
181 the size of which controls the flow rate of the sand. Calibration tests were carried out using two
182 separate nozzles with hole diameters of 5 mm and 9 mm, which provided average flow rates of
183 0.239 kg/min and 1.048 kg/min, respectively. Loose samples ($D_{R,L} \approx 50\%$) were prepared using
184 the large nozzle with a pouring height of 0.5 m, while dense samples ($D_{R,D} \approx 90\%$) were made
185 with the small nozzle at 1 m pouring height. It is worthwhile noting that the loose sample falls
186 within the ‘Medium dense’ range ($D_R = 35\% \sim 65\%$) and the dense sample within the ‘Very
187 dense’ range ($D_R = 85\% \sim 100\%$), based on BS EN ISO 14688-2 (2004). Layered samples with
188 different sand densities were prepared in the similar manner by changing the nozzle and hopper
189 height during sample preparation.

190

191 [Table 1 about here.]

192 [Table 2 about here.]

193 **3 Results and Discussion**

194 This section presents results obtained from the experiments described in the previous section.
195 Penetration resistance and soil deformation data are presented according to the schematic given
196 in Fig. 3, which also provides an illustration of some other geometric and engineering parameters.
197 The cone tip resistance (q_c) was calculated from the cone tip load, Q_{tip} , (from strain gauge data)
198 divided by the base area (A_b). The total pile load, Q_{total} , was obtained from the load cell at the
199 top of the probe. The depth of penetration is denoted as ‘ z ’, soil horizontal and vertical displace-
200 ments are referred to as Δx and Δy respectively, and ‘ h ’ represents the vertical position of a soil
201 element relative to the probe shoulder. All results in this paper are presented in model scale, and
202 compression positive notation is used for the derived strains.

203

204 [Fig. 3 about here.]

205 **3.1 Penetration resistance**

Fig. 4a provides the development of cone tip resistance q_c with penetration depth for each centrifuge test. As mentioned earlier, the strain gauge data from the half-probe proved to be unreliable, hence the cone tip resistance data presented here is from the full-probe. For penetration in soil with uniform density (T02 and T03), q_c generally increases linearly with z , and the rate at which resistance increases with depth is considerably greater in the uniform dense soil (T02) compared to the uniform loose soil (T03). Bolton et al. (1993), based on the dimensional analysis of CPT results from centrifuge tests and the observed linear relationship between the tip resistance (q_c) and vertical effective stress (σ'_{v0}), proposed the normalised tip resistance, Q , given by

$$Q = \frac{q_c - \sigma'_{v0}}{\sigma'_{v0}} \quad (1)$$

206 The linear relationship between q_c and z in Fig. 4a indicates that the normalised
 207 tip resistance Q is more appropriate for centrifuge penetration tests with a linear
 208 stress gradient compared to the non-linear relationships between q_c and σ'_{v0} obtained
 209 from calibration chamber tests, where $q_c \propto \sigma'_{v0}^{-0.5}$ is typically obtained (Robertson
 210 and Wride, 1998; Jamiolkowski et al., 2003). The variation of Q with normalised
 211 penetration depth, z/B , is shown in Fig. 4b. Ideally, the tests would have been
 212 taken to a greater soil depth and soil interfaces located where the variation of Q with
 213 depth remains constant, however this was not possible with the available experimen-
 214 tal equipment. This issue does not impact significantly on the conclusions of this
 215 analysis since the focus is on the transition of behaviour around the interfaces rather
 216 than the absolute values of resistance.

217

218 [Fig. 4 about here.]

219 For layered soil tests, the $q_c - z$ profiles in Fig. 4a show a change in trend (slope) near
 220 the soil interfaces. This transition zone is defined as the distance from the cone tip to
 221 the soil layer interface when the resistance trend changes. This occurs when the probe
 222 is either affected (tip moving towards interface) or is no longer affected (tip moving
 223 away from interface) by the soil in the adjacent layer. The size of the transition zone
 224 depends on the relative soil properties in the soil layers involved. It was found that
 225 the transition zones in dense sands were much larger than that in loose sands. For
 226 example, from Fig. 4a, for the test from loose to dense sand (T04), penetration resis-
 227 tance sensed the lower dense sand layer at about $1B$ above the soil interface, whereas
 228 it took about $4B$ below the interface to fully develop the resistance in the dense sand.

229

230 It should be noted that the density of the samples in each test is not exactly iden-
 231 tical, especially for the loose sands. From calibration tests for sand pouring, the
 232 variations of D_R were $90\% \pm 5\%$ for dense sand and $50\% \pm 10\%$ for loose sand. Sample
 233 inhomogeneity made it difficult to obtain repeatable resistance data. For example,
 234 comparing results of T03, T04 and T06, the data in Fig. 4a indicate that the loose
 235 sand in T04 was looser than T03, while for T06 the upper loose soil was relatively
 236 higher than T03. For this reason, little focus is placed on the absolute values of
 237 penetration resistance and emphasis is placed on transitional behaviour around the
 238 interfaces.

239

240 In order to quantify the transition of q_c between soil layers, the cone tip resistance
 241 ratio η , proposed by Xu and Lehane (2008), was defined as $\eta = q_c/q_{c,s}$. For the
 242 scenario of penetration from weak soil into strong soil, the value of η varies from
 243 $\eta_{min} = q_{c,w}/q_{c,s}$ in the weak soil to $\eta = 1$ in the strong soil. Note that $q_{c,w}$ and $q_{c,s}$
 244 represent the resistances in uniform weak and strong soil, respectively. In view of
 245 the good agreement of tip resistance in the upper dense sand layer in tests T02, T05,
 246 and T07 illustrated in Fig. 4a, the result of T02 was used as a reference in the strong
 247 soil ($q_{c,s}$) to evaluate the resistance ratio for layered soil tests. The resistance ratio
 248 curves against the relative distance to the soil interface (z_i/B) are presented in Fig. 5.

249

[Fig. 5 about here.]

250

Fig. 5a and b show the results of cone tip resistance ratio for two-layered soils
 (T04 and T05). Xu and Lehane (2008) performed a series of numerical analyses of
 spherical cavity expansion to evaluate layered effects on the resistance of piles and
 penetrometers. According to their parametric study and validation against centrifuge
 tests, they proposed the following relationship for resistance ratio:

$$\eta = \eta_{min} + (1 - \eta_{min}) \exp[-\exp(A_1 + A_2 \times z_i/B)] \quad (2)$$

251

where $A_1 = -0.22 \ln \eta_{min} + 0.11 \leq 1.5$ and $A_2 = -0.11 \ln \eta_{min} - 0.79 \leq -0.2$. The compar-
 252 isons of Equation (2) with the current centrifuge results are also provided in Fig. 5a
 253 and b, where the value of η_{min} for the Xu and Lehane (2008) line was taken as the
 254 resistance ratio obtained using q_c from tests T03 (uniform loose) and T02 (uniform
 255 dense) at the soil interface (i.e. $q_{c,min} = q_{c,T03}/q_{c,T02}$, where the subscripts denote the
 256 test ID). The small difference in $q_{c,min}$ in Fig. 5a and b is due to the slight variation
 257 in interface depth in tests T04 and T05. The experimental data in Fig. 5a should
 258 tend towards $\eta = 1$ at high vales of z_i/B ; the reason this does not occur is evident
 259 from the difference in q_c data for tests T04 and T02 in Fig. 4a, where the T04 data
 260 does not tend towards the T02 data at depth as would be expected. As a result, the

261 agreement between the test T04 data and the Xu and Lehane (2008) prediction in
 262 Fig. 5a is not very good in terms of the absolute value of resistance ratio, however the
 263 trend and size of the influence zone are both similar. The high values of resistance
 264 ratio (greater than 1) for $z_i/B < -5$ in Fig. 5b are a result of the small values of q_c
 265 used in the calculation of η nearer the ground surface; the agreement between q_c in
 266 the dense soil layer in tests T05 and T02 was actually quite good (see Fig. 4a). So
 267 one could assume that the experimental data tended towards $\eta = 1$ at this location,
 268 thereby giving a good overall agreement with the Xu and Lehane (2008) prediction.

269
 270 Also included in Fig. 5 are predictions of resistance ratio using the Mo et al. (2014a,b)
 271 method for interpretation of CPT data in layered soils. This method involves the
 272 prediction of the transition of penetration resistance in layered soils using analytical
 273 solutions for expanding cavities embedded in two different cohesive-frictional mate-
 274 rials. For the analytical prediction, soil model parameters were determined based
 275 on the relative density of the soil ($D_R = 50\%$ and $D_R = 90\%$) using the relation-
 276 ships of Bolton (1986) and Randolph et al. (1994). The in-situ confining pressure
 277 for cavity expansion analysis was assumed as the effective vertical stress at the lo-
 278 cation of the soil interface. The approach of Yasufuku and Hyde (1995) was applied
 279 to correlate the cavity pressure to cone resistance. A full description of the analyt-
 280 ical methodology is not possible here; readers may refer to (Mo, 2014) for full details.

281
 282 In Fig. 5a and b, the Mo (2014) prediction is shown to give a larger value of η_{min} than
 283 both the experimental and the Xu and Lehane (2008) values, but again the size and
 284 trend of the influence zone are predicted well. It should be noted that the value of
 285 η_{min} in the Mo (2014) prediction are independent of the experimental measurements
 286 of q_c , whereas the Xu and Lehane (2008) value of η_{min} was based on data from tests
 287 T03 and T02, as described above. It is therefore not surprising that the Mo (2014)
 288 predictions do not agree as well with the experimental data as the ones using Xu and
 289 Lehane (2008).

290
 291 The curves of cone tip resistance ratio for thin-layered soils (T06 and T07) are
 292 shown in Fig. 5c and d, where t is the thickness of the sandwiched soil layer and
 293 $\eta = q_{c,T06}/q_{c,T02}$ in Fig. 5c and $\eta = q_{c,T07}/q_{c,T02}$ in Fig. 5d. A smaller change in η across
 294 the thin layer indicates a greater thin-layer effect, since a value of η that approaches
 295 either 1.0 for a thin strong layer (Fig. 5c) or η_{min} for a thin weak layer (Fig. 5d)
 296 indicates that the penetration resistance in the thin layer approaches a value typical
 297 of a continuous layer of soil. In Fig. 5c, the experimental data of η at low values of
 298 $z_i/B < 0$ should tend towards a value of η_{min} which, based on test T04, should have

299 been about 0.4. From Fig. 4a, it is clear that the values of q_c in test T06 at shallow
300 depths are much greater than the uniform loose test T03, resulting in the very high
301 values of η in Fig. 5c. This may be due to some densification of the soil during
302 model package preparation. In Fig. 5d, the high values of η at shallower depths are
303 a result of the small values of q_c used in the calculation of η , as was the case for the
304 data in Fig. 5b. Considering these points, the experimental data in Fig. 5c and d
305 give a reasonably good idea of the transitional response of penetration resistance in
306 thin-layered soils.

307

308 Included in Fig. 5c and d are predictions based on the methodology of Vreugdenhil
309 et al. (1994), which gives an approximate analysis for interpretation of cone penetra-
310 tion results in multi-layer soils by representing a CPT using a circular uniform load.
311 To apply the Vreugdenhil et al. (1994) elastic solution for comparison with the ex-
312 perimental data, a stiffness ratio (G_w/G_s) is required to describe the transition curve,
313 which was assumed to be equal to the resistance ratio ($G_w/G_s = q_{c,w}/q_{c,s}$) obtained us-
314 ing the data from tests T03 (*weak, w*) and T02 (*strong, s*) at a depth midway between
315 the two soil interfaces in tests T06 and T07. The agreement between the Vreugdenhil
316 et al. (1994) predictions and the experimental data are shown to be good, though as
317 for the Xu and Lehane (2008) predictions, the evaluation of η_{min} was based on the
318 experimental data from tests T02 and T03 and was therefore not made independently.

319

320 The Mo (2014) analysis approach may also be used to evaluate the trend of penetra-
321 tion resistance in a thin soil layer. Results obtained using this method are included in
322 Fig. 5c and d. In this analysis, the in-situ confining pressure for the cavity expansion
323 analysis was assumed as the effective vertical stress at a depth mid-way between the
324 two soil interfaces. As for the two-layered soils, the method over-predicts the value
325 of η_{min} but provides a good evaluation of the size of the transition zone and a realistic
326 smooth transition of penetration resistance in multi-layered soils.

327

328 Also included in Fig 5c are values based on field data for a thin layer of strong soil
329 provided by Youd and Idriss (2001). Empirical equations were used to evaluate the
330 correction factor K_H ($= q_{c,s}/q_{c,max}$, proposed by Robertson and Fear, 1995 to correct
331 the cone resistance from the field measurements) with the thickness of the strong
332 layer (t/B). For $t/B = 5.42$ in T06, the correction parameter K_H varies from 1.51
333 to 1.82, and the corresponding maximum value of η is within the range of 0.550 to
334 0.662. This range of maximum value of η is less than the results of the centrifuge test
335 and the analytical solutions, indicating that this empirical method predicts a greater
336 thin-layer effect.

338 3.2 Soil displacements

339 This section presents distributions of displacements associated with the installation of probes under
 340 axisymmetric conditions in uniform as well as layered soils. The distributions of soil deformation
 341 around the penetrometer provide insights into the mechanisms that are responsible for the probe
 342 resistance data presented in the previous section. Using the GeoPIV analysis (White et al., 2003),
 343 soil element patches were created by meshing within the field of view in image-space. A patch size
 344 of 80 pixels was used which represents a nominal size of $2 \sim 3 \text{ mm}$ in object space, according to a
 345 particular transformation. The raw GeoPIV data was interpolated to a regular soil mesh in the
 346 ‘x-y’ system (see Fig. 3b) with a grid spacing of $1 \times 1 \text{ mm}$ ($x = -6 \sim -120 \text{ mm}; y = 0 \sim 200 \text{ mm}$),
 347 as well as the process of penetration with 1 mm per step. Also, strains were deduced from the
 348 displacements based on this re-established mesh. **[Reply 3-29] The results of uniform sand**
 349 **tests (T02 and T03) are presented first in this section to illustrate the effects of penet-**
 350 **ration depth and the relative density of the soil.** These data also serve as reference for later
 351 investigation of layered effects on soil deformation. **It should be recognised that the displace-**
 352 **ment data was obtained at the soil-Perspex interface and is therefore subject to the**
 353 **effect of boundary friction on displacements. One could expect that some ‘slip-stick’**
 354 **behaviour may have occurred, which would cause some spatial variation in the dis-**
 355 **placement data. Finally, the sample preparation for these tests induced some sample**
 356 **inhomogeneity which may also have caused some variation in observed displacements.**

357

358 Fig. 6 presents distributions of displacements at the depth of the probe shoulder ($h = 0$) with
 359 offset from the centreline of the probe ($2x/B$) when the probe is at different depths within the soil:
 360 **[Reply 3] $z/B = 2.5$ to 12.5 (z/B is the normalised penetration depth). The horizontal**
 361 **and vertical displacements ($2\Delta x/B$; $2\Delta y/B$) are also normalised by B and represent**
 362 **cumulative values for $h < 0$, which means that the displacements are those that oc-**
 363 **curred from $z/B = 0$ (initial state) up to the stated penetration depth.** Both lateral and
 364 vertical (downwards) displacements are shown to decrease exponentially with horizontal distance
 365 from the probe shoulder. This trend is comparable to the results of cavity expansion analysis,
 366 as has been noted by several other authors (e.g. Hird et al., 2007; Liu, 2010). The curves also
 367 illustrate the decay of the influence of the probe on distant elements. The horizontal size of the
 368 influence zone during penetration is $2x/B \approx 10$ for dense sand, and slightly smaller for loose sand
 369 ($2x/B \approx 7$). **For soil elements near the surface, displacements increase with depth,**
 370 **and negative values of $2\Delta y/B$ in dense sand illustrates heave at the surface.**

371

372

[Fig. 6 about here.]

373 Fig. 7 presents ‘instantaneous’ total displacement ($=\sqrt{\Delta x^2 + \Delta y^2}$) fields for the uniform dense
374 and loose sand tests. The term ‘instantaneous’ refers to the displacements that developed over an
375 interval of penetration distance, Δz , (e.g. $\Delta x|_{\Delta z} = \Delta x|_{z+\Delta z/2} - \Delta x|_{z-\Delta z/2}$) and may be used to
376 represent the velocity field at a given penetration stage. This type of plot is useful for illustrating
377 the mechanism of deformation at a given stage of penetration. Fig. 7 relates to a penetration
378 interval distance of $\Delta z = 6\text{ mm}$ when the probe was at a depth of 150 mm . The contours are
379 superimposed with displacement vectors to illustrate the direction of movement throughout this
380 interval. The contours are plotted only for values from 0.05 to 1.5, and the vectors were elimi-
381 nated for displacements less than 0.1 mm , which represent soil that hardly deformed during the
382 penetration interval. It may be observed that the influence zone in the instantaneous total dis-
383 placement field is a bulb around or a bit ahead of the cone tip. Soil elements adjacent to the probe
384 shaft show little deformation, which is mainly caused by the shaft friction. During this interval,
385 the soil in this bulb is displaced horizontally and vertically, and the displacement vectors grow
386 radially, which seems comparable to a spherical cavity expansion. Intuitively, the failure mode
387 is very similar to that proposed by Lee (1990), where zone III (a spherical zone below the probe
388 shoulder) is the spherical cavity expansion zone based on Vesic (1977). This phenomenon also
389 supports the analyses of the correlation between cone penetration and spherical cavity expansion
390 (e.g. Randolph et al., 1994; Yu and Mitchell, 1998; Gui and Jeng, 2009).

391
392 The displaced zone in the loose sand is smaller (i.e. the displacement is concentrated closer to the
393 cone tip) than in the dense sand. More downwards movements are observed in the loose sand
394 than the dense sand, whereas dense sand tends to have more lateral displacement than the loose
395 sand. It is also notable that the upper boundary of the influence zone in the dense sand is close
396 to an inclination line at 60° from vertical, whereas the loose sand has a boundary that inclines at
397 approximately 45° from vertical.

398

399 [Fig. 7 about here.]

400 The mechanism of soil deformation may also be studied by considering the path or trajectory
401 of a given soil element as it is affected by the probe. Fig. 8 shows trajectories of soil elements
402 at different offsets ($2x/B = 2, 3, 4, 5, 6$) from the probe and at a depth of $y = 120\text{ mm}$ which
403 were recorded as the probe approached and passed this horizon (up to a penetration distance of
404 $z = 160\text{ mm}$). Initially, the soil is shown to deform mainly downwards as a result of the probe,
405 however as the probe approaches closer to $y = 120\text{ mm}$, the soil elements begin to move laterally
406 (the state when the probe shoulder reaches $y = 120\text{ mm}$ is shown on the figure with a ‘ Δ ’ denoting
407 $h = 0$). The final state of the soil elements is marked by a ‘*’ and the 1:1 line between radial
408 and axial movement ($\Delta x : \Delta y$) is also shown on the figure as a dashed line. The final horizontal
409 displacement of the dense sand is generally a little larger than the vertical displacement; the final
410 position falls to the right of the 1:1 line. For the loose sand, the vertical displacement is observed

411 to be slightly larger than the horizontal displacement at the final state. The magnitude of dis-
412 placements within the loose sand is also observed to be smaller than in the dense sand. The ratio
413 between the total displacement at the final state of the soil elements in the loose and dense sands
414 decreases from 64% at $2x/B = 2$ to 33% at $2x/B = 6$.

415

416 In Fig. 8, the major proportion of displacement is noted to occur during the stage when $h < 0$
417 (i.e. as the probe approaches the horizon of the soil element), and little contribution is made when
418 $h > 0$ (after the probe shoulder passes). The displacement in the stage when $h > 0$ indicates
419 soil movements away from the probe, which is in contrast with observations by White (2002) who
420 showed that the direction of movement reversed back towards the pile at a magnitude of about 1%
421 of pile diameter. This led to the conclusion that soil stresses in the region above the probe shoul-
422 der were relaxed and that consequently shaft frictional forces were reduced. The data presented
423 here also shows a reversal of displacements near the probe shoulder of approximately 1% of the
424 pile radius, however it is noted to occur during the stage immediately before the probe shoulder
425 reaches the horizon of the soil element ($-0.5 < h/B < 0$). This difference is probably due to the
426 differing boundary conditions, where the tests here were axisymmetric with a conical tip and the
427 tests reported by White (2002) were plane-strain with a flat-bottomed probe. A comparison of
428 the trends and the magnitude of soil deformation between the two types of models is discussed
429 later in Section 3.3.

430

431

[Fig. 8 about here.]

432 Fig. 9 is an alternative view of the soil element path during penetration which gives an illustration
433 of the soil element distortions that occur during the probe penetration process. The soil elements
434 near the probe are described as $1\text{ mm} \times 1\text{ mm}$ squares. The deformed square elements at different
435 distances from the probe centreline indicate the deformation and distortion patterns within the
436 soil. After the original element is plotted with a 'o', the same element is superimposed every 5 mm
437 of penetration, and the final patch is marked with a '*'. The series of soil element patches record
438 the shape of the deformed elements and allow comparison of the element paths between dense and
439 loose sand tests. The deformed shape of the soil elements is noted to be more severe in the dense
440 soil than in the loose soil. The distortion of the soil elements is considered further in the next
441 section which examines soil strains.

442

443

[Fig. 9 about here.]

444 Layered effects on soil displacements

445 This section presents axisymmetric centrifuge experiment data of the effects of layering on soil
446 displacements. This type of data provides valuable insight into the mechanisms of soil behaviour

447 during penetration problems and has not been provided previously within the literature. This
448 section focuses on the results of soil deformation for tests with layered soils (T04 to T07).

449

450 The profiles of normalised cumulative vertical displacements ($2 \Delta y/B$) for soil at an
451 offset of $2x/B = 2$ in the uniform and layered sand tests are provided in Fig. 10. From
452 the results of $2 \Delta y/B$ in loose over dense sand (T04 in Fig. 10a), the peak above the
453 interface occurs at around $2B$, where the penetration resistance starts to be affected.
454 The influence zone beneath the interface is not as obvious due to the smooth nature
455 of the curves, however the data tends to level off at about $5B$ from the interface,
456 which is close to the value of $z_s = 4B$ from the penetration resistance data in Fig. 5a.
457 For the test with dense over loose sand (T05 in Fig. 10b), the peak occurs at the
458 interface, and it is not possible to define an influence zone in the strong overlying
459 soil due to the cumulative soil deformation. Comparing the result with the trend of
460 dense sand in T02, the soil starts to be affected at about $5B$ above the loose sand
461 layer. The influence zone in loose sand appears to be about $4B$, based on the point
462 at which the Δy profile levels out. The thin-layer effects on soil displacements for
463 T06 and T07 are also presented in Fig. 10 and compared against the corresponding
464 2-layer test as well as the uniform soil tests. For test T06, the vertical displacement
465 in the sandwiched dense layer increases steadily and reaches a maximum value just
466 above the dense-loose soil interface. For test T07, the vertical displacement decreases
467 steadily within the sandwiched loose sand layer and reaches a minima just above the
468 loose-dense soil interface. Comparing the influence zones in soil deformation with
469 that in penetration resistance, it is found that the sizes are different but correlated.
470 Due to the limited tests in this paper, further study on the penetration mechanisms
471 is required to investigate the relationship between the layered effects on both pene-
472 tration resistance and soil deformation.

473

474 [Fig. 10 about here.]

475 3.3 Soil strains

This section presents soil strains which were derived from the incremental displacement data introduced in the previous section. The calculation of strains was done by importing the measured displacement fields into a corresponding mesh within the finite difference software FLAC (Itasca, 2005) for each step of penetration, as suggested by Marshall (2009). Based on the axisymmetric condition of the experiments with Cauchy's infinitesimal strain tensor and a small deformation

assumption, the strains were calculated using:

$$\begin{aligned} \epsilon_{xx} &= -\frac{\partial \Delta x}{\partial |x|} & \epsilon_{yy} &= -\frac{\partial \Delta y}{\partial y} & \epsilon_{xy} &= -\frac{1}{2} \left(\frac{\partial \Delta x}{\partial y} + \frac{\partial \Delta y}{\partial |x|} \right) \\ \epsilon_{\theta\theta} &= -\frac{\Delta x}{|x|} & \epsilon_{x\theta} &= \epsilon_{y\theta} = 0 & \epsilon_{volume} &= \epsilon_{xx} + \epsilon_{yy} + \epsilon_{\theta\theta} \end{aligned} \quad (3)$$

476 The Mohr circle of strains in the ‘x-y’ plane is illustrated in Fig. 11a. Some smoothing was ap-
 477 plied to the strain data presented in this section in order to deal with the amplification of scatter
 478 obtained when calculating strains from the GeoPIV displacement data.

479

480 Fig. 11c-d shows the instantaneous strain fields with magnitude and direction of principal strain
 481 rate at a penetration depth of $z = 150 \text{ mm}$ **[Reply 3-39] and resulting from a probe dis-**
 482 **placement increment of 6 mm (i.e. $\epsilon|_{\Delta z} = \epsilon|_{z+\Delta z/2} - \epsilon|_{z-\Delta z/2}$).** The principal strain rates
 483 of $\dot{\epsilon}_1$ and $\dot{\epsilon}_2$ from the ‘x-y’ plane (refer to Fig. 11b) are shown, where $\dot{\epsilon}_1$ is compression and $\dot{\epsilon}_2$
 484 tension. The magnitude of strain rate is illustrated by the size of the crossing lines (a standard
 485 length for 10% strain rate is given in the plots). The main principal strain rate is directed from
 486 the cone tip, and decays significantly with relative distance. Despite the fact that sand is known
 487 to behave in a non-coaxial manner, the large strain around the probe cone leads to a reduced effect
 488 of non-coaxiality (Roscoe, 1970). Hence the directions of the principal strain rate provides some
 489 clues for estimation of directions and distributions of the principal stress rate. The directions of
 490 the principal strain rate between dense and loose sand are observed to be similar, with slightly
 491 smaller inclination from vertical for the loose sample.

492

493

[Fig. 11 about here.]

494 Strain paths shown in Fig. 12 reveal the evolution of strains (ϵ_{xx} , ϵ_{yy} , ϵ_{xy} , ϵ_{volume} , $\epsilon_{\theta\theta}$, ϵ_1 , ϵ_2)
 495 during probe installation. The strain histories are plotted against the relative position from the
 496 probe shoulder (h/B) for soil elements in the near field ($2x/B = 2$) at a depth of 120 mm for
 497 both dense and loose sand tests. The majority of the strain is shown to develop before the probe
 498 shoulder passes, and the strain remains nearly constant when $h > 0$.

499

500

[Fig. 12 about here.]

501 In Fig. 12, the strain reversal of ϵ_{xx} and ϵ_{yy} occurs before the probe shoulder passes. With pene-
 502 tration, ϵ_{xx} gradually drops to a minimum at $h/B \approx -2$, which is slightly earlier than when ϵ_{yy}
 503 reaches its maximum, followed by the phase of strain reversals. The strains change direction and
 504 reach an opposite peak at $h/B \approx -0.5$. The location where these two curves intersect suggests
 505 that the relatively small compressive strains (ϵ_{xx} and ϵ_{yy}) occur at $h/B \approx -1$, where ϵ_{xy} grows
 506 sharply to its maximum value. The value of shear strain in dense sand is larger than that in loose
 507 sand, which is also in accordance with the distorted soil element patches shown in Fig. 9. There
 508 is no obvious difference in the strain reversal for both dense and loose sand. The sensing distances

509 of ϵ_{xx} and ϵ_{yy} are shown to be about $8B$ in the dense sand and $5B$ in the loose sand. These
510 sensing distances may be compared to the influence zones in layered soils determined earlier from
511 the penetration resistance data. It was noted that the influence zone in dense soil was larger than
512 in loose soil, which agrees with the sensing distances determined from Fig. 4.

513

514 The phase from $h/B = -0.5$ to 0 exhibits a small proportion of strain reduction, which is most
515 notable in the ϵ_{xy} data for the dense sand. The two principal strains (ϵ_1 and ϵ_2) represent the
516 size of the Mohr circle in the 'XY' plane. Extensive $\epsilon_{\theta\theta}$ is the minimum principal strain and
517 continuously grows until the probe almost reaches the soil element horizon. Consequently, the
518 negative volumetric strain indicates the dilatant behaviour of the soil near the probe, whereas the
519 final state of loose sand appears to have nearly no dilation; this can be attributed to the relatively
520 high compressive ϵ_{xx} values in Fig. 12b.

521

522 The phenomenon of strain reversal discussed above was also reported by Baligh (1985) and
523 White and Bolton (2004). However, the former was an analytical solution that is only suit-
524 able to undrained clay and the latter was from calibration chamber tests in a plane-strain model.
525 The strain data from the axisymmetric model presented here, and in particular the strain reversal
526 behaviour illustrated in Fig. 12, are most applicable to conventional penetration problems in sand.

527

528 The variation of ϵ_{volume} with offset from the probe centreline is shown in Fig. 13 for $y = 150\text{ mm}$.
529 The eventual state of ϵ_{volume} also indicates the distribution of density after penetration. For dense
530 sand, the soil elements at $2x/B = 2 \sim 4$ show a peak dilation when the probe is just above the
531 soil element horizon ($h/B = -1 \sim -2$), followed by a quick transition to a final dilative state.
532 For the soil elements further away, there is a general increase in volumetric strain towards the
533 ultimate contractive state value. For the loose soil, there is no systematic trend in final volumetric
534 strain with offset. All the soil elements illustrate a final contractive state and the magnitude of
535 contractive volumetric strain is generally higher compared to the dense soil.

536

537

[Fig. 13 about here.]

538 The effect of the axisymmetric condition of the tests conducted as part of this project are illus-
539 trated in Fig. 14 by comparing soil strains against results from plane-strain tests reported by
540 White (2002). The tests conducted by White (2002) used a 32.2 mm plane-strain probe and a
541 calibration chamber with Fraction B silica sand, which is a larger grading of the same silica sand
542 used in these tests (D_{50} of Fraction B is 0.84 mm whereas it is 0.14 mm for Fraction E). The
543 ratio of probe diameter to average grain size (B/d_{50}) for the tests reported by White (2002) was
544 86 , whereas it was 38 for the centrifuge tests. All of the soil elements were selected at a similar
545 distance from the probe centreline ($2x/B = 2$ and 1.99). The data for the axisymmetric test
546 was taken at a depth of 120 mm with an initial vertical stress of 90 kPa , while the data from the

547 plane-strain test was under an isotropic stress condition of approximately 50 kPa .

548

549 Fig. 14 shows the horizontal and vertical strain at $2x/B = 2$ for the two test configurations.
550 The data shows that, compared to the axisymmetric test, the plane-strain test illustrated higher
551 vertical compressive strains before the probe passed the soil element and that the peak vertical
552 strain occurred earlier. Horizontal strains were considerably larger in the plane-strain test during
553 the stage when the probe approached the soil element, and ultimately stayed in a tensile state
554 whereas they went to a compressive state in the axisymmetric test. The higher horizontal strains
555 in the plane-strain tests can be attributed to the fact that the degree of freedom of the soil in
556 the out-of-plane direction is restricted in these tests, therefore the in-plane horizontal and vertical
557 strains respond to a greater degree due to the probe penetration. As a direct consequence of this,
558 the sensing distance for the plane-strain test is greater than the axisymmetric test, as indicated
559 in Fig. 14 where the strains begin to change at about $-10B$ for the plane-strain test and $-8B$
560 for the axisymmetric test.

561

562

[Fig. 14 about here.]

563 Layered effects on soil strains

564 The results of soil strains for the tests with layered soils are presented in this section. As shown
565 in Fig. 13, the volumetric strains are relatively dilative in dense sand and contractive in loose
566 sand. Fig. 15 shows the results of volumetric strain paths for soil elements at $2x/B = 2$ with
567 variation of distance to the soil interface for the 2-layered soil tests. The strain paths far away
568 from the interface have similar trends to those from the uniform tests. For the loose over dense
569 test (Fig. 15a), a transition of the trends from characteristically loose to dense occurs. For the
570 dense over loose test (Fig. 15b), there is also a transition of the trends, however the data obtained
571 when the probe was at the interface ($y = y_{int}$) shows somewhat unexpectedly high values of con-
572 traction which are not fully understood and may be a result of errors associated in the calculation
573 of strains. The transition zones for both tests are within a distance of about $2B$ from the interface.

574

575

[Fig. 15 about here.]

576 Fig. 16 provides the cumulative volumetric strain profiles for $2x/B = 2$ after 160 mm of pene-
577 tration. The ultimate value of ϵ_{volume} after the probe has passed a given location is about 0%
578 in loose sand and approximately -6% in dense sand. **[Reply1-12] The variation of the data**
579 **within the uniform soil tests is attributed to the issues identified earlier, namely the**
580 **effects of boundary friction, the scatter in the PIV data and its effect on calculated**
581 **strains, and the soil inhomogeneity caused by sample preparation.** For the layered tests,
582 there is a transition of ϵ_{volume} from these values within a rather small zone which is about $2B$ in

583 size.

584

585

[Fig. 16 about here.]

586 4 Conclusions

587 A series of full- and half-probe cone penetration tests were performed in various configurations of
588 silica sand in a 180° axisymmetric model container. The centrifuge penetration tests, together
589 with soil deformation measurement, provided an effective approach for investigation of penetra-
590 tion mechanisms around the probe. Uniform dense and loose sand tests showed a linear increase
591 of total load and tip resistance with depth. A transition of tip resistance was observed within a
592 zone of influence around the layered soil interfaces. The tip resistance ratio η , proposed by Xu
593 and Lehane (2008), was used to illustrate the transition of q_c from one soil layer to another. The
594 influence zone in stronger soil was larger than that in weaker soil and was also dependant on the
595 direction of probe travel. The characteristics of the influence zone were shown to be important for
596 thin-layer soil profiles where a ‘steady-state’ condition may not be reached within the thin layer,
597 depending on the relative properties of the soil layers.

598

599 The use of spherical cavity expansion methods for analysis of penetration problems was supported
600 by the observation of the instantaneous soil displacement around the cone tip. From the trajecto-
601 ries of soil elements, it was noted that the major proportion of the displacement occurred before
602 the probe passed, and little contribution was made during $h > 0$. In addition, the directions
603 of the principal strain rate provided some clues for estimation of directions and distributions of
604 the principal stress rate. Strain reversal during penetration in the axisymmetric model was also
605 quantified to indicate the severe distortion with rotation and dilation. The results of deformation
606 were also compared with data from White (2002) to examine the effect of particle size and to
607 illustrate the differences between plane-strain and axisymmetric tests.

608

609 The mechanism of deformation of layered soils around the probe was described and highlighted
610 using displacement and strain profiles. The variation of soil displacement with different profiles of
611 soil density illustrated the layering effect on soil displacement mechanisms. The layered effects on
612 soil strains were also investigated through the transitions of the strain paths and distributions of
613 cumulative volumetric strains.

614

615 **List of notation**

616	$\Delta x, \Delta y$	horizontal and vertical displacements
617	ϵ	strain
618	η	pile end bearing resistance ratio, proposed by Xu and Lehane (2008)
619	σ'_{v0}	initial vertical stress
620	A_b	base area of probe
621	B	diameter of penetrometer
622	D	diameter of centrifuge container
623	D_R	relative density of soil
624	d_{50}	grain diameter for which 50% of the sample (by weight) is smaller
625	e	void ratio of sand sample
626	G_s	specific gravity
627	h	vertical position of soil element relative to probe shoulder
628	K_H	correction factor for thin-layer effects
629	Q	normalised cone tip resistance
630	q_c	cone tip resistance
631	Q_{total}, Q_{tip}	total penetration load and tip load
632	t	thickness of sandwiched soil layer
633	x, y	horizontal and vertical locations of soil elements
634	z	depth of penetration
635	z_i	distance to soil interface
636	FOV	field of view
637	GeoPIV	geotechnical Particle Image Velocimetry
638	NCG	Nottingham Centre for Geomechanics

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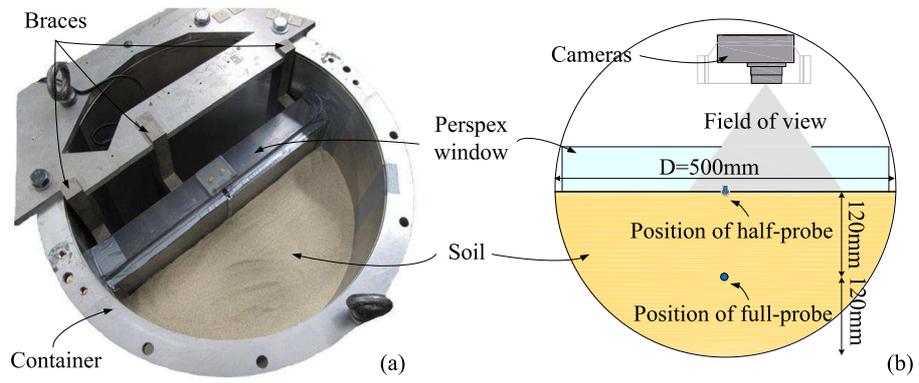


Fig. 1: The centrifuge container with Perspex window

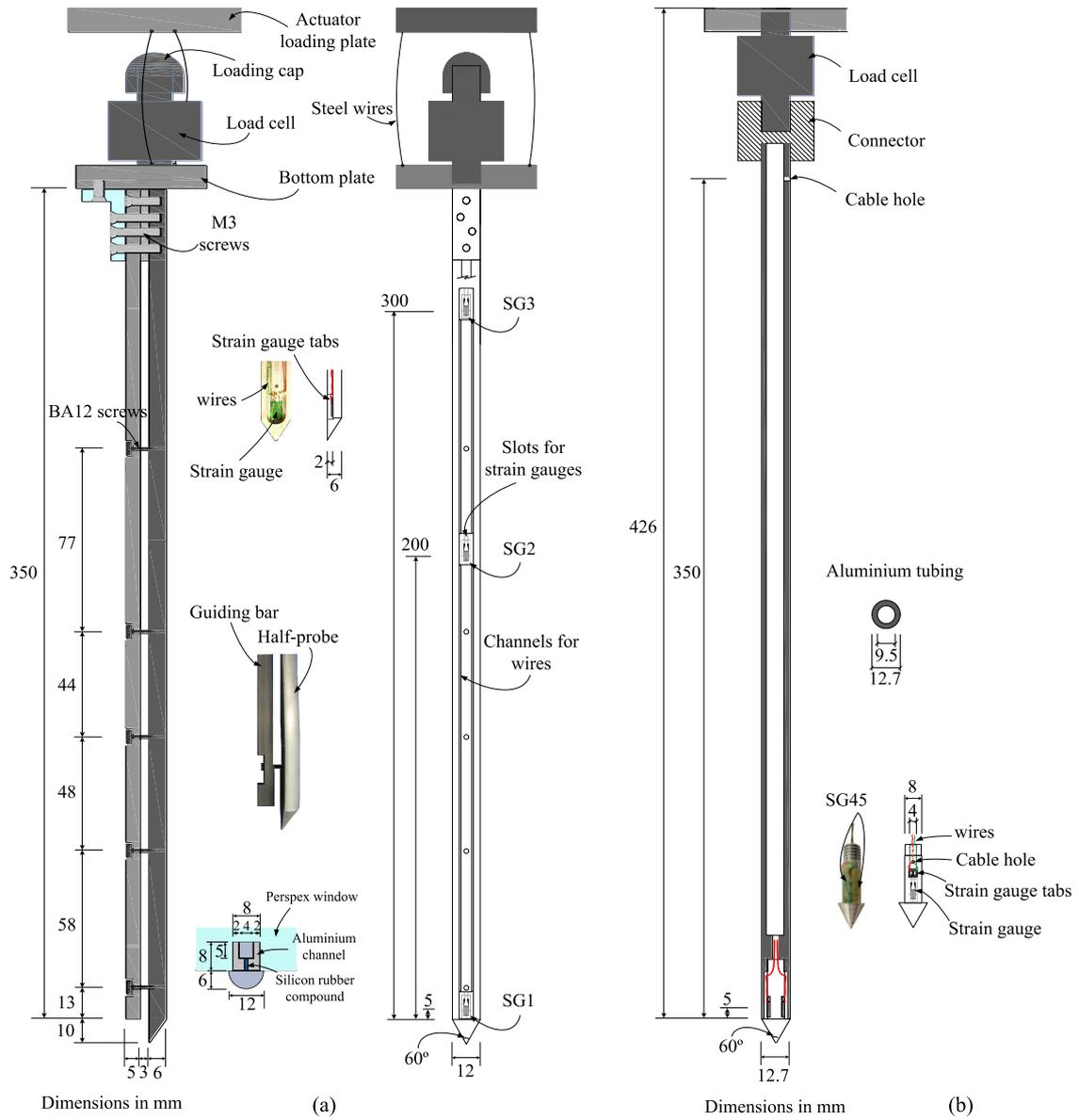


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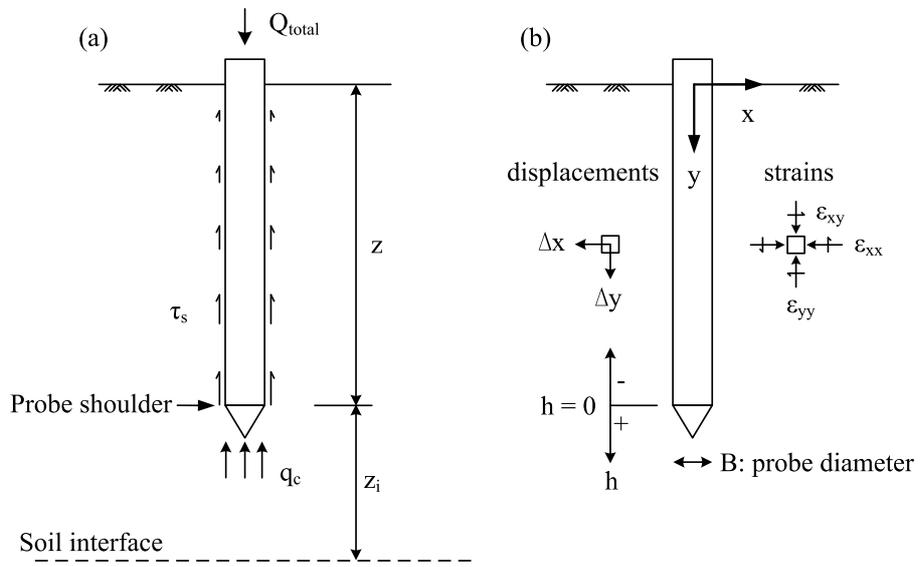


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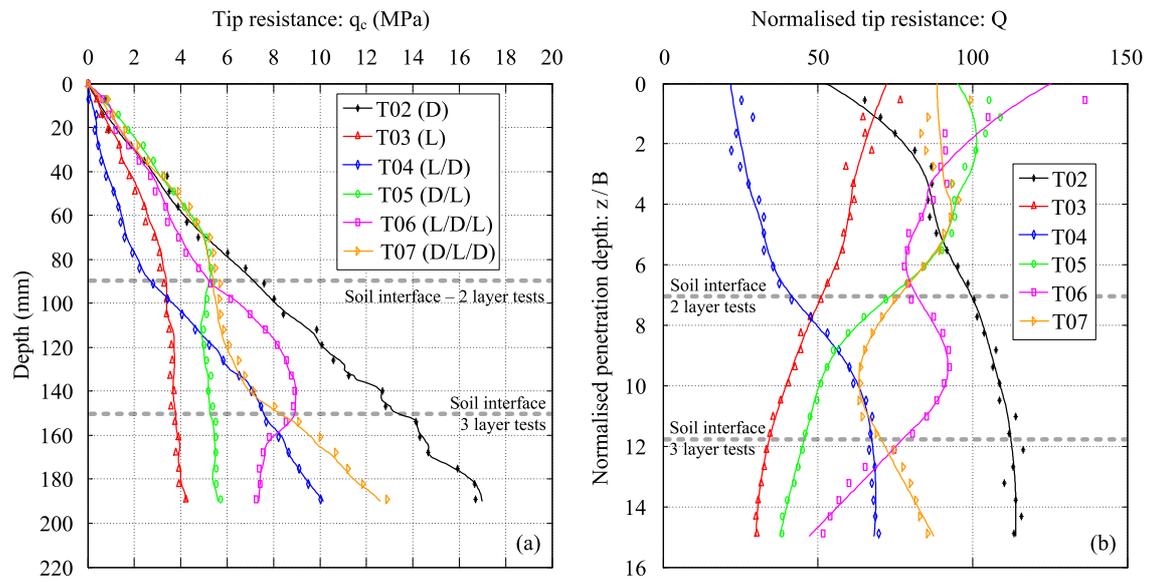


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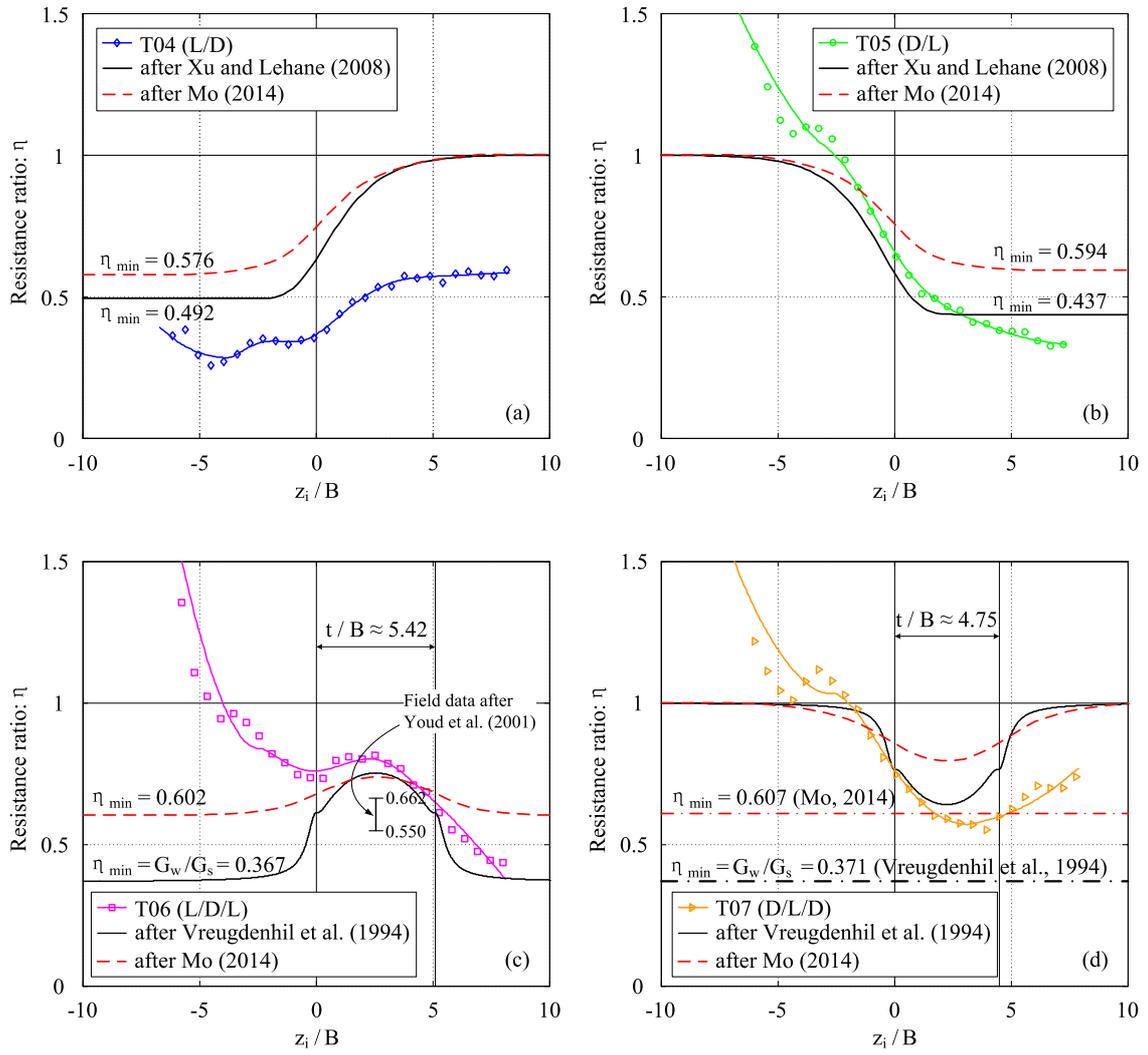


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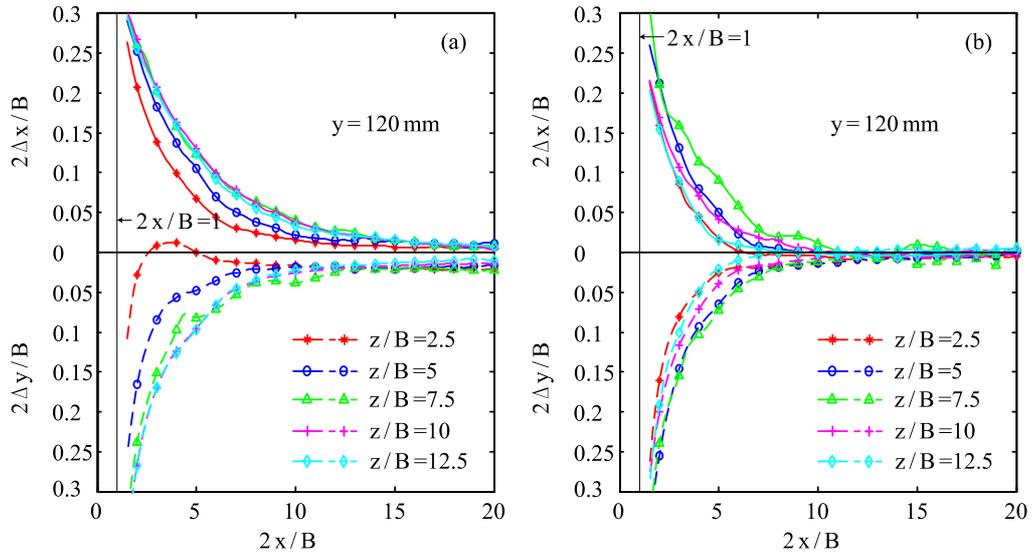


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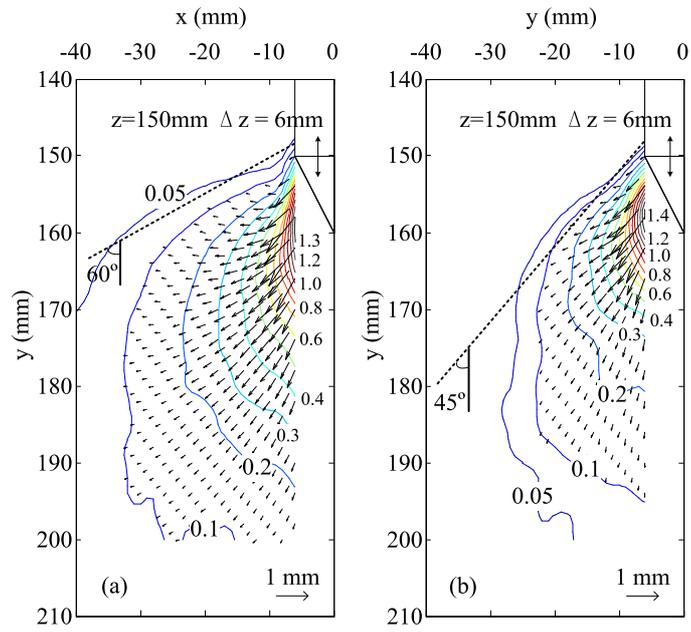


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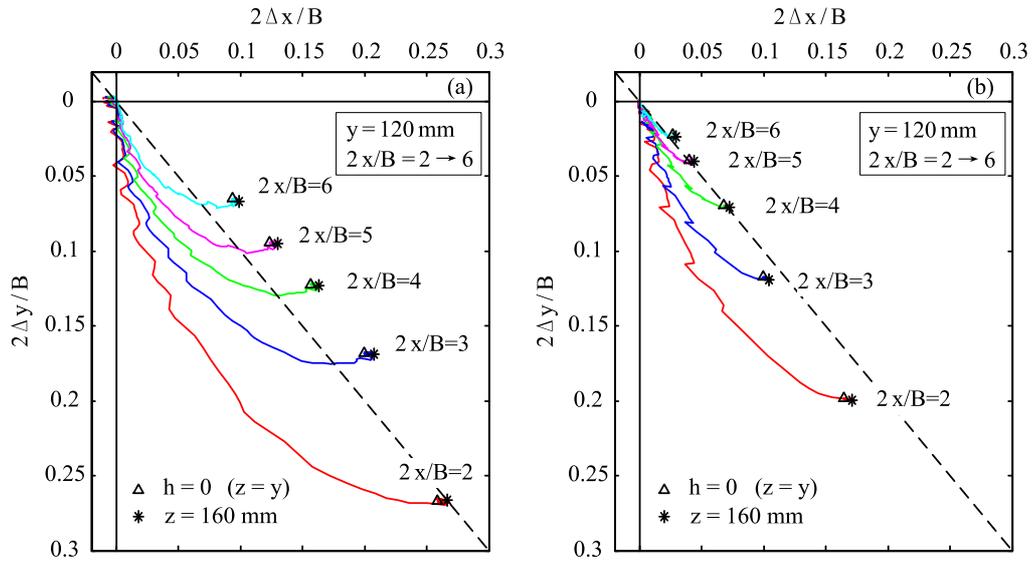


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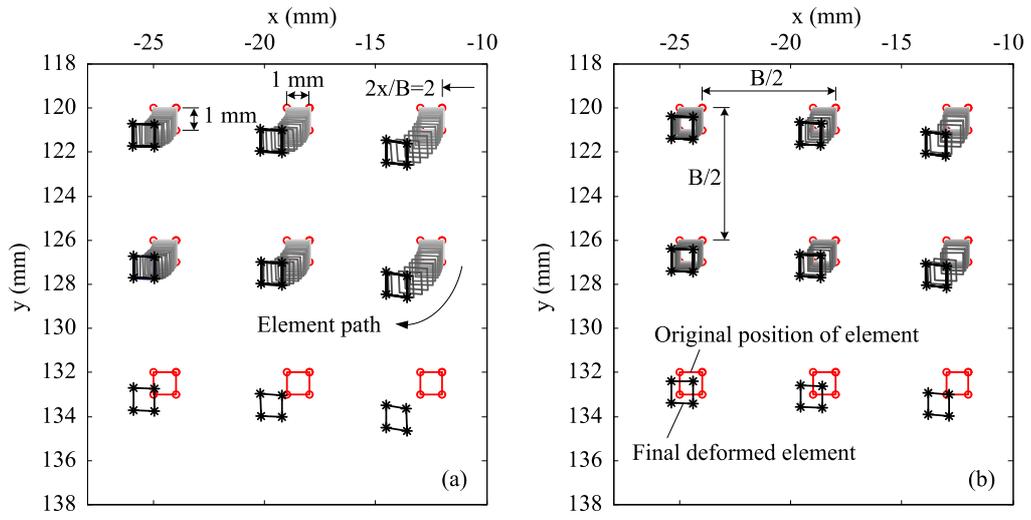


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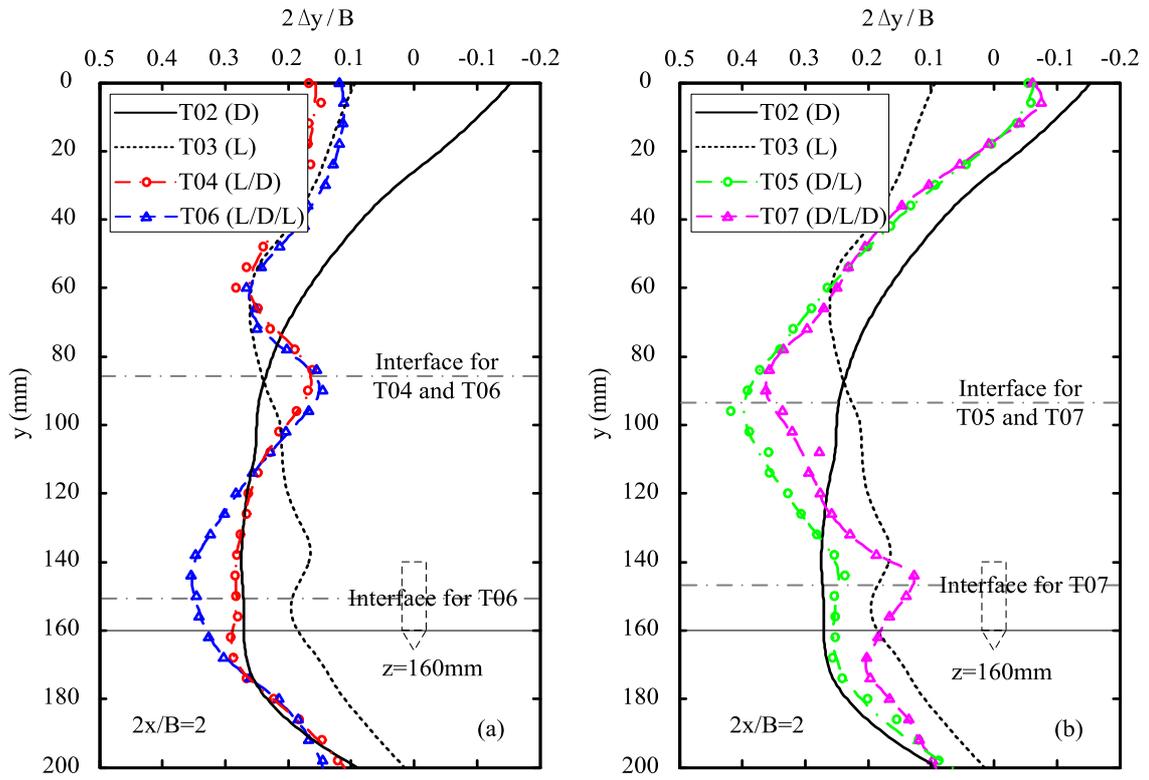


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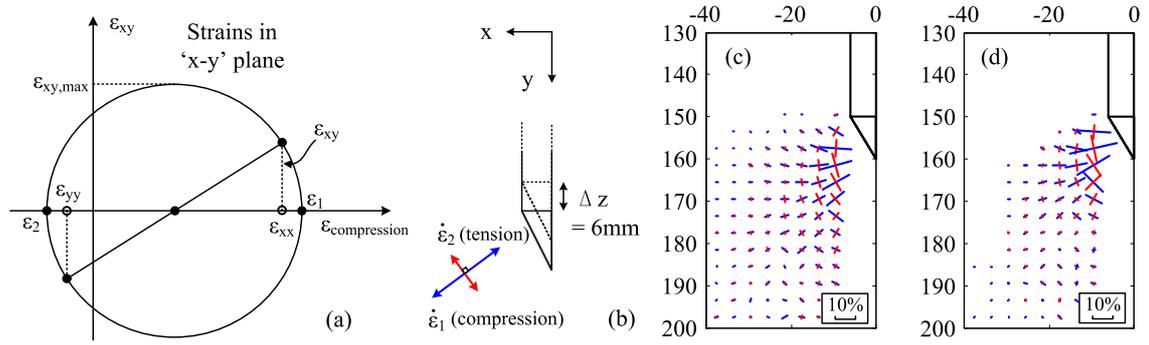


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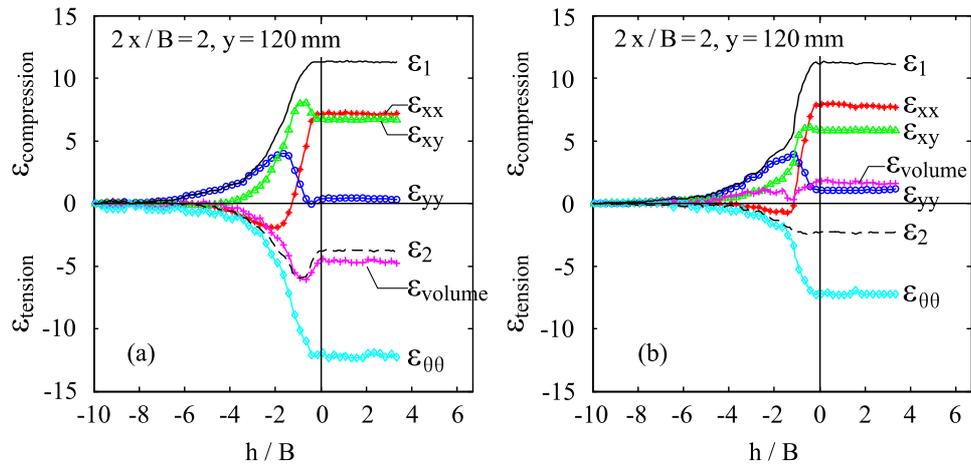


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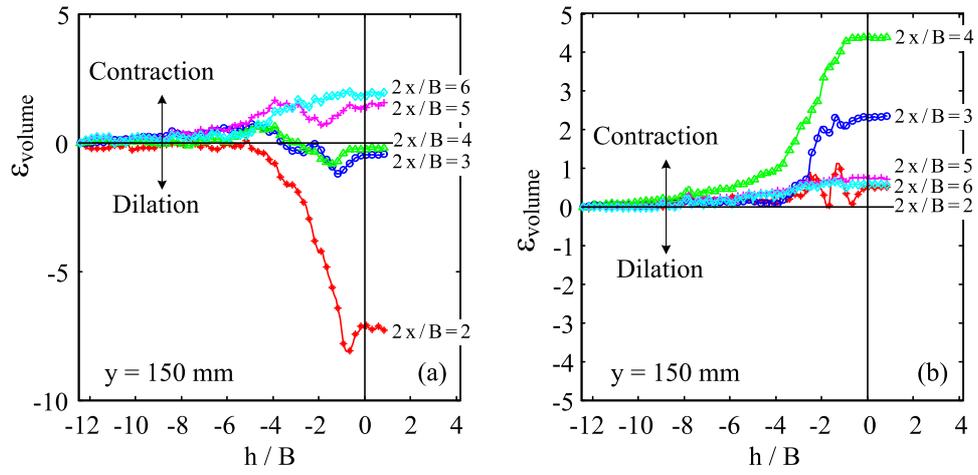


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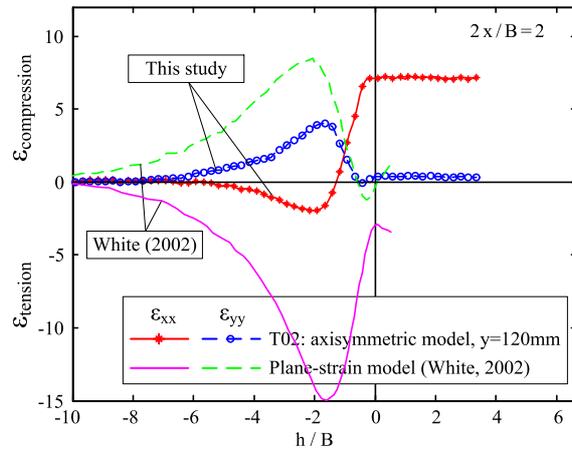


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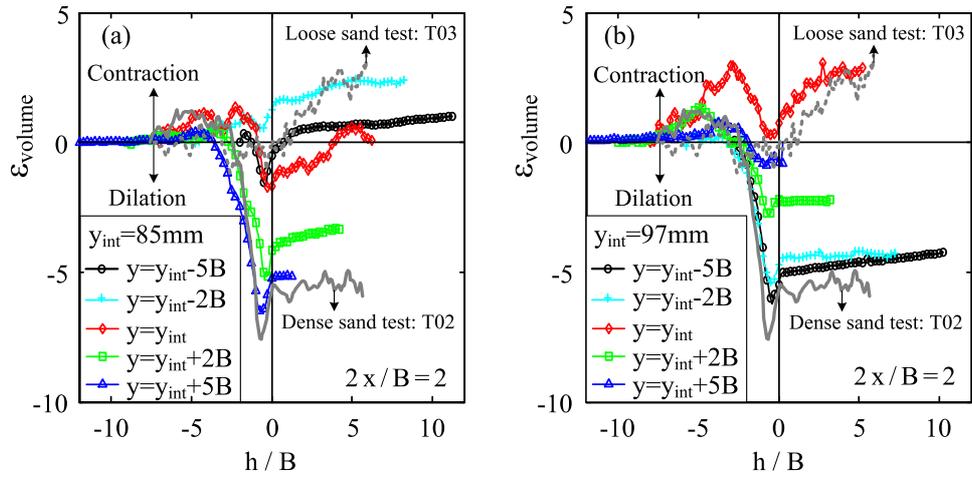


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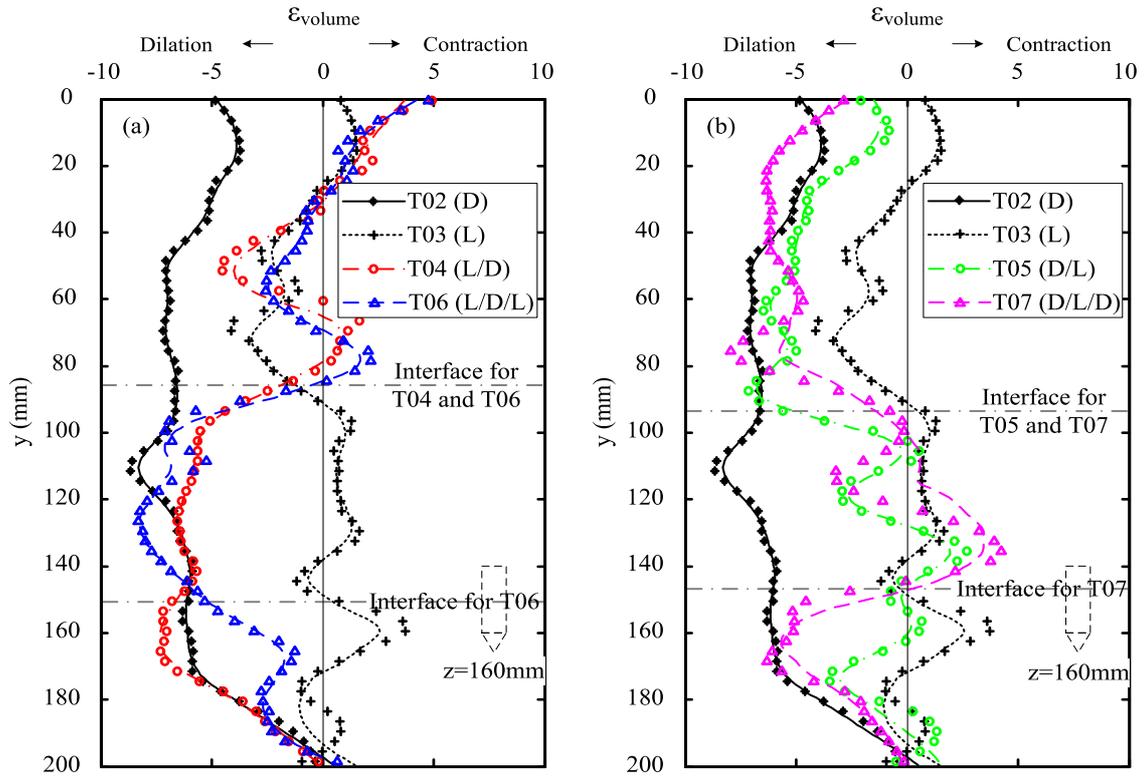


Fig. 16: Cumulative volumetric strain profiles for $2x/B = 2$ after 160 mm of penetration: (a) T04 and T06; (b) T05 and T07

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Table 1: Details of sample for each centrifuge test

Test ID	Soil Description	Depth of Soil 1 (<i>mm</i>)	Depth of Soil 2 (<i>mm</i>)	Depth of Soil 3 (<i>mm</i>)
T02	Uniform Dense (D)	301	-	-
T03	Uniform Loose (L)	298	-	-
T04	Loose over Dense (L/D)	85	205	-
T05	Dense over Loose (D/L)	97	201	-
T06	Thin Dense Layer (L/D/L)	87	65	142
T07	Thin Loose Layer (D/L/D)	90	57	153

Table 2: Properties of the Fraction E silica sand (Tan, 1990)

Property	Fraction E sand
Grain size d_{10} (mm)	0.095
Grain size d_{50} (mm)	0.14
Grain size d_{60} (mm)	0.15
Specific gravity G_s	2.65
Maximum void ratio (e_{max})	1.014
Minimum void ratio (e_{min})	0.613
Friction angle at constant volume (ϕ'_{cv})	32°