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# Comparison of Two-Individual Current Control and Vector Space Decomposition Control for Dual Three-Phase PMSM

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**Abstract** -- The relationship between the two-individual current control and the vector space decomposition (VSD) control for a dual three-phase permanent magnet synchronous machine (PMSM) is investigated in this paper. It is found that the VSD control is more flexible on controlling the fundamental current in  $\alpha\beta$  sub-plane and the fifth, seventh current harmonics in  $z_1z_2$  sub-plane with different PI gains, while the two-individual current control is comparable to the VSD control in having the same PI gains in the  $\alpha\beta$  and  $z_1z_2$  sub-planes. It is also found that the two-individual current control may have potential instability issues due to the mutual coupling between the two sets of three-phase windings. If the mutual coupling between the two sets is weak to some extent, then the two-individual current control could have the same dynamic performance as the VSD control without the stability issues. Experiments are conducted on a prototype dual three-phase PMSM to validate the theoretical analysis.

**Index Terms**-- double  $d$ - $q$  synchronous frame current control, double-star motor, dual three-phase, instability, two-individual current control, VSD control.

## I. INTRODUCTION

Multi-phase machines have been extensively employed in various applications such as electric ship propulsion, locomotive traction, electric and hybrid electric vehicles, "more-electric" aircraft, and high-power industrial applications [1-3]. They provide outstanding advantages [4-8], such as reduced phase current rating and torque ripple; a lower DC-link harmonic current; smooth magneto-motive force (MMF); improved efficiency; excellent fault tolerant characteristics and higher reliability at system level.

One of the most studied multi-phase machines is the six-phase machine [9], which can be easily driven by two individual classical three-phase voltage source inverters (VSIs). According to the shifted angle between the two sets of three-phase windings, the six-phase machine can be classified as symmetrical (shifted by  $0^\circ$  or  $60^\circ$ ) and asymmetrical (shifted by  $30^\circ$ ) six-phase/dual three-phase machine. The asymmetric dual three-phase machine is more attractive than the symmetrical one due to the cancellation of 6th torque harmonic [10]. The typical VSI for the dual three-phase machine with two isolated neutral points is shown in Fig. 1 [10], where the machine has two sets of three-phase windings, one set is designated as ABC, and the other set is XYZ shifted by  $30^\circ$  electrical degrees.

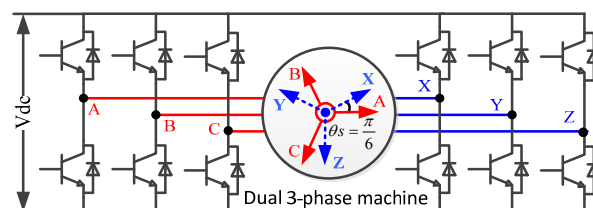


Fig. 1 Asymmetrical dual three-phase drive system [10].

Numerous current control strategies have been developed for the dual three-phase drive system [4-7, 11-18]. Two of the most interesting and widely used strategies are the vector space decomposition (VSD) control [11, 13, 16, 17], which treats the machine as a six-phase machine, and the two-individual current control [4, 5, 7, 12], which treats the machine as two single three-phase machines.

Since there is no mutual coupling between the  $\alpha\beta$  sub-plane and  $z_1z_2$  sub-plane [11, 14] in the VSD control, the currents in the  $\alpha\beta$  sub-plane and  $z_1z_2$  sub-plane can be regulated separately. As the torque is only related to  $\alpha\beta$  sub-plane, the VSD control can provide excellent dynamic torque performance without the influence of coupling voltages between two sets.

The two-individual current control is based on the double  $dq$  synchronous frames model [4, 5, 7, 12], where there is mutual coupling between the two  $dq$ -synchronous frames. Instead of the six-phase VSI, PWM strategies [11, 19-21], and complex matrix transformation of VSD control, two individual commercial single three-phase VSI inverters can be employed to drive each set of single three-phase windings in the dual three-phase machine individually. The two-individual current control is a very practical method in industry applications as it duplicates the vector control for a single three-phase machine. Meanwhile, it has the inherent advantage of suppressing the current unbalance resulting from asymmetries between the two sets of three-phase windings [5] and excellent fault tolerance capability.

The manuscript is expanding work in [22], as introduced in [22], the two-individual current control may have instability issues. The conditions for safely supplying the dual three-phase induction machine by two PWM-VSIs is introduced in [23, 24], where it was concluded that the multi-star machine supplied by independent PWM-VSIs has instability issues if a strong magnetic coupling between each set exists. In [25], the designs of coil pitch and special slot shape for a dual three-phase induction machine were

investigated, in order to increase the mutual leakage inductance to reduce the current harmonics for safe operation. However, how weak the magnetic coupling can be while still operating at a safe level for individual current control was not discussed.

In this paper, the two-individual current control and VSD control for dual three-phase PMSM are compared and their relationship is revealed. Based on their relationship, the instability of the two-individual current control is investigated. Firstly, the mathematical model of dual three-phase PMSM for two-individual current control and VSD control are briefly introduced in Section II. The relationship between them is demonstrated in Section III. Then, the instability of the two-individual current control is analyzed in detail with the aid of relationship to the VSD control in Section IV. Experiments are conducted in Section 0 to verify the analyses.

## II. MATHEMATICAL MODEL OF DUAL THREE-PHASE PMSM

### A. Inductance Modeling of Dual Three-Phase PMSM

Assuming that the induced back electromotive force (EMF) is sinusoidal; eddy current and hysteresis losses, mutual leakage inductance, saturation, the harmonic components in self-inductances and mutual inductances with orders higher than the second order [15] are neglected, the self-inductance can be expressed as

$$L_{PP} = L_{sl} + L_{dqavg} + L_{dqdiff} \cos(2\theta_P) \quad (1)$$

where

$$L_{dqavg} = (L_d + L_q) / 2, \quad L_{dqdiff} = (L_d - L_q) / 2 \quad (2)$$

The mutual inductance between phases in each set can be expressed as

$$M_{PQ} = M_{dqavg} \cos(\theta_P - \theta_Q) + M_{dqdiff} \cos(\theta_P + \theta_Q) \quad (3)$$

The mutual inductance between phases in different set of windings can be expressed as

$$M_{PQ} = M_{dq12avg} \cos(\theta_P - \theta_Q) + M_{dq12diff} \cos(\theta_P + \theta_Q) \quad (4)$$

where  $P$  stands for phase  $A, X, B, Y, C,$  or  $Z$ , while  $Q$  stands for another phase that is different with phase  $P$ .  $\theta_P$  and  $\theta_Q$  are the electrical angle of phase  $P$  and  $Q$  winding axis shifted from  $d$ -axis of PM rotor.  $L_{sl}$  is the phase leakage inductance,  $(L_{sl}+L_d)$  and  $(L_{sl}+L_q)$  are the phase self-inductances when the phase winding axis are aligned with  $d$ -axis and  $q$ -axis of PM rotor respectively.  $M_{dqavg}$  and  $M_{dqdiff}$  are the gains of DC and second harmonic components in the mutual inductances between phases in each set.  $M_{dq12avg}$  and  $M_{dq12diff}$  are the gains of DC and second harmonic components in the mutual inductances between phases in different sets

The measured self-inductances and mutual inductances of the prototype dual three-phase machine are shown in Fig. 2. After the FFT analyses of the measured inductances, it can be found that the dc components and 2nd harmonic components are dominant, which is in accordance with the inductance modeling(1), (3) and (4).

### B. Two-Individual Single Three-Phase Model

The dual three-phase PMSM is considered as two single three-phase machines with mutual coupling [4]. The voltage equations for each single three-phase machine in  $dq$ -frame can be expressed as (5) and (6).

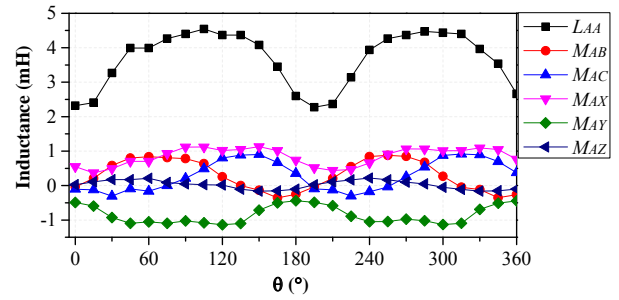


Fig. 2 Measured self- and mutual inductances of prototype PMSM.

$$\begin{bmatrix} v_{d1} \\ v_{q1} \end{bmatrix} = \begin{bmatrix} R_s + L_{d1}s & 0 \\ 0 & R + L_{q1}s \end{bmatrix} \begin{bmatrix} i_{d1} \\ i_{q1} \end{bmatrix} + \omega \begin{bmatrix} -L_{q1}i_{q1} \\ L_{d1}i_{d1} \end{bmatrix} + \omega \begin{bmatrix} 0 \\ \psi_{fd} \end{bmatrix} \\ + \underbrace{\begin{bmatrix} M_{d21}s & 0 \\ 0 & M_{q21}s \end{bmatrix} \begin{bmatrix} i_{d2} \\ i_{q2} \end{bmatrix} + \omega \begin{bmatrix} -M_{q21} \cdot i_{q2} \\ M_{d21} \cdot i_{d2} \end{bmatrix}}_{\text{coupling voltages caused by another set}} \quad (5)$$

$$\begin{bmatrix} v_{d2} \\ v_{q2} \end{bmatrix} = \begin{bmatrix} R_s + L_{d2}s & 0 \\ 0 & R + L_{q2}s \end{bmatrix} \begin{bmatrix} i_{d2} \\ i_{q2} \end{bmatrix} + \omega \begin{bmatrix} -L_{q2}i_{q2} \\ L_{d2}i_{d2} \end{bmatrix} + \omega \begin{bmatrix} 0 \\ \psi_{fd} \end{bmatrix} \\ + \underbrace{\begin{bmatrix} M_{d12}s & 0 \\ 0 & M_{q12}s \end{bmatrix} \begin{bmatrix} i_{d1} \\ i_{q1} \end{bmatrix} + \omega \begin{bmatrix} -M_{q12} \cdot i_{q1} \\ M_{d12} \cdot i_{d1} \end{bmatrix}}_{\text{coupling voltages caused by another set}} \quad (6)$$

where the subscripts 1, 2 stand for set of windings identified by phase ABC and XYZ, respectively;  $v_{d1}, v_{q1}, v_{d2}$  and  $v_{q2}$  are  $dq$ -axis voltages,  $i_{d1}, i_{q1}, i_{d2}, i_{q2}$  are  $dq$ -axis currents;  $M_{d21}$  and  $M_{d12}$  is the mutual inductances between the  $d$ -axis in each set,  $M_{q21}$  and  $M_{q12}$  is the mutual inductances between  $q$ -axis in each set;  $R_s$  is the stator winding resistance;  $\omega$  is the electrical speed;  $\psi_{fd}$  is  $d$ -axis PM flux.

According to (1)-(4), the inductances in  $dq$ -frame for each set of single three-phase machines can be expressed as

$$L_{d1} = L_{d2} = L_{sl} + L_{dqavg} + \frac{1}{2}M_{dqavg} + \frac{1}{2}(L_{dqdiff} + 2M_{dqdiff}) \quad (7)$$

$$L_{q1} = L_{q2} = L_{sl} + L_{dqavg} + \frac{1}{2}M_{dqavg} - \frac{1}{2}(L_{dqdiff} + 2M_{dqdiff}) \quad (8)$$

$$M_{d21} = M_{d12} = 3(M_{dq12avg} + M_{dq12diff}) / 2 \quad (9)$$

$$M_{q21} = M_{q12} = 3(M_{dq12avg} - M_{dq12diff}) / 2 \quad (10)$$

If there is no mutual coupling between two sets,  $M_{dq12avg}$  and  $M_{dq12diff}$  will be zero, therefore,  $M_{d21}, M_{d12}, M_{q12}$  and  $M_{q21}$  will be zero too, so as the mutual coupling voltages in (5) and (6). If there is full mutual coupling between two sets and between phases in each set, i.e. the  $M_{dqavg}$  and  $M_{dq12avg}$  are equal to  $L_{dqavg}$ , the  $M_{dqdiff}$  and  $M_{dq12diff}$  are equal to  $L_{dqdiff}$ , then (7)-(10) can be simplified as (11)-(14). In this case, there are large mutual coupling voltages in (5) and (6).

$$L_{d1} = L_{d2} = L_{sl} + 3L_d / 2 \quad (11)$$

$$L_{q1} = L_{q2} = L_{sl} + 3L_q / 2 \quad (12)$$

$$M_{d12} = M_{d21} = 3L_d / 2 \quad (13)$$

$$M_{q12} = M_{q21} = 3L_q / 2 \quad (14)$$

### C. VSD Model

The VSD control for dual three-phase machine is introduced in Appendix A. Based on the VSD control, the

voltage equations in  $dq$ -frame in  $\alpha\beta$  sub-plane and  $dqz$ -frame in  $z_1z_2$  sub-plane can be expressed as (15) and (16) respectively.

$$\begin{bmatrix} v_d \\ v_q \end{bmatrix} = \begin{bmatrix} R_s + L_d^{equ} s & 0 \\ 0 & R + L_q^{equ} s \end{bmatrix} \begin{bmatrix} i_d \\ i_q \end{bmatrix} + \omega \begin{bmatrix} -L_q^{equ} i_q \\ L_d^{equ} i_d + \psi_{fd} \end{bmatrix} \quad (15)$$

$$\begin{bmatrix} v_{dz} \\ v_{qz} \end{bmatrix} = \begin{bmatrix} R_s + L_{dz} s & 0 \\ 0 & R + L_{qz} s \end{bmatrix} \begin{bmatrix} i_{dz} \\ i_{qz} \end{bmatrix} + \omega \begin{bmatrix} -L_{qz} i_{qz} \\ L_{dz} i_{dz} \end{bmatrix} \quad (16)$$

where the equivalent inductances in  $dq$ -frame and  $dqz$ -frame can be expressed as (17)-(20) when the inductances of dual three-phase PMSM are modeled as (1)-(4) [15].

$$L_d^{equ} = L_{d1} + M_{d12} = L_{d2} + M_{d21} \quad (17)$$

$$L_q^{equ} = L_{q1} + M_{q12} = L_{q2} + M_{q21} \quad (18)$$

$$L_{dz} = L_{d1} - M_{d12} = L_{d2} - M_{d21} \quad (19)$$

$$L_{qz} = L_{q1} - M_{q12} = L_{q2} - M_{q21} \quad (20)$$

As can be seen from (15) and (16), there are no mutual coupling voltages between  $dq$ -frame and  $dqz$ -frame. The VSD control can be shown in Fig. 3 [26].

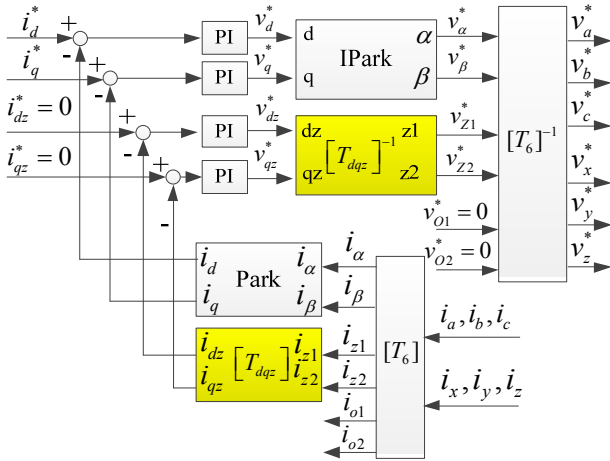


Fig. 3 VSD control [26].

### III. RELATIONSHIP BETWEEN TWO-INDIVIDUAL CURRENT CONTROL AND VSD CONTROL

According to the vector control theory for single three-phase machine and the VSD control for dual three-phase machines (detailed in the Appendix), it can be deduced that the variables in the dual three-phase machine and in each set of the single three-phase windings have the following relationship considering  $(6k\pm 1)$ th,  $k=1, 3, 5, \dots$  harmonics.

$$F_{dq} = (F_{dq1} + F_{dq2}) / 2; \quad F_{dqz} = (-F_{dq1} + F_{dq2}) / 2 \quad (21)$$

where  $F_{dq1} = [F_{d1} \ F_{q1}]^T$ ,  $F_{dq2} = [F_{d2} \ F_{q2}]^T$  are  $dq$ -axis currents or voltages in  $dq$ -frame for phase ABC and XYZ respectively.  $F_{dq} = [F_d \ F_q]^T$ ,  $F_{dqz} = [F_{dz} \ F_{qz}]^T$  are  $dq$ -axis currents or voltages in  $dq$ - and  $dqz$ -frame in the dual three-phase system.

(21) means the currents or voltages in  $dq$ - and  $dqz$ -frames in a dual three-phase system can be obtained from the  $dq$ -axis currents or voltages in the single 3-phase ABC and XYZ; and vice versa, the  $dq$ -axis currents or voltages in single 3-phase ABC and XYZ can be derived from the currents or voltages in  $dq$ - and  $dqz$ -frames in a dual three-phase system, which can be expressed as

$$F_{dq2} = F_{dq} + F_{dqz}; \quad F_{dq1} = F_{dq} - F_{dqz} \quad (22)$$

Usually, the PI controllers should be tuned on their respective plants. However, the first and the second set of three-phase windings are identical and their respective plants are the same. Therefore, the current controllers for each set in the two-individual current control have the same proportional and integral (PI) gains. The outputs of PI controllers can be expressed as

$$v_{dq1}^* = \left( k_p + \frac{k_i}{s} \right) (i_{dq}^* - i_{dq1}) \quad (23)$$

$$v_{dq2}^* = \left( k_p + \frac{k_i}{s} \right) (i_{dq}^* - i_{dq2}) \quad (24)$$

where  $i_{dq}^*$  means the  $dq$ -axis reference currents for each set,  $i_{dq1}$  denotes the  $dq$ -axis currents in the first set of single 3-phase ABC,  $i_{dq2}$  denotes the  $dq$ -axis currents in the second set of single 3-phase XYZ.

According to (22), (23) and (24) can be re-written as

$$v_{dq1}^* = \left( k_p + \frac{k_i}{s} \right) (i_{dq}^* - i_{dq}) + \left( k_p + \frac{k_i}{s} \right) (0 + i_{dqz}) \quad (25)$$

$$v_{dq2}^* = \left( k_p + \frac{k_i}{s} \right) (i_{dq}^* - i_{dq}) + \left( k_p + \frac{k_i}{s} \right) (0 - i_{dqz}) \quad (26)$$

Therefore, according to (21), the variables  $v_{dq}^*$  and  $v_{dqz}^*$  in the dual 3-phase system can be expressed as (27) and (28) respectively.

$$v_{dq}^* = (v_{dq1}^* + v_{dq2}^*) / 2 = \left( k_p + \frac{k_i}{s} \right) (i_{dq}^* - i_{dq}) \quad (27)$$

$$v_{dqz}^* = (-v_{dq1}^* + v_{dq2}^*) / 2 = \left( k_p + \frac{k_i}{s} \right) (0 - i_{dqz}) \quad (28)$$

(27) and (28) are exactly the current controllers in  $dq$ -frame in  $\alpha\beta$  sub-plane and in  $dqz$ -frame in  $z_1z_2$  sub-plane, shown respectively in Fig. 3. They have the same PI gains in  $\alpha\beta$  sub-plane and  $z_1z_2$  sub-plane. The above analysis shows that the two-individual current control is equivalent to the VSD control with the same PI gains for the current controllers in both  $\alpha\beta$  sub-plane and  $z_1z_2$  sub-plane.

The two-individual current control can be illustrated in Fig. 4 [7]. The relationship of two-individual current control and VSD control can be demonstrated in the dashed box in Fig. 4. For two-individual current control, the part in the dashed box can be treated as a dual 3-phase machine. The inputs are the  $dq$ -axis voltages and outputs are  $dq$ -axis currents in each single 3-phase system.

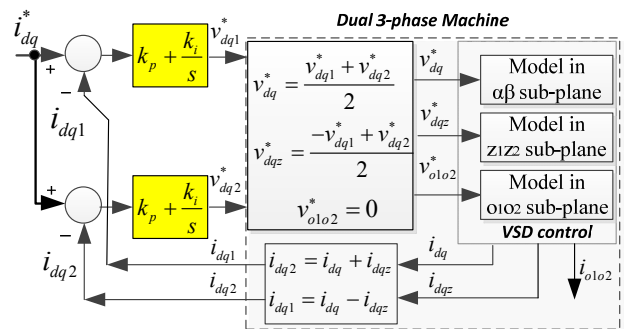


Fig. 4 Relationship between two-individual current control and VSD control.



Considering the variables' relationship between the single and dual 3-phase systems, (21) and (22), the dual 3-phase model in the dashed box in Fig. 4 can be further expanded according to the VSD theory. In the dashed box, the variables in the  $dq$ -frame in single 3-phase ABC and XYZ are converted to the variables in the  $\alpha\beta$ - $z_1z_2$ - $o_1o_2$  sub-planes in the dual 3-phase system, where  $V_{dq^*}$ ,  $V_{dqz^*}$  and  $V_{o1o2^*}$  are the reference voltages in  $\alpha\beta$ - $z_1z_2$ - $o_1o_2$  sub-planes respectively, the outputs are currents  $i_{dq}$ ,  $i_{dqz}$ , and  $i_{o1o2}$  in  $\alpha\beta$ - $z_1z_2$ - $o_1o_2$  sub-planes respectively, and then they are converted to the currents in  $dq$ -frame in single 3-phase ABC and XYZ. It is worth noting that the currents in  $o_1o_2$  sub-plane are zero as the neutral points of the two sets of single 3-phase windings are not accessible.

#### IV. INSTABILITY ANALYSIS OF TWO-INDIVIDUAL CURRENT CONTROL

The currents in  $\alpha\beta$  sub-plane are related to electromechanical energy conversion and the currents in  $z_1z_2$  sub-plane make no contribution to torque generation [11]. If VSD control is employed, the PI gains should be tuned according to the respective plants in  $\alpha\beta$  sub-plane and  $z_1z_2$  sub-plane. However, if the two-individual controller is employed, as discussed in Section III, the two-individual control is equivalent to the VSD control having the same PI gains in  $\alpha\beta$  sub-plane and  $z_1z_2$  sub-plane. To guarantee the dynamical performance of the two-individual current control, the PI gains should be optimized for its equivalent current controllers in  $\alpha\beta$  sub-plane in VSD control. Since its equivalent current controllers in  $z_1z_2$  sub-plane in VSD share the same PI gains as that in  $\alpha\beta$  sub-plane, the proportional gain may be relatively large in  $z_1z_2$  sub-plane and cause instability.

The equivalent inductances in  $\alpha\beta$  sub-plane (17)(18) and those in  $z_1z_2$  sub-plane (19)(20) are usually different due to the mutual coupling. For example, if there is full mutual coupling between the two sets and full mutual coupling between phases in each set, i.e.  $M_{dqavg}$  and  $M_{dq12avg}$  is equal to  $L_{dqavg}$ , the  $M_{dqdiff}$  and  $M_{dq12diff}$  is equal to  $L_{dqdiff}$ , (17)-(20) can be simplified as

$$L_d^{equ} = L_{sl} + 3L_d, \quad L_q^{equ} = L_{sl} + 3L_q. \quad (29)$$

$$L_{dz} = L_{qz} = L_{sl} \quad (30)$$

From (30), it can be seen that the inductances in  $z_1z_2$  sub-plane are only related with self-leakage inductance in this case, which may be far less than the inductances (29) in  $\alpha\beta$  sub-plane.

Neglecting the coupling voltages between the  $d$ -axis and  $q$ -axis in  $dq$ -frame and the coupling voltages between the  $dz$ -axis and  $qz$ -axis in  $dqz$ -frame, the mathematical model in  $dq$ - and  $dqz$ -frames shown in (15) and (16) can be simplified as a  $RL$  load [27, 28]. Then the current controller in  $dq$ - and  $dqz$ -frame can be simplified as Fig. 5.

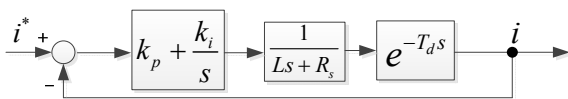


Fig. 5 Typical current control scheme.

In Fig. 5,  $T_d$  is the total delay time, which includes current sampling delay, PWM output delay, etc. To simplify the design of PI gains, the delay function  $e^{-T_d s}$  is usually simplified to a low-pass filter  $1/(1+sT_d)$  [28, 29]. If the dominant pole of  $-R_s/L$  is canceled by the zero point of the PI controller, the open loop of the whole system can be simplified as a typical first order system, then  $K_p$  and  $K_i$  can be optimally designed as [29]

$$K_p = \frac{L}{4\xi^2 T_d}; K_i = \frac{R_s}{4\xi^2 T_d} \quad (31)$$

where  $\xi$  is the damping factor, it is usually 0.707 for an acceptable rising time and overshoot simultaneously.

When the PI gains of the two-individual current control are optimized for its equivalent current controllers in  $\alpha\beta$  sub-plane in VSD, the PI gains for  $i_q$  current controller will be

$$K_p = \frac{I_q^{equ}}{4\xi^2 T_d}, \quad K_i = \frac{R_s}{4\xi^2 T_d} \quad (32)$$

If the PI gains are optimized for its equivalent current controllers in  $z_1z_2$  sub-plane, the PI gains for  $i_{qz}$  current controller should be

$$K_p = \frac{L_{qz}}{4\xi^2 T_d}, \quad K_i = \frac{R_s}{4\xi^2 T_d} \quad (33)$$

Define the ratio  $r_d$  and  $r_q$  as below

$$r_d = \frac{I_d^{equ}}{L_{dz}} = 1 + \frac{2M_{d12}}{L_{dz}} \quad (34)$$

$$r_q = \frac{I_q^{equ}}{L_{qz}} = 1 + \frac{2M_{q12}}{L_{qz}} \quad (35)$$

From (34) and (35), it can be seen that  $r_d$  and  $r_q$  increase as  $M_{d12}$  and  $M_{q12}$  increase, which means the ratio  $r_d$  and  $r_q$  will increase as the level of mutual coupling between the sets of three-phase windings increases.

If the PI gains for the two-individual current control loops are chosen for optimizing dynamic performance, the PI gains should be obtained from (32) for its equivalent  $q$ -axis current controller in  $\alpha\beta$  sub-plane. Since its equivalent current controllers in  $z_1z_2$  sub-plane share the same PI gains as its equivalent current controllers in  $\alpha\beta$  sub-plane,  $K_p$  for the equivalent  $i_{qz}$  current controller in  $z_1z_2$  sub-plane can be rewritten as (36), which is increased up to  $r_q$  times of that in (33).

$$K_p = \frac{L_q^{equ}}{4\xi^2 T_d} = \frac{r_q L_{qz}}{4\xi^2 T_d} \quad (36)$$

Therefore, the equivalent  $i_{qz}$  current control for two-individual current control can be illustrated as Fig. 6.

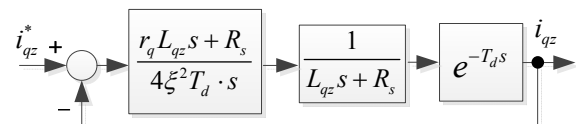


Fig. 6 Equivalent current control structure for  $i_{qz}$ .

To analyze the close loop root locus as the  $r_q$  increases,  $e^{-T_d s}$  is approximated as polynomial  $M(s)/N(s)$  by Padé approximation [30, 31], which is more precise for analysis

than the low-pass filter approximation. Then the close loop transfer function in Fig. 6 will be

$$G(s) = \frac{\left( \frac{r_q L_{qz} s + R_s}{4\xi^2 T_d s} \right) \frac{1}{L_{qz} s + R_s} \frac{M(s)}{N(s)}}{1 + \left( \frac{r_q L_{qz} s + R_s}{4\xi^2 T_d s} \right) \frac{1}{L_{qz} s + R_s} \frac{M(s)}{N(s)}} \quad (37)$$

The Eigen function of  $G(s)$  in (37) can be expressed as (38), which can be rewritten as (39).

$$D(s) = 4\xi^2 T_d s(L_{qz} s + R_s)N(s) + (r_q L_{qz} s + R_s)M(s) \\ = r_q L_{qz} s M(s) + 4\xi^2 T_d s(L_{qz} s + R_s)N(s) + R_s M(s) = 0 \quad (38)$$

$$1 + \frac{r_q L_{qz} s M(s)}{4\xi^2 T_d s(L_{qz} s + R_s)N(s) + R_s M(s)} = 0 \quad (39)$$

According to (39), the current controller with the same Eigen function as that in Fig. 6 can be shown in Fig. 7. As the close loop transfer function in Fig. 6 and Fig. 7 have the same Eigen function, they have the same root locus. In Fig. 7, the  $r_q$  becomes the gain of the forward path, which is helpful to analyse the root locus.

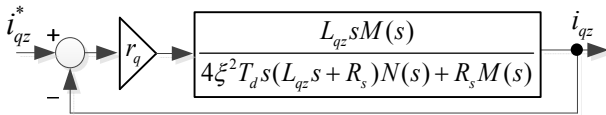


Fig. 7 Current control with same Eigen function

In the following analysis, the second order Padé approximation is adopted. The root locus of  $i_{qz}$  current control can be shown in Fig. 8, when  $T_d$  is  $2e-4s$ . It can be seen that all the poles are located in the left side of the plane when  $r_q$  is equal to 1. However, when  $r_q$  increases to the critical value 3.3, one pair of poles are located on the image axis, which means the system is in a critical stable state. As  $r_q$  continues to increase, the pair of poles will cross over the image axis, which means that the system tends to be unstable when the level of mutual coupling increases.

From the above analysis, it can be concluded that  $r_q$  in (35) should be lower than the critical value to guarantee the stable operation of the two-individual current controllers without compromising the dynamic torque performance, therefore the mutual inductance between the two sets should be carefully considered for the machine design.

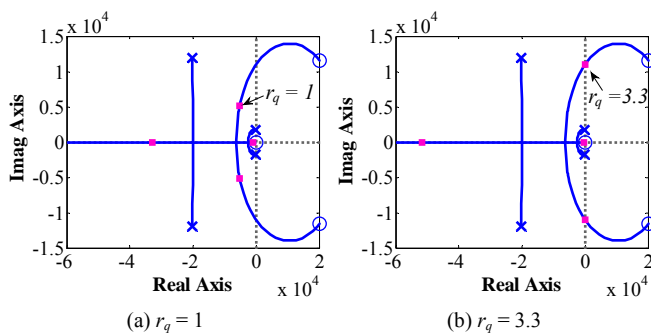


Fig. 8 Root loci of  $i_{qz}$  current control.

It is worth noting that the accuracy of the root locus is also related to the accuracy of  $L_{qz}$ ,  $R$  and  $e^{-T_d s}$ , therefore, the precise critical value may be slightly different to the critical value of 3.3 in Fig. 8(b) due to the inaccuracy of the parameters and Padé approximation. However, the trend of poles of close loop transfer function moving towards to the right plane as  $r_q$  increases is definitive.

## V. EXPERIMENTS

The hardware platform based on dSPACE DS1005 is shown in Fig. 9. The power topology is the same as Fig. 1, which has two individual single three-phase VSIs. The prototype dual 3-phase PMSM, whose design parameters are shown in TABLE I, is coupled to a PM dc machine used as an adjustable load by adjusting the power resistor. The execution rate of the current loop, current sampling frequency, and PWM frequency is configured to be 10 kHz. Two independent SVPWM modulators are employed for PWM generation for each channel.

Three experiments are conducted in this section. The first verifies that the two-individual current control is equivalent to the VSD control having the same PI gains for both  $\alpha\beta$  and  $z_1 z_2$  sub-planes. The second demonstrates the potential instability of the two-individual current control. The third shows that the two-individual current control has the same dynamic torque performance as VSD control when it is in safe operation with PI gains optimized for its equivalent current controllers in  $\alpha\beta$  sub-plane in VSD control.

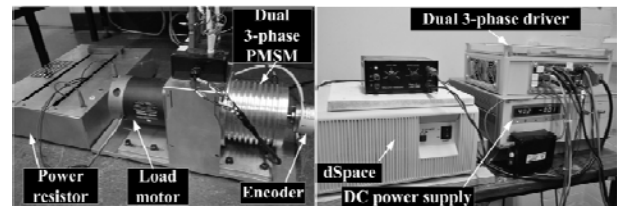


Fig. 9 Experimental setup for dual three-phase PMSM drive testing.

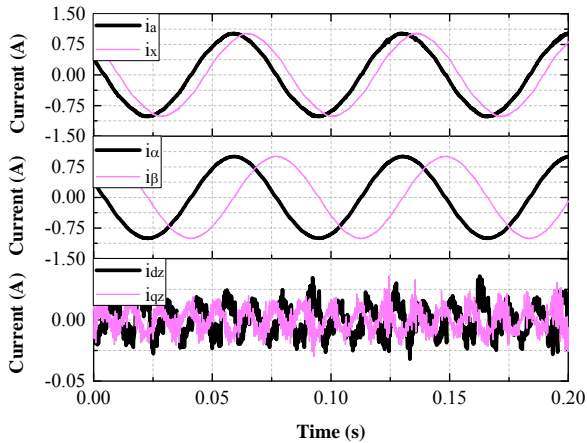
TABLE I PARAMETERS OF PROTOTYPE DUAL THREE-PHASE PMSM

Parameters	Value
Resistance ( $\Omega$ )	1.1
Equivalent $d$ -axis inductance in $\alpha\beta$ sub-plane $L_d^{equ}$ (mH)	4.58
Equivalent $q$ -axis inductance in $\alpha\beta$ sub-plane $L_q^{equ}$ (mH)	5.19
Equivalent $d$ -axis inductance in $z_1 z_2$ sub-plane $L_{dz}$ (mH)	2.42
Equivalent $q$ -axis inductance in $z_1 z_2$ sub-plane $L_{qz}$ (mH)	1.44
$r_d (L_q^{equ} / L_{dz})$	1.90
$r_q (L_q^{equ} / L_{qz})$	3.60
No-load flux linkage (Wb)	0.075
Pole pairs	5
DC-link voltage(V)	40

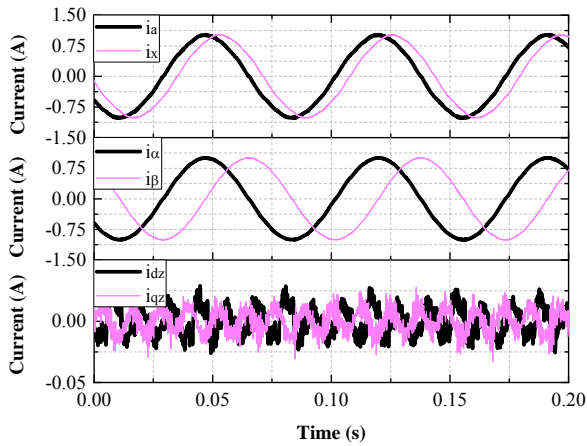
### A. Two-Individual Current Control and VSD Control

In this experiment, the drive works in constant current control mode, the  $i_q$  reference is 1A. The currents under the two-individual current control with PI gains optimized for current controller in  $\alpha\beta$  sub-plane in VSD control are shown in Fig. 10(a). The currents under the VSD control with the same PI gains for both  $\alpha\beta$  and  $z_1 z_2$  sub-planes are shown in Fig. 10(b). By comparing Fig. 10(a) and Fig. 10(b), it can be seen that their current profiles are equivalent, also their corresponding harmonics in Fig. 11(a) and Fig. 11(b) show

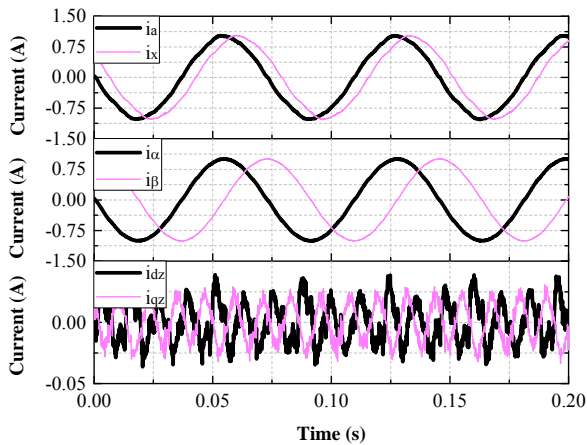
that they have the same spectrum, which means the two-individual current control is equivalent to the VSD control in this case.



(a) Two-individual current control with PI gains optimized for  $\alpha\beta$  sub-plane



(b) VSD control with same PI gains for both  $\alpha\beta$  and  $z_1z_2$  sub-planes as those in two-individual current control



(c) VSD control with PI gains optimized for  $\alpha\beta$  and  $z_1z_2$  sub-planes respectively

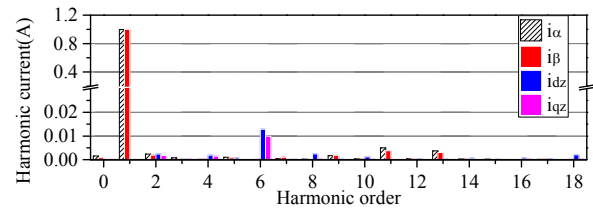
Fig. 10 Current profile comparison of two-individual current control and VSD control.

If the PI gains in the VSD control are optimized for the current controllers in  $\alpha\beta$  and  $z_1z_2$  sub-planes respectively, the experimental current is shown in Fig. 10(c), and the corresponding harmonic analyses are shown in Fig. 11(c). It

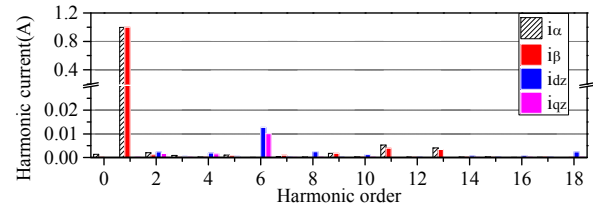
shows that the peak value of  $i_{dz}$  and  $i_{qz}$  are slightly higher than that in Fig. 10(a) and (b). This is because a smaller  $K_p$  (due to  $L_{qz} < L_q^{equ}$  and  $L_{dz} < L_d^{equ}$ ) is applied when PI gains are optimized for the current controller in  $z_1z_2$  sub-plane according to (31).

It is worth noting that although the references of  $i_{dz}$  and  $i_{qz}$  are zero in Fig. 3,  $i_{dz}$  and  $i_{qz}$  are not zero and the amplitudes are relatively large. This is because there are the 6<sup>th</sup> harmonic currents in  $i_{dz}$  and  $i_{qz}$  due to the 5<sup>th</sup> and 7<sup>th</sup> harmonics in the back-EMF and the inverter non-linearity, etc. The DC components can be regulated to zero by a PI controller. However, the 6<sup>th</sup> harmonic currents can only be suppressed rather than eliminated by PI controllers.

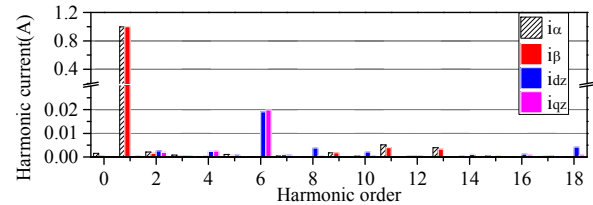
As demonstrated in the above three tests, it can be concluded that the VSD control is more flexible than the two-individual current control because the currents in  $\alpha\beta$  and  $z_1z_2$  sub-planes can be controlled separately and the PI gains for current controllers in each sub-plane can be optimized individually.



(a) Two-individual current control with PI gains optimized for  $\alpha\beta$  sub-plane



(b) VSD control with same PI gains for both  $\alpha\beta$  and  $z_1z_2$  sub-planes as those in two-individual current control



(c) VSD control with PI gains optimized for  $\alpha\beta$  and  $z_1z_2$  sub-planes respectively

Fig. 11 Current harmonics comparison of two-individual current control and VSD control.

### B. Potential Instability of Two-Individual Current Control

When the PI gains in the current controller in the  $z_1z_2$  sub-plane are optimized according to (31) by using inductances  $L_{dz}$  and  $L_{qz}$ , the equivalent  $r_d$  and  $r_q$  are equal to 1. In this case, the currents of  $i_{dz}$  and  $i_{qz}$  at the ready state operation are shown in Fig. 10 (c). However, when the PI gains in the current controller in the  $z_1z_2$  sub-plane are chosen to be the same as that in the  $\alpha\beta$  sub-plane,  $r_d$  and  $r_q$  will be equal to 1.9 and 3.6 respectively. In this case, the currents of  $i_{dz}$  and  $i_{qz}$  at the ready state operation are shown in Fig. 10 (b).

The step current responses of  $i_{dz}$  and  $i_{qz}$  in VSD control are shown in Fig.12 (a) and Fig.12 (b) respectively. Although the current amplitude of  $i_{dz}$  and  $i_{qz}$  at the ready state operation in Fig. 10(a) and (b) are lower than that in Fig. 10(c), it is evident that there are more oscillations in the step current response when  $r_q$  and  $r_d$  are bigger than 1. Since the ratio  $r_q$  (=3.6) is larger than  $r_d$  (=1.9), the oscillations in Fig.12 (b) is larger than that in Fig.12(a), which means the  $i_{qz}$  current controller tends to be more unstable than the  $i_{dz}$  current controller in this case study.

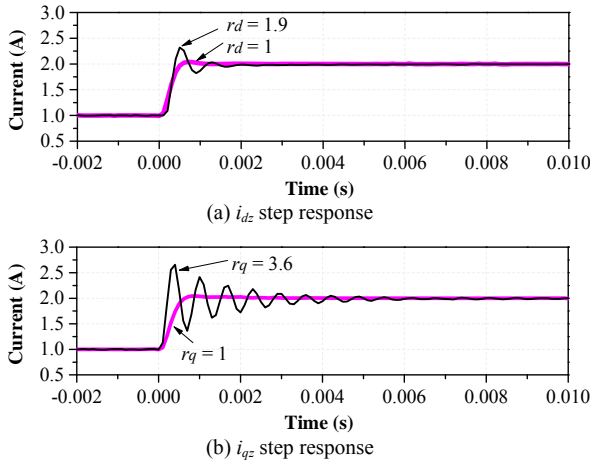


Fig.12 Step current response of  $i_{dz}$  and  $i_{qz}$ .

When  $K_p$  for the two-individual current controller is increased to 1.25 times of the proportional gain optimized for the current controller in the  $\alpha\beta$  sub-plane (32), the equivalent gain  $r_q$  of the forward path in Fig. 7 for current controller in  $dqz$ -frame will be increased to 4.5. The equivalent  $r_q$  is larger than the critical value 3.3 in Fig. 8(b) (this may be inaccurate due to inaccurate parameters and approximation). In this case, the  $i_{qz}$  current controller tends to be unstable. The steady current under the two-individual current control is shown in Fig.13. It can be seen that the  $i_{qz}$  current controller tends to be unstable, while the  $i_{dz}$  current controller and the current controllers in  $dq$ -frame in  $\alpha\beta$  sub-plane are still stable.

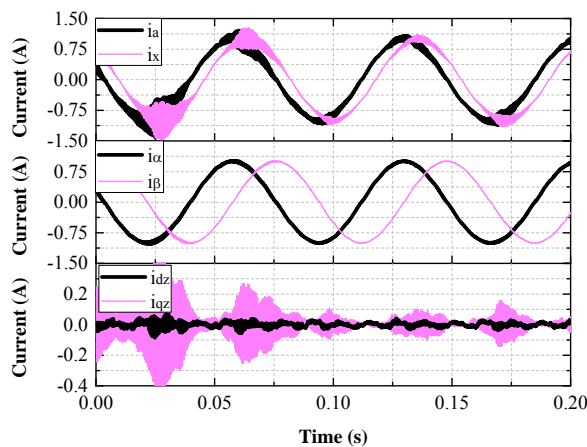


Fig.13 Experiments of current steady response assuming  $r_q = 4.5$ .

This experiment indicates that the two-individual current control may have potential instability issues if the actual  $r_q$  is larger than the critical value. To avoid the potential instability,  $K_p$  for two-individual control should be reduced, and consequently, the torque dynamic performance will be compromised. Therefore, if the mutual coupling between the two sets of the dual three-phase machine is not designed properly, the current control stability and torque dynamic performance may not be guaranteed at the same time. If there is strong mutual coupling between two sets and the two-individual current control has to be employed, the PI gains can be tuned according to the current response in the  $\alpha\beta$  sub-plane without causing the instability issues in the  $z_1z_2$  sub-plane.

### C. Comparison of Dynamical Performance

The torque dynamic performance of the two-individual current control and the VSD control are compared by step  $i_q$  current responses. The PI gains for the VSD control are optimized individually according to (31), whilst two-individual current control has the same PI gains as the current controller in  $\alpha\beta$  sub-plane in VSD control. The current reference is stepped from 0.5A to 1.5A at the time of 0s. The  $q$ -axis current feedback with VSD control and two-individual current control are shown in Fig. 14. It is evident that they have the equivalent  $i_q$  response, which indicates that they have the same torque dynamic performance. Therefore, if there is very strong mutual coupling between the first set and second set, the VSD control should be employed to guarantee the dynamic performance. However, if there is weak mutual coupling between the two sets, both two-individual current control and VSD control can be employed, depending on the practical implications of the application it is to be utilised for.

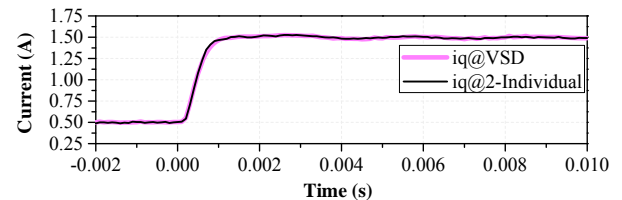


Fig. 14 Comparison of dynamic performance.

## VI. CONCLUSIONS

The two-individual current control and the VSD control for dual three-phase PMSM are compared and their relationship is revealed. The potential instability of the two-individual current control resulting from the mutual coupling between two sets of three-phase windings in the dual three-phase machine has been investigated. If the mutual coupling between two sets is weak, both the two-individual current control and VSD control can be employed. If the two-individual current control has to be employed in industry, to avoid the potential instability of the two-individual control, the ratio of the equivalent inductances in  $dq$ -frame and  $dqz$ -frame should be kept below a certain acceptable level, which provides the design criterion for mutual coupling between the two sets. It can be concluded that:

- a) The two-individual current control is equivalent to the VSD control having the same PI gains for current controllers



in both  $\alpha\beta$  and  $z_1z_2$  sub-planes;

b) The two-individual current control has potential instability issues when there is a strong mutual coupling between the two sets of single three-phase windings;

c) The two-individual current control could have the same dynamic performance as the VSD control without stability issues if the mutual coupling between two sets is weak to some extent.

## VII. APPENDIX A

### VSD CONTROL FOR DUAL THREE-PHASE MACHINE Equation Section (Next)

According to VSD theory [11], the six-dimensional machine system can be decomposed into three orthogonal sub-spaces, i.e.  $\alpha\beta$ ,  $z_1z_2$ ,  $o_1o_2$  sub-planes. By the transformation matrix(A1), different harmonics are mapped to different sub-planes. The fundamental and  $(12k\pm 1)$ th,  $k=1, 2, \dots$  harmonics in real frame are mapped to  $\alpha\beta$  sub-plane; the  $(6k\pm 1)$ th,  $k=1, 3, 5, \dots$  harmonics in real frame are mapped to  $z_1z_2$  sub-plane; the  $(3k)$ th,  $k=0, 1, 3, 5, \dots$  harmonics in real frame are mapped to  $o_1o_2$  sub-plane.

$$\begin{bmatrix} F_\alpha & F_\beta & F_{z_1} & F_{z_2} & F_{o_1} & F_{o_2} \end{bmatrix}^T = [T_6] \cdot \begin{bmatrix} F_a & F_x & F_b & F_y & F_c & F_z \end{bmatrix}^T \quad (A1)$$

where  $\theta_s = \pi/6$  and  $[T_6]$  can be expressed as

$$[T_6] = \frac{1}{3} \begin{bmatrix} 1 & \cos(\theta_s) & \cos(4\theta_s) & \cos(5\theta_s) & \cos(8\theta_s) & \cos(9\theta_s) \\ 0 & \sin(\theta_s) & \sin(4\theta_s) & \sin(5\theta_s) & \sin(8\theta_s) & \sin(9\theta_s) \\ 1 & \cos(5\theta_s) & \cos(8\theta_s) & \cos(\theta_s) & \cos(4\theta_s) & \cos(9\theta_s) \\ 0 & \sin(5\theta_s) & \sin(8\theta_s) & \sin(\theta_s) & \sin(4\theta_s) & \sin(9\theta_s) \\ 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 \end{bmatrix} \quad (A2)$$

By applying the standard Park transformation shown in (A3), the variables in  $\alpha\beta$  sub-plane can be converted to  $dq$  synchronous frame for dual three-phase system.

$$\begin{bmatrix} F_d \\ F_q \end{bmatrix} = [T_{dq}] \begin{bmatrix} F_\alpha \\ F_\beta \end{bmatrix}; \quad [T_{dq}] = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix} \quad (A3)$$

The variables in  $z_1z_2$  sub-plane can be converted to a new frame designated as  $dqz$ -frame by transformation as below [26].

$$\begin{bmatrix} F_{dz} \\ F_{qz} \end{bmatrix} = [T_{dqz}] \begin{bmatrix} F_{z_1} \\ F_{z_2} \end{bmatrix}; \quad [T_{dqz}] = \begin{bmatrix} -\cos\theta & \sin\theta \\ \sin\theta & \cos\theta \end{bmatrix} \quad (A4)$$

where  $F$  is  $v$ ,  $i$ , or  $\psi$ , which correspond to voltage, current, and flux respectively. Then the  $(6k\pm 1)$ th  $k=1, 3, 5, \dots$  harmonics in  $z_1z_2$  sub-plane are converted to  $(6k)$ th harmonics in  $dqz$  frame.

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modelling of real system uncertainty and robust stability, design and control of power electronic converters for enhanced power quality.



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