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eprints@whiterose.ac.uk https://eprints.whiterose.ac.uk/  Integration of aero-elastic belt into the built environment for lowenergy wind harnessing: current status and a case study
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## 9 ABSTRACT

Low-powered devices are ubiquitous in this modern age especially their application in 10 the urban and built environment. The myriad of low-energy applications extend from 11 12 wireless sensors, data loggers, transmitters and other small-scale electronics. These devices which operate in the microWatt to milliWatt power range and will play a 13 14 significant role in the future of smart cities providing power for extended operation with little or no battery dependence. Low energy harvesters such as the aero-elastic 15 belt are suitable for integration with wireless sensors and other small-scale electronic 16 17 devices and therefore there is a need for studying its optimal installation conditions. In this work, a case study presenting the Computational Fluid Dynamics 18 19 modelling of a building integrated with aero-elastic belts (electromagnetic 20 transduction type) was presented. The simulation used a gable-roof type building 21 model with a 27° pitch obtained from the literature. The atmospheric boundary layer flow was employed for the simulation of the incident wind. The work investigates the 22 23 effect of various wind speeds and aero-elastic belt locations on the performance of 24 the device giving insight on the potential for integration of the harvester into the built 25 environment.

26 The apex of the roof of the building yielded the highest power output for the aero-27 elastic belt due to flow speed-up maximisation in this region. This location produced 28 the largest power output under the 45° angle of approach, generating an estimated 29 62.4 milliWatts of power under accelerated wind in belt position of up to 6.2 m/s. For 30 wind velocity of 10 m/s, wind in this position accelerated up to approximately 14.4 31 m/s which is a 37.5% speed-up at the particular height. This occurred for an 32 oncoming wind 30° relative to the building facade. For velocity equal to 4.7 m/s under 33 0° wind direction, airflows in facade edges were the fastest at 5.4 m/s indicating a 34 15% speed-up along the edges of the building.

35

## 36 KEYWORDS

Aero-elastic flutter; Buildings; Computational Fluid Dynamics; Energy; Simulation;
 Aero-elastic belt

### 39 **1. INTRODUCTION**

The buildings sector demands 20 to 40% of total global power intake. This corresponds to values greater than the consumptions of industry and transport sectors [1]. Therefore new technologies that can mitigate or reduce the building energy demand are increasingly being developed; one of them is wind energy technology. One major benefit of building-integrated wind energy harvesting isbringing the power plant closer to the power consumers.

46

With the public having increased power creation capabilities, people can expect higher energy efficiency and reduced dependence to energy companies, lower carbon footprint and overall stimulation of the economy. Furthermore, it will decrease the load of the grid, dependence on diesel generators (in events of power outage) and more notably, lower transmission costs.

52

However, urban and suburban locations pose considerable problems for conventional mounted turbines. First is the significant turbulence in these areas, preventing the turbines from harnessing laminar wind flow. In these conditions wind turbine installers face deficiency in analysing the more complex wind conditions. This leads to the issues of unfavourable turbine site selection and therefore deficient power production.

59

Extreme vibration and noise generated by conventional wind turbine operation also present a great challenge in their integration into buildings. Another issue that rotational turbines face is the hazard of having blades fly off. These factors contribute to the anxiety of turbine installation among building owners and residents. But possibly the biggest challenge to the building-integrated wind turbine (BIWT) is its cost-effectiveness. Smaller wind turbines suitable for urban installations when fastened onto buildings have a high cost-to-energy-production ratio.

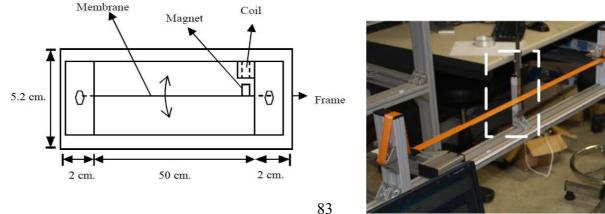
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68 An emerging and novel alternative to the conventional turbines are wind-induced 69 vibration energy harvesters. In recent years, low-energy power generation devices 70 have been receiving increased attention due to their potential integration with self-71 powered micro-devices and wireless sensor networks in urban areas. Nano-72 generators have a wide span of potential power applications ranging from 73 environmental and infrastructure monitoring, personal electronics to even wireless 74 biosensing [3]. The power produced by these nano-generators is adequate to run 75 light-emitting diodes [4], small liquid crystal displays [5] and self-powered wireless 76 sensor nodes [3].

77

Such devices like the aero-elastic belt as shown in Figure 1 can be in a form of a small-scale wind generator that takes advantage of the flutter effect. Unlike turbinebased generators, the aero-elastic belt is a small-scale, light and inexpensive direct-

81 conversion energy harvester which does not use any bearings, gears or rotors.



85 Fig 1. (a) Schematic diagram of an aero-elastic belt [6] (b) Example of experimental 86 aero-elastic belt setup [7]

87

88 The standard rotating wind turbines mostly are not as effective when transformed into 89 smaller types. However, flutter-based generators like the aero-elastic belt can designed to fit lighter applications. It can operate in the range of microWatt to 90 91 milliWatt power generation. Although the power output is low, it has its advantages compared to regular wind turbines. The aero-elastic belt is cost effective and can 92 93 also be made of simple household materials. The device is small, compact, modular 94 and suitable for turbulent flow, making it appropriate for integration with wireless 95 sensors – an area which has the biggest application potential for this technology [8]. 96

97 Current global demand for wireless sensors is increasing especially in applications of 98 equipment supervision and monitoring revolving around energy expenditure, usage, 99 storage and remote manipulation especially in the following areas:

- Medicine and health: prescription of patient-sensitive medications, remote monitoring and vital signs alerts
- Buildings: energy spending monitoring, security surveillance, structural health 102 103 monitoring, damage detection 104
  - Industry: systems tracking, data transfer, and equipment remote control
  - Infrastructure & environment: traffic monitoring, indoor air safety levels, air and water pollution levels
- 106 107

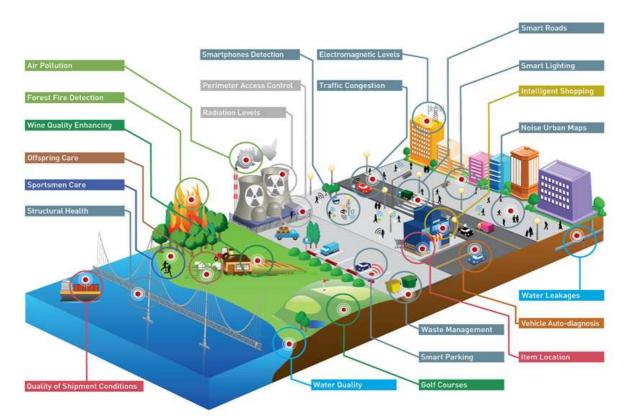
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108 These devices can be powered using low-energy generation technologies such as 109 flutter and vibration harvesters. Figure 2 illustrates the wide array of applications that 110 wireless sensors are operating in including, but not limited to, cities and urban 111 environments. The primary obstacles to what is referred to as the "deploy-and-forget" quality of wireless sensor networks (WSN) are their limited power capacity and their 112 113 batteries' unreliable lifespans. To overcome these issues, low-energy harvesting of ambient energy resources like air flow, water flow, vibrations, and even radio waves 114 115 has become an encouraging new field. Along with advancements in microelectronics, power requirements for wireless sensor nodes keep on dropping, ranging presently 116 from microWatts to a few milliWatts [8]. 117

118



- 119
- 120 121

Fig. 2. Applications of wireless sensors in smart cities [9]

122 The global market for energy harvesting devices and modules is growing with a 123 forecasted increase in value from \$19 Million in 2012 to \$227 Million in 2017 – a 12-124 times increase in five years, with an annual growth of 51% per annum. It is important 125 to mention that within the range of applications of energy harvesting devices, the 126 buildings sector makes up the biggest portion of the market.

127

128 In 2011, there were more than 1 Million harvester modules sold across the world for 129 building applications alone. This is due to the large network of wireless switches for 130 lighting, air conditioning and sensors detecting occupants' presence and measuring 131 ambient room conditions such as humidity, all found in commercial buildings. Driving the market growth of energy harvesters are the large reduction in installation costs 132 133 and maintenance-free operability requiring little or no wires [10]. Therefore, new 134 methods should be developed to further assess and optimised its integration with the 135 built environment.

136

In this paper, the current status of vibration energy harvesting technologies, their
 scopes, advantages and limitations will be discussed followed by case study
 focusing on the analysis of the integration of an aero-elastic flutter technology into
 buildings using Computational Fluid Dynamics (CFD) modelling.

## 141 2. PREVIOUS RELATED WORK

142 In the following sections, different technologies that can harness flow induced 143 vibration energy are examined.

## 145 **2.1 Flow-induced vibrations**

146

Aero-elastic flutter or simply referred to in this study as flutter, is a phenomenon of self-feeding oscillations upon which the aerodynamic forces on a structure associate with the inherent oscillation mode thereby producing fast recurring motion. Flutter can take place upon any body exposed to powerful steady fluid flow, under the precondition that a reinforcing feedback response ensues concerning the body's oscillation and the working fluid forces [8].

153

Flutter on itself can be severely catastrophic. Historic examples of flutter are the collapse of Tacoma Narrows Bridge and that of Brighton Chain Pier, as shown in Figure 3. The structures collapsed due to span failure caused by aero-elastic flutter [11]. Nevertheless, this seemingly violent nature of flutter can also be its source of strength when its potential for energy harnessing is explored.

159



Fig. 3. (a) A painting of the Brighton Chain Pier collapse in 1836 (b) A photo of the Tacoma Narrows bridge collapse in 1941 [11]

162 163

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161

Flow-induced vibrations (FIV) is an umbrella category that includes flutter-induced vibrations or what the study will refer to as aero-elastic flutter or simply flutter, and vortex-induced vibrations [8].

167

## 168 **2.1.1 Extracted power and efficiency**

169

For an incoming fluid flow, the energy that can be extracted is derived from the sum of two terms: the plunging term  $P_Y(t)$  and the pitching term  $P_{\theta}(t)$ :

172  
173 
$$P_{\theta}(t) = P_{Y}(t) + P_{\theta}(t) = F_{Y}(t) V_{Y}(t) + M(t) \omega(t)$$
(1)

174

175 where  $F_Y$  is the component of the force in the y-direction while *M* is the resulting 176 torque relative to the pitching centre.

- 177
- 178 Instantaneous power can be expressed in nondimensional form as:
- 179

$$C_P = \frac{P}{\frac{1}{2}\rho U_{\infty}^3 c} \tag{2}$$

185 186

182 When integrated over one cycle, this instantaneous  $C_P$  gives the time-averaged 183 power coefficient over one cycle called  $C_{Pmean}$ , given by the expression: 184

$$C_{Pmean} = C_{Phmean} + C_{P\theta mean} = \frac{1}{TU_{\infty}} \int_0^T [C_Y(t)V_Y(t) + C_M(t)\omega(t)]dt$$
(3)

187 where *T* is the period of oscillation,  $C_Y(t)$  is the instantaneous lift coefficient and 188  $C_M(t)$  is the momentum coefficient. These quantities are given in terms of  $\rho$ ,  $U_\infty$  and 189 *c*:

190 
$$C_Y(t) = F_Y(t) / \frac{1}{2} \rho U_{\infty}^2 c$$
 (4)

191 
$$C_M(t) = M(t) / \frac{1}{2} \rho U_{\infty}^2 c$$
 (5)

192

193 The ratio of the average total power yield to the total power obtainable from the 194 incoming airflow flowing across the swept

region is defined as the power-extraction efficiency  $\eta$ :

196

$$\eta = \frac{P_{mean}}{\frac{1}{2}\rho U_{\infty}^3 A} = C_{Pmean} \frac{c}{A} \tag{6}$$

197 198

where *A* is the overall vertical distance of the movement of the aerofoil with bothplunging and pitching motions being considered.

201

While it has been established that energy extracted from airflow originates from the sum of a plunging contribution  $C_{Ph}$  and a pitching contribution  $C_{P\theta}$ , for a foil with modified flapping motion the major source of extracted energy is through the plunging motion; the average extracted energy from the pitching motion is almost zero.

207

For a fixed pitching amplitude  $\theta_0$ ,  $C_{Pmean}$  increases with the reduced frequency *k* at first, then  $C_{Pmean}$  eventually decreases with the further increase in *k*. For every value of  $\theta_0$  there exists an optimal *k* for the maximum  $C_{Pmean}$ .

211

Similarly, for a fixed reduced frequency *k* this time, the same behaviour for  $C_{Pmean}$ can be noticed with respect to varying  $\theta_0$ . Due to their effects to the angle of attack, *k* and  $\theta_0$  were observed to affect the development of leading edge vortices (LEV) as well as changes in the lift coefficient  $C_Y$ . It was also observed that high values for *k*  and low values for  $\theta_0$  lead to higher plunging velocity  $V_Y$  and better synchronization between the lift coefficient and the plunging velocity compared to different scenarios. Concerning the amount of energy extracted, this is the best case. Therefore, to achieve the best performance for energy generation, relatively high *k* and low  $\theta_0$  are preferred [12].

221

## 222 2.2 Technologies

223

In this sub-section, three types of vibration energy harvesting technologies are
 reviewed; electromagnetic, piezoelectric and triboelectric devices.

226

## 227 **2.2.1 Electromagnetic Vibration Devices**

228

An example of an electromagnetic vibration device is the aero-elastic belt or also commonly known as the wind-belt, which is a small-scale wind generator that operates based on the phenomenon of aero-elastic flutter. The original invention puts the power production of wind-belts in the range from several milliWatts for the smallest-scale device to a 7.2 kWh device which is 1 m long operating in 6 m/s winds [13]. A significant upside is the production cost of such a low-power device could be very small as well.

236

237 In the study of Pimentel et al. [14], a wind-belt prototype was characterised. The 238 device was 50-cm long and supported by a Plexiglass frame, with a tensioned Mylar 239 membrane installed with bolts on its ends. This membrane had one side that is 240 smooth and the other rough, thereby producing a simple aerofoil. The generator had 241 an electromagnetic transducer incorporated in one end of the membrane. This 242 transducer makes use of two small neodymium (NdFeB) magnets and a static coil 243 positioned adjacent to the magnets. The wind flowing around the tensioned 244 membrane caused it to flutter while the magnets vibrate relative to the coil, therefore inducing a current flowing in the coil, producing electric power as shown in the results 245 in Figure 4. Based on the experimental results the minimum and maximum power 246 247 output were: 5 milliWatts for airflow velocity equal to 3.6 m/s and load resistance of 10  $\Omega$  and 171 mW at 20 m/s, 110  $\Omega$  resistance and 38.1 N membrane tension. 248

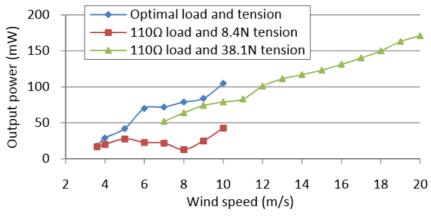




Fig. 4. Power output for the wind-belt experimental test setup in [14]

251

Numerous parameters that affects the wind belt harvester's performance like the membrane tension, membrane length, magnet position and number of magnet were investigated by Arroyo et al. [13] using experimental testing. The study highlighted the optimal values for the key parameters, focusing on low wind speeds ranging from 1 to 10 m/s but with powerful vibration acceleration [13]. The experimental results showing the amplitudes and frequencies for varying lengths of the ribbon used is shown in Figure 5.

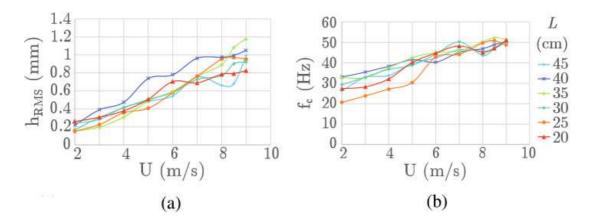


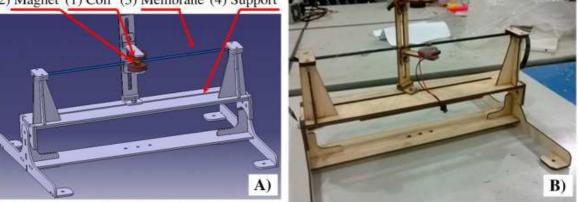
Fig. 5. (a) Amplitude and (b) Frequency of vibration as a function of wind speed for
various ribbon lengths [13]

- 261
- 263

Dinh Quy et al. [15] investigated a windbelt with the magnet mounted centrally along the flexible membrane made of a type of kite fabric called ripstop nylon fabric as shown in Figure 6. The single unit micro generator was able to produce power in the range of 3 - 5 mW. Five larger versions of these micro generators were combined to construct a windpanel, and together were able to generate 30 to 100 mW of power at wind speeds of less than 8 m/s. At low wind speeds between 3 to 6 m/s, the output current is approximately 0.2 to 0.5 mA, the generated voltage is between 2 to 2.5 V,

- and the generated power is about 2 to 3 mW, under membrane oscillation frequency 271
- 272 of approximately 5 Hz.

(2) Magnet (1) Coil (3) Membrane (4) Support



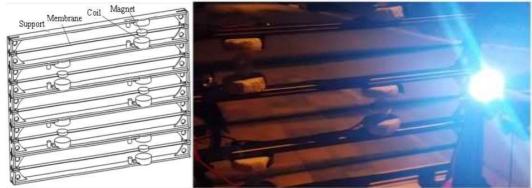
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275

Fig. 6. (a) 3D model of the wind belt design and (b) Fabricated test model studied in [15]

276

277 In Dinh Quy et al. [15] five of the single membrane generators were merged to 278 fabricate a windpanel to increase the overall power output. The design of a single 279 generator in this study was made in such a way that grouping can easily be 280 constructed or dismantled. For each generator, two conducting coils of 4000 turns 281 each were used and placed parallel to each other as shown in Figure 7.



- 282
- 283
- 284

Fig. 7. (a) The 3D model of the windpanel - a combination of five windbelts (b) Testing of the windpanel powering an LED light in actual wind conditions [15]

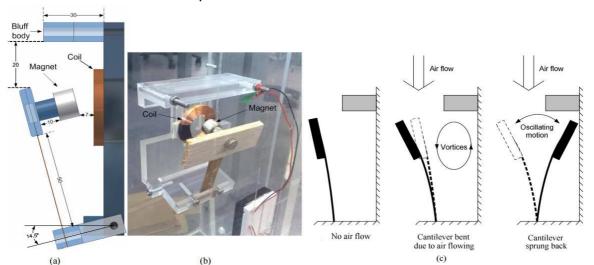
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286 The earlier versions of flutter generators had practical problems as identified by Fei 287 et al. [16]. One instance would be the physical contact of the vibrating membrane 288 with the conductors once the membrane oscillation amplitude is greatest during 289 strong winds. The positioning of the magnets fastened on the membrane must be 290 carefully examined to guarantee optimised magnetic flux experienced by the 291 conductors, which was also addressed by Dinh Quy et al. [15]. To tackle these 292 problems and at the same time increase the efficiency of energy harvesting by a 293 fluttering membrane, a novel variety of flutter-based-harvester was proposed in [16] 294 which consists of a beam that acts as the support, an electromagnetic resonator, a power management circuit, a supercapacitor for storage of charge [16] and a spring. 295

A thick polymer belt was used as the vibrating membrane having dimensions of 1 m by 25 mm by 0.2 mm. The electromagnetic resonator was positioned close to the end of the membrane. This was the preferred placement because of a higher bending stiffness of the membrane close to the secured ends. This configuration allowed a heavier magnet to be supported by the vibrating membrane [16]. The supercapacitor is easily replaceable.

302

Dibin Zhu et al. [17] investigated a device with an aerofoil connected to a beam which was positioned after a bluff body as illustrated in Figure 8. This harvesting device operated at a relatively low wind velocity of 2.5 m/s and generated power equal to microWatts. A disadvantage of this setup was requiring an initial displacement for the aerofoil in order to operate.



308

## Fig. 8. (a) Schematic of energy harvester studied in [17] with measurements in mm

- 310 (b) Experimental setup of the harvester (c) Operating principle of the energy
   311 harvester
- 312

313 Wang et al. [18] demonstrated a novel EMG-resonant-cavity wind generator 314 integrated with dual-branch reed and tuning fork vibrator. The study highlighted the 315 device's magnetic circuit being able to intensify the rate of change of the time-varying 316 magnetic flux. The tuning-fork assembly of the device was able to further decrease 317 system losses. Peak power output was observed to be 56 mW for airflow speed 318 equal to 20.3 m/s with corresponding conversion efficiency of 2.3% at airflow speed 319 of 4 m/s. The experiments provided evidence that the device can operate in a large 320 range of wind speeds. The diagrams and working process of this wind energy 321 harvester are shown in Figure 9.

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323

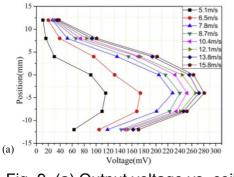
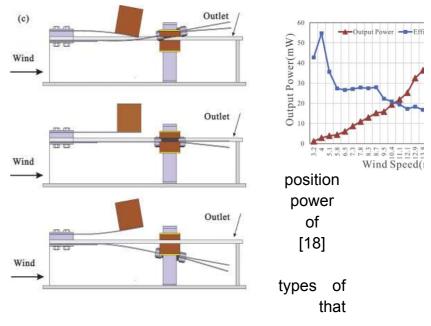


Fig. 9. (a) Output voltage vs. coil
[18] (b) Wind speed vs. max output
and efficiency (c) Working process
electromagnetic energy harvester

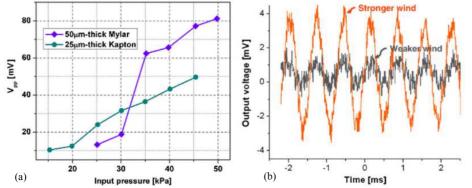
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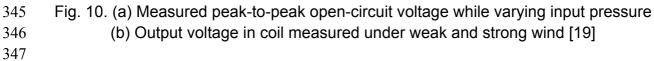
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330 Kim et al. [19] investigated two
331 electromagnetic energy harvesters
332 utilise direct airflow power



333 conversion to mechanical oscillations - (i) a wind-belt-like oscillatory linear energy 334 harvester specifically for powerful air streams and (ii) a harvester centred on a 335 Helmholtz resonator concentrated on sifting energy from weaker air current such as 336 environmental air streams. The proposed wind-belt-like energy harvester was 337 centred on the principle of aero-elastic flutter effect. It was composed of a polymer 338 resonator together with entrenched magnets, a polymer casing and copper coils. The moving part of the generator was made up of an oscillating membrane with fastened 339 340 permanent magnets, placed in the centre of the flow passage. The device casing had 341 an inlet and an outlet for the airflow. The peak-to-peak open-circuit voltage for two 342 types of belt materials, Mylar and Kapton, are shown in Figure 10 (a), while output 343 voltage was measured for different airflow strengths shown in Figure 10 (b).





The second energy harvester made use of a Helmholtz resonator as a mechanism to concentrate oncoming wind flow. In simple terms, a Helmholtz resonator has a chamber filled with air, with an unconstrained neck, in which an ordinary fluid oscillation takes place. Being a resonator, the air within the neck serves as the
oscillating weight while air within the air chamber serves as the elastic mechanism.
Figure 11 displays the operating principle for this energy harvester. This harvester is
claimed to be able to operate in extremely slow flows.

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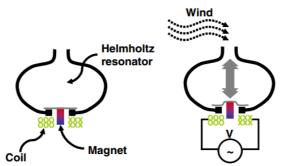
356 The wind-belt-like oscillatory energy harvester offered a peak to peak amplitude AC

voltage equivalent to 81 mV at frequency of 0.53 kHz, generating from an input of 50

358 kPa of pressure. The Helmholtz-resonator-centred generator reached a peak to peak

amplitude AC voltage of 4 mV at frequency of 1.4 kHz, from 0.2 kPa pressure input,

360 corresponding to 5 m/s or 10 mph wind speeds.



- Fig. 11. Schematic plan illustrating the principle of operation of energy harvester in
   [19]: (a) at rest state; (b) at resonance through wind flow.
- 364

Munaz et al. [20] demonstrated that there was potential for the power generation of the electromagnetic energy harvester via vibrations to be amplified many times over by the introduction of several magnets as the moving mass even if all other experimental variables were fixed. The device generated 224.72  $\mu$ W in DC power, having 200  $\Omega$  load resistance for a 5-magnet system. This device operates at a subtle resonance frequency equivalent to 6 Hz, which was deemed appropriate for handheld devices and remote sensing applications.

372

Wang et al. [21] discussed a study on energy harvesting through vibrations caused by the Karman vortex street through an electromagnetic harvester producing instantaneous power of 1.77  $\mu$ W under exposure to the vortex street. Figure 12 shows the measured displacement history and the open circuit voltage induced by the coil which measured approximately 20 mV peak-to-peak. In the same study it was stated that the vibrations can also be harnessed from other fluid flow - river streams, tire air pressure flow or fluids in mechanical equipment.

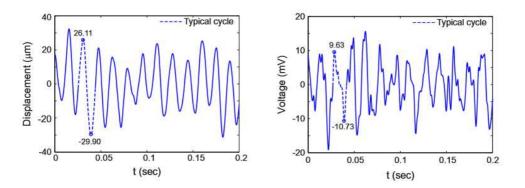
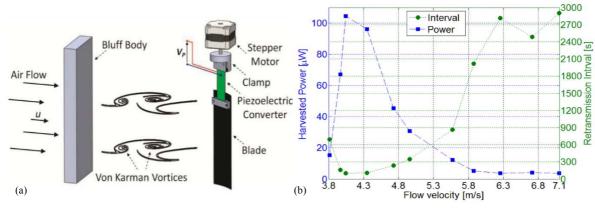


Fig. 12. (a) Magnet displacement and (b) Induced voltage by the coil for a typical
 cycle [21]

- 383 2.2.2 Piezoelectric Energy Harvesting Devices
- 384

385 Demori et al. [22] explored a piezoelectric energy harvesting illustrated in Figure 13 386 (a) where a stepper motor is attached to a piezoelectric converter that can vary the 387 beam angle relative to the flow. The output of the energy harvesting system together 388 with its power conditioning circuit was tested through measurements of the 389 transmission time versus flow. A peak power of 100 µW was collected and 390 transmission time of 2 s was measured. A retransmission interval under 2 minutes 391 was attained. It was noticed that for this system, the highest output was achieved 392 around flow velocity of 4 m/s, as shown in Figure 13 (b).



- 393
- Fig. 13. (a) Piezoelectric energy harvesting system schematic (b) Average power
   output and retransmission time interval as a function of air flow velocity [22]
- 396

397 Shan et al. [23] studied a macrofiber composite piezoelectric energy harvesting 398 device for water vortex, which generated 1.32  $\mu$ W power output under liquid water 399 flow speed of 0.5 m/s, showing the plausibility of using this harvesting technology for 400 liquid flow as well. Weinstein et al. [24] investigated power from a piezoelectric shaft 401 influenced by vortex shedding from a bluff cylinder, which generated 200  $\mu$ W and 3 402 mW of power at air velocities of 3 m/s and 5 m/s.

403

404 Li et al. [25] investigated a piezoelectric energy harvesting device which used flexible 405 piezoelectric materials as "stalks" together with polymer membrane acting as leaf-like 406 structures. The experiment result confirmed a maximum power output of 615 µW for 407 an airflow speed of 8 m/s and 5 M $\Omega$  resistance while using a two-layer stalk. The maximum power density was 2036  $\mu$ W/cm<sup>3</sup> for a single leaf. Furthermore, the work 408 noted that their energy harvesters demonstrated good power performance 409 410 normalized by volume, mass and expenditure. Although their harvesters performed 411 were not effective in terms of power per swept-area. The study recommended that 412 the swept-area performance could be enhanced through assembling multiple 413 harvesters behind one another. Figure 14 shows the performance of the piezo-leaf where in (b) different shapes of the leaf were tested including square, round, 414 415 isosceles triangle with  $30\Box$  base angle, isosceles triangle with  $45\Box$  base angle, 416 equilateral triangle, and rectangle (Sq, Ro, T30, T45, T60 and Re, respectively)

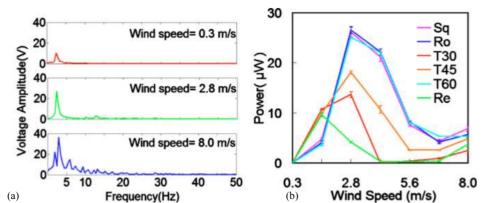
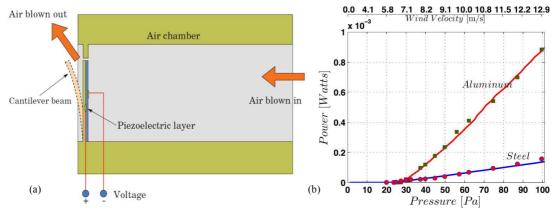


Fig. 14. (a) Wind response of piezo-leaf with varying wind speeds (b) Power output of the different shapes of piezo-leaf [25]

420

417

421 St. Clair et al. [26] investigated a micro-generator that utilised flow-generated self-422 excited fluctuations. This concept was analogous to a musical harmonica that 423 produces sounds through vibrations of its reeds when fluid is blown. This device 424 performed with an power generation from 0.1 to 0.8 mW while operating at airflow speeds spanning between 7.5 and 12.5 m/s. Figure 15 shows the general working 425 426 principle of the device and the maximum power output as a function of air pressure 427 for two types of beams (Aluminium and Steel) where the curves represent simulation 428 results and the dots indicate experimental results.



429

Fig. 15. (a) Piezoelectric energy harvester utilising flow-induced oscillations (b)
Maximum power output as function of air pressure for two beam types – Aluminium
and Steel [26]

434 Erturk et al. [27] examined the concept of piezo-aero-elasticity for energy harvesting 435 using a mathematical model and experiments. The harvester has a 50 cm long 436 aerofoil that is vertically oriented. Two piezoceramics of type Lead Zirconate 437 Titanate-5A (PZT-5A) were fastened to two extremities of the aerofoil. Upon 438 interacting with air, the aerofoil moves and triggers the piezoceramics thereby 439 generating electric current. The results showed 10.7 mW of power yield for 9.3 m/s 440 flutter velocity using a resistive load of 100 kΩ load.

441

442 Dickson [28] developed a novel deployable flutter energy harvester based on a structure resembling a tree composed of several "leaves" of piezoelectric devices. 443 444 Preliminary experiments demonstrated that power output by the cylinders was low 445 mainly due to the quality and dimensions of chosen piezoelectric materials. Yet there 446 were results referred to from Bryant et al. [29] and McCarthy et al. [30] that showed 447 that there was an optimum spacing for the tandem of devices that triggered trailing 448 cylindrical energy harvesters to generate appreciably greater energy compared to the leading harvester. It is noteworthy that this finding was in contrast to that of 449 450 conventional horizontal axis wind-turbines (HAWTs), for which tandem orientations 451 generally avoided because to energy harvesting shortfalls in wakes areas shown by Burton et al. [31]. Figure 16 shows the leaf-type harvester with its performance under 452 453 smooth and turbulent airflows.

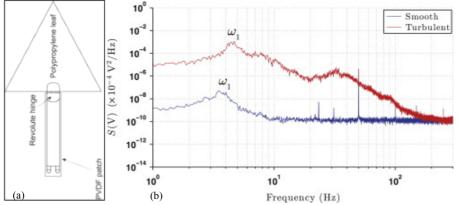


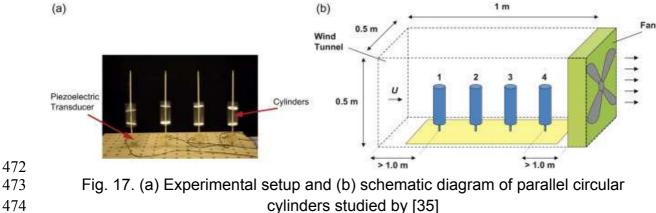


Fig. 16. (a) The Polyvinylidene-fluoride (PVDF) [28] leaf; and (b) Harvester's voltage
spectral density for smooth and turbulent wind flow of 8 m/s at 135° flow angle [32]
457

458 The "tree" concept was tested by Li et al. [33]. This harvester with leaves made of 459 Polyvinylidene-fluoride (PVDF) was subjected to wind speeds from 3 to 8 m/s. The 460 leaves are triangular in shape. It was earlier discovered in [25] that the triangular 461 shape provided the highest power output among several different tested shapes. It 462 was also found out that the energy harvester functioned best when it has flutter oscillations under the Limit-Cycle Oscillations (LCOs) as opposed to chaotic flutter 463 [34]. An electroactive area power density,  $P_{EAA} \leq 45 \,\mu W/cm^2$  was attained [25] by the 464 piezoelectric tree, where it was shown in [39] that 296 µW peak power war 465 466 harnessed at top speed of 8 m/s.

467

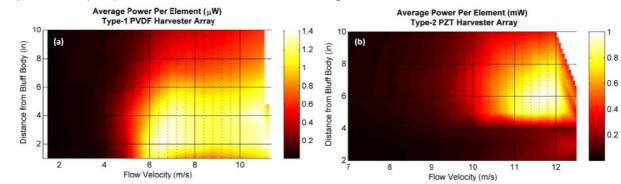
Hobbs and Hu [35] developed energy harvesters based on rounded cylinders which
were positioned in groupings at different spacings subject to wind tunnel flow as
shown in Figure 17. These cylinders were fastened to piezoelectric discs close to the
bottom and were allowed to oscillate in the cross-stream direction.



474 475

Hobeck and Inman [36] examined energy harvester called "piezoelectric grass". In
this investigation, several piezoelectric ceramic materials made of PZT were
configured such that there were bending oscillations in the structure near-wake flow.
Power output of 1 mW per PZT beam was attained for a flow speed of about 11.5

480 m/s, and it was also discovered that optimum turbulence conditions could maximised 481 the power output. Figure 18 shows how the average power output is related to the 482 position of the harvester with respect to the bluff body and the velocity of airflow for 483 two types of harvester arrays – PVDF and PZT. The PZT type generates higher 484 power output per element in the milliWatt range, as mentioned earlier.





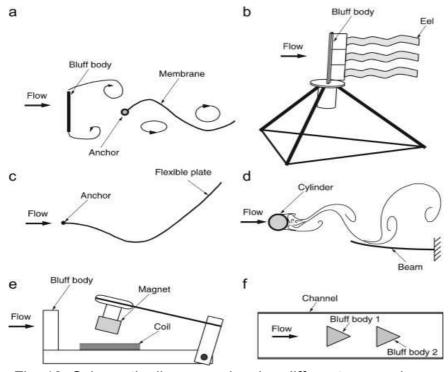
486 Fig. 18. Power output with varying flow velocity and bluff body position for (a) PVDF
 487 harvester array, and (b) PZT harvester array [36]

488

489 Akaydın et al. [37] investigated energy harvesting system based on piezoelectric 490 shaft along the trail of a round cylinder subjected to unsteady wind flow. As illustrated 491 in Figure 19 (d), the shaft is configured to be parallel with respect to the oncoming 492 wind and was held secured at the downstream edge. The study showed that the gap 493 between the vortices' circulation and the vortices distance from the shaft had 494 influence on the output power was. The greatest power was around 4  $\mu$ W with 495 Reynolds number of approximately 14800 at the shaft's resonant frequency.

496

497 A known mechanism for boosting pressure variation amplitudes occurring in a vortex 498 street was to utilise an array of structures in group configuration as shown in Figure 499 19 (f). [38] and [39] both stated that two bluff structures in arranged in such a way 500 could increase the hydrodynamic oscillations created by the phenomenon of vortex 501 shedding. Consistency of the vortices was also enhanced when two bluff structures 502 were present instead of a single one [40].

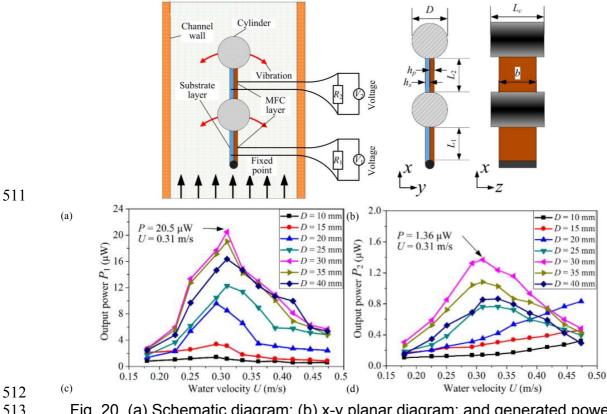


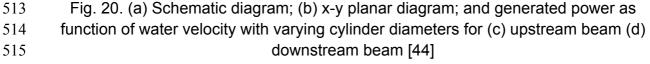
503 504

Fig. 19. Schematic diagrams showing different energy harvesting devices presented in (a) [41]; (b) [42]; (c) [43]; (d) [37]; (e) [17]; (f) [38]

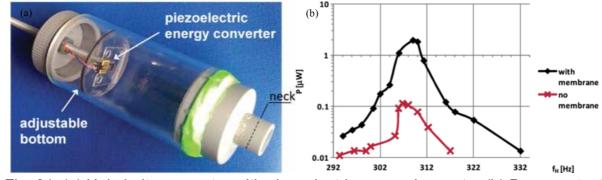
505 506

Song et al. [44] investigated a piezoelectric device based on composite cantilever immersed in water instead of air illustrated in Figure 20. Highest power output of the harvester was observed to be 21.86  $\mu$ W which was attained at a water flow of 0.31 m/s.





517 Matova et al. [45] described an energy harvester containing an enclosed 518 piezoelectric device inside a *Helmholtz resonator*, as shown in Figure 21 (a). It was 519 discovered in the study that enclosed harvesters performed better than exposed 520 harvesters because the enclosure negated the viscous effect of air within the 521 Helmholtz cavity and guaranteed that only the fluctuation stimulated the harvester. 522 Tests revealed that the energy harvester produced a peak power of 2 µW subjected to air flow speed of 13 m/s at a frequency of 309 Hz. However, a disadvantage of the 523 524 Helmholtz resonator was its resonant frequency's dependence to the surrounding 525 temperature. This entailed that this type of harvester could only be utilised in settings with steady temperature ranges, otherwise the harvester must be redesigned to 526 527 operate at a wider frequency range. Figure 21 (b) shows the generated power of the 528 harvester for a constant flow velocity of 14 m/s and load resistance of 3.3 MQ with 529 varying cavity volume of the Helmholtz resonator.



530 531

532

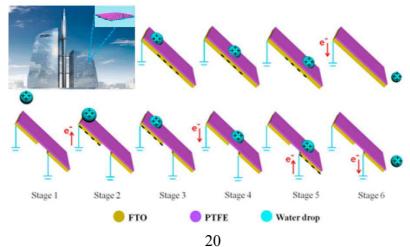
Fig. 21. (a) Helmholtz resonator with piezoelectric energy harvester (b) Power output of harvester for airflow of 14 m/s with resistance of 3.3 M $\Omega$  [45]

## 533 2.2.3 Triboelectric and Hybrid Generators

534 Xie et al. [46] proposed triboelectric nanogenerator (TENG) that was able to harvest 535 miniature wind energy ambient in normal human habitats developed utilising common 536 materials. This system had a rotating part that enabled the sweeping motion of several triboelectric films called polytetrafluoroethylene (PTFE), thereby making 537 538 alternating contact and separation with Aluminium sheets. This process of cyclical physical contact and disconnection between distinct planes with opposing 539 540 triboelectric charges was responsible for generating an induced voltage across two electrodes, therefore pushing flow of electrons in an alternating current. This 541 particular rotary triboelectric nanogenerator (R-TENG) was able to achieve a peak 542 power of 62.5 mW, a peak power density of about 39 W/m<sup>2</sup> at airflow speeds of 543 544 around 15 m/s, from approximately 250 V open-circuit voltage with a 0.25 mA shortcircuit current. This investigation had shown that triboelectric nanogenerators could 545 546 work hand-in-hand with wind power.

547

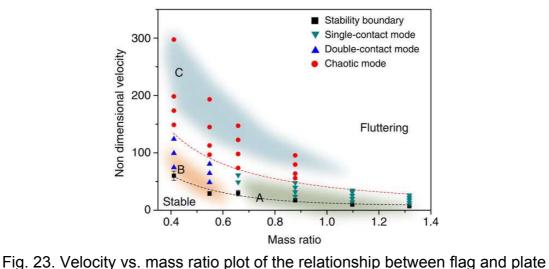
Liang et al. [47] investigated a *multi-unit transparent triboelectric nanogenerator* (MT-TENG), which is intended to harvest energy from ambient water movements like rain water as illustrated in Figure 22. The peak instantaneous power density was measured at 27.86 mW/m<sup>2</sup>. This value is 11.6 times larger than the output of a single transparent TENG of the same operating size.



554 Fig. 22. Working mechanism leading to the improved efficiency of the MT-TENG; 555 inset shows potential application in buildings [47]

556

557 Bae et al. [48] studied a flutter-based wind harvesting triboelectric generator. This 558 flutter-driven triboelectric generator (FTEG) is relatively small being only 7.5 cm long 559 and 5 cm wide. Nevertheless it demonstrated instantaneous outputs of approximately 560 200 V and current of 60 µA under 15 m/s wind speeds equivalent to 158 Hz. This 561 corresponds to 0.86 mW of output power. The authors also characterised the generator by its different modes of operation based on its components' contact type. 562 563 There are three modes they discovered: single, double and chaotic. The transitions 564 between modes are shown in Figure 23, wherein the transition from single to double-565 contact mode ensues corresponding to decreasing mass ratio.



behaviour showing the different contact modes [48].

566

567

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- 569

## 570

571 2.3 Challenges

572 573

Previous studies about the building environment's potential for wind energy harvesting highlighted the need for detailed and accurate analysis of wind flow around buildings. To utilise the effect of wind acceleration above or around buildings and to be able to determine the appropriate type of wind energy technology to be installed sufficient integration analysis has to be conducted. In addition, there is the challenge to analyse optimum position of the wind energy harvesters. Accurate simulations will lead to more information that can result to better decisions [2].

580

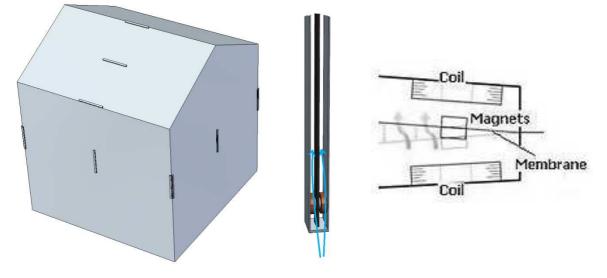
No previous work studied the integration of low-energy vibration harvesting devices in buildings or structures. Most studies for these energy harvesters are carried out in laboratory settings. There is also a lack in numerical studies about these energy technologies. There is a lack in research about the applications of these harvesters in the urban environment. Most theoretical works use unrealistic boundary conditions like the utilisation of uniform flow. Currently very few studies were done involving 587 actual field tests with real-world conditions. If low-energy harvesters are to become 588 widely commercial, field tests observable by the public need to be increased. This 589 study will address this by carrying out an urban flow simulation of a small building 590 integrated with low-energy harvesters and assess the impact of varying outdoor wind 591 conditions.

592

# 5933. CASE STUDY: ANALYSIS OF THE INTEGRATION WITH THE BUILT594ENVIRONMENT

595

596 The work will investigate the effect of various external conditions and device 597 locations on the performance of the aero elastic belt. The simulation will use a gableroof type building model with a 27° pitch as shown in Figure 24. The atmospheric 598 599 boundary layer (ABL) flow will be used for the simulation of the approach wind. The three-dimensional Reynolds-averaged Navier-Stokes (RANS) equations together 600 601 with the continuity and momentum equations will be solved using ANSYS FLUENT 16 for obtaining the velocity field and also pressure field. Sensitivity analyses for the 602 CFD grid resolutions will be executed for verification of modelling. In addition, the 603 604 results of the flow around the buildings and surface pressure coefficients will be validated with previous experimental work. The study will utilise regression analysis 605 and experimental data [6] to estimate the power output of the aero-elastic belt. The 606 607 coil used in the transducer are composed of 38 American wire gauge (awg) enamelled wire with 150 turns and approximately 25 ohms internal resistance [49]. 608 609 Figure 24 shows the location of the aero elastic belt around the building geometry.



610 611

Fig. 24. CAD geometry of building with aero-elastic belt devices

612

## 613 **3.1 Computational Fluid Dynamics modelling**

The fundamental assumptions for the numerical simulation involve a 3D, fully turbulent, and incompressible flow. The flow was modelled by making use of the standard  $k-\varepsilon$  turbulence model, which is a well-established research technique regarding airflows surrounding buildings [50]. The Finite Volume Method (FVM) was utilised with the CFD model together with the Semi-Implicit Method for Pressure619 Linked Equations (SIMPLE) velocity and pressure coupling algorithm using the 620 second order upwind discretisation. The governing equations are the continuity 621 equation (Eqn. 7), momentum equation (Eqn. 8) and energy equation (Eqn. 9). The 622 standard k- $\varepsilon$  transport model was employed to classify the turbulence kinetic energy 623 and flow dissipation rate within the simulation model. The transport equations are 624 shown in Eqn. 10 and Eqn. 11.

625

$$\frac{\partial}{\partial t}(\alpha_q \rho_q) + \nabla \cdot (\alpha_q \rho_q \vec{v}_q) = \sum_{\nu=1}^n (\dot{m}_{\rm pq} - \dot{m}_{\rm qp}) + S_q \tag{7}$$

$$\frac{\partial}{\partial t} (\alpha_q \rho_q \vec{v}_q) + \nabla \cdot (\alpha_q \rho_q \vec{v}_q \vec{v}_q) = -\alpha_q \nabla p + \nabla \cdot \bar{\tau}_q + \alpha_q \rho_q \vec{g} + \sum_{p=1}^n (\vec{R}_{pq} + \dot{m}_{pq} \vec{v}_{pq} - \dot{m}_{qp} \vec{v}_{qp}) + (\vec{F}_q + \vec{F}_{\text{lift},q} + \vec{F}_{\text{vm},q})$$
(8)

$$\frac{\partial}{\partial t}(\alpha_q \rho_q h_q) + \nabla \cdot (\alpha_q \rho_q \vec{u}_q h_q) = \alpha_q \frac{\partial p_q}{\partial t} + \bar{\tau}_q : \nabla \vec{u}_q - \nabla \cdot \vec{q}_q + S_q + \sum_{p=1}^n (Q_{pq} + \dot{m}_{pq} h_{pq} - \dot{m}_{qp} h_{qp})$$
(9)

626

where;  $\vec{v}_q$  denotes the velocity of phase q and  $\dot{m}_{pq}$  and  $\dot{m}_{qp}$  characterizes the mass transfer from the pth to qth phase and vice-versa.  $\bar{t}_q$  denotes the qth phase stressstrain tensor.  $h_q$  denotes the specific enthalpy of the qth phase and  $\vec{q}_q$  denotes the heat flux.  $Q_{pq}$  is the heat exchange intensity between the pth and qth phases and  $h_{pq}$ is the interface enthalpy.  $S_q$  denotes the source term.

632

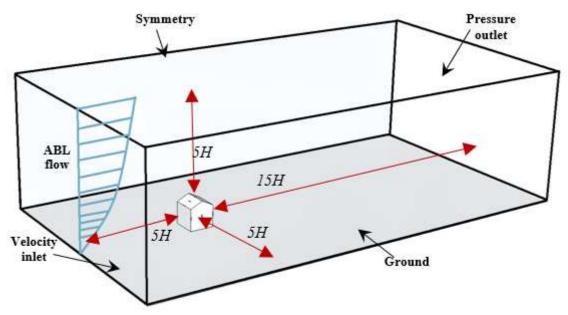
$$\frac{\partial}{\partial t}(pk) + \frac{\partial}{\partial x_i}(\rho k u_i) = \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + G_k + G_b - \rho \epsilon - Y_M + S_k$$
(10)

$$\frac{\partial}{\partial t}(\rho\epsilon) + \frac{\partial}{\partial x_i}(\rho\epsilon u_i) = \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_t}{\sigma_e} \right) \frac{\partial e}{\partial x_j} \right] + C_{1\epsilon} \frac{\epsilon}{k} (G_k + C_{3\epsilon} G_b) - C_{2\epsilon} \rho \frac{e^2}{k} + S_{\epsilon}$$
(11)

633

634 where;  $G_k$  denotes turbulence kinetic energy generation due to the mean velocity 635 gradients,  $G_b$  denotes turbulence kinetic energy generation due to buoyancy.  $Y_M$ 636 denotes the contribution of fluctuating dilatation in compressible turbulence to the 637 overall dissipation rate.  $C_{1\epsilon}$ ,  $C_{2\epsilon}$  and  $C_{3\epsilon}$  are constants,  $\sigma_k$  and  $\sigma_e$  are the turbulent 638 Prandtl numbers for k and  $\mathcal{E}$ .  $S_k$  and  $S_{\epsilon}$  are the source terms. The geometry (Figure 25) was designed making use of an academic standard CAD tool and then exported into ANSYS Geometry to generate a computational model. The shape of the building was based on [51], which is a gable roof type building with a roof pitch of 26.6°. The overall dimension of the building was 3.3m (L) x 3.3m (W) x 3m (H). The fluid volume was isolated from the solid model to generate a computational domain. The fluid domain contained an inlet on one side of the domain, and an outlet on the opposite boundary wall.

646 The COST 732 guideline [52] for environmental wind flow studies was used as the 647 basis for computational domain size and model location. According to the guidelines, for a single structure with the height H, the horizontal distance separating the 648 649 sidewalls of the structure and side boundaries of the computational domain must be 5H. Similarly, the vertical distance separating the roof and the top of domain must 650 651 also be 5H. Along the direction of the flow, the distance between the inlet and the facade of the building must be 5H. The distance between the leeward side and outlet, 652 however, must be 15H to allow for flow re-development behind the wake region. This 653 654 is also considering that for steady RANS calculations, fully developed flows are 655 generally assumed as the boundary condition [52].



656

657

658

659 Due to the complex nature of the model, a non-uniform mesh was utilised for volume 660 and surfaces of the computational domain [53]. The generated computational mesh of the building model is shown in Figure 26. The grid was improved and refined 661 662 according to the relevant critical areas for the simulation e.g. the aero-elastic belt. 663 The scales of the mesh element were stretched smoothly to resolve the areas with high gradient mesh and to enhance the precision of the results. The inflation factors 664 were adjusted with respect to the intricacy of the geometry face elements. This was 665 666 employed to generate a finely resolved mesh perpendicular to the wall and coarse mesh parallel to it [54]. 667

Fig. 25. Computational domain of building with aero-elastic belt devices

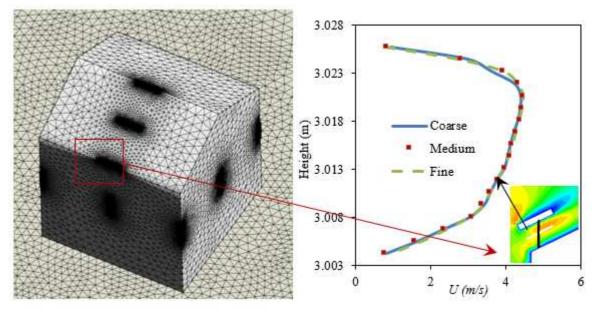




Fig. 26. (a) Computational grid (b) Sensitivity analysis

671 Sensitivity analysis was performed in order to confirm the computational modelling of 672 the building integrated with the aero-elastic belt. The computational grid was 673 established on a sensitivity analysis which was conducted by performing 674 supplementary simulations with the same domain and boundary conditions but with various gird sizes. This procedure then enlarged the number of elements from 2.44 M 675 676 elements (coarse) to 4.90 M elements (fine). The mean value of the wind speed in 677 the vertical line of the R1 belt was invoked as the error gauge (Figure 27 (b)). The 678 maximum error among the fine mesh and medium mesh was 3.4% or ±0.08 m/s 679 while the mean error was 1%. Therefore, the redundancy of model simulation with 680 finer mesh had no significant effects on the solutions.

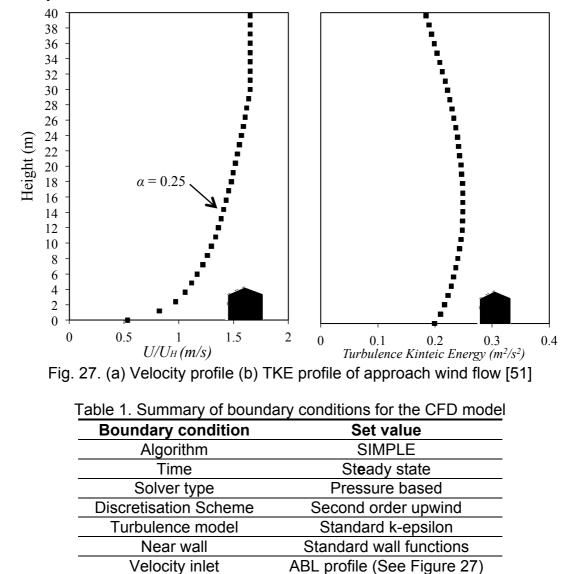
681

682 The boundary conditions were specified according to the AIJ guidelines [55]. The airflow velocity profile and turbulent kinetic energy (TKE) were enforced on the inlet 683 region which were based on [50], with the stream-wise velocity of the incident airflow 684 685 conforming to the power law with an alpha equal to 0.25. This exponent corresponds 686 to a sub-urban terrain (See Figure 27). The  $\varepsilon$  values for the k- $\varepsilon$  turbulence model 687 were obtained through the assumption of a local equilibrium of  $P_k = \varepsilon$  [50]. Standard 688 wall functions [56] were invoked for wall boundaries excluding the ground. The 689 ground region had adjusted wall functions relying on roughness values [57]. Based 690 on literature [57], this has to stipulated by an equivalent sand-grain roughness height  $k_s$  and roughness constant  $C_s$ . The non-homogeneousness of the ABL in the 691 horizontal dimension was limited by a suitable sand-grain roughness height and 692 roughness constant adapted for the inlet profiles, obeying the equation of [58] :  $k_s = \frac{9.793z_0}{c_s}$ 693

694 (12)

695 where  $z_0$  is the aerodynamic roughness height for sub-urban topography. Sand-grain 696 roughness height was set to 1.0 mm and roughness constant was set to 1.0 [51]. The 697 side walls and top wall of the domain were fixed as symmetry. This indicated zero 698 velocity in the normal direction and zero gradients for all pertinent variables at the

side and top walls. Zero static pressure was utilised for the outlet boundary. Theboundary conditions are reviewed in Table 1.



701

702 703 704

The solution convergence and pertinent variables were observed and the solution 706 707 was considered to be complete upon observation of invariant iterations. Furthermore, property conservation was also tested if attained for the converged solution, which 708 was executed by running a mass flux balance. This selection was obtainable from the 709 FLUENT flux report panel which permits the calculation of mass flow rate for 710 boundary zones. For the current model, the mass flow rate balance was lower than 711 712 the required value equivalent to a value less than 1% of minimum flux through 713 domain boundaries, i.e. inlet and outlet.

Pressure outlet

0 Pa

## 714 **3.2 Estimation of wind power**

715 The study utilised regression analysis using a polynomial curve of degree three to

extrapolate power output given integral-value wind speed. Experimental data from [6] was used, with varying wind speed and the corresponding output power, using the

718 optimal load and tension for an aero-elastic belt. A degree three polynomial is 719 analogous to the fundamental equation for wind power making the choice for this polynomial type more sensible. Regression analysis was able to obtain an R-squared 720 value of 0.9666. Using the manufacturer's specifications, cut-in wind speed is limited 721 722 to 3 m/s. Therefore in order to extract results using the same aero-elastic belt, 723 reconfiguration of the belt has to be done on installations on areas of the buildings with wind speeds lower than 3 m/s. This investigation simulated a gentle breeze, 724 725 which is category 3 in the Beaufort wind force scale.

#### 726 3.3 Method validation

727 Figure 28 (a) and (b) show a comparison between the experimental PIV results of [51] and the current modelling values for the airflow speed distribution around the 728 729 building model. The values for the airflow speed close to the windward wall seem to be at a lower speed in the model compared to the PIV results, however a similar 730 pattern was observed for most areas particularly close to the roof. Figure 28 (c) and 731 732 (d) show a comparison between the prediction of the current model and [51] of the pressure coefficient distribution around the building model. 733

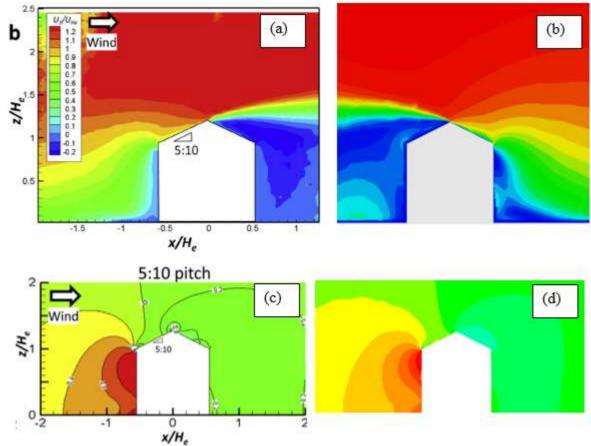
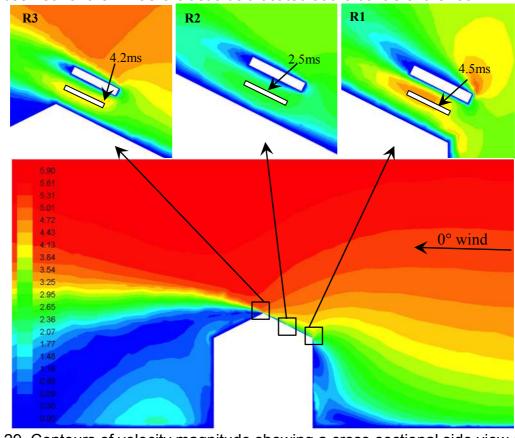




Fig. 28. (a) PIV measurements of velocity [51] (b) velocity distribution in the current model (c) pressure coefficient result [51] (d) pressure coefficient distribution in the 736 737 current model.

## 738 4. RESULTS AND DISCUSSION

739 Figure 29 displays the contours of the velocity field for the side view cross-sectional 740 area within the computational domain denoting the airflow distribution around the 741 building integrated with aero-elastic belt. On the left part of the plot the scale of airflow speed is displayed in m/s. Colour coding was employed to better illustrate the 742 fluid domain contour plots which range from 0 to 5.9 m/s. As observed, the incident 743 744 wind flowed from the right side of the domain and subsequently the airflow decreased 745 in speed as it moved towards the building and was then lifted upwards. Regions of 746 flow separation were detected on the lower windward side of the structure and also at the leeward side of the building and roof. Zoomed in views of the velocity distribution 747 748 around the aero-elastic belt R1, R2 and R3 are shown on top of the diagram. The results showed that the shape and angle of the roof had a significant influence to the 749 750 performance of the aero-elastic belt. In the diagram, it is clear that locating the device at the leeward side of the roof will result in little to no energy generation due to the 751 low wind speeds in this area. However, it should be noted that this was not the case 752 753 for other wind angles, for example when the wind is from the opposite direction. 754 Therefore, location surveying, wind assessment and detailed modelling are very 755 important when installing devices in buildings. At wind velocity ( $U_H$ ) 4.7 m/s and 0° 756 wind direction, the airflow speed in R1 was the highest at 4.5m/s while the lowest 757 was observed for the R2 aero-elastic belt located at the centre of the roof.



758 759 760

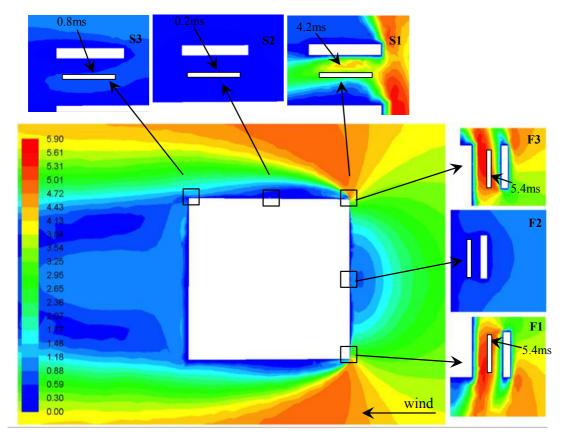
Fig. 29. Contours of velocity magnitude showing a cross-sectional side view of the
 building

761

Figure 30 displays the top view cross-section area for the velocity contours within the computational domain indicating the airflow distribution around the building integrated

with aero-elastic belt. The incident wind flowed from the right border of the domain and the airflow decreased in speed as it flowed closer to the building and accelerated as it flowed around the corners. Regions of flow separation were detected on the leeward and side areas of the building. Zoomed in views of the velocity distribution around the aero-elastic belt F1-F3 and S1-S3 are shown on top and right side of the diagram. At wind velocity (U<sub>H</sub>) 4.7 m/s and 0° wind direction, the airflow speed in F1 and F3 were the highest at 5.4m/s while the lowest was observed for the S2 and F2

aero-elastic belts located at the airflow recirculation zones.



772

Fig. 30. Contours of velocity magnitude showing a cross-sectional top view of the
 building

775 Figure 31 compares the maximum air velocity speed measured at the belt location for 776 roof installations R1, R2 and R3 at various wind directions. These setups behaved in a trend similar to each other, but the notable highest velocities were attained from the 777 R3 or apex installation. These setups had peak velocity values occurring at the 778 779 region between 30° to 60° orientation, with the maximum value obtained at 30°. There was significant speed decrease after 60° that could be attributed to the belt frame 780 781 corners which impeded the wind from flowing through the belt region and therefore 782 would reduce its performance or not allow the belt to flutter

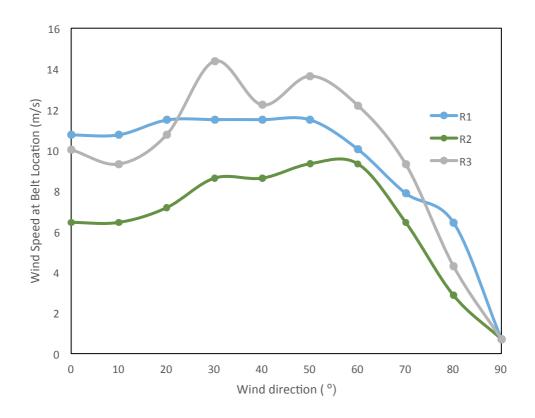




Fig. 31. Effect of wind direction on the wind speed at belt located on the roof for various wind angle of approach with outdoor wind  $U_H = 10 \text{ m/s}$ 

Figures 32 and 33 compare the maximum air velocity speed measured at the belt location for the windward and side installations, respectively at various wind directions. When comparing the two figures it was observed that the plot of F3 had a similar trend with the S1 belt which showed a significant performance drop in terms of velocity between 20-60°. This was also due to the frame of the wind belt which impeded the wind from flowing through the belt region and therefore would reduce its performance or not allows the belt to flutter

794

795 While the plot of F1 was a mirrored of S3, and F2 was mirrored S2. There is some 796 symmetry that can be expected as observing the locations in Figure 24. It is not a 797 perfect symmetry due to the roof shape having some effect on airflow. Looking at the 798 location with highest velocity values for the front side of the building, there was a significant decrease in velocity from 10° to 40°, accounting for approximately 83% 799 800 speed reduction, and same increase in speed was observed from 40° to 70°. For the side installation S1 the tipping point was at 50° where the change in angle exposure 801 past this point marked significant increase in velocity. From the results it was clear 802 803 that both the location of the device and wind direction had a significant effect on the 804 air speed achieved at the belt location. Therefore a complete detailed analysis of 805 these factors should be carried out when integrating wind belts to buildings to ensure 806 that the performance is optimised and also minimised the number of belts integrated 807 to the building.

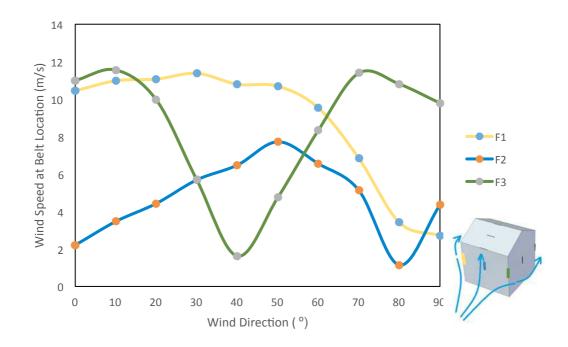
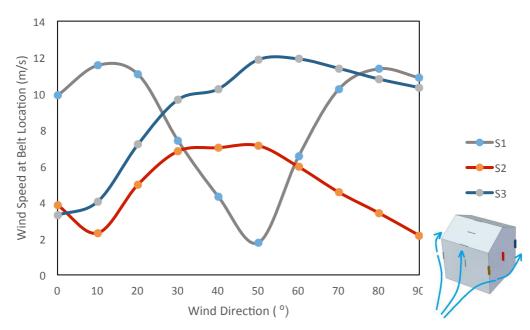


Fig. 32. Effect of wind direction on the wind speed at belt located on the windward side of building with outdoor wind at  $U_H = 10 \text{ m/s}$ 



811

Fig. 33. Effect of wind direction on the wind speed at belt located on the side of building with outdoor wind at  $U_H = 10 \text{ m/s}$ 

814

Figure 34 illustrates the effect of different outdoor wind speed U<sub>H</sub> values of 2, 4, 6, 8, and 10 m/s at 0° wind direction on the air speed achieved at the belt location. Similar trend was observed for all the curves with the highest speed achieved in R1 and F3 and lowest speed achieved in F2 and S2. The increase in the velocity profile corresponded to a proportional increased for the wind speed for all the belt locations.

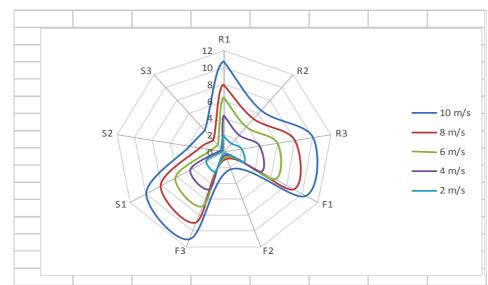




Fig. 34. Wind speeds gathered at belt position for various mounting locations for 0° wind angle of approach

823 824

Figure 35 depicts velocity results for 90° wind angle approach. At this angle the output of the roof installations were overtaken by those in the front and side, most notably by F3, S1 and S3 mainly because of the geometry of the belt frame. The frame restricts airflow in the perpendicular direction to the belt. Therefore for locations with this type of prevailing wind direction it will be better for the aero-elastic belts to be integrated through the front and side edges of the building.

831

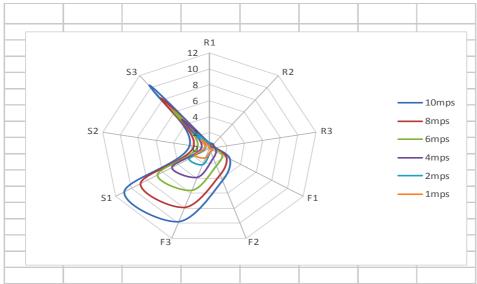


Fig. 35. Wind speeds gathered at belt position for various mounting locations for 90°
wind angle of approach

835

Figure 36 compares the estimated output of the device at various locations and wind directions of 0 to 90°, in increments of 10 degrees while maintaining a uniform outdoor wind velocity ( $U_H = 10 \text{ m/s}$ ). F1, F2 and F3 represent the aero-elastic belt mounted on the front face of the building; S1, S2 and S3 represent those on the side

- face, while R1, R2 and R3 are those for the roof locations. As observed, the highest
  power output comes from location R3 the apex of the building with an estimated
  output of 200.54 mW, resulting from wind speed that accelerated up to approximately
  14.4 m/s, approximately 37.5% speed-up at the particular height. This occurred for
  an incoming wind 30° relative to the building facade.
- 845

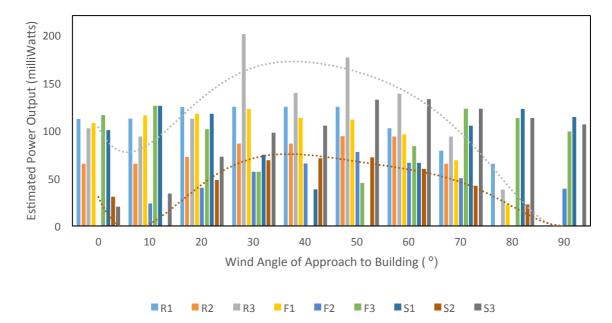
B46 Depending on prevailing wind direction of the area, the installation location of the belt b47 can be determined. The green trendline represents the power output trend for R3, the b10 location with the highest total power generation summed over 0 to 90 degrees. The b17 brown trendline shows the trend for S2, the location with the lowest summed power b18 generation over the same angular range.

851

852 Secondary to the building apex, locations on the edge also provide well above-853 average power output. Based on the simulated conditions, locations S3, F1 and R1 854 should be optimum locations for building integration of the aero-elastic belt, 855 considering the power averages for 0, 45 and 90-degree orientations.

856

The last locations an installer would want to put an aero-elastic belt on are the central areas of the building's faces (illustrated by F2 and S2). Taking into account angular averages these locations provided the least amount of power, with no power generated at all for some cases due to the wind speed not being able to make it to the aero-elastic belt's cut-in wind speed for generation. This finding can be considered by some to be a counterintuitive result, considering these locations are directly hit by the oncoming wind.



864

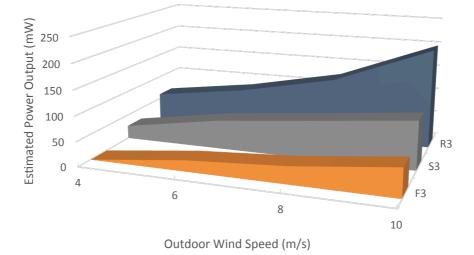
Fig. 36. Sample calculation based on aero-elastic belt (2-magnet-coil system) data
 measured from experimental data [6]

867

Figure 37 compares the estimated output of the device located in the three locations
 F3, S3 and R3 at various outdoor wind speeds. Among these three locations, at 30°

870 wind direction, R3 provided the highest output ranging between 59 to 200 mW, while

F3 showed the lowest output and only started to generate at outdoor wind velocity  $(U_{\rm H})$  above 4 m/s.



873

## Fig. 37. Impact of different outdoor wind speeds (U<sub>H</sub>) on the estimated output of the aero-elastic belt for locations F3, S3 and R3

## 876 5. CONCLUSIONS AND FUTURE WORKS

877

878 The aero-elastic belt is beneficial for low-energy wind harvesting in the built 879 environment due to its low cost and modularity. The necessity of investigating the integration of the aero-elastic belt into buildings utilising CFD analysis is evident. The 880 review of previous works on the aero-elastic belt showed that several authors have 881 assessed the performance of the device in uniform flows in the laboratory or wind 882 tunnel but did not investigate the effect of buildings on its performance. Therefore, 883 the current work addressed the issue by carrying out CFD modelling of a simplified 884 885 building model integrated with aero-elastic belts. The work investigated the effect of 886 various wind speeds and aero elastic belt locations on the performance of the device. The simulation used a gable-roof type building model with a 27° pitch obtained from 887 888 the literature. The ABL flow was utilised for the simulation of the incident wind. The 889 three-dimensional Reynolds-averaged Navier-Stokes equations jointly with the momentum and continuity equations were solved through ANSYS FLUENT 16 for 890 obtaining the flow velocity field and pressure field. Sensitivity analyses for the CFD 891 grid resolutions were implemented for verification of modelling. The results of the flow 892 893 around the buildings and pressure coefficients were validated with previous 894 experimental work. The study utilised regression analysis and experimental data to 895 estimate the power output of the aero-elastic belt.

896

In terms of potential for power generation from the aero-elastic belt, the apex of the roof or the highest point of the building recorded the highest power yield, with this location's production being the largest with the 45-degree approach of the wind relative to the building. Optimum placement of the aero-elastic belt would mean prioritising the roof and the trailing edges of the building, and not the leading edge
 nor centres of surfaces, to yield the highest possible power generation, depending on
 wind conditions.

- 905 Subject to the prevailing wind direction within the building environment, the 906 installation location with the highest potential for energy output on the front and side 907 faces of the building can be inferred with more confidence using the results of the 908 study. With respect to the physical geometry of the frame of containing the belt, the 909 cover can be further minimised to enable more wind to flow across the belt.
- 910

There is a potential for further scaling up the system in terms of size and configuration, with the plausibility of constructing an array of aero-elastic belts. The results showed the importance of using detailed CFD analysis to evaluate the aero elastic belt. The detailed velocity distribution results showed the capabilities of CFD on assessing the optimum location of the devices around the building. The modelling procedure and data presented in this work can be used by engineers/researchers to further investigate the integration of the aero-elastic belt in the urban environment.

918

919 Future studies on the aero-elastic belt installation in buildings will include simulations 920 using transient models which take into account non-uniform flow conditions. 921 Prospective investigations on the impact of varying shapes of the subject building 922 and also different locations of the device will also be conducted. Further studies will 923 investigate the impact of surrounding buildings on the performance of the device as 924 well. This will incorporate the shape of surrounding buildings, distance and 925 positioning, etc. Field tests will also be carried out to evaluate device performance in 926 actual conditions and assess other factors such as noise, visual and related 927 parameters. Economic analysis of the integration of the aero-elastic belt in buildings 928 will be conducted and compared with more established low-energy generation 929 devices.

## 930 NOMENCLATURE

## 931 Symbols

- 932 U Air velocity (m/s)
- 933 *p* Static pressure (Pa)
- 934 *H* Height (m)
- 935 L Length (m)
- 936 W Width (m)
- 937 x, y, z Direction
- 938 g gravitational acceleration (m/s<sup>2</sup>)
- 939  $S_M$  Mass added to the continuous phase from the dispersed second phase 940  $\tau$  Time in the past contributing in the integral response
- 941  $k_{eff}$  Effective conductivity (W/mk)
- 942  $\vec{J}_i$  Diffusion flux
- 943  $S_h$  Heat of chemical reaction and other volumetric heat source defined by
- 944 user 945 k Turbulence kinetic energy (m<sup>2</sup>/s<sup>2</sup>)
- 946  $\epsilon$  Turbulence dissipation rate (m<sup>2</sup>/s<sup>3</sup>)

947	$G_k$	Generation of turbulent kinetic energy due to the mean velocity
948	gradients	Concration of tabalent kinetic chergy due to the mean velocity
949	G <sub>b</sub>	Generation of turbulence kinetic energy due to buoyancy
950	$Y_M$	Fluctuating dilatation in compressible turbulence to the overall
951	1 M	dissipation rate
952	$\sigma_k$	Turbulent Prandtl numbers for turbulence kinetic energy
953	$\sigma_k$	Turbulent Prandtl numbers for energy dissipation rate
954	$S_k$	User defined source term for turbulence kinetic energy
955	$S_{\epsilon}$	User defined source term for energy dissipation rate
956	$k_s$	sand-grain roughness height (m)
957	C <sub>s</sub>	roughness constant
958	z <sub>0</sub>	Aerodynamic roughness length (m)
959	F1, F2, F3	
960	S1, S2, S3	
961	R1, R2, R3	Roof aero-elastic belts
962	Р	Power generated
963	$P_Y(t)$	Plunging contribution to the power
964	$P_{\Theta}(t)$	Pitching contribution to the power
965	$F_Y(t)$	y-component of force
966	$V_Y(t)$	Plunging velocity
967	$U_{\infty}$	Free-stream velocity
968	M(t)	Torque about pitching centre
969	$\omega(t)$	Angular velocity
970	$C_P$	Instantaneous power coefficient
971	$C_{Pmean}$	Time-averaged power coefficient
972	$C_{Ph}$	Pitching contribution to the power coefficient
973	$C_{P\Theta}$	Plunging contribution to the power coefficient
974	Т	Oscillation frequency
975	$C_Y(t)$	Instantaneous lift coefficient
976	$C_M(t)$	Momentum coefficient
977	η	Power-extraction efficiency
978	$\Theta_0$	Pitching amplitude
979	A	Overall vertical extent of foil motion
980		

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