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Analysis of flowability of cohesive powders using Distinct Element Method

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ABSTRACT

Computer simulations using Distinct Element Method (DEM) have been carried out to investigate the effect of cohesion on the flowability of polydisperse particulate systems. For this purpose, two assemblies with different values of surface energy and made of 3000 spheres with the mechanical properties of glass beads were considered. The analysis of the flowability of the powders is presented in terms of the unconfined yield stress as a function of strain rate for different pre-consolidation loads. For values of the surface energy of 1.0 J/m^2 and strain rates lower than 6 s^{-1} , the unconfined yield stress does not change significantly indicating a quasi-static behaviour of the particulate assemblies during the compression process. For larger strain rates, the unconfined yield stress varies with the power index of 1.2 of the strain rate. The influence of the pre-consolidating stress on the powder behaviour has also been investigated and a flow factor was obtained from the linear relationship between the unconfined yield stress and pre-consolidation stress. The computer simulations show qualitatively a good agreement with the experimental trends on highly cohesive powder flow behaviour.

Keywords: flowability, cohesive powders, unconfined, yield stress, polydisperse, glass beads, Distinct Element Method.

1. Introduction

The processing of many particulate materials may involve unit operations such as fluidisation, pneumatic conveying and storage in bins and hoppers. During processing, the behaviour of powders is strongly influenced by particle properties as well as the design and operating conditions of these units. The flowability of powders in such unit operations is an important issue as it can strongly influence the efficiency and reliable operation of these processes.

The flowability of powders is commonly analysed using the concept of Coulomb failure [1], which describes the existence of a limiting shear stress under which solids do not undergo plastic deformation. However, if the shear stresses are equal to the limiting shear stress, failure or plastic flow is observed in the material. The concept of Coulomb failure for solids was applied to granular materials [1] and was later used to optimise the design of hoppers by establishing a criterion for the flow of powders through the outlet of silos [2].

The flowability of powders is commonly characterised by using shear testers. These devices provide an indication of the shear strength of powders under a compressive load and can be used for the design of different operational units such as silos. Schwedes [3] has recently presented a comprehensive review on shear testing and has provided a comparison between different shear test devices and an analysis of the properties that influence the flowability of powders such as pre-consolidation, anisotropy [3, 4] and the influence of the stress history on the flow behaviour of powders.

Most published work in the field of flowability and shear behaviour of powders is experimental. However, in experiments the measurements are usually made only from the boundaries of the assemblies as any effort to probe the internal state of the assembly might interfere with the behaviour of the particles. In contrast, the use of computer simulation allows the probing of the internal behaviour of particulate assemblies under mechanical loading. Therefore, the analysis of the flowability and shear behaviour of powders using computer simulation is attracting increasing attention recently [5-9].

Thornton and co-workers [5-7] have analysed the influence of friction and bulk density on the quasi-static shear deformation of powders. Thornton and Antony [5-6] showed that the strong force chains developing within the assembly contributed much more to the deviator stress than the weak force networks. In addition, they reported that no large increase in dissipation of energy occurred when the interparticle friction was increased.

Recently, Thornton and Zhang [7] have simulated the development of shear bands in a two-dimensional box type shear cell using DEM. They showed that the shear stresses measured on the platens of the shear cell follows the same tendency as the stress tensor in the shear bands. They conclude that the behaviour of bulk particles is mainly controlled by the stresses developed in the shear bands. They also analysed the bed expansion during shearing in dense granular materials for normal applied loads between 10 and 20 MPa. Although the variation in the normal applied stress was very small, an increase in the bed expansion was clearly observed when the normal stress was increased.

Gröger *et al.* [8] have also investigated the shear strength of powders using DEM. In their simulations, they considered the cohesivity of the particles to originate from the presence of

liquid bridges between particles. They simulated the shear deformation of powders between two platens moving in opposite directions under a normal load. The particles were subjected to periodic boundary conditions. They provided a visual analysis of the behaviour of the powders during shearing at the peak shear stress. For this condition, the direction of the contacts carrying small forces coincided with the direction of the relative movement of the platen. However, the contacts carrying large forces were inclined in the direction perpendicular to the contacts with weakest forces. The orientation distribution of contacts is not affected by the relative movement of the platens, although the strong and weak networks of forces changed orientation producing a rotation of the principal stresses. However, the most important point is that the orientation distribution of contacts remains constant as if the sample would not have been sheared. These results are in contrast to the findings of other authors [5,6] who found that the anisotropy of orientation of contacts reaches a maximum at the peak of shear stress. Furthermore, Gröger *et al.* [8] compared the shear stress-shear strain profile obtained by DEM with that obtained experimentally by a Schulze shear tester. This comparison showed an outstanding agreement between simulation and experiments [8] indicating the reliability of DEM as a tool to predict the shear behaviour of powders.

In this paper, results of DEM simulations analysing the flowability of cohesive powders are reported. The flow factor as suggested by Jenike [1] for cohesive materials is also presented. The unconfined yield stress (UYS) of the powders has been obtained from simulating the uniaxial compression of particulate assemblies subjected to different values of pre-consolidating stress and strain rate. This is also presented here.

2. Simulation details

Two polydisperse systems made of 3000 spherical particles with properties corresponding to glass beads (Table 1) are considered. In order to perform the simulations a particle size distribution of the powders corresponding to a typical manufactured supply was chosen. This particle size distribution is nearly symmetric around its maximum at 125 μm with the range of the particle diameters being between 56 and 212 μm . The probability density of size distribution is given in Table 2.

The two systems were formed by generating two random assemblies of spheres and further allowing the deposition of particles by the action of gravity. The surface energies of the particles of the two systems were 1.0 and 0.1 J/m^2 , respectively. In order to minimise the differences between the two systems the initial particles positions were exactly the same for both cases.

The simulation program used here is based on the work of Thornton and coworkers [10,11]. The interparticle adhesion is according to the model of Johnson *et al.* [12]. According to this model the force to break a contact under normal tension, F_{OFF} , depends on the surface energy and the radii of the two particles in contact as given by

$$F_{OFF} = 3\pi\gamma R \quad (1)$$

where $R^{-1} = (R_1^{-1} + R_2^{-1})$ is the reduced radius of two particles in contact, γ is the surface energy and R_1 and R_2 the radii of the two particles in contact. The contact deformation in this work is only elastic.

When tangential forces act on the contact between particles the change in the radius of the contact area, a , is provided by the model of Savkoor and Briggs [13] according to Eq. 2:

$$a^3 = \frac{3R}{4E} \left\{ N + 2F_{OFF} + \sqrt{\left[4NF_{OFF} + 4F_{OFF}^2 - \frac{T^2 E}{4G} \right]} \right\} \quad (2)$$

where T and N are the applied tangential and normal forces and E and G are the reduced elastic and shear moduli, respectively. These are defined as functions of the elastic modulus, E_1 and E_2 and shear moduli, G_1 and G_2 , of the two particles in contact:

$$\frac{1}{E} = \frac{1-\nu_1^2}{E_1} + \frac{1-\nu_2^2}{E_2} \quad (3)$$

$$\frac{1}{G} = \frac{(2-\nu_1)}{G_1} + \frac{(2-\nu_2)}{G_2} \quad (4)$$

The above model treats the interparticle contact as an annular crack and defines the condition for crack extension due to shear stress, leading to Eq. 2.

The behaviour of the system has been analysed by monitoring the number of interparticle contacts, the pressure on the top platen and the stress tensor in the bulk.

The definition of stress tensor used here is due to Satake [14], where he considers a volume V , and defines a macroscopic stress acting on the volume based on the interparticle contact forces.

The components of the stress tensor are defined as

$$\sigma_{ij} = \frac{2}{V} \sum_I^M R N n_i n_j + \frac{2}{V} \sum_I^M R T n_i t_j \quad (5)$$

where Rn_i is the i component of the radius vector from the centre of the particle to the contact, Nn_i , Tt_j are the i and j components of the normal and tangential contact forces, respectively, and M the number of interparticle contacts. The sum of the forces in every contact of the assembly is divided by the volume of the assembly and therefore the information is given on the whole state of the stress of the system.

3. Simulation results

3.1. Formation of the assemblies

The particles were initially created within a cubic space. An elastic platen whose elastic modulus corresponds to steel was placed along the bottom side of the cube. The platen was frictionless and cohesionless. The side walls of the cube were taken as rigid boundaries in which the particles rebound without energy dissipation.

Initially, the particles were allowed to settle down within the cubic space by the action of gravity. In Table 3 the packing fraction, number of interparticle contacts and normal components of the stress tensor after the deposition of the particles are given. The components of the stress tensor were close for both assemblies, although they have different values of surface energy. This suggests that the surface energy does not produce a significant increase in the stress components when the packing of the assemblies is loose. This is in contrast to previous results [9] where the introduction of surface energy in a denser packed system (packing fraction 0.65) instantaneously initiated large oscillations in the stress ratios suggesting a large influence of

cohesion on the bulk behaviour of particles. However, in the case analysed here the system is more loosely packed and the particles were cohesive from the beginning of the simulation.

3.2. Effect of surface energy on the flowability of powders

The flow properties of particles are usually measured by using direct or indirect shear testers [3]. In the study carried out here, as commonly performed in the industry, the flowability of powders is analysed by determining the unconfined yield stress in uniaxial compression tests. The simulations are carried out in a similar way to the experimental procedure [3] and it is schematically shown in Fig. 1. The particulate assembly was placed in between elastic platens (steel) at the top and bottom surfaces. The side boundaries were removed and later the top platen was moved downwards with a specific strain rate. The unconfined yield stress is therefore the normal stress required to cause the failure of the assembly.

The number of interparticle contacts as well as the force acting on the top platen was monitored during the compression. The sample was considered to have failed when a sharp peak on the platen force accompanied by a significant drop in the number of contacts was observed. The force at this point divided by the platen area was taken as the unconfined yield stress (UYS).

Figure 2 shows on a log-log scale the UYS as a function of the strain rate for the cases of particles with surface energy values of 1.0 J/m^2 and 0.1 J/m^2 . The UYS does not depend on strain rate for values of strain rate lower than 2 s^{-1} for the system with 0.1 J/m^2 and lower than 6 s^{-1} for the case of system with surface energy 1.0 J/m^2 . This is qualitatively in agreement with experimental observations for the quasi-static regime [15] in which the UYS is independent of the strain rate. It may be noted that an increase of one order of magnitude in the value of the

surface energy produces a similar increase in the UYS for the quasi-static regime. These results are in agreement with previous simulations of a highly polydispersed system [9].

For values of strain rate larger than corresponding to the quasi-static regime (see Fig. 2), an almost linear relationship between UYS and strain rate, is observed. Fitting a power law to the simulation data, a power index of 1.2 is obtained. A power index of less than two suggests that the pressure originated in the system is not exclusively due to a kinetic contribution as observed in the case of rapid granular flows, but due to the influence of the interparticle friction. This behaviour is typical of systems with high values of packing fraction and corresponds to an intermediate regime between quasi-static and rapid granular flow as suggested by Tardos *et al.* [15]. This is discussed further below.

3.3. Compression of the assembly

It is well known that the flowability of powders depends on the pre-consolidating load [3]. In order to study the effect of the pre-consolidating stress on the unconfined yield stress, the system with the value of surface energy of 1.0 J/m^2 was compressed to higher levels of stress than tested above. The top platen was moved at a constant velocity of 0.01 m/s until a pre-specified value of pressure was reached. At this stage of compression, the material might accumulate large residual stresses. Therefore, before measuring the unconfined yield stress for different values of pre-consolidation stress it is necessary to allow the system to relax before carrying out further test using the assemblies.

Figure 3 shows the top platen stress and the number of interparticle contacts in the assembly as a function of the strain during compression. When the top platen contacts the top layer of particles

a sharp increase in the platen stress is observed without a significant change in the strain. With the increase in compression, the number of interparticle contacts decreases very slightly. However, the increase in strain produces a gradual increase in the platen stress albeit accompanied by stress fluctuations. Furthermore, as the assembly is compressed sudden drops in the platen force are observed. This is accompanied simultaneously by drops in the number of contacts. In some cases, the number of interparticle contacts is reduced by nearly 50%. These sharp drops might be due to the reorganisation of the force networks during the compression [6].

For different values of compression forces, the assembly was subjected to a relaxation process, with the objective of decreasing residual stresses and obtaining an equilibrium force network. This relaxation process was carried out by keeping the distance between the platens and the side boundary conditions constant and continuing cycling the simulation. This process produces a relaxation of the internal stresses by rearrangement of particles. As an example Fig. 4 shows a typical relaxation curve of the stresses. The stresses correspond to the platen pressure and the yy component of the stress tensor of the assembly. The similarity between the yy component of the stress tensor and the platen pressure suggests that both can be used indistinctively in order to measure the state of stress of the system. However, this may not be true in all cases since the stress tensor is a measure of the stress in the whole assembly and the platen stress is the stress on the surface of the material. In cases of high compressive strain rate, the stress in the boundary might not have enough time to propagate inside the assembly and both parameters could give significantly different values.

Several assemblies at different values of pre-consolidating stress have been obtained and analysed to investigate the effect of the pre-consolidating stress on the unconfined yield stress. Figure 5 shows the unconfined yield stress, σ_{UYS} , for different values of the pre-consolidating

stress σ_{YY} as a function of the strain rate. The larger the pre-consolidating stress the larger the unconfined yield stress as intuitively expected. The quasi-static regime is observable at all pre-consolidating stresses. In the intermediate regime, the strain rate sensitivity (*i.e.* the slope of the lines) seems to decrease as the pre-consolidating stress is increased.

In Fig. 6 the UYS for the quasi-static regime is plotted as a function of the pre-consolidating stress for the assembly with $\gamma = 1.0 \text{ J/m}^2$. This curve is known as the flow function as initially introduced by Jenike and measured using the Jenike shear cell [1]. The relationship between UYS and pre-consolidating stress seems to follow a linear relationship with a slope of approximately 0.8. The flow factor, ff , as defined by Jenike [2] is the inverse of the slope of this line according to the expression:

$$ff = \left(\frac{\sigma_{UYS}}{\sigma_{YY}} \right)^{-1} \quad (6)$$

The above approach in obtaining the flow factor differs from the method based on using the major principle stress at the steady state flow measure by a shear cell. The differences have been highlighted by Schwedes [3].

The flow factor in this case is 1.25. This number was compared with published data by de Jong [16] who classified the flowability of powders according to their cohesivity as given in Table 4. For flow factors between 1 and 2 the powders are very cohesive. This comparison shows a qualitative agreement between DEM results and experimental data [16].

4. DISCUSSION

The determination of the unconfined yield stress in the uniaxial test is more straightforward than using Jenike or Schulze shear testers. Furthermore, the direction of the principal stresses does not change if the confining walls are frictionless and therefore the major consolidation stress is easily known. However, the unconfined yield stress as determined by the uniaxial test should be lower than the unconfined yield stress as provided by a direct shear tester when the sample is subjected to pre-shearing. The reason for this, as explained by Schwedes [3], is that during uniaxial consolidation because the bulk density for the same pre-consolidation stress is smaller the sample does not reach the steady state flow.

The flow factor obtained from the simulation data has been compared in Table 4 with the literature data provided by de Jong [16] in which a relationship between the flowability of powders and flow factor is given. The comparison suggests that the Distinct Element Method provides a qualitatively reasonable agreement with the flow behaviour of real powders.

Tardos *et al.* [15] recently presented trends of variations of shear stress as a function of strain rate obtained in a Couette type device for glass beads. They observed three regimes, slow (corresponding to quasi-static regime), fast (corresponding to rapid granular flow) for which the power index is 2 and an intermediate regime in which the power index varies from 0 to 2. The simulations reported here and the experimental work of Tardos *et al.* [15] are obviously different in the way they were carried out. Nevertheless, the power index of 1.2 obtained in this work falls within the intermediate range of Tardos's correlation. The highest value of strain rate used in the simulations is 1000 s^{-1} . This is larger than the upper limit of the intermediate regime. However, there are a number of other factors which strongly influence the simulation and an agreement with the experimental data at high values of strain rate is not expected. These factors

are discussed below and clearly show the need for further investigations of shearing flows in which the effects of interparticle adhesion and interstitial drag are important.

In the present study the effect of plastic deformation and air drag have not been considered. These factors might impose a limit on the interpretation of the curve of unconfined yield stress versus strain rate for large values of strain rate. For the case of pre-consolidation stress of 10 kPa and strain rate of 100 s^{-1} , the largest interparticle contact stress is 80 MPa. Since the yield strength of glass beads is in the order of 0.1-1 GPa the influence of yield strength on the UYS is only significant for the largest values of strain rate and pre-consolidation stress shown in Fig. 5.

The influence of air drag on the behaviour of the particles is expected to be appreciable at high strain rates. There is, however, little work in the literature on this topic. The simulations here are not expected to be significantly affected in the lower end of the transition between quasi-static and intermediate regimes because of the relatively low particle velocity relative to surrounding air. However, further work at high strain rate is needed to clarify the boundaries where air drag becomes important.

It is also important to highlight the influence of the surface energy on the unconfined yield stress. An increase of one order of magnitude of the surface energy leads to a similar increase in the UYS. We also observe that the variation of the UYS with strain rate for the intermediate regime follows the same relationship for both values of surface energy for which a power law index of 1.2 is obtained. This trend requires a more in-depth analysis especially on the dissipative mechanisms present in the material.

5. CONCLUSIONS

The procedure for the determination of the unconfined yield stress from a uniaxial compression test has been simulated using Distinct Element Method. The effects of strain rate and surface energy have been quantified. An increase of one order of magnitude of the surface energy produced a similar increase in the unconfined yield stress.

The unconfined yield stress increases linearly with stress in agreement with the behaviour of some typical materials. However, the increase in the pre-consolidating stress has also produced a change of the slope of UYS versus strain rate. The exact reasons for this trend are unclear at present and further investigations are needed to address the various mechanisms of energy dissipation.

The flowability of the particles has been determined by using the flow factor, which has been obtained from the relationship between the unconfined yield stress and pre-consolidated stress. There is a qualitative agreement in the trend for the flow factor obtained in this work and the literature data. Further investigations are required to elucidate the role of plastic deformation characteristics and air effects on the UYS of particulate assemblies.

NOMENCLATURE

a	Contact area radius	m
E	Particle elastic modulus	N/m ²
F _{OFF}	Pull-off force	N
ff	Flow factor	-

G	Shear modulus	N/m^2
M	Number of particles in the system	-
N	Normal load in a contact	N
n	Unitary normal vector in a contact	-
R	Particle radius	m
T	Tangential contact force	N
V	Volume of the assembly	m^3
t	Unitary tangential vector in a contact	-
γ	Surface energy	J/m^2
ν	Poisson's ratio	-
σ_{ij}	Components of the stress tensor	N/m^2
σ_{UYS}	Unconfined yield stress	N/m^2

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Table 1. Particle properties (corresponding to glass beads) used in the simulations.

Elastic modulus (GPa)	70
Poisson ratio	0.3
Friction coefficient	0.3
Density (kg/m ³)	2600

Table 2. Particle size distribution

Particle No.	Size (μm)
5	312.0
23	177.0
276	146.0
671	125.4
955	103.2
756	86.2
385	72.0
30	60.1

Table 3. Properties of the agglomerates

Surface Energy (J/m ²)	Packing Fraction	Contacts	σ_{xx} (Pa)	σ_{yy} (Pa)	σ_{zz} (Pa)
1.0	0.44	6640	3.88	9.06	11.7
0.1	0.52	6469	4.49	10.4	2.49

Table 4. Flowability of powders (after de Jong, 1999)

Flow factor (ff)	Flowability
$ff < 1$	No flow
$1 < ff < 2$	Very cohesive
$2 < ff < 4$	Cohesive
$4 < ff < 10$	Easy flowing
$10 <$	Free flowing

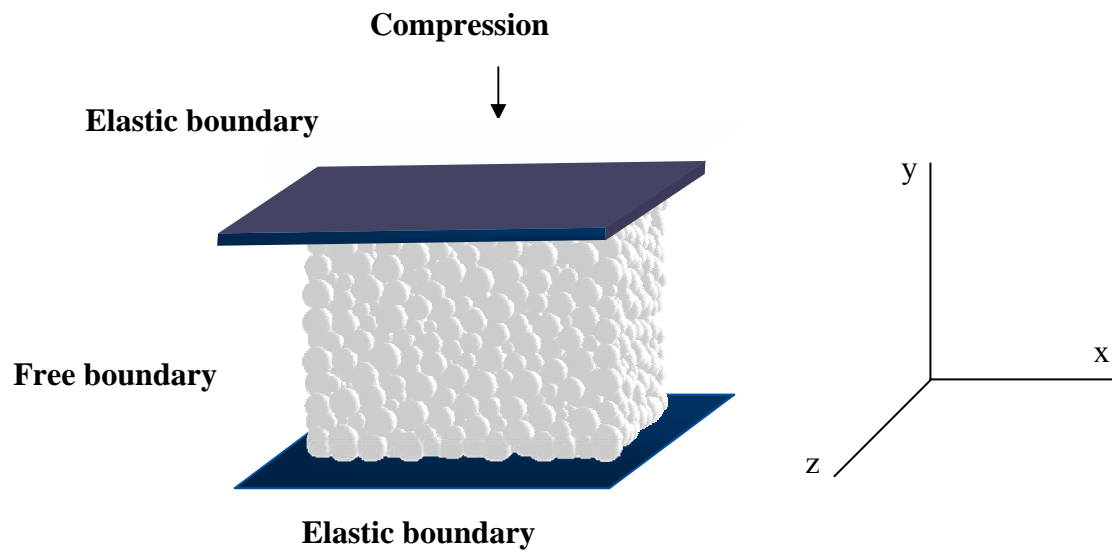


Fig. 1. Schematic diagram of the test for measuring the unconfined yield stress.

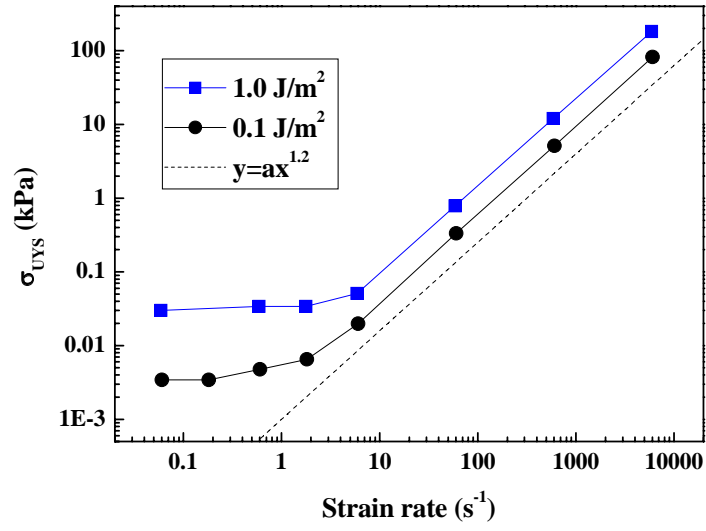


Fig. 2. Relationship between unconfined yield stress and strain rate for two values of surface energy.

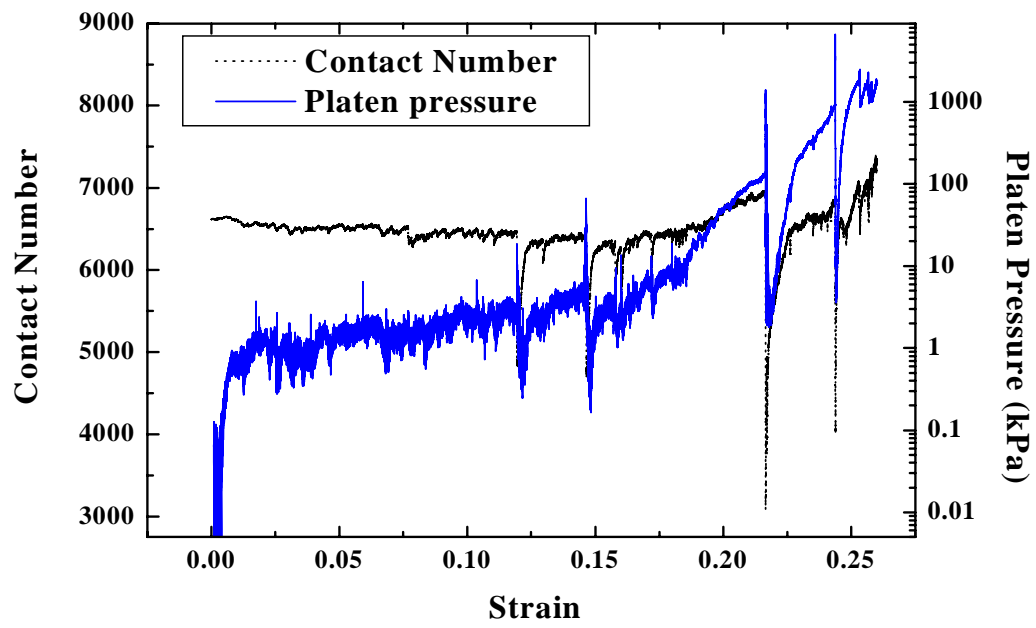


Fig. 3. Evolution of the platen pressure and contact number during confined compression

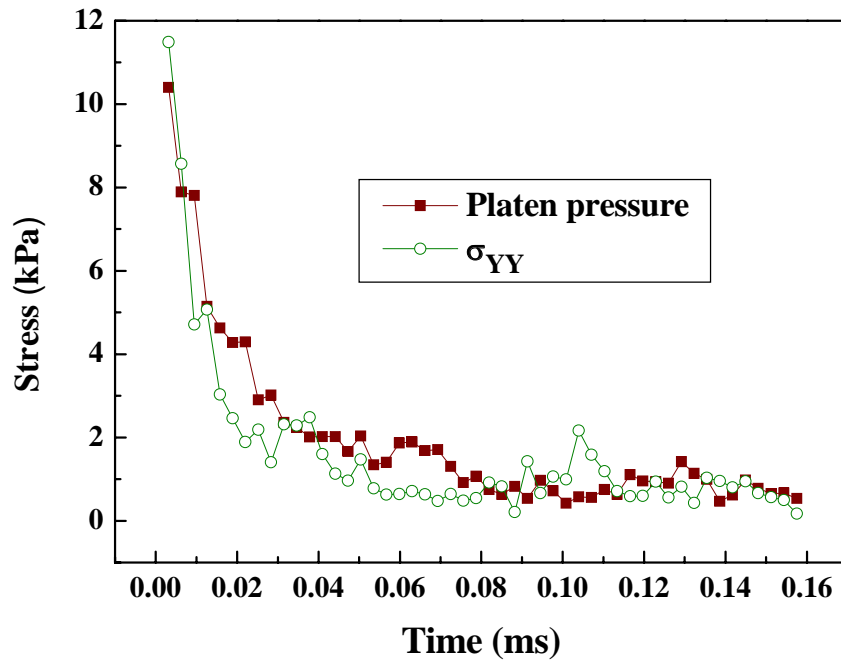


Fig. 4. Stress-time relaxation curve for an initial value of pre-consolidated stress of about 11KPa.

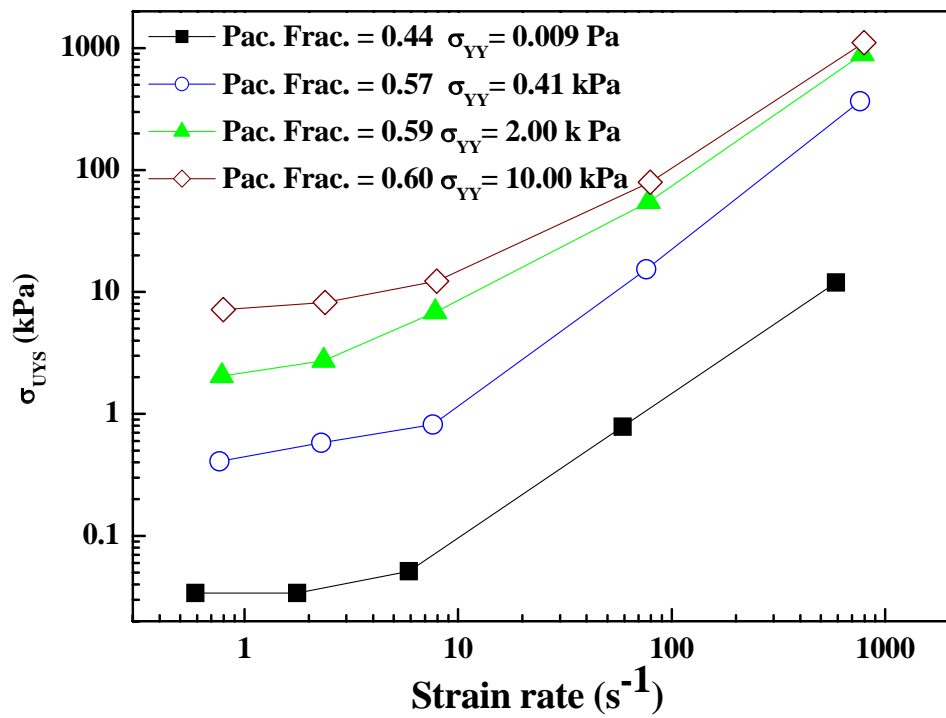


Fig. 5. Unconfined yield stress as a function of strain rate for different values of pre-consolidation stress.

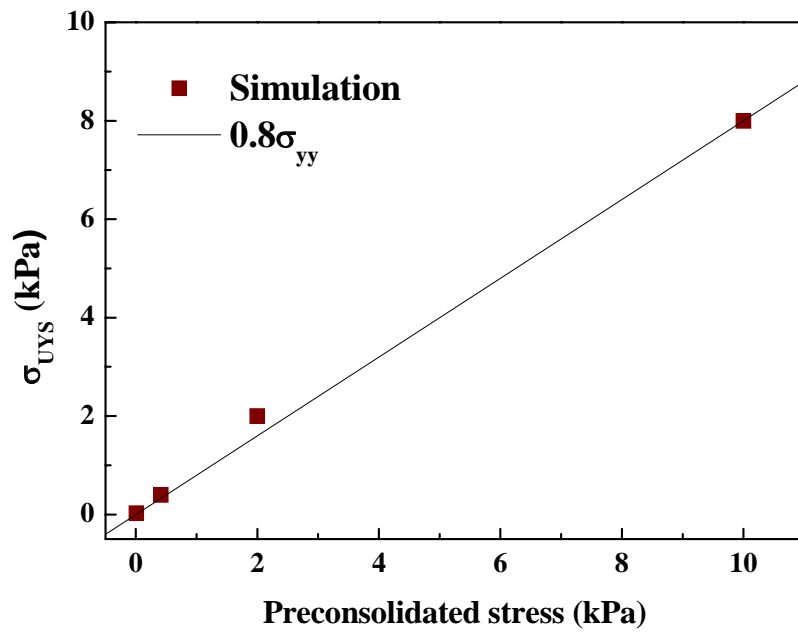


Fig. 6. Relationship between unconfined yield stress, σ_{UYS} , and pre-consolidation stress, σ_{yy} .

