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Geographically weighted correspondence matrices for *local* error reporting and change analyses: mapping the spatial distribution of errors and change

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Abstract

This letter describes and applies generic methods for generating local measures from the correspondence table. These were developed by integrating the functionality of two existing R packages: `gwxtab` and `differ`. They demonstrate how spatially explicit accuracy and error measures can be generated from local geographically weighted correspondence matrices, for example to compare classified and reference data (predicted and observed) for error analyses, and classes at times t_1 and t_2 for change analyses. The approaches in this letter extend earlier work that considered the measures derived from correspondence matrices in the context of generalized linear models and probability. Here the methods compute local, geographically weighted correspondence *matrices*, from which local statistics are directly calculated. In this case a selection of the overall and categorical difference measures proposed by Pontius and Milones (2011) and Pontius and Santacruz (2014), as well as spatially distributed estimates of kappa coefficients, User and Producer accuracies. The discussion reflects on the use of the correspondence matrix in remote sensing research, the philosophical underpinnings of *local* rather than *global* approaches for modelling landscape processes and the potential for policy and scientific benefits that local approaches support.

Key Words:

geographically weighted; accuracy and error; correspondence matrix; validation matrix; error matrix

1. Introduction

One of the under-explored research areas in remote sensing of land cover and land use is the investigation of local statistical models. Most remote sensing methods (classification, validation, change detection, etc) apply global approaches and models under the assumption that relationships between the variables or data under consideration remain constant over geographical space (Comber et al. 2012). Global models describe processes or patterns which are assumed to be location independent or stationary. Any spatial ‘variation’ in the results is driven by variation in data or variable values. However, this assumption of process spatial stationarity and invariance is contradicted by the many observations of spatial auto-correlation in remote sensing of landscape processes, especially classification error (from Campbell 1981 to Comber et al. 2016a), and more widely in geographic analyses under Tobler’s 1st law of geography (Tobler 1970). Spatial auto-correlation occurs when changes in properties of nearby features in geographic space are found to be correlated, contradicting the underlying assumption of independence in statistical analysis and inference. The result is process spatial non-stationarity when the statistical pattern or relationship observed in one region differs from that in another. An example of this *global* rather than *local* philosophy in remote sensing is the persistence of the use of the correspondence matrix. In error reporting this summarises the spatial coincidence of a classified dataset with a reference dataset, sometimes referred to as *predicted* and *observed* data, and in change analyses it summarises the class to class transitions between data collected at different times.

Recent research has started to address this fundamental statistical blind spot in remote sensing, and spatially sensitive approaches have been proposed for remote sensing classification (Comber et al. 2016b), data fusion (Lisev et al. 2016) and in applications where remote sensing data provides one of the input variables, for example mapping above ground biomass (Propastin 2012), population segregation (Yu and Wu 2004), net primary production (Wang et al. 2005) and in epidemiology (Khormi and Kumar 2011).

In remote sensing error analysis Foody (2005) calculated geographically distributed correspondence matrices and interpolated between them to generate surfaces of error. Extensions by Comber et al. (2012) and Comber (2013) developed geographically weighted (GW) measures accuracy from a GW logistic regression which were further extended to examine the spatio-temporal characteristics of classification accuracy by Tsutsumida and Comber (2015). All of these approaches provide spatially distributed measures of error that can be easily quantified using a simple logistic regression of the data in the correspondence matrix, as described in Comber (2013). However, many other measures may be calculated from the correspondence matrix including Kappa estimates (Congalton 1991) and the quantity and allocation disagreements suggested by Pontius and Millones (2011). Indeed, within statistics there is a long literature describing statistical measures that can be derived from the family of contingency tables (e.g. Hartigan and Kleiner 1981; Friendly 1994), of which the correspondence matrix is member. These are not straightforward to describe or formalise in a logistic regression, geographically weighted or not.

This letter describes a generic method for calculating spatially distributed correspondence matrices that support a much wider set of geographically weighted analyses of error, accuracy and correspondence. It uses the `gwxtab` R package (Brunsdon et al. 2016) as a framework for calculating local correspondence matrices. Then it uses these to calculate *local* difference metrics as described in Pontius and Milones (2011) and Pontius and Santacruz (2014) and implemented in the `diffeR` R package (Pontius and Santacruz 2015). For good measure we calculate local estimates of kappa coefficients and User and Producer accuracies. This letter highlights how thinking locally rather than globally can result in more spatially nuanced reportings of accuracy and other comparative measures such as change. It illustrates how generic tools such as `gwxtab` can be used to calculate local versions of any correspondence table derived metric, which can in turn be mapped, to generate novel, spatially distributed measures of accuracy.

2. Data and Methods

2.1 Data

The dataset used in this analysis was collated by International Institute for Applied Systems Analysis (IIASA) in Austria and is included in the `gwxtab` package. It describes land cover at 2,439 locations in the British Isles (minus the islands!) from 4 sources collapsed to 10 classes as described in Comber et al. (2013): volunteered land cover data collected by the Geo-Wiki initiative (Fritz et al. 2012), the GLC-2000 database (Fritz et al. 2003), the MODIS land cover product (Loveland et al. 2000) and GlobCover (Bicheron et al. 2008). The analyses in this letter compare the Geo-Wiki and MODIS data which are used here to illustrate the methods being proposed. Table 1 shows the correspondence matrix of the MODIS (rows) against the Geo-Wiki data (columns). The values in the table describe for each class, the counts of the data points in the first dataset that were assigned to each class in the second dataset. The off diagonal elements in the matrix summarise disagreements in the land cover classes allocated to pixels in each dataset.

Table 1. Matrix showing the correspondence between Geo-Wiki (columns) and MODIS (rows) land cover data' (or similar). The values are counts of the data points in each class in the Geo-Wiki data assigned to each class in the MODIS dataset.

	1	2	3	4	5	6	7	8	9	10
1. Forest	31	3	37	33	10	1	55	0	1	1
2. Shrub	0	0	0	1	0	0	31	0	0	0
3. Grass	11	4	26	62	15	1	19	0	5	1
4. Crop	13	1	117	355	10	1	78	0	2	3
5. Mosaic	53	1	293	135	1	0	89	0	2	1
6. Wetland	0	0	0	0	0	0	0	0	0	0
7. Urban	21	1	104	49	0	0	749	0	5	4
8. Snow	0	0	0	0	0	0	0	0	0	0
9. Barren	0	0	0	0	0	0	0	0	0	0
10. Water	0	0	1	1	0	0	1	0	0	0

2.2 Geographically weighted correspondence matrices

A correspondence matrix summarises the spatial intersection of 2 datasets and in a remote sensing error analysis, it compares the classified data with higher quality reference data at sample locations. In full a correspondence analysis, for example examining change over time, it summarises the spatial intersection of all data points or pixels. However, it provides no information about the spatial distribution of change or error, and the global measures derived the from correspondence matrix may mask local variations (McGwire and Fisher 2001).

The basic idea of geographically weighted approach is that local measures are computed from subsets of the full datasets at predefined locations. GW approaches seeks to quantify the spatial variation in relationships and in a GW analysis of local correspondence matrices, this describes the spatial variation in the correspondence between 2 datasets and generates spatially distributed measures of error, for example. At each location, a subset of the data falling under a kernel are weighted by their distance to that location and then used to construct the correspondence matrix. This local correspondence matrix can be used to calculate the statistic of interest.

The kernel size or bandwidth, can be fixed (e.g. 20 km) or it can be adaptive to subset the nearest n data points (e.g. 15%) and different kernel functions (shapes) can be used for the distance weighting. Generally larger bandwidths result in a greater degree of spatial smoothing. Gollini et al. (2015) describe some of these and methods for determining bandwidth optimally. In this case, an adaptive bandwidth of 15% was specified and a bisquare kernel were applied. For a given bandwidth h , this is defined by:

$$f(d) = \begin{cases} \left(1 - \left(\frac{d}{h}\right)^2\right)^2 & \text{if } d < h; \\ 0 & \text{otherwise.} \end{cases} \quad (1)$$

where d is the distance of the data point to the kernel centre.

Local, geographically weighted correspondence matrices were constructed comparing volunteered land cover data collected by the Geo-Wiki initiative (Fritz et al. 2012) with coincident MODIS global land cover at 4304 locations on a hexagonal grid covering the study area. The study area, grid and data points are shown in Figure 1, with 2 example locations labeled. Tables 2 and 3 show the *geographically weighted* correspondence matrices at these locations. As in Table 1, the values in the table describe the counts of pixels recorded in each class, in each dataset, but now just at that location. The table values are the sums of the *distance weighted* pixel counts.

Table 2. The local Geographically Weighted correspondence matrix at Location 1. The values are the counts of the geographically weighted data points in each class in the Geo-Wiki data assigned to each class in the MODIS dataset.

	1	2	3	4	5	6	7	8	9	10
1. Forest	1.58	0	3.30	0.00	0.01	0	0.00	0	0	0
2. Shrub	0.05	0	2.81	0.74	0.00	0	0.76	0	0	0
3. Grass	0.60	0	5.01	0.16	0.01	0	0.00	0	0	0
4. Crop	3.94	0	32.24	7.44	0.58	0	0.23	0	0	0
5. Mosaic	2.25	0	5.51	1.55	0.03	0	0.00	0	0	0
6. Wetland	0.00	0	0.41	0.24	0.00	0	0.00	0	0	0
7. Urban	0.91	0	4.46	0.79	0.09	0	18.66	0	0	0
8. Snow	0.00	0	0.00	0.00	0.00	0	0.00	0	0	0
9. Barren	0.94	0	2.95	0.00	0.00	0	0.00	0	0	0
10. Water	0.00	0	0.00	0.24	0.00	0	0.00	0	0	0

Table 3. The local Geographically Weighted correspondence matrix at Location 2. The values are the counts of the geographically weighted data points in each class in the Geo-Wiki data assigned to each class in the MODIS dataset.

	1	2	3	4	5	6	7	8	9	10
1. Forest	1.12	0	0.00	0.11	1.12	0	0.52	0	0	0
2. Shrub	0.18	0	0.00	0.00	0.07	0	0.00	0	0	0
3. Grass	0.83	0	0.11	2.08	2.10	0	0.62	0	0	0
4. Crop	1.15	0	0.11	11.27	3.73	0	0.94	0	0	0
5. Mosaic	0.88	0	0.04	1.57	0.24	0	0.00	0	0	0
6. Wetland	0.00	0	0.00	0.00	0.00	0	0.00	0	0	0

	1	2	3	4	5	6	7	8	9	10
7. Urban	0.95	0	0.28	0.62	1.71	0	3.90	0	0	0
8. Snow	0.00	0	0.00	0.00	0.00	0	0.00	0	0	0
9. Barren	0.00	0	0.00	0.47	0.31	0	0.00	0	0	0
10. Water	0.00	0	0.00	0.00	0.15	0	0.00	0	0	0

Accuracy measures: Quantity and Allocation Disagreements

Pontius and Millones (2011) and Pontius and Santacruz (2014) describe a number of methods for calculating difference metrics and composite measures of accuracy from the correspondence matrix. These are based around map-to-map cross-tabulations or correspondence matrices and can be used to compare mapped land cover data for error or change. For example, *quantity disagreement* is defined as the amount of difference between the *Observed* reference data and the *Predicted* classified data relative to the proportions of the classes in the *Observed* and *Predicted* data. It is computed from the sum of the row totals (the *Predicted* data) minus the sum of the column totals (the *Observed* data) divided by 2. Similarly, the *allocation disagreement* is defined as the amount of difference between the *Observed* data and the *Predicted* data that are due mis-matches in the spatial allocation of classes, relative to the class proportions. It is computed from the total number of pixels minus the diagonal agreement, minus the *quantity disagreement*. In all cases the measures can be computed from correspondence tables of counts of coincident pixels or proportions. Some of the measures from the `diffeR` package that were applied in this analysis are summarised in Table 4.

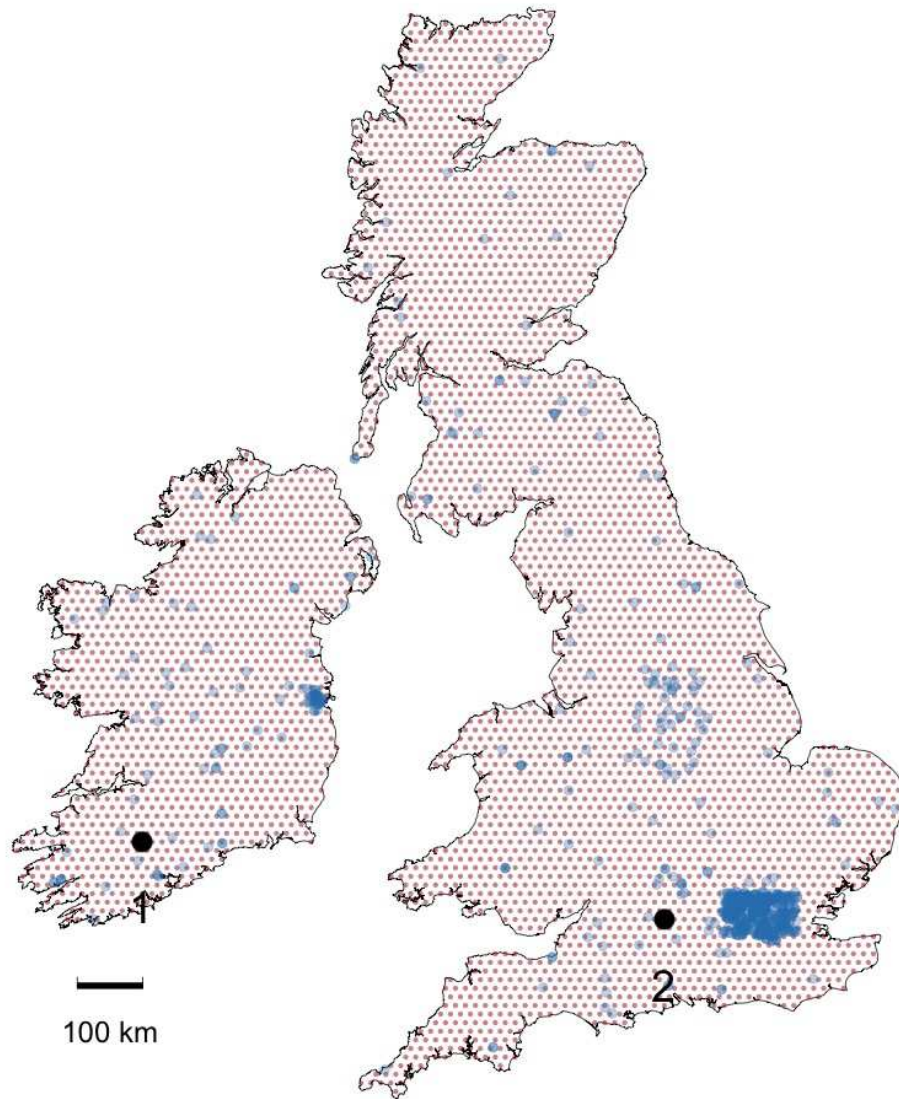


Figure 1: The study area, analysis grid in red, the data points shaded in blue with a transparency term to show their density, and 2 example locations.

Table 4: A summary of the difference and disagreement measures in the `differ` package

Measure	Function	Return value	Descriptions
Overall allocation difference	<code>overallAllocD</code>	Single value	The amount of difference between <i>observed</i> and <i>predicted</i> data due to the *less than maximum match* in the spatial allocation of the categories, given the proportions of the categories in both datasets.
Overall difference	<code>overallDiff</code>	Single value	The overall difference between tabulated <i>observed</i> and <i>predicted</i> data calculated from the sum of the quantity and allocation components of difference.
Overall exchange difference	<code>overallExchanged</code>	Single value	Exchange is the number of transitions from category <i>i</i> to category <i>j</i> in some observations and from category <i>j</i> to category <i>i</i> in an identical number of other observations.
Overall quantity difference	<code>overallQtyD</code>	Single value	This is the amount of difference between the <i>observed</i> variable and a <i>predicted</i> variable that is due to the less than maximum match in the proportions of the categories.
Overall shift difference	<code>overallShiftD</code>	Single value	Shift describes to the difference remaining after subtracting Quantity difference and Exchange from the Overall difference.
Category exchange difference	<code>exchangeDj</code>	Value for each class	The exchange value as above at the class level.
Category overall difference	<code>overallDiffCatj</code>	Value for each class	The overall difference as above at the class level.
Category quantity difference	<code>quantityDj</code>	Value for each class	The quantity difference as above at the class level.
Category shift difference	<code>shiftDj</code>	Value for each class	The shift difference as above at the class level.

Estimated Kappa Coefficient

Although now widely discredited, many remote sensing analyses still use the estimated kappa coefficient, $\hat{\kappa}$. It is defined as follows:

$$\hat{\kappa} = \frac{N \sum_{i=1}^r x_{ii} - \sum_{i=1}^r (x_{i+} \times x_{+i})}{N^2 - \sum_{i=1}^r (x_{i+} \times x_{+i})} \quad (2)$$

where N is the total number of observations in the matrix, r is the number of rows, x_{ii} is observations in row i and column i , x_{i+} and x_{+i} are the marginal totals of row i and column i , respectively. Essentially what this does is:

1. Multiply the sum of the diagonals by the table sum.
2. Then subtract from this the sum of the product of the row totals multiplied by the column totals.

3. Next, divide this by the sum of all the values in the table squared, minus the sum of the row and column marginal totals products.

The top part of the equation gives a measure of chance agreement and the bottom part a measure of the expected disagreements.

Code

The `R` markdown script used to produce this manuscript, including the text, all the `R` code, the data used in the analysis and code snippets used to produce the mapped figures, can be found at <https://github.com/lexcomber/RSLcode>

Results

A fixed bandwidth of 15% of the data points under a bisquare kernel was specified. At each location on the Grid in Figure 1 a geographically weighted correspondence matrix was constructed, comparing the MODIS and Geo-Wiki data. From these, the metrics described in Table 1 kappa coefficient estimates were computed. Maps of the spatial distribution of different accuracy measures are shown in Figure 2, 3 and 4. Figure 2 maps overall comparative measures and Figure 3 maps class specific measures from Pontius and Milones (2011) and Pontius and Santacruz (2014) as well spatially distributed, local estimated kappa coefficients. The definitions of the different measures can be found in the papers cited above or in the `diffeR` package. Room precludes the full description here but the critical point of developing these measures under a geographically framework, is that they are allowed to vary spatially. By way of example, Figure 4 maps User and Producer accuracies for the class or ‘urban’. It shows how and where the accuracies calculated from local cross-tabulations, vary from the global estimates from Table 1: User Accuracy has a global value of 0.803 and locally varies from 0.521 (1st quartile) to 0.723 (2nd quartile); Producer Accuracy has a global value of 0.733 and varies locally from 0.752 (1st quartile) to 0.939 (2nd quartile). An important point to note is that these variations do not reflect the distributions or densities of data points *per se*. Rather they reflect local measures calculated from local correspondence matrices at the locations mapped in Figure 1, under a window that draws in and weights data based on 15% bandwidth.

Discussion

The correspondence matrix is the *de facto* method in remote sensing for reporting comparisons between classified data, habitats, land cover and land use, for accuracy and error reporting and for summarise the results of change detection analyses. The local, spatially distributed, geographically weighted cross-tabulations described in this letter provide a framework for examining *how* and *where* measures derived from the correspondence matrix vary. They are an advance on the logistical regression methods suggested in Comber et al. (2012) and Comber (2013) because they support the generation of *any* local measure that the user wishes to specify. In this case the analyses integrated functions from two R packages: the `gwxtab` package to create local geographically weighted correspondence matrices and the overall and categorical difference measures in the `differ` package. The availability of open, free and transparent code provides a dynamic and rich research environment within which method extensions can be developed.

Whilst this paper advocates the application of local statistical models and spatially dependent methods, precisely because they reflect our understanding of nearly all processes and relationships we have encountered in natural and human sciences, (Tobler's 1st Law of Geography - Tobler 1970), we recognise that for many policy makers global statistics simplify complex data and provide an overall summary of the data and are therefore widely used. Local measures may not be intuitively understood. However, maps provide an incredibly powerful and accessible representation. So whilst policy makers may not immediately understand the various error measures in the `Differ` package, they will understand the mapped spatial distribution of a measure. It is therefore incumbent on the Remote Sensing community to more strongly engage with more advanced reporting techniques, such as local statistical models in their funded science. There is a previous example of this: land cover uncertainty reporting. In the 1980s and 1990s, policy makers struggled to understand that maps might contain errors and variations in representation. Now they do not: 10% reported error rates are readily understood. Providing open code and transparent methods (e.g through sites like <https://github.com/> is one way that the academic community could better support the up-skilling of policy makers (and maybe stimulate more interesting research being funded in Remote Sensing).

There are some important considerations related to the application of GW models, including bandwidth specification and kernel shape as described in Gollini et al. (2015). Here a bandwidth of 15% of the data points was selected but exploration using a range of bandwidths is recommended as bandwidth affects the degree of smoothing and thus the sensitivity of the analyses to the data distribution. As yet the `gwxtab` package does not include a function for bandwidth optimisation (as do other GW packages in R such as `GWmodel` and `spgwr`). This is an area that the developers of `gwxtab` are working on and will provide greater confidence in the results of the spatially distributed models, without requiring a formal sampling strategy.

The GW framework for correspondence tables presented here supports greater understanding of the spatial process and statistical relationships under investigation. This is important as the number and diversity of remote sensing derived products and applications increases and reflects the original aims of geographically weighted regression (Brunsdon et al. 1996). For example, it could be used to dynamically visualize accuracy, to characterise error, to provide local distributions of Chi-squared statistics, to explore the implications of different to locally focus additional ground-truth sampling, to assess the value of the imagery itself locally (e.g. LANDSAT versus MODIS), to explore the utility of different class definitions (e.g. Cropland vs. Managed grassland, which can be particularly difficult to classify) and to identify locales with missing and misaligned data.

Finally, spatially explicit approaches such as the GW correspondence matrices allow some of the dominant assumptions of spatial non-stationary of processes within remote sensing methods to be examined and tested. They accommodate the spatial auto-correlation found remote sensing data and analyses of many landscape processes.

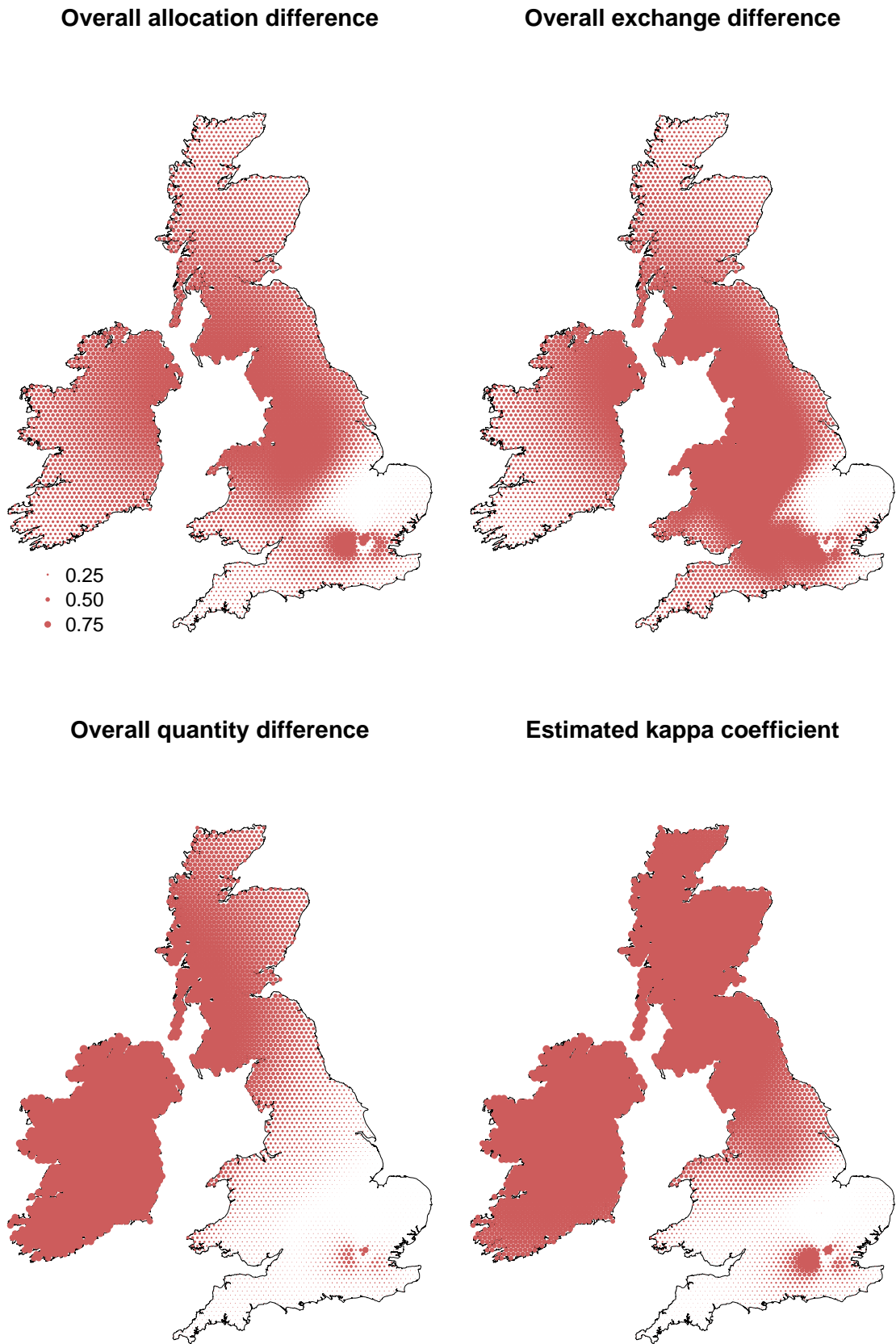
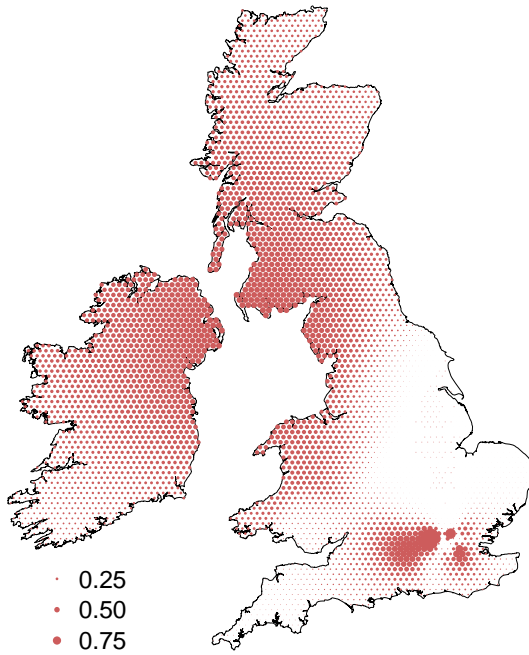
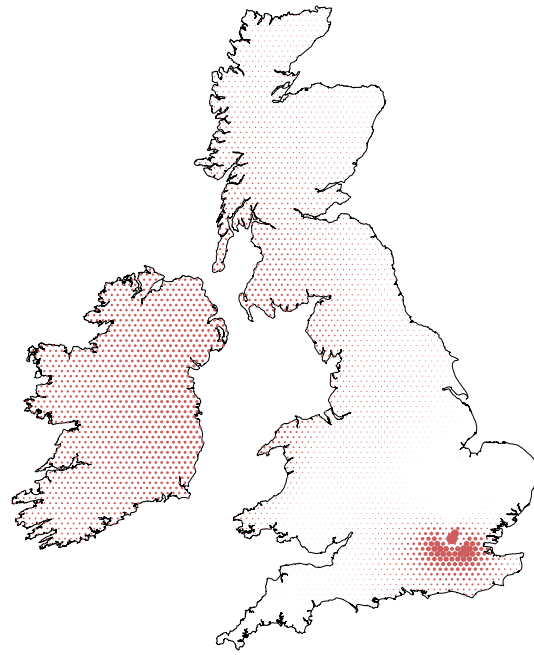


Figure 2: The spatial distribution of the difference measures, scaled to $[0, 1]$, comparing the Geo-Wiki crowdsourced data with MODIS data.

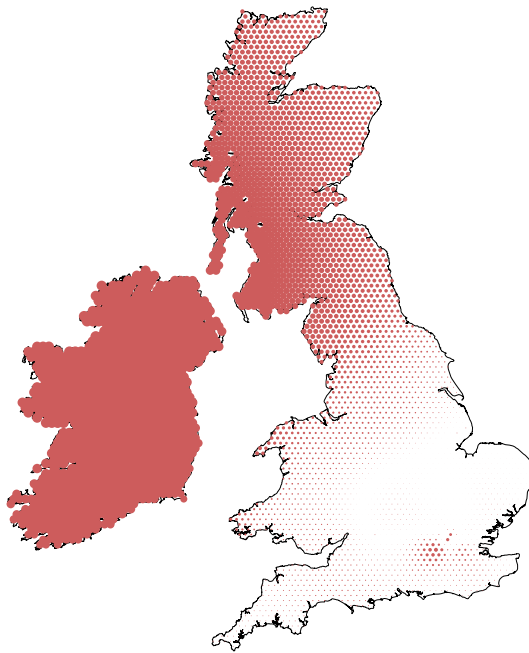
Exchange difference for 'forest'



Category Overall difference for 'urban'



Category quantity difference for 'grass'



Category shift difference

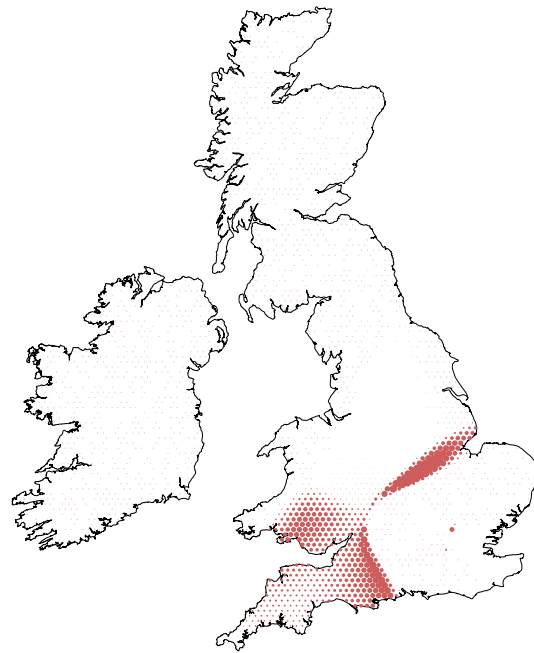


Figure 3: The spatial distribution of the class level, or categorical difference measures, scaled to [0, 1], comparing the Geo-Wiki crowdsourced data with MODIS data.

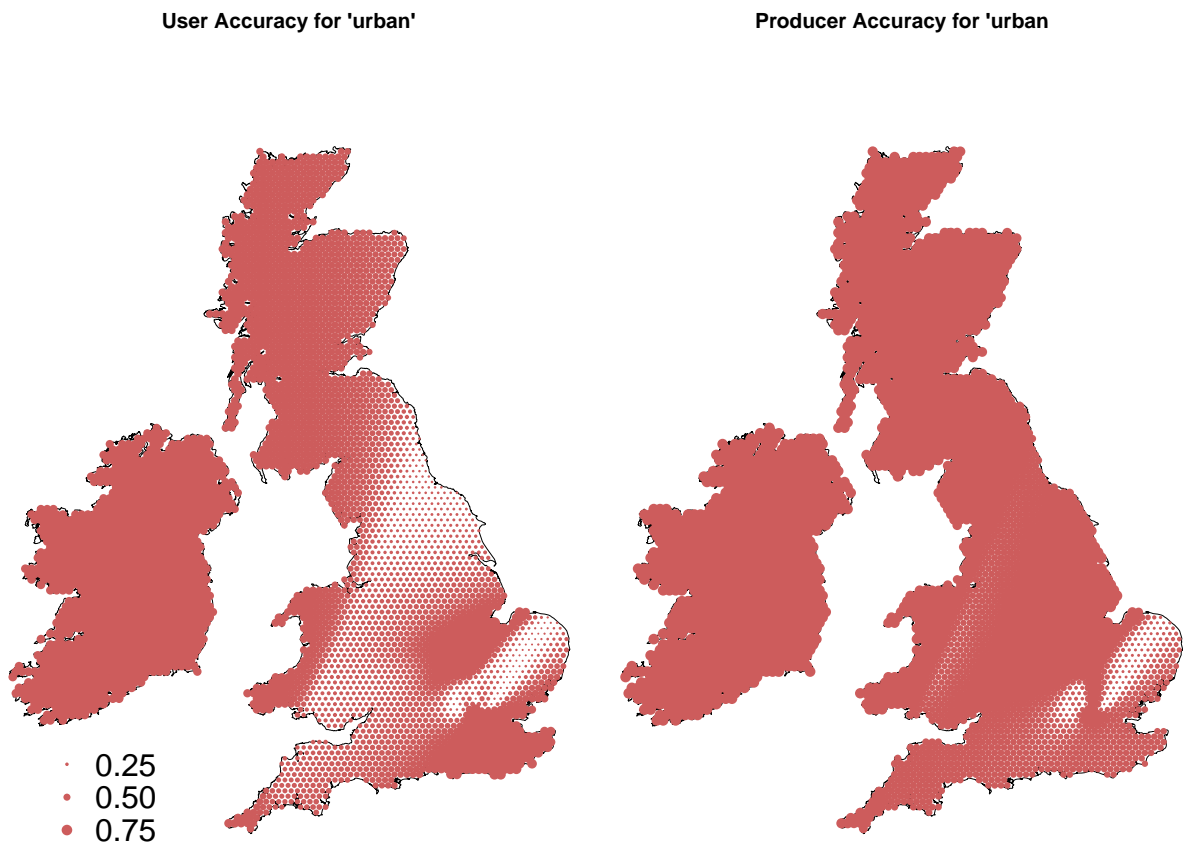


Figure 4: The spatial distribution of User and Producer accuracy values for the class of 'urban', scaled to $[0, 1]$, using the Geo-Wiki data to validate MODIS data.

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