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Distributed ice thickness and glacier volume in southern South America

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Abstract

South American glaciers, including those in Patagonia, presently contribute the largest amount of meltwater to sea level rise per unit glacier area in the world. Yet understanding of the mechanisms behind the associated glacier mass balance changes remains unquantified partly because models are hindered by a lack of knowledge of subglacial topography. This study applied a perfect-plasticity model along glacier centre-lines to derive a first-order estimate of ice thickness and then interpolated these thickness estimates across glacier areas. This produced the first complete coverage of distributed ice thickness, bed topography and volume for 617 glaciers between 41°S and 55°S and in 24 major glacier regions. Maximum modelled ice thicknesses reach 1631 m ± 179 m in the South Patagonian Icefield (SPI), 1315 m ± 145 m in the North Patagonian Icefield (NPI) and 936 m ± 103 m in Cordillera Darwin. The total modelled volume of ice is 1234.6 km³ ± 246.8 km³ for the NPI, 4326.6 km³ ± 865.2 km³ for the SPI and 151.9 km³ ± 30.38 km³ for Cordillera Darwin. The total volume was modelled to be 5955 km³ ± 1191 km³, which equates to 5458.3 Gt ± 1091.6 Gt ice and to 15.08 mm ± 3.01 mm sea level equivalent (SLE). However, a total area of 655 km² contains ice below sea level and there are 282 individual overdeepenings with a mean depth of 38 m and a total volume if filled with water to the brim of 102 km³. Adjusting the potential SLE for the ice volume below sea level and for the maximum potential storage of meltwater in these overdeepenings produces a maximum potential sea level rise (SLR) of 14.71 mm ± 2.94 mm. We provide a calculation of the present ice volume per major river catchment and we discuss likely changes to southern South America glaciers in the future. The ice thickness and subglacial topography modelled by this study will facilitate future studies of ice dynamics and glacier isostatic adjustment, and will be important for projecting water resources and glacier hazards.

Keywords sea level equivalent; sea level rise; Patagonia; South America; subglacial topography; overdeepening; hypsometry

39 **Highlights**

- 40 • New outlines and new centrelines for 617 glaciers between 41°S and 55°S
- 41 • Ice thickness statistics and ice volume per glacier reported
- 42 • Ice below sea level and within overdeepenings quantified
- 43 • Ice volume per major hydrological catchment determined

44

45 **Introduction and rationale**

46 The southern South America glaciers and Patagonian Icefields ([Figure 1](#)) are sensitive to climate
 47 change due to their relatively low latitude location, low-elevation termini and rapid response times
 48 (Oerlemans and Fortuin, 1992). They are the largest temperate ice masses in the Southern
 49 Hemisphere outside Antarctica and are sustained by the large volume of orographic precipitation that
 50 falls over the Andes under the prevailing Westerly winds (Carrasco et al., 2002; Casassa et al.,
 51 2002). Most of these ice masses are presently experiencing a negative mass balance, especially
 52 tidewater and lacustrine-terminating glaciers, but some glaciers, such as Pio XI, Moreno and
 53 Garibaldi, are presently displaying a positive mass balance (Schaefer et al., 2015). The general and
 54 dominant trend of ice mass loss is manifest in pronounced glacier recession (Davies and Glasser,
 55 2012) and the largest contribution to sea level rise per unit area in the world (Ivins et al., 2011;
 56 Mougnot and Rignot, 2015; Willis et al., 2012). Indeed this sea level contribution is ~ 10 % of that
 57 from all glaciers and ice caps worldwide (Rignot et al., 2003). Over the next two centuries, mass loss
 58 from these glaciers has implications for sea level rise (Braithwaite and Raper, 2002; Gardner et al.,
 59 2013; Glasser et al., 2011; Levermann et al., 2013), for increased hazards from glacial lake outburst
 60 floods (Anaconda et al., 2014; Dussaillant et al., 2009; Harrison et al., 2006; Loriaux and Casassa,
 61 2013), and for water resources.

62

63 Recent analysis of southern South America glaciers has yielded data regarding glacier area, areal and
 64 volume change since the Little Ice Age (LIA) (Davies and Glasser, 2012; Glasser et al. 2011), ice
 65 surface velocity (Rivera et al., 2012; Jaber et al., 2013; Mougnot and Rignot, 2015), surface mass
 66 balance (Koppes et al., 2011; Mernild et al., 2015; Schaefer et al., 2015; Willis et al., 2011) and
 67 surface thinning and elevation changes (dh/dt) (Rivera et al., 2007; Willis et al., 2012). These
 68 analyses are largely reliant on satellite observations due to the inherent difficulties in accessing large
 69 parts of the ice surface (cf. Paul and Mölg, 2014). There are few in situ observations (the few
 70 examples include Gourlet et al., 2016; Rivera and Casassa, 2002, and they target only the NPI and
 71 SPI) and none that cover all glaciers at a catchment-scale across the NPI, SPI, Cordillera Darwin,

72 Grand Campo Nevado and outlying small glaciers and icefields. As a result, directly observed data
73 on bed topography and ice thicknesses are sparse. Yet, these data are essential for calculations of ice
74 volume, potential sea level contribution, and are a key input parameter in numerical modelling
75 studies (Huybrechts, 2007), particularly when it is the smaller outlying glaciers and icefields with
76 fast response times that will respond most rapidly to climate change (Meier, 2007; Raper and
77 Braithwaite 2009). This study aims to provide the first complete regional calculation and assessment
78 of distributed glacier ice thickness and catchment-scale ice volume of all southern South America
79 glaciers (Figure 1).

80

81 **Southern South America: ice fields and volcanoes**

82 Our study area extends along the axis of the Andean mountain chain from Isla Hoste at 55 °S to
83 Parque Nacional Vicente Perez Rosales at 41°S (Figure 1). The highest peaks nearly reach 4000
84 m.asl and the terrain is generally steep. The area is characterised by a highly maritime climate with a
85 pronounced east-west precipitation gradient (cf. Figure 1), influenced by the westerly airflow over
86 the Andes (Aravena and Luckman, 2009; Garreaud et al., 2009). The steep orographically-driven
87 precipitation gradient produces precipitation on the western side of the Andes that is 100 % to 300 %
88 higher than on the eastern side. At 49 °S the precipitation totals are 7220 mm.yr⁻¹ east of the Andes,
89 and 209 mm.yr⁻¹ at Lago Argentino on the western side. Firn cores on the NPI confirm the east-west
90 gradient in accumulation (Rasmussen et al., 2007).

91

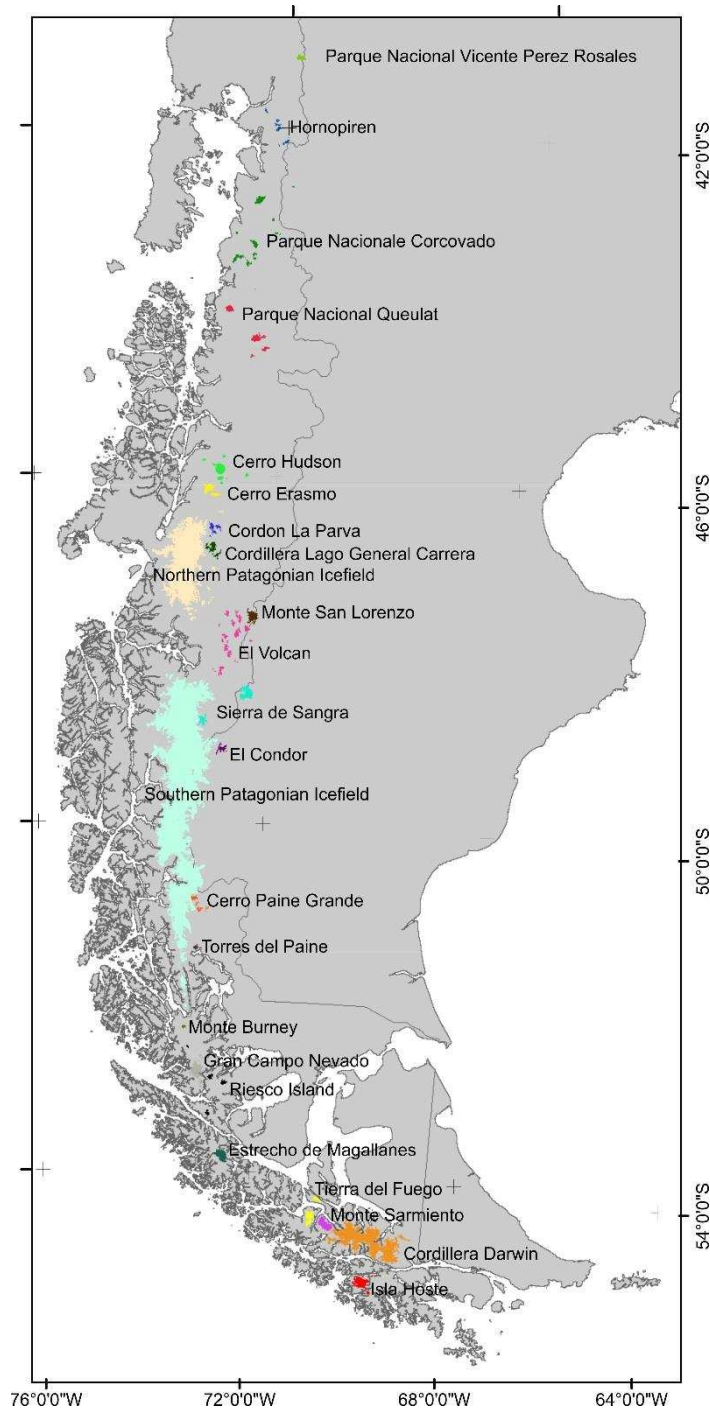
92 In Northern and Central Patagonia, precipitation has steadily decreased since around the 1960s
93 (Aravena and Luckman, 2009). Garreaud et al. (2013) found a 300 mm to 800 mm per decade
94 decrease in precipitation in north-central Patagonia, and a 200 mm to 300 mm per decade increase
95 south of 50 °S, which may account for generally positive glacier mass balances south of 50°S
96 (Shaefer et al., 2015), decreasing rates of glacier recession south of 50 °S after 2001 and faster rates
97 of recession north of 50 °S (cf. Davies and Glasser, 2012). There is also evidence of widespread air
98 temperature warming in Patagonia (Garreaud et al., 2013). Warming of the upper atmosphere (850
99 hPa; ca. 1400 m.asl) has been ~0.5 °C from 1960 to 1999, both in winter and summer and this
100 warming has caused a decreased in the amount of precipitation falling as snow and increased
101 ablation, exacerbating glacier recession (Rasmussen et al., 2007).

102

103 Some of these changes in precipitation have been related to variations in the strength of the
104 prevailing Southern Hemisphere Westerlies, with stronger westerlies augmenting local precipitation.
105 Stronger westerlies will also result in a decreased amplitude of the local air temperature annual cycle,

106 while weaker westerlies result in a colder winter and warmer summer, increasing temperature
107 seasonality (Garreaud et al., 2013). The core of the Southern Hemisphere Westerlies is currently 50
108 to 55°S, but through the Holocene latitudinal variations in these winds periodically brought increased
109 precipitation to the area, driving glacier advance and recession (Boex et al., 2013; Lamy et al., 2010;
110 Moreno et al., 2012) but with a pronounced east-west shift (Ackert et al., 2008).

111



112
113 **Figure 1.** Southern South America with the 24 major glacier regions of this study displayed in
114 unique colours.

115

116 The study area ([Figure 1](#)) includes 617 glaciers (mapped by Davies and Glasser, 2012; data available
117 from the GLIMS database: <http://nsidc.org/glims/>). These glaciers are found predominantly within
118 four key icefields: the North Patagonian Icefield (NPI), the South Patagonian Icefield (SPI), Gran
119 Campo Nevado (Schneider et al., 2007) and Cordillera Darwin (Bown et al. 2014), but also on
120 numerous outlying mountains and volcanoes (Rivera and Bown, 2013) ([Figure 1](#)).

121

122 In 2011, the total glacierised area of the study region was 22,717.5 km², with the SPI covering
123 13,218 km², the NPI covering 3,976 km², Cordillera Darwin covering 1832.7 km² and Gran Campo
124 Nevado covering 236.9 km² (Davies and Glasser, 2012). The large western outlet glaciers of the SPI
125 mostly extend down to sea level and calve into fjords, whilst those on the eastern side largely
126 terminate in large proglacial lakes (Warren and Sugden, 1993; Rasmussen et al., 2007). The NPI
127 glaciers have mean elevations of 1000 m to 1500 m, with one glacier (San Rafael) terminating in a
128 tidal lagoon, whilst the rest are lacustrine- or terrestrial-terminating glaciers. The ELA of outlet
129 glaciers of the NPI ranges from ~700 m.asl on the west and 1200 m.asl on the east (Kerr and Sugden,
130 1994; Barcaza et al., 2009). Snowline mapping in the SPI suggested that ELAs ranged from ~800 m
131 to 1400 m.asl (De Angelis, 2014).

132

133 **Previous ice-thickness measurements in southern South America**

134 Although the total ice area of the Patagonian Icefields is well constrained, the total ice volume is
135 poorly known. Most studies have focused on surface elevation change (dh/dt) using digital elevation
136 model (DEM) differencing, and from this have calculated glacier thinning and volume change
137 (Rignot et al., 2003; Willis et al., 2011). Alternatively, researchers have applied volume-area scaling
138 methods to estimate total ice volume (Grinsted, 2013), but this provides no data on bed topography
139 and has been criticised for being applied inconsistently or too simplistically (Bahr et al., 2014) and
140 because volume estimates are very sensitive to the scalar applied (Radic et al., 2008).

141

142 Glasser et al. (2011) estimated change in ice volume from the Little Ice Age (LIA) to present day by
143 inferring palaeo-ice thicknesses from trimlines, moraines and other geomorphological data and by
144 assuming a convex cross-valley ice surface profile at the LIA maximum. The change in ice volume
145 was calculated by differencing shapefiles of LIA glacier extent and glacier extent in 2002. However,
146 a lack of data on bed topography underneath present-day glaciers prevented the determination of
147 present-day ice volume.

148

149 There are just fourteen spot measurements of ice thickness in South America (Gärtner-Roer et al.,
150 2014). Distributed bed elevation and hence ice thickness data are available for some parts of the
151 Southern Patagonia Icefield, as derived using a radio-echo sounding system (Rivera and Casassa,
152 2002). A gravity traverse in the 1980s suggested that there was up to 1.5 km of ice on the NPI
153 (Casassa, 1987). Radar sounders have had little success, due to high absorption and scattering of
154 radar in temperate ice. Ground radars have been limited to ice thicknesses of ~700 m to 750 m of ice
155 (Raymond et al., 2005). Seismic measurements have indicated that Glaciar Moreno has a maximum
156 depth of 720 m (Rott et al., 1998). More recently, helicopter-borne gravity observations have
157 provided observations of ice thickness and bed topography across 49 % of the NPI and across 30 %
158 of the SPI but have excluded all glaciers outlying from the icefields (Gourlet et al., 2016). This
159 dataset is further limited in coverage because adverse weather during these helicopter surveys
160 prevented the survey of Glaciar San Quíntin on the NPI and Glaciar Greve on the SPI.

161

162 **Data sources and methods**

163 **DEM**

164 We obtained an Advanced Spaceborne Thermal Emission and Reflection Radiometer Global Digital
165 Elevation Model Version 2 (ASTER GDEM V2) mosaic from <http://asterweb.jpl.nasa.gov/gdem.asp>.
166 ASTER GDEM V2 has a 30 m (1 arc-second) grid of elevation postings, with accuracies of 20 m for
167 vertical data and 30 m for horizontal data at 95% confidence level.

168

169 **Glacier outlines**

170 Glacier drainage basins (Figure 2A) were obtained from Davies and Glasser (2012). They were
171 mapped from orthorectified (level 1G) Landsat Enhanced Thematic Mapper Plus (ETM+) images
172 from the year 2010-2011, which were pre-registered to the Universal Transverse Mercator (UTM)
173 World Geodetic System 1984 ellipsoidal elevation (WGS84), zone 18S projection. These images
174 have a spatial resolution of 30 m and a geositional accuracy of ± 50 m (Davies and Glasser, 2012).

175

176 The drainage basins were edited to include nunataks and this new dataset we refer to herein as
177 ‘glacier outlines’. Nunataks, or areas of ice-free terrain, were identified in this study using Landsat 8
178 Operational Land Imager (OLI) scenes and a mask derived from the Normalised Difference Snow
179 Index ($NDSI = (Green - SWIR)/(Green + SWIR)$). OLI scenes were selected to have been acquired
180 during summer months (December-March) to minimise cloud, snow and shadow. Threshold values
181 of the NDSI varied between 0.4 and 0.5, except for images covering Cordillera Darwin where
182 persistent cloud-cover limited the available data to a single scene. In this case a value of 0.25 was

183 used to avoid the inclusion of deep shadow. Some minor manual editing of the automatically-derived
184 nunataks was required to remove isolated pixels and pixel groups representing surface debris most
185 commonly medial moraine, and some supraglacial lakes and some clouds. Despite this editing, and
186 because we relied on a single Landsat scene per region, there is a chance that some nunataks were
187 not include, and a chance that some erroneous nunataks persist.

188

189 **Glacier centrelines**

190 The identification of glacier ice-surface flow trajectories requires fully distributed velocity fields.
191 These data are available for some of the outlet glaciers of the NPI and SPI (Jaber et al., 2014;
192 Mouginot and Rignot, 2015), but are lacking for Cordillera Darwin, Gran Campo Nevado, and the
193 numerous smaller outlet glaciers and icefields. The lack of a complete velocity dataset makes
194 regional scale applications of automatic flowline generation unachievable (Kienholz et al. 2014).

195

196 Whilst manual digitization of centrelines is a subjective process and is time consuming in
197 comparison to automatic extraction methods such as those using GIS hydrology tools (e.g. Schiefer
198 et al., 2008; Machguth and Huss 2014), cost-distance analysis (e.g. Kienholz et al. 2014) and
199 geometric analysis (e.g. Le Bris and Paul 2013), manual digitization is expert-driven. Unfortunately,
200 our attempts to use these automatic centreline calculation methods on southern South America
201 glaciers lead us to suggest that these automated techniques are also susceptible to edge cases and
202 frequently fail to operate in glaciers with a complex or unusual form. Furthermore, all the
203 aforementioned examples of automatic centreline extraction have been reported only in terms of
204 method development and are not with freely-available code and not with full testing on a regional
205 scale.

206

207 In this study, centrelines were manually digitized from the centre of a glacier terminus, propagating
208 up-glacier approximately midway between and parallel to the lateral margins of any glacier ablation
209 tongue, and thence towards any prominent saddles or cols on cirque headwalls or on ice divides
210 (Figure 2A). In the same manner centrelines were created for each major glacier tributary (Figure
211 2A) to produce a total of 1,995 centrelines. To permit comparisons between this and past studies, and
212 noting that our model mostly depends on ice surface slope, we did not make edits in the few cases
213 where our glacier outlines or our glacier centrelines did not exactly match those from ice surface
214 velocity analyses (Mouginot and Rignot, 2015).

215

216

217 **Calculating ice thickness at points along the centreline**

218 Ice thickness h of mountain glaciers can be estimated from a glacier surface slope α using a perfect
219 plasticity approach by:

220

$$221 \quad h = \frac{\tau_b}{fpg \tan \alpha} \quad (1)$$

222

223 where τ_b , is basal shear stress and a shape factor f is required to account for valley sides supporting
224 part of the weight of the glacier. In this study we used the ArcGIS tool developed by James and
225 Carrivick (2016), which extended existing perfect plasticity models from application along single
226 centrelines to fully 3D coverage, accommodated calculations on glaciers with complex geometry and
227 automated this approach for application to multiple glaciers or whole glacier regions. Since that
228 model is published (James and Carrivick, 2016) we simply cover the most salient points herein.

229

230 We calculated h at points spaced 50 m apart on all centrelines where that spacing was selected
231 considering the 30 m resolution of the ice surface model and the spatial coverage of this study.

232 Whilst f has been incorporated as a constant (usually 0.8 according to Nye 1965: e.g. Linsbauer, Paul
233 and Haeberli 2012), Li et al. (2012) developed a more physically realistic method to dynamically
234 adjust f depending on the local width of a glacier. In detail, Li et al. (2012) estimated ice thickness
235 perpendicular to the ice surface but in this study we are dealing with GIS-analysed glacier geometry
236 so to consider ‘vertical’ ice thickness, h , i.e. that perpendicular to a horizontal x-axis we re-write the
237 Li et al. (2012) equation as:

238

$$239 \quad h = \frac{0.9 w \left(\frac{\tau_B}{pg \tan \alpha} \right)}{0.9 w - \left(\frac{\tau_B}{pg \tan \alpha} \right)} \quad (2)$$

240

241 where w is half the glacier width at the specified point on a centreline.

242

243 Where nunataks are present, or where tributaries converge, Li et al. (2012) cautioned that this type of
244 width calculation may be inaccurate. We therefore implemented an automatic check for erroneous
245 values by: (i) checking if the perpendicular ‘width’ line intersected another centreline and (ii) cross
246 checking if the resulting f value (Eq. 1) is realistic (> 0.445 , equal to a half width to centreline
247 thickness ratio of 1: Nye 1965). At points where either of these conditions were met, h was
248 calculated using Eq. 1, with f set to that of the average of all points on the same tributary.

249

250 **Interpolating distributed ice thickness and bed topography**

251 Distributed ice thickness was interpolated from the centreline points across each glacier using the
 252 ANUDEM 5.3 interpolation routine, which is an iterative finite difference technique designed for the
 253 creation of hydrologically correct DEMs (Hutchinson 1989). ANUDEM generates preferably
 254 concave shaped landforms, thus mimicking the typical parabolic shape of (idealised) glacier beds
 255 (Linsbauer et al. 2009). It is commonly applied to estimating bed topography of both mountain
 256 valley glaciers (Farinotti et al., 2009; Li et al., 2012; Linsbauer et al., 2012; Fischer and Kuhn 2013)
 257 and ice sheets, such as within the Antarctica Bedmap2 dataset (Fretwell et al. 2013). In this study we
 258 forced the interpolation of ice thickness to zero at glacier outlines that were not in contact with
 259 another outline. Interpolations of ice thickness through ice divides was achieved simply by
 260 ‘dissolving’ (i.e. removing) those parts of glacier outlines that were in contact with each other.

261

262 Once thickness h for each grid cell in each glacier had been interpolated, total volume V was
 263 calculated:

264

$$265 \quad V = \sum(c^2h) \quad (3)$$

266 where c is the cellsize, which was 100 m.

267

268 James and Carrivick (2016) compared modelled (individual) glacier volume to that derived from
 269 field measurements of alpine glaciers around the world, and found worst-case 26.5 % underestimates
 270 and 16.6 % overestimates. For comparison errors for volume scaling approaches range from 30 %
 271 for large samples to 40 % when considering smaller (~ 200) samples (Farinotti and Huss 2013). Part
 272 of the model error in this study comes from the perfect-plasticity assumption, and part comes from
 273 the spatial interpolation from centreline thicknesses to glacier-wide thickness. Where James and
 274 Carrivick (2016) were able to compare centreline modelled thickness with thickness from field radar
 275 measurements on alpine glaciers around the world they found differences < 11 %. They also found
 276 that larger glaciers were least sensitive in terms of modelled volume to model parameters, which are
 277 described and explained in the next sub-section. Across southern South America 73 % of all glaciers
 278 are > 3 km² and > 96 % are of a mountain glacier type being underlain by high-relief subglacial bed
 279 topography that controls ice flow, so this an ideal study site in which to apply this model. In this
 280 study our uncertainty is spatially-variable and we therefore report modelled ice thickness with a
 281 mean uncertainty of ± 11 % and glacier volume with a mean uncertainty of ± 20 % but note that

282 these uncertainties will rise in the worst cases which are where there are large floating glacier
 283 termini.

284

285 To estimate sea level equivalent ice volume was converted to a mass via an estimate of ice density.
 286 We used a single theoretical value for ice of 916.7 kg.m^{-3} and assigned this globally to the whole
 287 study area. We acknowledge that this does not consider snow or firn, which in some parts of
 288 southern South America where snow accumulation is very high could be volumetrically significant.
 289 For example, Schwikowski et al, 2013 drilled on Pio XI glacier and found $\sim 50 \text{ m}$ of snow/ firn (with
 290 densities $< 800 \text{ kg.m}^{-3}$) and a similar $\sim 50 \text{ m}$ thickness of snow / firn was found on Tyndall glacier
 291 (Godoi et al., 2002). However, (i) these snow / firn depths account for $\sim 10 \%$ of the mean glacier
 292 thickness (as will be presented below) and (ii) we have no way of spatially-interpolating them either
 293 per glacier or for the whole of southern South America.

294

295 **Parameterisation**

296 The model employed in this study uses an ice surface DEM and glacier outlines to automatically
 297 derive glacier specific values of basal shear stress τ_b , slope averaging distance α_d , “effective width”
 298 slope threshold α_{lim} , and minimum slope threshold α_0 , as explained below.

299

300 τ_b is variable between individual glaciers due to basal water pressure, ice viscosity and subglacial
 301 sediment deformation, for example (Cuffey and Patterson, 2010). For ice thickness estimations such
 302 as those within in this study, τ_b does not have to be varied longitudinally for an individual glacier as a
 303 constant value can reproduce accurate thickness estimates along the length of a centreline (Li et al.
 304 2012). Whilst τ_b can be “constrained reasonably from just a few ice-thickness measurements” (Li et
 305 al. 2012 p.7), in southern South America $> 85 \%$ of all glaciers do not have any ice thickness
 306 measurements, thus requiring τ_b to be estimated. Previous studies have used an empirical
 307 relationship between altitudinal extent and τ_b that was developed by Haeberli and Hoelzle (1995) but
 308 the relationship is weak ($r^2 = 0.44$) and Linsbauer et al. (2012) reckoned an uncertainty of up to ± 45
 309 % using this method. Therefore in this study we employ a relationship established by Driedger and
 310 Kennard (1986a), using area and slope in an elevation band approach:

311

$$312 \quad \tau_b = 2.7 \cdot 10^4 \sum_{i=1}^n \left(\frac{A_i}{\cos \alpha_i} \right)^{0.106} \quad (4)$$

313

314 where the elevation band area (A_i) is in m^2 and τ_b is in Pa. This method was tested by Driedger and
 315 Kennard (1986b) as part of a volume estimation study, and they found a standard deviation of error
 316 of 5 % when comparing modelled with measured volumes. We calculated A_i and $\cos \alpha_i$ over 200 m
 317 ice-surface elevation bands to produce glacier specific average τ_b values that were consequently
 318 applied to each centreline point.

319

320 Reliable ice thickness h , estimates required analysis of the centreline gradient over an appropriate
 321 slope distance α_d . If α_d is too short small scale variations in the surface topography are produced in
 322 the estimated bed profile. Conversely, if α_d is too long, variations in the surface topography may be
 323 smoothed or omitted. Therefore α_d should be several times the local ice thickness (Paterson 1994). In
 324 this study we automatically set α_d to be 10 times the average ice thickness \bar{h} , with \bar{h} derived from a
 325 volume area scaling approach (Radić and Hock 2010):

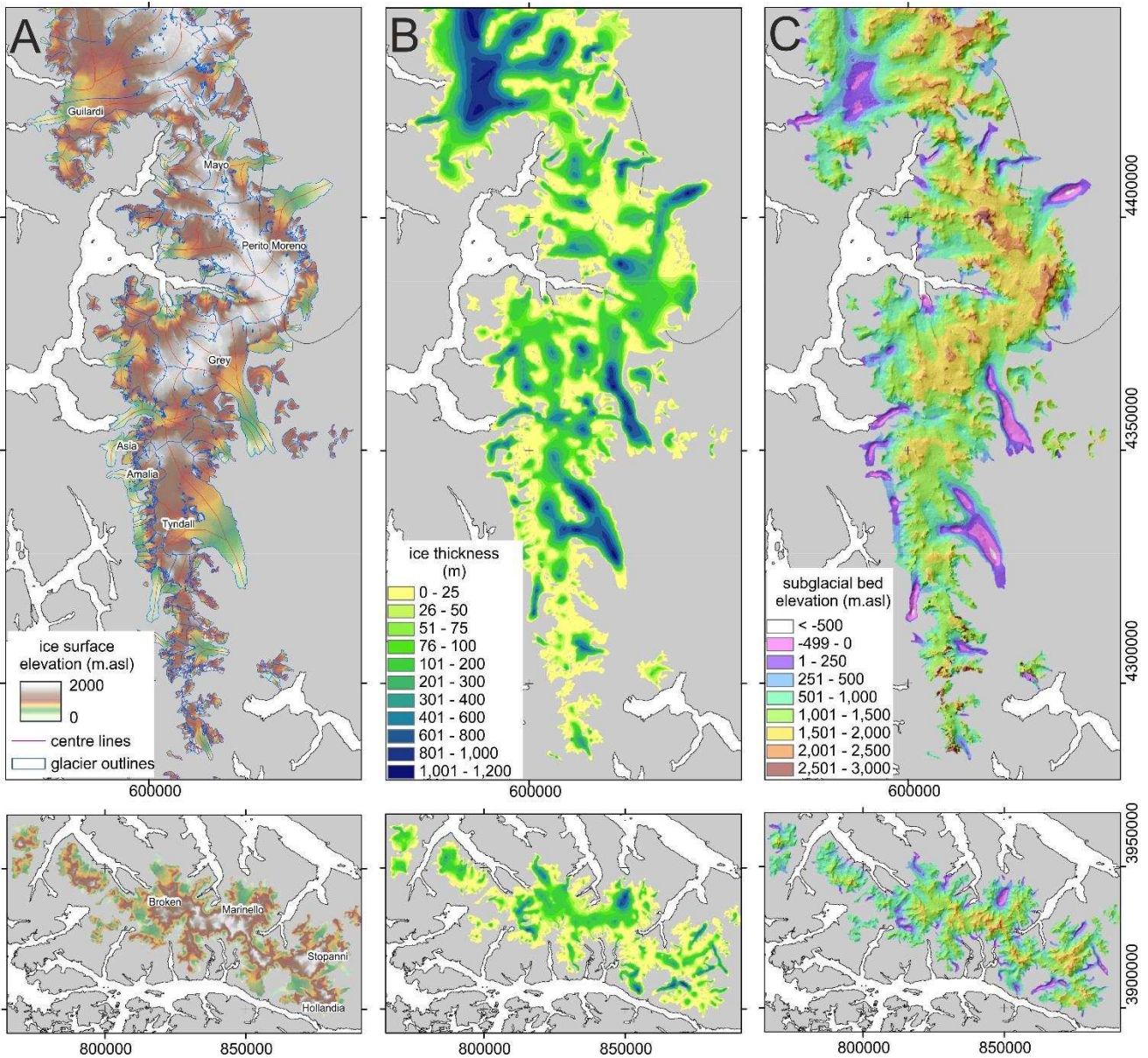
326

$$327 \quad \bar{h} = \frac{0.2055A^{1.375}}{A} \quad (5)$$

328 where A is glacier area. This α_d also usefully served to virtually eliminate the effects of some small
 329 areas of ‘noise’ in the ice surface DEM, which is an unfortunate artefact inherent in the GDEM
 330 product especially over areas of low-angle ice and snow.

331

332 Using Eq. 2, h will tend to infinity as surface slope tends to zero, meaning h may be overestimated in
 333 regions of flatter ice surface (Li et al. 2012; Farinotti et al. 2009). In this study a ‘minimum slope
 334 threshold’ α_0 of 1.7° was used to re-assign any lower slope values to that minimum value. We note
 335 that Farinotti et al. (2009) used 5° and Li et al. (2012) used 4° , but since 40 % of the ice surface in
 336 southern South America is 4 or less this was too high a value for application to the glaciers of
 337 southern South America. Additionally, the ‘low slope’ parts of ice surfaces are generally situated
 338 within the trunks of the major outlet glaciers (and not to the ‘plateau’ itself which commonly has
 339 clearly discernible drainage basin divides marked by either a change in curvature between adjacent
 340 steep $> 45^\circ$ slopes or by nunataks). Only 0.5 % of the ice surface in this study is $< 1.7^\circ$.



341
342

343 **Figure 2.** Examples from the southern part of the SPI (uppermost larger panels) and from the
344 Cordillera Darwin region (lowermost smaller panels) of the Digital Elevation Model (DEM), glacier
345 outlines and glacier centrelines (A), which together enabled modelling of distributed ice thickness
346 (B) and thus bed topography (hillshaded in these images) (C). Only major glaciers are named in
347 panel A for clarity. Both sets of panels have the same spatial scale and the same legends.
348

349

350 In this study we specified an ‘effective width slope threshold’ α_{lim} of 30° , so as to consider that where
351 glaciers are thin valley walls contribute negligible support and thus in this situation should not be
352 included in Eqn 2. This threshold of 30° represents h values of 27 m and 37 m as parameterised for
353 the European Alps (130 kPa) and for the New Zealand Alps (180 kPa), respectively (Hoelzle et al.
354 2007) and is the optimal value found during analysis by Li et al. (2012). These h values are also

355 consistent with Driedger and Kennard (1986a) who found a threshold $\bar{h} \sim 36$ m where glaciers obtain
 356 a critical shear stress and contributed to ice deformation.

357

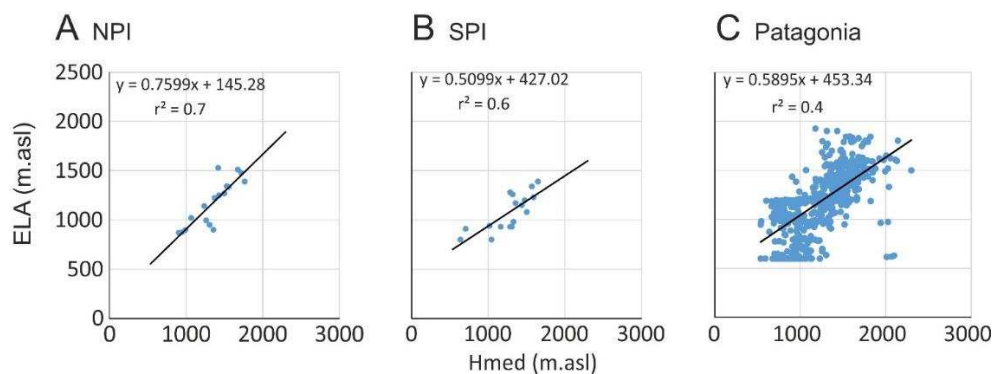
358 **ELA estimation**

359 Glacier equilibrium line altitudes delineate a theoretical boundary between zones of net accumulation
 360 and net ablation over multiple years. The inter-annual ELA fluctuates primarily due to changes in
 361 weather and can be approximated by the end-of-summer snowline (EOSS). Across Patagonia
 362 snowlines for 2002 to 2004 have only been measured via remote sensing for a few tens of SPI
 363 glaciers by De Angelis et al. (2014) and for the period 1979 to 2003 for a few tens of NPI glaciers by
 364 Bacaza et al. (2009). ELAs have also been modelled across southern South America via spatial
 365 interpolation of continuous automatic weather station data from 1960 to 1990 by Condom et al.
 366 (2007).

367

368 To extend analysis of ELAs across the whole of southern South America in this study, and mindful
 369 of the lack of knowledge of mass balance gradients (c.f. Raper and Braithwaite, 2009), we used the
 370 median elevation (Hmed) of glaciers as the most simple proxy for ELA, which was first proposed by
 371 Hess (1893) and has been widely used since (e.g. Carrivick and Brewer, 2004; Braithwaite and
 372 Raper, 2010; Davies and Glasser, 2012). We used Hmed as a proxy for ELA because we found
 373 correlations between the published values of EOSS for both the NPI ($r^2 = 0.72$: [Figure 3A](#)) and for
 374 the SPI ($r^2 = 0.6$: [Figure 3B](#)). The correlation of Hmed between the modelled ELA 1960 to 1990 of
 375 Condom et al. (2007) is less strong ($r^2 = 0.4$: [Figure 3C](#)) and has a spatial pattern of increasing
 376 discrepancy southwards ([SI_A](#)). We interpret this poorer correlation of Hmed with modelled ELA to
 377 suggest that glacier geometry has responded significantly to climate change during the 20 years
 378 between 1990 and our glacier outline inventory of 2010-2011 and thus that the modelled ELA of
 379 Condom et al. (2007) is not a good representation of the contemporary ELA.

380



382 **Figure 3.** Comparison of ELAs estimated from end-of-summer snowlines with median glacier
 383 elevation (Hmed) for the NPI (A) and SPI (B). Note different that the snowlines for the NPI and for
 384 the SPI were measured over different time periods and by Barcaza et al. (2009) and by De Angelis et
 385 al. (2014), respectively. Comparison of the long-term ELA as modelled via spatial interpolation of
 386 climate data 1960 to 1990 by Condom et al. (2007) with Hmed of glaciers in the 2010-2011 glacier
 387 inventory (C).
 388

389

390 **Spatial and statistical analysis**

391 Zonal statistics per glacier, per major glacial region and per major river catchment were extracted
 392 from ice-surface elevation, ice thickness, subglacial bed topography and ELA trend grids in ArcGIS.
 393 Bed elevations below sea level were automatically extracted via a binary reclassification of bed
 394 topography [> 0 m.asl = 0, < 0 m.asl = 1], conversion of the '1' values in this grid to polygons, and
 395 then zonal analysis of bed topography per polygon zone. Overdeepenings were automatically
 396 extracted from bed topography by 'filling sinks' in the bed topography and analysed in the same
 397 manner as for bed elevations. Major rivers and major lakes in southern South America were
 398 manually digitised in a GIS using Landsat images. River catchments that intersected glacier outlines
 399 were extracted from HydroSHEDS (Lehner et al., 2006), which is derived from elevation data of the
 400 Shuttle Radar Topography Mission (SRTM) at 90 m resolution.

401

402 **Results**

403

404 Overall, the 617 glaciers considered in this study cover an area of 22,121.9 km² with a mean
 405 thickness of 264 m and comprising a total volume of 5955 km³ ± 1191 km³. Using an ice density of
 406 916.7 kg.m⁻³, this volume equates to 5458.3 Gt ± 1091.6 Gt ice and to 15.08 mm ± 3.01 mm sea
 407 level equivalent (SLE).
 408

409

410 There is a wide range in Hmed of glaciers within each major glacier region (Table 1), reflecting the
 411 strong precipitation and temperature gradients in the area and the controls of these upon glacier
 412 surface energy balance and glacier mass balance. The difference in mean Hmed value between each
 413 major glacier region (Table 1) is crudely associated with latitude with lower mean Hmed occurring
 414 farther south. A table of glacier geometry, ice thickness and volume attributes, per glacier, is
 415 included in supplementary information (SI_Table1).
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Major glacier region	Mean ice thickness (m)	Max. ice thickness (m)	Volume (km ³)	Sea level equivalent (including ice mass below sea level) (mm)	Maximum potential sea level rise (excluding ice mass below sea level) (mm)	Minimum Hmed (m.asl)	Mean Hmed (m.asl)	Maximum Hmed (m.asl)
Gran Campo Nevado	79	639	19.7	0.05	0.05	537	841	1230
Cordon La Parva	33	379	2.6	0.01	0.01	1227	1547	1845
Northern Patagonian Icefield	305	1315	1234.6	3.13	3.10	904	1417	1809
Cerro Hudson	131	759	28.5	0.07	0.07	1259	1436	1594
Cerro Erasmo	107	871	14.9	0.04	0.04	1204	1429	1569
El Volcan	44	361	14.8	0.04	0.03	992	1529	1792
Cordillera Lago General Carrera	39	696	5.0	0.01	0.01	1490	1720	2299
Monte San Lorenzo	57	739	8.1	0.02	0.02	1340	1901	2131
Southern Patagonian Icefield	331	1649	4326.6	10.96	10.62	638	1242	2097
Sierra de Sangra	67	449	17.8	0.05	0.05	1416	1595	2026
Cordillera Darwin	82	936	151.9	0.38	0.37	602	950	1659
El Condor	50	552	3.8	0.01	0.01	1327	1435	1542
Isla Hoste	93	651	20.0	0.05	0.08	536	755	851
Monte Sarmiento	69	474	12.5	0.03	0.04	691	869	1141
Cerro Paine Grande	72	491	5.4	0.01	0.01	1056	1292	1537
Tierra del Fuego	63	379	9.9	0.03	0.02	664	770	814
Estrecho de Magallanes	222	845	39.9	0.10	0.10	404	724	976
Riesco Island	48	548	5.1	0.01	0.01	746	876	1071
Torres del Paine	28	178	0.7	0.00	0.00	543	1015	1353
Monte Burney	28	143	0.4	0.00	0.00	688	939	1123
Parque Nacional Corcovado	41	380	11.3	0.03	0.02	1259	1536	1820
Parque Nacional Queulat	72	639	14.9	0.04	0.04	1391	1481	1547
Parque Nacional Vicente Perez Rosales	40	143	2.6	0.01	0.01	1896	2152	2617
Hornopiren	44	278	4.1	0.01	0.01	1301	1620	1793

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Table 1. Glacier attributes per major region. Hmed is included as a proxy for ELA. In general ice thickness has an uncertainty of $\pm 11\%$ and volume has an uncertainty of $\pm 20\%$.

428 The NPI and SPI have mean modelled ice thickness of $305 \text{ m} \pm 33.5 \text{ m}$ and $331 \text{ m} \pm 36.4 \text{ m}$,
429 respectively, and we find that four other major glacier regions, namely Cerro Hudson, Cerro Erasmo
430 and Estrecho de Magallanes have mean modelled ice thicknesses $> 100 \text{ m}$ (Table 1). Maximum
431 modelled ice thicknesses reaches $1315 \text{ m} \pm 144.6 \text{ m}$ for the NPI and $1649 \text{ m} \pm 181.4 \text{ m}$ for the SPI
432 (Table 1). The total modelled volume of ice per major region is $4326.6 \text{ km}^3 \pm 865.3 \text{ km}^3$ for the SPI,
433 $1234.6 \text{ km}^3 \pm 246.9 \text{ km}^3$ for the NPI and $151.9 \text{ km}^3 \pm 30.4 \text{ km}^3$ for Cordillera Darwin (Table 1). All
434 other major glacier regions each contain a total of $< 40 \text{ km}^3$ glacier ice (Table 1).

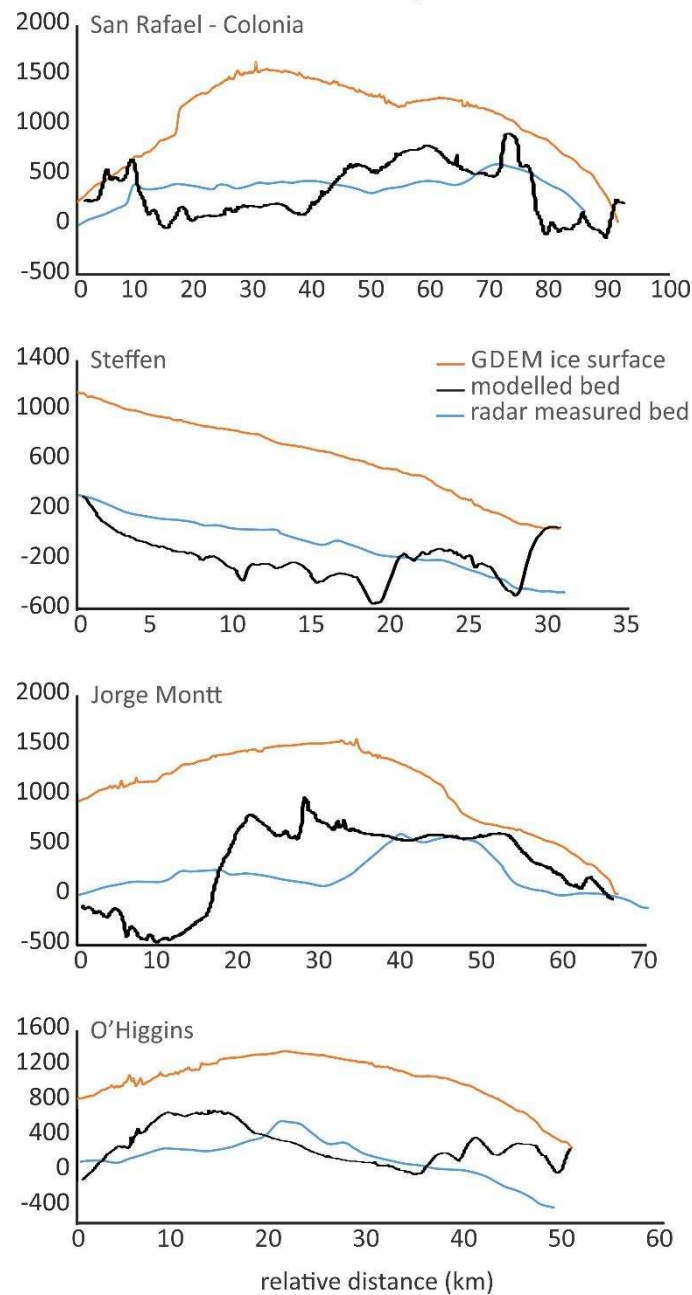
435

436 Our modelled ice thickness distribution, which is freely available as a downloadable ArcGIS-format
437 100 m grid raster via supplementary information, and a part of which is depicted in Figure 2B, can be
438 compared with that derived from gravity measurements by Gourlet et al. (2016) on the NPI and on
439 the northern part of the SPI. Our modelled subglacial bed topography has greater relief and
440 complexity than that derived by Gourlet et al (2014) from airborne gravity surveys (Figure 4).
441 Quantitatively, the mean ‘measured-modelled’ difference is 196 m , or $\sim 18 \%$ of ice thickness) along
442 the transects presented by Gourlet et al. (Figure 4), but it must be noted that unfortunately their
443 gravity survey lines do not correspond spatially to our centrelines. In more detail, their ice thickness
444 on these transects is an interpolation between their gravity lines, (ii) they acknowledged error in
445 narrow valleys and away from survey lines of $> 100 \text{ m}$, and (iii) our ice thickness along these
446 transects is an interpolation of that calculated along the centreline(s).

447

448 Profiles of bed topography along our centrelines are relatively bumpy in comparison to the estimated
449 bed topography between them and a glacier margin where the interpolation produces a very smooth
450 surface. This is a demonstration that our model has uncertainty in the centreline ice thickness
451 calculation, and then more uncertainty in the spatial interpolation of ice thickness. In general
452 therefore we suppose that our model reflects the general features and the orders of magnitude of ice
453 thicknesses in a region, especially with relatively small glaciers, but the complex subglacial
454 topography of the main icefields remains relatively crudely estimated.

455



456

457 **Figure 4:** Comparison of our modelled bed topography along transects presented by Gourlet et al.
 458 (2016) who derived ice thickness from airborne gravity measurements. The position of these
 459 transects is depicted in our Fig. SI_B.

460

461

462 Nevertheless, our modelled bed topography identifies mountain ridges submerged beneath the ice,
 463 major troughs submerged beneath the ice, major overdeepenings and substantial areas with ice below
 464 sea level (Figure 2C). This character of the southern South America subglacial topography has been
 465 noted before by Gourlet et al. (2016) for parts of the NPI and SPI but here we are able to produce a
 466 bed topography map with complete coverage across the whole area occupied by the Patagonian
 467 Icefields. The total area with ice beneath sea level is modelled to be contained with 73 zones

468 encompassing a total area of 655 km², with a mean elevation of -34 m ± 4 m and with a total volume
 469 of 91.5 km³ ± 18.3 km³. The five largest of these subglacial areas below sea level are each > 40 km²
 470 and each > 4 km³ and are beneath San Quintin and San Rafael on NPI, and beneath Jorge Montt,
 471 Occidental and Pio XI glaciers on the SPI. Other major glacier regions with bed elevations below
 472 zero are Gran Campo Nevado (total < 0.001 km³), Cordillera Darwin (total 0.4 km³), and Torres del
 473 Paine (total 0.05 km³).

474

475 The total area of glacier ice within subglacial enclosed topographic basins, or overdeepenings, which
 476 are prime locations for meltwater retention and thus which affect ice dynamics (Cook and Swift,
 477 2012) and represent possible (future) lakes, is modelled to be 1200 km². In total 282 individual
 478 overdeepenings are identified, with a mean depth of 38 m ± 4 m and a total volume (i.e. as if filled
 479 with water to the brim) of 101.7 km³ ± 20 km³. The five largest overdeepenings in terms of area and
 480 volume are all on the SPI on Jorge Montt, Occidental, O'Higgins, Viedma and Guilardi glaciers.
 481 These five overdeepenings each have a volume > 9 km³. Other major regions with overdeepenings
 482 are the NPI (total 9.75 km³), Gran Camp Nevado (0.065 km³), Cerro Erasmo (0.18 km³), Cerro
 483 Hudson (0.23 km³), Cordillera Darwin (5. 46 km³), El Condor (0.02 km³) and Estrecho de
 484 Magallanes (0.085 km²).

485

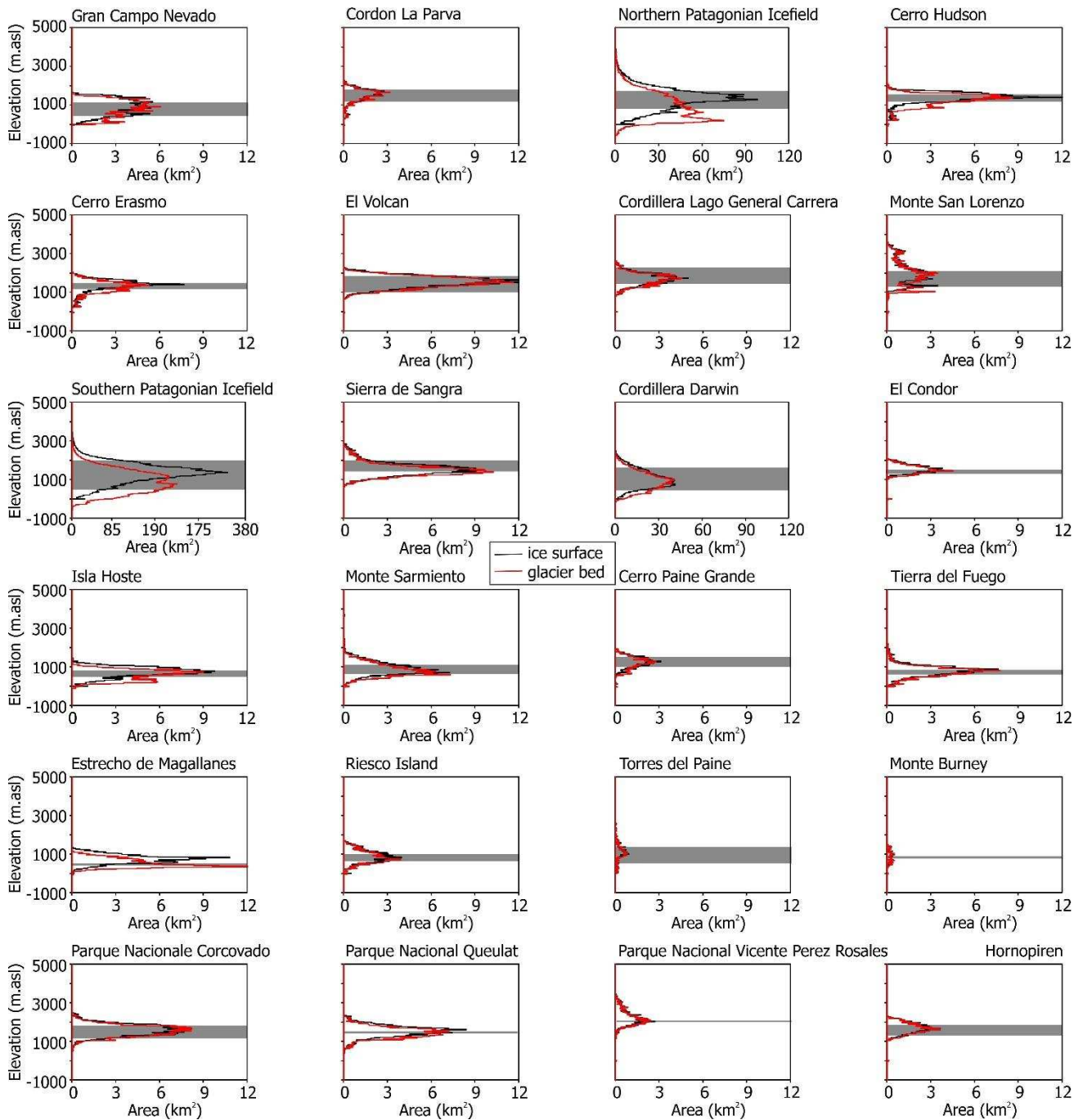
486 The maximum modelled depth of a single overdeepening is slightly > 400 m but the mean modelled
 487 depth of all overdeepenings is just 6.5 m. Overdeepenings with some part of their modelled depth >
 488 300 m are restricted to Steffen and San Rafael on the NPI and these are 12 km² and 22 km² in area,
 489 respectively, although several other (areally) larger though shallower overdeepenings occur in both
 490 glaciers and beneath other NPI glaciers. On the SPI Jorge Montt, O'Higgins, Pio XI, Viedma,
 491 Guilardi and Tyndall glaciers all have overdeepenings with some part of their modelled depths > 300
 492 m.

493

494 To consider potential future sea level rise (SLR) rather than total sea level equivalent (SLE), the
 495 volume of ice below sea level and potential lakes must be considered (c.f. Haeberli and Linsbauer,
 496 2013). We calculate the SLR of southern South America glaciers per major region (Table 1) and to a
 497 total of 14.71 mm ± 2.94 mm, which is 2.5 % less than the SLE. Ice below sea level accounted for 74
 498 % of this difference between SLE and SLR, and ice within overdeepenings, i.e. potential future
 499 lakes, accounted for 26 %.

500

501



502

503 **Figure 5.** Ice surface (black line) and bed (red line) hypsometry for all 24 major glacier regions in
 504 southern South America. Note x-axis is different for Southern Patagonian Icefield, Northern
 505 Patagonian Icefield and Cordillera Darwin. Grey horizontal bar represents range of ELAs as
 506 estimated from Hmed of each glacier.

507

508

509 The spatial variation in the difference between SLE and SLR across southern South America (Table
 510 1) is especially interesting because each region and indeed each individual glacier has a different
 511 climatic sensitivity / rates of recession (Davies and Glasser 2012; Gourlet et al. 2016). In a graphical
 512 manner the sensitivity to present climate and the consequences of possible future climatic changes
 513 (c.f. Raper and Braithwaite, 2009) on the glaciers of southern South America can be crudely

514 assessed. Glacier ice surface and subglacial bed elevation hypsometry is plotted per major region in
515 [Figure 5](#), together with the range of Hmed values for all glaciers in that region as a proxy for ELA.
516 Most pertinently, these graphs indicate that large amounts of ice in the NPI, SPI, and to a lesser
517 extent in Gran Campo Nevado, Cerro Hudson, Cordillera Darwin, Isla Hoste and Estrecho de
518 Magallanes regions already lies well below Hmed and thus depend for survival on replenishment via
519 ice flux from glacier accumulation areas. However, the glaciated area situated altitudinally above the
520 range of Hmed per major region is proportionally high ($> 20\%$ of all ice in the region) only for
521 Gran Campo Nevado, Monte San Lorenzo, El Condor, Isla Hoste, Tierra del Fuego, Estrecho de
522 Magallanes, Riesco Island, Monte Burney, Parque Nacional Queulat and Parque Nacional Vicente
523 Perez Rosales. These regions are all glaciers, ice caps and glaciated volcanoes outlying the major
524 (NPI and SPI) ice fields and the majority of them are in southern Patagonia. Clearly, a simple change
525 in ELA, such as a shift upwards in elevation by 100 m, will have dramatically spatially-differing
526 consequences for southern South America glaciers.

527

528 Analysis of the ice volume remaining within each major river catchment is an important concern for
529 water resources, including irrigation and hydropower, for example, especially given that southern
530 South America river flow records have exhibited a pronounced negative trend since the 1950s
531 (Masiokas et al., 2008). We find that only the Rio Chico and the Rio Santa Cruz catchments in
532 Argentina, and the Rio Chacabuco in Chile have modelled ice volumes $> 300 \text{ km}^3$ ([Figure 6](#)). The
533 Rio Deseado and the Rio Coyle catchments have modelled ice volumes $193 \text{ km}^3 \pm 38 \text{ km}^3$ and 181
534 $\text{km}^3 \pm 36 \text{ km}^3$, respectively, and a few other smaller catchments on the western side of the NPI and
535 on the western side of the SPI each have ice volumes within them of $< 100 \text{ km}^3$. The Rio Ibanez and
536 the Rio Simpson catchments in Chile have a modelled ice volume of $29 \text{ km}^3 \pm 6 \text{ km}^3$ and $24 \text{ km}^3 \pm 5$
537 km^3 , respectively. Except for a few small catchments at the southern end of the Cordillera Darwin
538 virtually all other river catchments across southern South America have modelled ice volumes < 10
539 km^3 ([Figure 6](#)). Where river catchments are large, but ice volumes are small and diminishing, river
540 flows must be progressively sustained by precipitation and any groundwater sources.

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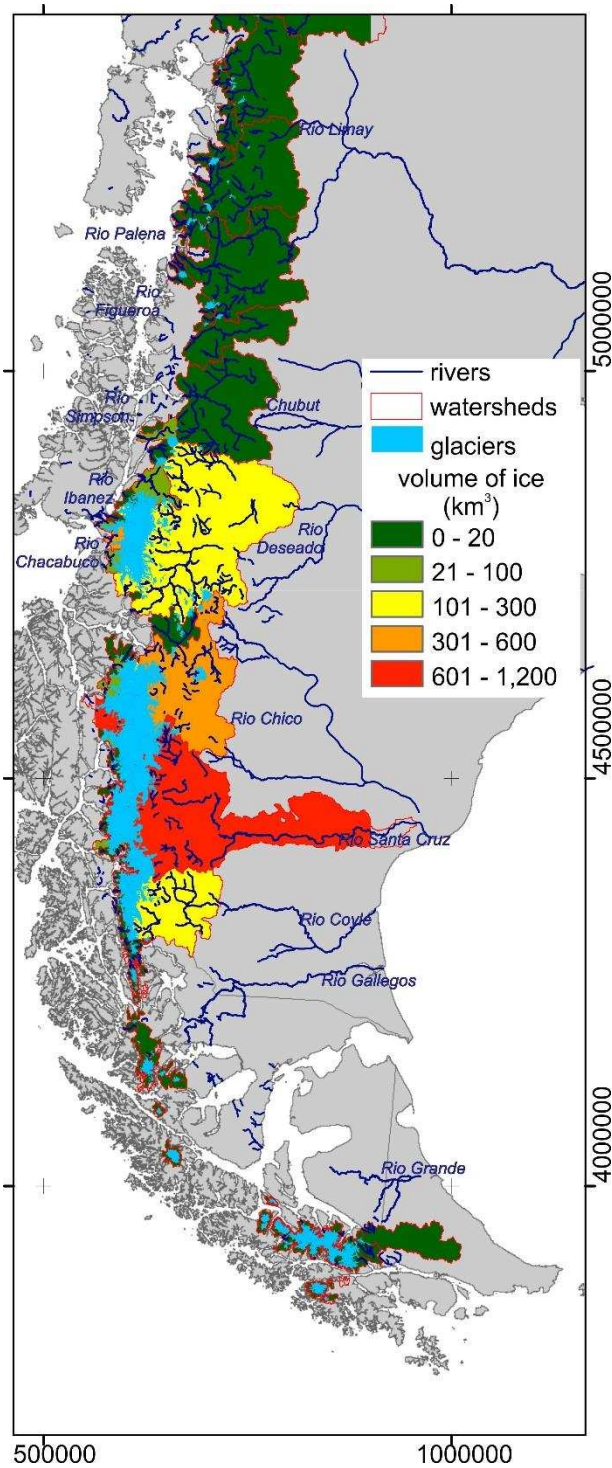


Figure 6. Total ice volume modelled for the major river catchments of Patagonia.

544

545 **Discussion**

546 **Regional total sea level contributions**

547 Huss and Farinotti (2012) used a physically-based approach to model ice thickness for Southern
 548 Andes glaciers ($n = 19,089$, area = $32,521 \text{ km}^2$) and reported a mean thickness of 205 m and a total
 549 volume $6,674 \pm 507 \text{ km}^3$. That mean thickness is slightly less than the mean thickness of 264 m

550 modelled in this study. Their total volume is 11 % more than our $5954.6 \text{ km}^3 \pm 1190.9 \text{ km}^3$, but both
 551 estimates agree within their respective uncertainty, and the uncertainty of the Huss and Farinotti
 552 model is ~ half that of our study. This suggests that whilst our study covers a smaller geographical
 553 region because it uses the World Glacier Inventory (WGI)-GLIMS outlines whereas Huss and
 554 Farinotti (2012) used the Randolph Glacier Inventory (RGI) outlines, it is apparently considering the
 555 vast majority of ice volume. Furthermore, Huss and Farinotti (2013) reported a SLE of 16.6 ± 1.3
 556 mm for Southern Andes glaciers, which can be compared to our $15.08 \text{ mm} \pm 3.01 \text{ mm}$ and to our
 557 SLR of $14.71 \text{ mm} \pm 2.9 \text{ mm}$. Furthermore, using Radic and Hock's (2011) projected SLE
 558 contributions of South American glaciers from 2000 to 2100 of 0.01 mm.yr^{-1} , we calculate those
 559 contributions would cause a reduction of 6.8 % of the total ice mass available over that time period.
 560 For interest, further comparison of Radic and Hock's estimates of SLE with that of Huss and
 561 Farinotti's and of the usage of the WGI-GLIMS glacier outlines versus those from the RGI has been
 562 explored further by Grinstead (2013).

563

564 SLE contributions from southern South America glaciers are accelerating. Rignot et al. (2003)
 565 reported rates of $0.042 \pm 0.002 \text{ mm.yr}^{-1}$ for 1968/1975 to 2000, but rates of $0.105 \pm 0.011 \text{ mm.yr}^{-1}$
 566 for 1995 to 2000. For the time period 2000 to 2012 Willis et al. (2012) reported SLE contributions
 567 from the SPI and the NPI combined of $0.067 \pm 0.004 \text{ mm.yr}^{-1}$. These rates over recent decades are an
 568 order of magnitude greater than that calculated over centennial scales since the Little Ice Age
 569 (Glasser et al., 2011: $0.0018 \text{ mm.yr}^{-1}$ from NPI since 1870, and $0.0034 \text{ mm.yr}^{-1}$ from SPI since 1650).
 570 The longer time to disappearance is produced using the most conservative SLE rate of Radic and
 571 Hock (2011), which is a process-based estimation, whereas the other shorter times to disappearance
 572 are simply via an extrapolation of modern rates and thus ignore probably future feedbacks between
 573 glacier mass balance and ice dynamics. The range of these published estimates of SLE highlight the
 574 need for future numerical modelling of southern South America glacier systems. The distributed ice
 575 thickness and bed topography datasets produced by this study will be very useful for this future
 576 modelling, and especially for examining any spatio-temporal variability in the response of glacier
 577 dynamics to climate change.

578

579 **Local topography and individual glacier dynamics**

580 Southern South America glacier changes in area and length since the Little Ice Age (LIA) have
 581 considerable spatial heterogeneity (Davies and Glasser, 2012) and likely will do so in the future too.
 582 Gourlet et al. (2016) recently discussed that local topography apparently exerts a much stronger
 583 control on glacier response variability across southern South America than regional climate gradients

584 (see regional ELA mapped in [SLA](#)). In this study we found it crucial to include nunataks in our
585 glacier outlines so as to delimit ice-free parts within glacier drainage basins to which ice thickness
586 should be interpolated to zero. Glaciers with termini that are retreating into overdeepened basins
587 such as Jorge Montt, Occidental, O'Higgins, Viedma and Guilardi, Steffen, Colonia and Tyndall,
588 could (i) store large amounts of meltwater subglacially with the potential for glacier outburst floods,
589 or 'jökulhlaups', and (ii) become lacustrine-terminating if not already with implications for ice
590 dynamics as well as for meltwater and sediment fluxes (Carrivick and Tweed, 2013; Loriaux and
591 Casassa, 2013). The numerous southern South America glaciers that presently terminate in the sea, a
592 tidal lagoon or a freshwater lake are subject to subaqueous melting and tidally-induced longitudinal
593 stresses (Truffer and Motyka, 2016). Our model poorly represents these tidewater glaciers due to
594 their floating termini. Glaciers with large zones of subglacial elevations below sea level will increase
595 in surface gradient and thus likely accelerate in velocity with ongoing terminus retreat.

596

597 Finally, whilst some southern South America glaciers are within semi-arid regions, many are located
598 in regions with steep topographic gradients and high precipitation rates and they have snow and firn
599 contributing to volumes (if determined geodetically) and accumulation enhanced by avalanching and
600 snow drift. Glaciers in these 'wet' conditions can be relatively insensitive to increasing air
601 temperatures, as has been modelled for Swiss glaciers (Huss and Fischer, 2016) and identified for an
602 Austrian glacier (Carrivick et al., 2015) and for glaciers in the Canadian Rockies (Debeer and Sharp,
603 2009). These spatio-temporal sensitivities of southern South America glaciers to air temperature and
604 to precipitation changes mean that projection of future hydrograph patterns per major river
605 catchment will need consideration of not only ice surface but also subglacial hypsometry, as
606 provided by this study, in relation to present and projected glacier ELAs.

607

608 **Conclusions and future work**

609 This first complete coverage of modelled distributed ice thickness, which we make freely available
610 as (i) an ArcGIS-format raster and (ii) a table of attributes per glacier (supplementary information)
611 across the whole of southern South America greatly extends in coverage and spatial detail the few
612 tens of available ice thickness point measurements in South America (Gärtner-Roer et al., 2014) and
613 the gravity measurements coverage of parts of the ice thickness of the NPI and SPI (Gourlet et al.,
614 2016). This first-order ice thickness modelling has in turn permitted modelling of bed topography
615 and of ice volume per glacier, per major glacier region and for southern South America in total. The
616 total ice volume of southern South America is $5955 \text{ km}^3 \pm 1191 \text{ km}^3$ and this volume equates to
617 $5458.3 \text{ Gt} \pm 1091.6 \text{ Gt}$ ice and to $15.08 \text{ mm} \pm 3.01 \text{ mm}$ sea level equivalent (SLE). Accounting for

618 bed elevations below sea level and overdeepenings that will likely store future meltwater, the
619 maximum potential sea level rise (SLR) from all southern South America glaciers is $14.71 \text{ mm} \pm 2.9$
620 mm. However, the rate at which individual glaciers will lose mass in the future depends on complex
621 feedbacks between glacier dynamics and local topography, glacier hypsometry and regional and
622 local ELAs and this study has produced those datasets.

623

624 Development of the estimates of ice thickness presented herein could focus firstly on derivation of
625 glacier flow lines rather than relying on relatively sparse centrelines, and should consider a routine
626 for better-representing floating glacier termini. Future studies could readily utilise the datasets
627 produced in this study in volume-area scaling (Bahr et al., 1997, 2014) and also volume-thickness
628 scaling and other area- and slope-dependant models (see Gärtner-Roer et al., 2014 for application of
629 these). In addition to V-A scaling, the parameters of altitude range-area, mean glacier thickness and
630 altitude range can be used for ice volume sensitivity analysis (c.f. Raper and Braithwaite, 2009),
631 although some consideration of mass balance gradient has yet to be worked out for all southern
632 South America glaciers. Future work on numerical process-based glacier mass balance modelling
633 will require distributed bed topography and ice thickness and is necessary to unravel the complex
634 feedbacks and process-links between glacier mass balance, glacier dynamics and tidewater and
635 lacustrine influences on glacier dynamics. The bed topography and especially the realisation of large
636 zones of subglacial elevations below sea level and the large zones of overdeepenings are important
637 for glacier or ice sheet models and for glacial isostatic adjustment models. They are also of concern
638 for potential future meltwater retention and thus for consideration of water resources and glacier
639 hazards.

640

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859 **Supplementary Information**

860

861 **Figure SI_A.** Glacier ELAs of the NPI (A), northern SPI (B) and southern SPI (C), highlighting
862 discrepancy that tends to increase southwards between ELA modelled 1970 to 1990 from zero degree
863 Celsius isotherm by Condom et al. (2007) and contemporary ELA as estimated by Hmed.

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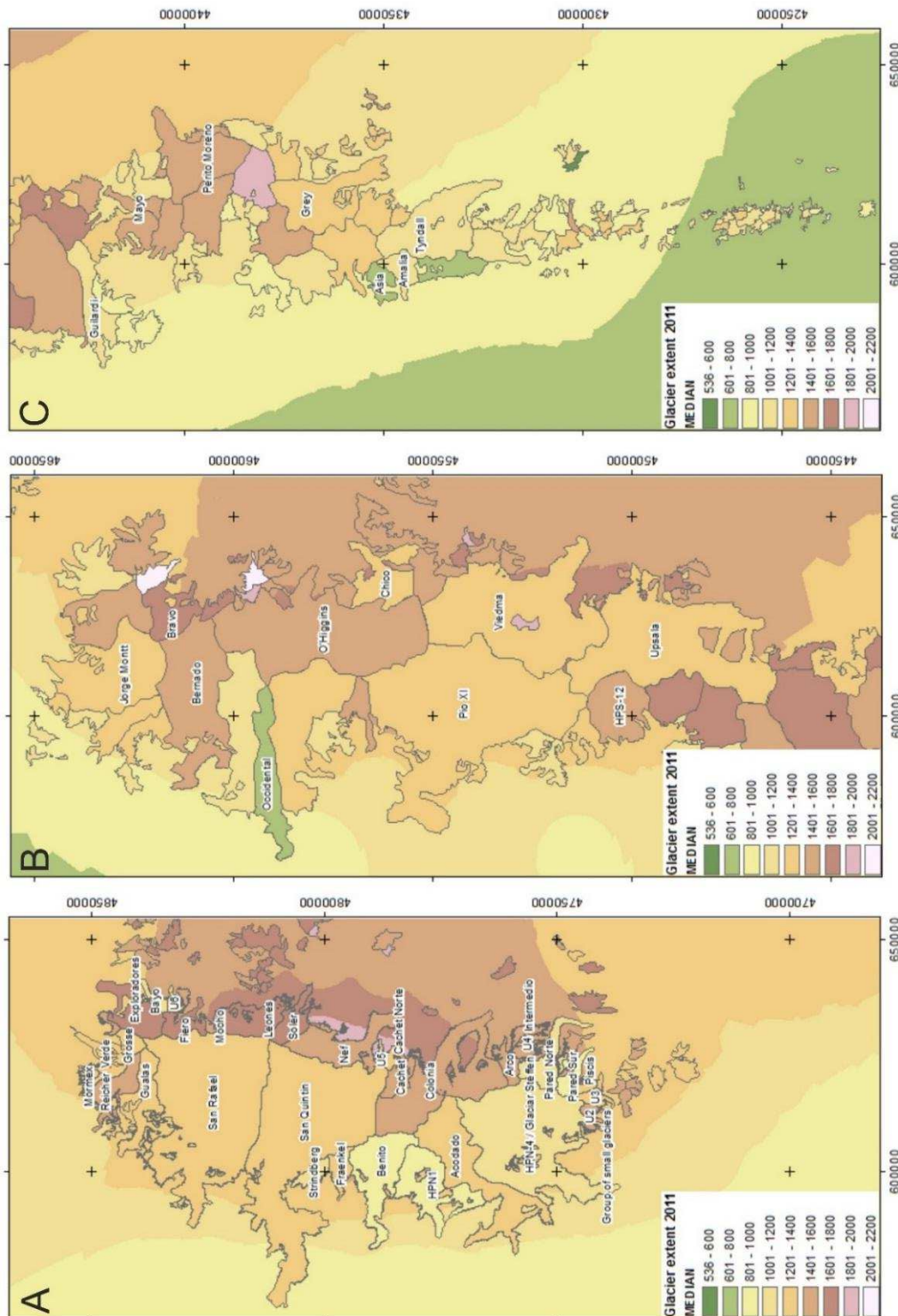
865 **Figure SI_B.** Subglacial bed elevation for NPI (A), northern SPI (B) and southern SPI (C) coloured
866 to emphasise those areas below sea level and major overdeepenings.

867

868 **SI_Table1.** Attributes of elevation, ELA, ice thickness and volume for 617 individual Patagonian
869 glaciers.

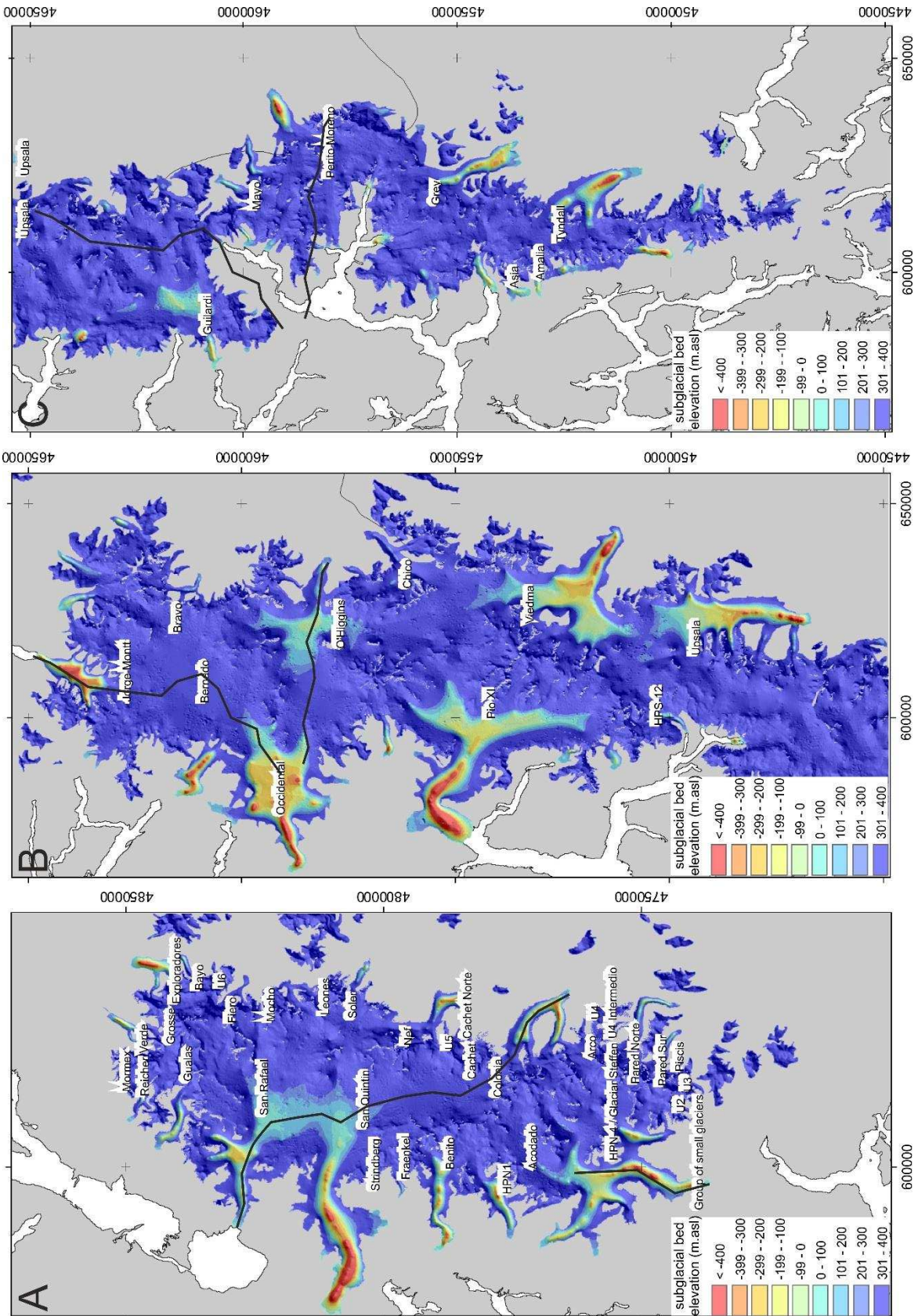
870

871 **SI_Dataset** Ice thickness ArcGIS format raster grid in UTM zone 18S projection.



872

873 **Figure SI_A.** Glacier ELAs of the NPI (A), northern SPI (B) and southern SPI (C), highlighting
 874 discrepancy that tends to increase southwards between ELA modelled 1970 to 1990 from zero degree
 875 Celsius isotherm by Condom et al. (2007) and contemporary ELA as estimated by Hmed. Thus the
 876 greater differences in colours between glaciers and the surrounding region, the more out of balance
 877 that glacier geometry might be interpreted to be with regional climate. Adjacent glaciers with
 878 differing Hmeds can be interpreted to represent differing response times as glaciers adjust to climate
 879 change due to local scale effects such as wind-blown snow inputs to mass balance, avalanching and
 880 topographic shading to direct shortwave radiation, for example.
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883 **Figure SI_B.** Subglacial bed elevation for NPI (A), northern SPI (B) and southern SPI (C) coloured
 884 to emphasise those areas below sea level and major overdeepenings. The black lines mark transects
 885 depicted in figure 4.