



# Agglomeration in counter-current spray drying towers. Part A: Particle growth and the effect of nozzle height



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## ABSTRACT

Agglomeration of particles and droplets is critical to the operation of spray dryers, however it remains relatively unexplored. This paper studies the effect of the nozzle height on product properties, wall deposits and dryer conditions in a counter-current spray drying tower of detergent with a swirling air flow. The process efficiency is driven by changes in particle agglomeration. To interpret the results and facilitate the study of swirl towers, it is useful to subdivide these units according to the sources of growth in (a) spray region(s), (b) concentrated near-wall region(s) and (c) wall deposits. The particles formed are very heterogeneous and show a size-dependent composition. In this case, particle properties are driven by the separation of solid and liquid phases during atomization and the formation of a heterogeneous set of droplets. Agglomeration serves to homogenise the product and create a distinct source of porosity. The capacity and energy consumption of the dryer are also determined by the evolution of the particle size, as fine powder is elutriated from the tower top and coarse particles are removed near the product. When the nozzle is moved to lower positions in the tower the increased temperature near the spray suppresses agglomeration, however the residence time is shortened and ultimately it leads to creation of wet, coarse granules. An optimum location is found high enough to maintain the drying efficiency but sufficiently far from the top exit to minimise the loss of fine particles. In this way, a capacity ratio (i.e. product vs spray dried powder)  $C > 90\%$  can be obtained and energy efficiency maximised.

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## 1. Introduction

Spray dryers are used to produce powders from the atomization of liquid feeds in dry hot air, where the volatile phases are removed. When droplets or particles come into contact they may stick to each other or the walls of the dryer and form agglomerates and deposits. These are rather poorly understood phenomena. Models often need to ignore the effect of particle contacts and concern only with a set of droplets as it is injected by a spray. However, agglomerates become bigger, lighter and non-spherical and disperse and dry in a very different way, which affects the dryer efficiency and the quality of the product. Understanding how and where agglomeration occurs is a challenge for many spray drying technologies [1,2] and the main pitfall of theoretical models [3–5] versus empirical approaches or the use of neural networks to try reproducing the complex net of relations between process conditions, drying rates [6] and deposition [7].

Formulating a theoretical model of agglomeration is complex because it needs to cover the entire particle history from atomization and coalescence [8,9] to the changes in the droplet surface [10–12]. Computational fluid dynamic models are very common to describe how the solids disperse and compute heat and mass transfer rates [13–16]. The particle-wall collisions are tracked to study deposition [17,18,19] and stochastic models are used to deal with impacts occurring in the air [20,21] and render the first descriptions of agglomeration in co-current devices [22–24]. The outcome of particle/droplet contacts was initially linked to the Ohnesorge number  $Oh^2$  (i.e. ratio of surface to viscous forces) in way to describe how a particle becomes less “sticky” as it dries [18,22,25]. But, in reality, the forces involved and the energy dissipated in an impact are complex functions of morphology. Recent work provides a neater account of the contact mechanics [26,27] and experimental collision charts [28], but it is yet to be applied in large frames.

Pilot or full scale experimentation is less frequent. Only few authors have related agglomeration to the operation conditions in co-current dryers or properties such as the glass transition temperature [29,30] in a way to delimit the areas where the particles grow [31,32]. No similar work is available for counter-current units or under the use of swirl. Swirl towers are typical of the production of thermally stable powders (e.g. detergents, ceramics) and in general, exhibit a higher level of

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agglomeration and wall deposition [33]. The counter-current flow leads to better energy efficiency but it makes the powder stagnate, which multiplies particle-particle contacts [5] particularly close to the walls where the swirl concentrates the solid phase [33]. The flow patterns are more complex and as a result the few models available [34,35] struggle to deal with accumulation, swirl stability [36] or fouling, and rarely mention the particle contacts [37]. Experimental works are scarce [38–40] and numerical tools rarely validated. The limited amount of data is due to known difficulties [41]: (a) costs and restricted access to production (b) complexity of gathering reliable and comprehensive data in full scale e.g. > 100 – 1000 m<sup>3</sup>, (c) multiple designs, (d) difficulty of sampling or installing probes inside a dryer, and so (e) difficulty in studying drying kinetics, agglomeration or fouling independently.

Every past attempt to study agglomeration during spray drying has looked into the contacts that occur in the air and associated the impacts to the walls only to the presence of deposits or some operational issues [42–44]. Recent work has made it imperative to reconsider this view and look at the wall deposition/resuspension dynamic as a key phenomenon. Clusters are seen to form, roll and break up at the walls of swirl counter-current towers of detergent [33] and tracer studies have demonstrated that the outer layers of the deposits are in fact continuously growing and breaking in an equilibrium that forms most of the coarse granules and drastically increases the residence time [45].

In summary, agglomeration during spray drying is not well understood, particularly in counter-current swirling flows where the role of the walls must be recognised. Huntington [5] listed some of the implications of particle growth during detergent manufacture. Swirl towers tend to maximise production whilst maintaining quality thresholds for the size and density of the spray dried product. As the rate increases, particles come into contact more frequently and the product becomes too coarse and wet. An appropriate number and location of sprays can minimise the number of particle contacts [5] but optimization is not possible without the ability to predict and control the agglomeration. In order to upgrade designs, reduce recirculation and better energy efficiency it is vital to understand where the most relevant contacts occur in a dryer and generate data to correlate the growth patterns to the configuration of sprays. To this purpose, two independent investigations have been carried out: (a) Part A, given here, provides a comprehensive examination of detergent production: it compartmentalises a swirl drying tower revisiting the list of particle contacts proposed by Huntington [5] in light of the new insights, and reports a series of experiments that link the position of a spray to the performance of the dryer in terms of capacity, efficiency and product quality, and (b) Part B is reported separately [46] and quantifies the interactions established when multiple spraying levels are used.

## 2. Experimental methods, tower subdivision and operation

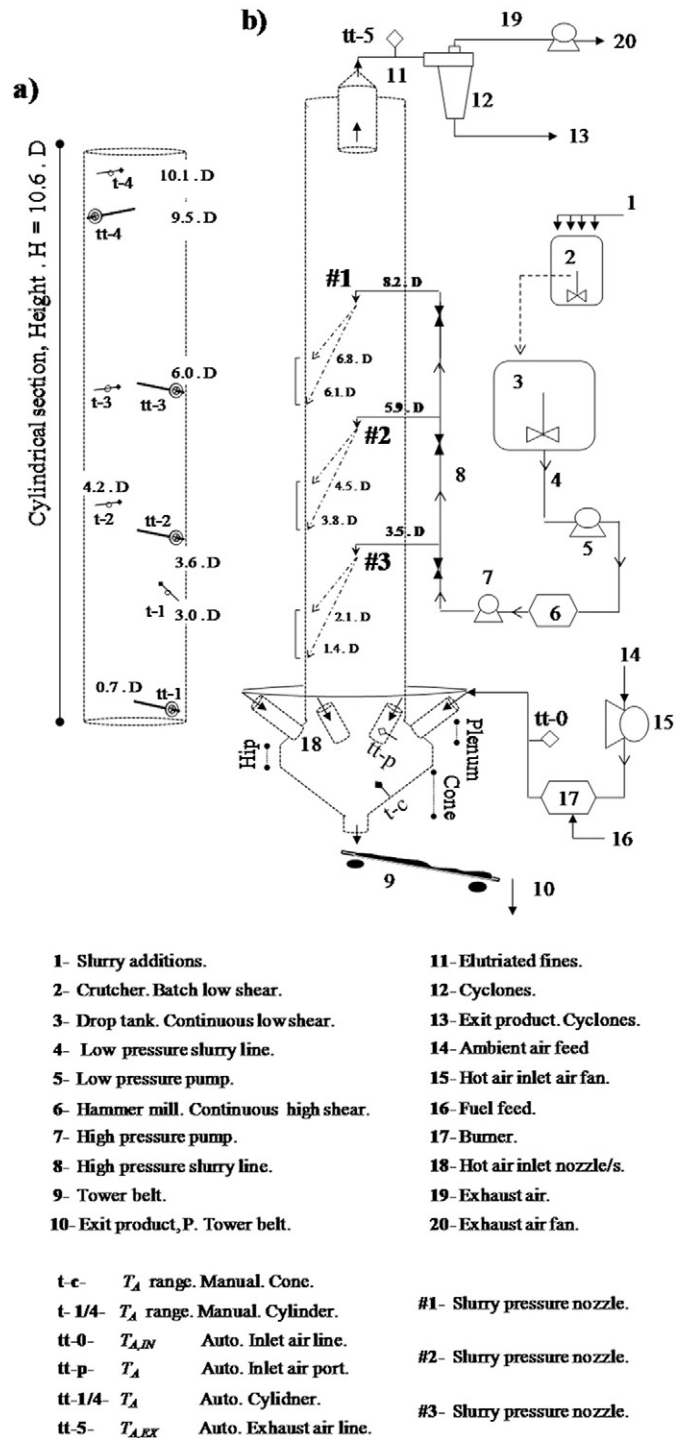
### 2.1. Unit design

A full scale counter-current swirl tower, property of Procter & Gamble was used to conduct the experiments. Table 1 and Fig. 1 describe the unit design and location of the nozzles used to atomize the slurry feed. A typical detergent formulation was used, containing aqueous and organic liquid phases obtained by addition of surfactant(s), polymer(s) and inorganic salt(s) to a solid content between 30 and 60% in mass. This slurry is prepared in a batch mixer, denoted '2' in Fig. 1, and fed to a homogenizer '3' for a continuous operation. It is pumped at low pressure '5' into a hammer mill '6' to break lumps and avoid blockages thereafter

**Table 1**  
Tower design parameters.

$d/D$	$H/D$	$\Omega_i$
0.29	10.58	5.1–5.4

\*  $\Omega_i$  initial swirl intensity [47].



**Fig. 1.** a) Location of temperature sensors, b) Design of a swirl counter-current dryer, location of spraying nozzles and projection on the wall (view of the thickness of a hollow spray).

and then it is brought to high pressure in '8' and delivered to a swirl pressure nozzle inside the unit. The same nozzle is used at all levels; it is placed at the centre of the chamber and faces down. Swirl pressure nozzles comprise of a swirl chamber where the feed is injected at high pressure followed by a tip with an outlet orifice; the swirling motion forms a thin slurry sheet at the outlet that breaks up as the flow exits atomizing the slurry into a hollow spray. Fig. 1 depicts the thickness of the hollow cone and its projection onto the walls. The reader is referred to Huntington [5] for a more detailed description.

Hot air is injected at the bottom of the chamber into the conical section, rises in the cylinder and exits from the top duct into a series of cyclones where the elutriated powder is collected. The alignment of the inlet air ports generates the swirling motion in the chamber, characterised by a strong anisotropy and periodical structures [47]. The majority of the product exits via the bottom of the tower and enters a transporting belt, after which the coarsest fractions are separated.

## 2.2. Measurement and instrumentation

The paste rheology was characterised with a cup and bob rheometer (TA Instruments Ltd. AR2000 ex) and the droplet size was examined with laser diffraction methods (Malvern Spraytec Particle Sizer, RTSizer 5.6) in an external rig that reproduces the atomization conditions set up in the dryer (i.e. temperature, pressure, rate, nozzle, slurry). Average droplet size distributions were obtained using several sprays from 1–2 s in duration and the spray angle was computed with image analysis.

Elutriation rates were measured by collecting the powder exiting the cyclones, denoted '13' in Fig. 1, and its size was analysed with laser diffraction (Sympatec GmbH HELOS/BR – Rodox, Lenses R2, R4 R7). Product was sampled at the exit of the belt '10' where an infrared probe (OMEGA OS551) measures the exit temperature. Ten consecutive ~1 kg samples were taken in ~30 min collecting the full stream, sealed, sampled down and sieved using the Taylor series. In the same period a bulk sample of 15–20 kg was collected blending consecutive samples. It was sealed and sieved in the next <4 h into 11 size classes (Russell Finex Model 17240). Each fraction was kept in a sealed container and later used for analysis of structure, porosity, and composition. Water and surfactant(s) contents, denoted  $X_w$  and  $X_s$ , were obtained with a Toledo Mettler Moisture Balance and analytical titrations ensuring errors <10% and 3% respectively for target values. The powder equilibrium relative humidity,  $erH$ , was measured with Rotronic HygroLab 3 (probes AW-DIO) and morphology examined under Scanning Electron Microscopy (Hitachi TM 1000). Particle intra-porosity  $\varepsilon$  was computed in each size fraction by measuring the absolute and envelope densities,  $\rho_{abs}$  and  $\rho_{env}$ , with He pycnometry (Micromeritics, AccuPyc II 1340) and Hg porosimetry (Micromeritics Autopore IV) respectively.

The deposits formed at the wall during periods of 10–15 min were photographed, collected and weighted to measure the initial net deposition rate,  $r_{d,o}$  [42] at several locations. The air temperature,  $T_A$ , was monitored at the inlet, tt-0, and exhaust air lines, tt-5. Inside the chamber,  $T_A$  was tracked using single K-type thermocouples that record the range of  $T_A$  in the radial direction either manually or automatically by placing thermocouples inside hollow metallic bars where individual openings expose each sensor to the air. The bars were aligned with the radius of the cylindrical chamber at four axial levels (Fig. 1). The bars were sufficiently far from the sprays to avoid any significant deposition or condensation [5]. These arrangements were validated against the exhaust probe tt-5 in the relevant range of temperature and humidity. The temperature of the wall of the chamber  $T_W$  was also monitored at the conical section to ensure the dryer is at a constant temperature before sampling is conducted i.e. constant heat loss  $Q_{Loss}$ .

## 2.3. Particle dynamics and tower subdivision

Fig. 2 depicts the initial trajectory (radial vs axial position) of different sized droplets to illustrate how the spray disperses according to numerical models, experimental deposition rates and the established experience in the field. In order to facilitate the design of experiments and model development, it is useful to subdivide a swirl tower into:

- 1- Wall region(s) - **WR**;
- 2- Nozzle region(s) - **NR**, comprised of:
  - Nozzle Inertial Region - **NIR**
  - Nozzle Terminal Region - **NTR**.

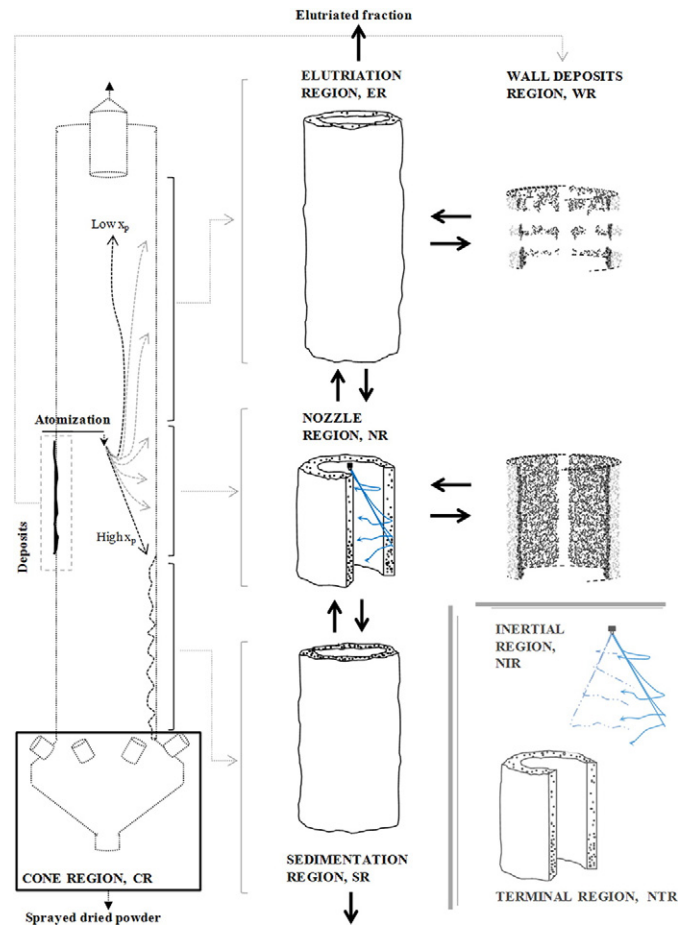


Fig. 2. Compartmentalization of a swirl counter-current dryer with a single central nozzle.

- 3- Sedimentation region(s) - **SR**;
- 4- Elutriation region(s) - **ER**; and
- 5- Cone region - **CR**.

The droplets and the hot air come into contact in the cylindrical chamber. The finest fractions are elutriated and depending on their response time, they either exit with the exhaust air or migrate to the walls at the top of the unit. Most of the powder becomes entrained in the swirling motion but it is sufficiently heavy to settle and flow down. Hassall [33] demonstrates that the cross-section of a swirl chamber has a sparse concentration of particles  $n$  apart from an outer ring close to the wall. One can focus in this region where most of the solid phase concentrates and dries. In a similar way to a cyclonic separator, the powder flows down swirling and colliding multiple times to the wall. The outer ring can be defined as the region where the solids move at terminal velocity  $U_{p,t}$  and thus simplify the formulation of kinetic models. It must be subdivided according to the nozzle position. In the areas above the nozzle and below the projection of the spray, ER and SR, particle-particle impacts occur at a low momentum simply due to different terminal velocities, but nearby the spray they involve also the wet droplets coming from the nozzle at much higher velocity. Therefore, in the nozzle region, one must distinguish two populations:

**NIR:** The inertial part of spray extends from the nozzle to the wall and contains the recently sprayed droplets whose motion depends on history. Approaching the wall, the drag decelerates droplets at different speeds depending on size and the particle history needs to be tracked in a momentum balance to preserve continuity [48]. Small droplets are quickly entrained in the swirl but large sizes barely modify their trajectory before colliding to the wall. Intermediate sized droplets become

partially entrained before reaching the wall (e.g.  $\sim 80\text{--}150\ \mu\text{m}$  droplets are expected to reach the wall above the nozzle level) but in this case (a central nozzle aligned down) most of the droplets are expected to collide the wall before reaching a terminal state e.g. the first impact for a  $400\ \mu\text{m}$  drop is estimated at  $\approx 10\ \text{m/s}$ .

**NTR:** A non-inertial population is concentrated close to the wall and free falls at a terminal velocity, exclusive function of local conditions, particle size and density. It comprises of the population of droplets that is fully entrained (smaller sizes) or that has already collided to the wall for the first time. It also includes a flow from ER and to a less extent SR. This work, Part A, focuses on a single spray so that the recirculation into the nozzle region is limited, but when multiple sprays are used the flow from lower or upper nozzle regions becomes a significant contributor to growth, Part B [46].

Finally, one must recognise the amount of material that is borne at the walls as a separate region, WR where the powder is fixed but remains subject to drying. Both WR and NR interact by rates of deposition and re-entrainment of material. Experimental quantification of the re-entrainment from the walls, identification of different erosion mechanisms and their effect in particle growth and residence time have been reported in a previous work [45].

#### 2.4. Operation and experimental set up

This paper studies the sources of agglomeration arising near the spray and how they respond to the position of the nozzle region NR in the chamber; Part B [46] studies how they are affected when two NR's are stacked. In this case, a central nozzle is moved from position #1 to #2 and #3 in Fig. 1 to modify the concentration and the heat exchanged in NR and cause more or less efficient contacts. Operation conditions are summarized in Table 2. The slurry rate  $M_s$  and atomization conditions (i.e. temperature and pressure) are kept constant. Inlet air temperature  $T_{A,IN}$  and mass rate  $M_A$  are also kept in a target value to dry the powder to an exit water content  $X_w$ , representative of industrial operation. In this way, the chamber develops the same range of superficial air velocity  $U_{av}$ , and one can associate the changes in the amount of elutriated powder  $M_E$ , the dryer energy efficiency  $\eta$  or the product properties to the way the dispersion of the solids is affected by the nozzle position.

**Table 2**  
Operation conditions as function of the nozzle position.

Scenario	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>
<i>Air phase</i>			
$M_A/M_{A,S_1}$	1.00 ± 0.01	1.00 ± 0.01	0.99 ± 0.01
$tt-0, T_{A,IN}$ (°C)	272.2 ± 2.1	273.0 ± 1.7	269.3 ± 2.3
$tt-5, T_{A,EX}$ (°C)	81.7 ± 0.5	86.8 ± 0.5	89.8 ± 1.7
$rH_{EX}$ (%)	20	17	14
<i>Particulate phase</i>			
Nozzle	#1	#2	#3
$M_s/M_{s,S_1}$	1.00 ± 0.02	1.00 ± 0.03	0.99 ± 0.01
$T_p - T_s$ (°C)	-4.7 ± 3.4	-1.4 ± 4.6	-2.5 ± 4.3
$X_w - X_{w,S_1}$ (%)	0	-0.69	4.5
$M_E$ (% $M_{EP}$ )	4.0	2.7	2.0
$M_R$ (% $M_{EP}$ )	8.5	5.3	27.0
C	0.875	0.920	0.710
<sup>a</sup> $U_{p,sd}$	>2–3 m/s	<sup>a</sup> $U_{p,w}$	>10 m/s

A: air, IN: inlet, EX: exhaust. S: slurry, P: powder at the exit belt, E: powder at the cyclones, R: powder removed as oversized, EP: full rate of spray dried powder.

<sup>a</sup> Sedimentation  $U_{p,sd}$  and initial wall impact velocity  $U_{p,w}$  for a droplet  $400\ \mu\text{m}$ .

### 3. Results and discussion

The following sections describe the operation (Section 3.1) the atomization of the slurry (Section 3.2), the temperature field in the dryer (Section 3.3) and the deposits associated to the spray (Section 3.4). Once the reader is clear on the characteristics of the initial set of droplets and the environment in the chamber, Sections 3.5 and 3.6 discuss the origin of agglomeration and the product size distributions and how different sources of growth could be considered in models based in the compartmentalization of the chamber. Finally, the consequences of agglomeration in the distribution of components across granules of different size and the generation of porosity are discussed (Sections 3.7 and 3.8).

#### 3.1. Elutriation and capacity

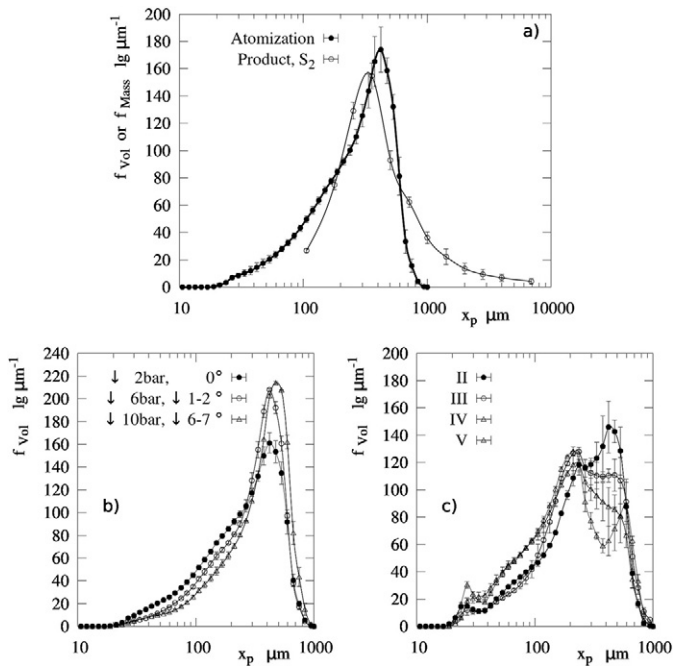
The capacity of the dryer is affected by the amount of powder discarded, which comprises of that considered too coarse, denoted  $M_R$  (i.e. computed here as the fraction  $x_{p>1800\ \mu\text{m}}$ ) and the powder collected in the cyclones, denoted  $M_E$ . The capacity ratio C given in Table 2 represents the usable fraction of the exit rate of spray dried powder  $M_{EP}$ . From a low nozzle position the fine powder flowing up (Fig. 2) has a longer time to migrate to the wall, concentrate and grow, which explains why the elutriation  $M_E$  reduces from 4.0% in S<sub>1</sub> to 2.7% and 2.0% in S<sub>2</sub> and S<sub>3</sub> (Table 2). This improves capacity in S<sub>2</sub> but when the nozzle is lowered to position #3 in S<sub>3</sub> the capacity ratio C drops again because of the formation of coarse granules that must be discarded and increase  $M_R$ . Notice how the capacity diminishes in S<sub>1</sub> because more powder is elutriated and in S<sub>3</sub> due to an excessive agglomeration.

#### 3.2. Atomization, ageing and solid-liquid separation

The detergent paste is strongly shear thinning, which facilitates atomization; the shear viscosity follows the power law  $\mu = 85.96 \cdot \dot{\gamma}^{-0.5634}$ . Fig. 3a compares the initial droplet size distribution to the product size in S<sub>2</sub>. The droplets show a wide distribution with a negative skew, a modal and median diameter  $x_{p,50}$  between  $390\text{--}425\ \mu\text{m}$  and  $275\text{--}310\ \mu\text{m}$  respectively;  $x_{p,50}$  and  $x_{p,90}$  are between  $77\text{--}98\ \mu\text{m}$  and  $521\text{--}549\ \mu\text{m}$ . The spray forms a hollow cone with a full angle of  $39 \pm 1^\circ$ .

Detergent slurries are complex fluids with several phases, air bubbles and suspended solids. The polymer(s) content and the surfactant(s) microstructure determine the water activity in each phase. As a result the slurry is subject to ageing and  $\mu$  can increase significantly during storage, leading to atomization of larger sizes. In a swirl pressure nozzle, a more viscous paste tends to generate a smaller air core at the tip, which thickens the slurry sheet and the size of the drops it breaks into [49]. Fig. 3b shows the effect of ageing during storage at a constant atomization rate. In order to determine the droplet size characteristic of these experiments (Fig. 3a) all measurements were taken at decreasing storage times until no variation was appreciated.

If the solids suspended in the slurry are large when compared with the slurry sheet formed at the tip, they can affect the breakup. Consider the limiting case of a paste containing mono-sized suspended solids. Only if the droplets formed were much larger than the solids could they have the average composition: if droplets were smaller than the solids, they must be comprised only of liquids and if they were comparable they may contain only a single solid or none. In essence, the liquid phases are excluded from droplets of a similar size to the solids in a paste. In practice, solids are poly-dispersed and the separation of phases depends to a balance between the energy input and the effect of viscosity and surface tension in the breakup of the sheet and the later contraction of ligaments into drops. Previous work on pneumatic and air dual nozzles give evidence of the effect of solid-liquid separation in droplet size. Solids  $>50\ \mu\text{m}$  are shown to govern the breakup in cases of low energy input and cause the segregation of solids and liquids into different droplet sizes [50]. The detergent paste used here contains much coarser

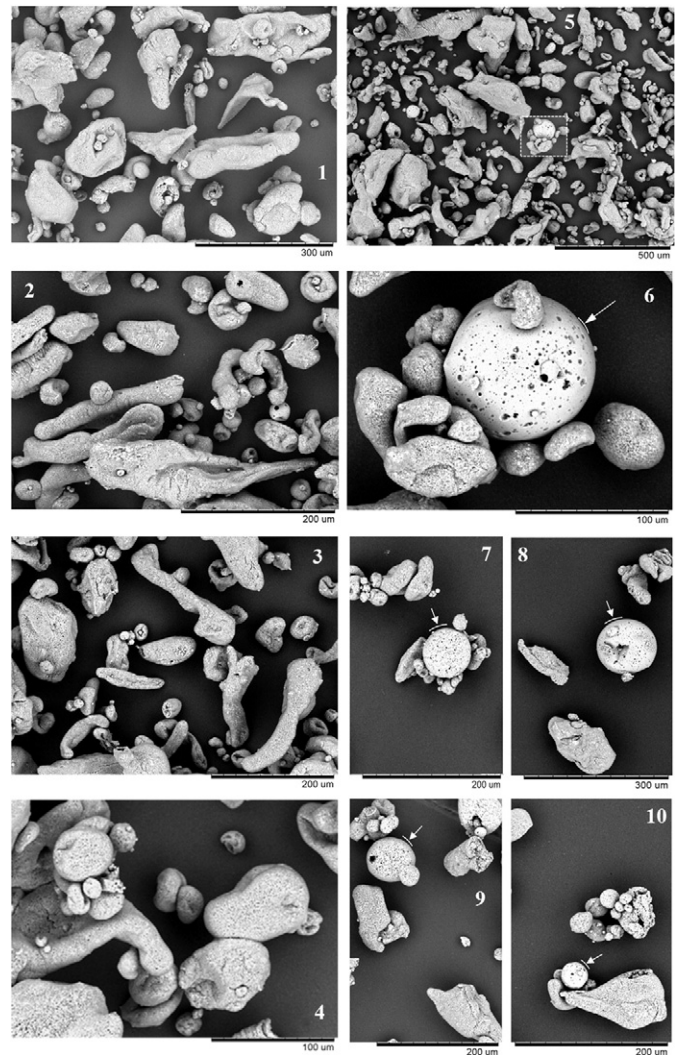


**Fig. 3.** Atomization. a) Droplet size vs product size  $S_2$ , Formula I. b) Effect of ageing in droplet size (increasing  $\mu$  and decreasing pressure) at constant rate. Formula I. c) Effect of phase separation in droplet size; bi-modal distributions at the same rate and nozzle for comparable detergents, formulas II, III, IV and V of decreasing  $\mu$ .

suspended solids ( $50\mu\text{m} < x_p < 200\mu\text{m}$ ), which appear larger than many of the droplets formed. In a similar way to the work of Mulhem [50], the exclusion of the solids leads to bi-modal size distributions when the energy input decreases sufficiently. Fig. 3c shows the atomization of comparable detergent formulas for decreasing  $\mu$  at the same nozzle and rate. As  $\mu$  and the energy input rise, both size modes begin to blend and approach the population used in this work (Fig. 3a). Here a second mode is no longer measurable but the phase separation is still significant.

The examination of the product confirms the uneven distribution of phases. Fig. 4 presents SEM micrographs of fine powder collected at the cyclones to illustrate the morphology of the droplets looking at single dry particles. They reveal a very heterogeneous nature; droplets contain many ligaments and a wide array of amorphous structures from elongated to planar shapes and small spherical drops. Figs. 4.4 to 4.10 show the presence of porous spheres of different colour and texture; the use of EDX (Energy dispersive X-Ray spectroscopy) serves as qualitative indicator of the origin of different structures e.g. the surface highlighted in Fig. 4.6 is linked to a higher content in inorganic salts than amorphous-like particles, which contain more carbon characteristic of the organic phases. Analysis of the powder composition provides further evidence: the smallest droplets contain more liquid phases such surfactant(s), and so the fraction of the product  $< 150\mu\text{m}$  presents 25–30% more surfactant(s) than the mode size; these difference are exacerbated in the elutriated powder to 33–34% in  $S_1$  and  $S_2$  and as much as 68% more in  $S_3$ .

The variation in droplet composition and structure complicates the system. Key properties such as the initial content in water, polymer(s), solid(s), surfactant(s) or the water diffusivity probably change for droplets of different sizes. It is clear that the content in solid(s) or surfactant(s) shall affect the mechanics of any contact, but perhaps the water activity remains a dominant factor for it defines how quick the surface dries turning stiff and less prone to agglomerate. The description of “stickiness” and its experimental characterization in drying matter is still an open area [51,52]. In this case only few components undergo transition through a glass state and key phenomena may include the evolution of surfactant(s) microstructures during drying, behaviour of polymers, crystallization processes or the effect that additives or changes

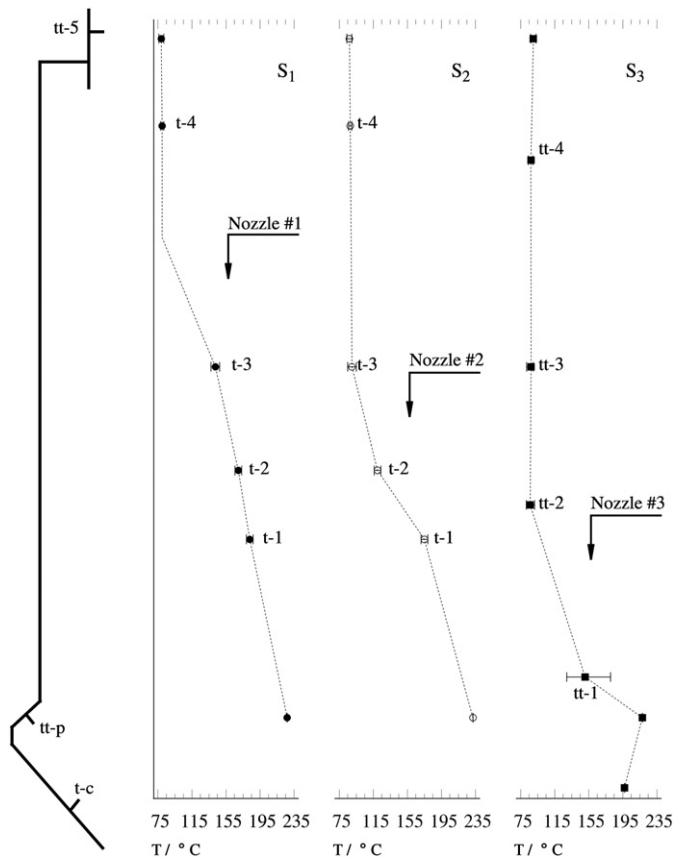


**Fig. 4.** Droplet morphology. Micrographs (1 to 4) show the presence of ligaments, small spherical drops and amorphous structures. Micrographs (6 to 10) show examples of rigid smooth particles associated to inorganic salts. Micrographs (1 to 6) correspond to  $S_2$  and (7 to 10) to the use of two nozzles in M<sub>13</sub> Part B [46].

in diffusivity may have in facilitating or impeding the formation of an outer crust when the droplets dry.

### 3.3. The drying environment

The axial profile of the air temperature  $T_A$  in the dryer is shown in Fig. 5.  $T_A$  decreases approaching the spray, after which it reaches the exhaust value,  $T_{A,EX}$ . A constant  $T_A$  indicates that the drying rate above the nozzle level must be minimal (i.e. note there is a low relative humidity and no air recirculation; thus drying must cause a noticeable decrease in  $T_A$ ). Table 3 presents the energy balance to the chamber, including the fraction of the heat exchanged between the phases  $Q_{EX}$  that is utilised in evaporation  $Q_{LAT}$  or in losses,  $Q_{LOSS}$ . All cases operate with large heat losses; for the most part they can be explained by the  $\Delta T$  between the air distributor (tt-0,  $T_{A,IN}$  in Table 2) and the plenum (tt-p in Fig. 5). The thermal efficiency,  $\eta_t$  [49] of a dryer is a common way to quantify the amount of energy transferred from the air, decreasing slightly from  $S_1$  to  $S_2$  and  $S_3$  (Table 3). However,  $\eta_t$  does not distinguish whether the energy is actually transferred to the solids or to the environment. In  $S_3$  the residence time of the powder is reduced and it becomes more difficult to convey the same amount of heat to the solid phase. As a result, the tower reaches higher temperatures and more heat is lost to the environment. This is better accounted for by the heat transfer efficiency  $\eta_h$  given



**Fig. 5.** Axial distribution of the air temperature,  $T_A$  as function of nozzle position.  $S_1$  (nozzle at  $z = 8.2 D$ ),  $S_2$  (nozzle at  $z = 5.9 D$ ),  $S_3$  (nozzle at  $z = 3.5 D$ ). Punctual measurements in t-1 to t-4 and cross-sectional average  $T_{A,av}$  in tt-1 to tt-4. Dimension of the cone not to scale.

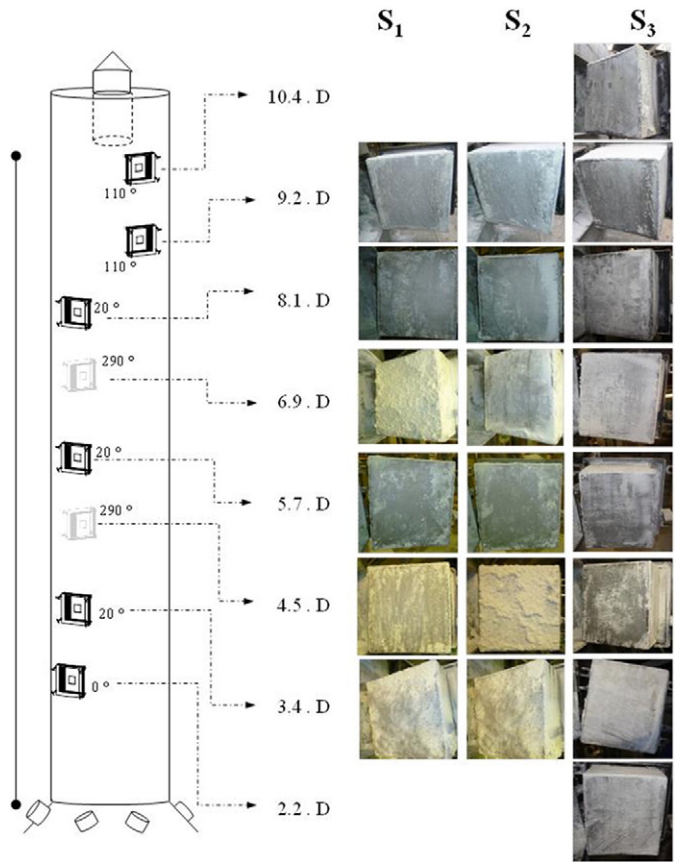
in Table 3 as the ratio of the inlet air enthalpy,  $H_{A,IN}$ , utilised in drying and heating the solids.  $\eta_h$  remains constant in  $S_1$  and  $S_2$  around  $\eta_h = 0.50$  and decreases significantly in  $S_3$  to 0.43, which means that one requires a much higher energy input to dry the product to the same level.

In a counter-current dryer it is not surprising to see most of the heat exchanged at the bottom where the temperature difference between the phases is the highest. However, the drying rate is also largely dependent on particle structure. Droplets initially shrink in a period dominated by external heat and mass transfer. Then formulas containing solids or crystalline structures [53] tend to form an outer crust that impedes the diffusion of water to the surface and the droplets start to heat up [12, 54]. Eventually they may reach the boiling temperature  $T_{Boil}$  and experience a sudden formation of vapour [55]. In this case, the water diffusivity drops from  $2.5 \cdot 10^{-10}$ – $5.5 \cdot 10^{-10} m^2/s$  at atomization to  $< 10^{-10} m^2/s$  as drying progresses, which ensures that the drying process in a mean size droplet becomes dominated by internal diffusion. However, it is the temperature history what determines whether it comes to boil. The saturation temperature  $T_{Boil}$  increases substantially as the particle dries, particularly when it reaches a low moisture content. Boiling tends to occur preferentially when wet large droplets are sprayed directly into areas of high  $T_A$  (i.e.  $S_3$ ) because a coarse size impedes diffusion and makes

**Table 3**  
Energy balance and energy efficiency.

Scenario	$S_1$	$S_2$	$S_3$
$Q_{Loss}$ (% $Q_{Ex}$ )	$34.8 \pm 1.3$	$31.3 \pm 1.1$	$40.6 \pm 0.5$
$Q_{Lat}$ (% $Q_{Ex}$ )	$65.2 \pm 1.3$	$68.7 \pm 1.1$	$59.4 \pm 0.5$
$\Delta H_{p,Sn}$ (% $Q_{Ex}$ )	$0.7 \pm 2.0$	$1.0 \pm 1.6$	$-1.5 \pm 0.9$
$\eta_t$	$0.76 \pm 0.01$	$0.74 \pm 0.01$	$0.72 \pm 0.02$
$\eta_h^a$	$0.50 \pm 0.02$	$0.51 \pm 0.02$	$0.43 \pm 0.01$

<sup>a</sup>  $\eta_h = Q_s/H_{A,IN}$  where  $Q_s$  is the rate of heat transferred to the solids.



**Fig. 6.** Inspection of the walls of the dryer and axial distribution of deposits.

heating faster, while high moisture reduces the boiling temperature. In contrast, when a large residence time  $\tau_p$  is spent in the cylinder (i.e.  $S_1$ ) the droplets dry progressively and  $T_{Boil}$  becomes too high before they face a high  $T_A$  at the bottom of the dryer. Given the high temperatures used in counter-current dryers, it is common to consider that the product reaches the boiling threshold. However this is not consistent with the evolution of the efficiency observed in Table 3. Under boiling one expects to see a correlation between  $T_p$  and  $X_w$  but in  $S_3$  the powder reaches the same temperature  $T_p$  at a higher water content  $X_w$  in Table 2. One must consider that the overall decrease in the drying efficiency when moving the nozzle down in  $S_3$  (Table 3) is simply proportional to a reduction in residence time  $\tau_p$  and relatively insensitive to the temperature faced by the solids.

### 3.4. Wall deposits

The inspection areas and the examination of the deposits are summarized in Fig. 6. The initial deposition rates are given in Table 4 as an indication of the rate of impacts to the wall. The highest rates are associated to the area of the spray projection (i.e.  $6.9 D$  and  $4.5 D$  from positions #1 and #2) where the droplets are still wet and collide the wall at high velocity. Here, thick wet deposits appear and remain subject to drying at relatively low temperatures. The amount of deposits increases when the nozzle is moved down from  $S_1$  to  $S_2$  due to the increasing air velocity at the bottom of the chamber and the concentration of more solids. The counter-flow and the swirl are responsible of deposition fluxes  $\sim 10$ – $30$  times higher than in co-current devices [42,43]. In  $S_3$  no deposition is appreciated at  $2.2 D$ . The inspection area lies near the projection from the spray from nozzle #3 (see Fig. 1) but the higher air velocities at the tower bottom are likely to shift the trajectories of the droplets up. The presence of deposits above the nozzle supports the dispersion pattern shown in Fig. 2 and demonstrates that part

**Table 4**

Initial net deposition rate  $r_{d,o}$ , as a function of nozzle position. Bold denotes the spray projection area.

Level	$S_1$	$S_2$	$S_3$
$z/D$		$g/s\ m^2$	
10.4	–	–	0
9.2	0	0	0
8.1	0	0.04	0
6.9	<b>0.91</b>	0.02	0.04
5.7	0	0	0
4.5	0	<b>1.81</b>	0
3.4	0	0	0.02
2.2	–	–	<b>0.01</b>

of the spray is elutriated up and then migrates to the wall at the top. As the nozzle approaches the top in  $S_1$ , the spray is located close enough to the exit for all the fines to be elutriated and the deposition above the nozzle becomes negligible.

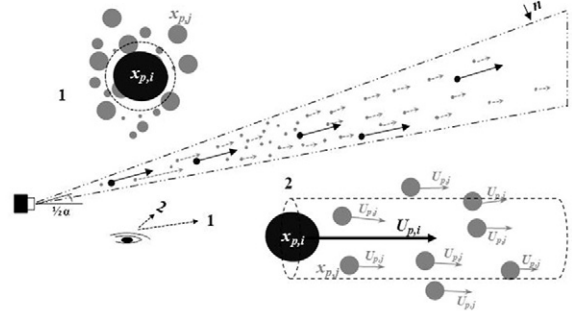
### 3.5. Sources of agglomeration and growth patterns

Huntington [5] lists different types of contacts depending on the drying stage of the particles, namely, -i- droplet/droplet contacts near a nozzle or -ii- when several sprays overlap, -iii- droplet/particle contacts and -iv- semi-dried/semi-dried contacts resulting from different terminal velocities. Contacts of the type -ii- occur only in towers where multiple nozzles are placed at the same level and are not considered here. The remaining are the result of air-borne collisions and their location and likelihood in a chamber can be anticipated. The growth above the spray,  $ER$  (Fig. 2), is necessarily limited; it is due to the stagnation of fines near the wall (i.e. responsible of deposits at the top of the dryer in Fig. 6) and it involves contacts at low relative velocity ( $<1\ m/s$ ) and moderate water content  $X_w$  because the elutriated powder dries rapidly above the nozzle (i.e.  $T_A$  remains constant in Fig. 5). In the region below the spray projection,  $SR$  (Fig. 2) the concentration increases and particle-particle contacts occur at higher velocity due to differences in size ( $<2\ m/s$ ), but as soon as the solids move down they enter a region of higher air temperature  $T_A$  and are likely to form an outer crust and turn non-deformable, which makes the contacts inefficient. Below the cylinder, in  $CR$  (Fig. 2) growth is likely to be negligible because the surface of the particles is already dry.

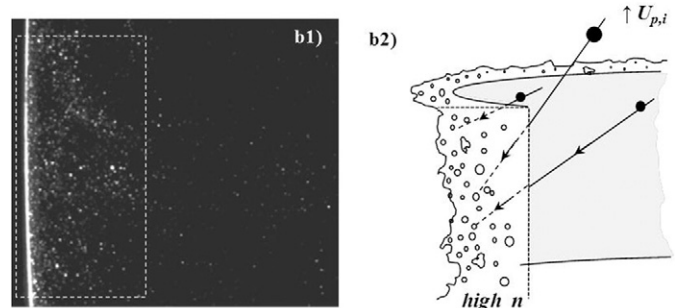
In the same way that the contacts to the wall are most efficient nearby the sprays, the particle-particle interactions occurring within the nozzle region  $NR$  are also the most likely to result in agglomeration: they involve the collisions at the highest momentum carried from the spray, when the surface of the droplets and particles remains wet and when at least one of the colliding partners is still deformable. Three sources of growth are illustrated in Fig. 7:

- **Coalescence in  $NIR$ .** Droplet-droplet contacts (i.e. contact -i- by Huntington [5]) occur at high relative velocities within the spray ( $<20\ m/s$ ). Fig. 7a shows how large droplets, less affected by drag, pick up smaller sizes that decelerate faster and concentrate. Coalescence and rates of collision are estimated from the diameter, concentration and velocity of both partners [48], and become significant only near the nozzle because the spray dilutes rapidly outwards.
- **Interaction between  $NIR$ - $NTR$ .** Droplets at high velocity do not concentrate sufficiently far from the nozzle to coalesce, but when reaching the walls they cruise across an annular region with a high concentration  $n$  of drier powder, depicted in Fig. 7b. In this area the spray comes into contact with harder granules (i.e. contact -iii- by Huntington [5]) comprised of (a) wet material recently sprayed, (b) drier clusters re-entrained from the deposits [33] and (c) fine powder that was dispersed upwards and came back down close to the wall (see Fig. 2). The contacts occur at a high relative velocity and deformability and so

### a) Coalescence and scrubbing effect in $NIR$



### b) Interaction between $NIR$ and $NTR$



### c) Wall deposition and re-entrainment

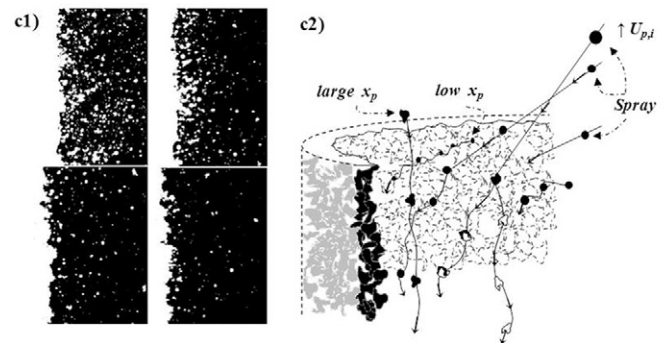


Fig. 7. Depiction of agglomeration sources in a nozzle region  $NR$  resulting from (a) coalescence (b) impacts due to stagnation within the spray projection in  $NTR$  (c) deposition and re-entrainment of clusters in  $WR$ . The Particle Image Velocimetry PIV images are reproduced from Hassall [33].

the amount of solids stagnated in  $NTR$  must be a vital contributor to agglomeration.

- **Wall-borne growth sources:** Within the spray projection, the impacts to the wall include high velocity wet droplets and drier and smaller particles at low inertia (see Fig. 7c). For decades, deposits were believed to be never re-suspended or detach only as large pieces [5], but as a matter of fact all sizes are involved in the deposition / re-entrainment cycle [45]. The difference between the size of the droplets deposited and the clusters re-entrained represents a net rate of growth at the wall, which responds to how the outer layer ages and breaks up due to drag, gravity and impacts. As a passing note, it can be argued that the high velocity drops that pick up particles close to the wall in Fig. 7b will in essence end up depositing in Fig. 7c. Subsequently, the properties of the clusters re-entrained later must be function of how the layer breaks rather than of the contacts before deposition. In this case, one could simplify Fig. 2 and merge  $WR$  and  $NTR$  into a boundary-layer approach similar to the work in cyclones [56], so that

one could describe a large dryer using a 3D flow model to determine how the spray disperses into *NTR* + *WR* and a 1D kinetic growth model thereafter.

The evolution of the product size is given in Fig. 8. The droplet size distribution in Fig. 3a and the product size distributions in Fig. 8 exhibit the same single size mode i.e. 300–425  $\mu\text{m}$  [57], but the product is clearly comprised of agglomerates, which evidence that such coarse droplets have either deposited or grown further. The statistics are given in Table 5. Mean values do not reflect well the change in the tail, which is key to understand the evolution of capacity (Table 2), energy efficiency (Table 3) and many aspects of performance e.g. packing factor, density, or solubility. When the nozzle operates from a high location,  $S_1$ , the agglomeration generates the mode size and a shoulder into 600–850  $\mu\text{m}$ . When the spray moves down in  $S_2$ , the production of granules into the shoulder reduces and the mode narrows. The suppression of agglomeration can be explained by the reduction in the efficiency of the particle contacts: the spray faces a higher air temperature  $T_A$  in the nozzle region and so the outer crust of the droplets is produced earlier and the surface becomes less prone to stick, which may reduce the level of coalescence in *NIR*, Fig. 7a.

One observes the same effect in the transition to a lower position in  $S_3$ : the shoulder eventually vanishes and the mode keeps on narrowing, but in turn a different source of agglomerates appears forming a plateau in the size distribution  $> 850 \mu\text{m}$ . This phenomenon must be linked to the higher concentration expected near the walls in *NTR*, and a stronger interaction with the deposits in *WR*. When the spray is brought down one enhances the heat transfer close to the nozzle because it faces higher temperatures but in turn the *NR* is located in areas of higher velocity. It is possible that the transition into forming a plateau corresponds to the point where the counter airflow starts to be strong enough to accumulate a significant amount of powder in *NTR*. If more solids stand in the projection of the spray they will multiply the contacts between high velocity droplets and stagnated powder, Fig. 7b, and ultimately the wall, Fig. 7c. Production of agglomerates in this range of size points to interactions occurring at the outer layer of the deposits, which are responsible of most of the agglomerates shown in Fig. 8  $> 850 \mu\text{m}$  in  $S_2$  (detailed quantification of the resuspended material during  $S_2$  is given in [45]).

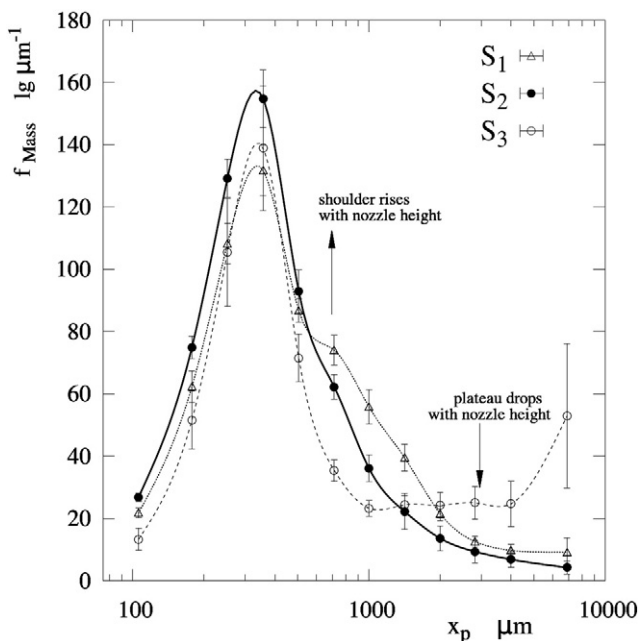


Fig. 8. Product size distribution as a function of the nozzle height:  $S_1$  (nozzle at  $z = 8.2D$ ),  $S_2$  (nozzle at  $z = 5.9D$ ),  $S_3$  (nozzle at  $z = 3.5D$ ) [57].

Table 5

Mass based product size distributions. Confidence intervals provide one standard deviation.

Scenario	$S_1$	$S_2$	$S_3$
$x_{p,10}, \mu\text{m}$	$173 \pm 4$	$161 \pm 3$	$195 \pm 12$
$x_{p,25}, \mu\text{m}$	$261 \pm 7$	$238 \pm 5$	$282 \pm 20$
$x_{p,50}, \mu\text{m}$	$413 \pm 15$	$360 \pm 10$	$456 \pm 98$
$x_{p,75}, \mu\text{m}$	$824 \pm 64$	$597 \pm 53$	$2224 \pm 1575$
$x_{p,90}, \mu\text{m}$	$1724 \pm 286$	$1168 \pm 232$	$x_{p,83} = 4760 \mu\text{m}$

$S_1$ ,  $S_2$  and  $S_3$  were conducted under initially cleaned walls, but the coverage and thickness of the deposits can affect the structure and turbulence of the air flow [58]. For that reason  $S_1$  was compared to an exact replicate obtained when the dryer initially showed a heavily built up wall, denoted  $S_{1-r}$  (for details see [58]). Both productions were indistinguishable in terms of efficiency and product size and composition, which suggests that once the operation progresses sufficiently and the deposits achieve a steady state thickness, the disruption to the flow became comparable.

### 3.6. Compartmentalization of swirl towers

The variety of particle contacts in a dryer complicates enormously the formulation of models. The mechanisms shown in Fig. 7 represent the main growth kinetics in a swirl tower. Eulerian-Lagrangian models are the most common in this context, but they face important challenges in a large vortex: (a) computational expense, (b) issues in tracking particle dispersion when anisotropy and swirl stability are important, and (c) enough resolution (i.e. parcel numbers/size bins) to track accurately the accumulation of wide particle size distributions or in large devices. The treatment of agglomeration is also computationally expensive and different contact mechanics can only be dealt with by increasing complexity. In turn, Eulerian-Eulerian modelling frames are unnecessarily complicated for a spray [48] but can easily deal with industrial scales. The theoretical subdivision proposed here (Fig. 2) facilitates the development of a large kinetic frame for a dryer. A similar approach to Tan [59] can serve to construct a compartmental model and discriminate the different type of contact associated to each region in Fig. 2. Tan rewrites the aggregation rate kernel in fluidised bed melt granulation as the product of a collision rate (fluid dynamics driven) and the probability of the collisions to result in growth, or collision efficiency (particle property driven). As opposed to a fluidised bed, in a dryer one expects the functional form of the rate of collisions to vary from the nozzle inertial region *NIR* (Fig. 2) where motion is dominated by the spray momentum, to the rest of the chamber where sedimentation kernels may be applicable [60–62]. The collision efficiency varies from one to another region as a function of the water content of the particles. It must change from coalescence in the spray, *NIR* (Fig. 7a) to a capture efficiency in the interaction between *NIR* and the nozzle terminal region *NTR* (Fig. 7b) or contacts between semidried droplets at different stage in *NTR*, *ER* or *SR* (Fig. 2). At the wall deposits *WR* (Fig. 7c), the outcome of particle impacts could be computed in terms of a deposition efficiency and a resuspension probability, which ultimately describes how particles grow at the walls due to the different size of the droplets deposited and the agglomerates resuspended [45].

A full resolution is very complex but this type of frame opens the way to multi-scale approaches. One can start to tailor experiments and micro-scale models to study how the rate and the efficiency of collisions in each region depend on the process conditions, and how the different regions interact, for instance by the flow to and from the walls *WR* [45] or through the placement of several nozzles [46]. In this way, a large kinetic frame may be constructed connecting standard models only for the most relevant regions using the same architecture but with different operation conditions.



### 3.7. Redistribution of active component(s) and particle drying history

The droplet composition varies as a function of size; thus the composition and the drying history of the agglomerates depend on the size of the droplets that formed them. Figs. 9 and 10 show respectively the content in surfactant(s)  $X_S$  and water  $X_W$  as function of particle size. As explained before, liquid phases such as water and surfactant(s) distribute preferentially in small droplets, and thus the finest powder contains more surfactant(s), see Fig. 9. Larger particles start to include droplets rich in solids (poor in liquids) and so they reach a minimum content in surfactant(s) and water in Figs. 9 and 10. Only when the agglomerates become sufficiently coarse to contain many primary particles they tend to show an average surfactant(s) content  $X_S$  in Fig. 9. In essence, the agglomeration of droplets of different composition serves to redistribute the surfactant(s) and homogenises the powder. The phase separation is neater in  $S_3$  because the mode size contains fewer agglomerates and more primary particles (i.e. droplets that did not agglomerate). The surfactant(s) content  $X_S$  at the mode size decreases by 17% in  $S_3$ . The lower content for particles  $<850 \mu\text{m}$  evidence that less of the surfactant(s) contained in fine droplets have agglomerated into coarse fractions. In contrast, as soon as the plateau starts to form in the size distribution shown in at Fig. 8 for granules  $>850 \mu\text{m}$ ,  $X_S$  recovers in Fig. 9. This correlation is a revealing fact: it supports the different origin suspected for the granules at the mode or the plateau i.e. lowering the nozzle in  $S_3$  causes simultaneously the suppression of growth into the agglomerates  $<850 \mu\text{m}$  (likely due to less efficient contacts within the spray) and the promotion into coarser sizes (likely due to a higher concentration in NTR and interactions at the wall WR).

The distribution of the water content  $X_W$ , given in Fig. 10 responds to the relation between particle size and residence time.  $X_W$  rises significantly for coarse granules because they settle faster and have a higher volume/surface ratio. It is useful to compare the evolution of  $X_W$  and the size distributions. Lowering the nozzle reduces the particle growth from  $S_1$  to  $S_2$  in Fig. 8 which allows drying the product further in Fig. 10. In  $S_3$  the agglomeration in the mode and shoulder keeps on reducing but the powder does not reach the same final water content because it has a lower residence time, which is only exacerbated for coarser granules. Therefore, one must associate the loss in drying efficiency ( $S_3$ , Table 3) not only to formation of the plateau but to a too low nozzle position.

Interestingly the powder  $<150 \mu\text{m}$  in  $S_1$  and  $S_2$  and  $<355 \mu\text{m}$  in  $S_3$  also exits with a higher water content. Smaller droplets contain more water due to the phase separation and fragments worn off the deposits [45]

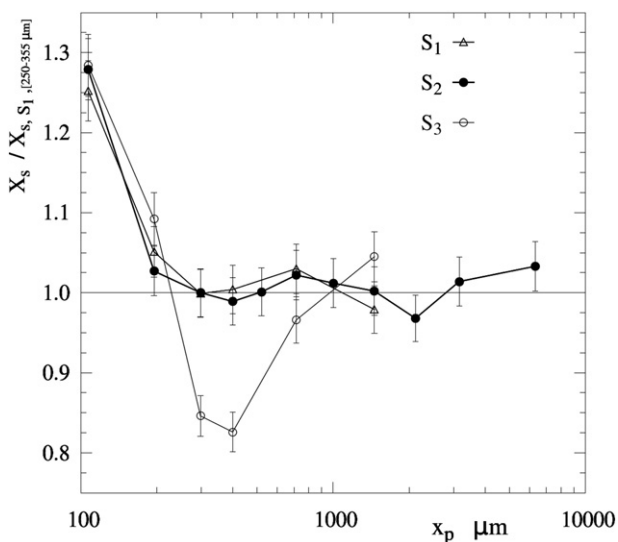


Fig. 9. Surfactant(s) content in the product,  $X_S$ , as function of the particle size, normalised to value of the mode size class in  $S_1$ .

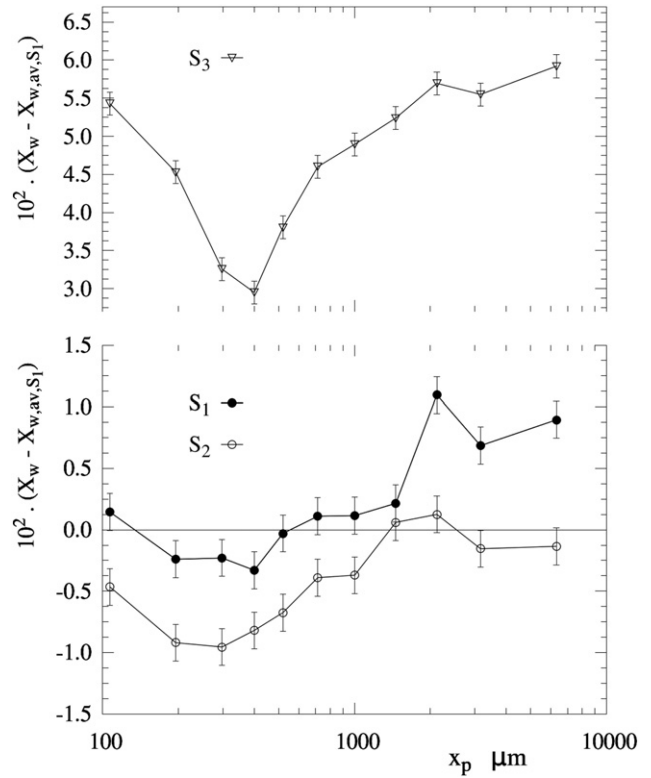


Fig. 10. Water content in the product,  $X_W$ , as function of particle size. Differences to the average value in  $S_1$ .

but the powder  $<150 \mu\text{m}$  would have dried rapidly faced to high temperatures at the bottom of the dryer. Fine particles do not experience a lower residence time in the chamber, nor do they exhibit a different drying isotherm. Fig. 11 showcases a typical relation between water content  $X_W$  and powder equilibrium relative humidity  $erH$  for this powder including several other productions of the same formula from nozzle #1 and nozzles #1 and #3 [63]. The exception to the trend is the powder elutriated, which does not undergo rapid drying rates at the top of the dryer and shows different porosity. Equilibration during sieving (1–4h) or the transport across the tower belt in Fig. 1 could be responsible for the absorption of water into the small particles, but not to the extent

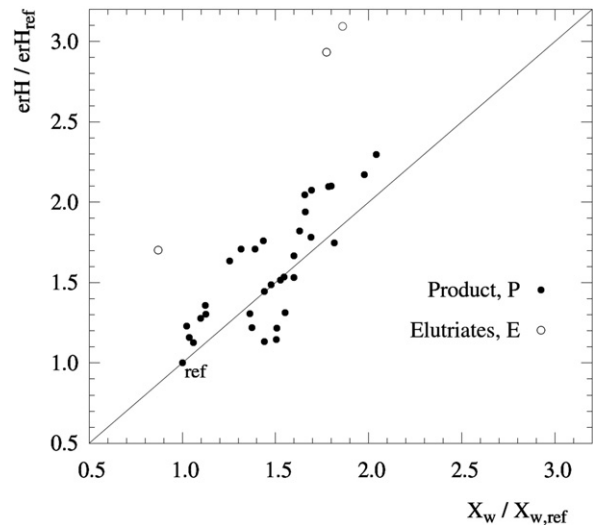
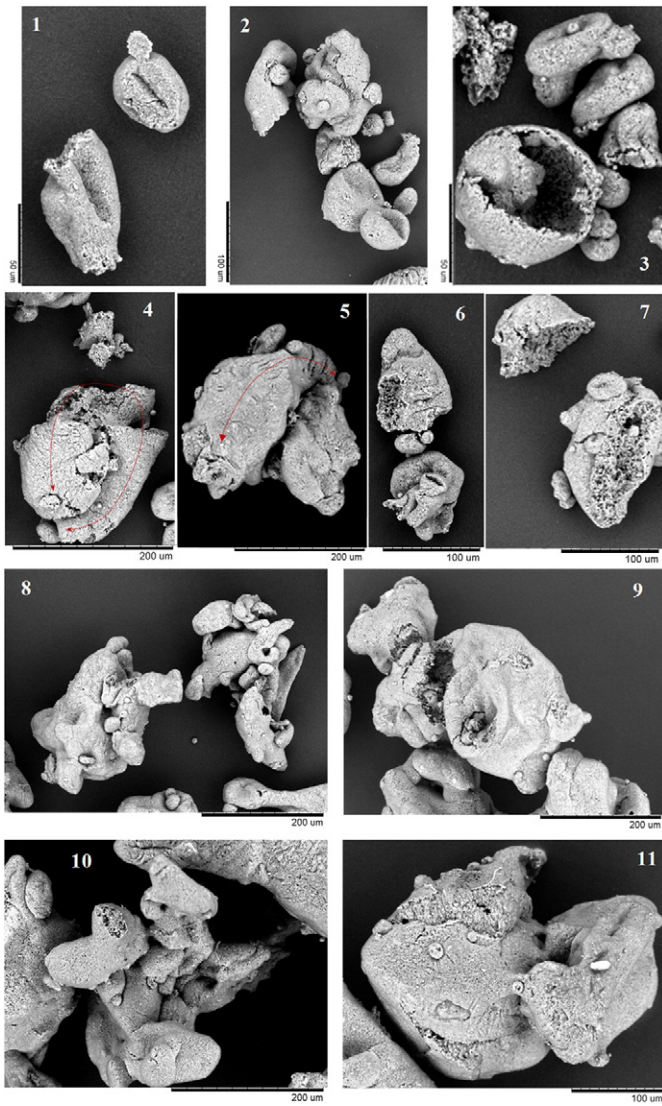


Fig. 11. Correlation of the powder water content  $X_W$  to the equilibrium relative humidity  $erH$  (20–25 °C) normalised to a reference point. Samples cover all particle size classes in the product and the elutriated powder for several productions of this formulation with single ( $S_{1-r}$ ,  $M_{1-r}$  [63]) and multiple nozzles ( $M_{13-r}$  [63]).



**Fig. 12.** Particle structure resulting from drying. SEM micrographs show examples of collapsed droplets (1,2), hollow particles (3), coiled ligaments (4,5) and common porous particles (6,7). Micrographs (8 to 11) show examples of the contacts and the solid bridges established in the agglomerates.

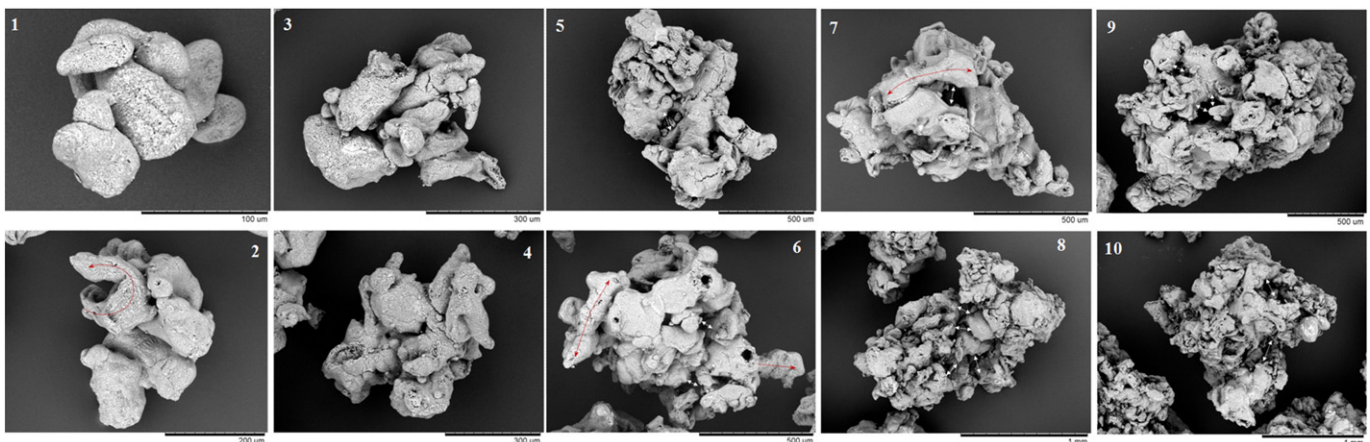
observed in Fig. 10. The moisture of the finest fractions must respond to attrition of fragile granules close to the exit where the full stream of powder comes together. The presence of fragments is consistent with the analysis of the morphology and explains why the finest fraction contains less surfactant(s) than the elutriated powder.

### 3.8. Generation of structure and density

#### 3.8.1. Morphology

The structure of primary droplets/particles (i.e. droplets that did not undergo agglomeration) is determined by the drying history and the response to boiling. After a crust is formed, droplets stop shrinking and can follow different evolutions. Earlier works describe how concentration gradients [64] or receding water interfaces [65] develop and more recently include populations of pores [66,67] and the migration of solids to the surface [12]. In every case, after a crust appears drying increases porosity up to a maximum given by the volume of water displaced unless vapour is formed. In this case, the rise in pressure may be relieved by bubbles bursting out (i.e. leaving behind cavities but no further porosity) or by the inflation of the drop (i.e. increasing porosity beyond the displacement of water) in a process referred to as “puffing” and often pointed at in detergent [68]. The inflation depends on the properties of the crust. Most authors assume them a priori, but Handscomb and Kraft [12] describe the limiting cases: (a) a crust that is inelastic: a bubble forms at the core and the solids migrate to the surface, forming a hollow particle that may or nor burst but remains un-inflated, (b) a crust that is elastic but losses elasticity when it dries: the particle inflates and after cooling it retains its shape showing an increased porosity (i.e. “puffing”) or (c) a crust that is elastic: the particle inflates when it boils but after cooling it collapses. Since the primary droplets show large differences in composition, many of these structures appear in the product. Fig. 4 shows a variety of ligaments and amorphous structures including spherical particles rich in salts. Fig. 12 includes examples of collapsed drops (Figs. 12-1, 12-2), hollow spheres (Fig. 12-3), coiled ligaments (Figs. 12-4, 12-5) and the common porous matrices revealed through bursts and broken sections (Figs. 12-6, 12-7).

The vast majority of the powder is in the form of complex shaped aggregates and it is unclear how they might respond to boiling. Fig. 12 shows typical solid bridges between the primary particles (Figs. 12-8 to 12-11), which must be formed either by diffusion at a long contact time (perhaps at the wall) or after drying of viscous bridges established at impact [2]. Most particles and bridges show a porous interior and a hollow core (Fig. 12-9), but no evidence of inflation or collapse, which



**Fig. 13.** Morphology of the agglomerates. Micrograph (1) shows the fraction  $150 \mu\text{m} < x_p < 250 \mu\text{m}$ ; (2) to  $250 \mu\text{m} < x_p < 350 \mu\text{m}$ ; (3,4) to  $450 \mu\text{m} < x_p < 600 \mu\text{m}$ ; (5) to  $600 \mu\text{m} < x_p < 850 \mu\text{m}$ ; (6,7,8) to  $850 \mu\text{m} < x_p < 1180 \mu\text{m}$ ; (9,10) to  $1180 \mu\text{m} < x_p < 1800 \mu\text{m}$ . The presence of surface cavities and embedded ligaments are highlighted in some of the micrographs.

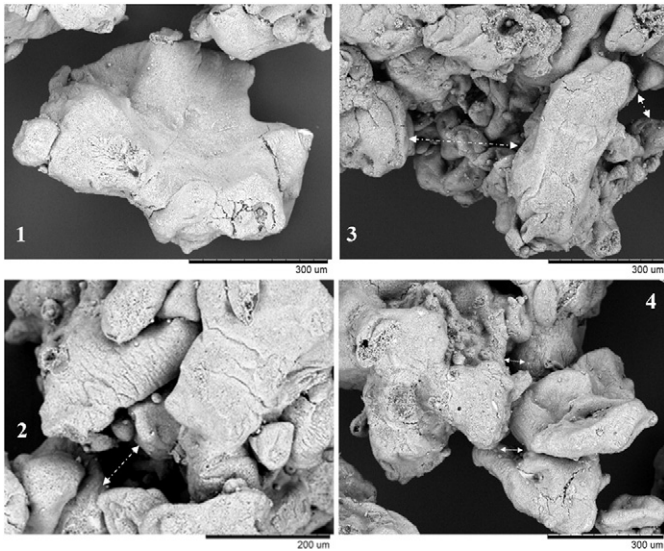


Fig. 14. Sources of porosity. Cracks, bursts and pores in the surface of primary particles and surface cavities due to agglomeration.

suggests that the crust must remain inelastic through the drying process. The agglomerates themselves evolve from grapelike structures at the finest fractions (e.g. Figs. 13-1, 13-4) to very complex shapes for large sizes (Figs. 13-5 to 13-10) in part because the primary droplets are deformable and elongated and in part due to the way ligaments appear embedded in the structure (e.g. Figs. 12-4, 12-5, 13-2, 13-5, 13-6). Large agglomerates show high aspect ratios and wide surface cavities larger than the primary particles that form them (e.g. Figs. 13-5 to 13-10). Supplementary material describing in more detail the structure of the powder in  $S_2$  is available elsewhere [63].

Two sources of porosity are easily identified in the product and illustrated in Fig. 14: one associated to agglomeration whereby the surface shows wide cavities that lead into an open structure, and another at the surface of each primary particle, where small pores and bursts lead through a porous crust into the interior. Fig. 14 includes details at a higher magnification to illustrate the porous nature of primary particles and evidence of surface pores, bursts and cracks. These features are clearly different from the cavities originated by the agglomeration.

### 3.8.2. Porosity

The porosimetry analysis reveals the characteristic pore sizes and highlights the effect of the surface cavities in reducing the particle density. Table 6 reports porosity  $\varepsilon$  and density as function of the particle size for  $S_2$ . The values given for  $\varepsilon_{abs}$  represent the volume contained in pores/cavities smaller than a threshold set according to the powder examination and conservative criteria ( $\varepsilon$  under-predicted). The threshold differentiates pores and cavities (e.g. intra-particle porosity) from inter-particle voids in the intrusion cycle of Hg porosimetry shown in Fig. 15. The use of narrow size classes causes a poor packing in the sample and makes inter-particle voids large so that they are filled first and appear as a pick in the right hand side of the graphs. The threshold is clear in small particles (e.g. Fig. 15b and d) and becomes more obscure for larger granules when the pores/cavities start to be comparable to inter-particle voids (e.g. Fig. 15c). In the coarsest fractions the entire volume shown in Fig. 15a corresponds to surface cavities and pores. Two clear maxima are visible, one leading to wide cavities between  $60.5 \mu\text{m} < x_{pore} < 90.7 \mu\text{m}$  and clearly associated to the effect of agglomeration, and another to micron-pores near  $0.8 \mu\text{m}$  and due to drying. The porosity attributable to micron-pores  $x_{pore} < 9 \mu\text{m}$  ranges between  $\varepsilon_{abs} = 23\text{--}27\%$  across the entire product, and decreases only for the granules  $> 2500 \mu\text{m}$  to  $\varepsilon_{abs} = 15\%$  for pores  $x_{pore} < 20 \mu\text{m}$ . The micron-size or “drying” pores appear at the same size range for the finest particles and the coarsest

Table 6

Particle density and porosity. Bulk, envelope and skeletal densities,  $\rho_{bulk}$ ,  $\rho_{env}$  and  $\rho_{ske}$  (see nomenclature) and the porosity between the thresholds for the envelope to the absolute density,  $\varepsilon_{abs}$  and between the envelope and skeletal density,  $\varepsilon_{ske}$ .

Size class, $\mu\text{m}$	Single nozzle operation, $S_2$					
	$\text{kg/m}^3$				%	
	$\rho_{bulk}$	$\rho_{env}$	$\rho_{ske}$	$\rho_{abs}$	$\varepsilon_{ske}$	$\varepsilon_{abs}$
Elutriated	0.67	0.97 <sup>1</sup>	1.79	1.76	45	45
<152	0.67	0.92 <sup>2</sup>	1.55	1.78	41	48
152–250	0.68	1.33 <sup>2</sup>	1.79	1.89	26	30
250–355	0.61	1.26 <sup>3</sup>	1.68	1.92	25	35
355–450	a	a	a	1.93	a	a
450–600	0.56	1.20 <sup>4</sup>	1.77	1.93	32	38
600–850	0.61	1.18 <sup>4</sup>	1.69	1.91	30	38
850–1180	0.69	1.11 <sup>4</sup>	1.56	1.92	29	42
1180–1800	0.88	1.17 <sup>4</sup>	1.69	1.93	31	39
1800–2500	0.81	1.14 <sup>4</sup>	1.62	1.91	30	40
2500–4000	1.15	1.31 <sup>4</sup>	2.01	1.91	35	31
>4000	1.04	1.11 <sup>4</sup>	1.94	1.89	43	41
<b>Average</b>	<b>~0.67</b>	<b>~1.19</b>	<b>~1.71</b>	<b>~1.90</b>	<b>~30</b>	<b>~37</b>

<sup>1,2,3,4</sup> Refer respectively to a pore threshold size to inter-particle cavities of 30.2, 33.0, 60.5, 90.7  $\mu\text{m}$ .

<sup>a</sup> Samples showing reproducibility issues.

agglomerates (compare Fig. 15a and b), which supports the presence of fragments described earlier. In turn, the elutriated powder, Fig. 15d, exhibits no similar micron pores very likely because it does not undergo such rapid drying rates at the top of the dryer.

In every case the porosity  $\varepsilon$  is lower than the volume of water displaced from the droplets, and so there is no evidence that inflation during boiling is a dominant way to generate porosity. In contrast, the porosity due to drying can be justified by the formation of an inelastic crust. The morphology of the powder and the contribution of large cavities to porosity indicate that the agglomeration must be considered an important contributor to the reduction of density, particularly in fractions  $> 850 \mu\text{m}$ . Furthermore, notice that the values of  $\varepsilon_{abs}$  reported for the coarsest granules represent an underprediction of the porosity because the agglomerates start to contain cavities too wide to be measured (i.e. the bulk density  $\rho_{bulk}$  is computed at  $x_{pore} < 353 \mu\text{m}$ , and starts to increase in Table 6 for fractions  $x_p > 850 \mu\text{m}$ ).

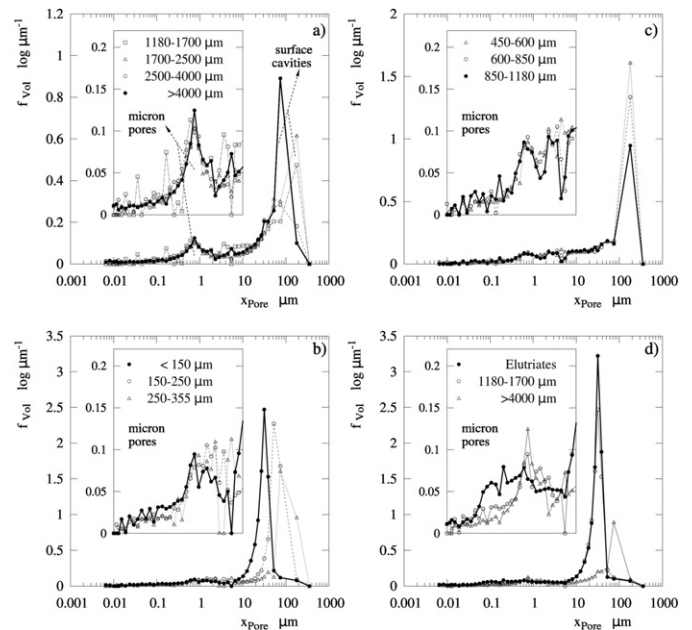


Fig. 15. Pore size distributions in the product for  $S_2$  (nozzle at  $z = 5.9 D$ ). Intrusion curves of Hg as function of particle size a)  $x_p > 1180 \mu\text{m}$ , b)  $x_p < 355 \mu\text{m}$ , c)  $450 \mu\text{m} < x_p < 1180 \mu\text{m}$ , d) comparison of elutriated powder and coarse fractions.

#### 4. Conclusions

- a) **Agglomeration, operation and efficiency:** In a swirl tower with a single detergent spray the drying rate above the nozzle level are negligible due to minimal recirculation of powder; most of the heat is exchanged at the bottom and below the cylindrical chamber. Wall deposits are caused by direct projection of the sprays and the elutriated powder that migrates to the wall at the top of the dryer. High nozzle positions generate wide product size distributions and promote the elutriation of powder, reducing capacity. Bringing the nozzle down inhibits the agglomeration into the mode size and narrows the distribution. Eventually, the residence time of the product reduces excessively and the nozzle enters areas of higher concentration, which causes insufficient drying and formation of coarse granules  $>850 \mu\text{m}$ . The drying efficiency  $\eta_h$  reduces from 0.50 to 0.43 and the excessive agglomeration makes capacity to drop from a maximum of 0.920 to 0.710. An optimum location is sufficiently far from the top to allow the fine powder to migrate to the walls and away from the bottom to maintain a sufficient residence time for the product to dry.
- b) **Composition heterogeneity and structure:** The atomization of detergents is prone to the separation of solid and liquid phases, which results in a size dependent distribution of water and active components in the product. The droplets exhibit a heterogeneous structure and contain many ligaments. In majority, the resulting powder comprises of non-spherical granules with high aspect ratios. Primary particles are bounded by solid bridges and form large cavities superimposed to micron pores due to drying. For this formulation no evidence suggests that droplet inflation is a dominant way to reduce density. Porosity is due to micron-sized pores due to drying ( $\varepsilon < 27\%$  across different size classes) and to the contribution of cavities formed during the agglomeration (up to  $\varepsilon > 25\%$  for the coarsest granules).
- c) **Compartmentalization and future work:** According to these observations and recent studies of fouling [45] a new compartmentalization has been proposed to help studying swirl drying towers. It is based in the recognition of the different sources of growth established within (a) the spray, (b) the near wall region in the spray projection (c) and the cycle of deposition/resuspension of material at the wall. This theoretical frame and the experimental data reported here can help in the extraction of growth kinetics and the development of future kinetic models for a drying tower.

#### Nomenclature

$A$	Cross-sectional area of the cylindrical chamber, $\text{m}^2$
$C$	Capacity ratio $C = 1 - ((M_E + M_R) / M_{EP})$ , —
$D$	Diameter of the cylindrical chamber, $\text{m}$
$d$	Diameter of the top exit in the dryer, tubular guard, $\text{m}$
$erH$	Equilibrium relative humidity of the product, %
$f$	Normalised size frequency in a probability density function Given in volume or mass base, $\log(\mu\text{m})^{-1}$
$H_A$	Enthalpy rate for the air phase taking ambient temperature as a reference, $\text{J s}^{-1}$
$\Delta H_{DA,sn}$	Enthalpy variation between outlet and inlet air in a dry basis, $\text{J s}^{-1}$
$\Delta H_{P,sn}$	Enthalpy variation between the outlet product, elutriates and water vapour and the inlet slurry, $\text{J s}^{-1}$
$M$	Mass rate, $\text{kg s}^{-1}$
$M_S$	Mass rate of slurry sprayed at the nozzle, $\text{kg s}^{-1}$
$M_E$	Mass rate of powder elutriated and collected at the cyclones, $\text{kg s}^{-1}$
$M_R$	Mass rate of oversized product exiting the tower belt, $\text{kg s}^{-1}$

$M_P$	Mass rate of the product exiting the tower belt, $\text{kg s}^{-1}$
$M_{EP}$	Overall rate of powder exiting the spray drying chamber, $\text{kg s}^{-1}$
$n$	Particle number concentration, $\text{m}^{-3}$
$Oh^2$	Ohnesorge number, $Oh^2 = 2\mu_p^2 / x_p \rho_p \sigma_p$
$Q_{Lat}$	Latent enthalpy rate of the water vapour generated in the chamber, $\text{J s}^{-1}$
$Q_{Loss}$	Rate of heat lost to the environment, $\text{J s}^{-1}$
$Q_{Ex}$	Rate of heat exchanged in the dryer $Q_{Ex} = Q_{Lat} + Q_{Loss} = -(\Delta H_{DA,sn} + \Delta H_{P,sn})$ , $\text{J s}^{-1}$
$Q_S$	Rate of heat transferred to the solid phase $Q_S = -(\Delta H_{DA,sn} + Q_{Loss}) = Q_{Lat} + \Delta H_{P,sn}$ , $\text{J s}^{-1}$
$r_{d,o}$	Initial net wall deposition rate, $\text{g s}^{-1} \text{m}^{-2}$
$rH$	Relative humidity of the air phase, %
$T$	Time averaged temperature, $^\circ\text{C}$
$T_{A,av}$	Cross-sectional average air temperature, $T_{A,av} = \int \rho_A U_{A,z} T_A dA / \int \rho U_{A,z} dA$ where normalised radial profiles for $U_{A,z}$ are taken an from isothermal case [46].
$U$	Time averaged velocity, $\text{m s}^{-1}$
$U_{av}$	Bulk or superficial air velocity, $\text{m s}^{-1}$
$U_{p,sd}$	Particle sedimentation or free falling velocity (axial component of $U_{p,t}$ ), $\text{m s}^{-1}$
$U_{p,t}$	Particle terminal velocity, $\text{m s}^{-1}$
$U_{p,w}$	Particle velocity for the first wall impact, $\text{m s}^{-1}$
$x_p$	Particle/droplet diameter, $\mu\text{m}$
$x_{p,pore}$	Pore/cavity/void diameter, $\mu\text{m}$
$X_S$	Product surfactant(s) mass fraction in a dry basis
$X_W$	Product water mass fraction
$z$	Axial position in the cylindrical chamber measured from the level of the air inlets, $\text{m}$

#### Greek letters and symbols

$\varepsilon_{abs}$	Intra-particle porosity in pores below the envelope threshold, %
$\varepsilon_{ske}$	Intra-particle porosity, in pores between the envelope and skeletal thresholds, %
$\eta_t$	Thermal efficiency in the dryer, $\eta_t = (T_{A,IN} - T_{A,EX}) / (T_{A,IN} - T_{amb})$
$\eta_h$	Heat transfer efficiency in the dryer, $\eta_h = Q_S / H_{A,IN}$
$\mu$	Slurry viscosity, $\text{kg s}^{-1} \text{m}^{-1}$
$\rho$	Density, $\text{kg m}^{-3}$
$\rho_{abs}$	Absolute particle density including no pores in He pycnometry, $\text{kg m}^{-3}$
$\rho_{bulk}$	Bulk particle density including cavities up to $x_{p,pore} < 353 \mu\text{m}$ in Hg porosimetry, $\text{kg m}^{-3}$
$\rho_{env}$	Envelope particle density including pores smaller than the threshold in Table 6 in Hg porosimetry, $\text{kg m}^{-3}$
$\rho_{ske}$	Skeletal particle density, including pores up to $x_{p,pore} < 6 \text{ nm}$ in Hg porosimetry, $\text{kg m}^{-3}$
$\Omega_i$	Design swirl intensity, non-dimensional flux of angular momentum [46].

#### Subscripts, superscripts and caps

$A$	For the air phase
$DA$	For dry air
$DS$	For dry slurry
$E$	For the elutriated powder
$EP$	For the full powder exiting the tower (elutriated fraction + product from the bottom)
$EX$	Exhaust conditions
$IN$	Inlet conditions
$P$	For the particle/product exiting the bottom end of the tower
$R$	For the fraction of oversized powder removed from the product
$S$	For surfactant(s)/for the solid phase/for the slurry mix at the nozzle

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