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# Phenomenological model and working mechanism of bio-inspired polymeric composites driven by water gradient

## Abstract

**Purpose** – To develop a phenomenological model to investigate the underlying mechanism of and to predict the bio-inspired performance under different thermo-temporal conditions.

**Design/methodology/approach** – Flory-Rehner free-energy functions are applied to quantitatively identify the driving forces in the viscously bio-inspired response of dynamic polymer network. Furthermore, permeation transition equation is adopted to couple water gradient and water sorption/desorption into the free-energy function.

**Findings** – The results show that the influence of potential energy on deformation can be related to a stretching ratio that uniquely determines water sorption/desorption, locomotion frequency and contractile stress. Finally, by means of combining the free-energy function and Arrhenius equation, a phenomenological thermo-temporal model is developed and verified by the experimental results.

**Research implications** – This study focuses on exploring the theoretical mechanism and significantly enhances understanding of relevant experimental features reported previously.

**Originality/value** – The outcome of this study will provide a powerful phenomenological and quantitative tool for study of shape memory effect in bio-inspired polymers.

**Keywords** - Bio-inspired polymer, Free-energy function, Thermo-temporal, Phenomenological modelling

**Paper type** Research paper

## Introduction

Bio-inspired polymers are a class of responsive materials that are able to derive their phenomenal properties from precisely controlled sequences and compositions of the constituents, which in turn lead to rearrangement of chain shapes and structures on external stimuli (Yu and Cölfen, 2004; Xia and Jiang, 2008; Venkatraman *et al.*, 2008). Bio-inspired polymers can adapt to surrounding environment and convert chemical or biochemical signals into thermal, optical, electrical and mechanical signals, and vice versa (Jones *et al.*, 1991; Bao and Suresh, 2003; Ayari *et al.*, 2007; Stuart *et al.*, 2010; Lu and Huang, 2013). The stimuli-responsive macromolecules are capable of conformational and chemical changes on receiving an external signal, accompanied by variations in the physical properties and thermo-temporal conditions of the polymer and derived from changes in the materials' environment (Gitsov and Fréchet, 1996; Liu and Urban, 2010; Roy *et al.*, 2010; Mather *et al.*, 2009). To intelligently design such systems, the novel physics and working mechanism of the bio-inspired polymers have been focused on in previous works (Börner, 2007; Creton and Gorb, 2007). Many effective approaches are aimed to apply biological components or biological design principles to dramatically extend their capability and applicability (Kim *et al.*, 2005; Trask *et al.*, 2007; Zhang *et al.*, 2012; Cianchetti *et al.*, 2009). Currently, these bio-inspired materials are playing an increasingly important role in a diverse range of applications, particularly in biomedical field (e.g. scaffolds for tissue engineering) (Pham *et al.*, 2006), pharmaceutical science (e.g., drug delivery devices) (Flores *et al.*, 2013), environmental science (Hu *et al.*, 2012), and nanotechnology (Ding *et al.*, 2007).

To enable biological functions, nature requires to selectively tailor molecular assemblies that provide a specific chemical function and structure (O'Reilly *et al.*, 2006). Bio-inspired and synthetic polymer composites are often prepared and actuated via mimicking the action of muscles that are capable of responding to the environment (Smela, 2003; Ebron *et al.*, 2006). A bio-inspired material, which is to absorb water and change its shape, has been designed by combining both a stiff polypyrrole (PPy) and a dynamic polyolborate network that is hydrolytically sensitive could be driven by water gradient (Ma *et al.*, 2013). The polyolborate network is sensitive to water by means of hydrolysis and reform of the borate ester crosslinking hub upon water sorption and desorption, and thus changes the mechanical

properties of the composite (Ma *et al.*, 2013). The polymer composite could exchange water with the environment to induce expansion or contraction (Ma *et al.*, 2013). The mechanical energy converted from the chemical potential energy of bio-inspired polymeric composites has been identified as the driving force (Lu and Huang, 2013; Lu *et al.*, 2014). In this study, Flory-Rehner free-energy functions are employed to quantitatively separate the effect and identify the driving force in bio-inspired viscous response of dynamic polymeric network. Working mechanism and bio-inspired performance under different thermo-temporal conditions have been investigated and modelled. By means of combining free-energy function and Arrhenius equation together, the influence of potential energy on deformation can be related by a stretching ratio that uniquely determines water sorption/desorption, locomotion frequency and contractile stress of this water gradient-driven polymeric composite. The phenomenological thermo-temporal model is verified by the available experimental results in the literature. This study focuses on the theoretical mechanism, which is a challenging issue and will significantly enhance our understanding of these experimental features.

### **The theoretical framework**

Flory-Rehner free energy equation is generally employed to describe thermodynamic of polymer solution, by comparing the free energy function before and after mixing (Lu, 2012). For the given bio-inspired PEE-PPy composite, water molecules penetrate into the polymer network and mix with the polyolborate macromolecules. There are two contributions to the free-energy function ( $W$ ) of the bio-inspired dynamic polymeric composite driven by water gradient in a water sorption and desorption cycle: stretching free-energy ( $W_s$ ) and mixing free-energy ( $W_m$ ) (Du and Zhang, 2010; Lu *et al.*, 2010), i.e.

$$W = W_s + W_m \quad (1)$$

The free-energy of stretching a network denotes the stretches ( $\lambda_1, \lambda_2, \lambda_3$ ) of the polymer by (He and Chen, 2000)

$$W_s(\lambda_1, \lambda_2, \lambda_3) = \frac{1}{2} NkT(\lambda_1^2 + \lambda_2^2 + \lambda_3^2 - 3 - 2 \log \lambda_1 \lambda_2 \lambda_3) \quad (2)$$

where  $N$  is the number of chains in the polymer divided by the volume of the polymer block in the referenced state, and  $kT$  is the energy of the individual particle in certain temperature.

Without the cross-linking network, polymer can be dissolved and form a solution. As the PEE-PPy composite driven by water gradient, the dynamic polyolborate network is hydrolytically sensitive to water by means of hydrolysis and reforming of the borate ester crosslinking hub upon water sorption and desorption. Here the mixing free-energy is taken as (He and Chen, 2000),

$$W_m(C) = \frac{kT}{v} \left[ \nu C \log \left( 1 + \frac{1}{\nu C} \right) + \frac{\chi}{1 + \nu C} \right] \quad (3)$$

where  $C$  is the number of the solvent molecules in the polymeric network and  $v$  is the volume of per solvent molecule.  $\nu C$  is the volume of the solvent molecules in the network divided by the volume of the polymers. Thus, Equation 3 can be substantiated by,

$$W = \frac{1}{2} NkT(\lambda_1^2 + \lambda_2^2 + \lambda_3^2 - 3 - 2 \log \lambda_1 \lambda_2 \lambda_3) + \frac{kT}{v} \left[ \nu C \log \left( 1 + \frac{1}{\nu C} \right) + \frac{\chi}{(1 + \nu C)} \right] \quad (4)$$

Considering a cubic solvent-swollen polymer without constraint to be stretched in three directions, and the stretches of polymer to a fixed value, namely  $\lambda_1, \lambda_2, \lambda_3$ . In the referenced state, no external loadings are applied on the block, and no solvent molecules are absorbed inside the block with dimensions of  $L_1 L_2 L_3$ . Exposing the polymer to solvent, the polymeric block is assumed to imbibe solvent molecules that diffuse into the interstitial space of the polymer chains. It is assumed that weights applied on the six surfaces of the block results in the dimensions of polymeric block changed to  $l_1 l_2 l_3$  (Zhao and Suo, 2007). Denote the stretches of the block by,

$$\lambda_1 = \frac{l_1}{L_1}, \quad \lambda_2 = \frac{l_2}{L_2}, \quad \lambda_3 = \frac{l_3}{L_3}. \quad (5)$$

It is assumed that both polymer molecules and solvent molecules are incompressible, as well as there is no void space inside the polymer block. When  $C$  solvent molecules are diffused into polymer, the volume of the polymer changes to  $\lambda_1 \lambda_2 \lambda_3 = 1 + \nu C$ .

Considering a cubic solvent-swollen polymer without constraint to be stretched in three directions, and the stretches of polymer to a fixed value, namely  $\lambda_1 = \lambda_2 = \lambda_3 = \lambda$ . Thus the  $(1 + \nu C)$  can be calculated by substituting  $\lambda$  into Equation 3, namely,  $1 + \nu C = \lambda^3$ . Equation 4 can be rewritten as,

$$\frac{\nu W}{kT} = \frac{3}{2} N\nu(\lambda^2 - 1 - 2 \log \lambda) + \left[ (\lambda^3 - 1) \log \left( \frac{\lambda^3}{\lambda^3 - 1} \right) + \frac{\chi}{\lambda^3} \right] \quad (6)$$

where  $N\nu$  is assumed to be a constant. Meanwhile when a cubic polymer is subject to a uniaxial stress along the longitudinal direction, it is under the uniaxial stress. The state of deformation can be characterized by the longitudinal stretch  $\lambda_1$  and two transverse stretches  $\lambda_2 = \lambda_3$ . In this case,  $1 + \nu C = \lambda_1 \lambda_2^2$ , the Equation 6 may be expressed as,

$$\frac{\nu W}{kT} = \frac{1}{2} N\nu(\lambda_1^2 + 2\lambda_2^2 - 3 - 2 \log \lambda_1 \lambda_2^2) + \left[ (\lambda_1 \lambda_2^2 - 1) \log \left( \frac{\lambda_1 \lambda_2^2}{\lambda_1 \lambda_2^2 - 1} \right) + \frac{\chi}{\lambda_1 \lambda_2^2} \right] \quad (7)$$

Figures 1(a) and (b) plots numerical results for free energy function with stretching ratio of PEE-PPy composite in mixing with water, where  $N\nu$  is assumed to be a constant. As presented in Equation 7, the change in free energy function is determined by two parameters, namely  $\chi$  and  $\lambda_2/\lambda_1$ , while it is essentially determined by the free-energy of stretching or free-energy of mixing in a certain range of stretching ratio.

(Take in Figure 1)

When PEE-PPy composite is immersed into water, water molecules are penetrated into the polymer network. Transport and immigration of water molecules is originated from the permeability ( $P$ ) of PEE-PPy composite. In such a case, it is a common practice to characterize mass transfer by the permeation flux (Roy, 1999; Ashley, 1985),

$$J = \frac{\phi_2 \cdot d}{A \cdot t} \quad (8)$$

where  $J$  is the normalized flux,  $\phi_2$  is the amount of water molecule,  $d$  is the thickness of polymer,  $A$  is the surface area of polymer, and  $t$  is the permeation time. Equation (8) may be rewritten as (Roy, 1999; Ashley, 1985),

$$\phi_2 = P \frac{A \cdot t \cdot p}{d} \quad (J = P \cdot p) \quad (9)$$

where  $p$  is osmotic pressure applied upon the polymer. We assume that individual PEE-PPy macromolecule and the mobile water molecule are incompressible. Assume that one unit of the dry macromolecules imbibes  $C$  numbers of water molecules and swells to  $\lambda_1, \lambda_2, \lambda_3$ . The water molecules contribute to the swelling of the polymer, the volume fraction of water molecules in PPy/water system is therefore presented as,

$$\phi_2 = \frac{\nu C}{1 + \nu C} = \frac{\lambda_1 \lambda_2 \lambda_3 - 1}{\lambda_1 \lambda_2 \lambda_3} \quad (10)$$

In combination of Equations 9 and 10, the constitutive relation between the pressure and stretch may be expressed as,

$$P \frac{A \cdot t \cdot \sigma}{d} = \frac{\lambda_1 \lambda_2 \lambda_3 - 1}{\lambda_1 \lambda_2 \lambda_3} \quad (11)$$

As the polymer area  $A$  and thickness  $d$  can be written as  $A = \lambda_1 \lambda_2$  and  $d = \lambda_3$ , respectively, Equation 11 may be rewritten as,

$$\phi_2 = P \frac{\lambda_1 \cdot \lambda_2 \cdot t \cdot \sigma}{\lambda_3} \xrightarrow{\lambda_3 = \lambda_3} \phi_2 = P(\lambda_1 \cdot t \cdot \sigma) = \frac{\lambda_1 \lambda_2^2 - 1}{\lambda_1 \lambda_2^2} \Rightarrow \sigma = \frac{\lambda_1 \lambda_2^2 - 1}{P(\lambda_1^2 \lambda_2^2 \cdot t)} \quad (12)$$

Figure 2 plots the constitutive relation of stress and stretching ratio. The numerical results reveal the trend as expected, i.e., with the increase of stretching ratio of  $(\lambda_2/\lambda_1)$ , higher pre-stress is needed, resulting in the decreasing of stress which is originated from osmotic pressure. On the other hand, the stress initially increases and then decreases with the increase in the stretching ratio of PEE-PPy composite where  $\lambda_2/\lambda_1 = 1$ ,  $\lambda_2/\lambda_1 = 1.25$  and  $\lambda_2/\lambda_1 = 1.5$ . The stress initially increases with the increase in the stretching ratio due to the

change in the area of polymer. And then it gradually decreases because the volume fraction of water molecules and pre-stress increase significantly.

(Take in Figure 2)

## Constitutive relationship and phenomenological modelling

### Constitutive modelling of stretching ratio and frequency

The PEE-PPy composite continuously flips and navigates due to water gradient, resulting from the nonuniform water absorption and asymmetric swelling of the bottom and top faces. Therefore, water gradient is reflected in the asymmetric film deformation and drives the polymer composite locomotion (Ma *et al.*, 2013). Assume that a unit volume of dry PEE-PPy composite imbibes  $C$  numbers of water molecules and swells to a volume of  $1 + \nu C = \lambda^3$  as the constituents are assumed to be a kind of incompressible. By the combination of Equations 11 and 12, the relationship between volume concentration of water and stretching ratio in a homogeneous state of deformation for free swelling (where  $\lambda_1 = \lambda_2 = \lambda_3 = \lambda$ ) can be obtained as,

$$\phi = \frac{\nu C}{1 + \nu C} = \frac{\lambda^3 - 1}{\lambda^3} \rightarrow \lambda = \left( \frac{1}{1 - \phi} \right)^{\frac{1}{3}} = \left( \frac{1}{1 - P \cdot \frac{S \cdot t \cdot p}{d}} \right)^{\frac{1}{3}} \quad (13)$$

where permeability of water solvent is of  $10^{-8} \text{ cm}^2 \cdot \text{s}^{-1} \cdot \text{Pa}^{-1}$ , polymer area  $S$  is  $1.7 \text{ cm} \times 3 \text{ cm}$  and the thickness  $d$  is  $3 \times 10^{-2} \text{ cm}$  (He and Chen, 2000). Here Equation 13 can be expressed as,

$$\lambda = \left( \frac{1}{1 - t \cdot p \cdot 1.7 \times 10^{-6}} \right)^{\frac{1}{3}} \quad (14)$$

Figures 3(a) and (b) plot the numerical results of stretching ratio as a function of the immersion time and saturated water vapour pressure of polymer, respectively. The change in the stretching ratio of PEE-PPy composite may affect the quantitative results and maintain the overall trend. Simulation shows the expected trend, i.e., the stretching ratio increases with an increase in immersion time and saturated water vapour pressure. As the immersion

time and saturated water vapour pressure gradually increases, many more incompressible water molecules are absorbed into the polymer composite, resulting in the volume of polymer mixture and stretching ratio increased.

(Take in Figure 3)

Polymer material obeys the relaxation rule, and the relationship between relaxation time and internal activation energy follows Eyring equation as (Nguyen1 *et al.*, 2010; Li and Xu, 2011; Lu, 2013),

$$\frac{1}{f} = \frac{1}{f_0} \exp\left(\frac{\Delta E}{RT}\right) \quad (15)$$

where  $f$  is the relaxation frequency,  $\Delta E$  is the internal activation energy of chain mobility,  $R$  is the gas constant,  $T$  is the absolute temperature and  $f_0$  is a given constant. As well known, the bio-inspired PEE-PPy composite is of elastic shape change in the mechanical cycle of shape change. The change in free energy is assumed to be equal to the internal activation energy that is the driving force for the water-gradient-induced shape change. Then, the Equation 15 can be rewritten as,

$$\frac{1}{f} = \frac{1}{f_0} \exp\left(\frac{W}{kT}\right) \quad (16)$$

In combination of Equations 6 and 16, the frequency can be expressed,

$$\frac{1}{f} = \frac{1}{f_0} \exp\left(\frac{1}{\nu}\right) \cdot \left\{ \frac{3}{2} N\nu(\lambda^2 - 1 - 2 \log \lambda) + \left[ (\lambda^3 - 1) \log\left(\frac{\lambda^3}{\lambda^3 - 1}\right) + \frac{\chi}{\lambda^3} \right] \right\} \quad (17)$$

Here, Equations 14 and 17 may be employed to characterise the effect of stretching ratio and saturated water vapour pressure on the frequency of the bio-inspired PEE-PPy composite.

$$\left\{ \frac{1}{f} = \frac{1}{f_0} \exp\left(\frac{1}{\nu}\right) \cdot \left\{ \frac{3}{2} N\nu(\lambda^2 - 1 - 2 \log \lambda) + \left[ (\lambda^3 - 1) \log\left(\frac{\lambda^3}{\lambda^3 - 1}\right) + \frac{\chi}{\lambda^3} \right] \right\} \right. \quad (18)$$

$$\left. \left\{ \lambda = \left( \frac{1}{1 - t \cdot p \cdot 1.7 \times 10^{-6}} \right)^{\frac{1}{3}} \right. \right.$$

Figures 4(a) and (b) plot numerical results for frequency with stretching ratio and osmotic pressure, respectively, at a different value of  $\chi$  and normalized immersion time of  $t$ . With an increase in both stretching ratio and osmotic pressure, the frequency of polymer composite gradually decreases in the whole trend. As indicated by Equation (18), the decrease in frequency is only contributed to the increase in the stretching ratio, namely the increase in osmotic pressure also results in the increase of stretching ratio. When the stretching ratio increases, the internal activation energy and free energy are increased, resulted in the frequency decreased according to the Arrhenius law (Lu, 2013).

(Take in Figure 4)

### Constitutive modelling of stress and stretching ratio in subject to mechanical loads

A cubic bio-inspired PEE-PPy composite is immersed in water. It is assumed that polymer composite imbibes water molecules, resulting in its volume expansion. Thermodynamics dictates that the free-energy reaches minimum as the polymer/water system becomes stable. Here, the stresses may be expressed as (Zhao and Suo, 2007),

$$S_1 = \frac{\partial W}{\partial \lambda_1}, \quad S_2 = \frac{\partial W}{\partial \lambda_2}, \quad S_3 = \frac{\partial W}{\partial \lambda_3} \quad (19)$$

In deriving Equation 19, we have regarded  $S_1, S_2, S_3$  as the loading parameters in three directions of the cubic polymer/water system. It is considered that the length of the cubic PEE-PPy composite is fixed, while two lateral directions are free to move. Let  $\lambda_1$  be the fixed stretch in the longitude direction by pre-stretching, and  $\lambda_2, \lambda_3$  ( $\lambda_2 = \lambda_3$ ) be the stretch in other directions, thus,  $1 + \nu C = \lambda_1 \lambda_2^2$ . Here, in a constraint state the constitutive relationship between stress and stretching ratio can be expressed as,

$$\frac{\nu S_1}{kT} = \frac{\nu}{kT} \frac{\delta W}{\delta \lambda_1} = 3\lambda_2^2 \log\left(1 - \frac{1}{\lambda_1 \lambda_2^2}\right) + \frac{3}{\lambda_1} + \frac{3\chi}{\lambda_1^2 \lambda_2^2} + N\nu \left[ \lambda_1 \left(1 + \frac{2\lambda_2^2}{\lambda_1^2}\right) - \frac{3}{\lambda_1} \right] \quad (20)$$

Equation 20 gives the equilibrium of  $\nu S_1/kT$  function for the water gradient-induced PEE-PPy composite subjected to a longitudinal loading. The characteristic of  $\nu S_1/kT$ , using

$\chi$  and stretch ratio  $\lambda_1/\lambda_2$  as parameters is plotted in Figure 5. Figures 5(a) and (b) plot the relationship between  $\nu S_1/kT$  function and stretch ratio  $\lambda_1/\lambda_2$ . For a given parameter, e.g.  $\chi = 0$ ,  $\chi = 0.5$ ,  $\chi = 0.7$ ,  $\chi = 1.0$  and  $\chi = 1.2$ , the  $\nu S_1/kT$  function sharply increases with the increase in stretching ratio in the initial stage. On the other hand, with stretching ratio further increasing,  $\nu S_1/kT$  function decreases more slowly. This numerical result reveals that the stress reaches to a constant value with higher stretch  $\lambda_1$ . And the decrease in  $\nu S_1/kT$  is slower. With the  $\chi$  increased, the mixing between polymer macromolecules and water molecules becomes difficult, because the free energy function and internal activation energy significantly increase. Here, the stress function therefore increases at the same stretching ratio, as shown in Figure 5(a). Meanwhile, the free energy function also increases with the swelling ratio of polymer, leading to a high value of stress at the same stretching ratio as presented in Figure 5(b). Both numerical results are due to the increase in the free energy function of polymer/water mixed system.

(Take in Figure 5)

Although the above simulation results are used for the constitutive relationship between stress and stretching ratio, it should be noted that each tested sample always presents a different and partial constitutive behaviour due to the difference in the free energy function and internal activation energy. Therefore, Figure 6 is presented and the curves are picked out from Figure 5 for comparison between analytical results and experimental results. Figure 6 presents the numerical results of stress as a function of expansion/contraction cycle times. These analytical results verify that the constitutive relationship between stress and expansion/contraction cycle times in bio-inspired PEE-PPy composite in response to water gradient. We can utilize these to account for the effects of expansion/contraction behaviour on the bio-inspired PEE-PPy composite.

(Take in Figure 6)

**Phenomenological modelling of bio-inspired polymer driven by water gradients**

As known, the thermodynamics of polymers obey the relaxation rule (Nguyen1 *et al.*, 2010; Li and Xu, 2011; Lu, 2013), which could be employed to theoretically predict the relationships between flipping frequency with the saturated water vapour pressure and transport cargo. Relaxation time of polymers verifies the Arrhenius law:  $\tau = \tau_0 \exp(\Delta E/RT)$ . The frequency  $f$  fulfils the condition  $2\pi f\tau = 1$ , which leads to  $f_0/f = \exp(\Delta E/RT)$ . According to the theory on the effect of atmospheric pressure and stress on the relaxation behaviour of polymers, the Arrhenius law is modified to  $f_0/f = \exp[(\Delta E - a\sigma)/RT]$ , as the polymer is constrained by atmospheric pressure ( $p$ ), and  $V$  is the volume change. The applicability of this equation can be verified where the increase in the atmospheric pressure ( $p$ ) is equivalent to the decrease of ( $f_0/f$ ), therefore increasing the flipping frequency ( $f$ ) as the activation energy ( $\Delta E$ ) and temperature ( $T$ ) are kept constant. Here  $f_0/f = \exp[(\Delta E - a\sigma)/RT]$  can be expressed as,

$$f_0/f = \exp[(\Delta E - pV)/RT] \quad (21)$$

It can be found that the frequency gradually increases with the increase in atmospheric pressure ( $p$ ). The frequency of flipping motion as a function of the saturated water vapour pressure at each substrate temperature indicates an exponential correlation, not a linear correlation. Moreover, an exponential expression is employed to fitting the experimental data, as shown in the Figure 7. Therefore, we substantiate that the frequency of flipping motion and the saturated water vapour pressure indicate an exponential correlation, based on the Arrhenius law and simulation result, respectively.

(Take in Figure 7)

The flipping frequency verifies the Arrhenius law  $f_0/f = \exp(\Delta E/RT)$ , the increase in the frequency ( $f$ ) is equivalent to the decrease in the activation energy ( $\Delta E$ ). And the decrease in the activation energy is equivalent to the decrease in the transport cargo ( $\sigma$ ) as the strain ( $\varepsilon$ ) is constant and  $\Delta E = \sigma \cdot \varepsilon$ . Therefore, the flipping frequency verifies the modified Arrhenius law,

$$f_0/f = \exp[(\sigma \cdot \varepsilon)/RT] \quad (22)$$

The applicability of this equation can be verified where the decrease in the flipping frequency ( $f$ ) is equivalent to the increase in the function of  $\exp[(\sigma \cdot \varepsilon)/RT]$ , therefore increasing the transport cargo, as the strain ( $\varepsilon$ ) and temperature ( $T$ ) being kept constant. Figures 8(a) and (b) present the numerical simulation for the effects of  $pV$  and  $\sigma\varepsilon$  on the flipping frequency of PEE-PPy composite as a function of atmospheric pressure. Furthermore, an exponential equation is employed to verify the accuracy of the Arrhenius law for predicting the correlation of flipping frequency and cargo, as shown in the Figure 9. Based on the fitting curve, it is proven that the applicability of the exponential equation for fitting the experimental data. Here we also substantiate that the flipping frequency and the cargo indicate an exponential correlation, based on the Arrhenius law and simulation result, respectively.

(Take in Figure 8)

(Take in Figure 9)

### **Concluding remarks**

In this study, we validated the effectiveness of a theoretical approach and phenomenological modelling for the underlying mechanism and bio-inspired performance of the PEE-PPy composite driven by water gradient under different thermo-temporal conditions. In this approach, the theoretical and phenomenological models from Flory-Rehner free-energy functions and permeation transition equation provide an effective way to describe and predict the bio-inspired response of PEE-PPy composite. Furthermore, the thermo-temporal and constitutive relationships among locomotion frequency, atmospheric pressure and contractile stress and stretching ratio have been modelled and simulated by means of combining the free-energy function and Arrhenius equation. We verified the accuracy of the analytical results by the available experimental results. In this work, the theoretical approach is developed to identify the working mechanism, characterize the bio-inspired performance and accurately predict bio-inspired behaviour of the PEE-PPy composite driven by water gradients.

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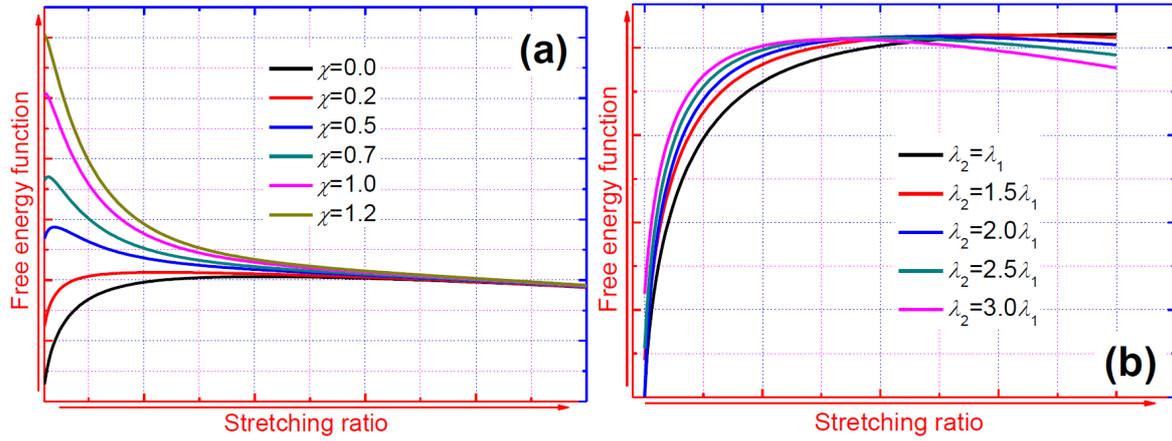
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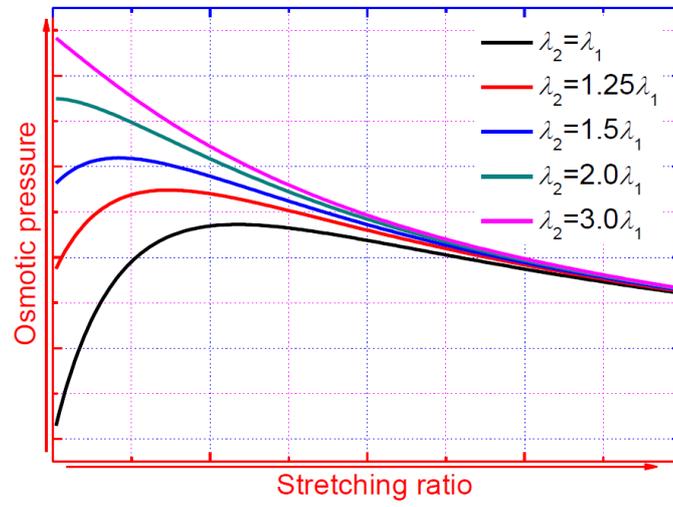
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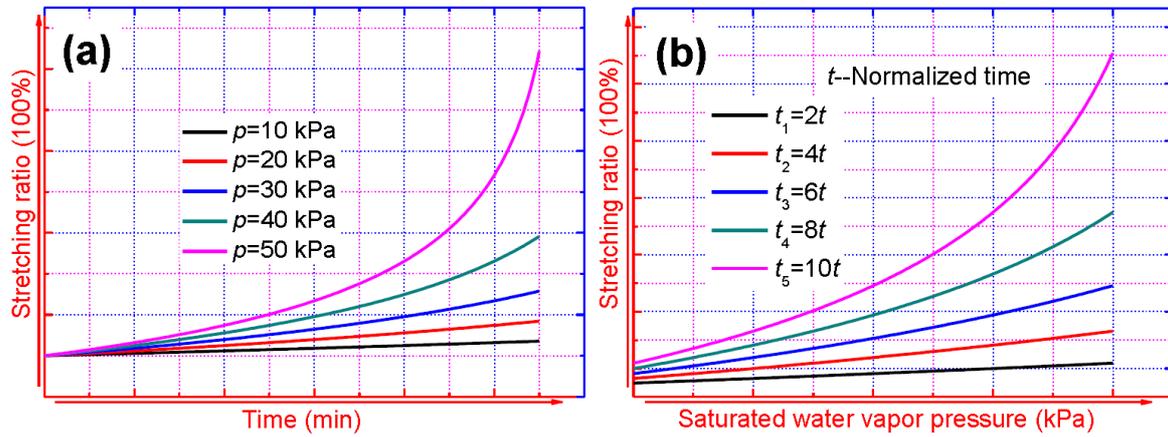
**Figure 1** Numerical simulation of the constitutive relation of free energy function and stretching ratio. (a)  $\chi=0.0, 0.2, 0.5, 0.7, 1.0$  and  $1.2$ ; (b)  $\lambda_2/\lambda_1=1.0, 1.5, 2.0, 2.5$  and  $3.0$ .



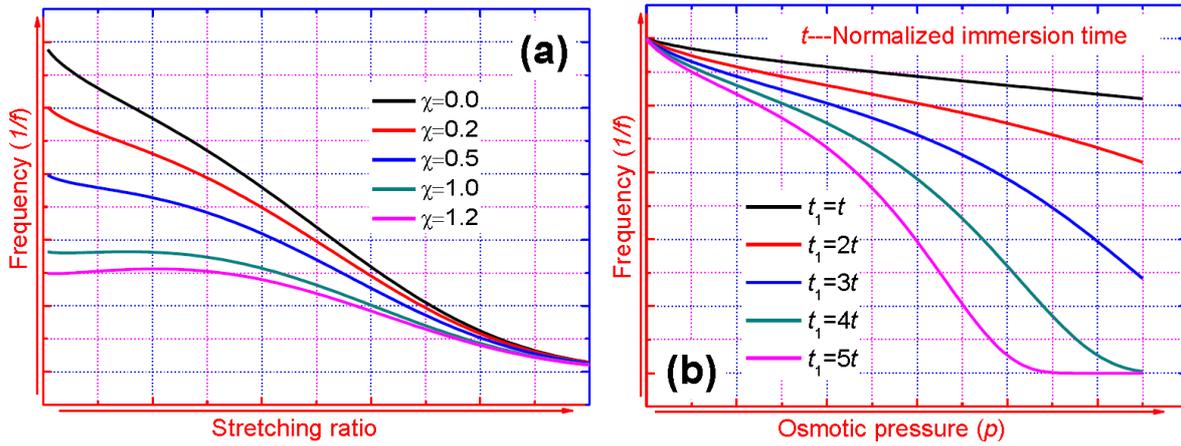
**Figure 2** Numerical simulation for the constitutive relation of stress and stretch



**Figure 3** Numerical simulation for the effect of immersion time and saturated water vapour pressure on the stretching ratio of PPy/water system. (a) Saturated water vapour pressure is of 10, 20, 30, 40 and 50 kPa; (b) Normalised time is of 2, 4, 6, 8 and 10t.

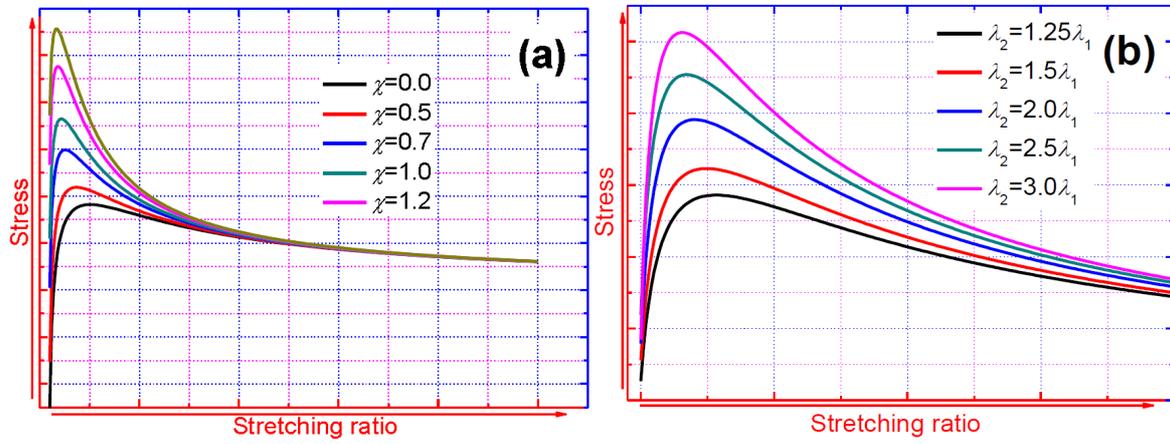


**Figure 4** Numerical simulation for the effect of stretching ratio and osmotic pressure on the frequency of PEE-PPy composite in response to water gradient. (a)  $\chi=0.0, 0.2, 0.5, 1.0$  and  $1.2$ ; (b)  $t_1=1, 2, 3, 4$  and  $5t$ .

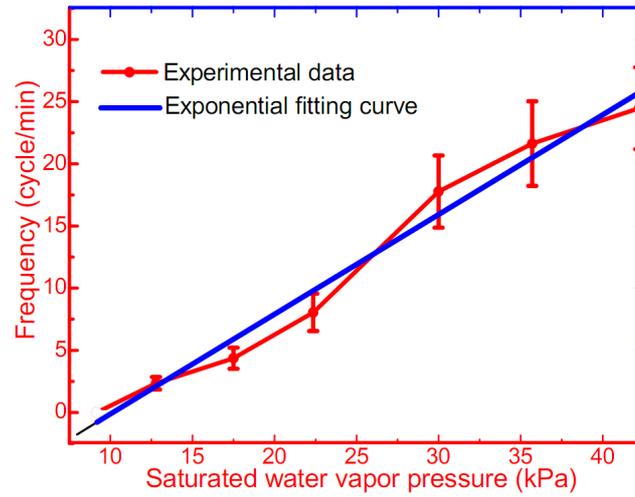


**Figure 5** Numerical simulation for the constitutive relation of stress and stretching ratio.

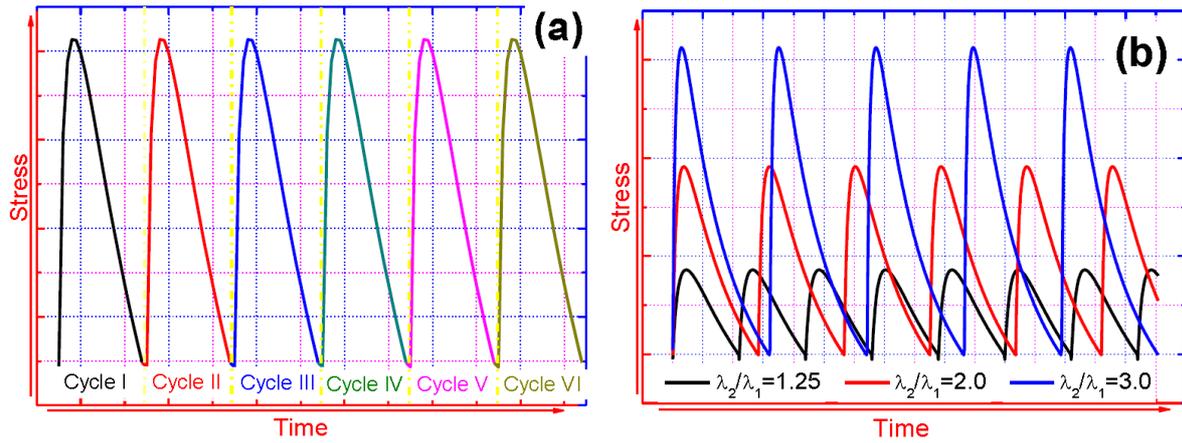
(a)  $\chi = 0, 0.5, 0.7, 1.0$  and  $1.2$ ; (b)  $\lambda_2/\lambda_1 = 1.25, 1.5, 2.0, 2.5$  and  $3.0$ .



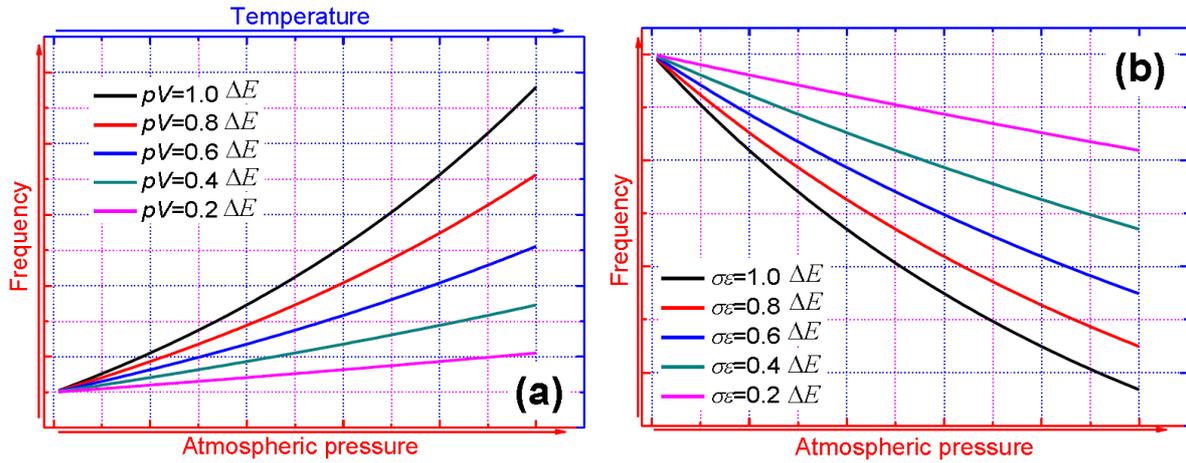
**Figure 6** An exponential correlation of the flipping frequency of flipping motion and the saturated water vapour pressure of the PEE-PPy composite [pentaerythritol ethoxylate (PPE) and Polypyrrole (PPy)]. The comparison between the previously experimental data obtained from Ma *et al.*, 2013 and the fitting plots and simulation result of Equation 20.



**Figure 7** Numerical simulation for the contractile stress in the PEE-PPy composite upon water sorption and desorption. (a) Mechanical performance of the PEE-PPy composite upon water sorption and desorption at a fixed value of  $\lambda_2/\lambda_1$ ; (b) Mechanical performance of the PEE-PPy composite upon water sorption and desorption at  $\lambda_2/\lambda_1 = 1.25, 2.0$  and  $3.0$ .



**Figure 8** Numerical simulation for the constitutive relationship between flipping frequency and atmospheric pressure for PEE-PPy composite. (a)  $pV=1.0 \Delta E$ ,  $0.8 \Delta E$ ,  $0.6 \Delta E$ ,  $0.4 \Delta E$  and  $0.2 \Delta E$ ; (b)  $\sigma\varepsilon = 1.0 \Delta E$ ,  $0.8 \Delta E$ ,  $0.6 \Delta E$ ,  $0.4 \Delta E$  and  $0.2 \Delta E$ .



**Figure 9** An exponential constitutive relationship of flipping frequency and the cargo of the PEE-PPy composite. The comparison between the previously experimental data obtained from Ma *et al.*, 2013 and the fitting plots and simulation result of Equation 21.

