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# Hyper-quicksort: energy efficient sorting via the TEMPLAR framework for Template Method Hyper-heuristics

**jerry.swan@cs.stir.ac.uk**  
**nathan.burles@york.ac.uk**

# Motivation

**Scalability** remains an issue for program synthesis:

- We don't yet know how to generate sizeable algorithms from scratch.
- *Generative* approaches such as *GP* still work best at the scale of *expressions* (though some recent promising results [6]).
- **Formal** approaches require a strong *mathematical background*.
- ... but *human ingenuity* **already** provides a vast repertoire of *specialized algorithms*, usually with known asymptotic behaviour.

Given these limitations, how can we best use **generative hyper-heuristics** to **improve** upon **human-designed algorithms**?

# The Template Method Pattern

- The **'Template Method' Design Pattern** [1] divides an algorithm into a *fixed skeleton* with one or more *variant* parts.
- The *fixed* parts *orchestrate the behaviour* of the *variant* parts.
- Example: Quicksort performance depends on the quality of the *pivot*, so we can treat the *pivot function* as a *variant part*:

```

DoubleArray qsort(DoubleArray arr) {
    double pivot = pivotFn( arr );
    // ^^^ pivotFn can be varied generatively
    return qsort( arr.filter( < pivot ) )
        ++ arr.filter( = pivot )
        ++ qsort( arr.filter( > pivot ) );
}

```

# Template Method Hyper-heuristics [10]

- So if we can express an algorithmic framework in template method terms, then we can *learn good implementations* for the *variant parts*.
- By ‘good’, we mean ‘biased towards the distribution to which the algorithm is exposed’.
- If our algorithms are *metaheuristics*, this means that they are *not subject to the ‘No Free Lunch’ theorem* [8], since the distribution over problem instances is *biased away from uniform* by the training set.
- Successfully demonstrated this approach to learn more effective GA selection and mutation operators [11, 9].

# A framework for generative hyper-heuristics

Generative hyper-heuristics can be specified by:

- A list of **variation points** describing the parts of the algorithm to be automatically generated.
- An **algorithm template** expressing the algorithm skeleton. The template produces a *customized version of the algorithm* from *automatically-generated implementations* of the variation points.
- A **fitness function** to evaluate the customized algorithm.
- An **algorithm factory** that *searches the space of variation points* to produce an *optimized version of the algorithm*.

# A functional description

For algorithm with function signature  $I \rightarrow O$ :

- $VP : (I_1 \rightarrow O_1) \times (I_2 \rightarrow O_2) \times \dots \times (I_n \rightarrow O_n)$ .
- $\text{Template} : VP \rightarrow (I \rightarrow O)$ .
- $\text{Fitness} : (I \rightarrow O) \rightarrow V$ .
- $\text{Factory} : VP \times \text{Template} \times \text{Fitness} \rightarrow (I \rightarrow O)$ .

## Why a Framework?

Generative HH are *laborious to implement* on a per-case basis, but *non-trivial to generalize*:

- The Factory is typically implemented via GP and is invoked repeatedly ...
- ... but popular GP implementations such as ECJ [3] and PushGP [7] *expect to be the 'top' of the system* ...
- ... hence are not easy to use for generative hyper-heuristics.
- Fitness of one VP depends on the other VPs, so *some fiddly software engineering is required* to enable 'dependency inversion'.
- *Heterogeneous signatures of VPs* needs special handling to retain any notion of type-safety.
- To prevent overfitting, cross-validation should be built-in to the fitness function by default.



## Interlude - higher-order functions in Java

```

interface Fun1<Arg,Result> {
    Result apply(Arg arg);
}
interface Fun2<Arg1,Arg2,Result> {
    Result apply(Arg1 arg1,Arg2 arg2);
}

// We can then use functions as parameters
// and return values:
Fun1<Int, String>
compose(Fun1<Int, Double> f, Fun1<Double, String> g) {
    return new Fun1<Int, String>() {
        String apply(Int arg) {
            return g.apply( f.apply( arg ) );
        }
    };
}

```

# Core TEMPLAR classes

```
public interface AlgTemplate<I,O> {
    public Fun1<I,O>
    makeAlg( ProgramList programs );
}

public class AlgFactory<I,O> {
    AlgFactory(GPConfig [] variationPointConfigs ,
        AlgTemplate<I,O> template) { ... }

    ProgramList run(FitnessCases<I,O> cases ,
        LossFn<O> lossFn) { ... }
}
```

## Trivial example - 'Identity' template

Just executes the generated program for the (sole) variation point:

```
class IdentityTemplate
implements AlgTemplate<Double, Double> {

    public Fun1<Double, Double>
    makeAlg(ProgramList progs) {
        // Wrap the VP in a function:
        return new Fun1<Double, Double>() {
            Double apply(Double arg) {
                return progs.get(0).execute(arg);
            }
        };
    }
}
```

# Using TEMPLAR

The end-user only needs to do this<sup>1</sup>:

```
// 1. Define an AlgTemplate subclass (previous slide).  
// 2. Set up the algorithm-specifics:  
AlgTemplate<Double, Double> template = new  
    IdentityTemplate();  
GPConfig[] vpConfigs = {new RationalFunctionConfig();}  
FitnessCases trainingSet = ...  
FitnessCases testSet = ...  
  
// 3. Invoke TEMPLAR:  
ProgramList bestVPs = Templar.trainAndTest(template,  
    vpConfigs,  
    trainingSet, testSet,  
    new RMSLossFn<Double>());  
println("best VPs:" + bestVPs);
```

---

<sup>1</sup>These examples describe *all* the code you need to write.

## Next simplest example - Composition Template

```

class CompositionTemplate
implements AlgTemplate<Int ,String> {
    Fun1<Int ,String> makeAlg(ProgramList progs) {
        f = new Fun1<Int ,Double>() {
            Double apply(Int arg) {
                return progs.get(0).execute(arg);
            }
        };
        g = new Fun1<Double ,String>() {
            String apply(Double arg) {
                return progs.get(1).execute(arg);
            }
        };
        // this template just composes
        // the two variant programs ...
        return compose(f,g);
    }
}

```

# HyperQuicksort

- Just follow the above steps for *any* algorithm you wish to optimize.
- We'll see how easy it is to create 'Hyper-quicksort' ...

# HyperQuicksort - Pivot Function

```

abstract class PivotFn
extends Fun2<DoubleArray , Intger , Double>{
    Double apply(DoubleArray a, Int recursionDepth);
}
class SedgewickPivotFn extends PivotFn {
    // counters the case of sorted
    // (or reverse-sorted) input
    Double apply(DoubleArray a, Int recursionDepth){
        return median(a.first , a[a.length/2], a.last);
    }
}

Int quicksort(DoubleArray a, PivotFn pivotFn);
// ^ instrumented to return some measure
// of pivotFn fitness (e.g. max recursion depth)

```

# HyperQuicksort - Alg Template

```

class QuicksortTemplate
implements AlgTemplate<DoubleArray, Int> {
    Fun1<DoubleArray, Int> makeAlg(ProgramList progs) -> {
        PivotFn pivotFn = (DoubleArray a, Int recursionDepth)
            -> {
                int progResult = progs[0].execute(a.size,
                    recursionDepth);
                int numSamples = min(abs(progResult), a.size);
                return median(randomSample(a, numSamples));
            };
        return (DoubleArray arg) -> Quicksort.sort(arg,
            pivotFn);
    }
}

```



## HyperQuicksort - Top Level

```

// 1. Define an AlgTemplate subclass (previous slide).
// 2. Configure GP to generate pivotFn VP:
List<Var> vars = {Var("size"), Var("recursionDepth")};
List<Node> funcSet = {IfFn(), LessFn(), AddFn(), ...};
GPParams params = ... // crossover, selection etc
GPConfig vpConfigs={new GPConfig(funcSet, vars, params);}

// 3. Invoke TEMPLAR
AlgTemplate<Double, Double> template = new
    QuicksortTemplate();
FitnessCases trainingSet = ...
FitnessCases testSet = ...
Templar.trainAndTest(template, vpConfigs, trainingSet,
    testSet, new RMSLossFn<Double>());

```

## Wait - there's more . . .

- Manual creation of GP nodes for function sets on custom solution representations (e.g. Timetable, RoutePlan, AntTrail etc) is tedious.
- Following [2], `Templar.FunctionSetGenerator` uses reflection to **automatically build a function set** from *any* Java object.
- By this means, a hyper-heuristic for *Iterated Local Search over bitstrings* was up and running from scratch **in under 20 minutes**
- By following the above steps, it's quick and easy to create a template for **your favourite algorithm here**.
- All you need now is *lots of CPU time . . .*

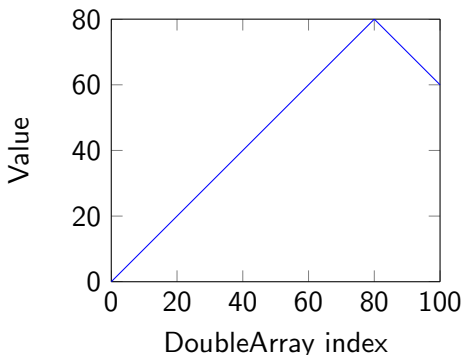
# Experiment - Setup

- EpochX for GP.
- JALEN [5] for power measurement.
  - Monitors execution time and processor utilisation to estimate power consumption.
  - Non-deterministic (e.g. other processes), and accuracy limited by platform (up to nanosecond).
  - Multiple arrays need to be sorted for each measurement (100).
  - Oracular pivot function.

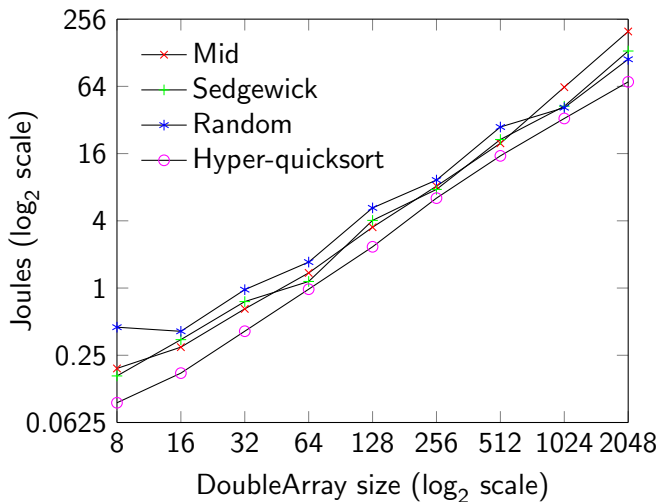
# Experiment - Pipeorgan Distribution [4]

**Training set size:** 70 (\* 100).

**Testing set size:** 100 (at 9 different array lengths, \* 1000).



# Results



# Results - Table

Array size	Middle index			Sedgewick			Hyper-quicksort (J)
	J	p	e	J	p	e	
8	0.191	7.46e-32	0.981	0.163	8.37e-32	0.980	0.094
16	0.296	1.20e-30	0.971	0.345	1.25e-31	0.979	0.173
32	0.651	8.13e-32	0.980	0.757	7.25e-32	0.981	0.410
64	1.366	4.80e-33	0.990	1.145	1.68e-30	0.970	0.976
128	3.505	4.80e-33	0.990	4.034	4.14e-33	0.991	2.341
256	8.175	4.14e-33	0.991	7.646	3.41e-32	0.983	6.387
512	19.777	4.33e-34	0.998	21.391	3.62e-34	0.999	15.268
1024	62.961	2.52e-34	1.000	42.508	6.44e-33	0.989	33.012
2048	198.438	2.52e-34	1.000	132.663	2.52e-34	1.000	70.234

Array size	Random index		
	J	p	e
8	0.446	8.37e-32	0.980
16	0.410	8.37e-32	0.980
32	0.967	4.80e-33	0.990
64	1.708	4.80e-33	0.990
128	5.221	2.52e-34	1.000
256	9.269	8.87e-34	0.996
512	27.685	2.52e-34	1.000
1024	41.245	3.61e-32	0.983
2048	111.894	3.47e-33	0.991

# Experiment - Conclusions

- P-values (Mann-Whitney U-test) and effect sizes (Vargha-Delaney  $\hat{A}_{12}$ ) clearly show Hyper-quicksort provides significant improvement on pipeorgan distributions.
- Intermediate results showed that minimal recursion doesn't always equate to minimal power consumption, as pivot function becomes more demanding.
- Imprecision and non-determinism of power measurement imposes time constraints on experimentation.

## Conclusion and Future Work

- Algorithms can be decomposed into *templates* consisting of a fixed skeleton and a collection of variant components.
- By judicious choice of function signatures, we can use generative methods (GP etc) to create variant components that are tuned to some target distribution.
- In implementation terms, TEMPLAR makes **generative HH for any algorithm** a matter of **GP parameter tuning**.
- New methods of power consumption modelling are in development. . .



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