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### Learning by Observation through System Identification

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# Learning by Observation through System Identification

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#### Abstract

In our previous works, we present a new method to program mobile robots —"code identification by demonstration"— based on algorithmically transferring human behaviours to robot control code using transparent mathematical functions. Our approach has three stages: i) first extracting the trajectory of the desired behaviour by observing the human, ii) making the robot follow the human trajectory blindly to log the robot's own perception perceived along that trajectory, and finally iii) linking the robot's perception to the desired behaviour to obtain a generalised, sensor-based model.

So far we used an external, camera based motion tracking system to log the trajectory of the human demonstrator during his initial demonstration of the desired motion. Because such tracking systems are complicated to set up and expensive, we propose an alternative method to obtain trajectory information, using the robot's own sensor perception.

In this method, we train a mathematical polynomial using the NARMAX system identification methodology which maps the position of the "red jacket" worn by the demonstrator in the image captured by the robot's camera, to the relative position of the demonstrator in the real world according to the robot.

We demonstrate the viability of this approach by teaching a Scitos G5 mobile robot to achieve door traversal behaviour.

#### 1. Introduction

Increasingly, personalised robots — robots especially designed and programmed for an individual's needs and preferences — are being used to support humans in their daily lives, most notably in the area of service robotics. Arguably, the closer the robot is programmed to the individual's needs, the more useful it is, and we believe that giving people the opportunity to program their own robots, rather than programming robots for them, will push robotics research one step further in the personalised robotics field.

However, traditional robot programming techniques besides being costly, time-consuming and error prone (Iglesias et al., 2005) — require specialised technical skills from different disciplines and it is not reasonable to expect end-users to have these skills.

In (Nehmzow et al., 2007) and (Akanyeti et al., 2007b) we presented a novel method to translate human behaviours into robot control code algorithmically, using system identification techniques such as Armax (Auto-Regressive Moving Average models with eXogenous inputs) (Eykhoff, 1974) and Narmax (Nonlinear Armax) (Billings and Chen, 1998). These techniques produce linear or nonlinear polynomial functions that model the relationship between the robot's sensor perception and motor response.

Our method has three stages: i) The human operator demonstrates the desired behaviour to the robot. ii) the robot imitates the desired behaviour blindly (i.e.without using sensor perception), using recursive, sensor-free polynomials. During this first run through the task the robot logs perception-action data to obtain a sensor-based control model, and iii) using the logged data, we obtain a sensor-based controller, using transparent mathematical functions which capture the fundamental relationship between the robot's perception and the desired motor response.

During the human user's initial demonstration of the desired motion, so far we used an external, camera based motion tracking system to log the trajectory information. Such tracking systems are complicated to set up and we can not expect the end users who want to program their own robots would have this kind of expensive facility in their houses.

In this paper, we therefore propose a new method replacing the Vicon motion tracking system with the Narmax polynomial models which are trained to predict the position of the demonstrator using the robot's own vision system.

### 2. Methodology and Experimental Setup

### 2.1 Narmax system identification methodology

The Narmax modeling approach is a parameter estimation methodology for identifying both the important model terms and the parameters of unknown nonlinear dynamic systems.



For multiple input, single output noiseless systems this model takes the form of equation 1. A detailed discussions can be found in (Billings and Chen, 1998), (Korenberg et al., 1988, Billings and Voon, 1986).

y(n)

(1)

$$= f(u_{1}(n), u_{1}(n-1), u_{1}(n-2), \cdots, u_{1}(n-N_{u}), 
u_{1}(n)^{2}, u_{1}(n-1)^{2}, u_{1}(n-2)^{2}, \cdots, u_{1}(n-N_{u})^{2}, 
\cdots, 
u_{1}(n)^{I}, u_{1}(n-1)^{I}, u_{1}(n-2)^{I}, \cdots, u_{1}(n-N_{u})^{I}, 
u_{2}(n), u_{2}(n-1), u_{2}(n-2)^{I}, \cdots, u_{2}(n-N_{u}), 
u_{2}(n)^{2}, u_{2}(n-1)^{2}, u_{2}(n-2)^{2}, \cdots, u_{2}(n-N_{u})^{2}, 
\cdots, 
u_{2}(n)^{I}, u_{2}(n-1)^{I}, u_{2}(n-2)^{I}, \cdots, u_{2}(n-N_{u})^{I}, 
\cdots, 
u_{d}(n), u_{d}(n-1), u_{d}(n-2), \cdots, u_{d}(n-N_{u}), 
u_{d}(n)^{2}, u_{d}(n-1)^{2}, u_{d}(n-2)^{2}, \cdots, u_{d}(n-N_{u})^{2}, 
\cdots, 
u_{d}(n)^{I}, u_{d}(n-1)^{I}, u_{d}(n-2)^{I}, \cdots, u_{d}(n-N_{u})^{I}, 
y(n-1), y(n-2), \cdots, y(n-N_{y}), 
y(n-1)^{2}, y(n-2)^{2}, \cdots, y(n-N_{y})^{I})$$

y(n) and u(n) are the sampled output and input signals at time *n* respectively,  $N_y$  and  $N_u$  are the regression orders of the output and input respectively, *d* is the dimension of the input vector and *l* is the degree of the polynomial. f()is a non-linear function and here taken to be a polynomial multi-resolution expansion of its arguments. Expansions such as multi-resolution wavelets or Bernstein coefficients can be used as an alternative to the polynomial expansions considered in this study.

The representation of the task as a transparent, analysable model enables us to investigate the various factors that affect robot behaviour for the task at hand. For instance, we can identify input-output relationships such as the sensitivity of a robot's behaviour to particular sensors (Roberto Iglesias and Billings, 2005), or make predictions of behaviour when a particular input is presented to the robot (Akanyeti et al., 2007a).

#### 2.2 Learning by Observation

**Human demonstration** First, the human user demonstrates the desired behaviour by performing it in the target environment. For the purpose of this paper we confined our experiments to 2-dimensional navigation problems due to the limited motion capabilities of our robot (2 degrees of motion, translational and rotational, figure 1). During this initial demonstration, we log the *x* and *y* position of the human user using the motion tracking system. Once the operator's trajectory is logged, we compute the translational and rotational velocities of the human by using consecutive (x, y) samples along the trajectory.

Sensorless trajectory following In a second stage, we use the Narmax system identification method to obtain two

sensor-free polynomials, one expressing rotational velocity as a function of time and past rotational velocities, the other expressing the translational velocity as a function of time and past linear velocities. We then use these two sensor-free polynomials to drive the robot along the trajectory the human had taken earlier, now logging sensor readings and velocities.

**Obtaining the final, sensor-based controllers** The sensorfree controllers obtained at stage II are essentially ballistic controllers that drive the robot along the desired trajectory as long as the robot is started from the same initial positions as the human. However, for real-world applications it is essential that sensor feedback is used to control the motion of the robot.

In the final stage we therefore use the Narmax system identification method to obtain sensor-based controllers, using the previously logged sensor-motor pairings. This controller can subsequently be used to control the robot in the target environment, copying the original behaviour exhibited by the human demonstrator.

#### 2.3 Experimental Setup

The experiments described in this paper were conducted in the 100 square meter circular robotics arena of the University of Essex. The arena is equipped with a Vicon motion tracking system which can deliver position data (x, y and z) for the full range of targets using reflective markers and high speed, high resolution cameras. The tracking system is capable of sampling the motion upto 100Hz within a 10mm range accuracy.

We used a Scitos G5 mobile robot called REX (figure 1). The robot is equipped with a ring of 24 sonar and 24 infra-red sensors, both uniformly distributed. A Hokuyo laser range finder is also present on the front part of the robot. This range sensor has a wide angular range (240 degree) with a radial resolution of 0.36 degree and distance resolution of less than 1cm. The robot also incorporates a colour video camera with  $640 \times 480$  pixels resolution which can deliver colour images upto 60Hz.

#### 3. Human Trajectory Prediction

In this section we propose an alternative method to obtain the trajectory information of the human user during his demonstration of the desired behaviour, using the robot's own sensor perception rather than the Vicon motion tracking system.

#### 3.1 Method

Our method is based on training a mathematical polynomial using the Narmax system identification methodology (see section 3.2) which maps the position of the "red jacket" — worn by the demonstrator — in the robot's camera image, with the relative position of the demonstrator referenced to the robot coordinate frame (see figure 2 and 3).

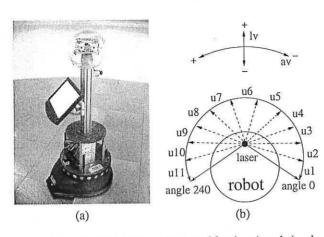


Figure 1: REX (a). RAX has two degrees of freedom (translational and rotational) and equipped with the laser range finder. The range finder has a wide angular range (240 degree) with a radial resolution of 0.36 degree and distance resolution of less than 1cm. During experiments, in order to decrease the dimensionality of the input space to Narmax model, we coarse coded the laser readings into 11 sectors ( $u_1$  to  $u_{11}$ ) by averaging 62 readings for each 22 degree intervals (b).

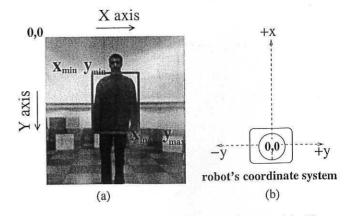


Figure 3: The output image after a pre processing stage (a). The demonstrator's jacket was isolated from the rest of the image. The position of the jacket was computed using a blob colouring algorithm based on the image coordinate frame as shown in the figure. The position information of the jacket is then fed to Narmax polynomials which are trained to predict the real position of the demonstrator relative to the robot's reference coordinate system shown in (b).

**Finding the position of the jacket** Figure 4 shows the block diagram that illustrates how we extract the position of the red jacket from the captured images.

First we rectify the captured images in order to minimize the effect of distortion due to the oval shape of the camera lens. Once the image is rectified, we convert it into "chromaticity colour space" which is less illumination dependent that the RGB colour space.

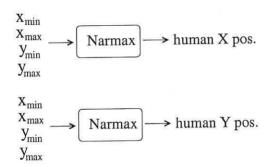


Figure 2: Position prediction models. These models are mathematical descriptions that define the relationship between the position of the jacket in the image and the relative position of the demonstrator referenced to the robot's coordinate system.  $(x_{min}, y_{min})$  and  $(x_{max}, y_{max})$  are the coordinates of the "left up" and "right down" corners of the rectangle surrounding the red jacket respectively (see figure 3). These coordinates are computed by separating the "red jacket" from the background of the image using a blob colouring algorithm.

$$C_r = \frac{R}{R+G+B} \tag{2}$$

$$C_g = \frac{G}{R+G+B} \tag{3}$$

$$C_b = \frac{B}{R+G+B} \tag{4}$$

where  $C_r$ ,  $C_g$  and  $C_b$  are the red chromaticity, green chromaticity and blue chromaticity components respectively, and R, G and B are the red, green and blue values respectively of the colour to be described.

In the final stage, we separate the jacket from the background of the image by using a blob colouring algorithm. Blob colouring is a technique used to find regions of similar colour in the image. The connected pixels are grouped together if they have similar intensity values and assigned to different regions if the difference in their intensity values is bigger than a certain threshold.

At the end of the blob coloring algorithm, we assume that the biggest red coloured region corresponds to the red jacket — we assume that there is no bigger red coloured object than the jacket itself in the image. We compute the minimum rectangular box which can frame the jacket entirely (figure 3). The coordinates of the "left up" and "right down" corners of

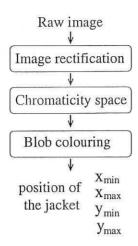


Figure 4: The block diagram that illustrates how the position of the red jacket is extracted from the captured images. First the images are rectified in order to minimize the effect of distortion due to the oval shape of the camera lens. Once the image is rectified, it is converted into chromaticity space which is less illuminant dependent. And in the final stage, the jacket is separated from the background of the image by blob colouring algorithm (see figure 3).

the rectangle are then fed to Narmax polynomials obtained as described in section 3.2 to predict the position of the demonstrator.

## 3.2 Acquisition of estimation and training data set in order to obtain Narmax polynomials

In order to collect training data for the estimation of the demonstrator's position, the human trainer wearing a red jacket walked randomly in the robot's field of view for half an hour. During the training session the robot was static and the robot's camera was aligned parallel to the floor so that the robot's field of view has the maximum coverage area for the demonstrator.

During this time the position of the jacket in the captured images and the relative position of the demonstrator referenced to the robot — obtained through the Vicon motion tracking system — were logged synchronously every 250ms. Figure 5 shows stream of original and the processed images captured during the training session.

#### 3.3 Obtaining position prediction models

We then used the Narmax system identification procedure to estimate the relative position of the demonstrator referenced to the robot as a function of the position of the jacket in the image ( $x_{min}$ ,  $x_{max}$ ,  $y_{min}$  and  $y_{max}$ ). The X position prediction model was chosen to be second degree with no regression in the input and output (i.e. l = 2,  $N_u = 0$ ,  $N_y = 0$ ). The resulting model contained 6 terms. The Y position prediction model was chosen to be fourth degree with no regression in the input and the output (i.e. l = 4,  $N_u = 0$ ,  $N_y = 0$ ) and contained 7

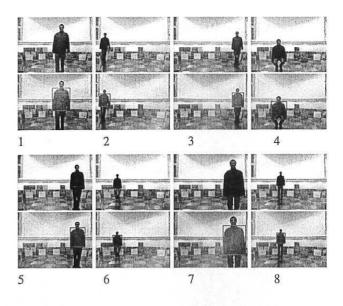


Figure 5: Stream of images captured by the robot's camera during the acquisition of the training data set used in obtaining Narmax model in order to calculate the relative position of the demonstrator according to the robot. Each image is pre processed using the procedure given in figure 4 in order to extract the position of the red jacket in the image.

terms. Both models are given in table 1.

X(n) =	Y(n) =
+14.684	-4.128
+0.148 * u(n,3)	-0.015 * u(n, 1)
-0.184 * u(n, 4)	+0.051 * u(n,2)
$+0.001 * u(n,3)^2$	$-0.001 * u(n,2)^2$
$+0.001 * u(n,4)^2$	$+0.001 * u(n,1) * u(n,2)^2$
-0.001 * u(n,3) * u(n,4)	$+0.001 * u(n, 1) * u(n, 1)^3$
	$-0.001 * u(n, 1) * u(n, 2)^3$

Table 1: Two position polynomials which link the perception of the robot to the position of the demonstrator in the robot's reference frame. X(n) and Y(n) are the x position (in m) and y position (in rad/s) of the demonstrator at time instant n and  $u_1$  to  $u_4$  are the  $x_{min}$ ,  $x_{max}$ ,  $y_{min}$  and  $y_{max}$  coordinates of the "red jacket blob" extracted from the image as described in figure 4.

Figure 6 shows the predicted and actual position of the demonstrator in the robot's coordinate frame.

**Model validation** We compared the predicted position of the demonstrator with the actual position by analysing the error distributions. The results show that the average error between the predicted and actual position of the demonstrator is less than  $10 \pm 0.3$  cm for both models (see figure 7).

#### 4. Experiment: Door Traversal

After obtaining position prediction models, we tested the viability of our method by teaching the robot to achieve door-

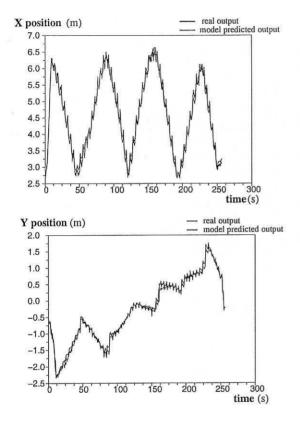


Figure 6: The predicted and actual position of the demonstrator in the robot's coordinate frame.

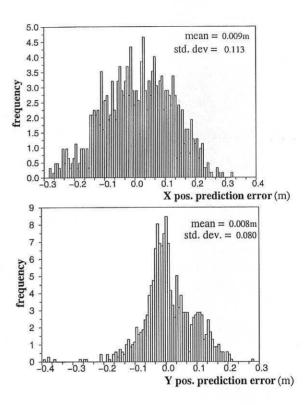


Figure 7: The error distributions of the X position prediction model and the Y position prediction model. The average error between the predicted and actual position of the demonstrator is less than  $10\pm0.3$ cm for both models.

traversal behaviour. The demonstrator walked through two consecutive door like openings of 120cm width. During this time, the robot calculates the trajectory of the demonstrator using the trajectory capturing mechanism described in section 3. every 250ms. Figure 8 shows the general experimental scenario in which the demonstrator performed the desired behaviour while the robot was observing him. Figure 9 shows the stream of images which were captured and processed by the robot during the demonstration.

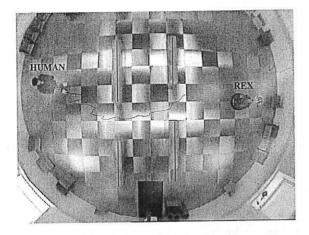


Figure 8: The trajectory followed by the demonstrator while passing through the two door like openings of 120cm width. While the demonstrator was performing the desired behaviour, the robot was observing him and calculating the demonstrator's relative trajectory according to the robot itself using position prediction models given in table 2.

Analysis of the observed trajectory reveals that there is noise in the data because of two reasons:

- 1. There is a constant oscillation in the motion of the demonstrator, which originates from the swinging motion perpendicular to the heading direction. This is a general characteristic of the two legged locomotion in humans.
- 2. The polynomials that compute the position of the demonstrator reference to the robot are extremely sensitive to how accurate the position of the jacket is extracted from the image. The blob colouring algorithm is not a very robust method of image segmentation in the environments where the illumination is variant.

We eliminate the noise by using a low pass filter, assuming that the demonstrator didn't do sharp changes in the heading direction while performing the desired task. We then computed the translational and rotational velocities of the demonstrator along the trajectory (see figure 10).

**Sensorless trajectory following** Having obtained the velocity information of the demonstrator along the desired path, we used them to drive the robot blindly in the test environment. During this first robot interaction with the environment,

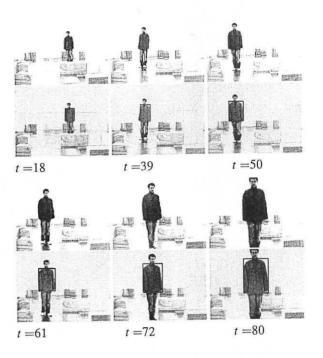


Figure 9: Stream of six images captured by the robot's camera during the demonstration of the desired behaviour. The numbers below each image indicates the frame number of the image where the robot's sampling rate of capturing images is 250ms. The captured images are then pre processed as described in section 3. in order to extract the position of the "jacket".

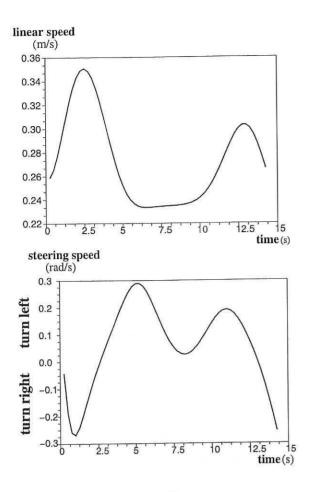


Figure 10: The translational and rotational speed graphs of the demonstrator while performing the desired behaviour shown in figure 8. The noise due to the oscillatory motion of the demonstrator and also due to the lightning conditions that affect the performance of the trajectory capturing mechanism while obtaining the trajectory of the demonstrator was removed from the data by low past filtering.

laser readings and the robot's translational and rotational velocities were logged in every 250ms (see figure 11).

**Sensor signal encoding** In order to decrease the dimensionality of the input space to the Narmax model, we coarse coded the laser readings into 11 sectors by averaging 62 readings for each 22 degree intervals. We then used the Narmax identification procedure to estimate the robot's translational and rotational velocities as a function of the coarse coded laser readings  $(u_1, u_2, \dots, u_{11}$  (see figure 1)).

Both the translational and the steering speed model were chosen to be second degree. No regression was used in the inputs and output (i.e. l = 2,  $N_u = 0$ ,  $N_y = 0$ ) resulting in non linear Narmax structures. The both models contained 18 terms (table 2).

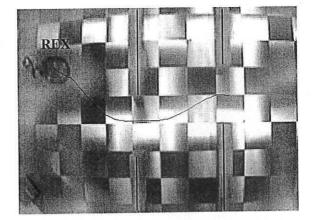


Figure 11: The trajectory of the robot under the control of the given velocity commands obtained from the human trajectory. The robot goes along the human trajectory given in figure without using any sensory perception. During this time, it logs its own perception perceived along the trajectory and the velocity commands. The logged data is then used to obtain sensor based controllers which links the perception of the robot to the desired behaviour.

**Model validation** We then let the sensor based models drive the robot in the test environment starting from 15 different locations. Figure 12 shows that the obtained models are successfull in driving the robot through the both door like openings without crashing into the walls.

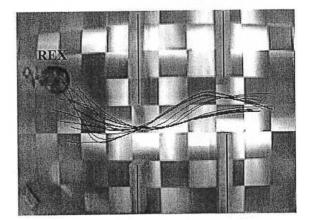


Figure 12: The trajectories of the robot under the control of sensor based controllers given in table 2. The robot was started from 15 different locations and it passed through the both door like openings successfully.

#### 5. Conclusion and Future Work

In this paper we introduce a new mechanism to program robots — programming by demonstration — based on algorithmically transferring observed human behaviours into robot control code, using transparent system identification

$l\nu(n) =$	av(n) =
-0.751	+2.260
+0.059 * u(n,3)	-0.054 * u(n,3)
+0.243 * u(n,4)	-0.480 * u(n, 4)
+0.040 * u(n,5)	-0.144 * u(n,5)
+0.139 * u(n,6)	-0.637 * u(n, 6)
+0.219 * u(n,7)	-0.195 * u(n,7)
-0.040 * u(n, 8)	+0.212 * u(n, 8)
-0.001 * u(n,9)	-0.056 * u(n,9)
$-0.003 * u(n,3)^2$	$-0.003 * u(n,3)^2$
$-0.008 * u(n,4)^2$	$+0.014 * u(n,4)^2$
$-0.007 * u(n, 6)^2$	$+0.004 * u(n,5)^2$
$-0.024 * u(n,7)^2$	$+0.085 * u(n, 6)^2$
$+0.008 * u(n, 8)^2$	$-0.029 * u(n, 8)^2$
$-0.003 * u(n,9)^2$	$+0.013 * u(n,9)^2$
-0.010 * u(n,3) * u(n,4)	+0.012 * u(n,3) * u(n,4)
-0.001 * u(n,3) * u(n,5)	-0.004 * u(n,3) * u(n,8)
-0.028 * u(n,4) * u(n,6)	+0.033 * u(n,4) * u(n,6)
-0.024 * u(n, 4) * u(n, 7)	+0.050 * u(n,4) * u(n,7)

Table 2: Experiment 3. Two sensor-based polynomials which link the perception of the robot to the desired behaviour shown in figure 11. lv(n) and av(n) are the translational velocity (in m/s) and rotational velocity (in rad/s) of the robot at time instant n and  $u_1$  to  $u_{11}$ are the coarse coded laser readings starting from the right extreme of the robot

#### techniques.

To obtain such sensor-motor controllers, we first demonstrate the desired motion to the robot by walking in the target environment. Using this demonstration, we obtain recurrent, sensor free models that allow the robot to follow the same trajectory (blindly). During this motion the robot logs its own perception action pairs, which are subsequently used as training data for the Narmax modeling approach that determines the final, sensor-based models which identify the coupling between sensory perception and motor responses as non linear polynomials. These models are then used to control the robot.

So far we used an external, camera based motion tracking system to log the trajectory of the human demonstrator during his initial demonstration of the desired motion. Besides being expensive, such tracking systems are complicated to set up and we can not expect the end users who want to program their own robots would have this kind of facility in their houses.

Therefore we enhanced our method by replacing the Vicon motion tracking system with the Narmax polynomial models which are trained to predict the position of the demonstrator using the robot's own vision system. The statistical analysis showed that the obtained models are able to predict the position of the demonstrator with a  $10\pm0.3$ cm accuracy given that the position of the jacket is computed accurately during the image pre processing stage.

#### 5.1 Future Work

The different experimental scenarios of obtaining trajectory information using robot's own vision system reveals that the performance of the position prediction models is dependent on how accurate the image pre processing stage extracts the position information of the jacket from the captured images. The blob colouring algorithm is not a robust method in image segmentation especially in the environments where illumination intensity is subject to noise and variant. Therefore we are currently investigating the alternatives to blob colouring algorithm which can give us more accurate positioning under different lightning conditions.

Furthermore, we are investigating the scaling properties of the presented approach, as well as methods of analysing the obtained models in order to be able to modify them off-line. Overall, the work already carried out and that proposed forms part of our ongoing research to develop a theory of robotenvironment interaction.

#### Acknowledgments

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