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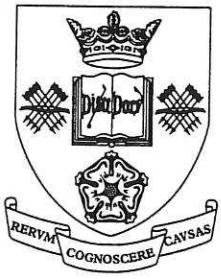

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COMPARISON OF THE DYNAMICAL PROCESSES IN PLASMA TURBULENCE OBSERVED IN THE HIGH- AND LOW-β REGIONS OF THE TERRESTRIAL FORESHOCK

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ABSTRACT

This paper highlights the fact that the dynamical processes that characterise plasma turbulence observed in the high-β region of the terrestrial foreshock are significantly different from the dynamical processes identified in the low-β region. The study is based on a time-domain model identified from measurements taken by AMPTE-UKS and AMPTE-IRM satellites.

INTRODUCTION

Nonlinear system identification based on the NARMAX model (Leontaritis and Billings, 1987) has been previously applied to analyse developed turbulence observed upstream of the quasi-parallel part of the terrestrial bow-shock. The data used in the study (Schwartz and Burgess, 1991; Schwartz *et al.*, 1992) was recorded by the magnetometer instruments aboard AMPTE UKS (PI D. Southwood) and AMPTE IRM (PI H. Lühr) satellites (Southwood *et al.*, 1985; Lühr *et al.*, 1985). One thousand pairs of measurements of B_y taken by AMPTE UKS and AMPTE IRM, considered to be the input and the output respectively of a nonlinear dynamical system, were used to estimate a time domain model of the turbulence (Coca et al., 1999). The plasma β (the ratio of thermal pressure to magnetic pressure) over the time interval considered for identification (500-750 seconds past 10:50:00 UT) was low compared with a previous interval of observation (0-150 second past 10:50:00 UT).
This study compares the model predictions over the time intervals characterised by high and low plasma β, using data not used in estimating the model. The aim is to investigate if the dynamics in the high-β region can also be described accurately by the model identified from observations in the low-β region.

NONLINEAR MODEL IDENTIFICATION

A Volterra polynomial model, which is just a particular type of NARMAX model

$$y(t) = f(u(t-1),..., u(t-n_u), e(t-1),..., e(t-n_e)) + e(t)$$

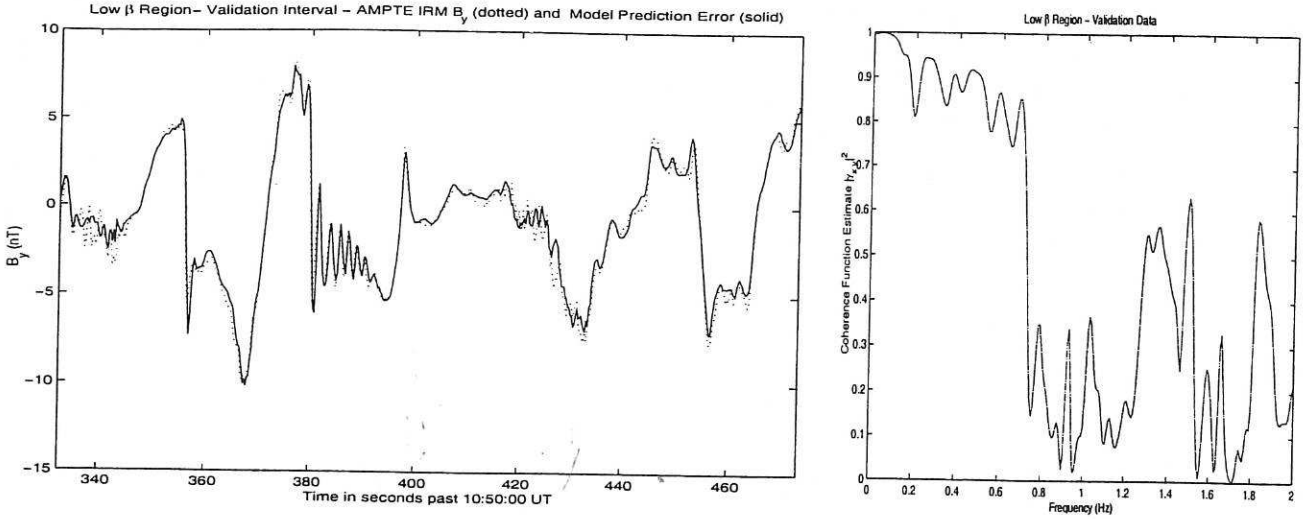
where $u(k)$, $y(k)$, $e(k)$ denote the input, output and prediction error respectively, n_u and n_e are the maximum input and output lags, and $f(\cdot)$ is a cubic multivariable polynomial, was identified from the data recorded over the estimation interval (500-750 seconds past 10:50:00 UT). This interval was chosen because of the high amplitude range and frequency content of the input measurements (AMPTE UKS) over this interval.
The identified model included deterministic and stochastic terms. The model validation tests performed on the resulting model have shown that there were no unmodelled nonlinear processes.

MODEL PREDICTIONS IN THE LOW-β REGION

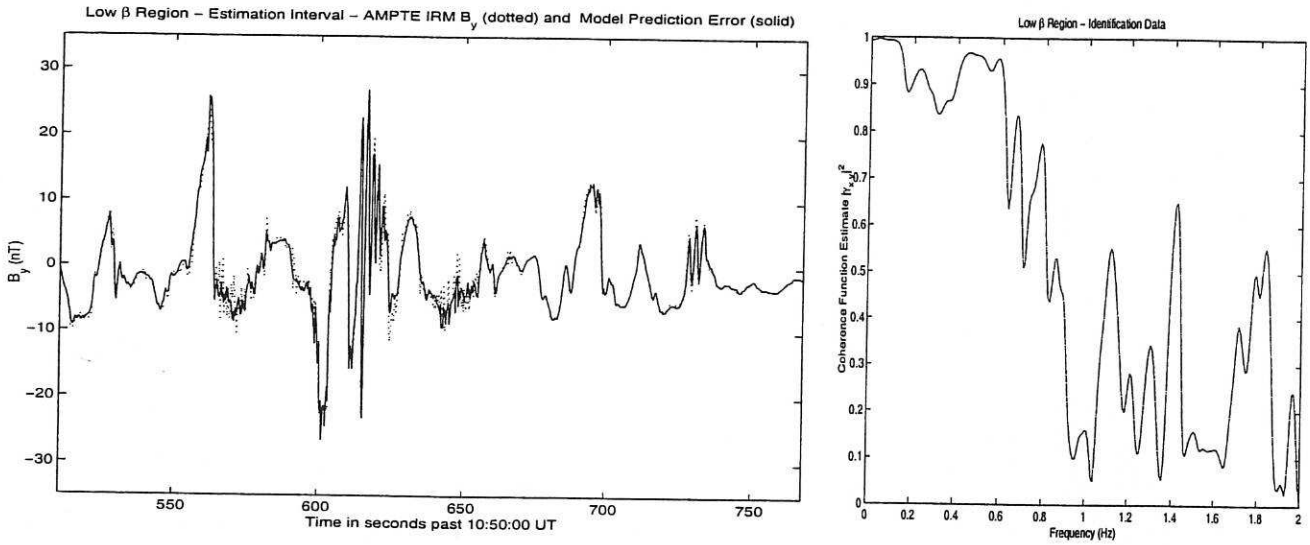
The deterministic part of the identified model was simulated using the AMPTE UKS data as the input. The resulting model predicted output was compared with the original AMPTE IRM measurements in the low-β interval.
Figure (1.a) shows the measurements of B_y taken by AMPTE IRM (dotted) superimposed with the model predicted output (solid) over the estimation interval. To investigate how the model performs over different frequencies the coherence function $|\gamma(\omega)|^2$ calculated for the real measurements and the model predicted output over the same interval are shown in Figure (1.b). Figure (2.a) shows the measurements of B_y taken by AMPTE IRM (dotted) superimposed with the model predicted output (solid) over a different interval not used in estimation. The coherence function $|\gamma(\omega)|^2$ calculated for the real measurements and the model predicted output over the same interval are shown in Figure (2.b).
In both cases the model predictions are very accurate over the frequency range which contains most energy of the turbulence.

MODEL PREDICTIONS IN THE HIGH-β REGION

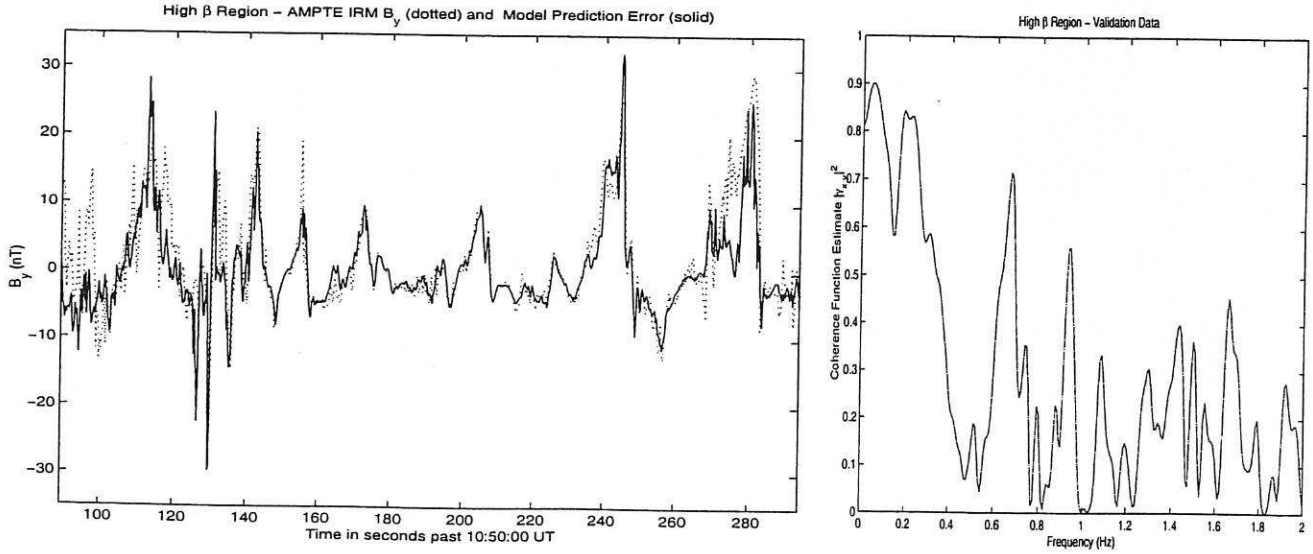
Figure (3.a) shows the model prediction output (solid) is superimposed on the real measurements (dotted) taken over an interval characterised by a higher value of β. The coherence function for this interval is shown in Figure (3.b). In this case the model predictions are quite poor compared to the previous intervals analysed. In particular the coherence functions show that the model fails to predict accurately in the 0.2÷0.6 Hz frequency range where the whistler waves are usually observed.



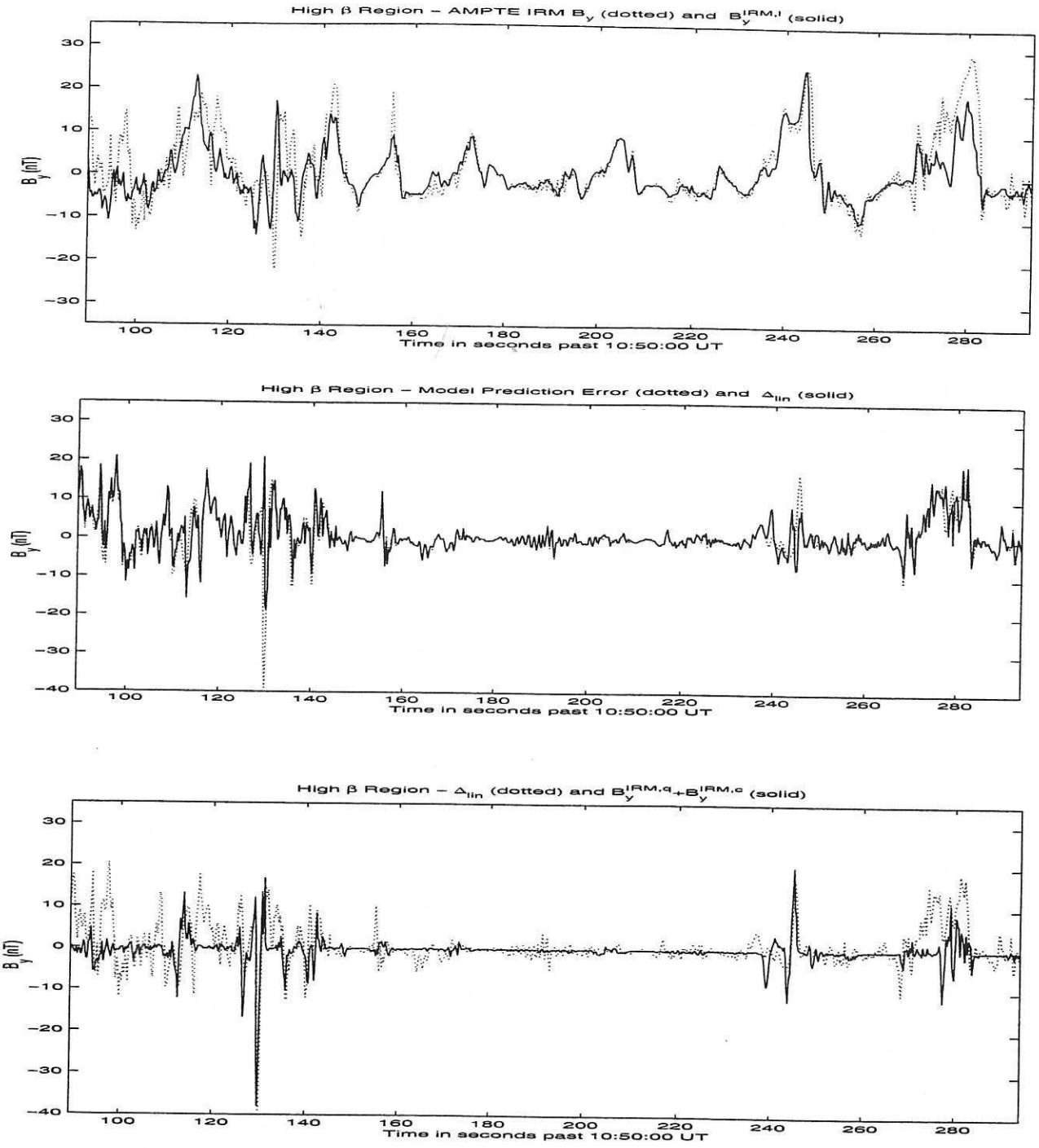
Figures 1: (a) Model predictions over the low β estimation interval (b) Coherence



Figures 2: (a) Model predictions over the low β validation interval (b) Coherence



Figures 3. (a) Model predictions over the high β validation interval (b) Coherence



Figures 4: (a) AMPTE IRM and $B_y^{IRM,l}$ (b) Model error and Δ_{lin} (c) Model error and $B_y^{IRM,q} + B_y^{IRM,,c}$

The model predicted output has been decomposed into its linear, quadratic and cubic contributions $B_y^{IRM,l}$, $B_y^{IRM,q}$ and $B_y^{IRM,c}$.

Figure (4.a) shows the measurements of B_y (dotted) superimposed by the linear model predictions $B_y^{IRM,l}$ (solid). Figure (4.b) shows the prediction error (dotted) superimposed with the linear prediction error $\Delta_{lin}(k)$ (solid) while Figure (4.c) shows the linear prediction error $\Delta_{lin}(k)$ (dotted) super-imposed by the combined quadratic and cubic components $B_y^{IRM,q}+B_y^{IRM,,c}$ (solid).

CONCLUSIONS

The results clearly indicate that the dynamics of the turbulence in the region characterised by higher β values is significantly different from the dynamics in the lower β part. In particular, Figures (4.a,b,c) indicate that while the low amplitude structures are still described quite well by the linear part of the model, the quadratic and cubic nonlinearities in the model fail to compensate the linear prediction errors that occur for

the higher amplitude structures. This suggests that the main changes in the dynamics that occur in the high-β region involve mainly the nonlinear, three- and four-wave interaction processes. A more comprehensive study is under way.

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