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OPEN Superconductivity in ordered Li–Al–B compounds

K. Hussain¹, S. J. Donaldson¹, E. Karaca^{1,2,3}, P. J. P. Byrne¹, P. J. Hasnip¹ & M. I. J. Probert¹✉

Using first principles calculations, we show that $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ materials have strong electron-phonon coupling, with many having a superconducting critical temperature (T_c) that exceeds that of the more familiar MgB_2 at ambient pressure. In particular, we find that LiAlB_4 is the most stable member of the family, with $T_c > 44$ K whilst the peak T_c is with Li_3AlB_8 which has $T_c > 77$ K. Our results reveal that these materials are both thermodynamically and dynamically stable, with strong electron-phonon coupling, indicating significant potential for practical superconducting applications.

The discovery of magnesium diboride (MgB_2) as a superconducting material in 2001^{1,2} exceeded expectations for the predicted limitations of critical temperatures (T_c) within the Bardeen-Cooper-Schrieffer (BCS) theory of superconductivity³. The structure of MgB_2 consists of monatomic layers of honeycomb-structured boron sheets and magnesium atoms, which are centred above each boron ring. It crystallizes in the P6/mmm space group (No. 191) with the layers perpendicular to the c lattice direction. The electronic states are analogous to benzene, where the σ -bonds are constrained by the boron planes to form covalent bonds through sp^2 -hybridised boron orbitals. A key ingredient to high T_c lies with the honeycomb-structured boron sheets, within which the E_{2g} phonon mode relates to the in-plane vibration of light boron atoms. With the σ -band concentrated along the B–B axes, this particular phonon mode causes significant distortion in the σ -bond network, shifting the electronic states and contributing significantly to the electron-phonon coupling within MgB_2 . To date, MgB_2 has the highest experimental T_c at ambient pressure for a BCS-type superconductor at 39 K. Inspired by this, we consider materials that are isostructural to MgB_2 in search of similar electron-phonon coupling, whilst incorporating lighter elements in order to achieve higher critical temperatures.

In order to be able to rapidly evaluate many potential materials, we used first principles calculations based upon Density Functional Theory (DFT). In particular, we used the CASTEP code⁴ which has recently gained the ability to calculate the electron-phonon coupling parameter, and we validated this approach (see 'Validation Study' section in the Supplementary Material for details) using the Quantum Espresso (QE) package^{5,6} which has a well-established electron-phonon coupling capability. Using CASTEP, we evaluated the binding enthalpy and structural stability of various candidate borides, and in particular, the ordered Li–Al–B system. We used the CASTEP Genetic Algorithm (GA)⁷ to find the global minimum energy structure of LiAlB_4 , which was indeed found to be isostructural to MgB_2 . We then evaluated the superconducting properties of this material using CASTEP (see below for details) and found $T_c = 49$ K. As this was an extraordinarily high value, we validated the calculation by simulating the same structure with QE, and found $T_c = 44$ K - in remarkable agreement with CASTEP, given the exponential sensitivity of T_c to the different parameters used with two independent codes. This validation of the results gave us confidence in the prediction that the T_c of LiAlB_4 is significantly above that of MgB_2 .

Finally, we then used the CASTEP Convex Hull GA⁸ (CHGA) to search the full Li–Al–B ternary space in order to find other candidate structures (see Convex Hull GA Section in the Supplementary Material for details), and used QE to evaluate their T_c . A number of thermodynamically stable candidates of the general form $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ were found, with the same MgB_2 type structure, as shown in Fig. 1. Analysis of the binding enthalpy showed that LiAlB_4 was the most stable, with very little energy difference between the 'ordered' P6/mmm structures, comprising separate layers of Li and Al, and the 'disordered' P6/mmc structures with mixtures of Li and Al in each non-B layer. For $x \geq 2$ we found that the CHGA favoured $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ structures with mixed Li/Al layers (P6₃/mmc structures) which would then have additional entropic stabilization at finite temperatures as there are many more possibilities. In this paper we focus on the 'ordered' P6/mmm structures with monatomic Li and Al layers for convenience, and to keep the number of structures manageable. We have found that the family of ordered $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ materials has great superconductivity potential, and that LiAlB_4 is the most stable member of the family, with $T_c > 44$ K whilst Li_3AlB_8 has T_c approaching 80 K. The significance of this is that the T_c of LiAlB_4 exceeds that of MgB_2 , whilst the T_c of Li_3AlB_8 even exceeds the

¹School of Physics, Engineering and Technology, University of York, York YO10 5DD, UK. ²Faculty of Sciences, Department of Physics, Sakarya University, 54050 Sakarya, Turkey. ³Center for Advanced Laser Techniques, Institute of Physics, 10000 Zagreb, Croatia. ✉email: matt.probert@york.ac.uk

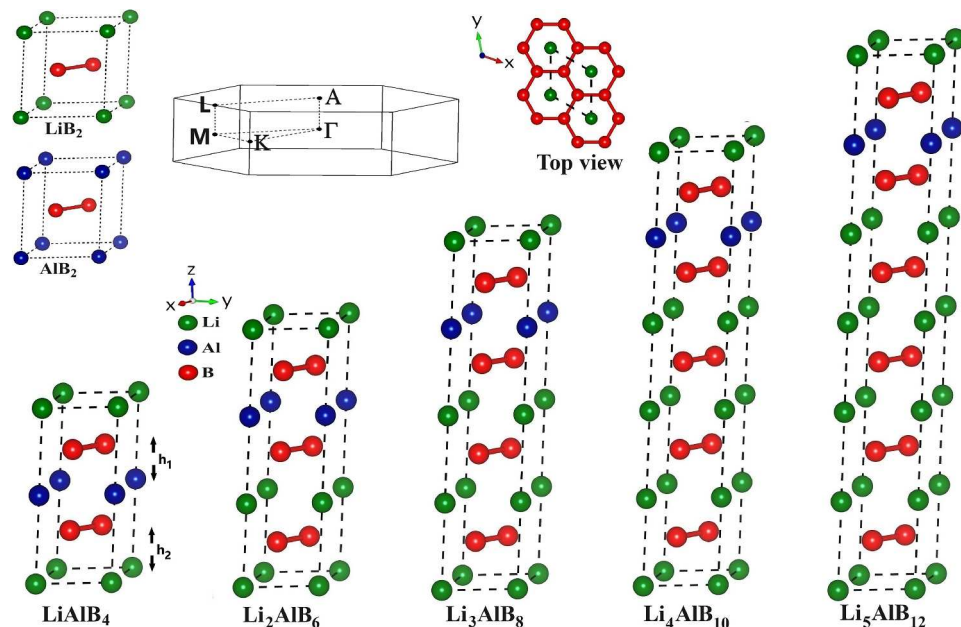


Figure 1. Schematic representation of the hexagonal crystal structure of $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$. Li, Al, and B atoms are represented in green, blue, and red. The unit-cell is shown with dashed black lines. Additionally, top-view projections of these crystals and their corresponding Brillouin zones are provided.

boiling point of liquid N_2 at 77 K. We find that $x \geq 2$ can have even higher T_c values, although there may be experimental challenges in growing these phases.

Results Structure

Inspired by MgAlB_4 , a known superconductor with a T_c of 12 K⁹, we considered layered materials with the structure M-B-Al-B, where M=Mg, Li, Ca, Na or Be, and each layer contains a single type of atom. We considered YCrB_4 type structures, as Tayran *et al.*¹⁰ has shown these to be thermodynamically stable, and also MgB_2 type structures. Only for MgAlB_4 and LiAlB_4 did we find that the MgB_2 -type structure was more stable. Since T_c is usually higher for lighter elements, we chose LiAlB_4 to investigate in more detail.

LiAlB_4 has a honeycomb boron atomic layer that is sandwiched between layers of Li and Al, which is structurally similar to MgB_2 . The optimized structure of LiAlB_4 shows that it crystallizes in the hexagonal P6/mmm space group (No. 191) with Wyckoff positions for atoms at Li (1a) (0,0,0), Al (1b) (0,0,1/2) and B (4h) (1/3,2/3, z_B). Thus, the crystal structure of LiAlB_4 is determined by three different parameters: two crystal lattice parameters (a and c) and one internal parameter (z_B). Full structural parameters are given in Table S2 of the Supplementary Material.

In order to compare different structures with different stoichiometries, we used the binding enthalpy per atom as in Ref.¹¹. This is defined as:

$$\Delta H = \frac{1}{N} \left(E_{\text{total}} - \sum_{\alpha} N_{\alpha} \mu_{\alpha} \right), \quad (1)$$

where E_{total} is the total calculated enthalpy of a particular cell of Li–Al–B system, N is the total number of atoms in the cell, N_{α} is the number of atoms of species α and μ_{α} is the chemical potential of species α . The binding enthalpy of a stable compound is negative, and the results are shown in Fig. 2. Details of the binding enthalpy, lattice parameters and bond lengths are given in Table S2 of the Supplementary Material. In general, the interlayer distance of Li–B is slightly larger than the interlayer distance in MgB_2 , while the Al–B distance is quite small. The boron bonding is strongly anisotropic and similar to graphite.

We find that the LiAlB_4 has the lowest formation enthalpy of all the structures considered in this work, implying that it is more stable. Hence this material is the primary focus of our study. The other ordered phases (see below) are also thermodynamically stable, and might also be realized experimentally under appropriate growth conditions.

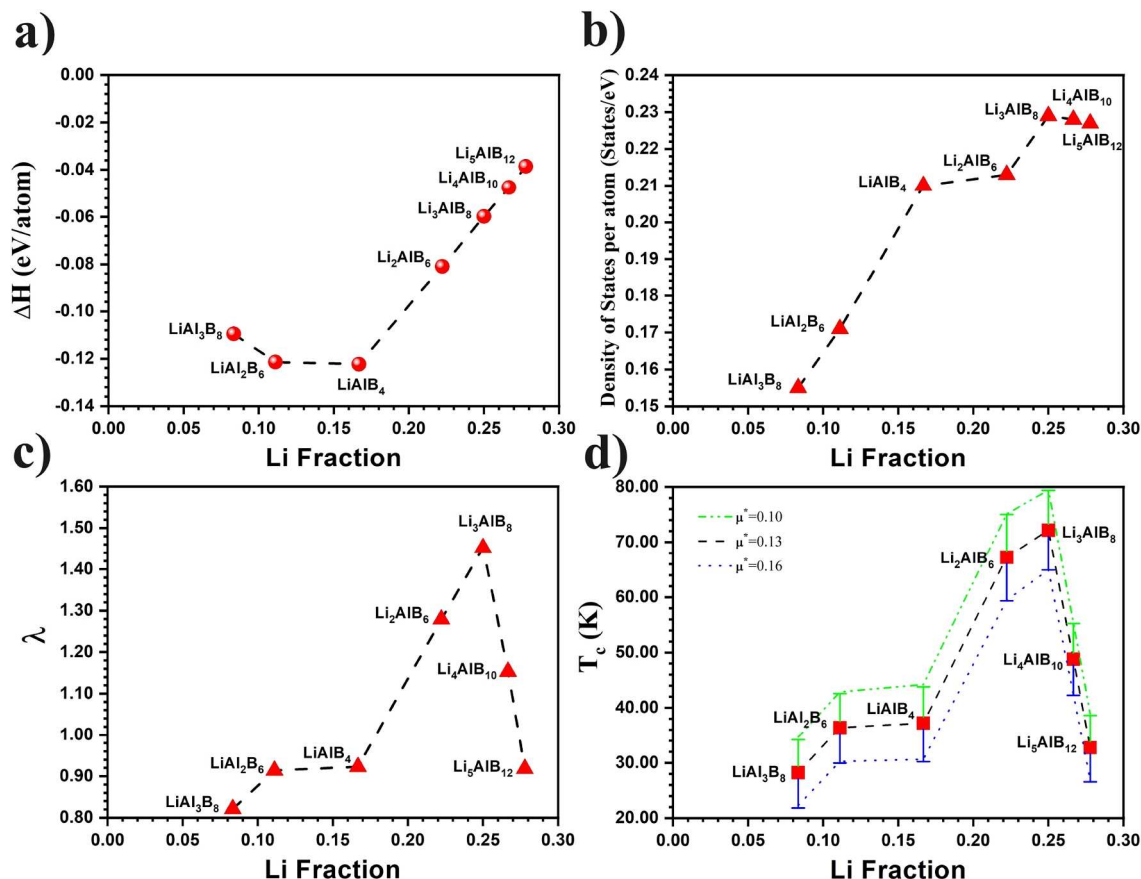


Figure 2. Li fraction dependence of (a) the binding enthalpy, (b) electronic density of states at the Fermi level, (c) average electron-phonon coupling constant (λ), (d) superconducting temperature (T_c) for the likely range of μ^* values (0.10 ... 0.16).

Electronic structure

The electronic properties of LiAlB₄ are given in Fig. 3, including the band structure in the Brillouin zone and the total and partial densities of states (DOS and PDOS). The electronic band structure and DOS of LiAlB₄ are similar to that of its isostructural counterpart MgAlB₄¹¹. It is clear that LiAlB₄ is metallic, with five energy bands crossing the Fermi level at different points (“k-points”) in the Brillouin zone. The LiAlB₄ material has practically no dispersion in the $\Gamma - A$ direction, as expected due to the large separation between boron layers. The band structure of P6/mmm-LiAlB₄ exhibits a quasi-2D character, similar to that of MgB₂. This similarity suggests the possibility of excellent superconductivity, as MgB₂ has three energy bands crossing the Fermi level, whilst LiAlB₄ has five. In addition, MgB₂ has a doubly degenerate flat band near the Fermi level in the $\Gamma - A$ direction, while LiAlB₄ contains two doubly degenerate flat bands. Thus, the electronic density of states at the Fermi level ($N(E_F)$) of LiAlB₄ could be higher than MgB₂. Figure 3 shows the total and partial densities of states for LiAlB₄ to better understand the electronic structure. The PDOS is dominated by the orbital hybridization of B 2p below the Fermi level, indicating strong B-B covalent bonding. In addition, the Al p and B s orbitals below the Fermi level have similar behaviours, suggesting strong bonding between Al-B atoms. Corresponding data for MgB₂ is provided in Fig. S3. of the Supplementary Material.

The electronic density of states at the Fermi level ($N(E_F)$) is crucial for metallic phases and superconductivity, as Cooper pairs of electrons have energies close to the Fermi level. The value of the electron-phonon coupling parameter (λ) is directly proportional to $N(E_F)$, according to the McMillan-Hopfield expression¹²:

$$\lambda = \frac{N(E_F)\langle I^2 \rangle}{\langle M \rangle \langle \omega^2 \rangle} \quad (2)$$

where $\langle \omega^2 \rangle$ denotes the average squared phonon frequency, $\langle I^2 \rangle$ describes the average squared electron-phonon matrix element and $\langle M \rangle$ is the average atomic mass. The density of states (DOS) of LiAlB₄ is determined to be 1.261 states/eV per formula unit, which, as expected, is greater than that of MgB₂ (0.561 states/eV per formula unit). Since the mean mass of LiAlB₄ is also lower than that of MgB₂, the McMillan-Hopfield expression suggests that LiAlB₄ should have a larger electron-phonon coupling parameter (and hence T_c) than MgB₂. The density of states (DOS) in LiAlB₄ and MgB₂ materials is dominated by B 2p states, contributing approximately

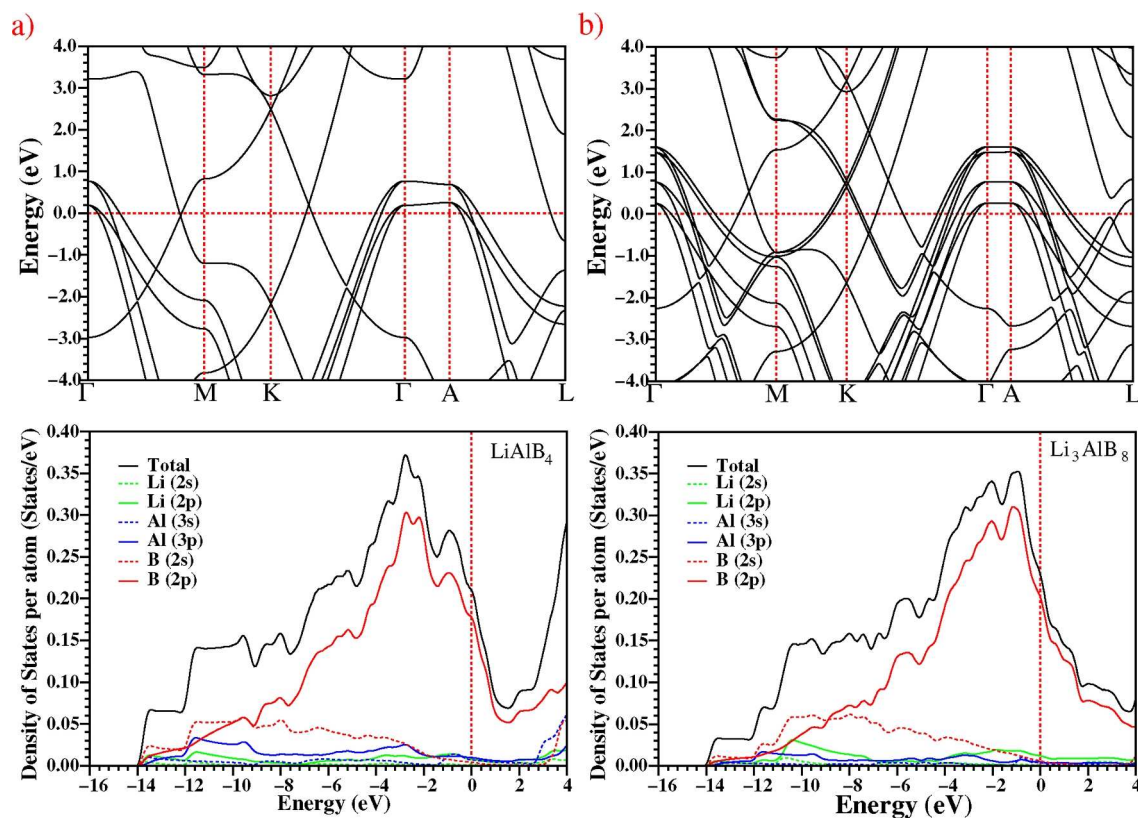


Figure 3. Upper panel: The calculated electronic band structure along the high symmetry directions in the first Brillouin zone; lower panel: calculated total and partial electronic density of states for (a) LiAlB_4 and (b) Li_3AlB_8 .

85% (1.063 states/eV) and 91% (0.511 states/eV), respectively. It is clear that boron atoms play a crucial role in the phenomenon of superconductivity in these materials. The contribution of Li at the Fermi level is negligible.

The Fermi surface sheets and the Brillouin zone of LiAlB_4 are shown in Fig. 4. The four σ -bonding bands cross the Fermi level, as shown in Fig. 3, creating four cylindrical Fermi sheets surrounding the Γ point and along the Γ -A direction. The Fermi surface of the π -band consists of planar honeycomb tubular networks. In quasi-two-dimensional (2D) systems, cylindrical Fermi sheets lead to a strong electron-phonon coupling with a specific phonon mode^{13–15}. The existence of twice as many cylindrical Fermi surfaces in LiAlB_4 , compared to MgB_2 ^{16,17}, also suggests potentially strong electron-phonon coupling. This could lead to an anisotropic, multi-gap superconducting state, as found in MgB_2 . Kafle *et al.* found in their study on Li-B compounds, isostructural to MgB_2 , that the anisotropic Migdal-Eliashberg formalism increased the T_c value by nearly three times compared to the isotropic calculations¹⁸. In this work, we have only used the isotropic approximation, and as such, even higher values of T_c might be found with the anisotropic Migdal-Eliashberg formalism. This would be an interesting topic for further study.

Phonons

The examination of phonon dispersion, total and partial phonon density of states (PhDOS), and electron-phonon spectral function of any superconductor is crucial because they play an important role in superconductivity. The LiAlB_4 compound has a primitive unit cell of six atoms and hence 18 phonon modes, consisting of three acoustic modes and 15 optical modes. The phonon spectrum and PhDOS for LiAlB_4 are shown in Fig. 5; the absence of imaginary frequencies indicates that LiAlB_4 is dynamically stable.

The vibrational modes can be divided into three sections: a low-frequency region up to 9.1 THz; a medium-frequency region ranging from 9.1 to 10.8 THz; and a high-frequency region above 10.8 THz. The low-frequency region, which contains the acoustic and low-frequency optic branches, mainly comprises vibrational modes of Al, with minor contributions from Li and B atoms, at a similar frequency to those found in MgB_2 for Mg-related modes. In the medium-frequency region, Li vibrations are dominant, with a minor contribution from Al-B hybridization. The high-frequency region is formed by the vibrations of B-B atoms. In the 20–27 THz region, two phonon branches (B_{1g} , E_{2g}) originating from B atoms show phonon anomalies in the Γ -M, K- Γ , and Γ -A directions.

The electron-phonon coupling parameters for the E_{2g} phonon mode are significantly larger than those for the other phonon modes, which is similar to MgB_2 . In addition, for LiAlB_4 , the electron-phonon coupling

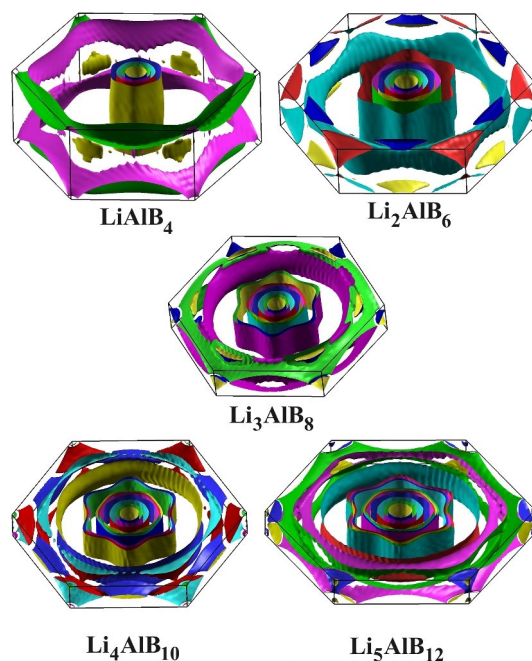


Figure 4. The Fermi surface of $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ for $1 \leq x \leq 5$ and $y = 1$ rendered using XCrySDen³⁵ v1.6.2 from <http://www.xcrysden.org>.

parameter of the A_{1g} and B_{1g} modes, which originate from the B atoms, has a significantly large value at the Γ point. The electron-phonon coupling parameters of IR-active optical phonon modes at the Γ point are zero. A detailed analysis of the optical phonon modes at the zone centre is given in the 'Additional Phonon Analysis of LiAlB_4 ' section of the Supplementary Material.

Our phonon dispersion for LiAlB_4 closely resembles that of MgB_2 ; however, MgB_2 exhibits anomalies just in the doubly degenerate E_{2g} mode^{19–22}. The presence of more phonon anomalies in LiAlB_4 (and multiple flat bands in the electronic band structure along the Γ -A direction) suggests that it may have a larger electron-phonon coupling, and thus a considerably higher T_c .

Superconducting properties

Following from the discussion of vibrational properties, Fig. 5 shows the Eliashberg spectral function ($\alpha^2F(\omega)$) and the frequency variation of the average electron-phonon coupling parameter (λ) for LiAlB_4 . We find λ for LiAlB_4 to be 1.104 and 0.923 with CASTEP and QE (see Table 1), respectively. The difference in λ obtained from the two programs may be due to the different pseudopotentials used and k-point settings (see Method section for details). The phonon modes in the low-frequency region are dominated by Al atoms, contributing 12% to the total λ . The Migdal-Eliashberg theory predicts that low-frequency phonon modes will significantly contribute to the electron-phonon interaction (see Eq. 4); however, this is not the case for the LiAlB_4 material, suggesting that Al atoms do not play an important role in the superconducting mechanism. This is consistent with the findings of Li *et al.* for $\text{Mg}_{1-x}\text{Al}_x\text{B}_2$, where T_c gradually decreased with increasing Al concentration⁹. The phonon density of states exhibits a strong peak related to Li atoms in the narrow frequency range of 9.1 THz to 10.8 THz. This region contributes 10% to the total λ . This medium-frequency contribution is lacking in MgB_2 , for which the Mg-related modes have low coupling. The results suggest that a higher Li ratio will lead to increased λ and, thus, T_c . The contribution of high-frequency phonon vibrations above 10.8 THz, mostly related to the B-B atoms, is 78%, implying that superconductivity in LiAlB_4 is mainly controlled by boron modes, as is also the case with MgB_2 . We can therefore conclude that the origin of superconductivity is similar in each of these compounds. The logarithmic average phonon frequencies calculated with CASTEP and QE are 614.4 and 722.3 K, respectively. As discussed (see 'Validation Study' section in the Supplementary Material), we found the best fit T_c for MgB_2 was with $\mu^* = 0.10$ according to the Allen-Dynes modification of the McMillan formula. Using the same value of μ^* for LiAlB_4 , we predict $T_c = 44.21$ K with QE and 49.39 K with CASTEP. In general, reasonable values for μ^* are in the range 0.10 to 0.16. Using $\mu^* = 0.16$ we find T_c is 30.63 K for LiAlB_4 , which is therefore the lower-limit of theoretically likely values. In addition, we observe that for the other materials studied, T_c decreases as μ^* increases (see Table S3 of the Supplementary Material) as shown in Fig. 2d.

Superstructures

Having demonstrated the superconducting potential of LiAlB_4 , we used the CASTEP genetic algorithm⁷ and its recently developed convex hull functionality⁸ to search the Li-Al-B ternary structure space for other stable structures, with a particular focus on increasing proportions of the lighter Li atoms. A number of

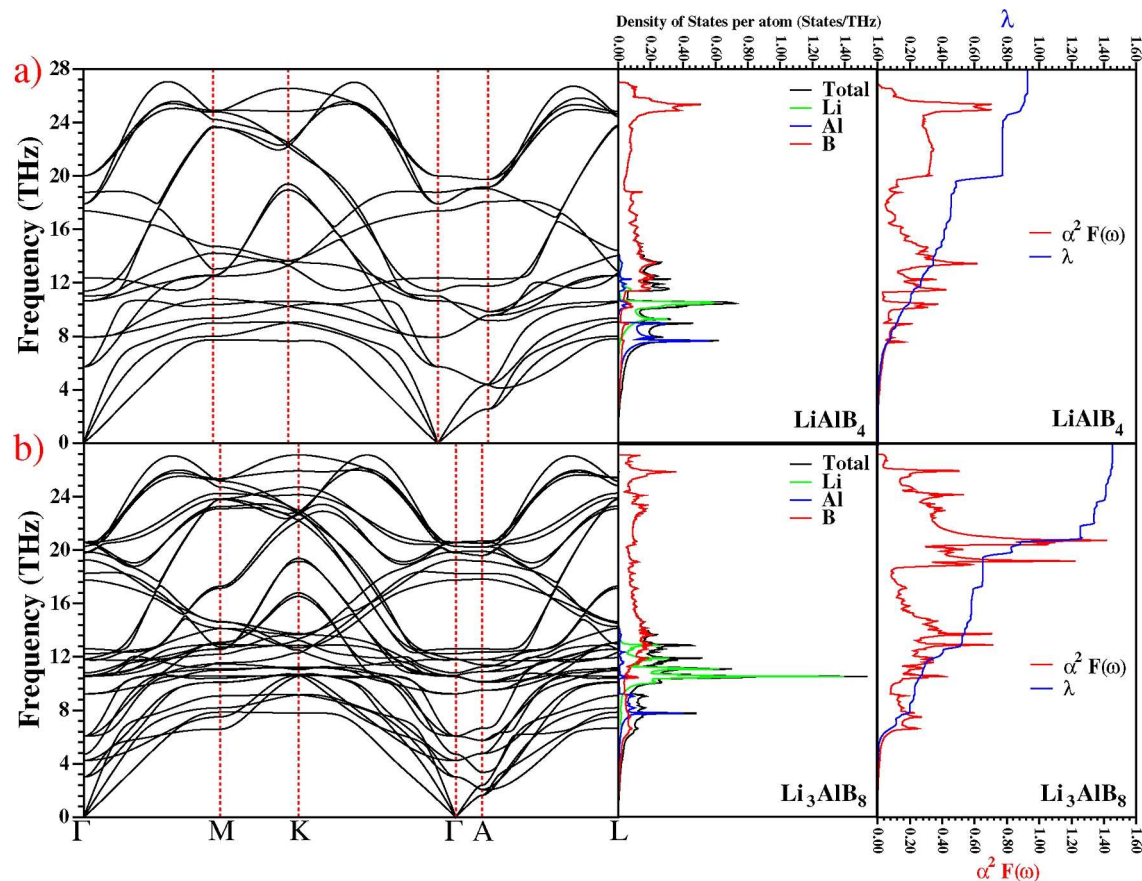


Figure 5. Phonon dispersion curves, total, partial vibrational density of states and the calculated electron-phonon spectral function $\alpha^2 F(\omega)$ (red line) and the variation of the electron-phonon coupling parameter (blue line) with rising frequency $\lambda(\omega)$ for (a) LiAlB_4 and (b) Li_3AlB_8 . Note that the different unit cell parameters of LiAlB_4 and Li_3AlB_8 mean that the spacing of Γ -M etc. is different, and hence the red dashed vertical lines that show the special points in the Brillouin zone do not exactly line up in the (a) and (b) panels.

Material	ω_{1n} (K)	λ	T_c (K) ^a	Eliashberg T_c (K) ^b
AlB_2	476.2	0.529	7.18	4.923
Ref. ²⁷ (GGA with QE)		0.430	3.43	
LiAl_3B_8 (GGA with QE)	702.2	0.821	34.66	38.958
LiAl_2B_6 (GGA with QE)	647.3	0.914	42.87	49.359
LiAlB_4 (GGA with CASTEP)	614.4	1.104	49.39	
LiAlB_4 (GGA with QE)	722.3	0.923	44.21	57.277
Li_2AlB_6 (GGA with QE)	778.2	1.279	75.14	80.604
Li_3AlB_8 (GGA with QE)	718.9	1.452	79.42	88.167
$\text{Li}_4\text{AlB}_{10}$ (GGA with QE)	650.3	1.153	55.38	57.839
$\text{Li}_5\text{AlB}_{12}$ (GGA with QE)	642.4	0.918	38.93	46.266
LiB_2 (GGA with QE)	641.1	0.848	33.71	28.492
Ref. ²⁶ (GGA with QE)	621.0	0.830	31.40	

Table 1. The logarithmic frequency (ω_{1n}), the average electron-phonon coupling parameter (λ) and the superconducting transition temperature (T_c in K) using $\mu^* = 0.10$ for the hexagonal Li–Al–B system and compared with previous theoretical results. ^aValue calculated using standard Allen-Dynes equation. ^b Value calculated using a2Tc with full Eliashberg method

thermodynamically stable candidates of the general form $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ were found, with the same MgB_2 type structure (see Convex Hull GA Section in the Supplementary Material for details). For LiAlB_4 we found that there was very little energy difference between the ‘ordered’ P6/mmm structures, with separate layers of Li and Al, and the ‘disordered’ P6/mmc structures with mixtures of Li and Al in each non-B layer. In this paper, we focus on the ‘ordered’ P6/mmm structures with monatomic Li and Al layers for convenience and to keep the number of structures manageable; however, we note that for $x \geq 2$ the CHGA favoured $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ structures with mixed Li/Al layers (P6₃/mmc structures), which have higher configurational entropy and so could be stabilised further at finite temperatures. Figure 2a shows the variation in binding enthalpy for different possible superstructures in the ordered $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ family, as the Li fraction changes. The lowest formation enthalpy of all was for the LiAlB_4 structure, which suggests that this compound is more stable compared to other Li–Al–B systems, although other ordered phases are possible.

The electronic band structure and Fermi surfaces of these potential superconductors have been investigated in detail, and found to be broadly similar across the $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ ordered family of systems. For each value of x , there are two more bands that cross the Fermi level, and an extra doubly degenerate flat band appears in the $\Gamma - A$ direction. Figure 2b shows the change in $N(E_F)$ per atom as a function of the Li fraction. The highest value of $N(E_F)$ per atom is found in Li_3AlB_8 , which is nearly identical to $\text{Li}_4\text{AlB}_{10}$ and $\text{Li}_5\text{AlB}_{12}$. The Fermi surfaces of these materials are shown in Fig. 4. The circular Fermi sheet originating from $\text{Li}_4\text{AlB}_{10}$ and $\text{Li}_5\text{AlB}_{12}$ is further away from the $\Gamma - A$ direction, indicating a decrease in the electron-phonon interaction along the $\Gamma - A$ direction compared to Li_3AlB_8 . Additionally, the Fermi nesting of Li_3AlB_8 is stronger than the other materials, particularly along the K–M–L direction. The significant Fermi nesting seen in Li_3AlB_8 reveals stronger electron-phonon interactions, potentially resulting in the highest T_c ^{23–25}.

The phonon properties of all $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$, like their electrical properties, show broadly similar characteristics. In Fig. 5a and b, the phonon properties of LiAlB_4 (the most thermodynamically stable) and Li_3AlB_8 (the greatest electron-phonon coupling) are presented. For Li_3AlB_8 , two additional phonon branches in the 20–25 THz range, originating from boron atoms, exhibit phonon anomalies, indicating stronger electron-phonon interactions. As seen in Fig. 5, the electron-phonon coupling parameter of Li_3AlB_8 exhibits a sudden increase from 0.88 to 1.26, contributing 26% to the total λ . All phonon branches for Li_3AlB_8 are approximately 0.2 THz lower compared to those of $\text{Li}_4\text{AlB}_{10}$ and $\text{Li}_5\text{AlB}_{12}$. It is these lower phonon frequencies, combined with a high $N(E_F)$ and strong Fermi nesting, which leads to its strong electron-phonon interactions. In Table 1, we present the λ and T_c values for all materials. As expected, Li_3AlB_8 has the highest T_c , calculated to be 79.42 K, assuming $\mu^* = 0.10$ as before. This value is remarkably higher than that of MgB_2 and notably exceeds the boiling point of liquid nitrogen (77.3 K), highlighting its potential for practical superconducting applications. Whilst this value of μ^* gave the best fit for the T_c of MgB_2 , μ^* is material-dependent, with the common range being from 0.10 to 0.16. We find that increasing μ^* reduces T_c . However, even the largest $\mu^* = 0.16$ gives $T_c = 64.98$ K for Li_3AlB_8 , which is still significantly higher than that of MgB_2 . For completeness, we show the effect of different values of μ^* on T_c in Fig. 2, for all the candidate $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ structures. We also considered the two natural end-point structures, LiB_2 and AlB_2 , both having P6/mmm symmetry. We find that LiB_2 ($T_c = 33.71$ K) has a much higher T_c than AlB_2 ($T_c = 7.18$ K), which is in excellent agreement with previous theoretical values^{26,27}. All the calculated T_c values are given in Table 1.

For all the $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ materials we find $\lambda \geq 0.8$ which corresponds to strong coupling. The usual Allen-Dynes approach to T_c is a weak coupling approximation, and hence we also calculate T_c for all these materials using the full Eliashberg method with C.J. Pickard’s ‘a2Tc’ code. These results are also included in Table 1. For the binary materials, using a2Tc reduces the predicted T_c , and for the ternaries it increases it. This confirms our overall conclusion of unusually high T_c in the Li–Al–B system.

Summary

We have investigated the physical and superconducting properties of stable ordered P6/mmm structures in the Li–Al–B system using first-principles methods. We find that the $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ materials have a lot of promise as ambient pressure superconductors due to their unusually strong electron-phonon coupling. The electron-phonon interaction is studied for the first time using the CASTEP code, and it was found to be consistent with results obtained from Quantum Espresso. Our results indicate that $\text{Li}_x\text{Al}_y\text{B}_{2(x+y)}$ compounds are thermodynamically and dynamically stable. Notably, our results show that LiAlB_4 is the most stable and has $T_c = 44.21$ K, whilst Li_3AlB_8 has the highest superconducting critical temperature with $T_c = 79.42$ K with $\mu^* = 0.10$, surpassing even liquid nitrogen temperatures. This promising result underscores the need for experimental validation of our results.

Method

The binding enthalpy for each different structure was evaluated in *ab initio* calculations using density functional theory (DFT) in the CASTEP code⁴ using the PBE approximation²⁸ and norm-conserving pseudopotentials²⁹. Following convergence tests, the CASTEP PBE calculations used a $27 \times 27 \times 12$ **k**-point Monkhorst-Pack (MP) grid with a plane-wave cut-off energy of 900 eV and a grid size of $2G_{max}$ [except for the high-throughput CASTEP-GA calculations, which used a slightly lower plane-wave cut-off energy of 700 eV for speed]. The electronic properties were calculated with a fine **k**-point MP grid of $54 \times 54 \times 24$, while phonon properties were calculated using Density Functional Perturbation Theory³⁰ on a $9 \times 9 \times 4$ **q**-point MP grid with $27 \times 27 \times 12$ **k**-points. The phonon interpolation was carried out across 10,000 Fermi surface points and the electron-phonon coupling calculation on 243 **q**-vectors linking Fermi surface points.

With the CASTEP code, we find $T_c = 49.39$ K for LiAlB_4 . A confirmatory calculation of the same structure with the Quantum Espresso (QE) code utilizing finer parameters (60 Ry cutoff for wave functions and 600 Ry for

charge density, a $32 \times 32 \times 16$ MP grid for the ground state and $40 \times 40 \times 20$ MP grid for electronic and Fermi surface calculations) produced $T_c = 44.21$ K.

To calculate the superconducting properties, we use the Migdal-Eliashberg approach^{31,32}, as outlined in other works, e.g. Ref.²⁵. This formalism has recently been implemented³³ in CASTEP and was used to calculate the electron-phonon interaction and hence the critical temperature (T_c). In this formalism, the Eliashberg spectral function¹² is described as follows:

$$\alpha^2 F(\omega) = \frac{1}{2\pi N(E_F)} \sum_{qj} \frac{\gamma_{qj}}{\hbar\omega_{qj}} \delta(\omega - \omega_{qj}), \quad (3)$$

where $N(E_F)$ is the electron density of states per atom and spin at the Fermi level, and α is the average of all phonons with energy ω in the BZ. The average electron-phonon coupling constant is determined by^{12,34}:

$$\lambda(\omega) = 2 \int_0^\infty \frac{\alpha^2 F(\omega')}{\omega'} d\omega'. \quad (4)$$

The value of $\lambda(\omega)$ is then used to determine the logarithmic average phonon frequency (ω_{ln}) using

$$\omega_{ln} = \exp \left(2\lambda^{-1} \int_0^\infty \frac{d\omega}{\omega} \alpha^2 F(\omega) \ln \omega \right). \quad (5)$$

Finally, the Allen-Dynes modification of the McMillan formula is used with these values of λ and ω_{ln} to determine the superconducting transition temperature T_c :

$$T_c = \frac{\omega_{ln}}{1.2} \exp \left(-\frac{1.04(1 + \lambda)}{\lambda - \mu^*(1 + 0.62\lambda)} \right), \quad (6)$$

where μ^* represents an effective screened Coulomb repulsion parameter. The value of μ^* typically ranges from 0.10 to 0.16 in most studies^{12,34}. We use $\mu^* = 0.10$ for all materials in this study, as this gave the best fit to experimental values of T_c for MgB₂ - see 'Validation Study' section and FIG. S1 in the Supplementary Material for details.

Data Availability

The data created and analysed during the current study are available from <https://doi.org/10.15124/f7a8d4f7-2f7b-4992-a84d-3dbeec36b995>

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Author contributions

All authors co-wrote the paper. KH performed the CASTEP DFT calculations and EK performed the QE DFT calculations. SD wrote the code for the convex hull search and performed the calculations to identify the candidate structures. PJPB wrote the CASTEP electron-phonon code and superconductivity analysis scripts. PJH gave theoretical and computational insights and guidance, and MIJP conceived and designed the study.

Additional information

Supplementary Information The online version contains supplementary material available at <https://doi.org/10.1038/s41598-024-84542-6>.

Correspondence and requests for materials should be addressed to M.I.J.P.

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