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# Effect of Nanoscale Defects on the Thermal Conductivity of Graphene

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## Abstract

There are remarkable theoretical efforts geared towards understanding the impact of fabrication-induced defects on the operational behaviour of a single layer graphene. These studies have been focused mainly on atomic defects, while nanoscale pinholes and patches of two layers thick (bilayer) attached on a monolayer graphene are inevitable during the synthesis process. In this work the influence of these nanoscale defects on the graphene thermal conductivity is studied via non-equilibrium molecular dynamics simulations. The thermal conductivity of a single layer zigzag and armchair oriented graphene is modelled capturing the effect of voids and bilayer imperfections. A single layer graphene sheet with a size of 50 nm × 10 nm is analysed having an elliptical defect of up to 6 nm (major axis). Our results exhibit a reduction of over 20 % in thermal conductivity with increasing temperature and about 75 % drop with increasing void size. The decrease in the thermal conductivity is 15 % for the single layer graphene with a bilayer defect of 6 nm in diameter. This study demonstrates a dramatic influence of defect shape on the thermal conductivity of graphene, where defects with elliptical shapes demonstrate a higher thermal transfer in graphene compared to circular ones. This work provides a guideline of how to quantify the effect of fabrication induced defects on thermal conductivity of graphene.

*Keywords:* Graphene, Thermal Conductivity, Pinhole, Bilayer, Molecular Dynamics

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## 1. Introduction

Graphene – as a 2D sheet of carbon atoms arranged in a honeycomb lattice – has introduced unique properties with a wide range of applications in bioengineering [1], electronics [2], energy storage [3] and composite structures [4–6]. In addition to superior electrical conductivity and mechanical strength [7, 8], an outstanding thermal conductivity has been reported for the single layer graphene [9, 10]. This raises attentions to use graphene for multi-functional purposes. For example, graphene is utilised in batteries as an electrode to enhance device performance as well as thermal management applications [11, 12]. Although the extreme thermal conductivity of graphene can be obtained for the perfect crystal structure without defects [9, 10, 13], porosities in graphene — as an electrode — improve ions and electrons transports in energy storage devices [14]. Furthermore, defects are inevitable during the synthesis and integration processes [15–17], which have profound influence on the thermal conductivity of graphene. This has inspired many studies to understand the thermal behaviour of defective graphene-based structures.

Experimental measurements have demonstrated a wide range of thermal conductivity for the single layer graphene [9, 10, 18], which is attributed to various parameters including substrate, size and defects [13, 19]. Those defects mainly include point vacancies, impurities, and dislocations [15, 20]. In addition to those atomic scale defects, nanoscale pinholes and multi-layer regions are other imperfections, which can be imposed during the manufacturing processes [16, 21–24]. Those defects can be induced intentionally as well

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18 for nanoengineering purposes. For example, nanoporous graphene has offered numerous applications in the  
19 field of sensing and energy storage [12, 14, 25]. Therefore, taking into account the influence of defects on the  
20 thermal conductivity of graphene has become the motivation of various studies. Experimental observations  
21 report a dramatic decrease in the thermal conductivity of defective graphene [26]. To support experimental  
22 studies, theoretical approaches have been used widely to understand the impact of defects on the thermal  
23 behaviour. Molecular dynamics (MD) simulations are found to be a useful tool among various theoretical  
24 techniques to model the thermal conductivity of graphene [27–29].

25 A series of studies has employed MD simulations to understand the thermal transfer in graphene with  
26 various defects. This includes vacancies [27, 30], Stone-Wales (SW) [31, 32] and nitrogen doping [33] de-  
27 fects, which generally reduce the thermal conductivity of graphene with different intensities. In addition to  
28 those crystal imperfections, recent studies focus on the effect of voids on the thermal behaviour of graphene  
29 [34]. Although those works have examined the thermal conductivity of graphene with atomic imperfections,  
30 scale effect is the primary challenge to understand the physical behaviour of nanostructures [35]. A high  
31 density nanoscale pinhole defects with a wide range of diameters of 1 nm to 10 nm has been observed during  
32 the graphene synthesis processes [21]. Moreover, few-layer regions form during the fabrication monolayer  
33 graphene — especially in epitaxial processes — with significant impacts on the physical behaviour through  
34 structural non-uniformity [16, 36, 37]. For example, thermal annealing the substrate during epitaxial pro-  
35 cesses can initiate a new graphene layer before a complete formation of the first layer on the entire surface  
36 [16, 38]. Step edges on the substrate is another reason to create bilayer regions in single layer graphene  
37 sheets [36]. Moreover, a non-uniform exfoliation process leaves bilayer defects in monolayer graphene [16, 39].  
38 While atomic-scale defects have been the centre of attention for most of theoretical works so far [27, 30–34],  
39 the effect of those nanoscale defects on the graphene thermal transport necessitates to be addressed to bridge  
40 the gap between atomic and micro-scale defects. This work uses atomic simulations to understand the effect  
41 of nanoscale pinholes (voids) and bilayer regions on the thermal conductivity of the single layer graphene.  
42 Non-equilibrium MD (NEMD) method is carried out along the zigzag and armchair orientations of graphene  
43 sheets at the temperature in a range of 100 K to 500 K. This study will present the theoretical framework of  
44 the NEMD method. Then, void and bilayer defects will be studied focusing on the size effect on the thermal  
45 transport. After comparing with atomic scale defects, this study will be concluded with a discussion on the  
46 effect of void and bilayer shape on the thermal behaviour of graphene.

## 47 2. Simulation Methods

48 This work employs MD simulations to study the effect of voids and bilayer defects on the thermal  
49 conductivity of graphene. The optimized Tersoff potential [40] is used in LAMMPS code [41] to model the  
50 thermal transport along zigzag and armchair directions. Graphene sheets with size of 50 nm × 10 nm are  
51 considered with circle shape defects (void or bilayer region) at the centre in a diameter of  $D$  as shown in Fig.  
52 1. Those nanoscale defects can form during the graphene synthesis processes [16, 21, 36]. The considered  
53 simulation dimensions are an average graphene sheet size for theoretical studies [31, 42, 43]. Lennard-  
54 Jones potential [44] is used to model the interaction between inter-layers in bilayer defects (inset in Fig.1  
55 (b)). Periodic boundary condition is applied along  $x$ - and  $y$ -directions to represent graphene sheets rather  
56 than graphene nanoribbons. In this study, NEMD method is utilised to measure the thermal conductivity at  
57 temperature of 100 K to 500 K, which is the major framework among theoretical simulations on the graphene  
58 thermal analysis [27, 30–34]. In this method, carbon atoms at two ends of graphene sheets are fixed to avoid  
59 from sublimating (grey shaded atoms in Fig. 1). Then, other atoms are divided into sub-groups along the  
60 longitudinal direction ( $x$ -direction). The first sub-group is considered as the cold reservoir, while the last  
61 sub-group is assigned as the hot reservoir (inset in Fig.1 (a)). All simulations are carried out with a time  
62 step of 1 fs. The graphene sheets were first relaxed using canonical (NVT) ensemble by the Nose-Hoover  
63 thermostat for 100 ps. This is followed by applying a temperature difference along  $x$ -direction. In this step,  
64 the temperature of atoms in the cold reservoir is reduced for 10 K, while the temperature of atoms in the  
65 hot reservoir is increased for 10 K. This impose a temperature difference of  $\Delta T = 20$  K between reservoirs  
66 through NVT ensemble, where atoms in the remaining sub-groups are maintained under constant energy

67 (NVE) for 3 ns. This work studies the thermal conductivity of zigzag and armchair graphene sheets, which  
 68 have been studied mainly through theoretical investigations [13]

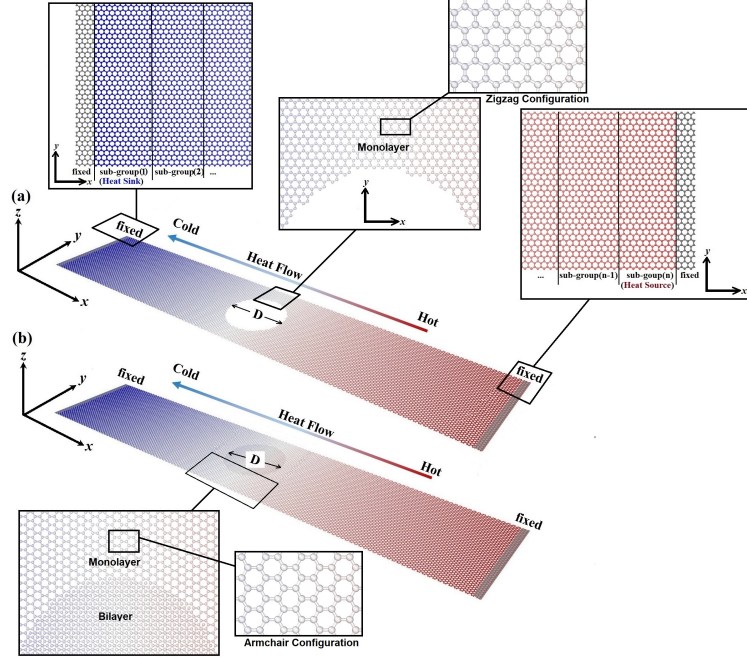


Figure 1: Schematic of NEMD model to evaluate the thermal conductivity of single layer graphene sheets having nanoscale (a) void, and (b) bilayer defects, with a diameter of  $D$ . The close-ups in panel (a) demonstrate sub-groups and assigned heat source and heat sink with an inset to void defect in zigzag chirality. The close-up in panel (b) presents bilayer region in monolayer armchair graphene.

69 To maintain a temperature difference at both ends of graphene sheets in a steady-state condition, the  
 70 added energy into the hot reservoir should be the same amount as the energy removed from the cold reservoir.  
 71 The rate of the change of the energy transferred between those sources over time is estimated as the heat  
 72 flux,  $q_x$ . Then, the thermal conductivity,  $\kappa$ , is calculated based on the Fourier law for one-dimensional  
 73 structures as

$$74 \quad q_x = -\kappa A_c \frac{dT}{dx} \quad (1)$$

75 where  $\frac{dT}{dx}$  is the temperature gradient and  $A_c$  is the cross-sectional area of the structure. Temperature of  
 76  $i^{th}$  sub-group,  $T_i$ , is computed as

$$77 \quad T_i = \frac{2}{3Nk_B} \sum_j \frac{p_j^2}{2m_j} \quad (2)$$

78 where  $p$  is the momentum,  $m$  is atomic mass,  $N$  and  $k_B$  are number of carbon atoms in this sub-group and  
 79 the Boltzman constant, respectively. Here the thickness of the single layer graphene is considered as  $3.4 \text{ \AA}$   
 80 [27, 33]. In the remainder of this work, the thermal conductivity of pristine graphene without any defects is  
 81 first calculated for temperature of 100 K to 500 K. Then, the influence of defects on the thermal transport  
 82 will be studied for graphene sheets. This work will be concluded by discussing the effect of void and bilayer  
 83 shapes on the thermal behaviour of graphene.

### 3. Results and Discussions

The thermal conductivity of pristine graphene,  $\kappa_0$ , is studied first through using NEMD method. Fig. 2 exhibits the thermal conductivity of defect-free zigzag and armchair graphene sheets at the temperature in a range of 100 K to 500 K compared with previous works [18, 28, 34, 42]. In the first instance, a thermal conductivity in a range of 400  $W/Km$  to 550  $W/Km$  is obtained for defect free graphene sheets, which is comparable the thermal conductivity reported through previous experimental [18] and theoretical studies with the same interatomic potential [28, 34, 42]. The thermal conductivity reduces with increasing temperature for both orientations, while a higher thermal transport is obtained for the zigzag chirality. Although some works predict isotropic thermal conductivity for graphene [45, 46], a higher thermal conductivity in zigzag chirality has been reported for monolayer graphene as well [27, 31–33, 42]. Here, the thermal conductivity of zigzag graphene is found to be 8-20% higher than those armchair sheets, while this anisotropy in the thermal conductivity of graphene nanoribbons can reach to 50% reported in previous studies [27, 32]. This chirality effect is attributed to the phonon scattering rates at the armchair and zigzag edges due to the finite size, where the graphene flake size is less than the phonon mean free path [13, 27]. Similar temperature effect has been reported previously through experimental [9, 13] and computational [13, 33] studies. This reduction in the thermal conductivity can be attributed to the phonon-phonon and phonon-boundary scatterings at higher temperatures [13]. After calculating the thermal conductivity of defect-free graphene, the influence of voids and bilayer defects (Fig. 1) on the thermal transport of graphene sheets is studied through NEMD simulations. In this regard, the heat flux and temperature gradient are analysed to understand the contribution of defects on the thermal behaviour.

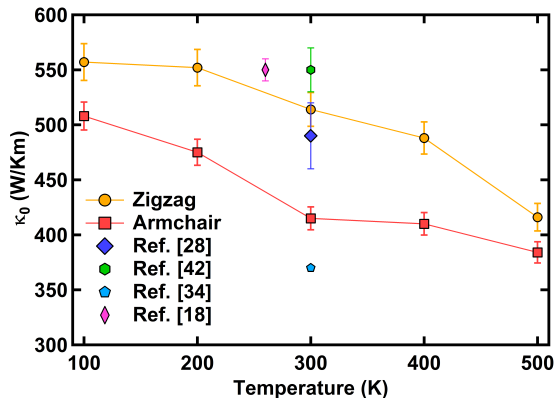


Figure 2: The thermal conductivity of the zigzag and armchair oriented pristine (defect-free) graphene as a function of temperature. To compare with previous studies, results from Ref. [18, 28, 34, 42] are presented.

Fig. 3 shows the amount of energy added to the hot reservoirs and removed from the cold reservoirs of the zigzag graphene sheets with voids and bilayer defects at 100 K. In the first instant, regardless of defects, results exhibit a same energy value exchanged between atoms in the heat source and heat sink regions. The energy exchange has a linear trend over the simulation time, which represents a steady-state heat flux and energy conservation during the simulations. Fig. 3 exhibits a different impact from voids and bilayer defects into the energy exchange of graphene sheets. Although bilayer defects have a negligible effect on the heat flux, increasing the void diameter reduces the amount of energy exchanged between the hot and cold reservoirs. The heat flux changes from 0.77  $eV/ps$  to 0.58  $eV/ps$  with increasing the void diameter from 2 nm to 6 nm. The same effect from voids and bilayer defects on the heat flux was observed for the armchair chirality and higher temperatures.

After calculating the heat flux, the temperature distribution along the longitudinal direction of graphene sheets is estimated for the steady-state condition through using Eq. (2). Fig. 4. demonstrates the temperature profile of the zigzag oriented defective graphene sheets at temperature of 100 K. A part from reservoirs at both ends, the temperature gradient demonstrates a linear trend along the pristine graphene,  $(dT/dx)_P$ .

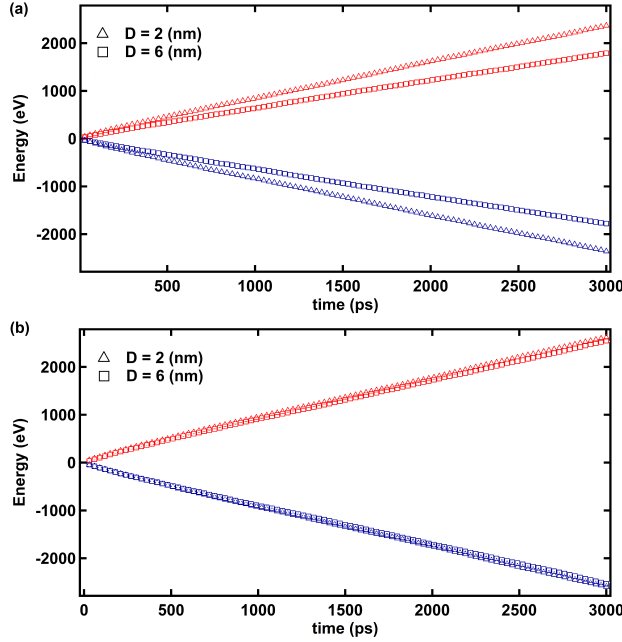


Figure 3: Energy added to hot reservoirs, red marks, and removed from cold reservoirs, blue marks, at a temperature of 100 K for the zigzag graphene sheets having (a) void and (b) bilayer defects with a diameter of  $D$ .

118 Although this linear trend has a higher gradient at the void regions,  $(dT/dx)_V > (dT/dx)_P$ , the temperature  
 119 gradient at other locations is the same as the pristine graphene. This implies a different thermal conductivity  
 120 in slabs at the void position than the groups of atoms without any defect. In contrast, bilayer regions  
 121 change the temperature gradient along graphene through inducing a spike at the temperature profile. The  
 122 temperature gradient for defect-free graphene is estimated through fitting linear trend approached following  
 123 previous works [31–34, 42, 43], while temperature difference divided by the defect length is used to calculate  
 124 the temperature gradient in defect regions as suggested previously for local nonequilibrium transports [47].  
 125 After predicting the temperature gradient and heat flux, the thermal conductivity of defective graphene  
 126 sheets is calculated as a combination of pristine slabs and a defect region by using the Fourier law in Eq.  
 127 (1).

128 Fig. 5 shows the void size effect on the thermal conductivity of graphene at temperature of 100 K  
 129 500 K compared with atomic scale defects [31–33]. The thermal conductivity of defective graphene was  
 130 normalised by the thermal conductivity of pristine graphene,  $\kappa_0$ . An overall analysis exhibits a reduction  
 131 of the thermal conductivity with increasing the pore size. Results demonstrate a change in the normalised  
 132 thermal conductivity from 0.7 to 0.27 with increasing the void diameter from 2 nm to 6 nm at temperature  
 133 of 100 K. This change in the thermal conductivity of defective graphene depends on the temperature for  
 134 either chirality. For example, the normalised thermal conductivity of the zigzag graphene sheets with  
 135 voids in a diameter of 2 nm raises from 0.7 to 0.84 through changing temperature from 100 K to 500 K,  
 136 while this change for the armchair graphene is negligible for the temperature more than 300 K. Therefore,  
 137 in addition to temperature, the pore size effect on the thermal conductivity depends on the chirality of  
 138 graphene as well. Now let us compare those results with previous studies on atomic-scale defects, which  
 139 are mainly missing atoms or bonding distortions distributed in the lattice structure of graphene observed  
 140 through experimental examinations [48]. A reduction of the thermal conductivity of graphene about 75 %  
 141 was reported in the presence of 1 % Stone-Wales or bivacancy defects [31, 32], which is comparable with the  
 142 thermal conductivity of graphene sheets with a void in a diameter of 6 nm representing a defect density of  
 143 5.6%. A similar change in the thermal conductivity were reported for graphene with 3 % nitrogen atoms [33].  
 144 This indicates a severe impact on the thermal conductivity from induced atomic defects during fabrication

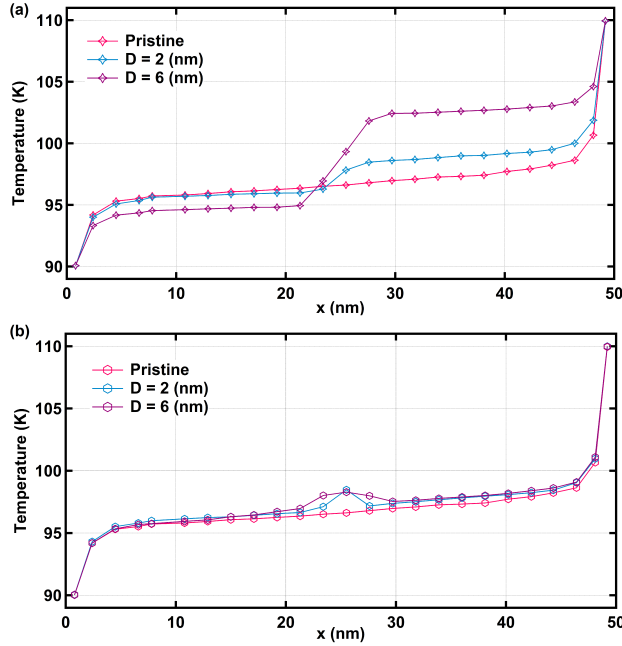


Figure 4: Temperature profile in a steady-state heat transfer at temperature of 100 K along the zigzag graphene sheets having (a) void and (b) bilayer defects with a diameter of  $D$ .

145 processes compared to nanoscale voids. The significant difference between atomic-scale defects and nanoscale  
 146 ones on the thermal conductivity of graphene can be discussed through various aspects. The impact of defect  
 147 distribution on the thermal transport parameters —including temperature gradient and heat flux (Eq. 1)  
 148 —is one aspect to be considered. For example, the temperature gradient in defect regions is different than  
 149 those with the perfect crystal structure of graphene. Atomic-scale defects are distributed along graphene  
 150 sheets [30–32, 34], while, in contrast, nanoscale defects are constrained in one region as shown in Fig. 1.  
 151 Therefore, distributed atomic-scale defects in graphene constitutes more changes along the thermal gradient  
 152 compared to those nanoscale pinholes. The phonon transport is another aspect to be considered to explain  
 153 the difference between atomic-scale defects and nanoscale ones on the thermal behaviour of graphene, which  
 154 will be discussed in the following.

155 Now we proceed with the incorporation of bilayer defects on the thermal conductivity of graphene. In this  
 156 study, atomic interactions in each graphene layer are modelled through using the optimised Tersoff potential  
 157 [40], while Lennard-Jones [44] is used to model carbon interactions between graphene layers. The Lennard-  
 158 Jones potential for interlayer interactions is found to be weak to model bilayer defects with a diameter of  
 159 2 nm at a temperature more than 100 K. The influence of bilayer defects on the thermal conductivity of  
 160 the single layer graphene is analysed based on the defect size and temperature. First, the size effect is  
 161 studied at temperature of 100 K (Fig. 6 (a)). The thermal conductivity of zigzag graphene reduces about  
 162 5 % with increasing the defect diameter to 4 nm. This change raises to 13 % for a bilayer defect with a  
 163 diameter of 6 nm. For the armchair chirality, independent of the bilayer defect size, a reduction about 15  
 164 % is observed for the thermal transfer of graphene sheets. While, similar to voids (pinholes), bilayer defects  
 165 reduce the thermal conductivity of graphene, the impact of bilayer defects on the thermal behaviour of  
 166 graphene is significantly less than void defects (Fig. 5). After analysing the bilayer defect size, the effect of  
 167 temperature on the thermal transport is studied for graphene sheets having bilayer defects with a diameter of  
 168 6 nm (Fig. 6 (b)). In the first instance, results demonstrate that raising temperature reduces the impact of  
 169 bilayer defects on the thermal behaviour of graphene for either chirality. A normalised thermal conductivity  
 170 about 0.85 is obtained for defective graphene sheets at temperature of 100 K, while the thermal transport  
 171 changes to about the thermal conductivity of defect-free graphene at temperature of 500 K. Although the

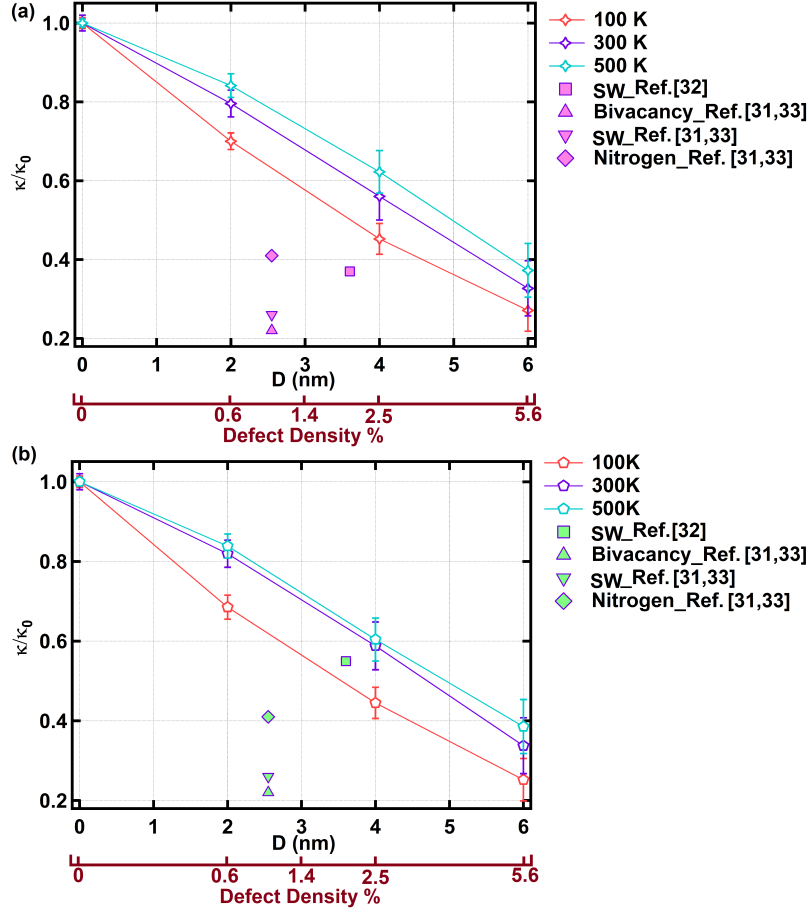


Figure 5: Normalised thermal conductivity of the (a) zigzag and (b) armchair graphene as a function of void size for temperature of 100 K to 500 K. Defect density for each diameter is indicated on an unscaled red axis. Results compared with atomic-scale defects including 2 % Stone-Wales (SW), 1 % Bivacancy and 1 % Nitrogen defects at temperature of 300 K from Ref. [31–33].

172 thermal behaviour of multi-layers graphene was studied previously [42], here, for the first time, the influence  
 173 of bilayer defects on the thermal transfer of the single layer graphene is investigated as a function of size.  
 174 Increasing temperature reduces the impact of bilayer defects on the thermal conductivity, where a similar  
 175 behaviour has been obtained for void defects as well (Fig. 5). This temperature effect has been observed  
 176 on the thermal behaviour of defective graphene sheets through previous studies, which is attributed to the  
 177 dominance of phonon-defect scattering compared to phonon-phonon scattering [32, 43, 49].

178 The thermal conductivity of graphene with a perfect crystal structure is controlled by phonon-phonon  
 179 scattering, known as intrinsic. Defects in graphene change the thermal transport through extrinsic effects  
 180 of phonon-defect scattering [13]. One can compute the number of vibrational states per unit frequency,  
 181 called density of state (DOS), to evaluate the phonon scattering in defective graphene, which is frequently  
 182 used to explain the thermal conductivity of graphene with atomic-scale defects [30, 31, 33]. An overall  
 183 analysis on the mechanism of thermal transfer in graphene sheets with void and bilayer defects can be  
 184 obtained through phonon DOS computations. The phonon spectrum is calculated by Fourier transform of  
 185 the velocity autocorrelation function during the steady-state condition [50] as

$$186 \quad DOS(\omega) = \frac{1}{\sqrt{2\pi}} \int e^{-i\omega t} \langle v(t)v(0) \rangle dt \quad (3)$$

187 Here  $\omega$  is the frequency and  $v$  is the velocity of carbon atoms. Fig. 7 demonstrates DOS for defect-free

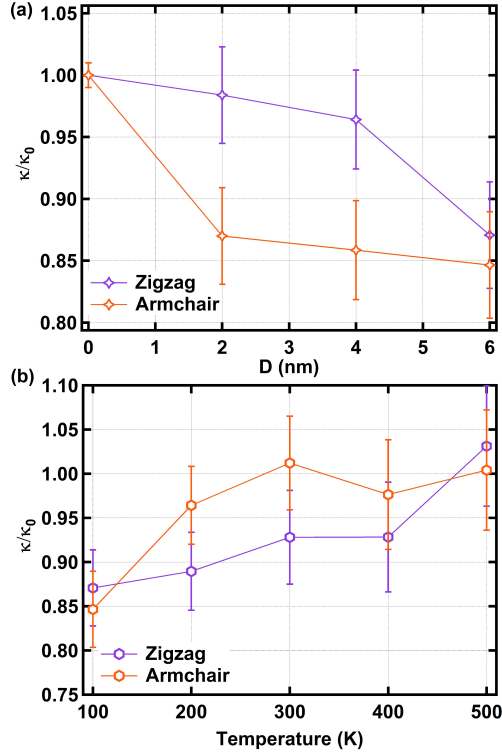


Figure 6: Normalised thermal conductivity of graphene sheets with bilayer defects (a) as a function of the bilayer defect size at temperature of 100 K, (b) with a diameter of 6 nm as function of temperature.

188 graphene and graphene sheets having void and bilayer defects with a diameter of 6 nm at temperature of  
 189 500 K. Those computations were performed for the zigzag chirality. The pristine graphene exhibits two  
 190 main peaks at frequencies around 12 THz and 50 THz representing ballistic thermal transport. A similar  
 191 spectrum is obtained for the graphene sheet with a bilayer defect. While DOS for both defect-free and  
 192 bilayer defect graphene sheets are identical, low frequency peak is enhanced significantly at the graphene  
 193 sheet with a void defect. This can be linked to the scattering of phonons through defects in graphene [20],  
 194 which leads to the reduction of graphene thermal conductivity. Fig. 7 exhibits a slight damping about 12  
 195 % in the main peak at 50 THz in the graphene sheet with void defect. This damping of the main peak is  
 196 reported to be significant due to atomic scale defects [31, 33]. Therefore, the severe effect of atomic defects  
 197 compared to nanoscale ones (demonstrated in Fig. 5) on the graphene thermal conductivity can be linked to  
 198 the intensity of phonon scattering. The insignificant change of the thermal conductivity in graphene sheets  
 199 due to the presence of bilayer regions as observed in Fig. 6 can be traced back to the low collision of  
 200 phonons, similar to the ballistic thermal transport in defect-free graphene.

201 The influence of void and bilayer defects on the thermal behaviour of graphene has been discussed so far  
 202 for circular shape, while nanoscale defects (voids and bilayer regions) with oval shapes have been observed  
 203 during the fabrication processes [16, 24, 36, 37, 51]. Moreover, recent studies highlight the importance  
 204 of pore shape on the physical behaviour of nanomaterials [52, 53]. Void and bilayer shape effects on the  
 205 thermal conductivity of graphene are studied for elliptical profile. Here, NEMD method is used to model  
 206 the thermal conductivity of graphene sheets with horizontal ellipse (H-ellipse) and vertical ellipse (V-ellipse)  
 207 defects as shown in Fig. 8, where the defect density is the same as those with circular shape in a diameter of  
 208 6 nm. This leads to a defect density, defined as the density of defect over the density of defect-free graphene  
 209 sheet, of 5.6 %. The H-ellipse and V-ellipse defect shapes stand for the major axis of the ellipse aligned and  
 210 orthogonal to the heat flow direction ( $x$ -direction), respectively.

211 Fig. 9 exhibits the effect of void and bilayer shape on the thermal conductivity of graphene. An overall

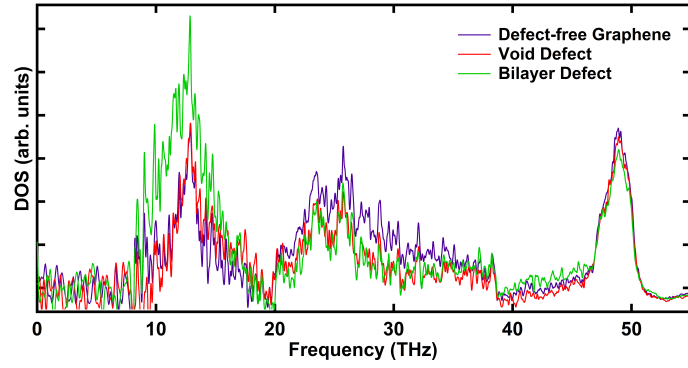


Figure 7: Phonon spectra of graphene sheets with (a) defect-free structure, (b) void and (c) bilayer defects in a diameter of 6 nm in the zigzag chirality at temperature of 500 K.

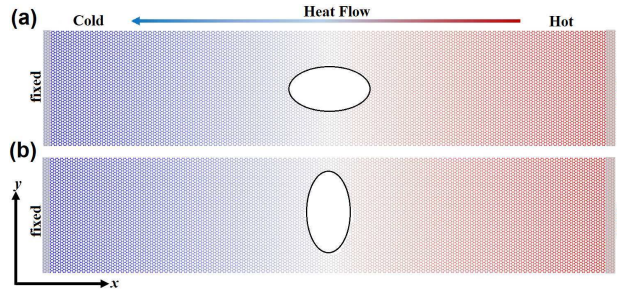


Figure 8: Schematic of NEMD model to calculate the thermal conductivity of single layer graphene with nanoscale (a) H-ellipse, and (b) V-ellipse defects with a defect density of 5.6 %.

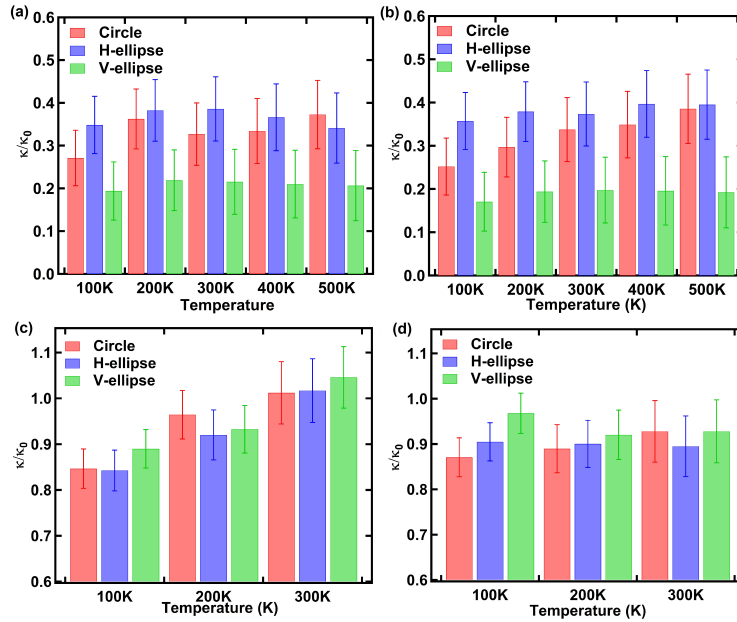


Figure 9: Normalised thermal conductivity as a function of temperature for the zigzag graphene with (a) void and (c) bilayer defects, and the armchair graphene with (b) void, (d) bilayer defects in different shapes of circle, H-ellipse and V-ellipse with the same defect density.

analysis demonstrates a significant defect shape effect on the thermal transfer. Starting from void defects, a lower thermal conductivity is obtained for the V-ellipse shape in either chirality, while the H-ellipse shape has the utmost thermal conductivity for both zigzag and armchair directions (Fig.9 (a) and (b)). The scenario of the defect shape is completely different for bilayer defects, where the V-ellipse shape exhibits a higher thermal conductivity compared to those with H-ellipse and circular shapes. A higher thermal conductivity in the H-ellipse pore shape compared to the V-ellipse and circle shapes was reported previously for defective graphene [34]. Defect shapes can be controlled during the fabrication processes to optimise the physical properties of graphene [24, 51, 54]. Although this work focus on the thermal transport in graphene with defects in circular and elliptical shapes based on experimental observations [16, 24, 36, 37, 51], studying other defect shapes remains for further investigations. Here a nanoscale defect in graphene sheets is modelled to study the thermal behaviour, while experimental observations have presented a range of nanoscale defects with various shapes distributed across graphene sheets [16, 21–24]. Multiscale modelling approaches can be used to model the thermal transfer of graphene sheets with randomly distributed defects through further studies [55].

#### 4. Concluding remarks

This work addresses the impact of nanoscale void and bilayer defects on the thermal behaviour of graphene sheets. Here NEMD computations are used to study defect size effects on the zigzag and armchair oriented graphene. Although findings exhibit a reduction on the thermal conductivity of graphene sheets with increasing the defect size, the thermal transfer is more sensitive with voids compared to bilayer defects. The change in the thermal conductivity of defective graphene is found to be less through raising temperature due to the dominance of phonon-defect scattering compared to phonon-phonon scattering. Here results are compared with previously presented atomic-scale defects, which indicates a dramatic influence of atomic defects on the thermal conductivity compared to nanoscale voids due to a higher phonon scattering. This raises attention on the development of fabrication process more on atomic defects [16, 48]. After studying the defect size, this work investigates the influence of nanoscale defect shapes on the thermal behaviour of graphene, which demonstrates a significant defect shape effect with a higher thermal conductivity in elliptical shapes compared to circular ones with the same defect density. This can be linked to defect projected area perpendicular to the heat flow direction [34]. This study sheds light on defective graphene for engineering design in manufacturing process as well as multifunctional purposes.

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