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Theory of momentum-resolved magnon electron energy loss spectra: The case of Yttrium Iron Garnet

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We explore the inelastic spectra of electrons impinging in a magnetic system. The methodology here presented is intended to highlight the charge-dependent interaction of the electron beam in a STEM-EELS experiment, and the local vector potential generated by the magnetic lattice. This interaction shows an intensity 10^{-2} smaller than the purely spin interaction, which is taken to be functionally the same as in the inelastic neutron experiment. On the other hand, it shows a strong scattering vector dependence (κ^{-4}) and a dependence with the relative orientation between the probe wavevector and the local magnetic moments of the solid. We present YIG as a case study due to its high interest by the community.

Keywords: Spintronics, Magnonics, antiferromagnetic, yttrium iron garnet, YIG

I. INTRODUCTION

For quite some time, Moore's Law, especially the concern about its potential end, has driven research into new computing approaches beyond traditional CMOS technology. One approach that has attracted attention is to use the spin degree of freedom to substitute or integrate with the current electronic computation. To this objective, magnonics has been extensively studied, it encompasses the study of fundamental properties of magnons, which are quanta of the dynamic eigen-excitation of magnetically ordered materials in the form of spin-waves [1][2].

To systematically investigate the generation, manipulation, and identification of spin-waves, or magnons, there is a requisite focus on improving the methodologies for both exciting and probing these phenomena. Magnons are commonly studied by inelastic neutron scattering (INS) techniques, time-resolved Kerr microscopy [3], and Brillouin light scattering (BLS) [4]. While these techniques probe the energy-momentum dispersion of magnons with high energy resolution, their spatial resolution is fundamentally limited to hundreds of nanometres.

Over the past decade, meV-level STEM-EELS has made significant strides, achieving atomic-level contrast[5], detecting spectral signatures of individual impurity atoms [6], and conducting spatial- and angle-resolved measurements on defects in crystalline materials [7].

The method's potential expansion into studying magnons is anticipated due to the overlapping energy range with vibrational modes in solid-state materials. Despite the weaker interaction of magnetic moments with the electron beam compared to the Coulomb potential, by up to 3 or 4 orders of magnitude, which makes their detection challenging, [8][9] recent advancements in hybrid-pixel detectors, leading to a drastic improvement in the dynamic range and low background noise, with signals a mere 10^7 of the full beam intensity readily detectable [10], and improved monochromator and spectrometer design, resulting in increased energy resolutions in particular at lower acceleration voltages (4.2meV at 30kV [11]), offer enhanced sensitivity and signal detection, making the exploration of magnon excitation feasible in experimental settings.

Theoretical approaches for evaluating the EEL spectra have focused on spin-polarized probes and Low-energy

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electrons in a surface reflection geometry (REELS), in bulk materials. In our case we will explore the effects of non-spin-polarized beam in the meV-level STEM-EELS apparatus, using YIG as a prototypical material, accounting for the electron's interaction with the vector potential produced by the magnons in the system.

II. METHODS

The evaluation of the inelastic scattering of electrons by magnons requires the evaluation of the doubly differ-

$$\frac{d^2\sigma}{d\Omega d\mathbf{k}_1} = \frac{1}{N} \frac{N_0 V \sum_{n_0, n_1} P_{n_0} \mathbf{k}_1^2 |\langle n_1, \mathbf{k}_1 | H_{inter} | n_0, \mathbf{k}_0 \rangle|^2 \delta(E_{n_0} + E_0 - E_{n_1} - E_1)}{(2\pi)^2 \hbar(j_0)_z} \tag{1}$$

where we are denoting a scattering process where the system undergoes a transition from state n_0 to n_1 with energies E_0 and E_1 , respectively, simultaneously the scattered particle changed its momentum from k_0 with energy E_0 to k_1 with energy E_1 . The interaction between the particle and the material is encapsulated by the interaction Hamiltonian H_{inter} , while the current density of the particle beam along the z-direction is denoted by $(j_0)_z$. Here, P_{n_0} signifies the probability of the material to be in state n_0 before any scattering event. While N, represents the number of statterers, N_0 is the number of particles in state k_0 , and V is the volume of the unit cell.

The choice of H_{inter} is the central point of the discussion. In our case, we are interested in the interaction of an electron beam with the magnetic structure of the system. Disregarding the charge, the problem returns to a similar situation as to the INS, the usual interaction is taken in terms of an interaction between the magnetic field generated by the intrinsic magnetic moment of the electrons and the orbital angular momentum. This interaction leads to an exchange-like term and a term involving the sample's electron motion. In the case of orbital quenched systems only the former terms is taken in account. In our approach, the interaction will be assumed to be given by the vector potential deriving from the magnons in the solid and its effect on the canonical momentum of the passing probe electrons. This interaction is only present in the case of electrons as a probe. We will then focus on the methodological development of this contribution to the total EELS by magnons.

The interaction can be written by ignoring the weaker \hat{A}^2 terms and assuming orbital quenching, we have [12],

$$H_{inter} = i\left(\frac{\mu_0 \mu_B^2}{\pi}\right) \sum_j \left[\hat{S}_j \times \frac{\mathbf{r} - \mathbf{r}_j}{|\mathbf{r} - \mathbf{r}_j|^3}\right] \cdot \nabla_r \qquad (2)$$

where we have the spin operator in site N is given by \hat{S}_i , μ_B is the Bohr magneton and μ_0 is the permeability

of free space.

With a semi-classical approach to the spin operators, justified by assuming that S >> 1, we can note our spins in the laboratory frame as:

$$\mathbf{S}_i = S(\sin\theta_i \cos\phi_i, \sin\theta_i \sin\phi_i, \cos\theta_i) \tag{3}$$

with θ being the polar angle in spherical coordinates and ϕ the azimuthal angle. We can perform a transformation to the local reference frame of the spin, given by:

$$\mathcal{R}_{j}^{-1} = \begin{pmatrix} \cos\theta_{j}\cos\phi_{j} & -\sin\phi_{j} & \sin\theta_{j}\cos\phi_{j} \\ \cos\theta_{j}\sin\phi_{j} & \cos\phi_{j} & \sin\theta_{j}\sin\phi_{j} \\ -\sin\theta_{j} & 0 & \cos\theta_{j} \end{pmatrix}$$

$$= \begin{pmatrix} A_{11}^{j} & A_{12}^{j} & A_{13}^{j} \\ A_{21}^{j} & A_{22}^{j} & A_{23}^{j} \\ A_{31}^{j} & A_{32}^{j} & A_{33}^{j} \end{pmatrix}$$

$$(4)$$

Which allows us to write $\overline{\mathbf{S}}_i = \mathbf{U}_i \cdot \mathbf{S}_i$. In this notation, $\overline{\mathbf{S}}_i$ refers to the local reference frame and \mathbf{S}_i is the laboratory reference frame. Hence we can substitute in our interaction Hamiltonian $\mathbf{S}_i = \mathbf{U}_i^{-1} \cdot \overline{\mathbf{S}}_i$, such that,

$$H_{inter} = i\left(\frac{\mu_0 \mu_B^2}{\pi}\right) \sum_j \left[\mathcal{R}_j^{-1} \cdot \overline{\mathbf{S}}_j \times \frac{\mathbf{r} - \mathbf{r}_j}{|\mathbf{r} - \mathbf{r}_j|^3} \right] \cdot \nabla_r$$
(5)

Assuming that the scattering particle doesn't interact with the system before or after the scattering event, i.e., no multiple scattering events, we can write the total wave function as a product between a plane wave and the magnetic states,

$$|\mathbf{k}_{\mathbf{i}}, n_i\rangle \to |\mathbf{k}_{\mathbf{i}}\rangle|n_i\rangle$$
 (6)

for i = 0, 1. Here we have, $|\mathbf{k}_i\rangle = e^{-ik_i \cdot r}$ being the state of the probing beam, while $|n_i\rangle$, represents the state

of the solid, which for our purposes is only transiting between magnetic states, such that $H_0|n_i\rangle = E_i|n_i\rangle$ with H_0 being the Heisemberg Hamiltonian.

To further our analysis, let's focus on the interaction term. Substituting (2) in the Fermi's Golden rule present in (1), while taking (6) into account we have,

$$\langle n_0, \mathbf{k}_0 | H_{inter} | n_1, \mathbf{k}_1 \rangle = \left(\frac{\mu_0 \mu_B^2}{\pi}\right) \langle n_1 | i \int \sum_j e^{-i(\mathbf{k}_1 - \mathbf{k}_0) \cdot \mathbf{r}} \\ \left[\left(\mathcal{R}_j^{-1} \cdot \overline{\mathbf{S}}_j \right) \times \frac{\mathbf{r} - \mathbf{r}_j}{|\mathbf{r} - \mathbf{r}_j|^3} \right] \cdot \mathbf{k}_0 d\mathbf{r} | n_0 \rangle$$

$$\tag{7}$$

taking the integral over $d\mathbf{r}$ which is the same as taking the Fourier transform, where we used the result,

$$FT\left[\frac{\mathbf{r}-\mathbf{r}_j}{|\mathbf{r}-\mathbf{r}_j|^3}\right] = \frac{2i\mathbf{q}}{q^2}e^{i\mathbf{q}\cdot\mathbf{r}_j} \tag{8}$$

where we defined $\mathbf{q} = (\mathbf{k}_1 - \mathbf{k}_0)$. Then the summation over *j* results in a discrete Fourier transform of the spinoperators, leading to the result,

$$\langle n_0, \mathbf{k}_0 | H_{inter} | n_1, \mathbf{k}_1 \rangle = -\left(\frac{\mu_0 \mu_B^2 \sqrt{N}}{\pi}\right) \langle n_1 | \sum_r e^{-i\mathbf{q} \cdot \mathbf{r}_r} \\ \left[\left(\mathcal{R}_r^{-1} \cdot \overline{\mathbf{S}}_q^{(r)} \right) \times \frac{2\mathbf{q}}{q^2} \right] \cdot \mathbf{k}_0 | n_0 \rangle$$

$$(9)$$

where the summation over r labels the sum of magnetic moments in the lattice within the unit cell. Finally, we will use the Holstein-Primakoff transformation in the spin-wave approximation, with S_r as the magnitude of the spin angular momentum, given by, in Fourier space,

$$\begin{cases} S_q^{x(r)} &= \frac{\sqrt{2S(r)}}{2} \left(a_q^{(r)} + a_q^{\dagger(r)} \right) \\ S_q^{y(r)} &= \frac{\sqrt{2S(r)}}{2i} \left(a_q^{(r)} - a_q^{\dagger(r)} \right) \\ S_q^{z(r)} &= S^{(r)} - a_q^{\dagger(r)} a_q^{(r)} \end{cases}$$
(10)

Noting that $a_q^{\dagger(r)}|n_0\rangle = \sqrt{N_q + 1}|n_1\rangle$ while $a_q^{(r)}|n_0\rangle = 0$. In this sense we have two separate contributions to the spectra, one coming from the creation of a magnon and

one from the destruction of one, referring to the possibility of Stokes and anti-Stokes scattering, note that with this $S_q^{z(r)}$ doesn't contribute to the inelastic scattering process. Focusing on Stakes scattering only we will only keep the creation operators. Finally, for a general unit cell for both colinear and non-colinear spin-structures, the application of the creation and annihilation operators presume a diagonal Hamiltonian, hence we need to make sure that we have a consistent diagonalisation method for all these cases. To achieve this we will use the method outlined in [13][14][15]. In the case of the Heisenberg Hamiltonian in the second quantization under the spinwave approximation, we can write,

$$H_2 = v_{\mathbf{q}}^{\dagger} \cdot \mathbf{L} \cdot v_{\mathbf{q}} \tag{11}$$

where we defined:

$$v^{\dagger} = (a_{\mathbf{q}}^{(1)\dagger}, ..., a_{\mathbf{q}}^{(M)\dagger} | a_{-\mathbf{q}}^{(1)}, ..., a_{-\mathbf{q}}^{(M)})$$
(12)

We diagonalize L(q) with the unitary transformation $L'(q) = UL'(q)U^{\dagger}$, where U^{\dagger} is a matrix which columns are the eigenvectors of L, this allow us to write:

$$H_2 = \vec{v}^{\dagger} U^{\dagger} U \mathbf{L} U^{\dagger} U \vec{v} = w^{\dagger} L' w \tag{13}$$

having defined $w^{\dagger} = \vec{v}^{\dagger} U^{\dagger}$ given by:

$$w^{\dagger} = (\alpha_{\mathbf{q}}^{(1)\dagger}, ..., \alpha_{\mathbf{q}}^{(M)\dagger} | \alpha_{-\mathbf{q}}^{(1)}, ..., \alpha_{-\mathbf{q}}^{(M)})$$
(14)

while in real space we have:

0

$$u_{\mathbf{q}}^{(r)} = \sum_{m=1}^{M} \left(U_{r,m}^{\dagger}(\mathbf{q}) \alpha_{\mathbf{q}}^{(m)} + U_{r,m+N}^{\dagger} \alpha_{-\mathbf{q}}^{\dagger(m)} \right)$$
(15)

$$a_{-\mathbf{q}}^{\dagger(r)} = \sum_{m=1}^{M} \left(U_{r+N,m}^{\dagger} \alpha_{\mathbf{q}}^{(m)} + U_{r+N,m+N}^{\dagger} \alpha_{-\mathbf{q}}^{\dagger(m)} \right) \quad (16)$$

with all these definitions in place, we can write (9) as,

$$\langle n_0, \mathbf{k}_0 | H_{inter} | n_1, \mathbf{k}_1 \rangle = -\left(\frac{\mu_0 \mu_B^2 \sqrt{N}}{\pi q^2 V}\right) \sum_{r=1}^M \sum_{m=1}^M \sqrt{2S_{(m)} \left(N_q^{(m)} + 1\right)} e^{-i\mathbf{q}\cdot\mathbf{r}_r} \left[\varepsilon_{\alpha\beta\gamma} \left\{V_{r\beta}^- U_{r,m+N}^\dagger + V_{r\beta}^+ U_{r+N,m+N}^\dagger\right\} q_\gamma\right] k_{0d}$$

$$= -\left(\frac{\mu_0 \mu_B^2 \sqrt{N}}{\pi q^2 V}\right) \mathcal{S}'(n_0, \mathbf{k}_0 \to n_1, \mathbf{k}_1)$$

$$(17)$$

where we used Einstein's summation rule, where repeat-

ing Greek indexes are summed, for the vector opera-

tions, with $\varepsilon_{\alpha\beta\gamma}$ the Levi-Civita epsilon, defined $\mathcal{S}'(n_0,$ $\mathbf{k}_0 \rightarrow n_1, \mathbf{k}_1$) as a short-hand notation for the summation terms, and n_0 and n_1 define the state of the solid without a magnon (ground state) and after the production of a magnon by the probe, respectively. We also defined,

Finally using $(j_0)_z = \frac{N_0}{V} \frac{\hbar k_0}{m}$ and $dE_1 = \frac{\hbar^2 k_1}{m} dk_1$ we can write (1)

$$V_{r\alpha}^{\pm} = (\mathcal{R}_r)_{x\alpha} \pm i(\mathcal{R}_r)_{y\alpha} \tag{18}$$

 $\pm i(\mathcal{D})$

$$\frac{d^2\sigma}{d\Omega dE_1} = \left(\frac{\mu_0 \mu_B^2 m}{2\hbar^2 \pi^2}\right)^2 \frac{1}{q^4} \frac{k_1}{k_0} \sum_{n_0, n_1} P_{n_0} |\mathcal{S}'(n_0, \mathbf{k}_0 \to n_1, \mathbf{k}_1)|^2 \delta(E_{n_0} + E_0 - E_{n_1} - E_1)$$
(19)

(10)

the coupling where constant, inthis case. $(\mu_0 \mu_B^2 m/2\hbar^2 \pi^2)^2 = 0.002$ Barn. Note that similarly to the case of inelastic scattering of electrons by phonons, the magnon case exhibits a q^{-4} dependence which, paired with the q^2 dependence of $\mathcal{S}'(n_0, \mathbf{k}_0 \rightarrow n_1,$ \mathbf{k}_1) give an overall dependence of q^{-2} . Hence, corroborating with the discussion in [16] we expect the signal to be strongest in the first Brillouin zone, in contrast with the cases when neutrons or photons are used, where the data has a stronger signal for larger q.

In the next section, we will compare EELS as an inelastic probe of magnons, and inelastic neutron scattering (INS) which is a well-regarded probing method for momentum-resolved analysis of quasi-particle dispersion relations [17].

For our analysis, we will use YIG as a prototypical material for study, due to the high interest of the community in its Thz magnons capability and high free-path length.

For the calculation of the underlying magnon dispersion, we will use the exchange parameters proposed from fitting inelastic neutron scattering in [18].

Note that, for the third nearest neighbours, there are two possibilities of exchange parameters J_{3a} and J_{3b} . These two exchange paths are dissimilar and can be distinguished due to the symmetry of the crystal when rotated about the bond vector. The J_{3a} exchange path exhibits a 2-fold symmetry, while the J_{3b} exchange path obey the higher D3 symmetry point group.

For the inelastic neutron scattering calculation, we used the method described in [13], where the double-cross section is given by,

$$\frac{d^2\sigma}{d\Omega d\omega} = \left(\frac{\gamma e^2}{m_e c^2}\right)^2 \left[\frac{g}{2}f(\kappa)\right]^2 \frac{k_f}{k_i} \sum_{\alpha,\beta} \left(\delta_{\alpha\beta} - \frac{\kappa_\alpha \kappa_\beta}{\kappa^2}\right) S_{\alpha\beta}(\kappa,\omega)$$
(20)

where $(\gamma e^2/m_e c^2)^2 = 0.291$ barns is the coupling constant of the neutron to the unpaired electron spins (note the use of cgs units), g is the Landé factor, and $f(\kappa)$ is the magnetic form factor. We also define κ , which is the scattering vector, such that $\kappa = k_f - k_i$, which is the difference in momentum of the incoming and out-

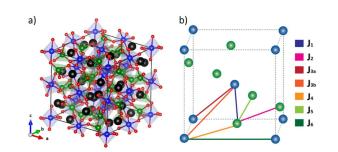


FIG. 1: Crystal structure and magnetic exchange paths in Yttrium Iron Garnet (YIG). The conventional unit cell of YIG is represented,

with the majority tetrahedral sites marked in green and the minority octahedral sites in blue. Yttrium is

depicted as black spheres, and oxygen as red spheres. The first octant of the YIG unit cell is shown,

highlighting the two distinct Fe3+ sites: tetrahedral sites in green and octahedral sites in blue [18].

going neutrons. Using the notation q for the momentum of the magnons, we have the relation $\kappa = \mathbf{G} + q$, with \mathbf{G} a reciprocal lattice vector.

We point out that the coupling constant for EELS is two orders of magnitude larger than the neutron's. This difference is counteracted by the flux of particles in the two experiments. The neutron scattering experiment has a typical flux of 10^{14} neutrons cm⁻²s⁻¹ [19], which is 10^5 times lower than the typical 10^{19} electrons cm⁻²s⁻¹[20] in an electron microscope, leading to a lower exposition time required by the EELS experiment compared to the JNS.

III. RESULTS

In figure 2 we compare the experimentally acquired INS given in [18] with the calculated INS using Eq. 20 and the calculated charge-only EELS using Eq. 19. We can see the similarities between the experiment and the

calculated spectra for the INS, and compared with the EELS, the same modes are active. Under the discussion made before, both the intensities given in the figures 2-b and 2-c coexist in the EELS spectra. The main differences between the interaction forms, arise from the q dependence and the dependence between the intensity with the angle between the beam orientation and the local magnetic moments' orientation.

Taking the definition of the spin orientation given in 3, we will keep $\phi = 0$ and change the value of θ . In figure 2 we kept the orientation of the magnetic moments aligned with oriented parallel to the axis of $\theta = \pi/2$ and $\phi = 0$, while the electron/neutron beam is kept along the z-axis.

In figure 3 we see a strong dependence on the magnetic moments orientation. Here we see that the proposed interaction shows a dependence of the intensity as we change the polar angle θ of the orientation magnetic moments axis of orientation. In the path $\Gamma - H$ the intensity varies with a cossine relation with the angle between the spin and the beam angles.

IV. CONCLUSION

The proposed methodology is intended to facilitate the distinction of magnon-related pecks in the EELS exper-

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iments when paired with the evaluation of the phonon EEL spectrum. The high spatial resolution united with the magnetic moment orientation sensitive nature of the non-spin polarized EELS spectrum, and given the difference in q dependence, a particular choice of spectra taken from different, but related, scattering vectors can be used to probe local differences in the orientation of the Curie/Neel vector relative to the electron beam momentum.

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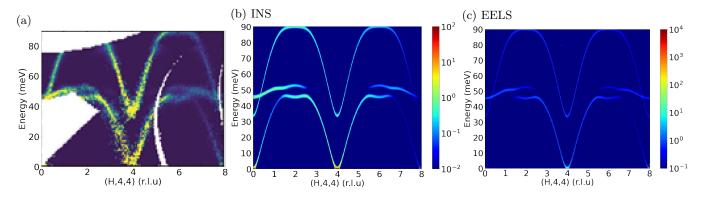
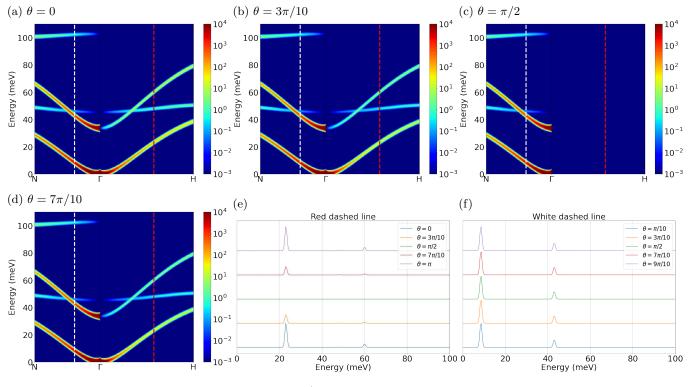


FIG. 2: Inelastic scattering by magnons: a) Experimental inelastic neutron scattering [18], b) theoretical evaluation of inelastic neutron scattering,

c) charge-related EELS. All the calculations were performed for a relative angle between the probe's wave vector and the Nèel vector $\theta = \pi/2$.





for varying relative angles θ between the probe's wave vector and the Nèel vector. e-f) Angle dependent intensity for a particular point in momentum space,

showing a strong angle dependence on the point represented by the red dashed line,

but not on the point represented by the white dashed line.