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Ades, A. E., Welton, N J, Dias, Sofia orcid.org/0000-0002-2172-0221 et al. (2 more authors) (2024) Twenty years of network meta-analysis:continuing controversies and recent developments. Research Synthesis Methods. jrsm.1700. ISSN: 1759-2887

https://doi.org/10.1002/jrsm.1700

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HISTORICAL REVIEW



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Twenty years of network meta-analysis: Continuing controversies and recent developments

A. E. Ades | Nicky J. Welton | Sofia Dias | David M. Phillippo | Deborah M. Caldwell¹

Correspondence

A. E. Ades, Population Health Sciences, Bristol Medical School, 38 Whatley Road, Bristol BS8 2PS, UK.

Email: t.ades@bristol.ac.uk

Abstract

Network meta-analysis (NMA) is an extension of pairwise meta-analysis (PMA) which combines evidence from trials on multiple treatments in connected networks. NMA delivers internally consistent estimates of relative treatment efficacy, needed for rational decision making. Over its first 20 years NMA's use has grown exponentially, with applications in both health technology assessment (HTA), primarily re-imbursement decisions and clinical guideline development, and clinical research publications. This has been a period of transition in meta-analysis, first from its roots in educational and social psychology, where large heterogeneous datasets could be explored to find effect modifiers, to smaller pairwise meta-analyses in clinical medicine on average with less than six studies. This has been followed by narrowly-focused estimation of the effects of specific treatments at specific doses in specific populations in sparse networks, where direct comparisons are unavailable or informed by only one or two studies. NMA is a powerful and well-established technique but, in spite of the exponential increase in applications, doubts about the reliability and validity of NMA persist. Here we outline the continuing controversies, and review some recent developments. We suggest that heterogeneity should be minimized, as it poses a threat to the reliability of NMA which has not been fully appreciated, perhaps because it has not been seen as a problem in PMA. More research is needed on the extent of heterogeneity and inconsistency in datasets used for decision making, on formal methods for making recommendations based on NMA, and on the further development of multi-level network meta-regression.

KEYWORDS

heterogeneity, inconsistency, medical decision making, network meta-analysis, populationadjustment, systematic review

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¹Population Health Sciences, Bristol Medical School, Bristol, UK

²Centre for Reviews and Dissemination, University of York, York, UK

Highlights

What is already known

- It is commonly stated that network meta-analysis relies on three assumptions (homogeneity, similarity, and consistency), that it is vulnerable to confounding like observational studies, and that direct evidence is more reliable that indirect evidence.
- A fourth assumption, transitivity, has been introduced, which requires that trials are similar in all respects apart from the treatments.
- Methodological and reporting guidelines emphasise a range of a posteriori checks on whether assumptions regarding consistency and transitivity are met.
- Heterogeneity is often tolerated or regarded as inevitable, or even desirable: to be considered in the same way as in pairwise meta-analysis.

What is new

- Exchangeability is the single assumption underlying both pairwise and network meta-analysis, but it is difficult to detect departures from it in practice, let alone verify it.
- The exchangeability assumption imposes no limit on the extent of quantitative heterogeneity.
- Heterogeneity increases the expected absolute error in pairwise comparisons, indirect comparisons, and NMA, and may introduce inconsistency between direct and indirect estimates, even when exchangeability is satisfied. This effect is due to second-order sampling variation.
- The risk of such realized error and inconsistency increases with between-studies standard deviation, and if treatment comparisons are directly informed by fewer trials.
- Most direct comparisons in treatment networks are informed by only one or two trials.

Potential impact for RSM readers

- When making recommendations based on NMA, robustness to bias, heterogeneity and inconsistency in the evidence should be checked where possible by threshold analysis. Alternatively, in clinical studies, CINeMA software can be used to reveal the impact on estimates of particular items of data.
- Every effort should be made to reduce quantitative heterogeneity, by carefully
 specifying the target population, by modelling and adjusting for study-related
 and reporting biases, by appropriately synthesizing outcomes reported in different ways and times, by avoiding treatment "lumping," and when possible by
 using multi-level network meta-regression to model and control for differences
 in patient characteristics.

1 | INTRODUCTION

Some twenty years have passed since Lumley¹ introduced the term "network meta-analysis" (NMA), referring to an extension of pairwise meta-analysis (PMA) to connected networks of randomized trial evidence, such as the network of A versus B, A versus C, A versus D, A versus E, B versus D, C versus D, illustrated in Figure 1. A 2018 bibliometric analysis² showed an exponential growth,

recording some 2850 publications in 771 journals and in 6 languages, from over 350 institutes in 85 countries; 82% were from the USA, China, and the UK. NMA has become a core methodology in comparative effectiveness research and in health technology assessment (HTA).

Forms of network meta-analysis had appeared before Lumley's 2002 paper,^{3–5} including in the 1992 Confidence Profile Method.⁶ The most commonly used model is that of Higgins and Whitehead.⁷ Their objective was to

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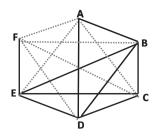


FIGURE 1 A connected network of trials on six treatments A, B, C, D, E, and F. Trial evidence (solid lines) exists on 9 of the 15 possible pairwise contrasts, AB, AD, BC, BD, BE, CD, CE, DE, EF. The remaining contrasts (dashed lines) are informed by indirect evidence. It would be possible to obtain *direct* estimates $\hat{d}_{AB}^{Dir}, \hat{d}_{AD}^{Dir}, \hat{d}_{BC}^{Dir}, \hat{d}_{BC$

strengthen inference on a single relative effect by introducing external indirect evidence, but their model extends readily to any number of treatments in any connected network of trials.^{8–10}

The 20th anniversary of NMA is a good moment to reflect on the state of the field. In spite of its widespread and growing use, many tutorial papers, texts, and commentaries continue to express doubts about its validity and reliability. There are also conflicting views on fundamental issues such as whether NMA evidence should be viewed as "observational," and thus whether it estimates causal effects or just associations. Further, while Lumley's original model allowed for inconsistency between direct and indirect evidence, the majority of applied work has assumed consistency, in spite of empirical evidence that inconsistency is prevalent in typical networks. New models and parameterizations have appeared, 20,21 some in response to these findings.

The trickle of negative commentary is now impacting on patients: during stakeholder consultations on draft guidelines for treatments for depression, issued by the National Institute of Health and Care Excellence (NICE) in the UK, 23 Members of Parliament signed a motion describing NMA as "a flawed methodology," and 45 stakeholder organizations called it "an experimental technique" and pressed NICE not to base recommendations on the results from NMA. ²³

In this paper we reflect on areas of controversy that remain after the first 20 years of explosive growth in the use of NMA, suggesting possible resolutions, and reviewing new developments. We begin with a brief summary of what NMA is, and then give some context on the way NMA has been used in practice. We focus on issues of principle and interpretation, including assumptions, validity of inferences, and reliability. Some additional content appears in Supplementary Materials. We make no attempt to duplicate practical guidance already available. 16,24-31

Areas for further research are suggested throughout.

2 | WHAT IS NMA?

How should one analyse data from a connected network of trials, such as the one shown in Figure 1? The objective is to identify the best of the six treatments A, B, C, D, E, and F in a specific target population. We might consider a pairwise meta-analysis (PMA) on each of the nine sets of trials on which direct evidence is available: this would generate a series of unrelated relative treatment effect estimates $\hat{d}_{AB}, \hat{d}_{AC}, \hat{d}_{AD}, \hat{d}_{BC}, \dots \hat{d}_{DE}$. However, we cannot determine the best treatment from these estimates as they lack coherence: in any given group of patients, and for any three treatments, the true treatment effects must obey the relationship $d_{AC} = d_{AB} + d_{BC}$, on an appropriate scale. Unrelated estimates of each pair of treatments do not have this property, which is essential for rational decision-making. NMA is a method that delivers a set of coherent estimates that have the property $\hat{d}_{AC}^{con} = \hat{d}_{AB}^{con} +$ \hat{d}_{RC}^{con} for every set of three treatments. It also delivers coherent estimates of the additional contrasts, represented by the dashed lines in Figure 1, which have not been trialled.

A related concept which has been discussed separately is the "indirect comparison." This is where inferences are made about the effect of C relative to A (which has not been compared in a trial), based on "direct" evidence from AB and BC trials, using the relationship $\widehat{d}_{AC}^{Int}=\widehat{d}_{AB}^{Dir}+\widehat{d}_{BC}^{Dir}$. An indirect comparison is a special case of an NMA.

3 | THE FIRST TWENTY YEARS: A CHANGING CONTEXT

3.1 | Broad versus Narrow review questions and syntheses

A 2018 review in Nature noted that the same metaanalytic techniques are being used "with two different fundamental goals in mind." First, the estimation of specific treatment effects in specific populations, and second the broad generalization often based on large numbers of studies, accompanied by attempts to identify the reasons for heterogeneity. In a similar vein, broad syntheses, pooling data on different products and different patient groups, have been seen as useful for testing a scientific question as to whether a class of treatment works "in principle."^{34,35}

In the educational and social sciences where metaanalysis originated, the "broad" perspective has prevailed from the outset, including explicit calls to maximise between-study variation by including studies on a variety of subjects, exposed to different procedures in a range of settings.^{36,37} Moderator analysis, that is sub-group analysis and meta-regression, was then recommended to identify effect modifiers.

Tutorial texts and commentaries aimed at medical audiences have also encouraged researchers to embrace a diversity of trials in their meta-analyses, declaring that heterogeneity is desirable, inevitable, or both. ^{24,38,39} Gøtzsche uses homoeopathy trials as an example, and clearly has the "in principle" type of analysis in mind, pointing to the loss of power if trials are split into subgroups. ⁴⁰ But this argument does not work if the intention is to accurately estimate treatment effects, unless the level of heterogeneity is low. In the presence of substantial heterogeneity we can only draw conclusions about the *range* of effects. ⁴¹

This has created a degree of ambiguity and confusion: heterogeneity is "bad" because it makes interpretation of an effect estimate difficult, 34,38 if it cannot be explained by effect modifiers, but it is also "good" because its presence allows us to explore effect modifiers. 24,37 This "apples and oranges" debate has been a mainstay of the PMA literature for many years, especially in social and psychological studies. 42

But while social science meta-analysts could debate how to choose effect modifiers and how many could be studied, ⁴² their counterparts in medicine would be lucky if they could investigate even one. A study of nearly 15,000 Cochrane Reviews up to 2008 showed that 75% of meta-analyses were based on 7 or fewer studies. ⁴³ Given that the recommended lower limit for meta-regression is 10, ⁴⁴ it is surely unrealistic to believe that effect modifiers can be properly studied. Standard methods have very limited power to even detect heterogeneity, ⁴⁵ let alone identify effect modifiers. ³⁴

3.2 | Medical decision making and systematic review

NMA is most often used in healthcare research, to determine which of a set of interventions is "best" based on all the trials that compare two or more of them. In a decision-making context, the NMA forms the evidence input for treatment recommendations. In the simplest case, the

decision-maker adopts the single "best" treatment, this being the one with the highest expected value on a previously chosen evaluative criterion. This could be efficacy, or cost-effectiveness based on Net Benefit, Which is monetized quality-adjusted life years (QALYs) minus lifetime costs, or any scheme like Multi-Criteria Decision Analysis that weights different outcomes. Alternative ways of deriving treatment recommendations from an NMA are explored in Section 14.

Probabilistic⁴⁹ decision models or cost-effectiveness models, often incorporating a model of the natural history of the disease, are used by agencies that make reimbursement decisions such as the NICE.⁵⁰ and by the professional societies and colleges who issue clinical guidelines. It is essential that the joint statistical uncertainty in the NMA estimates is propagated through the decision model. This can be conveniently achieved by posterior simulation from a Bayesian NMA embedded within the decision model or, if frequentist methods are preferred, by boot-strap resampling, or by forward simulation from the maximum likelihood estimates and their variance-covariance matrix.⁵¹ Bavesian Markov Chain Monte Carlo (MCMC) software for NMA is available from the NICE Decision Support Unit, 52 from ISPOR (International Society for Pharmaceutical Outcomes Research), 29 a 2018 textbook, 53 and several software packages. 54,55 Frequentist software is also readily available. 56,57

Whatever the evaluative criteria, a decision context requires that interventions are narrowly defined: different doses of the same drug and different co-treatments are considered different treatments. "Lumping" over different doses or treatments is generally avoided as different doses have different costs and side-effects and are, indeed, intended to have different effects. Similarly, different treatment recommendations will be made for treatment-naïve patients and for patients who have failed on first-line therapy, so that re-imbursement decisions in particular tend to be applied to specific dose regimes in narrowly defined, clinically homogeneous populations. The decision-making context is thus inherently "narrow" in definitions of treatments and target populations.

Cochrane systematic reviews are also intended to inform clinicians' choice of treatment, but instead have emphasized completeness of inclusion of trials using the treatments under study, including grey literature. This inevitably draws together qualitatively heterogeneous sets of patients who may be at different points in the disease pathway, exemplifying the "broad" approach to synthesis. Analysts at NICE, sometimes explicitly, start with a broad Cochrane review, and then select studies relevant to their narrower target population.

Interestingly, Cochrane Systematic Reviews appear to have become narrower in scope, at least in some clinical areas. The 2009 review of biologics in rheumatoid arthritis combined trials with different doses, with and without cotreatments, and in different patient groups (first line, failed on non-biologics, and failed on biologics). Several years later the same authors produced separate NMAs in four different patient groups, 60-63 each review distinguishing different doses and different co-treatments.

Whether or not this represents a more general convergence in NMA practice, there remain distinct differences between NMAs undertaken for a clinical research paper and those used for decision making. This is most clearly seen in the more proactive approach to bias- and covariate-adjustment in a decision setting (Sections 12 and 13), compared to simply documenting bias^{64,65} or down-grading evidence for bias, "indirectness," or other attributes. ^{66,67}

The first 20 years of NMA have, therefore, been a period of transition. First, a transition from the large reviews seen in the social and educational sciences, to smaller reviews in medicine, where sub-group analysis is barely feasible. Then a transition from PMA to NMA at a time when high levels of clinical and quantitative heterogeneity were either welcomed or tolerated without comment, and finally to routine use in decision making, which is generally incompatible with clinical heterogeneity, and where unexplained heterogeneity poses particular difficulties that we explore below.

4 | WHAT ARE THE ASSUMPTIONS OF NMA, AND ARE THEY DIFFERENT FROM PMA?

4.1 | Three assumptions: homogeneity, similarity, consistency

Song et al⁶⁸ described three assumptions which they stated were required by NMA. *Homogeneity*, which was also assumed in PMA, and two further assumptions, *similarity* and *consistency*, which were required for NMA. In their words:⁶⁸ homogeneity means that each trial "estimates the same single treatment effect ... or different treatment effects distributed around a typical value"; similarity requires that trials in the different treatment comparison sets "are similar for moderators of relative treatment effect." Finally, consistency requires there is no conflict between the parameters estimated by "direct" and "indirect" evidence (see Figure 1). Later papers introduced another term, *transitivity*, ^{12,14} which requires that "indirect comparisons validly estimate the unobserved head-to-head comparison," ^{12,69} equivalent to consistency. Transitivity

was also seen as requiring that trials are similar in every important respect other than treatment,⁷⁰ equivalent to similarity.

Song et al's three assumptions have been repeated in methodology and tutorial papers, sometimes verbatim, ⁷¹ but also with variations such as: dropping similarity; ⁷² dropping homogeneity; ⁷³ adding transitivity; ¹⁵ dropping similarity and transitivity. ⁷⁴ Transitivity and similarity have been viewed as the same assumption, ¹² but "similarity reduces to homogeneity" in a single head-to-head comparison. ¹² Also, "the notion of transitivity is analogous to ... homogeneity"; or that "a lack of transitivity causes inconsistency"; ¹⁴ or that it is "incorrect" to consider transitivity and consistency as the same. ⁷⁵ Evidently, there has been a lack of clarity about the precise definition of these terms, and the relationships between them. We provide a set of recommended definitions in Table 1.

4.2 | Or a single assumption: exchangeability (qualitative homogeneity)

It appears that Song et al used the term "homogeneity" as a qualitative construct. On this reading, the homogeneity assumption is a characterization of the standard "random effects" model, in which trial treatment effects are samples from a distribution, for example: $\delta_{i,AB} \sim Normal(d_{AB}, \sigma_{AB}^2)$. In this sense homogeneity is similar to exchangeability (Table 1), as previously recognized in the Bayesian literature. 76,77 although neither make specific distributional assumptions. Song et al's⁶⁸ version of the homogeneity/exchangeability assumption correctly captures the "randomness" recognized in every account of random effects meta-analysis. Consistency is then not an additional assumption required by NMA, as we ourselves once believed, 9,10 it is in fact a corollary of exchangeability. 78 The reasoning is as follows. Assuming a linear predictor scale on which treatment effects are additive, if a meta-analysis of AB trials is characterized by trial-specific relative treatment effects $\delta_{i,AB} \sim Normal(d_{AB}, \sigma_{AB}^2)$, drawn from a normal distribution with between-trial variance σ_{AB}^2 and a meta-analysis of BC trials by $\delta_{i,BC}$ \sim $Normal(d_{BC}, \sigma_{BC}^2)$, then it follows that the true AC treatment effects must conform to $\delta_{i,AC} = \delta_{i,AB} + \delta_{i,BC}$, and therefore that $\delta_{i,AC} \sim Normal(d_{AC}, \sigma_{AC}^2)$ where $d_{AC} =$ $d_{AB} + d_{BC}$ is the "consistency assumption." It can also be deduced that $Minimum(\sigma_{AC}^2, \sigma_{BC}^2) < \sigma_{AC}^2 < \sigma_{AB}^2 + \sigma_{BC}^2$, which is a 2nd order consistency relating the three variances.⁷⁹ This is the triangle inequality in which the standard errors correspond to the side lengths of an acute-angled triangle (Supplementary Note 1).

Because exchangeability implies similarity with respect to effect modifiers across treatment comparisons, all three



TABLE 1 Definitions of terms.

Term	Definition
Exchangeability	Random variables are said to be exchangeable (qualitatively homogeneous), if a sequence of those variables has a joint probability distribution that is unchanged if the sequence is reordered. For example, if some studies were in treatment-naïve patients and other studies in non-naïve, then we could a priori create sequences of treatment effects that had different joint distributions.
Qualitative homogeneity/ heterogeneity	Same as Exchangeability/lack of exchangeability.
Quantitative homogeneity/ heterogeneity	The hypothesis of quantitative homogeneity is tested by, for example, Cochrane's Q-statistic, ²¹² or comparing the fit of fixed and random effects models. Quantitative heterogeneity is what is measured by between-trials variance. Heterogeneity refers to variation <i>within</i> treatment comparisons.
Consistency	Direct and indirect sources of evidence estimate the exact same parameters. A corollary of exchangeability.
Similarity	Distribution of effect modifiers is similar across direct and indirect sources of evidence. Implied by exchangeability.
Transitivity	(a) equivalent to consistency, or (b) equivalent to similarity
Incoherence	Same as inconsistency; lack of consistency between treatment comparisons.

of Song et al's requirements can be derived from exchangeability, along with transitivity in both its senses.

4.3 | Quantitative versus qualitative heterogeneity

As well as its exchangeability meaning, homogeneity has also been interpreted in a *quantitative* sense. Several authors have concluded that the homogeneity assumption requires that relative treatment effects have to be *quantitatively* similar, 71,72,80 and that it can be verified or ruled out by statistical tests of homogeneity, 27,74 or measured by I^2 statistics. 81

However, the fact is that, whether one prefers the broad or narrow approach to synthesis, there is no technical requirement in either PMA or NMA for treatment effects to be quantitatively homogeneous; indeed, there is no theoretical limit on how quantitatively heterogeneous treatment effects can be. Think of a basket of green apples: however much they vary in size they are still homogeneous (exchangeable). They become non-exchangeable if, for example, oranges get in; which can happen if colour is not recognized as a potential effect modifier.

5 | HOW TO ESTABLISH EXCHANGEABILITY

If exchangeability is the only assumption, how can it be checked and verified? Establishing exchangeability a posteriori by statistical analysis requires a demonstration that subsets of the data are "similar to an adequate approximation", based on sub-group analyses, with the definitions of both "similar" and "subsets" being decided by context. However, as noted above, fewer than 25% of Cochrane PMAs consist of more than seven studies, and most NMAs will be under-powered to detect subgroups. Tests for inconsistency are also investigations of whether treatment effects in pre-defined sub-sets of the data are similar. But these are also inherently weakly powered, as well as being hampered by insufficient data (see Section 10).

Establishing exchangeability a posteriori will therefore seldom be feasible. Unless large numbers of trials are under study, the judgement of exchangeability of relative treatment effects in a given network can only be made a priori on the basis of topic expertise. It is here that the concepts of similarity and transitivity have value, providing a rationale for a range of informal checks and investigations recommended in tutorial papers and checklists. 26,28,29,31,83 Table 2 summarises the various prior and posterior approaches to checking NMA assumptions.

6 | DOES NMA ESTIMATE CAUSAL EFFECTS OR ASSOCIATIONS?

When refereeing an applied paper recently, one of us was surprised to read the following editorial comment: "Results of this meta/network association analysis should be described in terms of association, not in terms of a causal effect."

The 2008 Cochrane Handbook⁸⁴ stated that "indirect comparisons ... are essentially observational findings across

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TABLE 2 Methods for checking the exchangeability assumption, with selected references.

A posteriori checks and statistical tests	Subgroup analysis, meta-regression ²¹³ ; network meta-regression. ²¹⁴ Single loop inconsistencies. ³² Multiple independent inconsistencies. ²¹⁵
	Node-Splitting. ²¹⁶
	Graphical Comparison of consistency and inconsistency models. ¹⁰
	Design-by-treatment interaction models. 19,21,126
	Measures of and tests for between-comparison variance. 1,10,126,217
A priori checks for similarity/ transitivity	Examination of outcomes in control groups may provide clues about potential effect modifiers. 31,218 For example severity, previous treatment, age, calendar time.
	Examination of the distribution of potential effect modifiers across different treatment comparisons. 31,83
	Joint randomizability: 12 it should be possible to randomize every treatment to each of the trial populations; equivalently, it should be possible to have a multi-arm trial that includes all the treatments; equivalently, in each trial treatments that are missing are missing-at-random with respect to their efficacy.

trials, and may suffer the biases of observational studies, for example due to confounding". This statement has been repeated almost verbatim in the 2019 edition⁷⁰ and in tutorial papers on NMA. ^{14,27,85–87} When randomized trials are contrasted with observational studies, the term "confounding variables" usually refers to *prognostic variables*, factors that impact the absolute outcomes, but not necessarily on relative treatment effects. But indirect comparisons are *not* vulnerable to confounding in this sense, because randomization ensures that prognostic variables are balanced over arms in each trial. Thus, PMA, indirect comparisons and NMA all respect randomization and all produce weighted averages or linear combinations of relative treatment effects, ^{78,88} each of which are controlled for prognostic factors.

A similar claim is that NMA is a form of sub-group analysis or meta-regression, and that NMA is therefore "observational" because regression coefficients cannot be interpreted as causal effects, only as associations. ¹² Both PMA and NMA, and indeed RCTs themselves, can be analysed as regressions with treatment as the covariate. But this does not prevent the coefficients being interpreted as estimates of causal effects, due to randomization.

Relative treatment effects are, however, affected by effect modifiers, and estimates produced by PMAs, indirect comparisons and NMAs, will be dependent on the distribution of effect modifiers in included studies. ⁸³ In this sense PMA can be and has been regarded as observational in nature. ^{89,90} But, how can it be possible to draw causal inferences from a single randomized trial, but not from 2 or 3 trials?

Heterogeneity does not prevent a pooled effect from being causal, but it still has a profound impact on what can be concluded from it:

- A single trial identifies a causal effect, but in the presence of unrecognized effect modifiers, we may remain uncertain about the population or circumstances in which it applies.³⁸ (Possibly, this explains why trials are hard to replicate.⁹¹)
- If, in a synthesis of several trials, the effects are quantitatively homogeneous, this increases certainty about the population in which the causal effect occurs.
- If the treatment effects are quantitatively heterogeneous, we can remain confident that there are causal effects in the populations studied, but we may now be uncertain about their size and direction in any new population.³⁸
- In the extreme case of a statistically strong pooled effect, whose 95% interval does not include zero effect, but where the distribution of effects does cross the zero line, we are still confident there is a causal effect, but now we have no idea in which population(s) it occurs.

A large proportion of random effect meta-analyses appear to be in this final category (Supplementary Note 2).

7 | NETWORK GEOMETRY AND BIAS

The PRISMA-NMA check-list asks authors "to explore the geometry" of the treatment network ... and the potential biases related to it," and "provide an ... overview of gaps in the evidence, and potential biases reflected in the network structure." This advice requires clarification because it is unclear what kinds of bias or bias mechanisms are being associated with network structure.

Related to the idea that NMA is "observational" is that it is vulnerable to selection bias. The supposed bias occurs "when the choice of comparator in a study is dependent on the relative treatment effect." A similar claim, under the name "opportunity bias," is that indirect comparisons of treatments A and C via treatment B will be biased unless allocation of patients to AB comparisons and BC comparisons is random. 93 Likewise, it has been claimed that the transitivity assumption is violated if the choice of comparators is related directly or indirectly to the relative efficacy of the interventions. 12

Choice of comparators is far from random. New products are generally trialled against placebo to gain regulatory approval, and it is no surprise that industry trials tend—on average—to favour new drug treatments over placebo. Hanufacturers may also deliberately game the system by comparing their product to competitor products at a less effective dose. Has earned the name "comparator preference bias". But as long as the different doses are reflected as separate treatment nodes, the appropriate indirect comparisons can be made and bias caused by "lumping" different doses is avoided.

Network structure certainly needs to be monitored and understood, because it determines how potentially biased evidence in one part of the network is propagated across the network to cause bias in NMA estimates. ^{97,98} However, the network structure cannot lead to bias in and of itself (Supplement Note 3).

8 | IS "DIRECT" EVIDENCE BETTER THAN "INDIRECT" EVIDENCE?

A repeated claim in the literature is that "direct" evidence is better than "indirect." ^{28,71,99–101} Investigators have been advised to prefer direct evidence when it is available, ⁸⁴ to include indirect only when direct evidence is insufficient, ^{17,27,87,93} to "distinguish between direct and indirect evidence", and to "justify using indirect evidence." Some of these ideas may have been fuelled by the belief (Section 4) that NMA makes more assumptions, requires more checking, and is therefore inherently more dangerous and unreliable than PMA. We have not been able to find any theoretical foundation for this advice, and the standard formula $\widehat{d}_{AC}^{Ind} = \widehat{d}_{AB}^{Dir} + \widehat{d}_{BC}^{Dir}$ tells us that if the direct evidence is unbiased, then the indirect estimates must be unbiased too.

The relative merits of direct and indirect evidence can be discussed if only two or three treatments are involved, but in larger networks it eventually becomes impossible to prefer one to the other or even to keep them distinct: the same evidence that is direct for one contrast is indirect for another. After all, in Figure 1, the 29 indirect estimates (19 based on 3-treatment loops and 10 on 4-treatment loops), and the set of 15 coherent NMA estimates combining both direct and indirect evidence, are all linear functions of the same 9 "direct" estimates.⁷⁸

9 | DANGERS OF HETEROGENEITY ARE MAGNIFIED BY A SMALL NUMBER OF TRIALS

In this section we show that quantitative heterogeneity manifests itself as increased expected absolute error which affects both direct and indirect estimates and leads to inconsistency, the risk being greater as the number of trials diminishes, even when exchangeability is satisfied.

9.1 | Second order sampling error in PMA

Following a 1993 meta-analysis, magnesium was seen as an effective intervention following acute myocardial infarction.¹⁰² The negative findings from the ISIS-4 super-trial therefore took the trialists by surprise, 103 while leading experts called the earlier meta-analysis results "discrepant" and "misleading." 104 However, a predictive cross-validation analysis 105,106 shows that while the treatment effect in ISIS-4 is indeed statistically significantly different from the meta-analytic pooled effect, it is entirely within the prediction interval for a new trial. In other words, given the degree of between-studies variation in previous trials, a trial with an effect as small as ISIS-4 should not have been unexpected.⁵³ The estimated between-study standard deviation (SD) was 0.58 on the log odds scale;⁵³ meaning that effects as much as a factor of 3 higher or lower than the median effect could be within the 95% envelope. This high level of heterogeneity was not commented on, or even documented, reflecting the permissive attitude to heterogeneity that prevailed at the time, and to some extent still does.

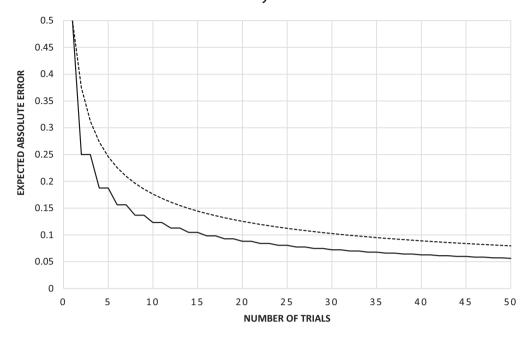
The ISIS-4 trial has been also used to illustrate publication bias, ¹⁰⁷ and the role of sceptical Bayesian priors. ¹⁰⁸ The confusion over whether ISIS-4 was unexpected or exactly in line with the existing evidence would be less likely to occur now, as opinion is shifting away from the pooled mean and its confidence interval as the appropriate summary, and towards the predictive effect in a new study. ¹⁰⁹ There has also been further progress on methods for outlier detection in NMA. ^{110–112}

The error in the predictive effect reflects the sampling error arising from a single draw from the random effect distribution. We may extend this concept from a single study to syntheses of 2, 3 or more studies. This has been described as *second-order sampling error*.⁴⁵ Imagine a

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absolute error in direct and indirect comparisons, in the presence of an unknown effect modifier with effect size 1 unit, present on 50% of RCTs. A is placebo, B and C are active treatments in the same class, such that the effect modifier changes their treatment effects relative to placebo to the same extent. Solid line: error in direct \hat{d}_{AB}^{Dir} estimates, and in indirect estimates $\hat{d}_{AC}^{Ind} = \hat{d}_{AB}^{Dir} + \hat{d}_{BC}^{Dir}$. Dashed line: error in indirect estimates $\hat{d}_{AC}^{Ind} = \hat{d}_{AC}^{Dir} - \hat{d}_{AB}^{Dir}$.



meta-analysis of infinitely large trials in which quantitative heterogeneity arises from a single unrecognized trial-level effect modifier, which is present in 50% of all trials, although this is not known to investigators. The relative treatment effect in the absence of the effect modifier is 1, and in its presence 2. The "average" treatment effect is $(0.5 \times 1.0 + 0.5 \times 2.0) = 1.5$. The expected bias of the meta-analysis relative to this target is zero, regardless of the number of trials. However, no single trial will ever estimate this target: it will always be 0.5 higher or 0.5 lower. If the effect modifier is known, separate analyses can be conducted on each subset. But with an unrecognized effect modifier, we do not know if a trial has delivered an overestimate or an underestimate. The expected absolute error is the appropriate statistic to reflect what we might call the realized error in the result of any given meta-analysis. The expected absolute error in a meta-analysis decreases as the number of trials increases,⁵³ from 0.5 if the meta-analysis consisted of a single trial, to 0.25 with two trials and 0.12 with 10 (see Figure 2). Recall that 75% of published Cochrane Collaboration PMAs before 2009 consisted of 7 or fewer trials. 43

9.2 | Second order sampling error in indirect comparisons

Extending these "thought experiments" to indirect comparisons, assume that treatment A is placebo and treatments B and C are active treatments in the same class, so that the effect modifier changes the outcomes on treatments B and C in exactly the same way. The C versus B treatment effect in BC trials, \widehat{d}_{BC}^{Dir} , is therefore not affected

by the effect modifier. In the indirect estimate: $\widehat{d}_{AC}^{Ind} = \widehat{d}_{AB}^{Dir} + \widehat{d}_{BC}^{Dir}$, the expected absolute error in \widehat{d}_{AC}^{Ind} is exactly the same as the expected absolute error in the direct estimates \widehat{d}_{AB}^{Dir} , as shown in Figure 2. However, if we estimate the BC effect indirectly from the two active-placebo comparisons, we find that $\widehat{d}_{BC}^{Ind} = \widehat{d}_{AC}^{Dir} - \widehat{d}_{AB}^{Dir}$ now has a higher expected absolute error (Figure 2). The realized error in this form of indirect comparison, which is probably the most common, is especially large.

Second order sampling error arising from heterogeneity can therefore result in realized error in direct and indirect estimates, and statistical inconsistency between them. Critically, sampling error generates inconsistency between direct and indirect estimates, even under exchangeability, that is even when the consistency assumption holds at the level of the parameters. The extent of the inconsistency depends only on the number of trials (Figure 2) and the degree of heterogeneity. The problem of realized error due to second order sampling only disappears if there is no heterogeneity. Analyses of many thousands of metaanalyses found median between-studies SD around 0.3 units on the standard normal scale (Supplement Note 4), which seems high when compared to the benchmark 0.2, 0.5, 0.8 for small, medium and large effect sizes. 113

The danger of meta-analytic estimates based on small numbers of trials is especially relevant to NMAs, because most comparisons are directly informed by only one or two trials. In a report based on 201 networks published before 2019, 92% included a comparison informed by only one study; there was a median 1.3 studies per direct comparison, and the 90% percentile was less than 1.6.82 Another collection, from 2013, of 93 Cochrane Review

NMAs had a median 1 study per comparison, and 67% had less than 2.¹¹⁴ In Song et al's 2011 study of inconsistency, 50% of the 3-edged evidence loops were supported by 5 or fewer studies.¹⁸

It is a benefit of NMA that it allows *all* the evidence to contribute to each comparison, so that in cases where direct evidence from one or two trials delivers an extreme estimate, it is generally moderated by indirect evidence. (This effect is limited by the geometry of the network; it does not hold for comparisons that involve a "dead end" in the network graph. (Interestingly, in empirical studies, most of the evidence on each comparison is indirect. (116)

10 | ALTERNATIVE PARAMETERIZATIONS

10.1 | Arm-based models

The models most often used for NMA, as we noted in the introduction, are *contrast-based*, ^{10,117} with relative treatment effects drawn from random effect distributions. An alternative puts a multivariate-normal model on arm effects. ^{118–120} *Arm-based* models are equivalent to contrast-based models in which a random effect model is also put on the study-specific effects. ¹²¹ (Note that contrast-based models may have arm-based likelihoods). Putting a model on study effects has been avoided both in traditional PMA and NMA as it allows study effects to contribute information on relative treatment effects, and this risks introducing bias if the trial effect model is mis-specified. ^{121,122}

A second feature of arm-based models is that they oblige users to inform the absolute outcomes and the relative effects from the same data. In practice, information on absolute outcomes is better sourced from external evidence, such as register studies or single contemporary trials. This is the strategy commonly adopted by decision modellers. 124

10.2 | Inconsistency models

Two definitions of inconsistency have been proposed. Loop inconsistency occurs if the meta-analytic estimate of the direct AC effect, \widehat{d}_{AC}^{Dir} , differs from the indirect estimate $\widehat{d}_{AC}^{Ind} = \widehat{d}_{AB}^{Dir} + \widehat{d}_{BC}^{Dir}$. Its detection is achieved by testing the null hypothesis that inconsistency terms for all loops $\widehat{\omega}_{ABC} = \widehat{d}_{AC}^{Dir} - \left(\widehat{d}_{AB}^{Dir} + \widehat{d}_{BC}^{Dir}\right)$ are zero. 10,125

In networks with multi-arm trials the definition of the loop inconsistency terms depends on how the model is parameterized. *Design inconsistency*^{20,126} avoids this problem by including both loop inconsistencies and

differences between the AB effects estimated in AB, ABC, ABD sets of trials. It has lower power to detect inconsistency due to having more parameters than the loop-inconsistency approach.

Inconsistency models have been used primarily to detect inconsistency by goodness of fit tests and residual plots from the two models. ^{10,127} However, Lumley's original NMA models, which allowed for loop inconsistencies, and Jackson et al's design inconsistency models were intended for routine use in applications. ^{21,128} This strategy is supported by several papers reporting that inconsistency is more prevalent than would be expected by chance (Supplementary Note 5). ^{18,19,82}

However, the implications of these reports are unclear. First, they are based on data from Cochrane reviews and clinical literature from a period where high levels of clinical and quantitative heterogeneity were tolerated. Second, comparison of consistency and inconsistency models is limited to two methodological papers, 21,128 in which differences between estimates from consistency and inconsistency models were either barely perceptible, or differed by only a fraction of the between-studies (within-comparison) standard deviation. Model choice did not impact on the ranking of treatments by their expected effects. In practice, researchers have been hesitant to use inconsistency models in routine applications; possibly because of the dependence on parameterization of loop inconsistency models, and the difficulty understanding what design inconsistency may represent.

10.3 | Remaining research questions on inconsistency

The studies on prevalence of inconsistency should be repeated, looking separately at networks informing reimbursement decisions, clinical guideline recommendations, and other NMAs published in clinical journals. As before, 43,129 research should also distinguish between different disease areas: less between-study variation might be expected in networks of cancer treatments than in networks of depression trials or complex interventions, where trial populations are more variable. Updating these studies could provide more appropriately targeted data on suitable prior distributions for between-studies variance parameters. 43,130 Research on the prevalence of inconsistency⁸² and work on inconsistency models²¹ has assumed that the inconsistency terms are themselves exchangeable, drawn for example from a random effects distribution. Some of the published examples, however, suggest otherwise: plotting residuals from consistency and inconsistency models against each

other can reveal that inconsistency is largely confined to just one or two comparisons. ^{127,131} Further research would clarify the prevalence of both exchangeable or non-exchangeable inconsistency, and the extent to which choice of model impacts on treatment recommendations.

11 | THE RELIABILITY OF NMA

A posteriori checks on exchangeability assumptions are unlikely to be conclusive (Section 5). Therefore, whatever a priori efforts are made minimize the risk of non-exchangeability, investigators need to assess the reliability of conclusions based on NMA. Distinct approaches have emerged.

11.1 | GRADE certainty of evidence ratings

GRADE is a method for ascribing a "quality" or "certainty" rating (high, moderate, low, very low) to every PMA estimate. These ratings are based on assessments in five domains: risk of bias (study limitations), imprecision, inconsistency (quantitative heterogeneity), indirectness (applicability), publication bias.66 To extend this to NMA it was proposed that the GRADE process must be applied to every direct estimate, and then to every indirect estimate. 67 The rating attached to each indirect estimate would be the lowest of the ratings of its two direct components. Then the certainty rating attributed to each NMA estimate would be the highest of the direct and indirect ratings. In the Figure 1 network there are 21 indirect estimates based on triangular evidence loops: the same quality ratings belonging to the 9 direct estimates are therefore recycled a total of $2 \times 21 + 9 = 51$ times to produce the NMA quality ratings.

If the direct and indirect estimates are substantially different from each other, researchers are advised to choose the one with the highest certainty. 67 GRADE could then deliver an incoherent set of estimates (A > B, B > C, C > A). Nevertheless, the Working Group confirmed that certainty should take preference over expected efficacy 132 (though see Section 14).

The GRADE approach requires a subjective quality rating for every item of direct and indirect evidence, which is laborious to implement in networks where there may be several hundred indirect comparisons. Subsequent clarifications and elaborations have made this time-consuming process even more complex, with unclear benefits.

11.2 | Confidence in network metaanalysis—CINeMA

The potential for incoherence and the multiple recycling of the same ratings can be avoided by exploiting the fact that each NMA estimate is a linear combination of the direct effect estimates and a set of coefficients which represent their relative contribution. These coefficients, elements of the so-called *contributions matrix*, can be multiplied into modified GRADE ratings attaching to each direct comparison, to provide a coherent confidence rating for every NMA estimate, and a confidence rating for the whole network. This approach was subsequently refined as Confidence In Network Meta-Analysis (CINEMA) and streamlined with user-friendly software (Supplement Note 6).

There are drawbacks, however. First, GRADE-type assessments are required on all items of evidence at the outset, each requiring subjective judgements, including judgements of how much heterogeneity or inconsistency should be allowed before an item of evidence is downrated. As with GRADE, further complexity is introduced because of the overlap in multiple uncertainty-related concepts: imprecision, indirectness, heterogeneity, inconsistency (incoherence), and transitivity. Elaborate precautions have to be implemented to avoid double counting. 98,132,134,136

However quality or confidence ratings for NMA estimates are generated, it is unclear how they are intended to impact on treatment decisions, because there is no relation between the confidence in evidence and the impact of that evidence on the rank ordering of treatments. 137,138

11.3 | Threshold analysis: reliability of recommendations based on NMA

Providing an accurate analysis of the impact of every piece of direct evidence on every NMA estimate, CINeMA presents investigators with almost too much information. To reduce the dimensionality of the problem we can instead investigate the robustness of recommendations based on NMA evidence to potential biases and uncertainties in the data. This is done via a specific form of threshold analysis, 138,139 a standard technique in decision analysis.46 Threshold analysis for NMA asks the question: "given the imprecision, uncertain relevance, potential biases in the trial estimates, and possible inconsistency or intransitivity, how much would the evidence have to change before this impacts the treatment recommendation?"138,139 This question can be asked about the evidence from single trials, or the pooled evidence on each treatment contrast, or applied to treatment effects in selected subsets of trials, for example those at higher risk

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of bias.¹⁴⁰ Underlying the threshold analysis is the same algebra, based on the hat matrix, that is used in the CIN-eMA approach.

Threshold analysis defines the invariant intervals over which the evidence can change without impacting on recommendations. In larger NMAs it can turn out that no plausible change in the evidence, whether due to bias or sampling error, could change the recommendations. 138 (The definition of "plausible" introduces a subjective element into what is otherwise a purely mechanical process). In other cases the credible intervals extend beyond the invariant regions, indicating that the recommendation is sensitive to uncertainty. 138 Threshold analysis identifies what may be a small number of trials or treatment comparisons to which the recommendation is sensitive, so that these can be further scrutinized. By contrast, both GRADE and CINeMA require every item of evidence to be researched and rated at the outset, and in multiple ways. However, this disadvantage will be substantially offset by accumulating evidence in "living" reviews. 141

Whilst GRADE and CINeMA must, in their current forms, be carried out separately for each outcome, threshold analysis can be applied to treatment recommendations based on decision models that incorporate multiple outcomes, cost-effectiveness, ¹³⁹ inconsistency, and bias modelling (Section 13). ^{131,142} However, more work is needed to develop computational methods to apply it to the full range of non-linear economic models typically seen in HTA.

12 | POPULATION-ADJUSTED TREATMENT EFFECTS

In the presence of effect modifiers relative treatment effects estimated in trials will differ from the effects that would be observed in a target population. The purpose of population-adjustment methods is to project, or extrapolate, treatment effect estimates onto a specified target population. Solutions include: simple direct standardization; ^{143,144} model-based standardization, ¹⁴⁵ a form of reweighing by propensity scores; outcome regression; and doubly robust estimation. ¹⁴⁶ The properties of these methods, their variants, target estimands, and scope of application were reviewed previously. ^{147,148} Another approach reweights according to propensity calculated from a baseline risk score. ¹⁴⁹

Two important innovations, Matching Adjusted Indirect Comparisons (MAIC)¹⁵⁰ and Simulated Treatment Comparisons (STC)^{151,152} extended the above methods to indirect comparisons and specifically to evidence structures including both IPD and aggregate data (AgD).

MAIC and STC address a situation that is common in HTA, where, given IPD from a manufacturer's AB trial (A being placebo and B an active treatment), the aim is to generate an indirect BC comparison from AgD available from a competitor's AC trial. MAIC achieves this using a modified propensity score reweighting, and STC by covariate adjustment. Detailed analyses of both methods have been published 147,148 and their performance has been assessed in simulation studies. 153 A critical problem with both methods is that they are limited to extrapolating the AB and BC relative treatment effects into the population represented in the (competitor's) AC trial. For the same reason they can only be applied in (AB-AC) indirect comparisons, not to wider networks. We begin our description of more general methods by considering evidence networks consisting entirely of IPD.

12.1 | The relation between treatment effects at individual patient and aggregate levels

Covariate adjustment is recommended in the analysis of individual trials because it increases the precision of estimated treatment effects, controls for baseline imbalances, and avoids aggregation bias when trial outcomes are nonlinear. For the same reasons, IPD meta-regression is recognized to be the gold standard; it also allows individual level effect modifiers to be studied and accounted for in a way that is not possible when only AgD is available.

Decisions about which treatment is best are, however, made for whole populations, which requires estimation of the absolute effects of treatment at the marginal (AgD) level. Starting from an IPD meta-analysis including regression coefficients for prognostic variables, effect modifiers and treatment effects, one may obtain an average probability in a specified target population by integrating the individual outcomes over the target joint covariate distribution. Note that for non-linear link functions, such as log, logit or probit, the relative treatment effects at the AgD and IPD levels are not the same, as has sometimes been assumed. 161–163

12.2 | Multi-level network meta-regression (ML-NMR)

Multi-Level Network Meta-regression (ML-NMR), ^{153,160,164} illustrated in Figure 3, reconstructs an IPD analysis of connected networks consisting of any combination of IPD and AgD trials. It has the important property that, if all trials provide IPD, it is equivalent to the gold standard IPD meta-regression; if all provide AgD it is equivalent to a

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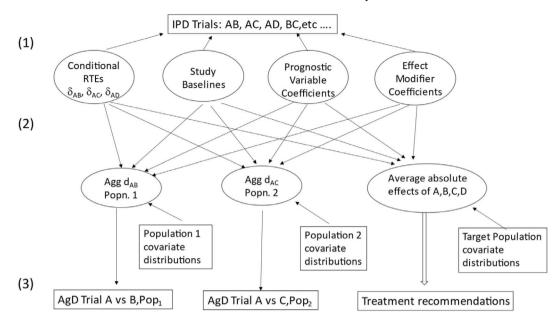


FIGURE 3 Multilevel network meta-regression (ML-NMR). Schematic Directed Acyclic Graph showing how (a) individual patient data, and (b) population average absolute treatment effects from aggregate data trials, jointly inform a common set of parameters, which then predict treatment effects in a target population. (1) IPD network meta-regression: relative treatment effect (RTE), study baselines, regression coefficients for prognostic variables and for effect modifiers at the IPD level are informed by a connected IPD network of trials on treatments. (2) Integration step: calculation of population average relative and absolute treatment effects in specific populations, including the target population for the decision. (3) Information from AgD trials back-propagated to contribute further parameter information.

standard NMA. ML-NMR coherently relates the individual- and aggregate-level models by integrating over the joint covariate distribution in each AgD study (Supplement Note 7), which avoids the aggregation bias caused by plugging-in mean covariate values in non-linear models, as was proposed in earlier work on combining IPD and AgD in NMA. 161–163 Unlike MAIC and STC, ML-NMR can be applied to any number of AgD and IPD trials and in networks of any complexity. Furthermore, with non-collapsible effect measures such as (log) odds ratios, ML-NMR correctly combines marginal and conditional effects and can produce both marginal and conditional estimates. Crucially, only ML-NMR can generate treatment comparisons in any specified population.

In practice, it is frequently necessary to assume that each effect modifier impacts on a set of treatments in the exact same way (the Shared Effect Modifier—SEM assumption), in order to estimate the model with the available data. In most population-adjustment analyses treatments belong to classes of drugs within which the SEM assumption is reasonable. With IPD on multiple comparisons the assumption can be tested, ¹⁶⁴ and if necessary abandoned. Limited experience so far shows that ML-NMR estimates treatment effects more precisely than standard NMA, as it takes account of individual, within-study variation, ^{153,164} and reduces between-study

heterogeneity and inconsistency by accounting for the different effect modifier distributions rather than averaging over them.

12.3 | Network meta-interpolation (NMI)

NMI uses information on AgD level relative treatment effects in sub-groups. If all trials report the relative treatment effect in both, say, severe and non-severe subgroups, it would be possible to estimate the relative treatment effect on the linear predictor scale in each trial that would be observed with any specified (target) proportion of severe patients. A standard NMA can then be run at the target values of that effect modifier. This can be extended to multiple sub-group dimensions using a best linear unbiased estimator approach based on marginal subgroup estimates and covariate correlations, 165 without the need for data on sub-group combinations (as with ML-NMR, the covariate correlations are borrowed from available IPD). NMI does not require the SEM assumption, as effect modifier information has to be available on all trials. However, because NMI works at the level of population average conditional effects, it cannot access the patient-level regression parameters needed to estimate absolute average treatment effects in the target population. This limits its use in HTA.

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12.4 | Research priorities in population adjustment

Population adjustment methodology is an active area of research, with rapid uptake in submissions to reimbursement bodies such as NICE.55 Several variations of MAIC and STC have been proposed, 166,167 but the fundamental inability of MAIC and STC to extend to larger networks remains, and a recent report commissioned by the NICE Decision Support Unit suggests that ML-NMR should be the preferred approach. 168 Ongoing research aims to extend ML-NMR to incorporate subgroup analyses and regression coefficients reported by AgD studies, in order to aid estimation and reduce reliance on the SEM assumption. This opens the door to performing ML-NMR analyses without any IPD at all, recreating the equivalent IPD NMA without the difficulties of obtaining IPD. Such advances have the potential to revolutionise evidence synthesis. Standardized reporting of the necessary summary statistics, including the joint covariate distributions, regression coefficients and covariance matrices, would further increase the applicability of ML-NMR. Technical methods for accessing IPD without jeopardising confidentiality or intellectual property are also being developed. 169,170

13 | BIAS-ADJUSTMENT

13.1 | Quality-related bias in RCTs

A 1995 study by Schultz et al. ¹⁷¹ showed that RCTs at high risk of bias through failure of allocation concealment or lack of blinding tended to exaggerate treatment effects. Since then a series of meta-epidemiological studies have provided evidence of quality-related biases in specific disease areas and for specific kinds of outcome measure. ^{172–174} The bias model assumes that low risk studies estimate a relative effect δ_i and the high risk studies estimate $\delta_i + \beta_i$ with a bias distribution $\beta_i \sim N(b, \sigma_B^2)$. The meta-epidemiological studies provide empirically-based priors for bias distributions, so that studies at low and at high risk of bias can then be incorporated in a single meta-analysis. ¹⁷⁵

In NMA, the extra degrees of freedom can be leveraged to estimate the bias distribution associated with high-risk studies, and then generate biasadjusted relative treatment effects, using only the data at hand. This has been applied to quality-related bias, 176 novel agent (optimism) bias, 177 small-study bias, 178 sponsor-bias, 95 and biases associated with missing data.

13.2 | The use of non-randomized studies to estimate relative treatment effects?

The use of non-randomized studies (NRSs) to estimate relative treatment effects has been debated for over 40 years and remains controversial. Various reasons for incorporating NRS evidence, besides a lack of RCT evidence, have been advanced: that RCTs may have poor external validity, ¹⁸¹ that RCTs may be unable to predict treatment effects in the 'real world', ^{163,182} and that inclusion of NRS evidence will make the results more generalisable. ^{183,184} The way estimates are derived from NRS has received little attention in the synthesis literature (Supplement Note 8).

The generalisability argument takes us back to the "broad" versus "narrow" debate. If the focus is on specific treatment regimens at specific points in a disease pathway, the advantage of greater generalisability is unclear. Regarding external validity, it is true that RCT populations may have a patient mix than differs from the target distribution, but it is unclear in what way case—control and cohort studies are more "real" or externally valid than RCTs. If IPD is available, population-adjustment methods like ML-NMR (section 12) are designed to map RCT treatment effects over to any specified population, possibly based on a register, without the need to estimate relative treatment effects directly from NRS data.

A Cochrane review comparing relative treatment effects in RCTs and NRSs reported that *on average* there is little difference, ¹⁸⁵ although "substantial heterogeneity" was reported in the odds ratio of RCT to NRS effects Thus, *in any given analysis*, a substantial absolute difference between the RCT effect and the NRS effect can be expected (Supplement Note 9). In practice, the true heterogeneity in RCT:NRS odds ratios is considerably greater, as the review examined average effects from meta-analyses consisting of between 19 and 530 studies.

13.3 | Methods for incorporating NRS evidence on relative treatment effects

Meta-analytic methods for incorporating NRS, reviewed in more detail elsewhere, ^{186,187} divide into three classes. In the first category NRS evidence is used to provide a prior distribution for the relative treatment effect, which can be down-weighted in various ways, ^{188,189} and to various extents, in recognition of the likelihood of bias. ^{163,181} Choosing a specific weight is problematic, which might explain why the most common approach is to accord NRSs the same weight as RCTs. ¹⁸³

A second approach introduces a third hierarchical level representing different 'types' of evidence, ^{163,181,182,184,190} for example RCT and NRS, perhaps also distinguishing casecontrol, and cohort studies. The target estimand is now the mean of the study-type distribution. But this is clearly not an estimate of the causal effect which RCTs are designed to identify. Further, its value depends on the amount of evidence on each type, and the between-type variance, which is poorly estimated with so few types, and hence influenced by priors.

Both the 3-level hierarchical model and the down-weighting methods may mitigate the bias attaching to NRS, but they inevitably incorporate it into the final estimates. The degree of influence of NRS and hence the level of bias, is subject to arbitrary choices: neither method has the transparency or consistency needed for accountable decision making.¹⁹¹

By contrast, the NMA bias-adjustment approach^{176,177} (Section 13.1) can be applied to RCT and NRS evidence, to generate bias-adjusted and down-weighted estimates in a relatively objective way,¹⁸⁴ although modelling choices regarding direction of bias and its dependence on treatment comparison are necessary. An interesting extension¹⁹² adds a further parameter for probability of bias. While this increases flexibility, applications so far^{163,192} have used strongly informative, investigator-originated, priors for this parameter, again lacking in transparency.

14 | METHODS FOR DERIVING RECOMMENDATIONS FROM NMA

So far, we have assumed that the optimal treatment was the one with the highest expected value on the chosen evaluative criterion. This is theoretically optimal in an economic sense, ¹⁹³ but the implication that uncertainty does not matter ¹⁹⁴ jars with epidemiological thinking.

One way to liberalise the way recommendations are derived, suggested in our work on threshold analysis, would be to recommend all treatments showing an improvement of size X or more, relative to the standard reference treatment, and which are within a margin X of the most effective treatment.¹³⁸ The quantity X could, for example, be a minimal clinically important difference(MCID). Such a procedure automatically picks out the best K treatments, with K determined by the margin X. It could also be modified to take account of uncertainty by requiring a given posterior probability of superiority. A similar method was adopted in the GRADE Working Group's 2020 guidance on how to draw up recommendations. 195,196 However, the final GRADE categories are reconsidered in the light of their consistency with other pairwise comparisons, and as previously noted, a more certain treatment may in the end be

preferred to a less certain one with a higher expected efficacy. ^{67,132}

New methods for deriving ordered treatment rankings are being actively researched. Rankings based on the SUCRA (Surface under the cumulative ranking curve) statistic, or equivalently on the P-score statistic, reflect both the mean (rank) outcome value and its uncertainty. A more general formulation ranks treatments according to the probability that their effect exceeds a given threshold, and this can be extended to rankings that combine multiple outcomes, each with its own threshold.

Statistical decision theory^{202,203} provides another means of trading expected efficacy for certainty that is perhaps easier to justify theoretically. Put simply, the probability that a decision based on expected value is wrong gives rise to an expected loss, which can then be subtracted from the expected value of the decision, thus adjusting for uncertainty. Calculations of this sort, similar to those used to assess the value of acquiring further information,²⁰⁴ have been discussed in the context of value-based pricing of pharmaceutical products.^{205,206} Further research is needed to find a definition of optimality that will accommodate multiple treatment recommendations while penalising uncertainty, whether decisions are based on efficacy, cost-effectiveness, or some other evaluative function.

In the context of reimbursement decisions, methods that take account of uncertainty as well as expected value could have societal benefits, incentivizing the production of higher quality data,²⁰⁷ and countering the trend to include one-arm studies and other NRS evidence in estimates of causal effects.

15 | CONCLUSIONS

15.1 | Summary of findings

The first 20 years of NMA have been a period of transition. As the PMA practices accepted in social and educational sciences were adopted in clinical studies. Investigators may have become accustomed to averaging quantitatively heterogeneous treatment effects, but with too few trials to allow causes of heterogeneity to be identified. These practices were then carried over to the newly emerging NMA. But while tutorial papers and reporting guidelines were right to cite "concerns" and "challenges," 12,26 the emphasis was on the need to guard against inconsistency and intransitivity, while the practice of averaging over heterogeneous treatment effects remained unquestioned. In the Cochrane Handbook, the validity of NMA is said to rely on the fulfilment of the transitivity and coherence (loop consistency) assumptions, while heterogeneity is considered in the same

TABLE 3 Methods for reducing quantitative heterogeneity (between-studies variation) in evidence synthesis, with selected references.

Cause of heterogeneity		Methods to reduce heterogeneity
Treatment variation	heterogeneity, as instead be consider randomized to detreatments, which	ment (dose, co-treatments, and multiple components) have been averaged over in the primary analysis, creating nd then explored as effect modifiers rather than causal effects. Dose, treatment regime, and co-treatment should dered as treatment modifiers. Patients cannot be randomized to different characteristics, but they can be lifferent doses and co-treatments. NMA offers the opportunity to distinguish between different doses and co-ch reduces between-study heterogeneity relative to models that "lump" treatments together. In addition, the truent can be modelled, reducing the number of parameters and increasing network connectivity.
	Dose	For examples of dose models, see reference. ⁵³ More complex dose models for synthesis of pharmacometric studies are also available, known as model-based network meta-analysis. ^{219,220}
	Treatment components	These models are used when treatments consist of multiple components, each of which has a separate effect. The effects of each component are considered to be independent and additive on the linear predictor scale, although interactions may also be modelled. Examples include educational, cognitive, behavioural, and relaxation components in studies of psychological interventions; and long-acting beta agonists and inhaled corticosteroids as components in treatments for chronic obstructive pulmonary disease. Prequentist software is available. These methods are likely to assume greater importance in studies of complex or behavioral interventions, where between-trials variation in treatments is particularly large.
	Class effects	Class models are used when there are several treatments that can be considered "similar," 5,225,226 for example SSRI's for social anxiety. They are a compromise between assuming that a class of differen treatments all have the same effect, which may result in excessive heterogeneity, and assuming they a have independent and different effects which can lead to uncertain estimates. The class model assume the treatment effects are drawn from a distribution. 53
Bias Adjustment	RCT	Indicators of lower quality trials, such as lack of allocation concealment or lack of blinding, are not only associated with larger observed treatment effects (Section 13.1), but also with more between-study heterogeneity. Applications of NMA bias-adjustment models substantially reduce between-study heterogeneity by removing variation in bias. Estimation of, and adjustment for, bias, can be contrasted with approaches that simply document it or use it to downgrade evidence. 13.65,98,136
	NRS	The same methods can be applied to Non-Randomized Studies. Much of the between-studies variance seen in NRSs is absorbed into the bias distribution, reducing the between-studies variance in relative treatment effects. ¹⁸⁴ The other methods reviewed above (Section 13.3) result in estimates that are biased to an unknown extent.
Multiple outcomes and outcomes reported in different ways	separate synthe kinds of evidend outcomes of the them. 229 A standard standard single borrowing of stranslyses, 234–236 Modelling the strugborrowing of stranslyses of stranslyses, 234–236 Modelling the strugborrowing of stranslyses, 234–236	t more than one related outcome, and different trials frequently report different outcomes. Rather than a sis for each outcome, it is preferable, especially for decision making purposes, to incorporate the different ce into a single coherent model. The simplest approach is a within-trial synthesis combining multiple e same type and on the same scale into a single mean effect, taking account of the correlation between dard univariate synthesis can then follow. Alternatively, different scores, such as verbal and maths test combined into a composite outcome. Alternatively, different scores, such as verbal and maths test combined into a composite outcome. It is seen for multiple outcomes, with incomplete reporting across trials, Multivariate Normal Random Effects analysis has been proposed and extended to network meta-analysis. This is a generalization of negle outcome model to multivariate structures at both within- and between-trial levels, and in theory allow rength across outcomes. Estimates from MVNRE are, however, usually very close to those from univariate unless there is both a high proportion of missing data and a high correlation between outcomes. The cutural or logical relationships between outcomes directly, rather than just their correlation, allows a greater rength across outcomes. Some examples are given below. Models of this type should be checked for clinical their assumptions tested statistically wherever possible. Outcomes in trials of treatments for Psoriatic Arthritis are often recorded in terms of the proportion showing 50%, 75%, or 90% improvement in PASI (Psoriasis Area and Severity Index). Rather than a
	categories	snowing 50%, 75%, or 90% improvement in PASI (Psoriasis Area and Severity Index). Rather than a separate synthesis at each cutoff, a more robust and inclusive analysis can be achieved by treating these as ordered categorial outcomes, with a common treatment effect at each cutoff. 53,117 This correctly captures the negative correlations between proportions of responses falling into each category, and increases network connectivity. Similar ordered benchmarks are used in Rheumatoid Arthritis trials, based on the American College of Rheumatology scale: ACR-50, ACR-75, etc.
	Scale of Measurement	Trials of treatments for depression report outcomes on a wide range of scales, such as the Beck Depression Inventory, and the Hamilton Depression Rating Scale. Patient- and Clinician-Reported Outcomes of this sor are routinely used in studies of anxiety and many other psychological and neurological disorders. The usual strategy is to convert all mean treatment effects to Standardised Mean Differences by dividing the mean effect from each study by the study standard deviation (SD). This introduces unwanted heterogeneity, ²³⁸ alsk known as "range variation", ⁴⁵ because trial populations vary widely in their variance ²³⁹ and estimated SDs are also subject to sampling variation. One alternative is Ratio of Means, ²⁴⁰ which assumes that treatments act multiplicatively. If sufficient trials report on more than one scale, simultaneous synthesis and mapping of all outcomes onto a common scale has also been proposed. ^{239,241}

TABLE 3 (Continued)

Cause of heterogeneity		Methods to reduce heterogeneity
	Multiple time points	Binary outcomes reported at different time points can be converted to independent observations, and modelled with piece-wise constant hazards. ^{242,243} Multiple continuous observations in which the treatment effect is allowed to vary over time can be modelled using fractional polynomials, ²⁴⁴ or assuming functional forms specifically tailored to the evidence. ^{219,220}
	Structural relationships	Cancer studies may report either time to progression-free survival (PFS) or overall survival (OS), or both. A common approach has been to model the OS and PFS log hazard ratios using MVNRE, ²⁴⁵ and similar models are used routinely in the surrogate endpoint literature. ^{246–248} An alternative approach is to estimate NMA models of PFS and Post-Progression Survival (PPS), subject to the structural constraint PSF + PPS=OS, using area-under- the-curve (AUC) as an outcome, up to a restricted follow-up time. ²⁴⁹ This method requires that Kaplan Meier curves are digitized so that AUC can be measured. ²⁵⁰ The limitation to restricted mean survival can be avoided by using external register data to extrapolate survival curves. ^{251,252} Other examples where structurally related outcomes are reported in a variety of ways are: (1) combining data on PFS, OS and probability of response in a single model. ²⁵³ (2) combining data on median survival time, mean survival time, and proportion surviving. ²⁵⁴ (3) 'Chain of evidence' structures in which trials report one or more of: the proportion of patients reaching endpoint A, the proportion reaching later endpoint B, and the proportion reaching B conditional on having reached A. ²⁵⁵
Survival models	proportional hareconstruct the investigators to	-to-event (survival) trials is usually based on the reported hazard ratios from Cox survival models, assuming azards (PH). Most trial reports include Kaplan Meier curves and algorithms have been published which a original curve from the digitised image. ²⁵⁰ Although abandonment of the PH assumption requires adopt new measures of treatment effect, ²⁵⁶ it allows a wide range of more flexible models, ^{257,258} including neter survival curves, ^{257,259} fractional polynomials, ²⁶⁰ restricted mean survival time, ²⁶¹ splines, ²⁶² and piece-ial models. ²⁴²

way as in PMA.⁷⁰ Similarly, AHRQ guidance calls for (quantitative) homogeneity of direct evidence in NMA, but notes that this applies to all forms of synthesis, and the emphasis is again on checking inconsistency.²⁷ The fact that heterogeneity can itself introduce inconsistency, especially when there are few trials, and the dire impact, of having most NMA comparisons informed directly by only one or two trials (Figure 2), has not been widely appreciated.

NMA finds its natural place in medical decision making, where it is needed to compare specific treatments in specific patient populations. In this context, where quantitative heterogeneity and inconsistency are likely to be far less, NMA may be less problematic.

This paper has tried to clarify, if not resolve, the continuing controversies surrounding NMA. Our findings are:

- There is only one assumption, exchangeability, from which the consistency assumption can be derived, and which implies similarity and transitivity. However, this assumption is weak and hard to test, let alone verify, especially in small datasets; it is only in larger NMAs that it has any practical significance.
- Exchangeability places no limit on quantitative heterogeneity. But heterogeneity results in lack of interpretability, and when contrasts are informed by few trials, can increase realized error and lead to inconsistency between direct and indirect estimates.

- Estimates of relative treatment effects from PMA, indirect comparisons and NMA are estimates of causal effects: any interactions observed in investigations of subgroups are associations. For this reason, it is important that differences in treatments, such as dose differences, are analysed as different treatments, not as sub-groups.
- Network geometry is important to understanding how biased evidence in one part of the network could influence estimates elsewhere. It may also reflect biases in what evidence is collected or reported, but it cannot in itself cause NMA estimates to be biased.

15.2 | Recommendations for practice

Besides general recommendations on the need for threshold analyses, and other forms of sensitivity analysis such as quantitative bias analysis, ²⁰⁸ our main recommendation, in line with our main findings, is that quantitative heterogeneity should be minimized. Heterogeneity undermines the relevance of estimates to the target population (Section 6), and increases realized error and inconsistency, even under exchangeability, especially when contrasts are informed by small numbers of studies (Section 9). Reducing heterogeneity will also reduce the impact of any lack of exchangeability.

Clinical heterogeneity is an important source of between-trials variation. However, the decision to adopt

either a "narrow" or "broad" approach to patient inclusion is best taken by re-imbursement agencies or guideline developers, not methodologists, while bearing in mind that broad inclusion may result in quantitative heterogeneity and put recommendations at increased risk of error, to an extent determined by the between-studies SD. It is concerning that it may be difficult to reduce the heterogeneity in studies of psychological or complex interventions, where there is so much variation between interventions and their implementation as well as variation in study populations (Supplement Note 10).

There is a growing body of literature on statistical modelling methods for reducing quantitative heterogeneity in evidence synthesis (Table 3). This includes variation in treatments (dose, treatment components), bias-adjustment, methodological variation, and time-to-event (survival) outcomes. Many of these strategies are under-utilized.²⁰⁹ Also included in Table 3 are a range of multivariate methods that allow disparate forms of data, that would otherwise be analysed separately, to be aggregated into a single coherent analysis. This increases network connectivity and robustness of conclusions. Separate analysis of multiple outcomes ignores within-study correlations, increases heterogeneity, lowers the precision of estimates,²¹⁰ and creates a multiplicity problem.²¹¹ ML-NMR and NMI should be adopted whenever possible: these are the key methodologies capable of reducing the impact of between-trials variation in patient characteristics.

AUTHOR CONTRIBUTIONS

A. E. Ades: Conceptualization; methodology; writing – original draft; writing – review and editing. Nicky J. Welton: Methodology; writing – review and editing. Sofia Dias: Methodology; writing – review and editing. David M. Phillippo: Methodology; writing – review and editing. Deborah M. Caldwell: Conceptualization; methodology; writing – review and editing.

ACKNOWLEDGMENTS

The authors would like to thank JRSM's editors and reviewers for their contributions to the paper.

CONFLICT OF INTEREST STATEMENT

The authors declare no conflicts of interest.

DATA AVAILABILITY STATEMENT

Data sharing is not applicable to this article as no new data were created or analysed in this study.

ORCID

A. E. Ades https://orcid.org/0000-0001-7822-3552 Nicky J. Welton https://orcid.org/0000-0003-2198-3205 Sofia Dias https://orcid.org/0000-0002-2172-0221 David M. Phillippo https://orcid.org/0000-0003-2672-7841

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AUTHOR BIOGRAPHIES

A. E. Ades is Professor Emeritus at the University of Bristol, working on evidence synthesis for decision making and epidemiology. He received the Ingram Olkin award for Lifetime Achievement in Research Synthesis Methodology in 2010.

Nicky J. Welton is Professor of Statistical and Health Economic Modelling at the University of Bristol working on methods for evidence synthesis in healthcare decision-making. She is co-Director of the Guidelines Technical Support Unit for NICE, and Co-Director of the Bristol Technology Assessment Group.

Sofia Dias is Professor in Health Technology Assessment at the University of York working on methods for evidence synthesis in healthcare decision-making. She is Director of the NIHR funded Centre for Reviews and Dissemination/Centre for Health Economics Technology Assessment Reviews Group.

David M. Phillippo is Research Fellow in Evidence Synthesis at the University of Bristol. His research focuses on methods for network meta-analysis and population adjustment.

Deborah M. Caldwell is Professor of Epidemiology and Public Health at the University of Bristol, working on evidence synthesis for decision making and epidemiology. She is Co-Director of the NIHR funded Bristol Evidence Synthesis Group and Co-Convenor of the Cochrane Comparing Multiple Interventions Methods Group.

SUPPORTING INFORMATION

Additional supporting information can be found online in the Supporting Information section at the end of this article.

How to cite this article: Ades AE, Welton NJ, Dias S, Phillippo DM, Caldwell DM. Twenty years of network meta-analysis: Continuing controversies and recent developments. *Res Syn Meth.* 2024;1-26. doi:10.1002/jrsm.1700.