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The evolution of protoplanetary disc radii and disc masses in star-forming regions

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ABSTRACT

Protoplanetary discs are crucial to understanding how planets form and evolve, but these objects are subject to the vagaries of the birth environments of their host stars. In particular, photoionizing radiation from massive stars has been shown to be an effective agent in disrupting protoplanetary discs. External photoevaporation leads to the inward evolution of the radii of discs, whereas the internal viscous evolution of the disc causes the radii to evolve outwards. We couple *N*-body simulations of star-forming regions with a post-processing analysis of disc evolution to determine how the radius and mass distributions of protoplanetary discs evolve in young star-forming regions. To be consistent with observations, we find that the initial disc radii must be of the order of 100 au, even though these discs are readily destroyed by photoevaporation from massive stars. Furthermore, the observed disc radius distribution in the Orion Nebula Cluster (ONC) is more consistent with moderate initial stellar densities ($100 \text{ M}_{\odot} \text{ pc}^{-3}$), in tension with dynamical models that posit much higher initial densities for the ONC. Furthermore, we cannot reproduce the observed disc radius distribution in the Lupus star-forming region if its discs are subject to external photoevaporation. A more detailed comparison is not possible due to the well-documented uncertainties in determining the ages of pre-main-sequence (disc-hosting) stars.

Key words: methods: numerical-protoplanetary discs-photodissociation region (PDR)-open clusters and associations: general.

1 INTRODUCTION

Most stars form in groups with between 10 and 10^4 stellar siblings (Lada & Lada 2003; Gutermuth et al. 2009; Bressert et al. 2010). Some of these groups coalesce to form long-lived bound star clusters (Kruijssen 2012) or unbound associations (Wright 2020; Wright et al. 2022). While the evolution and fate of star-forming regions is likely to be more nuanced than this dichotomy, at early ages (<10 Myr) the stellar density in all of these regions significantly exceeds the stellar density in the Milky Way's disc by several orders of magnitude (Korchagin et al. 2003).

Planets are observed to be forming (Haisch, Lada & Lada 2001; Richert et al. 2018), and in some cases are thought to have already formed (Alves et al. 2020) when their host stars are still embedded in these stellar groups, implying that the birth environment of stars has a direct influence on the planet formation process (e.g. Adams 2010; Parker 2020).

The most dense star-forming regions ($\tilde{\rho} > 10^4 \, M_{\odot} \, pc^{-3}$) can cause the truncation of protoplanetary discs due to interactions with passing stars (Vincke & Pfalzner 2018; Winter et al. 2018a), and moderately dense star-forming regions ($\tilde{\rho} > 10^2 \, M_{\odot} \, pc^{-3}$) can lead to planetary orbits being altered or disrupted (Bonnell et al. 2001; Parker & Quanz 2012; Cai et al. 2017). Intriguingly, even star-forming regions with modest to low stellar densities ($\tilde{\rho} \ge 10 \, M_{\odot} \, pc^{-3}$) can affect

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planet formation if these regions contain stars massive enough to produce photoionizing extreme ultraviolet (EUV) and far-ultraviolet (FUV) radiation. EUV and FUV radiation readily evaporates the gas component of protoplanetary discs (e.g. Johnstone, Hollenbach & Bally 1998; Störzer & Hollenbach 1999; Hollenbach, Yorke & Johnstone 2000; Scally & Clarke 2001; Adams et al. 2004; Fatuzzo & Adams 2008; Winter et al. 2018b; Nicholson et al. 2019; Parker, Nicholson & Alcock 2021a; and many others), and to a lesser extent the dust (Haworth et al. 2018).

In addition to external photoevaporation from EUV/FUV radiation produced by massive stars, many other processes affect the evolution of protoplanetary discs, including internal photoevaporation from the host star, and both internal and external X-ray-driven evaporation (Picogna et al. 2019; Coleman & Haworth 2022). Notably, even in the absence of external effects, the disc is expected to evolve due to viscous spreading (Lynden-Bell & Pringle 1974; Hartmann et al. 1998), leading to rapid outward evolution of its radius (Concha-Ramírez et al. 2019a).

In previous work (Parker et al. 2021a), we have shown that the stellar density is the main factor in determining how many discs are destroyed by external photoevaporation. In some of those models, we also included a prescription for viscous spreading, and the net effect of this viscous evolution was to accelerate the mass lost from the disc due to photoevaporation. The reason for this is that the disc mass lost from photoevaporation, combined with spreading of the disc due to viscous evolution, acts to reduce the surface density of the disc and make the material more susceptible to further photoevaporation.

Table 1. A summary of the observational data with which we will compare our simulated disc radius and disc mass distributions. The table lists the star-forming region, the parameter (either mass or radius), the observational type (gas or dust), the line colour/style used in our figures, and the reference for these data. We also list the estimated age of each region and the reference for this age.

Region	Parameter	Obs. type	Line	Disc reference	Age (Myr)	Age references
ONC ONC	Radius Mass	Dust Dust	Solid red Solid red	Eisner et al. (2018) Eisner et al. (2018)	2.5	Jeffries et al. (2011), Da Rio et al. (2010)
Taurus Taurus	Radius Mass	Dust Dust	Solid pink Solid pink	Tripathi et al. (2017) Andrews et al. (2013)	1–6.3	Krolikowski, Kraus & Rizzuto (2021)
ρ Oph ρ Oph ρ Oph	Radius Radius Mass	Dust Dust Dust	Solid orange Dotted orange Solid orange	Tripathi et al. (2017) Cieza et al. (2019) Cieza et al. (2019)	0.3–6	Rigliaco et al. (2016), Grasser et al. (2021)
Lupus Lupus Lupus Lupus Lupus	Radius Radius Radius Mass Mass	Dust Gas Dust Dust Gas	Solid mint green Dashed mint green Dotted mint green Solid mint green Dashed mint green	Ansdell et al. (2018) Ansdell et al. (2018) Tazzari et al. (2017) Ansdell et al. (2016) Ansdell et al. (2016)	6	Luhman (2020)
Upper Sco	Radius	Dust	Solid purple	Barenfeld et al. (2017)	5–11	Preibisch et al. (2002), Pecaut, Mamajek & Bubar (2012)
Upper Sco	Mass	Dust	Solid purple	Barenfeld et al. (2017)		
σ Ori	Mass	Dust	Solid apple green	Ansdell et al. (2017)	3–5	Zapatero Osorio et al. (2002), Oliveira et al. (2002) Mayne & Naylor (2008)
λ Ori	Mass	Dust	Raspberry	Ansdell et al. (2020)	3–10	Mayne & Naylor (2008), Bell et al. (2013)

These simulations used the FRIED grid of models (Haworth et al. 2018), which show that the gas component of the discs is readily evaporated in radiation fields more than 10 times that of the background interstellar medium (ISM), but the dust component largely remains. However, work by Sellek, Booth & Clarke (2020) showed that external FUV photoevaporation would still alter the dust radius, with this roughly following the gas radius in their simulations.

There has also been a huge proliferation in observational data on protoplanetary discs (see Miotello et al. 2022, for a recent review), in part due to the (Atacama Large Millimeter Array (ALMA) telescope that has provided dust continuum measurements of disc masses and radii (Eisner et al. 2018; Otter et al. 2021), and in some cases detections of CO to trace the gas component of the discs.

In this paper, we compare the evolution of protoplanetary disc radii and disc masses in simulations in which we calculate the effects of mass-loss due to photoevaporation, and the subsequent inward evolution of the disc radius. In the same models, we also implement viscous evolution, which causes the disc radius to move outwards. We compare our disc radii, disc masses, and the overall fraction of discs to recent observational data.

The paper is organized as follows. In Section 2, we describe the observational data with which we will compare our models. In Section 3, we describe the set-up of the *N*-body simulations and the implementation of external photoevaporation, and viscous evolution, of the protoplanetary discs. We present our results in Section 4, we provide a discussion in Section 5, and we conclude in Section 6.

2 OBSERVATIONAL DATA

We will compare our simulated disc evolution to observational data from nearby star-forming regions. The observational data are collated from various sources, and the disc masses are usually derived from the continuum measurements of the dust component. Where the original papers quote disc masses, these are usually given in Earth masses (M_{\oplus}) . We assume a gas-to-dust ratio of 100 and multiply the dust masses by this factor to make a comparison with our simulations. In some of the papers, the continuum fluxes at 1.3 mm, $F_{1.3 \text{ mm}}$, are given and for ρ Oph we follow Cieza et al. (2019) and convert this into a dust mass (this is a simplified version of the method presented in Andrews et al. 2013, with various assumptions about the values used in the Planck function):

$$M_{\rm dust} = 0.58 \frac{F_{1.3\,\rm mm}}{\rm mJy} M_{\oplus}.$$
 (1)

For λ Ori, we follow Ansdell et al. (2020) and convert the continuum flux at 1.25 mm, $F_{1.25 \text{ mm}}$, into disc mass using

$$M_{\rm dust} = 4 \frac{F_{1.25\,\rm mm}}{\rm mJy} M_{\oplus}.$$
(2)

All other disc masses are taken directly from the papers cited in the fifth column of Table 1.

Similarly, the disc radii are usually taken directly from the literature sources, although the ρ Oph disc radii from Cieza et al. (2019) are estimated from the full width at half-maximum assuming a distance to the star-forming region of d = 140 pc.

The observational data are shown in Fig. 1. In panel (a), we show the disc radius cumulative distributions for the Orion Nebula Cluster (ONC, red line; Eisner et al. 2018), Taurus (pink line; Tripathi et al. 2017, note that this sample is likely to be incomplete), and Upper Sco (purple line; Barenfeld et al. 2017). We show data for ρ Oph from two different studies: Tripathi et al. (2017, the orange solid line) and Cieza et al. (2019, the orange dotted line). For Lupus, data on both the dust radii (mint green dashed line) and gas radii (mint green solid line) come from Ansdell et al. (2018) and the dust radii from Tazzari et al. (2017, the mint green dotted line, note that this sample is also likely to be incomplete). The initial radii in one set of our simulations are shown by the blue lines, designed to mimic the Eisner et al. (2018) distribution with mean 16 au and variance $\sigma_{\log rdisc} = 0.25$.

In panel (b), we show the disc mass cumulative distributions for σ Ori (the apple green line; Ansdell et al. 2017), the ONC (red line; Eisner et al. 2018), Taurus (pink line; Andrews et al. 2013), ρ Oph (the orange line; Cieza et al. 2019), Upper Sco (purple line; Barenfeld et al. 2017), and λ Ori (the raspberry line; Ansdell et al. 2020). Data



Figure 1. The observational data we will use to compare with our simulations. The blue lines in each panel are the initial conditions for our simulations. In panel (a), these blue lines are a Gaussian fit to the ONC data (the red line). In each panel, the mint green dashed line represents the respective gas distribution, whereas solid lines represent the dust distributions. Dotted lines indicate an alternative dust radius in ρ Oph (orange line) and Lupus (mint green line).

for both the gas masses and dust masses are shown for Lupus (the mint green lines; Ansdell et al. 2016). The initial mass distribution in all of our simulations (see the next section) is shown by the blue lines.

We will compare our simulated disc populations to the observational data at various ages. Stellar ages are notoriously difficult to estimate (Bell et al. 2013), and many of the star-forming regions we will compare our data with have more than one age estimate, or a broad range. For this reason, we will compare our simulations to the observations for a broad range of ages.

As an example, the current best estimate for the age of the ONC is around 2.5 Myr (Jeffries et al. 2011), but there is some debate about the range of ages, or age spread, in this region (Reggiani et al. 2011; Beccari et al. 2017). We will therefore compare our simulated disc radii, masses, and overall disc fraction to the observations for the ONC at both 1 and 5 Myr in the simulations. We adopt this practice for all of the observed star-forming regions.

To facilitate a comparison with our simulations, in Table 2, we calculate the stellar density and radiation field (in G_0) for each region. We calculate the local density for each star, $\tilde{\rho}$, which is the local volume density out to the 10th nearest neighbour. We first obtain the local surface density to the 10th nearest neighbour, then assume a depth of 1 pc to calculate the number density. We then convert this into a mass density by multiplying by the average mass in the initial mass function (IMF), i.e. $0.2 M_{\odot}$. We quote the median density in each region, but also show the interquartile range in the format $\tilde{\rho} = [\text{median}]_{-25}^{+75 \text{ percentile}}$. We do not have accurate mass determinations for all of the stars in each region, and so we multiply the number densities by this average mass. Note that these densities are the *median* in these regions; the central densities or the densities in the areas of highest clustering will be much higher (e.g. King et al. 2012).

In Table 2, we also show the numbers of stars that emit photoionizing radiation (i.e. those $\geq 5 M_{\odot}$) and the median and interquartile ranges of the FUV fluxes calculated in each star-forming region. To do this, we take FUV luminosities from Armitage (2000) and then calculate the flux at each $<5 M_{\odot}$ star. We then convert this flux into Habing (1968) units, $G_0 = 1.6 \times 10^{-3} \text{ erg s}^{-1} \text{ cm}^{-2}$, where $1G_0$ is the background flux in the ISM.

3 METHOD

In this section, we describe the *N*-body simulations we use to model star-forming regions, the post-processing analysis we use to follow the evolution of protoplanetary discs, and the observational data with which we will compare our simulations.

3.1 Star-forming regions

We model the dynamical evolution of young star-forming regions using the KIRA integrator within the Starlab environment (Portegies Zwart et al. 1999, 2001). This allows us to accurately calculate the FUV and EUV radiation fields used to determine the mass-loss due to photoevaporation from our protoplanetary discs.

We adopt several different sets of initial conditions for these simulations in order to model a comprehensive range of star-forming regions. Our models contain either N = 1500 or 150 stars, and we vary the initial radius so that the median local stellar density in the simulations varies between 10 and $1000 \text{ M}_{\odot} \text{ pc}^{-3}$.

We draw stellar masses from the IMF described in Maschberger (2013), which has a probability density function of the form

$$p(m) \propto \left(\frac{m}{\mu}\right)^{-\alpha} \left(1 + \left(\frac{m}{\mu}\right)^{1-\alpha}\right)^{-\beta}.$$
 (3)

Here, $\mu = 0.2 \text{ M}_{\odot}$ is the average stellar mass, $\alpha = 2.3$ is the Salpeter (1955) power-law exponent for higher mass stars, and $\beta = 1.4$ describes the slope of the IMF for low-mass objects (which also deviates from the lognormal form; Bastian, Covey & Meyer 2010). We randomly sample this distribution in the mass range $0.1-50 \text{ M}_{\odot}$, such that brown dwarfs are not included in the simulations. For simplicity, we also do not include primordial binaries, although these are likely ubiquitous in star-forming regions.

In the simulations where we draw N = 1500 stars from the IMF, we typically obtain between 10 and 50 stars with mass $\geq 5 M_{\odot}$, which would emit photoionizing radiation. When we select N = 150 stars, in some realizations, there are no stars $\geq 5 M_{\odot}$, although usually there are at least one to two examples (Parker et al. 2021a,b).

Region	Density $(M_{\odot} pc^{-3})$	OB star content	G_0	References
ONC	33^{+132}_{-12}	3 O-type stars, 8 B-type stars	14103^{+85221}_{-4326}	Hillenbrand & Hartmann (1998)
Taurus	$0.8^{+3.9}_{-0.1}$	None	1 (background ISM)	Güdel et al. (2007)
ρ Oph	13^{+25}_{-6}	2 B-type stars	57^{+202}_{-31}	Parker, Maschberger & Alves de Oliveira (2012)
Lupus	$0.2^{+1.9}_{-0.02}$	None	4 [from nearby (~10 pc) OB assoc.]	Galli et al. (2020), Cleeves et al. (2016)
Upper Sco	$0.6^{+1.2}_{-0.3}$	17 B-type stars	47^{+108}_{-29}	Luhman (2020)
σ Ori	$0.9\substack{+2.0 \\ -0.4}$	6 B-type stars	557^{+1786}_{-323}	Caballero et al. (2019)
λ Ori	2^{+5}_{-1}	1 O-type star, 6 B-type stars	1713_{-696}^{+4577}	Bayo et al. (2011)

Table 2. Stellar density and estimated radiation field (in G_0) for the star-forming regions in this work. The columns are the region, mass density, OB star content, G_0 (calculated in 2D), and the reference for the census (and in the case of Lupus, the estimate for G_0 from disc modelling).

Young star-forming regions are observed to exhibit spatial and kinematic substructure (Larson 1981, 1995; Gomez et al. 1993; Cartwright & Whitworth 2004; Sánchez & Alfaro 2009; Jaehnig, Da Rio & Tan 2015; Wright et al. 2016; Buckner et al. 2019). To mimic this in our initial conditions, we use a box fractal generator (Goodwin & Whitworth 2004), in which the degree of spatial and kinematic substructure is governed by just one parameter, the fractal dimension D. For details of the set-up of these fractals, we refer the interested reader to Goodwin & Whitworth (2004) and Daffern-Powell & Parker (2020), but we briefly describe them here.

The fractals are set up by placing a 'parent' particle at the centre of a cube of side N_{div} , which spawns N_{div}^3 subcubes. Each of these subcubes contains a 'child' particle at its centre, and the fractal is constructed by determining how many successive generations of 'children' are produced. The likelihood of each successive generation producing their own children is given by N^{D-3} , where *D* is the fractal dimension.

Fewer generations are produced when the fractal dimension is lower, leading to a less uniform appearance and hence more substructure. Star-forming regions with a low fractal dimension (e.g. D = 1.6) have a high degree of substructure, whereas regions with higher values (e.g. D = 2.0, 2.6) have less structure and regions with D = 3.0 are approximately uniform.

The velocities of the parent particles are drawn from a Gaussian distribution of mean zero, and the velocities of the child particles inherit this velocity plus a small random component that scales as N^{D-3} but becomes progressively smaller on each generation. This means that physically close particles have very similar velocities, but more distant particles can have very uncorrelated velocities.

In our simulations, we adopt D = 2.0 for all our simulations, which gives a moderate amount of spatial and kinematic substructure. We scale the velocities to a virial ratio $\alpha_{\rm vir} = T/|\Omega|$, where T and $|\Omega|$ are the total kinetic and potential energies, respectively. The velocities of young stars are often observed to be subvirial along filaments, so we adopt a subvirial ratio ($\alpha_{\rm vir} = 0.3$) in all of our simulations.

Finally, we scale the radii of the fractals to achieve the required stellar density. For our regions with N = 1500 stars, radii of 1, 2.5, and 5.5 pc lead to median local densities of 1000, 100, and $10 M_{\odot} \text{ pc}^{-3}$, respectively, whereas our regions with N = 150 stars have radii of 0.75 pc to establish initial stellar densities of $100 M_{\odot} \text{ pc}^{-3}$.

We evolve our simulations for 10 Myr using KIRA, in order to encompass the full protoplanetary disc evolutionary phase. We do not include stellar evolution in the calculations.

3.2 Disc photoevaporation and evolution

We follow the evolution of protoplanetary discs in a post-processing analysis, such that the discs are not included in the *N*-body integrations. We calculate the FUV radiation field for each star at each snapshot in the *N*-body simulations using the L_{FUV} luminosities in Armitage (2000):

$$F_{\rm FUV} = \frac{L_{\rm FUV}}{4\pi d^2},\tag{4}$$

where *d* is the distance from each low-mass star to each star with mass $\geq 5 \,\mathrm{M}_{\odot}$. Below this mass, the FUV flux becomes negligible. In the simulations that contain more than one massive star, we sum these fluxes to obtain the FUV radiation field for each disc-bearing star. This FUV radiation field is then scaled to the Habing (1968) unit, $G_0 = 1.8 \times 10^{-3} \,\mathrm{erg \, s^{-1} \, cm^{-2}}$, which is the background FUV flux in the ISM.

For each star in the range $0.1 < M_{\star}/M_{\odot} < 3$, we assign it a disc of mass

$$M_{\rm disc} = 0.1 \, M_{\star}.\tag{5}$$

We adopt three different distributions for the initial disc radii. First, we adopt a delta function where all the discs have radii $r_{\rm disc} = 10$ au, secondly, a delta function where all of the discs have $r_{\rm disc} = 100$ au, and finally, we draw discs from a Gaussian distribution of mean 16 au and variance $\sigma_{\log r_{\rm disc}} = 0.25$, designed to closely mimic the observed distribution of disc radii in the ONC (Eisner et al. 2018).

To calculate the mass-loss due to FUV radiation, we use the FRIED grid of models from Haworth et al. (2018), which uses the stellar mass M_{\star} , radiation field G_0 , disc mass M_{disc} , and disc radius r_{disc} as an input, and produces a mass-loss rate \dot{M}_{FUV} as an output. As the FRIED grid produces discrete values, we perform a linear interpolation over disc mass and mass-loss.

In addition to calculating the mass-loss due to FUV radiation, we also calculate the (usually much smaller) mass-loss due to EUV radiation. To calculate the mass-loss due to EUV radiation, we adopt the following prescription from Johnstone et al. (1998):

$$\dot{M}_{\rm EUV} \simeq 8 \times 10^{-12} r_{\rm disc}^{3/2} \sqrt{\frac{\Phi_i}{d^2}} \,\,{\rm M}_{\odot} \,\,{\rm yr}^{-1}.$$
 (6)

Here, Φ_i is the ionizing EUV photon luminosity from each massive star in units of 10^{49} s⁻¹ and is dependent on the stellar mass according to the observations of Vacca, Garmany & Shull (1996) and Sternberg, Hoffmann & Pauldrach (2003). For example, a 41 M_{\odot} star has $\Phi = 10^{49}$ s⁻¹ and a 23 M_{\odot} star has $\Phi = 10^{48}$ s⁻¹. The disc radius r_{disc} is expressed in units of au and the distance to the massive star *d* is in pc.

We subtract mass from the discs according to the FUV-induced mass-loss rate in the FRIED grid and the EUV-induced mass-loss rate from equation (6). Models of mass-loss in discs usually assume that the mass is removed from the edge of the disc (where the surface density is lowest), and we would expect the radius of the disc to decrease in this scenario. We employ a very simple way of reducing the radius by assuming that the surface density of the disc at 1 au, $\Sigma_{1 \text{ au}}$, from the host star remains constant during mass-loss (see also Haworth et al. 2018; Haworth & Clarke 2019). If

$$\Sigma_{1 \text{ au}} = \frac{M_{\text{disc}}}{2\pi r_{\text{disc}}[1 \text{ au}]},\tag{7}$$

where M_{disc} is the disc mass, and r_{disc} is the radius of the disc, then if the surface density at 1 au remains constant, a reduction in mass due to photoevaporation will result in the disc radius decreasing by a factor equal to the disc mass decrease.

The decrease in disc radius due to photoevaporation will be countered to some degree by expansion due to the internal viscous evolution of the disc. We implement a very simple prescription for the outward evolution of the disc radius due to viscosity following the procedure in Concha-Ramírez, Vaher & Portegies Zwart (2019b).

First, we define a temperature profile for the disc, according to

$$T(R) = T_{1 au} R^{-q}, \tag{8}$$

where *R* is the distance from the host star, and $T_{1 \text{ au}}$ is the temperature at 1 au from the host star and is derived from the stellar luminosity. For a 1 M_{\odot} star, we derive $T_{1 \text{ au}} = 393$ K, although $T_{1 \text{ au}} = 300$ K is more commonly adopted. We assume a main-sequence mass–luminosity relation, and use data from Cox (2000). We adopt q = 0.5 (Hartmann et al. 1998).

In the model of Hartmann et al. (1998), the characteristic initial radius $R_c(0)$ is defined by

$$R_c(0) = R' \left(\frac{M_\star}{M_\odot}\right)^{0.5},\tag{9}$$

where R' = 30 au. At some time *t*, the characteristic radius $R_c(t)$ at that time is given by (Lynden-Bell & Pringle 1974)

$$R_{c}(t) = \left(1 + \frac{t}{t_{\nu}}\right)^{\frac{1}{2-\gamma}} R_{c}(0),$$
(10)

where the viscosity exponent γ is unity (Andrews et al. 2010). t_{ν} is the viscous time-scale, and is given by

$$t_{\nu} = \frac{\mu_{\rm mol} m_p R_c(0)^{0.5+q} \sqrt{GM_{\star}}}{3\alpha (2-\gamma)^2 k_{\rm B} T R^q},$$
(11)

where μ_{mol} is the mean molecular weight of the material in the disc (we adopt $\mu_{mol} = 2$), m_p is the proton mass, *G* is the gravitational constant, M_{\star} is the mass of the star, $k_{\rm B}$ is the Boltzmann constant, and *T* and *R* are the temperature and distance from the host star, as described above. α is the turbulent mixing strength (Shakura & Sunyaev 1973), and based on observations of T Tauri stars, Hartmann et al. (1998) adopt $\alpha = 10^{-2}$ (see also Isella, Carpenter & Sargent 2009; Andrews et al. 2010). This α leads to significant viscous spreading, and we note that some recent work suggests much lower values, of the order of $\alpha \sim 10^{-3}-10^{-4}$ (Pinte et al. 2016; Flaherty et al. 2020). One can see from equations (11) and (10) that reducing α would reduce the size of the outward change in radius. To test this in our simulations, in Appendix B, we present results for simulations with $\alpha = 10^{-4}$.

We set $r_{\text{disc}} = R$ to be the radius of the disc, and following massloss due to photoevaporation and the subsequent inward movement of the disc radius according to equation (7), we calculate the change

Table 3. A summary of the different initial conditions of our simulated starforming regions. The columns show the number of stars, N_{stars} , the initial radius of the star-forming region, r_F , the initial median local stellar density, $\tilde{\rho}$, and the initial distribution for the radii of protoplanetary discs, r_d .

N _{stars}	r_F (pc)	$\tilde{ ho}({ m M}_{\odot}{ m pc}^{-3})$	r_d (au)
1500	1	1000	100
1500	2.5	100	10
1500	2.5	100	100
1500	2.5	100	Eisner et al. (2018)
1500	5.5	10	100
150	0.75	100	100

in characteristic radius $(R_c(t_n)/R_c(t_{n-1}))$ and scale the disc radius r_{disc} accordingly:

$$r_{\rm disc}(t_n) = r_{\rm disc}(t_{n-1}) \frac{R_c(t_n)}{R_c(t_{n-1})}.$$
(12)

Both the inward evolution of the disc radius due to mass-loss and the outward viscous evolution occur on much shorter time-scales than the gravitational interactions between stars in the star-forming regions. We therefore adopt a time-step of 10^{-3} Myr for the disc evolution calculations (Parker et al. 2021a).

In the calculations of Haworth et al. (2018), the mass lost from discs due to FUV radiation is predominantly gas, whereas the discs mostly retain their dust component. However, Sellek et al. (2020) find that during mass-loss, the dust radius follows the inward evolution of the gas radius. In our analysis, we assume that the mass lost from the disc is in the form of gas, and that the dust radius follows the gas radius (both inwards due to photoevaporation and outwards due to viscous spreading). However, we note that although the dust radius may follow the gas radius during photoevaporation, the two are by no means the same. Sanchis et al. (2021) and Long et al. (2022) find that the gas radii of discs in nearby star-forming regions (Lupus, ρ Oph, and Upper Sco) are at least a factor of 2 larger than the dust radii.

A summary of the simulations is given in Table 3.

3.3 Comparison with observational data

In our simulations, the initial disc radius is either 10 or 100 au, or drawn from a Gaussian to mimic the Eisner et al. (2018) distribution. At subsequent snapshots, the disc radius is set by equation (12). However, the observed disc radii are defined in different ways. In Lupus (Tazzari et al. 2017) and Upper Sco (Barenfeld et al. 2017), the radius is the point at which 95 per cent of the flux is enclosed, whereas for the ONC, Eisner et al. (2018) adopt the half-width at half-maximum (HWHM) major axes of Gaussian fits. Eisner et al. (2018) report a difference of less than a factor of 2 in these measurements. However, for Taurus and ρ Oph, Tripathi et al. (2017) adopt the point at which 68 per cent of the flux is enclosed.

Concha-Ramírez et al. (2019b) derive an expression using the characteristic radius R_c to convert between the full disc radius and the radius $R_{0.95}$ that encloses 95 per cent of the mass. They obtain $R_{0.95} \simeq 3R_c(t)$, and for the radius that encloses 68 per cent of the flux, $R_{0.68} \simeq R_c(t)$. As an example, after 10 Myr of viscous evolution with the parameters defined above, a 1 M_{\odot} star with $M_{disc} = 0.1$ M_{\odot} and initial disc radius $r_{disc} = 100$ au expands to a radius of 173 au. It has $R_c(t) = 56$ au, so $R_{0.95} \simeq 170$ au.

Given the similarities between $R_{0.95}$ and the radius defined by the Gaussian HWHM, we can make a direct comparison between the simulation data and the observed data for the ONC, Lupus,



Figure 2. The evolution of the local stellar density (the volume density within a sphere that encompasses the 10 nearest neighbours to each star) and the median G_0 field in our simulations. The top row shows the median local density in 10 realizations of the same star-forming region (indicated by the different blue lines). The bottom row shows the median FUV flux, G_0 , in each simulation, again shown by blue lines of different hues. The values for the observed star-forming regions are shown. We omit the G_0 value for Taurus, as this region does not contain any OB stars, nor is it close enough to an OB association to receive any flux from extra-associated stars, i.e. stars from a nearby star-forming region.

Upper Sco, σ Ori, and λ Ori. Because the disc radii for ρ Oph and Taurus are derived from $R_{0.68} \simeq R_c(t)$, when comparing our simulation data, a caveat is that a direct comparison would likely require a scaling of the observed disc distributions to larger radii. However, in the case of Taurus, this region has a low to non-existent G_0 field, so any disc photoevaporation would likely be minimal.

4 RESULTS

In all of our results, we show 10 realizations of the same simulation, identical apart from the random number seed used to generate the simulations. This means that statistically, the distributions of stellar masses, stellar positions, and stellar velocities are the same. However, each realization contains statistical variations, including in the numbers of massive stars in each simulation.

4.1 Evolution of stellar density and G₀

We begin by showing the evolution of the median local stellar density and the median G_0 in our simulations in Fig. 2. Each simulation is shown by a blue line of different hue, and the observed values are shown in different colours. The 'error' bars on $\tilde{\rho}$ and G_0 are the interquartile ranges of the observed values (i.e. the median, and 25th and 75th percentiles), whereas the error bars on the ages of the observed regions indicate the ranges quoted in the literature.

Of the observed regions, the ONC is closer to the N = 1500 star simulations in terms of the numbers of members, whereas Lupus, Taurus, ρ Oph, and σ Ori are closer to the N = 150 star simulations. λ Ori and Upper Sco straddle the two regimes. The present-day densities and G_0 fields in the ONC and λ Ori are both consistent with moderate to high $(100-1000 \text{ M}_{\odot} \text{ pc}^{-3})$ initial densities, whereas the other (low-*N*) regions are more consistent with moderately dense $(100 \text{ M}_{\odot} \text{ pc}^{-3})$ initial conditions. We will use these constraints when

interpreting the evolution of disc masses and radii in the following analysis.

4.2 Inward radius evolution only

We first show an example where the disc radii evolve inwards according to equation (7), but where there is no viscous spreading. In Fig. 3, the initial density of the star-forming region is $100 \text{ M}_{\odot} \text{ pc}^{-3}$, the region contains N = 1500 stars, and the disc radii are all initially $r_d = 100$ au. We show the disc radius (top row) and disc mass (middle row) distributions at 1, 5, and 10 Myr, and show the corresponding observational data for the younger regions (left-hand panels), all regions (middle panels), and the oldest regions (right-hand panels).

As mass is lost from the discs due to photoevaporation, the radii move inwards, but at such a rate that the simulated disc radius distributions are not consistent with those in the observed star-forming regions at any age [this discrepancy is worse for the simulations where the discs have even smaller (10 au) initial radii].

Despite the seemingly dramatic evolution of the discs, the massloss from the discs due to photoevaporation is relatively modest; no simulations are consistent with the observations of discs at ages of \sim 1 Myr. There is some overlap between our simulations and the observed regions at 5 Myr (determining accurate stellar ages and hence disc ages is notoriously difficult; Bell et al. 2013), but at 5 Myr, the disc radius distributions are completely inconsistent with the observed distributions.

We show the individual disc mass versus disc radius for one of our simulations at 1 and 5 Myr in Figs 3(g) and (h). The structure in the simulation data is caused by the resolution of the FRIED grid. When a disc loses mass due to photoevaporation, its radius moves inwards. However, if the new radius is closer to a different subset of FRIED models with smaller radii, the rate of photoevaporation



0.8

0.6

0.4

CDF

(g) 1 Myr (h) 5 Myr Figure 3. Results for simulations in which the initial disc radii are drawn from a delta function with $r_{\rm disc} = 100$ au, and the discs are only allowed to evolve inwards due to external photoevaporation. The star-forming regions have a moderate initial stellar density ($\tilde{\rho} \sim 100 \, M_{\odot} \, pc^{-3}$). In panels (a)–(c), we show the cumulative distributions of disc radii at different ages, and in panels (d)-(f), we show the cumulative distributions of disc masses. The blue lines of varying hues show the results from the 10 individual N-body simulations. The mint green dashed line represents the respective gas distribution in the Lupus star-forming region, whereas solid lines represent the dust distributions. Dotted lines indicate an alternative dust radius for ρ Oph (orange line) and Lupus (mint green line); see Table 1 for further details. In panels (g) and (h), we show the disc mass versus disc radius for four observed star-forming regions at 1 and 5 Myr, and data from one post-processed N-body simulation are shown by the black points. We plot the disc fractions (defined as when the discs have non-zero mass) as a function of time in our N-body simulations in panel (i), with observational data taken from Richert et al. (2018) and Ribas, Bouy & Merín (2015).

10

ONC

Oph

0.8

0.6

0.4

0.2

0

0.8

0.6

0.4

0.2

0.1

0.01

10

10

10

0.1

(Mo)

disc mass

0 × 10

CDF

Ó.1

Ori ONC

Oph

10

ONC

o Opl

10

(e) 5 Myr

10

(b) 5 Myr

CDF

1000

decreases and a 'pile-up' of points occurs. Both of these plots show that the masses of the surviving discs are too high to be consistent with the observational data.

NC

0.8

0.6

0.4

0.2

Ó.1

0.6

0.4

0.2

0 10

ONC

0.1

0.01

10-3

10

10

0.1

disc mass (M_o)

Op Op

upus

Uppe

CDF

10

disc radius (au)

(a) 1 Myr

 σ Ori

Taurus o Opł

10

10

(d) 1 Myr

10

disc radius (au)

100

1000

disc mass (M_{\odot})

0.01

0.1

ONC 0.8

100

CDF

Finally, we plot the evolution of the protoplanetary disc fraction in these simulations [i.e. the number of stars that have some $(M_{\rm disc} > 0)$ disc mass at a given time – in practice, most of the remaining discs are always $\gtrsim\,10^{-3}\,M_\odot$ – divided by the total number of stars that had discs initially] in Fig. 3(i). The simulation data are shown by the blue lines of various hues, and in this plot, we also show the observed disc fractions in star-forming regions.

The simulations display a wide range of disc fractions; in some models, up to 80 per cent of the discs are destroyed very quickly, whereas in others the destruction rate is much lower (20-50 per cent).

4.3 Including viscous evolution

We now present the results of simulations where in addition to inward evolution of the disc radius due to photoevaporation, we allow the discs to spread outwards due to viscous evolution. We keep the other parameters in the simulation fixed (i.e. initial stellar density, which remains at $100 \,\mathrm{M_{\odot}}\,\mathrm{pc^{-3}}$, and number of stars, N = 1500). The amount



Figure 4. Results for simulations in which the initial disc radii are drawn from a delta function with $r_{disc} = 100$ au, and the discs are allowed to evolve inwards due to external photoevaporation, and outwards due to viscous spreading. The star-forming regions have a moderate initial stellar density ($\tilde{\rho} \sim 100 \, M_{\odot} \, pc^{-3}$). In panels (a)–(c), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc masses. The blue lines of varying hues show the results from the 10 individual *N*-body simulations. The mint green dashed line represents the respective gas distribution in the Lupus star-forming region, whereas solid lines represent the dust distributions. Dotted lines indicate an alternative dust radius for ρ Oph (orange line) and Lupus (mint green line); see Table 1 for further details. In panels (g) and (h), we show the disc mass versus disc radius for four observed star-forming regions at 1 and 5 Myr, and data from one post-processed *N*-body simulations in panel (i), with observational data taken from Richert et al. (2018) and Ribas et al. (2015).

of viscous spreading depends quite strongly on the chosen viscous parameter, α , which is set to $\alpha = 10^{-2}$. In Appendix B, we show results for $\alpha = 10^{-4}$, which are very similar to the simulations where the discs evolve inwards due to photoevaporation only.

4.3.1 Initial disc radii $r_{disc} = 100 au$

In our first model with viscous evolution, we present the evolution of discs with initial radii all set to $r_{\text{disc}} = 100 \text{ au}$ in Fig. 4. In the first 5 Myr, the effects of photoevaporation cause the disc radii to

decrease, but this is countered by the effects of viscous spreading. When no viscous evolution was included (in Fig. 3), mass-loss from photoevaporation caused the inward decrease in radius, which in turn decreased the potency of photoevaporative mass-loss in the next time-step (as the surface density of material at the edge of the disc increased). However, when the disc then reacts to viscous spreading, the radius increases, lowering the surface density of material and making the disc more susceptible to further mass-loss due to photoevaporation.

In 4 out of 10 of our simulations, the majority (>85 per cent) of discs are destroyed within the first Myr (see Fig. 4i), and in the



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Figure 5. Results for simulations in which the initial disc radii are drawn from a delta function with $r_{\text{disc}} = 10$ au, and the discs are allowed to evolve inwards due to external photoevaporation, and outwards due to viscous spreading. The star-forming regions have a moderate initial stellar density ($\tilde{\rho} \sim 100 \text{ M}_{\odot} \text{ pc}^{-3}$). In panels (a)–(c), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc masses. The blue lines of varying hues show the results from the 10 individual *N*-body simulations. The mint green dashed line represents the respective gas distribution in the Lupus star-forming region, whereas solid lines represent the dust distributions. Dotted lines indicate an alternative dust radius for ρ Oph (orange line) and Lupus (mint green line); see Table 1 for further details. In panels (g) and (h), we show the disc mass versus disc radius for four observed star-forming regions at 1 and 5 Myr, and data from one post-processed *N*-body simulations in panel (i), with observational data taken from Richert et al. (2018) and Ribas et al. (2015).

remaining six simulations, the majority of discs are destroyed after 5–6 Myr. This is evident in the cumulative distributions of the disc radii at 5 and 10 Myr (panels b and c), where some of the lines only contain a handful of systems.

After 1 Myr of evolution, the disc radii in the simulations sit between the observed distributions in the ONC (the red line) and in Taurus and ρ Oph (the orange and pink lines), and then after 5 Myr, the majority of disc radii from the simulations are smaller than the observed distribution in the ONC and the other regions (Fig. 4b). As shown in Fig. 4(i), most of the discs are destroyed at 10 Myr, but those that survive are generally consistent with the observed distribution for Upper Sco (the purple line in Fig. 4i).

The disc mass distributions follow a similar pattern. After 1 Myr of evolution, most of the simulated disc distributions are consistent with the observed distributions for the ONC, Taurus, and ρ Oph. At 5 Myr, the disc mass cumulative distributions from the simulated data have moved to lower values, but individual simulations are also consistent with the majority of the observed data.

As more of the discs are destroyed between 5 and 10 Myr, there is a slight systematic shift in the cumulative distributions of the simulated discs to higher masses. This is not that the discs are gaining mass,

but rather the low-mass discs present at earlier times have been destroyed, and the cumulative distributions are dominated by the surviving, more massive discs. [At this stage in the simulations, the FUV radiation field is decreasing in strength as the star-forming regions expand, reducing the amount of mass-loss from discs (Parker et al. 2021a).]

The individual disc mass versus disc radius plots (Figs 4g and h) are consistent with the observations after 1 Myr, but then display lower masses than the majority of the observed discs, except for the older population in Upper Sco. In addition, the simulated disc masses are also higher than the observed disc fractions (Fig. 4i).

4.3.2 Initial disc radii $r_{disc} = 10 au$

In Fig. 5, we show the results for N = 1500, $\tilde{\rho} \sim 100 \,\text{M}_{\odot} \,\text{pc}^{-3}$ starforming regions where the initial disc radii are all drawn from a delta function with $r_{\text{disc}} = 10$ au.

The overall disc fraction decreases steadily throughout the 10 Myr period of the simulations, and is consistent with some of the higher observed disc fractions, but not the lower disc fractions at earlier ages [i.e. in panel (i), the (simulation) lines do not overlay the grey (observed) points for ages <4 Myr and disc fractions <50 per cent]. As many of the discs survive the duration of the simulation, the cumulative distributions of the simulation data do not display the low-*N* noise apparent in the data from the $r_{\text{disc}} = 100$ au simulations.

In general, the disc radii evolve to smaller values, although viscous spreading does lead to discs with radii up to 100 au. After 1 Myr, some of the simulation data are consistent with the observed disc radius distribution from the ONC, but no other star-forming regions (Fig. 5). At later times, the simulation data are not consistent with any of the observed distributions (Figs 5b and c).

The disc masses from the simulation data remain too high after 1 Myr to be consistent with the observations (Fig. 5d), and while they are consistent with the ONC after 5 Myr (Fig. 5e), at this age, the disc radius distributions are clearly inconsistent (Fig. 5b).

This is also seen in the plots that show the individual disc masses and disc radii. After 1 Myr, the disc masses are higher than those in the observed regions (Fig. 5g), and after 5 Myr, there are many discs with small radii and masses that cannot be directly compared to observational data (Fig. 5h).

We therefore suggest that for these initial conditions, the initial disc radii are likely to be much larger than 10 au, despite these discs being more susceptible to photoevaporation.

4.3.3 Initial disc radii from Eisner et al. (2018)

We also ran a set of simulations in which the disc radii were drawn from the Eisner et al. (2018) data, in order to demonstrate that the present-day disc radius distribution cannot be the initial distribution. Because the median disc radius in the data set is only a little over 10 au, we found very similar results to our numerical experiments with a delta function at $r_{disc} = 10$ au. We include these plots in Appendix A.

4.4 High stellar density

We now focus on star-forming regions with N = 1500 stars, but with high initial stellar densities ($\tilde{\rho} \sim 1000 \text{ M}_{\odot} \text{ pc}^{-3}$). Such high densities have been postulated as the initial conditions for some, and potenFirst, we note that in a similar vein to the moderate-density initial conditions, an initial disc radius distribution where the discs have small ($r_{disc} = 10 \text{ au}$) radii is inconsistent with the observational data. While some of the discs in the simulations survive the 10 Myr duration, the disc radius distributions rapidly evolve to small (<10 au) radii, even with viscous spreading counteracting (some of) the effects of inward evolution due to photoevaporation. As in the moderate-density simulations, the mass distributions of the surviving discs are not consistent with the observed distributions.

In Fig. 6, we show the evolution of discs where the initial radii are all $r_{disc} = 100$ au. In 4 out of 10 simulations, the discs are all destroyed in the first 0.5 Myr, and in the remaining six simulations, only between 5 and 20 per cent of discs remain (Fig. 6i).

After 1 Myr, the disc radii from the simulations are smaller than the observed data (Fig. 6a), although at 5 Myr several simulations are consistent with both the ONC and other regions (Taurus, ρ Oph, and Upper Sco), with the caveat that there are very few discs remaining at this time.

Interestingly, at all ages, several of the disc mass distributions from the simulations are consistent with the observed distributions (Figs 6d–f). However, the individual disc mass versus disc radius plots (Figs 6g and h), and the disc fractions (Fig. 6i), show that after 1 Myr, very few discs remain, due to the high G_0 fields in these dense regions.

Finally, we note that simulations with these densities could facilitate truncation of discs due to direct dynamical encounters, although such densities need to be maintained over several Myr (Vincke & Pfalzner 2018; Winter et al. 2018b). However, in our simulations, such high densities are not maintained for more than a \sim Myr (Fig. 2).

4.5 Low stellar density

The present-day density of nearby star-forming regions spans a wide range (Bressert et al. 2010), from several $M_{\odot} \text{ pc}^{-3}$ to several $100 \text{ M}_{\odot} \text{ pc}^{-3}$. In particular, of the observed regions, Taurus has a very low density (less than $5 \text{ M}_{\odot} \text{ pc}^{-3}$). We therefore run simulations with an initial median stellar density $\tilde{\rho} \sim 10 \text{ M}_{\odot} \text{ pc}^{-3}$. These simulations have radiation fields much lower than the high-density simulations (100–1000*G*₀), but still high due to the relatively high numbers of OB stars.

Again, for simulations in which the initial disc distribution is a delta function with $r_{\rm disc} = 10$ au, the evolution of the disc radius distribution moves inwards as the simulations progress, but when the disc radii are in the same regime as the observed distributions, the disc masses are too high, and when the mass distributions are consistent with the observations, the disc radii are too small. Furthermore, none of the simulations have disc fractions consistent with the observed disc fractions in Richert et al. (2018).

We therefore just focus on the simulations where the initial disc radii are drawn from a delta function with $r_{\rm disc} = 100$ au. In Fig. 7, we show the evolution of the disc radii and masses in these simulations. After 1–5 Myr, the disc radius distributions from the simulations are consistent with the observations of discs in Taurus, and ρ Oph, but not the ONC (Figs 7a and b). At later ages (10 Myr, Fig. 7c), the radius distributions from the simulations are consistent with the observations of Upper Sco.

The mass distributions from the simulations are consistent with those observed in Taurus and ρ Oph after 1 Myr (Fig. 7d), but at later times, the masses are too low. The continued destruction of



Figure 6. Results for simulations in which the initial disc radii are drawn from a delta function with $r_d = 100$ au, and the discs are allowed to evolve inwards due to external photoevaporation, and outwards due to viscous spreading. The star-forming regions have high initial stellar density ($\tilde{\rho} \sim 1000 \, M_{\odot} \, pc^{-3}$). In panels (a)–(c), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc masses. The blue lines of varying hues show the results from the 10 individual *N*-body simulations. The mint green dashed line represents the respective gas distribution in the Lupus star-forming region, whereas solid lines represent the dust distributions. Dotted lines indicate an alternative dust radius for ρ Oph (orange line) and Lupus (mint green line); see Table 1 for further details. In panels (g) and (h), we show the disc mass versus disc radius for four observed star-forming regions at 1 and 5 Myr, and data from one post-processed *N*-body simulations in panel (i), with observational data taken from Richert et al. (2018) and Ribas et al. (2015).

discs also preferentially removes low-mass discs, so after 10 Myr, the cumulative mass distributions of discs remaining in the simulations have actually evolved to higher masses [Fig. 7(f), though we reiterate that this is not because the discs have actually gained mass].

The simulations exhibit a wide range of disc fractions (Fig. 7i), encompassing the entire range of observed disc fractions at varying ages. The individual disc mass versus disc radius distributions (Figs 7g and h) show that the surviving population is consistent with the observations at 1 Myr, but consistent only with Upper Sco at 5 Myr.

4.6 N = 150 stars

Our analysis thus far has been based on star-forming regions with N = 1500 stars, which from a typical sampling of the IMF leads to around five massive stars that produce ionizing photons. We now present the results for star-forming regions that contain N = 150 stars, and from random sampling of the IMF, these regions contain far fewer massive stars (in some instances, no stars more massive than around 5 M_☉). Many of the star-forming regions with which we compare observational data (e.g. Taurus, ρ Oph, Lupus, σ Ori) only contain a few hundred stars.



Figure 7. Results for simulations in which the initial disc radii are drawn from a delta function with $r_{disc} = 100$ au, and the discs are allowed to evolve inwards due to external photoevaporation, and outwards due to viscous spreading. The star-forming regions have low initial stellar density ($\tilde{\rho} \sim 10 \, M_{\odot} \, pc^{-3}$). In panels (a)–(c), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc masses. The blue lines of varying hues show the results from the 10 individual *N*-body simulations. The mint green dashed line represents the respective gas distribution in the Lupus star-forming region, whereas solid lines represent the dust distributions. Dotted lines indicate an alternative dust radius for ρ Oph (orange line) and Lupus (mint green line); see Table 1 for further details. In panels (g) and (h), we show the disc mass versus disc radius for four observed star-forming regions at 1 and 5 Myr, and data from one post-processed *N*-body simulations in panel (i), with observational data taken from Richert et al. (2018) and Ribas et al. (2015).

We set the radii of the star-forming regions to be such that the initial median stellar density is the same as in our moderatedensity simulations, i.e. $\tilde{\rho} \sim 100 \, M_{\odot} \, \mathrm{pc^{-3}}$. We present the results for simulations in which the initial disc radii are drawn from a delta function with $r_{\rm disc} = 100 \, \mathrm{au}$.

We find that the disc radius distributions from our simulations are partially consistent with the observed regions (in particular, Taurus and ρ Oph) for discs $r_{\text{disc}} > \sim 50$ au, but there are too many discs with very small radii in our simulations (Figs 8a and b).

After 1 Myr of evolution, the disc mass distributions from the simulations are similar to many of those in the observed starforming regions (Fig. 8d), but then subsequent mass-loss causes the distributions in the simulations to evolve to lower masses than are observed (Fig. 8e). As with previous simulations, the surviving disc population at 10 Myr is consistent with the observations of Upper Sco, but not λ Ori (Fig. 8f).

As in the other simulations, the plots of individual disc mass versus disc radius are broadly consistent with some of the observed



Figure 8. Results for simulations in which the initial disc radii are drawn from a delta function with $r_{\text{disc}} = 100$ au, and the discs are allowed to evolve inwards due to external photoevaporation, and outwards due to viscous spreading. The star-forming regions have a moderate initial stellar density ($\tilde{\rho} \sim 100 \, M_{\odot} \, \text{pc}^{-3}$), but with fewer stars (N = 150). In panels (a)–(c), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc radius for ρ -Dody simulations. The mint green dashed line represents the respective gas distribution in the Lupus star-forming region, whereas solid lines represent the dust distributions. Dotted lines indicate an alternative dust radius for ρ Oph (orange line) and Lupus (mint green line); see Table 1 for further details. In panels (g) and (h), we show the disc mass versus disc radius for four observed star-forming regions at 1 and 5 Myr, and data from all 10 post-processed *N*-body simulations are shown by the black points. We plot the disc fractions (defined as when the discs have non-zero mass) as a function of time in our *N*-body simulations in panel (i), with observational data taken from Richert et al. (2018) and Ribas et al. (2015).

values (Figs 8g and h); in this instance, we have combined all 10 simulations due to the low number of stars in each individual simulation.

Finally, we note that in 4 out of 10 simulations, the fraction of discs is reduced within the first Myr, such that the simulations are not consistent with any observed disc fraction (see Fig. 8i). However, the simulations with lower FUV and EUV radiation fields retain a substantial number of discs, and are consistent with the observed disc fractions from Richert et al. (2018).

5 DISCUSSION

Before discussing our results, we deem it prudent to discuss the caveats in our models, as we are wary of overinterpreting some of the evolution we see in our simulated disc populations. We will then attempt to draw conclusions based on the evolution of the disc radius distributions, disc mass distributions, and disc fractions.

The observed disc fractions are usually calculated by determining whether a star has an infrared excess, thought to be the signature of a disc with micrometre-sized dust grains. Given that most of the mass lost from a disc due to photoevaporation is gas, comparing the disc fractions in our simulations with the observed fractions is unlikely to be a straightforward comparison.

A similar caveat exists when comparing the dust mass distributions. We have taken the observed disc masses, assumed a 1:100 dustto-gas ratio, and then adjusted the observed distributions accordingly. The mass lost due to FUV photoevaporation is predominantly gas, and so again conclusions drawn from these comparisons should be made with caution.

During the photoevaporation of the gas, the dust grains will likely be coagulating into larger grains that are subsequently prone to inward migration (Weidenschilling 1977b; Birnstiel, Dullemond & Brauer 2010) and settling about the disc mid-plane (Goldreich & Ward 1973; Drazkowska et al. 2022). It is therefore unclear whether the dust radius (as probed by the majority of the cited observational samples) accurately traces the gas radius.

Observations indicate that the gas and dust radii may be similar (e.g. Ansdell et al. 2018), although gas radii are likely to be higher by a factor of around 2 (Sanchis et al. 2021; Long et al. 2022) and simulations show the dust radius moves with the gas radius during disc evolution (both inward evolution due to external photoevaporation and outward evolution due to viscous spreading; Sellek et al. 2020).

Our initial disc mass distributions assume that the initial mass is 10 per cent of the host star mass, and we have not tested any other distributions in our analysis. We believe this is a reasonable assumption [discs in the early phases (Class I and Class II) of protostellar evolution are thought to have masses up to $0.1 M_{\star}$; e.g. Weidenschilling 1977a; Beckwith et al. 1990; Andrews & Williams 2005; Eisner & Carpenter 2006; Sheehan & Eisner 2017], although we note that other work assumes lower initial disc masses (e.g. Parker et al. 2021b), with lower masses leading to greater destruction of the disc population.

In the majority of our simulations, our initial disc radii are drawn from a delta function, with either $r_{\text{disc}} = 10$ au or $r_{\text{disc}} = 100$ au. Coleman & Haworth (2022) assume an initial radius distribution of the form

$$r_{\rm disc} = 200 \,\mathrm{au} \left(\frac{M_{\star}}{\mathrm{M}_{\odot}}\right)^{0.3}.$$
(13)

We note that in this distribution the smallest discs would have radii $r_{\rm disc} \ge 100$ au, assuming our lower limit to the stellar IMF of $M_{\star} = 0.1 \,\mathrm{M}_{\odot}$, and hence be even more susceptible to destruction from photoevaporation in our simulations.

Despite using a delta function as an input, the variable G_0 field and different disc mass for each individual star means that the disc radius distribution rapidly changes to resemble a similar shape to the observed distributions. We find that in the absence of viscous evolution, the change in the disc radius due to external photoevaporation never produces any of the observed disc radius distributions, with the surviving disc radii always being smaller than those in the observed star-forming regions.

We add a further caveat here that our prescription for the change in disc radius due to photoevaporation assumes the disc radius changes in proportion to the reduction in disc mass (following Haworth et al. 2018), but other implementations of the change in disc radius could potentially produce different results.

We find that assuming an initial disc radius distribution where the discs are $r_{\text{disc}} = 10$ au never produces the observed disc radius distributions, with the simulated disc radii all becoming too small. Conversely, these discs are less susceptible to mass-loss from photoevaporation, and their masses are always too high. As the observed ONC disc radius distribution (Eisner et al. 2018) has a median radius of \sim 20 au, we note that the ONC disc distribution must have evolved from a distribution with larger radii, unless the discs are initially much less massive than 0.1 M_{\star} .

The simulations that are most consistent with the observed disc radius distributions are those where the disc radii are $r_{disc} = 100$ au and the initial stellar density is $\tilde{\rho} \sim 100 \, M_{\odot} \, pc^{-3}$ (Fig. 4). The density in these simulations remains fairly constant over time (Parker et al. 2021a), but we note that the observed present-day density in the ONC is slightly higher, at around $400 \, M_{\odot} \, pc^{-3}$ (King et al. 2012). Analyses of the spatial and kinematic distributions of stars in the ONC suggest a much higher initial density (Allison et al. 2010; Allison & Goodwin 2011; Parker et al. 2014; Schoettler et al. 2020), which would place our results in tension with those dynamical considerations.

Simulations with more dense initial conditions for the ONC ($\tilde{\rho} \sim 1000 \ M_{\odot} \ pc^{-3}$, Fig. 6) would only be consistent with the disc radius observations if a fairly substantial number of discs with small radii (<5 au) exist, currently beyond the resolution of the observations. We note that these high densities are inconsistent with the observed disc fraction in the ONC, although this carries the significant caveat that we are mainly modelling the loss of gas from the discs, and the disc fractions are calculated based on infrared excess from micrometresized dust particles.

Low-density simulations ($\tilde{\rho} \sim 10 \, M_{\odot} \, pc^{-3}$, Fig. 7) produce radius (and disc mass) distributions that are consistent with the observations of Taurus and ρ Oph, as well as Upper Sco at later ages, but not the ONC.

Many of the observed star-forming regions contain only several hundred stars, and many of these regions do not contain very massive stars. However, Haworth et al. (2017) show that discs in Lupus have been affected by external photoevaporation, and in Fig. 8 we show the results from simulations with N = 150 stars, rather than N = 1500 stars. Interestingly, we cannot reproduce the disc radius distribution observed in Lupus with our models, suggesting that our models are missing a crucial aspect of disc evolution (Coleman & Haworth 2022). Haworth et al. (2017) suggest that the extended diffuse emission around IM Lup could be due to external photoevaporation from the OB association adjacent to this region. The radiation field in Lupus is still low (~4G₀), so any mass-loss due to photoevaporation rate of $\dot{M} \sim 10^{-8} \,\mathrm{M_\odot} \,\mathrm{yr^{-1}}$.

6 CONCLUSIONS

We present *N*-body simulations of star-forming regions of different stellar densities in which we calculate the EUV and FUV radiation fields from intermediate to massive stars (>5 M_{\odot}). We then perform a post-processing analysis to calculate the mass lost from protoplanetary discs depending on the strength of the radiation fields at each point in time in the simulations. We then calculate the inward evolution of the disc radii, and the outward evolution due to viscous spreading. We compare the radius and mass distributions to recent observations. Our conclusions are the following:

(i) Our simulated disc radius distributions are only consistent with the observational data if we allow viscous spreading to occur following any inward evolution of the disc radius due to external photoevaporation.

(ii) The initial disc distribution in the ONC cannot be the same as that currently observed, and we extend this conclusion to state that the initial disc radius distribution *must be* dominated by discs with radii $\gg 10$ au.

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(iii) The simulations that best reproduce the observed disc radius distribution in the ONC have only moderate ($\tilde{\rho} \sim 100 \, M_{\odot} \, pc^{-3}$) stellar densities, in tension with dynamical models for the ONC that predict much higher stellar densities. This tension can only be resolved if the external photoevaporation only destroys the gas component of discs and the observed discs in the ONC are mostly gas-free.

(iv) Our models fail to reproduce the relatively large radii observed in the Lupus star-forming region. This could be due to a lack of external photoevaporation in this star-forming region, although recent analysis tailored to Lupus suggests that external photoevaporation has occurred to the discs in this region (Haworth et al. 2017).

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DATA AVAILABILITY

The data generated in this study will be made available upon reasonable request to the corresponding author.

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APPENDIX A: THE ONC DISC RADIUS DISTRIBUTION AS SIMULATION INPUT

In Fig. A1, we show the results for regions with moderate stellar density ($\tilde{\rho} \sim 100 \,\mathrm{M_{\odot} \, pc^{-3}}$) where the initial disc radii are drawn from a similar distribution to that observed for the ONC (Eisner et al. 2018). As the median radius in this distribution is around 16 au, the distributions evolve in a very similar way to the simulations in which we set all of the disc radii to be $r_{\rm disc} = 10 \,\mathrm{au}$.



Figure A1. Results for simulations in which the initial disc radii are drawn from a Gaussian designed to mimic the observed Eisner et al. (2018) radius distribution, and the discs are allowed to evolve inwards due to external photoevaporation, and outwards due to viscous spreading. The star-forming regions have a moderate initial stellar density ($\tilde{\rho} \sim 100 \, M_{\odot} \, pc^{-3}$). In panels (a)–(c), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc masses. The blue lines of varying hues show the results from the 10 individual *N*-body simulations. The mint green dashed line represents the respective gas distribution in the Lupus star-forming region, whereas solid lines represent the dust distributions. Dotted lines indicate an alternative dust radius for ρ Oph (orange line) and Lupus (mint green line); see Table 1 for further details. In panels (g) and (h), we show the disc mass versus disc radius for four observed star-forming regions at 1 and 5 Myr, and data from one post-processed *N*-body simulation are shown by the black points. We plot the disc fractions (defined as when the discs have non-zero mass) as a function of time in our *N*-body simulations in panel (i), with observational data taken from Richert et al. (2018) and Ribas et al. (2015).

APPENDIX B: SIMULATIONS WITH $\alpha = 10^{-4}$

We run a set of our default simulations ($N_{\star} = 1500$, $\tilde{\rho} \sim 100 \,\mathrm{M_{\odot} \, pc^{-3}}$, $r_{\rm disc} = 100 \,\mathrm{au}$ with viscous evolution). However, for the turbulent mixing parameter, we adopt $\alpha = 10^{-4}$, instead of $\alpha = 10^{-2}$.

We show the evolution of the disc radii, disc masses, and disc fractions in Fig. B1. The effect of reducing α is that there

is very little viscous spreading, and inward evolution of the disc due to photoevaporation dominates instead. As a result, the disc radius and disc mass distributions, and disc fractions, are very similar to our simulations where solely inward evolution of the disc due to photoevaporation occurs (compare Fig. B1 with Fig. 3 – with very little difference between the two sets of plots).



Figure B1. Results for simulations in which the initial disc radii are all 100 au and the discs are allowed to evolve inwards due to external photoevaporation, and outwards due to viscous spreading, but where the viscosity parameter is now $\alpha = 1 \times 10^{-4}$, rather than $\alpha = 1 \times 10^{-2}$. The star-forming regions have a moderate initial stellar density ($\tilde{\rho} \sim 100 \, M_{\odot} \, pc^{-3}$). In panels (a)–(c), we show the cumulative distributions of disc radii at different ages, and in panels (d)–(f), we show the cumulative distributions of disc masses. The blue lines of varying hues show the results from the 10 individual *N*-body simulations. The mint green dashed line represents the respective gas distribution in the Lupus star-forming region, whereas solid lines represent the dust distributions. Dotted lines indicate an alternative dust radius for ρ Oph (orange line) and Lupus (mint green line); see Table 1 for further details. In panels (g) and (h), we show the disc mass versus disc radius for four observed star-forming regions at 1 and 5 Myr, and data from one post-processed *N*-body simulation are shown by the black points. We plot the disc fractions (defined as when the discs have non-zero mass) as a function of time in our *N*-body simulations in panel (i), with observational data taken from Richert et al. (2018) and Ribas et al. (2015).

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