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https://doi.org/10.1063/5.0045702

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Engineering electron wavefunctions in asymmetrically confined quasi onedimensional structures

Cite as: Appl. Phys. Lett. **118**, 124002 (2021); https://doi.org/10.1063/5.0045702 Submitted: 28 January 2021 • Accepted: 07 March 2021 • Published Online: 22 March 2021

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Cite as: Appl. Phys. Lett. **118**, 124002 (2021); doi: 10.1063/5.0045702 Submitted: 28 January 2021 · Accepted: 7 March 2021 · Published Online: 22 March 2021

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ABSTRACT

We present results on electron transport in quasi-one dimensional quantum wires in GaAs/AlGaAs heterostructures obtained using an asymmetric confinement potential. The variation of the energy levels of the spatially quantized states is followed from strong confinement through weak confinement to the onset of two dimensionality. An anticrossing of the initial ground and first excited states is found as the asymmetry of the potential is varied, giving rise to two anticrossing events, which occur on either side of symmetric confinement. We present results analyzing this behavior and showing how it can be affected by the inhomogeneity in background potential. The use of an enhanced source-drain voltage to alter the energy levels is shown to be a significant validation of the analysis by showing the formation of double rows of electrons, which correlate with the anticrossing.

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Electron transport in low-dimensional semiconductor nanostructures particularly one-dimensional (1D) systems generates widespread interest among theorists and experimentalists due to the rich fundamental aspects of quantum condensed matter physics. The two-dimensional electron gas (2DEG) formed at the interface of GaAs/AlGaAs heterostructure forms the basis of a typical 1D system.^{1–10} Using patterned split gates,³ the 2DEG is electrostatically constricted into a narrow 1D channel, a quantum wire, whose conductance consists of quantized plateaus in units of N.2e²/h, where N = 1,2,3... is the number of allowed 1D subbands and the factor 2 is due to spin degeneracy. Generally, in a strongly confined 1D system, the simplest approach is to assume a parabolic potential $(V_p(y) = m^* \omega^2 y^2/2)$, where ω is the angular frequency and m^* is the effective mass), with the electrons acting in a non-interacting manner.¹⁰ In order to search for interaction effects, the system was modified by incorporating a top gate to tailor the carrier concentration within the 1D channel, which resulted in many quantum features previously inaccessible^{5,7,8,11-14} including the observation of fractionally quantized conductance. In addition to reducing the carrier concentration in the 1D channel, the top gate helps weakening the confinement potential, which enhances electron-electron interactions to reconfigure a line of 1D electrons into two rows.^{5,7} This behavior was predicted theoretically on the basis that the increase in the Coulomb interaction $(V_c \sim e^2/r, \text{ where e is})$ the electronic charge and r is the separation between electrons, when $V_{\rm c}$ $\geq V_p$) would cause electrons to relax sideways^{15–17} despite the confinement potential. The net result is a reconfiguration of a line of 1D electrons into a localized zigzag and subsequently into a two-row spatial arrangement, an Incipient Wigner lattice. The zigzag requires electrons in one row to be located midway between the electrons in the other row, an aspect that cannot be confirmed by conductance measurements (supplementary material); however, the zigzag scenario of the formation of a new ground state with two centers of charge has been imaged by transverse electron focusing.¹⁸ The zigzag phase would occur when $r_s \cong r_0$, where r_s $\sim 1/2n_{1D}$ is the Wigner Seitz radius, n_{1D} is the density of 1D electrons, and $r_0 \sim (2e^2/\varepsilon m^* \omega^2)^{3/2}$ is the characteristic length scale, in which ε is the dielectric constant, when $V_c \sim V_p$, or $a_B \ll r$ and $r_0 \gg 1$, where a_B is the Bohr radius.^{16,17,19,20} The Wigner state of 1D electrons contains many intriguing spin and charges phases including a suggestion of paired electrons.

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Very recently, a low density, weakly confined, 1D quantum wire displayed fractional conductance plateaus when the confinement potential was tailored to be asymmetric and the system had entered a zigzag phase. This system resulted in a variety of fractional states that were particularly pronounced at 1/2, 1/4, 1/6, and 2/5 in the absence of a magnetic field.^{8,11} Numerical calculations performed on modified 1D systems^{19,23,24} suggested that the electron density and transverse confinement can be engineered effectively to investigate novel quantum effects.

In this Letter, we show that by tuning a variable confinement potential established by asymmetrically biasing a pair of split gates, two gapless states can be produced as a consequence of anticrossing of the initial, non-interacting, ground and first excited states in the 1D constriction.

The experimental devices were fabricated from GaAs/AlGaAs heterostructures grown using molecular beam epitaxy. The layer details for sample 1 and sample 2 are given in the supplementary material. The 2DEG formed up to 290 nm beneath the surface had a low-temperature mobility of 1.6×10^6 cm²/V s (2.0×10^6 cm²/V s) and an electron density of 9.0×10^{10} cm⁻² (1.0×10^{11} cm⁻²) for sample 1 (sample 2). A pair of split gates of length (width) $0.4 \,\mu m$ $(0.7 \,\mu\text{m})$ and a top gate of length 1 μm separated by a 300 nm thick insulating layer of cross-linked poly(methyl methacrylate) (PMMA) were patterned by a standard lithographic technique on sample 1, while sample 2 was without a top gate. The two-terminal differential conductance (G) measurements were performed using an excitation voltage of 10 μ V at 73 Hz in a cryofree dilution refrigerator with a lattice temperature of 25 mK.^{7,8} In Figs. 2 and 3, the transconductance (dG/dV_{sg}) of conductance data is plotted in a grayscale plot, where the regions in gray are the risers and black are plateaus in the conductance plot, respectively.

Numerical calculations^{10,23,25,26} indicate that symmetric biasing the split gates results in a parabolic potential and electrons are strongly confined. However, there has not been the same degree of investigation on the effects of decreasing the confinement potential with an asymmetric bias. This is particularly true of the case when the electron gas relaxes and the energy is determined by both the electron-electron repulsion and the spatial confinement.^{7,8,12}

We establish the asymmetry in the potential by applying a fixed voltage with an offset, $V_{\rm A}+\Delta {
m V}_{
m SG}$, to one of the split gates, A, and the other gate, B, whose voltage is $V_{\rm B}$, is then swept. The offset on A is then further incremented by a fixed value, ΔV_{SG} , and B is then swept as before [Fig. 1(a)]. Through this method, we are able to create an asymmetric 1D channel by applying an incremental offset voltage on gate A (gate B) and sweeping gate B (gate A). This approach will produce a variable confinement potential from being highly asymmetric to symmetric to again highly asymmetric (see the supplementary material). Widening the system by a highly asymmetric potential provides a weaker confinement of the electrons, enhancing the role of their mutual repulsion compared to the spatial confinement energy. The density distribution in the ground state for a wide channel screens and flattens the potential to produce a dual charge distribution as shown in Fig. 1(c).^{16,19,23} Numerical calculations performed in a square well with two particles showed the density distribution dividing into two as a function of the width of the well.²

Figure 2 shows conductance characteristics of a 1D quantum wire (sample 1) formed by split gates, and the top gate is held at zero



FIG. 1. (a) A schematic of asymmetric biasing on a pair of gates A and B. The transport direction is from source, S toward drain, D. The length, L, of the 1D channel is 400 nm, and the width, W, is 700 nm. (b) An artistic approach of a possible variation of the potential profile taking place in the system. The left triangular shape profile shows a possible case when gate A is acting like a hard wall, and gate B produces a varying potential. By offsetting gate A further, a symmetric parabolic potential can be achieved when equal confinement voltages are applied. The reverse situation of the triangular profile as seen on the right is achieved where gate B is now acting as a hard wall. (c) A cartoon to explain a possible mechanism where the density distribution takes a different form in a flat bottom potential as a function of increasing width of the channel. Here, $W1 < W_2 < W_3$.

voltage. A fixed voltage, $V_{\rm A}$, with an additional variable offset voltage, $\Delta V_{\rm SG}$ such that $V_{\rm A} + \Delta V_{\rm SG} =$ -0.4 V (here, $\Delta V_{\rm SG} =$ 0 V), is applied to gate A, and the voltage $V_{\rm B}$ on gate B is swept to produce the first trace on the left in Fig. 2(a). Next, ΔV_{SG} is successively incremented negatively by -0.1 V, and B is swept to produce successive conductance traces from left to right until the voltage on gate A becomes -5.8 V. Starting from the left, weakly resolved conductance plateaus are seen due to the channel being very wide and close to the 2D limit. At this stage, the system is highly asymmetric with $V_{\rm A} = -0.4$ V and $V_{\rm B} = -5.8$ V. Successive traces, formed by relaxing the asymmetry in confinement potential, show the emergence of well-defined plateaus along with a short lived $0.7(2e^2/h)$ feature, indicating that the system tends to enter a comparatively confined regime. Further relaxation of the asymmetry results in plateaus weakening again (traces between $V_{\rm B}$ of -5.5 to -4.0 V), with the second plateau at $4e^2/h$ weakening faster and before the plateau at $2e^2/h$, particularly shown by the trace at V_B \sim -4.0 V. On further relaxing the asymmetry, the plateau at 2e²/h disappears, resulting in an anticrossing as seen previously.^{5,7} We note that (1) the regular plateaus reappear as the offset on the gate is further increased until the far right where there is a weakening and (2) there is a gradual reduction in spacing between the consecutive conductance traces. This indicates that the electrons are more responsive to the change in split gates voltage as expected if the wavefunction is more extended across the channel so increasing the coupling to the gates. Figure 2(b) shows a grayscale plot showing a "well-defined" anticrossing of ground and first excited states illustrated by an arrow in black at $V_{\rm A} + \Delta V_{\rm SG}, V_{\rm B}$ (-1.5 V, -3.0 V). A second anticrossing may be present at $V_{\rm A} + \Delta V_{\rm SG}$, $V_{\rm B}$ (-5.7 V, -0.5 V), but the confinement is now such that levels are very close together approaching two dimensionality. We

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FIG. 2. (a) Conductance characteristics measured by sweeping voltage on gate *B*, $V_{\rm B}$, as a function of increasing negative offset voltage ($\Delta V_{\rm SG} = -0.1$ V) on gate *A* so that $V_{\rm A}$ ranges from -0.4 V(left) to -5.8 V(right). The inset shows a device schematic where split gates are shown in yellow and a top gate over the split gates in orange. (b) A grayscale plot showing an anticrossing of the ground and first excited states at $V_{\rm A} + \Delta V_{\rm SG}$, $V_{\rm B}$ (-1.5 V, -3.0 V) as indicated by a black arrow.

did not use the top gate in this measurement to avoid any possible electrostatic complication, and we establish that the top gate is not essential for the observation of anticrossing, a robust effect seen in top gated, split gates devices.^{5–7} There have been previous reports of observations of crossing and anticrossing of energy levels in trenched quantum wires and bilayer systems.^{28,29}

We show results from the 1D devices (sample 2) that were without any physical top gate over the split gates in Fig. 3. The voltage is fixed with an additional variable offset voltage, $V_{
m B}+\Delta V_{
m SG}$, initially at -1.15 V, corresponding to a highly asymmetric confinement, where $\Delta V_{\rm SG} = -0.05$ V is applied to gate *B*, and the voltage $V_{\rm A}$ is swept, which results in the conductance plots shown in Fig. 3(a). On the left, the system is highly asymmetric as $V_{\rm B} + \Delta V_{\rm SG} = -1.15 \, {\rm V}$ and $V_{\rm A}$ = -5.5 V and successive traces on relaxing the potential asymmetry show the emergence of well-defined plateaus, indicating that the system is entering a comparatively stronger confinement regime. On further relaxing (weakening), the asymmetry is observed by increasing the negative offset voltage on gate B (traces between V_B of -4.0 and -3.0 V), in which the second plateau at $4e^2/h$ weakens and reappears when the plateau at 2e²/h had weakened significantly so, giving rise to a direct jump in conductance from 0 to $4e^2/h$, as also seen in Fig. 2. Correspondingly, the grayscale plot in Fig. 3(b) shows a clear



FIG. 3. (a) Conductance characteristics measured by sweeping voltage on gate A, $V_{\rm A}$, as a function of increasing negative offset voltage ($\Delta V_{\rm SG} = -0.05$ V) on gate B so that $V_{\rm B}$ ranges from -1.15 V(left) to -6.65 V(right). The inset shows the device schematic where split gates are shown in yellow. (b). A grayscale plot showing two sets of anticrossing of the ground and first excited states, one at $V_{\rm A}$, $V_{\rm B} + \Delta V_{\rm SG}$ (-3.3 V, -2.0 V) and the other at $V_{\rm A}$, $V_{\rm B} + \Delta V_{\rm SG}$ (-1.6 V, -4.5 V). A dotted white line through the grayscale plot shows the subbands that are experiencing a symmetric potential. The inset shows a magnified view of conductance data shown in (a) where $V_{\rm A}$ ranges from \sim -2.1 to -1.0 V.

anticrossing at V_A , $V_B + \Delta V_{SG}$ (-3.3 V, -2.0 V), which we label AX1. On further increasing the negative offset voltage on gate *B*, the regular quantized conductance plateaus emerge until $V_{\rm A}\,{\sim}\,{-}1.6\,{\rm V}$ and $V_{\rm B}$ = -4.5 V. At this stage, the spacing between the traces is too narrow, and therefore, a magnified view of this section of data is shown in the inset in Fig. 3(b). Remarkably, there is another anticrossing (AX2) appearing at around $V_{\rm A}$, $V_{\rm B} + \Delta V_{\rm SG}$ (-1.6 V, -4.5 V), which was completed unexpected. Both the AXs are appearing due to (1) widening of the channel as shown in Fig. 1(c) and (2) an associated enhancement in the importance of the electron-electron interaction. The dotted white line illustrates an almost symmetric potential profile as the voltages on the two gates are almost similar along this line. This indicates that under the given voltage values, the system starts with a highly asymmetric potential, and with gradual lifting of the asymmetry, AX1 appears; further lifting the asymmetry past the anticrossing results in an almost symmetric potential to be felt by the electrons when they are along the white dotted-line regime. Beyond this, an increase in offset applied to gate B rebuilds the asymmetry in the system and the system generates a further anticross with the appearance of AX2. However, it

is not clear why a wide ground state should anticross with the previous ground and now first excited state. An inspection of the grayscale plot indicates that at a more negative voltage, there could be a transition between the first and second excited states. This previous second excited state, which is very broad, then anticrosses the ground state at AX1 so accounting for the further reduced separation of the plots, and such behavior of excited states has been found in the presence of a strong magnetic field.^{6,7} The conductance plateaus in this regime of behavior weaken at AX2 but do not disappear as they do so near AX1. It is also interesting that the new ground state following the anticross AX1 persists when the potential is symmetric, in agreement with a previous finding that an anticross can occur in a symmetric potential.^{5,7} These two effects occurring on either side of symmetric point (dotted white line) indicate that the system is very clean and free from major defects.

To confirm that the effect is not arising from an impurity potential, we repeated the measurement by swapping the gates, i.e., now, gate *B* is sweeping and the offset is applied on gate *A*. Similar results were obtained with two sets of anticrossings AX3 and AX4 (see the supplementary material).

Figure 4 shows the effect of applying a fixed dc source-drain bias of 3 mV on the conductance characteristics in sample 2, where gate A is swept, while an incremental offset is applied on gate B. Previous work has shown that measurements of differential conductance in the presence of an enhanced source-drain voltage have revealed that both spin and momentum degeneracy are lifted.³⁰ In Fig. 4, the first trace on the left is where the offset on gate *B* is set at $V_{\rm B} + \Delta V_{\rm SG} = -1.5 \,\rm V.$ The $0.25(2e^2/h)$ plateau persists despite increasing offset on the gate B or relaxing the asymmetric potential until around $V_{\rm A} \sim -3.5$ V when an additional plateau at 0.5(2e²/h) was observed (blue trace). This value of gate voltage is where the anticross occurs in the Ohmic regime with the weak first plateau being observed at 2e²/h and 0.5(2e²/h) absent, which further confirms that the confinement potential at the anticross results in two rows of charge each having a conductance of $0.25(2e^2/2h)$ as seen in Refs. 6 and 7. The existence of the two separate rows indicates that they do not couple, and their subsequent disappearance beyond the region of anticross implies that the two centers of charge have now linked in one wavefunction, i.e., the rows have become coupled.

The interaction between electrons and subsequent entanglement in closely separated rows such as ladder compounds is a topic of considerable interest. It has been suggested that the interaction between two rows in the quasi-1D system as described here is responsible for the observation of non-magnetic fractional quantization of conductance.^{8,11,12} The manner in which rows form and their subsequent behavior, such as whether completely separate or coupled in a single



FIG. 4. The effect of a fixed source drain bias, $V_{sd} = 3 \text{ mV}$, on the differential conductance of a device from sample 2 by sweeping gate A and offsetting gate B (i.e., $V_B + \Delta V_{SG}$) from -1.5 V(left) to -4.4 V (right) with increments of $\Delta V_{SG} = -0.06 \text{ V}$.

wavefunction, are, therefore, of considerable importance in understanding the mechanism underlying fractional quantization. In addition, fractional plateaus have been observed,¹² which possess even denominators pointing to the existence of electron pairing as a result of the row formation. Such pairing appears as a result of entanglement indicated by formation of a single wavefunction involving two centers of charge. It has been shown previously that a zigzag phase can be traced and imaged using transverse electron focusing where subpeaks corresponding to two centers of electron density are observed in the first focusing peak.¹⁸ This result combined with the analysis of conductance shown here and observation of row formation are very strong evidence for the confirmation of theoretical suggestions of rich spin and charge phases in the zigzag.^{13,14,16,17}

In conclusion, we have investigated the engineering of electron wavefunctions in quasi-1D channels. We have shown that there are two sets of anticrossings on either side of a symmetric, wide 1D channel as a function of manipulating asymmetry in the confinement potential. The formation of separate rows is confirmed by measurements of the non-Ohmic differential conductance. We suggest that exciting 1D quantum physics can be exploited using confinement manipulation, which enables us to follow the energy levels from the single electron situation where the levels are determined by the size quantization through the increasingly interaction dominated regime. The form of the wavefunctions and their energetics then deviate strongly from the independent electron behavior with a drastic change in the ground state and modification of the ground wavefunction, which becomes more laterally extended in the strongly interacting regime.

See the supplementary material for additional data to support experimental results.

The authors are grateful to the late Professor Berggren and Professor Bose for many fruitful discussions. This work was funded by the Engineering and Physical Sciences Research Council (EPSRC), United Kingdom Research and Innovation (UKRI), UK, and the UKRI Future Leaders Fellowship (Reference: MR/S015728/1).

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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