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Article

# Uniaxial Creep Test Analysis on Creep Characteristics of Fully Weathered Sandy Shale

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Abstract: The creep damage behavior of rocks is very important for evaluating the stability and safety of key rock engineering. Based on the Lianhua Tunnel Project in China, this paper aims to study the creep damage mechanics, the influencing factors and the creep constitutive models of sandy shale. In order to achieve these goals, a uniaxial compressive strength test and a creep test under different moisture contents and load levels were carried out. According to the test results, the creep parameters (elastic coefficients  $E_1$  and  $E_2$  and viscosity coefficients  $\eta_1$  and  $\eta_2$ ) of the Burgers Model were achieved, and the relationship between the creep parameters and moisture content,  $\omega$ , was established accordingly  $(E_1 = f(\omega), E_2 = f(\omega), \eta_1 = f(\omega), \eta_2 = f(\omega))$ . A fully weathered sandy-shale creep constitutive model considering moisture content was finally obtained. Test results showed that creep deformation increases with any increase in load level or moisture content, and the influence of moisture content is more significant. For instance, creep deformation increased by 35% when the load increased by 50%, and creep deformation increased by 82% when the moisture content increased by 45%. In addition, the creep rate in the steady stage and the duration of the primary creep stage increased with any increase in moisture content or load level. The higher the moisture content, the greater the influence of creep deformation on the total deformation. The creep model of fully weathered sandy shale showed that the elastic coefficients  $(E_1, E_2)$  and the viscosity coefficients ( $\eta_1$ ,  $\eta_2$ ) are negatively correlated to moisture content;  $E_1$  is negatively correlated to load level; and  $E_2$ ,  $\eta_1$  and  $\eta_2$  are positively correlated to load level. Qualitative and quantitative analysis of fully weathered sandy shale can improve the existing research of creep properties and is expected to provide theoretical support for treatment of large deformation disasters in the fully weathered sandy-shale stratum.

**Keywords:** fully weathered sandy shale; uniaxial creep test; Burgers model; moisture content; load level; creep constitutive model



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# 1. Introduction

The creep damage behavior of rocks is very important for evaluating the stability and safety of key rock engineering such as underground tunnels, high slope stability, dam basements and nuclear-waste disposal [1–5]. Thus, the study of rock creep has become one of the key points in the field of infrastructural construction.

Based on infrastructures such as the Wanfu Coal Mine [6] in China; the Renhuling Tunnel Project [7] in China; large caverns in Japan [8]; and other projects in Italy [9], Iran [10], etc., studies of rock creep characteristics were carried out by scholars at home and abroad.

In the aspect of the influence of the rock creep effect, Zhu et al. [11] indicated that the rock creep effect can bring unpredictable delayed failure for tunnel lining; Wang et al. [12]

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pointed out that the rock creep effect affects the long-term stability and the failure mode of tunnel lining. In the aspect of influencing factors of creep effect, Zhu et al. [7] and Sun et al. [6] conducted research on tuff and sandstone, respectively, and discussed the laws of how moisture content affects creep behavior. Chen et al. [8] studied the creep behavior of light tuff stone, coarse sandstone and sandy mudstone under triaxial compression and discussed the influence of rock properties and axial stress on creep behavior. Li et al. [13] studied the creep behavior of host salt rock and the influence of long-term mechanical and thermal loads. In the aspect of the creep constitutive equation, Okubo et al. [14] obtained the complete creep curves and the constitutive equation of Akiyoshi marble, Tako sandstone, Sanjome andesite, Kawazu tuff and Inada granite under a uniaxial compression test. Maranini et al. [9] presented an experimental study on the creep behavior of porous chalk and implemented an elastic-plastic model using the experimental results. Wang et al. [15] established a modified Nishihara Rheological Model considering the effect of thermal–mechanical coupling. Gutierrez-Ch et al. [16] proposed new soil/rock creep models through analyzing the applicability of the discrete element method with rate process theory. Zohravi et al. [10] proposed a new constitutive model for the time-dependent behavior of rocks with consideration of damage parameter.

As mentioned, most of the above studies were aimed at tuff, sandstone, mudstone, marble, andesite, granite and other types of rocks. There is still a lack of research on the creep characteristics of fully weathered sandy shale. However, in practical engineering, the fully weathered sandy-shale stratum is often undercrossed by mountain tunnel construction projects in the southwest of China. The fully weathered sandy-shale stratum can be easily disintegrated via groundwater immersion and has the characteristics of poor erosion resistance, developed joint fissures and soft and broken rock mass, which all lead to an indispensable creep effect. Due to the creep effect, fully weathered sandy-shale status is prone to causing large deformation disasters and tunnel instability, resulting in casualties, mechanical losses and construction delays and seriously affecting the safety of tunnel construction [17]. Thus, it is urgent to study the creep effect of fully weathered sandy shale. In addition, many scholars have tried to explore a suitable rock creep constitutive model and have reached a series of achievements; however, there is no ideal creep constitutive model with wide applicability. Hence, there is still much work to be carried out on the theoretical research of rock creep constitutive models [1].

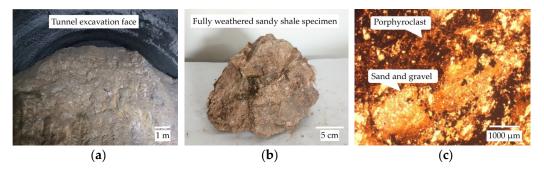
Therefore, based on the large deformation treatment engineering of fully weathered sandy shale in the Lianhua Tunnel of Pinglian Expressway in Jiangxi, China, this study carried out a uniaxial compressive strength experiment and a creep experiment to study creep mechanical behavior. On the basis of the Burgers model, the correlations between creep parameters and moisture content under different load levels were analyzed. The mathematical relationship between creep parameters and moisture content was established subsequently through means of data fitting and regression analysis. Finally, a creep model of fully weathered sandy shale, considering moisture content, was achieved. It is expected that these research findings can provide theoretical support for treatment of large deformation disasters in the fully weathered sandy-shale stratum.

# 2. Laboratory Experiments of Fully Weathered Sandy Shale

#### 2.1. Experimental Material

Fully weathered sandy shale is widely developed in the Lianhua Tunnel Project of Pinglian Expressway, Jiangxi, China. In practical engineering, when tunnel construction passes through this stratum, the surrounding rock, which is rich in water and weak and broken, is likely to be seriously destroyed and deformed. Large deformation disasters in the Lianhua Tunnel occur occasionally during the tunnel excavation. In order to study creep characteristics, fully weathered sandy-shale specimens were taken from where large deformation occurred in the Lianhua Tunnel Project. Images of fully weathered sandy shale in situ, in the lab and under a polarizing microscope (Nikon ECLIPSE-E200) are shown in Figure 1.

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**Figure 1.** Images of fully weathered sandy shale. (a) Fully weathered sandy shale in situ, (b) a specimen in the lab and (c) the lamellar texture under a microscope.

# 2.2. Uniaxial Compressive Strength Test

In order to obtain the strength-influence law and failure mode of fully weathered sandy shale under different moisture contents, a uniaxial compressive strength test was carried out. The test results thereof also provided the loading basis for the following creep test.

Accordingly with the Industrial Standard of China (JTG E41-2005): Rock Test Procedures for Highway Engineering [18], nine cylindrical standard specimens, each with a diameter of 50 mm and a height of 100 mm, were prepared. Three specimens were taken out to measure the average moisture content, which was 20.35% and considered the natural moisture content. The rest of the specimens were stored in the container, undisturbed.

For the purpose of analyzing the impact of the moisture content on fully weathered sandy shale, the rest of the specimens were divided into three groups (two in each group), whose moisture contents were close to 0%, 20.35% and 29.18%, respectively. The first group of specimens was placed in a drying oven to ensure that the moisture of the specimens was completely evaporated. The second group had the natural moisture content and needed no treatment. The third group was humidified with intermittent water replenishment until the moisture content reached the target content. After all of the specimens met the requirements, the uniaxial compressive mechanical test was carried out with a YSH-2 lime soil unconfined pressure gauge.

The uniaxial compressive strength and failure mode under different moisture conditions are shown in Table 1 and Figure 2.

Specimen Number	Moisture Content ω	nt ω Average Compressive Strength	
1–1; 1–2	Close to 0%	1068.8 kPa	

320.2 kPa

191.0 kPa

20.35%

29.18%

**Table 1.** Results of the uniaxial compression test.

2-1; 2-2

3-1; 3-2

It can be seen from Table 1 that compressive strength obviously decreased with increases in moisture content. The uniaxial strength value of fully weathered sandy shale was at the maximum in the dry state, which was 1068.8 kPa. The compressive strength was 320.2 kPa when the moisture content was 20.35%. However, the compressive strength was only 191 kPa when the moisture content reached 29.18%, which is about 82% lower than that in the dry state.

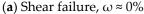
As shown in Figure 2, the failure modes of specimens in dry and wet states were different. In the dry state, oblique cracks appeared at the bottom of the specimen as soon as the load action was applied. Soon afterward, blocks shed off from the specimen, and a slight expansion appeared. The cracks gradually developed downward during the test, and the specimen was finally destroyed with the increasing load, forming a 30-degree surface of rupture through the specimen. This failure model can be called tensile shear failure. In the wet state, the expansion of the specimen was rather obvious, and vertical cracks appeared

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at the top of the specimen. Cracks at the top of the specimen gradually developed along the vertical direction and finally merged with the cracks caused by expansion. The specimen was finally destroyed and formed a vertical rupture surface; this is called tensile failure.

Compared with the wet state, rock in the dry state had relatively high compressive strength. From the microscopic perspective, the reason for this is that fully weathered sandy shale has developed pores and fissures; when moisture content is high, the cohesive strength between the particles would be obviously reduced, resulting in weakening of the integrity of the rock.







(**b**) Tensile failure,  $\omega = 29.18\%$ 

**Figure 2.** Failure modes from the uniaxial compressive test: (a) shear failure with a moisture content of close to 0% and (b) tensile failure with a moisture content of 29.18%.

#### 2.3. Uniaxial Creep Characteristic Test

In order to study the creep characteristics of the specimens, a uniaxial creep experiment was carried out. Test specimens were standard and cylindrical, each with a diameter of 50 mm and a height of 100 mm, which is the same as in Section 2.2.

### 2.3.1. Test Equipment

A triple uniaxial compression rheometer produced by Nanjing Soil Instrument Factory was used as the test equipment (shown in Figure 3). Load could be applied with manual loading weights. The displacement deformation of the specimen was measured with a dial gauge, and the data were recorded in real time.



(a) Composition of creep test system



(b) Test loading system

**Figure 3.** Uniaxial creep characteristic test system: (a) composition of the creep test system and (b) the test loading system.

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#### 2.3.2. Test Scheme

#### (1) The value of moisture content

In practical engineering, the large deformation disasters of the Lianhua Tunnel Project mainly occur in the rainy season. Thus, referring to the field-measured moisture content value of the project in the rainy season, the moisture contents of the specimens were determined to be 15.80%, 17.85%, 20.35%, 26.91% and 29.18%, respectively.

# (2) Step loading

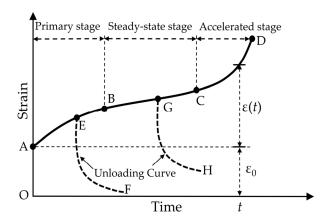
The loading method was step loading, which is applied step by step; the next step load cannot be applied until the deformation of the specimens becomes stable or the loading time meets the requirement. The specimens were installed at the center position of the equipment base so that the axial of each specimen coincided with the load line of the loading equipment to ensure that the specimen would not be damaged in the action of eccentric force.

According to previous research results, the sand layer would creep when the load reached 12.5~80% of the ultimate pressure [19]. On the basis of the peak strength of the specimen obtained from the uniaxial compressive strength test in Section 2.2, the minimum value of 191 kPa was chosen as the ultimate pressure to ensure that the specimen would not be instantaneously damaged due to high load. Thus, a five-grade load procedure was set up in this test at 20%, 30%, 40%, 50% and 60% of the ultimate pressure, accordingly (the values of the pressure were 38.2 kPa, 57.3 kPa, 76.4 kPa, 95.5 kPa and 114.6 kPa). Each level lasted for 52 h, and the subsequent load level could not be loaded until the specimen deformation had entered a stable state. The instantaneous displacement value of the specimen was recorded with measuring equipment as soon as the load was applied. The data was recorded at every 0.5 h in the first 6 h and at every 2 h after 6 h, at every load level. The indoor temperature was 25 degrees Celsius during the test.

# 3. Analysis of the Creep Test Results

# 3.1. Typical Rock Creep Curve

The typical creep curve of rocks under certain pressure is shown in Figure 4. In this figure,  $\varepsilon(t)$  represents the creep strain at time t, and  $\varepsilon_0$  represents the instantaneous strain under certain pressure. Thus, the total strain at time t under certain pressure is the sum of  $\varepsilon(t)$  and  $\varepsilon_0$ .



**Figure 4.** Typical rock creep curve, where AB is the primary creep stage, BC is the steady-state creep stage, CD is the accelerated creep stage, EF is the unloading curve during the primary creep stage, GH is the unloading curve during the steady-state creep stage,  $\varepsilon_0$  is the instantaneous strain and  $\varepsilon(t)$  is the creep strain at time t.

Creep deformation can be divided into three phases: AB, BC and CD. The OA segment is instantaneous strain, with no creep occurring. The AB segment is the waning phase of creep, with a decreasing curve slope and a decreasing deformation rate, that is called

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the primary creep stage. It can be seen from the unloading curve, EF, that the form of deformation is mainly elastic in this stage. The BC phase is called the steady-state creep stage, where the curve slope is constant and the deformation rate is basically unchanged. It can be seen from the unloading curve, GH, that both elastic and plastic deformation occur in this stage. The CD stage is called the accelerated creep stage, where the curve is upward and the slope increases sharply with time. At this stage, deformation is mainly plastic and the rock is prone to damage.

# 3.2. Creep Characteristic Test-Result Analysis

The uniaxial creep characteristic test results of fully weathered sandy shale with different moisture contents are shown in Figure 5 and Table 2.

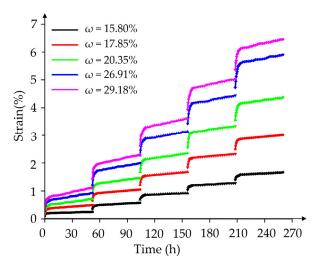


Figure 5. Strain-time curve of step loading.

**Table 2.** Creep characteristics of specimens with different moisture contents.

Moisture Content	Pressure (kPa)	Instantaneous Elastic Deformation (mm)	Steady Creep Deformation Rate (mm/h)	Creep Deformation (mm)
	38.2	0.102	$1.06 \times 10^{-3}$	0.148
	57.3	0.105	$1.62 \times 10^{-3}$	0.206
15.80%	76.4	0.109	$1.68 \times 10^{-3}$	0.226
	95.5	0.110	$1.72 \times 10^{-3}$	0.257
	114.6	0.114	$2.27 \times 10^{-3}$	0.271
	38.2	0.159	$2.96 \times 10^{-3}$	0.333
	57.3	0.161	$3.10 \times 10^{-3}$	0.396
17.85%	76.4	0.163	$3.23 \times 10^{-3}$	0.464
	95.5	0.164	$3.42 \times 10^{-3}$	0.491
	114.6	0.169	$3.60 \times 10^{-3}$	0.514
	38.2	0.194	$4.75 \times 10^{-3}$	0.524
	57.3	0.197	$4.93 \times 10^{-3}$	0.560
20.35%	76.4	0.199	$5.16 \times 10^{-3}$	0.681
	95.5	0.202	$5.37 \times 10^{-3}$	0.793
	114.6	0.204	$5.50 \times 10^{-3}$	0.825
	38.2	0.270	$6.54 \times 10^{-3}$	0.659
	57.3	0.276	$7.03 \times 10^{-3}$	0.731
26.91%	76.4	0.277	$7.15 \times 10^{-3}$	0.867
	95.5	0.280	$7.70 \times 10^{-3}$	1.018
	114.6	0.284	$8.16 \times 10^{-3}$	1.176

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Table 2. Cont.

Moisture Content	Pressure (kPa)	Instantaneous Elastic Deformation (mm)	Steady Creep Deformation Rate (mm/h)	Creep Deformation (mm)
	38.2	0.321	$8.72 \times 10^{-3}$	0.800
	57.3	0.324	$8.84 \times 10^{-3}$	0.861
29.18%	76.4	0.328	$9.05 \times 10^{-3}$	0.974
	95.5	0.331	$9.26 \times 10^{-3}$	1.130
	114.6	0.410	$9.38 \times 10^{-3}$	1.204

The test results show that the creep deformation of fully weathered sandy shale has the following rules:

- (1) The specimen undergoes instantaneous elastic deformation as soon as the load is applied. With an increase in loading time, the creep undergoes the primary creep stage and the steady-state creep stage. At the end of loading, the creep deformation tends to be stable and has not yet entered into the accelerated creep stage;
- (2) The instantaneous elastic deformation of the specimen increases with an increase in moisture content. For instance, under a load of 38.2 kPa, the instantaneous elastic deformation was 0.102 mm with a moisture content of 15.8%, while the instantaneous elastic deformation was 0.321 mm with a moisture content of 29.18%. The instantaneous elastic deformation increased by 68% when the moisture content increased by 45%. The reason for this is that the increase in moisture content weakens the cementation force and the friction force between the soil particles and results in the increasing deformation of the specimen;
- (3) The ratio of creep deformation to total deformation increases with any increase in moisture content. For instance, under a load of 38.2 kPa, the deformation of the specimen with a moisture content of 15.8% accounted for 59% of the total deformation, while the deformation of the specimen with a moisture content of 29.18% accounted for 71%. This shows that the higher the moisture content, the greater the influence of the creep deformation on the total deformation of fully weathered sandy shale, which needs great attention in engineering;
- (4) The test results show that the higher the moisture content and the higher the load level, the longer the initial creep duration of the specimen. For instance, when the moisture content was 15.8%, the duration of the initial creep was 90 min under the load of 38.2 kPa, while the duration of the initial creep was 130 min under the load of 57.3 kPa. When the moisture content was 29.18%, the duration of the initial creep was 120 min under the load of 38.2 kPa, while the duration of the initial creep was 190 min under the load of 57.3 kPa. In other words, when the moisture content increased from 15.8% to 29.18% under the load of 38.2 kPa, the duration of the initial creep increased by 25%. When the load level increased from 38.2 kPa to 57.3 kPa, the duration of the initial creep increased by 31%, with a moisture content of 15.8%. The main reason for this is that the existence of water makes the internal pores of the specimen interpenetrate. A specimen with higher moisture content needs more time to adjust and reorganize the initial particles to reach a steady state;
- (5) Creep deformation increases with any increase in load level or moisture content, and the influence of moisture content is more significant. For instance, when the moisture content was 15.8%, the creep deformation was 0.148 mm under a load of 38.2 kPa and 0.226 mm under a load of 76.4 kPa. That is, the creep deformation increased by 35% when the load increased by 50% under the same moisture content. Under a load of 38.2 kPa, the creep deformation was 0.148 mm when the moisture content of the specimen was 15.8% and 0.800 mm when the moisture content of the specimen was 29.18%. That is, the creep deformation increased by 82% when the moisture content increased by 45% under the same load level;

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(6) The steady creep deformation rate increases with any increase in moisture content or load level, and the influence of moisture content is more significant. For instance, when the moisture content was 15.8%, the steady creep deformation rate was  $1.06 \times 10^{-3}$  mm/h under a load of 38.2 kPa and  $1.68 \times 10^{-3}$  mm/h under a load of 76.4 kPa. That is, the steady creep deformation rate increased by 37% when the load increased by 50% under the same moisture content. Under a load of 38.2 kPa, the steady creep deformation rate was  $1.06 \times 10^{-3}$  mm/h when the moisture content of the specimen was 15.8% and  $1.06 \times 10^{-3}$  mm/h when the moisture content of the specimen was 15.8%. That is, the steady creep deformation rate increased by  $1.06 \times 10^{-3}$  mm/h when the moisture content of the specimen was  $1.06 \times 10^{-3}$  mm/h when the moisture content of the specimen was  $1.06 \times 10^{-3}$  mm/h when the moisture content of the specimen was  $1.06 \times 10^{-3}$  mm/h when the moisture content of the specimen with low moisture content was close to zero, and the creep deformation no longer increased. Therefore, reducing moisture content is beneficial in controlling creep deformation and ensuring stability of rock.

#### 4. Creep Model of Fully Weathered Sandy Shale, Considering the Moisture Content

It can be seen above that moisture content has a significant influence on the creep characteristics of fully weathered sandy shale. In this chapter, based on the Burgers creep model, creep equations of fully weathered sandy shale, considering moisture content, are established in order to describe its creep behavior more comprehensively.

#### 4.1. Creep Model of Fully Weathered Sandy Shale

The creep experiment curve of the fully weathered sandy shale has the following characteristics:

- (1) Instantaneous deformation occurs at the moment of loading and the deformation of the specimen can be partially recovered after unloading, so there must be elastic elements in the creep model.
- (2) There is a nonlinear relationship between deformation and time. The deformation of the specimen increases with an extension of loading time.
- (3) The uniaxial compressive strength of the specimen was low and the integrity was poor. The creep phenomenon appeared at a relatively low stress level.

Based on the above points, the Burgers model, which is suitable for viscoelastic soil, was chosen as the basic creep model for fully weathered sandy shale. The Burgers creep model is shown in Figure 6. The elastic component shown in the figure is represented with a spring, and its stress–strain relationship satisfies Hooke's law. The viscous component shown in the figure is represented with a dashpot, and its stress–strain rate relationship is linear. If the elastic component and the viscous component are connected in series, the model is called Maxwell-body. If the elastic component and the viscous component are connected in parallel, the model is called Kelvin-body. In Figure 6,  $E_1$  and  $E_2$  are the elastic coefficients of Maxwell-body and Kelvin-body, respectively, and  $E_1$  and  $E_2$  are the corresponding elastic strain;  $E_1$  and  $E_2$  are the viscosity coefficients of Maxwell-body and Kelvin-body, respectively, and  $E_1$  and  $E_2$  are the corresponding viscous strain.

The constitutive equation of the Burgers model is shown in Equation(1):

$$\sigma + \left(\frac{\eta_2}{E_1} + \frac{\eta_2}{E_2} + \frac{\eta_1}{E_2}\right)\dot{\sigma} + \frac{\eta_1\eta_2}{E_1E_2}\ddot{\sigma} = \eta_1\dot{\varepsilon} + \frac{\eta_1\eta_2}{E_2}\ddot{\varepsilon} \tag{1}$$

In this equation,  $\sigma$  is the initial compressive stress;  $\dot{\sigma}$  is the stress rate;  $\ddot{\sigma}$  is the change rate of the stress rate;  $\dot{\varepsilon}$  is the strain rate;  $\dot{\varepsilon}$  is the change rate of the strain rate; and the meanings of  $E_1$ ,  $E_2$ ,  $\eta_1$  and  $\eta_2$  are as described above.

When the stress,  $\sigma$ , is constant, the creep equation is simplified as Equation (2) and the Burgers creep curve is shown in Figure 7, where t is loading time;  $\varepsilon$  is the strain of surrounding rock; and the meanings of  $E_1$ ,  $E_2$ ,  $\eta_1$  and  $\eta_2$  are as described above.

$$\varepsilon(t) = \frac{\sigma}{E_1} + \frac{\sigma}{\eta_1}t + \frac{\sigma}{E_2}\left(1 - e^{-\frac{E_2}{\eta_2}t}\right) \tag{2}$$

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Through the methods of data fitting and regression analysis, creep parameters in the Burgers model can be obtained on the basis of creep experiment results. The fitting results and the values of each parameter are shown in Figure 8 and Table 3. All of the correlation coefficients,  $R^2$ , of the equations were greater than 0.99, indicating that the Burgers model fits well with the experimental data.

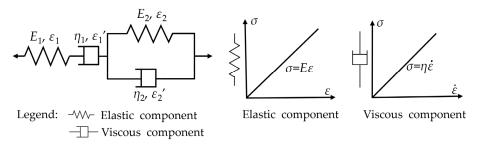


Figure 6. The Burgers creep model: a combination of elastic components and viscous components.

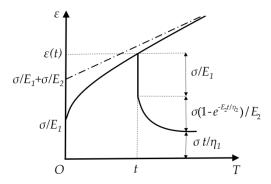
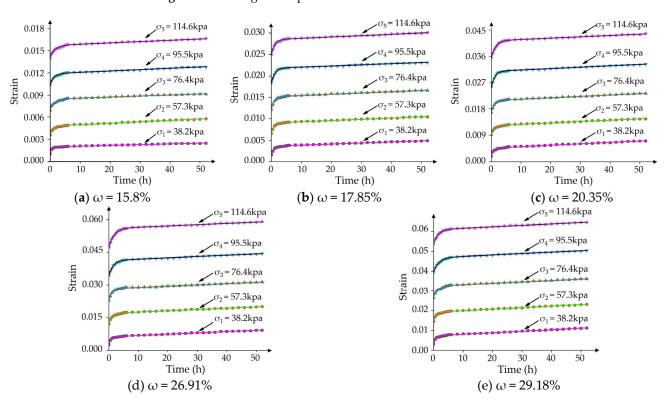


Figure 7. The Burgers creep curve.



**Figure 8.** Fitting results of strain–time curves: (a)  $\omega = 15.8\%$ , (b)  $\omega = 17.85\%$ , (c)  $\omega = 20.35\%$ , (d)  $\omega = 26.91\%$  and (e)  $\omega = 29.18\%$ .

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**Table 3.** Creep model parameters.

Moisture Content	σ (kPa)	E <sub>1</sub> (kPa)	E <sub>2</sub> (kPa)	η <sub>1</sub> (kPa·h)	η <sub>2</sub> (kPa·h)
	38.2	37,106	41,455	2,666,666	22,238
	57.3	15,896	49,291	3,980,900	55,653
15 000/	76.4	10,919	51,881	5,471,200	86,896
15.80%	95.5	9172	64,157	5,221,700	81,234
	114.6	8108	72,362	6,543,700	122,970
	Mean value	16,240	55,829	4,776,833	73,798
	38.2	23,810	19,168	1,530,400	17,731
17.85%	57.3	8750	23,478	2,003,300	22,565
	76.4	6293	24,956	2,598,800	27,251
	95.5	5212	27,216	3,687,100	30,471
	114.6	4583	32,970	3,701,700	38,354
	Mean value	9730	25,558	2,704,260	27,274
	38.2	18,192	14,482	823,410	13,901
20.35%	57.3	6186	19,001	1,228,400	20,719
	76.4	4567	17,786	1,616,000	19,692
	95.5	3752	17,398	2,013,500	19,494
	114.6	3232	19,499	2,577,100	28,702
	Mean value	7186	17,633	1,651,682	20,502
	38.2	13,574	11,111	649,260	8539
26.91%	57.3	4679	13,351	960,070	14,895
	76.4	3352	14,613	1,315,200	16,697
	95.5	2789	14,106	1,605,700	20,206
	114.6	2423	15,875	1,939,400	23,450
	Mean value	5363	13,811	1,293,926	16,757
	38.2	11,399	9705	493,800	7795
29.18%	57.3	3912	12,192	756,310	12,868
	76.4	2860	13,188	1,068,500	18,258
	95.5	2412	13,430	1,346,500	17,284
	114.6	2130	13,152	1,580,900	20,684
	Mean value	4543	12,314	1,049,202	15,378

# 4.2. Analysis of Creep Model Parameters

# (1) Effects of moisture content on creep model parameters

It can be seen from Table 3 that  $E_1/E_2/\eta_1/\eta_2$  decrease with any increase in moisture content when the load level is constant. For example, when the moisture content of the specimen increased from 15.8% to 29.18%, creep parameter  $E_1$  decreased by 69%,  $E_2$  decreased by 77%,  $\eta_1$  decreased by 81% and  $\eta_2$  decreased by 65%, correspondingly, under a load of 38.2 kPa. According to the research results of Yang et al. [20], elastic coefficient  $E_1$  is negatively correlated with instantaneous elastic deformation; elastic coefficient  $E_2$  is negatively correlated with initial creep; viscosity coefficient  $\eta_1$  is negatively correlated with the initial creep and the steady creep rate; and viscosity coefficient  $\eta_2$  is negatively correlated with the initial creep rate. Therefore, it can be seen that with an increase in moisture content, the instantaneous elastic deformation, initial creep, initial creep rate and steady creep rate would increase significantly, which is consistent with the conclusions of the creep test.

#### (2) Effects of load level on creep model parameters

It can be seen from Table 3 that with an increase in load value,  $E_1$  decreases while  $E_2/\eta_1/\eta_2$  increase. For instance, when the load value increased from 38.2 kPa to 114.6 kPa, creep parameter  $E_1$  decreased by 56%,  $E_2$  increased by 26%,  $\eta_1$  increased by 44% and  $\eta_2$  increased by 70%, with a constant moisture content of 15.8%. The changes of  $E_1$  and  $\eta_2$  were more significant, which means that with an increase in load level, instantaneous elastic strain increases while the initial creep rate decreases. The reason for this is that as

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the degree of compaction of the specimen increases under the action of the previous load, the friction force and the interlocking force between soil particles increases, which leads to a decrease in the initial creep deformation rate and prolongation of the initial creep stage. However, even though the increase in instantaneous elastic creep was greater than the decrease in initial creep deformation, the total creep deformation still showed an increasing trend, which is consistent with the creep test results.

#### 4.3. Establishment of the Creep Equations Considering the Moisture Content

The creep equation for fully weathered sandy shale with different moisture contents can be conducted as Equation (3):

$$\varepsilon = \begin{cases} \frac{\sigma}{16,240} + \frac{t}{4,776,833}\sigma + \frac{1 - e^{-\frac{55,829}{37,798}t}}{55,829}\sigma, & \omega = 15.80\% \\ \frac{\sigma}{9729} + \frac{t}{2,704,260}\sigma + \frac{1 - e^{-\frac{55,557}{25,557}}}{25,557}\sigma, & \omega = 17.85\% \\ \frac{\sigma}{7185} + \frac{t}{1,651,682}\sigma + \frac{1 - e^{-\frac{10,633}{25,501}t}}{17,633}\sigma, & \omega = 20.35\% \\ \frac{\sigma}{5363} + \frac{t}{1,293,926}\sigma + \frac{1 - e^{-\frac{10,791}{15,791}}}{12,791}\sigma, & \omega = 26.91\% \\ \frac{\sigma}{4542} + \frac{t}{1,049,202}\sigma + \frac{1 - e^{-\frac{13,093}{13,093}}}{13,093}\sigma, & \omega = 29.18\% \end{cases}$$

The relationship of the creep parameters (elastic coefficients  $E_1/E_2$  and viscosity coefficients  $\eta_1/\eta_2$ ) and the moisture content,  $\omega$ , of fully weathered sandy shale can be obtained with the fitting regression method, as shown in Equations (4)–(7).

$$E_1 = 5.385 \times 10^{11} \omega^{-6.399} + 4678 \tag{4}$$

$$E_2 = 3.404 \times 10^{16} \omega^{-9.932} + 13,390 \tag{5}$$

$$\eta_1 = 8.326 \times 10^{14} \omega^{-6.968} + 1.083 \times 10^6$$
 (6)

$$\eta_2 = 1.971 \times 10^{19} \omega^{-12.13} + 16,100$$
(7)

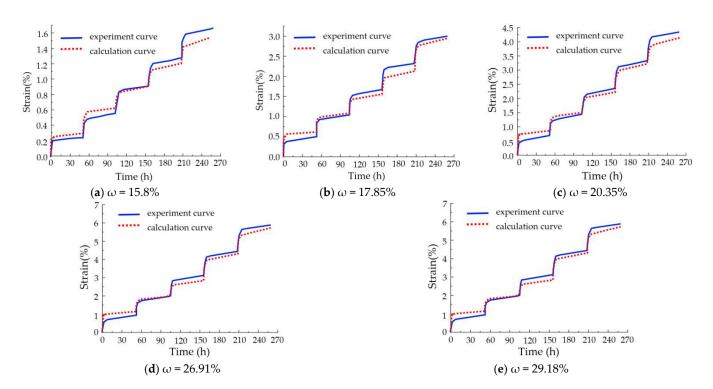
The correlation coefficient,  $R^2$ , of each fitting equation was greater than 0.99, indicating that the Burgers model fit well with the experimental data. Through means of substituting the above relationship into the Burgers creep equation, the creep equation considering the moisture content can be achieved, as shown in Equation (8). This equation can describe the creep behavior of fully weathered sandy shale with moisture content in the range of  $15.8 \sim 29.18\%$ .

$$\varepsilon = \frac{\sigma}{5.385 \times 10^{11} \omega^{-6.399} + 4678} + \frac{t}{8.326 \times 10^{14} \omega^{-6.968} + 1.083 \times 10^{6}} \sigma + \frac{1 - e^{-\frac{3.404 \times 10^{16} \omega^{-9.932} + 13.390}{1.971 \times 10^{19} \omega^{-12.13} + 16,100}}}{3.404 \times 10^{16} \omega^{-9.932} + 13,390} \sigma$$
(8)

In this equation,  $\varepsilon$  is the strain of fully weathered sandy shale,  $\sigma$  is the stress of fully weathered sandy shale (kPa),  $\omega$  is the moisture content of fully weathered sandy shale, t is creep time (h) and  $P_{\rm u}$  is the ultimate pressure of fully weathered sandy shale.

In order to verify the accuracy of the creep equation, the calculation results of Equation (8) were compared with the creep experimental data. Results are shown in Figure 9. It can be seen that the creep experiment curve is basically consistent with the obtained creep equation curve, proving that the creep equation can describe the creep behavior of fully weathered sandy shale.

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**Figure 9.** Experiment curve and calculation curve of specimens: (a)  $\omega = 15.8\%$ , (b)  $\omega = 17.85\%$ , (c)  $\omega = 20.35\%$ , (d)  $\omega = 26.91\%$  and (e)  $\omega = 29.18\%$ .

#### 4.4. Discussion of the Creep Equations Considering the Moisture Content

Based on the compressive and creep test results and the Burgers model, a creep constitutive equation of fully weathered sandy shale was obtained and is shown in Equation (8). It can be seen that creep strain is positively correlated with the first power of  $\sigma$  and positively correlated with the sixth or higher power of moisture content. This is a quantitative result of the influence of moisture content and load level, meaning that the greater the moisture content, the higher the load level, resulting in larger creep deformation, and moisture content has a more significant influence on creep behavior than does load level. In addition, it also can be seen that the second and the third expression in Equation (8) are related to loading time, t, of which the second term is the expression of the first power of t and the third term is the expression of the reciprocal of the exponential function of t. That is to say, when the moisture content and the load level are fixed values, the creep strain values show a nonlinear growth trend with an increase in time and the creep rate becomes slower and slower until the creep deformation reaches a certain degree and the rock arrives at a stable state.

In particular, since the creep test was carried out under the condition of moisture content of  $15.8\sim29.18\%$  and load levels of  $20\sim60\%$  of the ultimate compressive strength, the optimum-use condition of Equation (8) is when the moisture content is between 15.8 and 29.18% and the load level is no more than 60% of the ultimate compressive strength. When the load exceeds this limit, the soil is likely to enter the accelerated creep stage, which would affect the accuracy of calculation results. However, this equation still has an important guiding significance to the large-deformation disasters of a large amount of sandy-shale tunnel excavation projects. Using this equation, creep deformation during the construction and trial periods can be judged under measured water-content and stress conditions. In summary, this creep model is not only a modification to the Burgers model but also a powerful supplement to the theory of creep characteristics of sandy shale.

#### 5. Conclusions

(1) Fully weathered sandy shale is easy to disintegrate in water, and its strength is high in the dry state. With an increase in moisture content, the compressive strength of the

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- specimen decreases significantly. The compressive strength of the specimen with a moisture content of 29.18% was only 18% of the specimen in the dry state.
- (2) The creep characteristic curves of fully weathered sandy shale under the load of 20~60% of the ultimate strength had only two creep stages, the primary creep stage and the steady-state creep stage, with no accelerated creep stage. The creep deformation increased with time nonlinearly.
- (3) The creep behavior of fully weathered sandy shale is obviously affected by moisture content and load level. The greater the moisture content, the higher the load level, resulting in larger instantaneous elastic deformation, a larger steady creep rate and greater creep deformation. The duration of initial creep is longer as well. Moisture content has a more significant influence on creep behavior than does load level. In the later part of the steady-state creep stage, the creep rate of specimens with low moisture content was close to zero, the creep deformation no longer increased and the specimens entered a stable state. Therefore, it is quite beneficial to reduce moisture content in order to control creep deformation.
- (4) The elastic coefficients  $E_1/E_2$  and viscosity coefficients  $\eta_1/\eta_2$  are correlated with moisture content and load level.  $E_1/E_2/\eta_1/\eta_2$  decrease with an increase in moisture content;  $E_1$  decreases with an increase in load level while  $E_2/\eta_1/\eta_2$  increase with an increase in load level.
- (5) The creep model of fully weathered sandy shale, considering moisture content, fits well with the creep experiment. It is expected to provide a theoretical basis for the large deformation mechanism and disaster treatment of fully weathered sandy shale.

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