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# Validation of a novel numerical model to predict regionalized blood flow in the coronary arteries

Daniel J. Taylor <sup>1,\*</sup>, Jeroen Feher<sup>2</sup>, Krzysztof Czechowicz <sup>1</sup>, Ian Halliday<sup>1,3</sup>, D.R. Hose<sup>1,3</sup>, Rebecca Gosling <sup>1,3,4</sup>, Louise Aubiniere-Robb<sup>1</sup>, Marcel van't Veer<sup>5,6</sup>, Danielle C. J. Keulards<sup>5</sup>, Pim Tonino<sup>5,6</sup>, Michel Rochette<sup>2</sup>, Julian P Gunn<sup>1,3,4</sup>, and Paul D. Morris<sup>1,3,4</sup>

<sup>1</sup>Department of Infection, Immunity and Cardiovascular Science, University of Sheffield, Sheffield, UK; <sup>2</sup>ANSYS Research and Development, Lyon, France; <sup>3</sup>Insigneo Institute for In Silico Medicine, Sheffield, UK; <sup>4</sup>Department of Cardiology, Sheffield Teaching Hospitals NHS Foundation Trust, Sheffield, UK; <sup>5</sup>Department of Cardiology, Catharina Hospital, Eindhoven, Netherlands; and <sup>6</sup>Department of Biomechanical Engineering, Eindhoven University of Technology, Eindhoven, Netherlands

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## Aims

Ischaemic heart disease results from insufficient coronary blood flow. Direct measurement of absolute flow (mL/min) is feasible, but has not entered routine clinical practice in most catheterization laboratories. Interventional cardiologists, therefore, rely on surrogate markers of flow. Recently, we described a computational fluid dynamics (CFD) method for predicting flow that differentiates inlet, side branch, and outlet flows during angiography. In the current study, we evaluate a new method that regionalizes flow along the length of the artery.

## Methods and results

Three-dimensional coronary anatomy was reconstructed from angiograms from 20 patients with chronic coronary syndrome. All flows were computed using CFD by applying the pressure gradient to the reconstructed geometry. Side branch flow was modelled as a porous wall boundary. Side branch flow magnitude was based on morphometric scaling laws with two models: a homogeneous model with flow loss along the entire arterial length; and a regionalized model with flow proportional to local taper. Flow results were validated against invasive measurements of flow by continuous infusion thermodilution (Coroventis™, Abbott). Both methods quantified flow relative to the invasive measures: homogeneous ( $r$  0.47,  $P$  0.006; zero bias; 95% CI –168 to +168 mL/min); regionalized method ( $r$  0.43,  $P$  0.013; zero bias; 95% CI –175 to +175 mL/min).

## Conclusion

During angiography and pressure wire assessment, coronary flow can now be regionalized and differentiated at the inlet, outlet, and side branches. The effect of epicardial disease on agreement suggests the model may be best targeted at cases with a stenosis close to side branches.

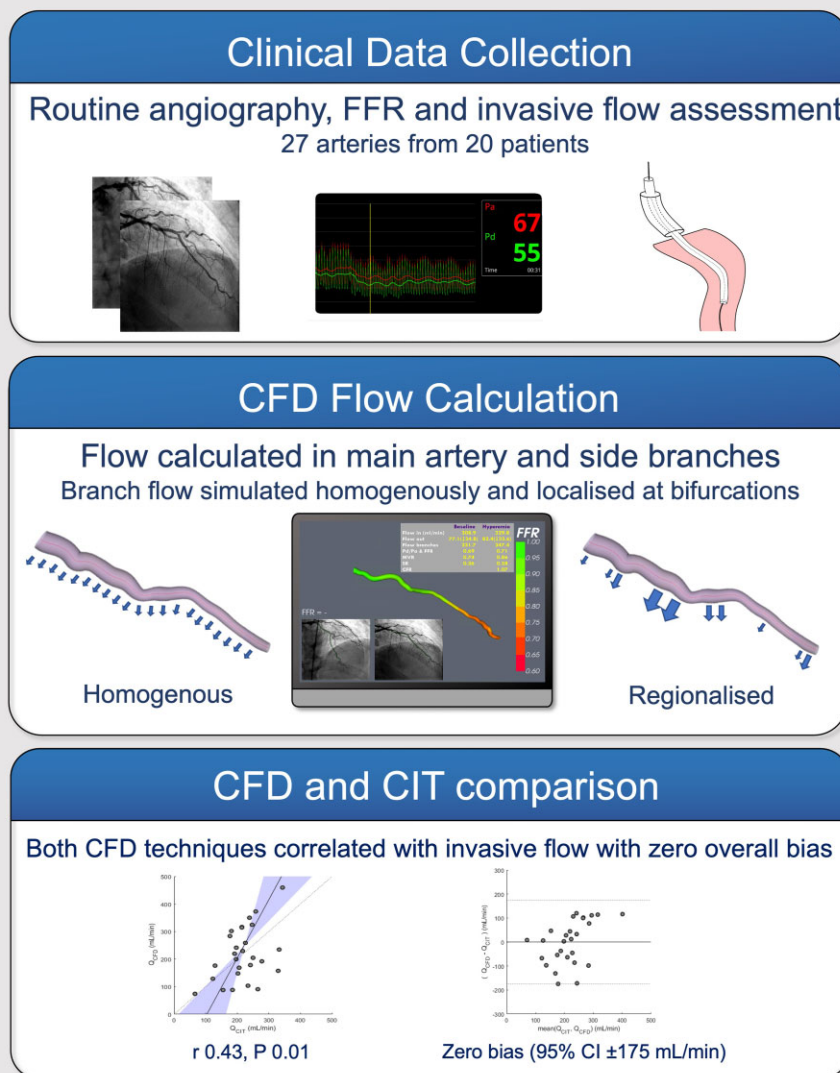
\* Corresponding author. Tel: +44 114 215 9500, Email: [daniel.taylor@sheffield.ac.uk](mailto:daniel.taylor@sheffield.ac.uk)

Work performed at The University of Sheffield.

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## Graphical Abstract



## Keywords

Coronary flow • Bifurcation • Computational Fluid Dynamics

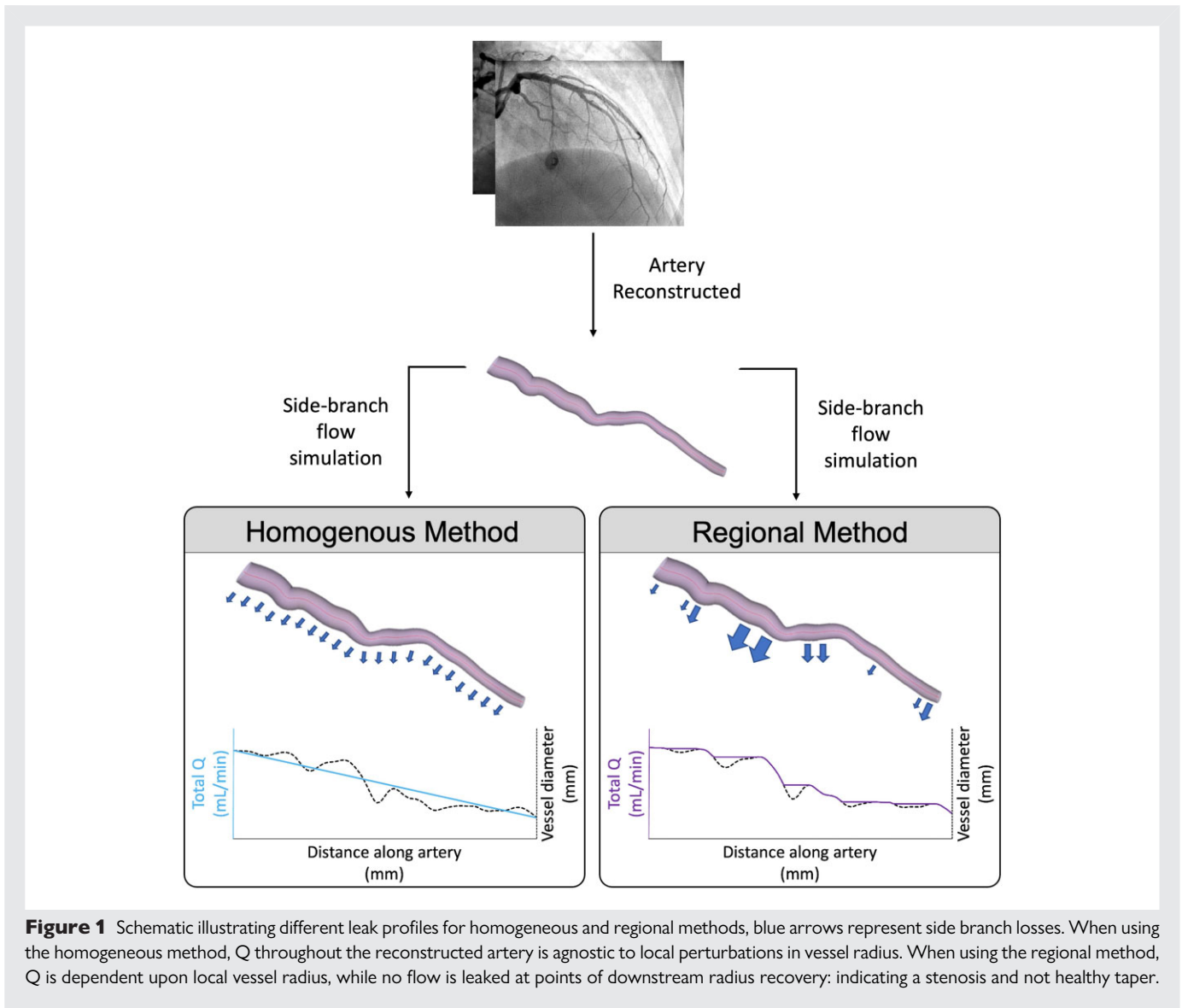
## Introduction

Ischaemic heart disease (IHD) is the leading cause of death worldwide. IHD results from an insufficiency of coronary blood flow ( $Q$ ), commonly caused by occlusive coronary arterial disease and encompasses a wide variety of clinical syndromes including symptomatic ischaemia (angina), myocardial infarction, and heart failure. Interventional treatments are effective in restoring  $Q$ , but should only be targeted at lesions that result in ischaemia. There is, however, no technique available for routine clinical use in the cardiac catheterization laboratory which directly measures  $Q$ . Over several decades, cardiologists have relied upon indirect surrogate markers, such as thermodilution-derived mean transit time, Doppler-derived flow velocity, and pressure-derived fractional flow reserve (FFR) and related indices<sup>1–3</sup> and, more recently, ‘virtual’ FFR (vFFR), computed from angiographic images.<sup>4</sup> All these methods

have strengths and weaknesses, but none measure ‘absolute’  $Q$  in mL/min. FFR is the ratio of distal to proximal translesional pressure measurements, but it only expresses *fractional* and not absolute reductions in  $Q$  and it cannot diagnose coronary microvascular disease (MVD); a common but often overlooked cause of IHD.<sup>5–10</sup>

Two methods have been developed to quantify  $Q$ . The first, continuous infusion thermodilution (CIT), is the most established and validated method and uses the Rayflow™ infusion catheter (Hexacath, Paris, Fr).<sup>11,12</sup> The second, virtuQ™, derives  $Q$  from a computational fluid dynamics (CFD) simulation based upon the 3D angiographic anatomy and pressure wire measurements, and is the subject of this study.<sup>13</sup> Both methods also quantify absolute microvascular resistance ( $R_{\text{micro}}$ ) and so provide a comprehensive evaluation of the entire coronary circulation. A limitation of the CFD method was that it only considered the main vessel and was agnostic to side branch flow.<sup>13</sup> While





**Figure 1** Schematic illustrating different leak profiles for homogeneous and regional methods, blue arrows represent side branch losses. When using the homogeneous method, Q throughout the reconstructed artery is agnostic to local perturbations in vessel radius. When using the regional method, Q is dependent upon local vessel radius, while no flow is leaked at points of downstream radius recovery; indicating a stenosis and not healthy taper.

included left anterior descending (LAD) arteries ( $n = 18$ ), left circumflex (Cx) arteries ( $n = 7$ ), and right coronary arteries (RCA) ( $n = 2$ ). The mean  $Q_{CIT}$  was  $219 (\pm 61)$  mL/min and the median  $R_{microCIT}$  was  $360 [290\text{--}450]$  mmHg min/L. The majority of included cases contained minimal epicardial disease, with a mean FFR of  $0.87 (\pm 0.08)$  and only three cases meeting a clinical threshold of FFR significance ( $\leq 0.80$ ). Median percentage stenosis assessed by operator, 2D QCA and 3D QCA was  $10\%$  [0–25%],  $16\%$  [0–31%], and  $15\%$  [0–33%], respectively (full details of cases shown in Table 1). No included cases contained diffuse epicardial disease. Using a threshold of  $460$  mmHg min/L,<sup>25–27</sup> five (25%) patients had clinically significant MVD as assessed by  $R_{microCIT}$ .

**The homogeneous porous wall boundary method**

The homogeneous porous wall boundary method disclosed a mean  $Q_{CFD}$  of  $219 (\pm 86)$  mL/min. There was a statistically significant correlation between  $Q_{CFD}$  and  $Q_{CIT}$  ( $r$  0.473,  $P$  0.006), Passing and Bablok

regression identified constant and proportional differences between techniques ( $c$  coefficient  $-202$ , 95% CI  $-633$  to  $-20$ ;  $m$  coefficient  $2.03$ , 95% CI  $1.15$  to  $4.07$ ), the mean delta between techniques was zero and the 95% Bland Altman limits of agreement were  $-168$  to  $+168$  mL/min (Figure 2). The proportional differences between  $Q_{CFD}$  and  $Q_{CIT}$  was characterized by an increase in bias for higher flow rates, which is visually displayed by Bland Altman analysis. A significant correlation between  $R_{microCFD}$  and  $R_{microCIT}$  was also observed ( $r$  0.647,  $P$  0.0001), constant and proportional differences were present ( $c$  coefficient  $-400$ , 95% CI  $-950$  to  $-90$ ;  $m$  coefficient  $2.07$ , 95% CI  $1.15$  to  $3.67$ ), the mean delta between techniques was  $+30$  mmHg min/L and the 95% Bland Altman limits of agreement were  $-210$  to  $+480$  mmHg min/L (Figure 3).

**The regional porous wall boundary method**

The regional porous wall boundary method disclosed a mean  $Q_{CFD}$  of  $219 (\pm 96)$  mL/min. The correlation between  $Q_{CFD}$  and  $Q_{CIT}$  was

**Table 1** Reconstructed vessel characteristics and flows

Case		FFR	Percentage stenosis			Q results (mL/min)		Rmicro results (mmHg min/L)	
Vessel	Number		Operator	2D	3D	Q <sub>CIT</sub>	Q <sub>CFD</sub>	Rmicro <sub>CIT</sub>	Rmicro <sub>CFD</sub>
LAD	01	0.87	10	16	11	343	459	250	184
	02	0.82	0	15	22	182	302	340	191
	03	0.69	10	29	34	192	219	320	276
	04	0.83	15	31	30	197	241	320	259
	05	0.83	15	9	8	215	316	310	196
	06	0.85	5	17	16	202	148	410	547
	07	0.84	5	19	11	177	283	280	164
	08	0.81	0	0	0	278	192	210	274
	09	0.86	20	16	15	217	229	350	330
	10	0.86	0	0	0	330	157	210	410
	11	0.97	0	0	0	234	103	360	761
	12	0.74	35	43	55	66	74	1140	992
	13	0.83	40	31	33	123	129	520	462
	14	0.95	25	18	37	185	88	460	969
	15	0.93	0	0	0	239	350	320	203
	16	0.81	10	10	11	226	258	390	329
	17	0.91	35	33	32	155	87	450	793
	18	0.93	20	32	39	206	169	400	482
LCx	19	0.98	0	0	0	333	234	290	402
	20	0.95	45	53	43	247	324	360	253
	21	0.88	50	39	33	215	314	600	392
	22	0.78	40	31	15	130	176	580	420
	23	0.93	15	9	12	259	373	270	176
	24	0.96	0	0	0	197	199	540	521
	25	0.96	0	0	0	265	91	250	716
RCA	26	0.96	5	12	19	242	178	400	538
	27	0.97	10	26	23	250	204	390	465

All reported CFD results acquired using the regional porous wall boundary method.

Q<sub>CIT</sub>, absolute coronary flow measured with Rayflow catheter after correction applied (mL/min); Rmicro<sub>CIT</sub>, microvascular resistance measured with Rayflow catheter after correction applied (mmHg min/L); QCA, quantitative coronary angiography; LAD, left anterior descending artery; LCx, circumflex artery; RCA, right coronary artery.

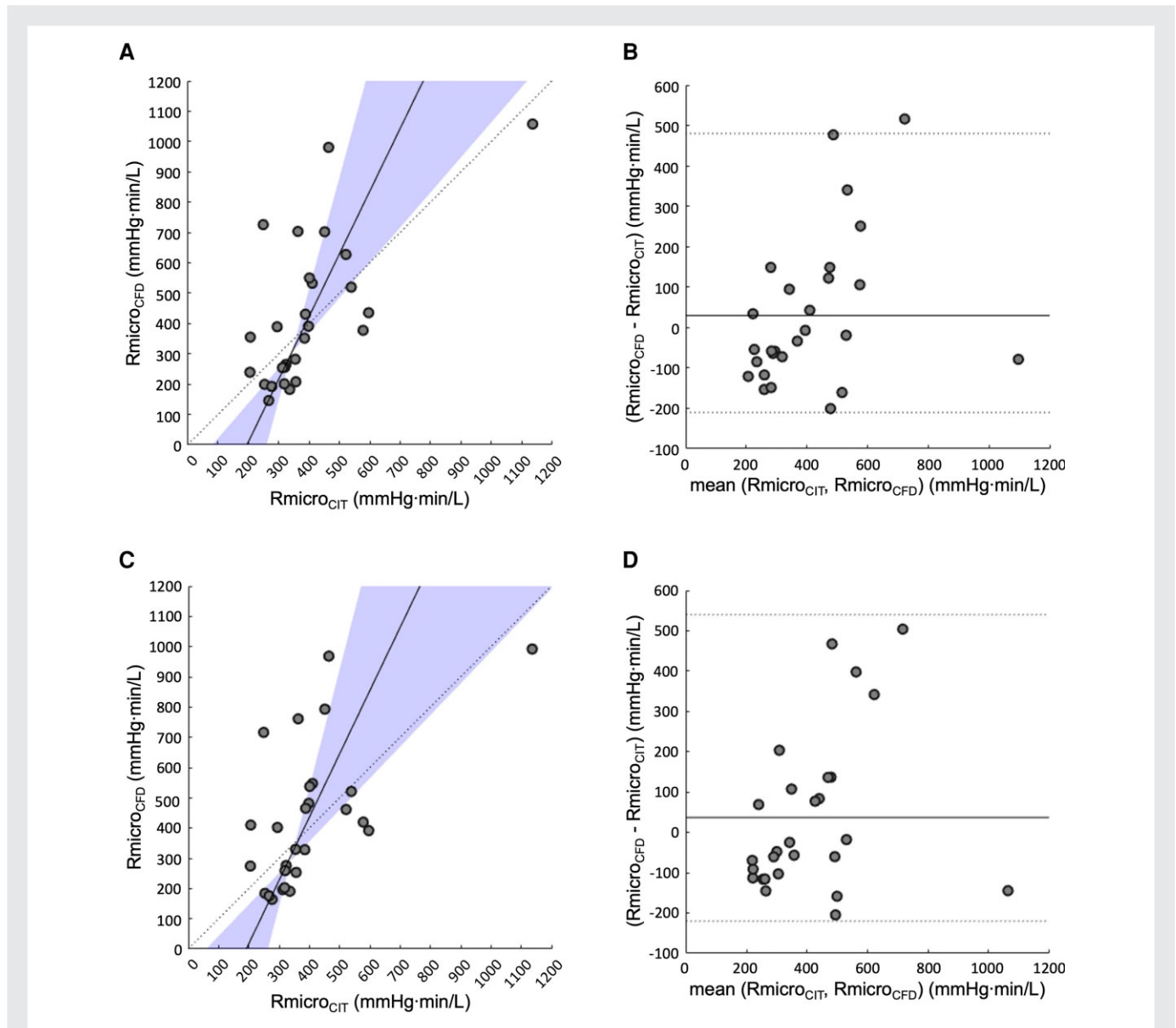
significant ( $r$  0.429,  $P$  0.0127), Passing and Bablok regression identified constant and proportional differences between techniques ( $c$  coefficient  $-220$ , 95% CI  $-687$  to  $-16$ ;  $m$  coefficient  $2.12$ , 95% CI  $1.18$  to  $4.19$ ), the mean delta between techniques was zero and the 95% Bland Altman limits of agreement were  $-175$  to  $+175$  mL/min (Figure 2). Agreement between Q<sub>CFD</sub> and Q<sub>CIT</sub> was not superior for either the homogeneous or regional techniques ( $t$  0.0023,  $P$  0.998). A significant correlation between Rmicro<sub>CFD</sub> and Rmicro<sub>CIT</sub> was also observed ( $r$  0.586,  $P$  0.0006), constant and proportional differences were present ( $c$  coefficient  $-400$ , 95% CI  $-1030$  to  $-60$ ;  $m$  coefficient  $2.09$ , 95% CI  $1.04$  to  $3.90$ ), the mean delta between techniques was  $+37$  mmHg min/L and the 95% Bland Altman limits of agreement were  $-220$  to  $+540$  mmHg min/L (Figure 3). Agreement between Rmicro<sub>CFD</sub> and Rmicro<sub>CIT</sub> was not superior for either the homogeneous or regional techniques ( $U$  363,  $P$  0.944) (full CFD results shown in Table 1). Using a threshold of 460 mmHg min/L, seven (35%) patients had clinically significant MVD as assessed by Rmicro<sub>CFD</sub>. Using Rmicro<sub>CIT</sub> as gold standard measurements, the sensitivity, specificity, positive predictive value, and negative predictive value of the CFD technique was 80%, 80%, 57%, and 92%, respectively.

## Determinants of agreement

Certain patient and vessel characteristics did appear to influence agreement between the CFD and invasive measurements. For homogeneous and regional porous wall boundary methods, respectively, Q agreement was significantly correlated with translesional pressure drop ( $P_a - P_d$ ) ( $r$  0.449,  $P$  0.0094;  $r$  0.391,  $P$  0.0217), FFR ( $r$   $-0.399$ ,  $P$  0.0196;  $r$   $-0.334$ ,  $P$  0.0441) and percentage stenosis assessed by 2D ( $r$  0.355,  $P$  0.0345;  $r$  0.472,  $P$  0.0065) and 3D QCA ( $r$  0.369,  $P$  0.0292;  $r$  0.489,  $P$  0.0048). This meant, for both homogeneous and regional techniques, that agreement between Q<sub>CFD</sub> and Q<sub>CIT</sub> improved in cases with greater disease burden assessed by pressure wire studies, 2D QCA and 3D QCA. For the regional method, Q agreement also correlated with visually assessed stenosis ( $r$  0.371,  $P$  0.0282).

For Rmicro, both homogeneous and regional techniques correlated with translesional pressure drop ( $r$  0.359,  $P$  0.0330;  $r$  0.340,  $P$  0.0415) and FFR ( $r$   $-0.368$ ,  $P$  0.0295;  $r$   $-0.364$ ,  $P$  0.0310), but no effect was seen for any assessment of stenosis (full results are shown in Table 2). This meant, for both homogeneous and regional techniques, that agreement between Rmicro<sub>CFD</sub> and Rmicro<sub>CIT</sub> improved in cases





**Figure 3** Correlation and agreement between  $R_{micro\_CFD}$  and  $R_{micro\_CIT}$ . (A) Passing and Bablok showing correlation between  $R_{micro\_CFD}$  and  $R_{micro\_CIT}$  for the homogeneous porous wall boundary method. (B) Bland Altman plot showing agreement between  $R_{micro\_CFD}$  and  $R_{micro\_CIT}$  for the homogeneous porous wall boundary method. (C) Passing and Bablok showing correlation between  $R_{micro\_CFD}$  and  $R_{micro\_CIT}$  for the regional porous wall boundary method. (D) Bland Altman plot showing agreement between  $R_{micro\_CFD}$  and  $R_{micro\_CIT}$  for the regional porous wall boundary method.

## Current indices for estimating flow

The superiority of translational pressure indices over standard angiography alone is well documented<sup>9,10</sup> and has led to the emergence of FFR as the current ‘gold standard’ evaluation of an epicardial lesion’s haemodynamic significance. However, this technique expresses *percentage* reduction in flow and does not quantify MVD. Combined use of FFR with other indices of coronary flow, such as coronary flow reserve (CFR) and index of microvascular resistance (IMR), allows for quantification of disease in both epicardial and microvascular compartments, but this requires additional time and hardware and is currently reserved for a relatively small number of patients. Additionally, the binary nature of treatment thresholds means different indices may conflict and all fail

to quantify a direct determinant of myocardial ischaemia – absolute Q. The CIT technique addresses these issues but requires a dedicated infusion catheter and accuracy may be decreased in arteries with multiple, large bifurcations. In contrast, virtuQ may quantify Q at the inlet, outlet, and side branches of reconstructed arteries, along with all of the above-mentioned indices of flow from standard angiography and pressure wire assessment.

## How this technique compares with others

The Rayflow CIT and virtuQ CFD methods quantify Q within the cardiac catheterization laboratory. Previously, one direct *in-vitro* validation of virtuQ outlet Q results has been performed, reporting a bias of



**Table 2 Correlations between  $Q_{CFD}$  and  $Q_{CIT}$  agreement and  $R_{micro_{CFD}}$  and  $R_{micro_{CIT}}$  agreement with various arterial reconstruction and demographic variables**

	Homogeneous method		Regional method	
	Pearson's <i>r</i>	<i>P</i>	Pearson's <i>r</i>	<i>P</i>
<b>Q</b>				
Percentage stenosis				
Visual assessment	0.237	0.117	0.371	0.0282
2D QCA	0.355	0.0345	0.471	0.0065
3D QCA	0.369	0.0292	0.489	0.0048
Pressure wire assessment				
$P_a - P_d$	0.449	0.0094	0.391	0.0217
FFR	-0.399	0.0196	-0.334	0.0441
Vessel taper				
Inlet diameter – outlet diameter	-0.313	0.0561	-0.194	0.166
<b>[Rmicro]</b>				
Percentage stenosis				
Visual assessment	-0.020	0.462	0.028	0.445
2D QCA	0.172	0.195	0.184	0.179
3D QCA	0.064	0.375	0.066	0.372
Pressure wire assessment				
$P_a - P_d$	0.359	0.0330	0.340	0.0415
FFR	-0.368	0.0295	-0.364	0.0310
Vessel taper				
Inlet diameter – outlet diameter	0.136	0.249	0.132	0.256

QCA, quantitative coronary angiography;  $P_a$ , proximal pressure under adenosine-induced hyperaemia (mmHg);  $P_d$ , distal pressure under adenosine-induced hyperaemia (mmHg).

+2.08 ± 3.45 mL/min<sup>13</sup> and our previous validation of inlet  $Q_{CFD}$  using the homogeneous porous wall boundary method reported zero bias between CIT results with 95% limits of agreement of ±168 mL/min.<sup>15</sup> More data are available for the latest, monorail Rayflow catheter design. An *in-vitro* trial of  $Q_{CIT}$  reported a bias of -6.5 ± 15.5 mL/min<sup>12</sup> and one animal study reported a bias of +5 ± 8 mL/min from Q measured in 12 pigs (mean Q 37 mL/min).<sup>28</sup> A direct validation study of the CIT method with [<sup>15</sup>O]H<sub>2</sub>O positron emission tomography (PET) in 25 patients referred for coronary angiography showed a bias between techniques of -0.9 ± 35 mL/min (95% limits of agreement -70 to +68 mL/min; mean Q across all included vessels 176 mL/min).<sup>29</sup>

In the present study, we reported moderate correlation between CIT and CFD Q for the regional porous wall boundary method. The 95% limits of agreement were ±175 mL/min. These limits of agreement are larger than reported in previous studies of different datasets,<sup>12,13,28,29</sup> even when accounting for the larger mean Q of patients included in the current study. Several factors may have negatively influenced agreement, the most important of which is likely to be characteristics of included arteries.  $Q_{CFD}$  accuracy is critically dependent upon agreement between simulated flow patterns and those occurring *in-vivo*. In healthy arteries, coronary flow is governed predominantly by Poiseuille (viscous) effects and as such, results are extremely sensitive to errors in reconstruction diameter. To put this into context, in a theoretical case taking the average outlet diameter and  $Q_{CFD}$  of cases

included in this study, an error in outlet reconstruction diameter of ± one single pixel would vary outlet  $Q_{CFD}$  from -42 to +62 mL/min (assuming Poiseuille's law with a constant pressure gradient across the artery). This error will be further magnified for inlet  $Q_{CFD}$ , when side branch flow is accounted for. Conversely, the complex flow patterns observed in diseased arteries reduce the dominance of Poiseuille effects on flow local to the disease, thereby reducing the sensitivity of  $Q_{CFD}$  to small errors in reconstruction diameter. This phenomenon is evidenced by both the correlations observed between  $Q_{CFD}$  and  $Q_{CIT}$  agreement with percentage luminal stenosis and translesional pressure gradients; both of which are markers of disease severity, and the clustering of cases without any appreciable epicardial disease at the higher error ranges. This means agreement between the two methods would likely have improved through inclusion of cases with moderate to severe epicardial disease.

Furthermore, the CIT method is dependent upon assumptions such as the complete mixing between saline infusate and blood prior to side branches and negligible heat loss to the vessel wall. These conditions may not be observed in patients, therefore resulting in inaccuracies of the CIT technique.<sup>12,28,29</sup> It is therefore important to consider the limits of agreement reported in this study as an amalgamation of the errors of both CFD and CIT methods and not solely attribute them to either technique.

The absence of any significant difference in *total* side branch flow between the homogeneous and regional porous wall boundary method was reassuring. The main advantage of the regionalized technique is that it seeks to concentrate side branch flow to the location of side branches. This may have advantages for more precise flow predictions when planning intervention just proximal or distal to significant bifurcation points. This, however, is more challenging to validate given that there are no methods that accurately predict coronary blood flow with this level of localization.

Intra-operator variability was excellent for both  $Q_{CFD}$  and  $R_{micro_{CFD}}$ . For both porous wall boundary methods, intra-observer variability was less than 5% for outlet  $Q_{CFD}$  and 4% for  $R_{micro_{CFD}}$ , which is considerably lower than previously reported results, of 10% and 11% for the same parameters, respectively.<sup>13</sup>

## Limitations

The number of included patients was modest and case exclusion rate was high, but this in keeping with similar retrospective computational studies and no exclusion criteria were applied on successfully modelled cases to improve accuracy. A disproportionate number of LAD arteries were included in this study. Moreover, our model of side branch flow relies on vessel taper, and the proximal RCA has less taper due to a relative lack of major side branches. For both these reasons, the model may lack generalisability for RCA modelling. Future studies will therefore aim to include more RCA's and include posterior descending and posterior left ventricular branches. Of the included arterial cases, only two (7%) met the criteria for moderate stenosis (>40%) as graded by either 2D or 3D QCA and three (11%) met the FFR threshold of haemodynamic significance (≤0.80). As previously described, this has negative implications for the accuracy of  $Q_{CFD}$  and provides the first clinical, supporting evidence of the previously reported requirement for a translesional pressure drop.<sup>13</sup> Because this was a retrospective analysis of angiograms captured at another centre, the protocols were not optimized for virtuQ processing<sup>4</sup> which may have affected reconstruction accuracy of included cases. Also, the correction calculation to accommodate for the partial coronary arterial lumen occlusion introduced by the *in-situ* Rayflow catheter is currently unvalidated. Clinically, the patient cohort for which absolute Q assessment will be of value and thresholds for intervention are currently unknown and subject to ongoing research.<sup>30</sup> Fournier et al. have previously reported a difference in hyperaemic LAD flow between healthy and

