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**The effects of GDL anisotropic transport properties on the PEFC performance**

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## 1 **Abstract**

2 **Purpose** – This paper aims to numerically investigate the impact of gas diffusion layer (GDL)  
3 anisotropic transport properties on the overall and local performance of polymer electrolyte  
4 fuel cells (PEFCs).

5 **Design/methodology/approach** – A three-dimensional numerical model of a polymer  
6 electrolyte fuel cell with a single straight channel has been developed to investigate the  
7 sensitivity of the fuel cell performance to the GDL anisotropic transport properties – gas  
8 permeability, diffusivity, thermal conductivity, and electrical conductivity. Realistic  
9 experimentally estimated GDL transport properties were incorporated into the developed PEFC  
10 model, and a parametric study was performed to show the effect of these properties on fuel cell  
11 performance and the distribution of the key variables of current density and oxygen  
12 concentration within the cathode GDL.

13 **Findings** – The results showed that the anisotropy of the GDL must be captured to avoid  
14 overestimation/underestimation of the performance of the modelled fuel cell. **The results also**  
15 **showed that the fuel cell performance and the distributions of current density and oxygen mass**  
16 **fraction within the cathode GDL are highly sensitive** to the through-plane electrical  
17 conductivity of the GDL and, to a lesser extent, the through-plane diffusivity, and the thermal  
18 conductivity of the GDL. The fuel cell performance is almost insensitive to the gas permeability  
19 of the GDL.

20 **Practical implications** – The current study improves the understanding of the importance of  
21 the GDL anisotropy in the modelling of fuel cells and provides useful insights on improving  
22 the efficiency of the fuel cells.

1 **Originality/value** – Realistic experimentally estimated GDL transport properties has been  
2 incorporated into the PEFC model for the first time, allowing for more accurate prediction of  
3 the PEFC performance.

## 4 **1. Introduction**

5 The gas diffusion layer (GDL) of the polymer electrolyte fuel cell (PEFC) is made up of solid  
6 (carbon, binder, and PTFE) and void phases. It is a crucially important component for the PEFC  
7 as it is responsible for the transport of gas reactants, heat and electrons between the flow-field  
8 plates and the catalyst layers, and provision of mechanical support to the delicate catalyst layers  
9 (Carcadea et al., 2007; El-Kharouf and Pollet, 2012). It is evident that limited transfer rate of  
10 gas reactants to the catalyst layers results in a decreased overall PEFC performance (Hassan et  
11 al., 2011; Ismail et al., 2016; Chen et al., 2020). On the other hand, high availability of reactant  
12 gases in the catalyst reaction sites does not only improves fuel cell performance but also  
13 reduces the amount of precious platinum catalyst required for the electrochemical reactions in  
14 the cell, thus making the PEFC more efficient and cost-effective (Gostick et al., 2006). To this  
15 end, the GDL should possess high mass transport properties (i.e., gas diffusivity and  
16 permeability) to quickly supply enough reactant gases to the catalyst layers and at the same  
17 time effectively remove excess water generated at the cathode catalyst layer. Equally the GDL  
18 should demonstrate high electrical conductivity to minimise ohmic losses and high thermal  
19 conductivity to dissipate/keep heat generated within the membrane electrode assembly (MEA)  
20 and subsequently prevent the dry-out of the membrane electrolyte or water flooding (Chen et  
21 al., 2020).

22 The conventional GDLs are made from carbon fibres which are preferentially oriented in the  
23 in-plane direction, thus resulting in anisotropic transport properties (Ismail et al., 2012). To this  
24 end, there have been several experimental and numerical studies on investigating the

1 anisotropic nature of the GDL and estimating its transport properties in different principal  
2 directions. Zamel et al. (2012) developed a 3-D reconstruction model of a carbon paper GDL  
3 to numerically estimate the effective electrical conductivity, at different values of porosity, for  
4 both through -plane and in-plane directions. They found the in-plane electrical conductivity to  
5 be higher than that in the through-plane direction by about 25% for high GDL porosity values  
6 between 0.7 to 0.9 and by about 44% for low porosity values between 0.4 to 0.6. They also  
7 proposed mathematical correlations to determine the effective electrical conductivity for the  
8 carbon fibre paper GDL and found the tortuosity factor to be 3.4 in the through-plane direction  
9 while for the in-plane it was reported to be 1.7. Zamel et al. (2010) numerically estimated the  
10 effective thermal conductivity of untreated carbon fibre paper GDL and found the thermal  
11 conductivity to be higher in the in-plane as compared to that of the through-plane by a factor  
12 of about 2. Veyret and Tsotridis (2010) developed a 3-D numerical model to estimate the  
13 effective thermal conductivity of the GDL. They reported that the anisotropic ratio for the GDL  
14 thermal conductivity (i.e., the ratio between the in-plane and the through- plane thermal  
15 conductivity) increases with increasing GDL porosity. Kramer et al. (2008) applied  
16 electrochemical impedance spectroscopy (EIS) to measure the effective diffusivity in the in-  
17 plane and through-plane directions as a function of the compression of the GDL paper and  
18 found that the in-plane effective diffusivity decreased from 0.6 to 0.2, at a porosity of 50%.  
19 While that of the through-plane direction decreased from 0.3 to 0.1. Fluckiger et al. (2008),  
20 using the electrochemical diffusimetry method initially developed by Kramer et al. (2008),  
21 measured the in-plane and through-plane diffusivities for three different carbon fibre paper  
22 materials. They investigated the effect of the binder structure and the Teflon treatment on the  
23 anisotropy and the effective diffusivity of the different GDL samples. They showed that an  
24 improved through-plane diffusivity is essential for high limiting current densities. Also, they  
25 reported that the ratio of the in-plane diffusivity to the through-plane diffusivity depends on

1 the orientation of the carbon fibres, the properties of the binders, the PTFE treatment as well  
2  
3 as the GDL compression. Ramousse et al. (2008) theoretically and experimentally estimated  
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5 the thermal conductivity of Quintech, and SGL carbon felts used as GDL in PEFCs. They  
6  
7 reported the effective thermal conductivity of the carbon felts to be an order of magnitude lower  
8  
9 than those of pure carbon papers measured in most literature. Ismail et al. (2010,2011)  
10  
11 experimentally measured the through-plane and in-plane gas permeability for multiple coated  
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13 and uncoated SGL GDLs. They found that the through-plane gas permeability of the coated  
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15 GDLs is one order of magnitude lower than the corresponding in-plane gas permeability. In  
16  
17 another work, Ismail et al. (2010) measured the in-plane and through-plane conductivity of  
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19 uncoated and coated SGL GDL samples and found that the in-plane conductivity (when  
20  
21 incorporating the contact resistance between the GDL and the bipolar plate) is two orders of  
22  
23 magnitude higher than the through-plane conductivity and this is mainly due to the preferential  
24  
25 alignment of the carbon fibres in the in-plane directions. Gostick et al. (2006) measured the gas  
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27 permeability in three principal directions for several carbon fibre GDL substrates including  
28  
29 SGL and Toray GDLs. They also measured the in-plane permeability of the GDL samples as a  
30  
31 function of compression. They reported that the GDL samples with the most highly aligned  
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33 fibres displayed the highest anisotropy, and their through-plane and in-plane permeability  
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35 values could differ by a factor of 2. Becker et al. (2009) combined both experimental and  
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37 numerical approaches to characterise the anisotropic transport properties of a Toray TGP-H-  
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39 060 carbon paper. They reported the in-plane diffusivity to be twice that of the through-plane.  
40  
41 They also found the in-plane permeability to be four times higher than the through-plane  
42  
43 permeability. Likewise, the in-plane electrical conductivity was found to be an order of  
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45 magnitude higher than that in the through-plane direction. Using periodic surface modelling,  
46  
47 Didari et al. (2014) numerically characterised the gas permeability and the relative diffusivity  
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49 for a Toray GDL. They reported the through-plane and the in-plane permeabilities to be  $6.8 \times$   
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1  $10^{-12}\text{m}^2$  and  $1.19 \times 10^{-11}\text{m}^2$ , respectively. While the through-plane and the in-plane relative  
2 diffusivities of the GDL was found to be 0.42 and 0.67, respectively. Gostick (2013) developed  
3 a 3D pore network model of the GDL to numerically characterise the diffusivity of Toray  
4 carbon GDL and found the through-plane diffusivity to be 0.21 while that of the in-plane  
5 direction was reported to be 0.45. James et al. (2012) used X-ray computed tomography of the  
6 GDL to numerically estimate transport properties of an SGL carbon substrate: 30BA. They  
7 showed that the effective electrical conductivity and diffusivity in the in-plane directions are  
8 four times larger than those in the through-plane direction. Nam and Kaviany (2003) developed  
9 a numerical model to estimate the effective diffusivity of carbon fibre GDL as a function of the  
10 porosity of the GDL and water saturation. They showed that the fibre alignment in the lateral  
11 direction, where there is no pore blockage, results in a higher in-plane effective diffusivity.  
12 Also, at low porosities (less than 0.45), the through-plane diffusivity was found to be larger  
13 than that in the in-plane direction.

14 Clearly not capturing the anisotropic nature of the GDL in the PEFC models would  
15 negatively impact the accuracy of the predictions of the PEFC models. The literature shows  
16 that there have been some attempts to investigate the impact of the anisotropic GDL on the  
17 performance of the modelled PEFCs. Pharaoh et al. (2006) investigated the effect of the  
18 anisotropic diffusivity and electrical conductivity on the performance of the modelled PEFC  
19 cathode. They showed that treating the electrodes as isotropic porous media yields significantly  
20 different current density predictions than anisotropic treatments. Using a 2-D single phase  
21 numerical PEFC, Bapat and Thynell (2008) investigated the effects of the anisotropic thermal  
22 conductivity and the thermal contact conductance on temperature distribution in the PEFC.  
23 They reported that though an increase in the in-plane thermal conductivity of the GDL resulted  
24 in smaller temperature gradients, the improvement in the heat transport is limited by the thermal  
25 contact resistance between the GDL and the bipolar plate. Pasaogullari et al. (2004) developed

1 a 2-D, non-isothermal, two-phase cathode side PEFC model to investigate the effect of the  
2 GDL anisotropy on the coupled heat and mass transfer within the cathode of the PEFC. They  
3 showed that the maximum temperature difference in the GDL is a strong function of the of the  
4 GDL anisotropy. Also, they reported that relatively high in-plane thermal conductivity values  
5 result in significantly different liquid water saturation distributions. Hyunchul (2009)  
6 developed a 3-D, two -phase PEFC model to study the effects of GDL anisotropic transport  
7 properties on the PEFC performance as well as on the heat and water transport in the cell. The  
8 author reported a significant variation of the PEFC temperature along the through-plane  
9 direction when the in-plane thermal conductivity is an order of magnitude higher than the  
10 through-plane thermal conductivity. Alhazmi et al. (2013) numerically investigated the effect  
11 of the GDL anisotropic thermal conductivity at three different PEFC operating temperatures,  
12 using a 3-D multiphase model of the PEFC. They reported a greater sensitivity of the  
13 temperature gradients within the PEFC to the in-plane thermal conductivity of the GDL as  
14 opposed to that of the through -plane direction. They also reported an increase in the power  
15 density of the PEFC when the in-plane and through-plane thermal conductivities are increased.  
16 Xing et al. (2015) studied the effect of GDL anisotropy on the transport of species, electric  
17 charge, heat, and liquid water in PEFCs operated at various loads, using a non-isothermal multi-  
18 phase flow numerical model of the PEFC. They reported that the anisotropic gas diffusivity  
19 does not influence the PEFC cell performance at low current densities, but it does at higher  
20 current densities. Their results showed negligible influence of the anisotropic gas permeability  
21 and thermal conductivity on the PEFC performance. *Yoshimune et al. (2022) experimentally  
22 measured the through-plane diffusivity for Toray carbon paper GDL, TGP-H-060, using  
23 infrared absorption carbon dioxide sensor. They found the through-plane diffusivity of the  
24 GDL sample to be  $0.36 \pm 0.02$  at a temperature of 25°C. Taş and Elden (2020) experimentally  
25 measured the through-plane and in-plane electrical conductivities of SGL34BA and SGL34BC*



1 gas diffusion layers. They investigated the effects of the PEFC operating temperature, the  
2 relative humidity, and the clamping pressure on the anisotropic electrical conductivities of the  
3 tested gas diffusion materials. They reported no significant change in the in-plane electrical  
4 conductivity, of both the SGL34BA and SGL34BC GDL samples, with increasing PEFC  
5 operating temperature and clamping pressure. However, there was a significant change in the  
6 in-plane electrical conductivity for the measured GDL samples under different relative  
7 humidities. Taş and Elden (2022) numerically developed a three-dimensional PEFC model in  
8 which they integrated their previously experimentally measured values of the anisotropic  
9 electrical conductivities for the above-mentioned gas diffusion layers. In their model, they  
10 investigated the effects of the PEFC operating temperature and the relative humidity on the  
11 anisotropic electrical conductivities of the GDL samples. They reported an increase in the  
12 output current densities in the in-plane direction with an increase in the temperature. For the  
13 through-plane directional component, they reported a maximum value of current density in the  
14 region of the GDL lying underneath the ribs of the bipolar plates. Zhang et al. (2017) developed  
15 a three-dimensional multiphase PEFC model to investigate the channel and gas diffusion layer  
16 flows in the PEM fuel cell. They investigated the effect of the GDL anisotropic effective  
17 electrical conductivity, gas diffusivity and permeability (but not the thermal conductivity) on  
18 the performance of the modelled PEFC. They reported the oxygen mass fraction distribution  
19 to be overpredicted for the case with isotropic GDL transport properties. Wang et al. (2022)  
20 developed a three-dimensional multiphase PEFC model with a through-plane and in-plane  
21 synergetic gradient porosity distribution in the cathode gas diffusion layer. They reported that  
22 a higher porosity within the region of the GDL lying close to the flow channel improves the  
23 transport of the gas reactants and the liquid water removal from the PEFC; this results in a  
24 uniform distribution of oxygen and current density within the cathode GDL. Yu et al. (2022)  
25 also developed a three-dimensional, non-isothermal and two-phase PEFC model incorporating

1 the difference in porosities of the region of the GDL under the rib and that under the gas flow  
2 channel. They investigated the effects of the GDL anisotropic transport properties on the  
3 current density distribution within the PEFC, temperature distribution, liquid water, and gas  
4 reactant concentrations. In addition, they reported that there is a lower current density  
5 distribution at the region of the GDL lying under the gas channel when the cell is operated at  
6 lower cell voltages. Ismail et al. (2012) developed a 3-D PEFC model of an in-house built  
7 PEFC to study the effects of the GDL anisotropic gas permeability and electrical conductivity  
8 on the performance of the PEFC. They found that the PEFC performance to be almost  
9 insensitive to the GDL anisotropic permeability and highly sensitive to the GDL anisotropic  
10 electrical conductivity. Li et al. (2017) developed a 3-D, two-phase, non-isothermal model of  
11 the PEFC in which they investigated the effects of GDL anisotropic gas permeability, gas  
12 diffusivity thermal conductivity and electrical conductivity on PEFC performance. They  
13 demonstrated that the temperature of the anisotropic case is more uniform and lower than that  
14 of the isotropic case owing to the relatively high in-plane thermal conductivity at high current  
15 densities. They also reported severe liquid water saturation in the isotropic GDL case model as  
16 compared to that of the anisotropic case.

17 Notably, in all the above studies, there have been no three-dimensional numerical PEFC models  
18 that incorporated the experimentally measured multidimensional values of each of the gas  
19 diffusivity, the gas permeability, the thermal conductivity, and the electrical conductivity of  
20 the GDLs. Therefore, to improve predictions, we have built a three-dimensional PEFC model  
21 which accounts for the anisotropic nature of the GDLs though employing experimentally  
22 measured values of the above key transport properties. After validating the model, we have  
23 performed a parametric study by realistically increasing/decreasing the base experimentally-  
24 estimated value of each of the above-mentioned transport properties. This is done to investigate  
25 the impact of not capturing the anisotropy for each of the above-mentioned transport properties

1 on the performance of the modelled PEM fuel cell and the distribution of the key variables of  
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1 on the performance of the modelled PEM fuel cell and the distribution of the key variables of  
2 current density and oxygen concentration, and subsequently obtain insights on how to improve  
3 the fuel cell efficiency.

## 4 **2. Model description and transport equations**

5 This section details the conservation equations that govern the transport of the physical  
6 quantities and their source terms as well as the electrochemical reactions which occur within  
7 the PEM fuel cell. The PEFC model developed in this study is based on the PEFC model of  
8 Berning et al. (2002).

### 9 **2.1. Model assumptions**

10 The following assumptions are made to simplify the PEFC model:

- 11 • Steady-state operation.
- 12 • Laminar and incompressible flow.
- 13 • Membrane is impermeable to the reactant gases.
- 14 • Uniform compression on all components of the fuel cell.
- 15 • Water exists in vapour phase only to isolate the impact of water saturation and solely  
16 focus on the impact of the GDL anisotropy.

### 17 **2.2. Model geometry**

18 The computational domain of the PEFC model consists of cathode and anode bipolar plates (or  
19 current collectors), cathode and anode flow channels, cathode and anode catalyst layers and the  
20 membrane electrolyte. The computational domain is, to save computational time, limited to a  
21 portion incorporating cathode and anode straight gas flow channels. Further, due to symmetry,

1 only half channel width is considered; see Figure 1. The geometrical, operational, and physical  
 2 parameters are presented in Table 1.

3 **[Figure 1]**

### 4 **2.3. Transport equations**

5 The following equations govern the transport of the physical quantities in all components of  
 6 the modelled PEFC (Gostick et al., 2006; Ismail et al., 2012; Bruggeman, 1935; Pharaoh et al,  
 7 2006; Alhazmi et al., 2013; Li et al., 2017; Zawodzinski et al., 1993):

#### 8 **Mass transport equation**

$$9 \quad \nabla \cdot (\varepsilon \rho \vec{u}) = 0 \quad (1)$$

10 where  $\rho$  is the gas mixture fluid density,  $\varepsilon$  is the porosity and  $\vec{u}$  is the fluid velocity vector.

#### 11 **Momentum transport equation**

$$12 \quad \nabla \cdot (\varepsilon \rho \vec{u} \vec{u}) = -\varepsilon \nabla P + \nabla \cdot (\mu \nabla \varepsilon \vec{u}) + \frac{\varepsilon^2 \mu \vec{u}}{K} \quad (2)$$

13 where  $P$  is the pressure of gas mixtures,  $\mu$  is the dynamic viscosity of the fluid and  $K$  is the  
 14 permeability of the porous medium.

#### 15 **Species transport equation**

$$16 \quad \nabla \cdot (\varepsilon \rho \vec{u} Y_k) = \nabla \cdot (\rho D_{kj}^{eff} \nabla Y_k) + S_k \quad (3)$$

17 where  $Y_k$  is the mass fraction of species  $k$  and  $D_{kj}^{eff}$  is the effective binary diffusivity of species  
 18  $j$  into  $k$ .  $D_{kj}^{eff}$  is calculated using the Bruggeman's correlation as follows (Bruggeman, 1935):

$$19 \quad D_{kj}^{eff} = \varepsilon^\tau D_{kj} \quad (4)$$

1 where  $\tau$  is the tortuosity of the porous medium and  $D_{jk}$  is bulk binary diffusivity of species  $k$   
 2 into  $j$ .  $S_k$  is the source term that represents either consumption/production of species  $k$  ( $H_2$ ,  $O_2$   
 3 or  $H_2O$ ) and is given as follows (Ismail et al., 2012):

$$4 \quad S_{H_2} = -\frac{i_a a_a}{2F} M_{H_2} \quad (5)$$

$$5 \quad S_{O_2} = -\frac{i_c a_c}{4F} M_{O_2} \quad (6)$$

$$6 \quad S_{H_2O} = \frac{i_c a_c}{2F} M_{H_2O} \quad (7)$$

7 where  $i_a$  and  $i_c$  are the anodic and cathodic local current density respectively,  $a_a$  and  $a_c$  are the  
 8 anodic and cathodic specific surface areas respectively,  $F$  is Faraday's constant (96485 C/mol)  
 9 and  $M_{H_2}$ ,  $M_{O_2}$  and  $M_{H_2O}$  are the molecular weights for hydrogen, oxygen and water,  
 10 respectively.

### 11 **Energy transport equation**

$$12 \quad \nabla \cdot (\rho c_p \vec{u} T) = \nabla \cdot (k_{eff} \nabla T) + S_e \quad (8)$$

13 where  $T$  is the temperature,  $c_p$  is the specific heat capacity of the gas mixtures,  $k_{eff}$  is the  
 14 effective thermal conductivity.  $S_e$  is the heat source term and takes one of the following forms  
 15 in each fuel cell component (Li et al., 2017):

$$16 \quad S_e = \begin{cases} i_s^2 / \sigma_s & \text{for anode and cathode GDLs} \\ R_a \left[ \eta_a - \frac{T \Delta S_a}{2F} \right] + \frac{i_s^2}{\sigma_s} + \frac{i_m^2}{\sigma_m} & \text{for anode catalyst layer} \\ R_c \left[ -\eta_c - \frac{T \Delta S_c}{2F} \right] + \frac{i_s^2}{\sigma_s} + \frac{i_m^2}{\sigma_m} & \text{for cathode catalyst layer} \end{cases} \quad (9)$$

17 where  $R_a$  and  $R_c$  are the anode and cathode exchange current densities,  $i_s$  and  $i_m$  are the solid  
 18 phase and membrane phase current densities,  $\sigma_s$  and  $\sigma_m$  are the electrical and ionic  
 19 conductivities of the solid and membrane phases respectively, and  $\eta_a$  and  $\eta_c$  are the anodic and

1 cathodic overpotential,  $\Delta S_a$  and  $\Delta S_c$  are the reaction entropies at anode and cathode catalyst  
 2 layers respectively.

### 3 Charge transport equations

4 Two potential equations for the electronic and ionic conduction are solved. The equations are  
 5 expressed as follows:

$$6 \nabla \cdot (\sigma_s \nabla \phi_s) = S_{\phi,s} \quad (10)$$

$$7 \nabla \cdot (\sigma_m \nabla \phi_m) = S_{\phi,m} \quad (11)$$

8 where  $\phi_s$  and  $\phi_m$  are the electrical (solid phase) and ionic (membrane phase) potentials  
 9 respectively.  $S_{\phi,s}$  and  $S_{\phi,m}$  are the solid-phase potential and membrane-phase potential  
 10 respectively and are given as follows (Alhazmi et al., 2013):

$$11 S_{\phi,s} = \begin{cases} j_a \text{ at the anode CL} \\ -j_c \text{ at the cathode CL} \end{cases} \quad (12)$$

$$12 S_{\phi,m} = \begin{cases} -j_a \text{ at the anode CL} \\ j_c \text{ at the cathode CL} \end{cases} \quad (13)$$

13 where  $j_a$  and  $j_c$  are the volumetric exchange current density ( $\text{A/m}^3$ ) at the anode and cathode  
 14 catalyst layers respectively and are obtained using Butler-Volmer equations (Zawodzinski et  
 15 al., 1993):

$$16 j_a = i_a^{ref} a_a \left( \frac{c_{H_2}}{c_{H_2}^{ref}} \right)^{0.5} \left[ \exp\left( \frac{\alpha_{a,a} F}{RT} \eta_{act,a} \right) - \exp\left( \frac{\alpha_{a,c} F}{RT} \eta_{act,a} \right) \right] \quad (14)$$

$$17 j_c = i_c^{ref} a_c \left( \frac{c_{O_2}}{c_{O_2}^{ref}} \right) \left[ \exp\left( \frac{\alpha_{c,a} F}{RT} \eta_{act,c} \right) - \exp\left( \frac{\alpha_{c,c} F}{RT} \eta_{act,c} \right) \right] \quad (15)$$

18 where  $i_a^{ref}$  and  $i_c^{ref}$  are the reference anodic and cathodic exchange current density respectively,  
 19  $\alpha_{a,a}$  and  $\alpha_{a,c}$  are respectively the anode and cathode transfer coefficients for the electrochemical

1 reactions in the anode catalyst layer,  $\alpha_{c,a}$  and  $\alpha_{c,c}$  are respectively the anode and cathode  
 2 transfer coefficients in the cathode catalyst layer,  $c_{H_2}^{ref}$  and  $c_{O_2}^{ref}$  are the reference hydrogen and  
 3 oxygen concentrations respectively,  $F$  is the Faraday's constant and  $R$  is the universal gas  
 4 constant.  $\eta_{act,a}$  and  $\eta_{act,c}$  are the anodic and cathodic overpotential and are given as follows:

$$5 \quad \eta_{act,a} = \phi_s - \phi_m \quad (16)$$

$$6 \quad \eta_{act,c} = \phi_s - \phi_m - E_0 \quad (17)$$

7 where  $E_0$  is the reference potential of the electrodes and is equal to zero for the anode, while  
 8 for the cathode it is equal to the equilibrium cell potential ( $E_r$ ) (Gostick et al., 2006; Pharaoh  
 9 et al., 2006):

$$10 \quad E_r = 1.482 - 0.000845T + 0.0000431T \ln(P_{H_2} P_{O_2}^{0.5}) \quad (18)$$

11 The membrane ionic conductivity,  $\sigma_m$ , is estimated using an empirical correlation developed  
 12 by Springer et al. (1991):

$$13 \quad \phi_m = (0.005139\lambda - 0.00326) \exp\left[1268\left(\frac{1}{303} - \frac{1}{T}\right)\right] \quad (19)$$

14 where  $\lambda$  is the membrane water content which is empirically correlated by Zawodzinski et  
 15 al.(1993):

$$16 \quad \lambda = \begin{cases} 1.409 + 11.26ac - 18.77ac^2 + 16.21ac^3, & 0 < ac \leq 1 \\ 10.11 + 2.944(ac - 1), & 1 < ac \leq 3 \\ 16.8, & ac > 3 \end{cases} \quad (20)$$

17 where  $ac$  is the water activity and is given as (Ismail et al., 2012):

$$18 \quad ac = \frac{P_v}{P_s} \quad (21)$$

19 where  $P_v$  is the partial pressure of water vapour and  $P_s$  is the pressure of saturated water vapor  
 20 which is given by (Ismail et al., 2012):

$$\log(P_s) = -2.1794 + 0.02953(T - 273.15) - 9.1837 \times 10^{-5}(T - 273.15)^2 + 1.4454 \times 10^{-7}(T - 273.15)^3 \quad (22)$$

#### 2.4. Boundary conditions and numerical procedure

Velocity inlet boundary conditions are specified for the anode and cathode gas flow channels. The operating temperature (353K) and the species mass fractions are specified at the flow channel inlets. The fluid inlet velocity is defined as a function of a typical operating current density ( $i_{op}$ ) which is in this case 500 mA/cm<sup>2</sup>, the active area of the fuel cell ( $A_{act}$ ), the channel cross-sectional area ( $A_{ch}$ ), and the stoichiometric ratio ( $\xi$ ) of the reactant gas which was set as 2 for both hydrogen and oxygen gases. Therefore, the anodic and the cathodic inlet velocities are given as follows (Berning et al., 2002):

$$u_a = \xi \frac{i_{op}}{2F} A_{act} \frac{1}{X_{H_2} P_c A_{ch}} \frac{RT}{P_c} \quad (23)$$

$$u_c = \xi \frac{i_{op}}{4F} A_{act} \frac{1}{X_{O_2} P_c A_{ch}} \frac{RT}{P_c} \quad (24)$$

Zero-flux boundary conditions are specified for all wall boundaries, except for the anode and cathode terminals (i.e., the top surfaces of the current collectors). The pressure outlet boundary conditions are specified at the outlet of the gas flow channels. Potentiostatic boundary conditions are specified for the anode and cathode current collector terminals of the cell, respectively, with the electrical potential for the anode set to zero (ground voltage) and that of the cathode set to the cell operating voltage ( $V_{cell}$ ). A constant operating temperature of 353K is set for both the anode and cathode terminals. The equations governing the transport of mass, heat, and charge in the PEFC model and the coupled boundary conditions were solved iteratively, using the commercial software ANSYS FLUENT. The Semi-implicit Method for Pressure Linked Equations (SIMPLE) algorithm is employed for the pressure-velocity coupling with the second-order upwind discretization scheme for the conservation of



1 momentum, species, energy, and charge equations. The model was found to give mesh-  
2 independent solution with a mesh of about 1.4 million cells; doubling this number result in a  
3 variation of less than 0.3% in the key performance indicator which is, in this case, the average  
4 current density at 0.55 V. The distribution of the mesh is shown in Figure 2.

5 **[Figure 2 and Table 1]**

### 6 **3. Results and discussion**

7 The modelled PEFC was simulated for different cell voltages and the polarisation curve was  
8 then generated. Figure 3 shows that the modelling data results are in good agreement with the  
9 experimental data extracted from Ticianelli et al. (1998). However, the model slightly under-  
10 predicts the performance of the fuel cell at lower cell voltages. This is most likely to be due to  
11 the fact that the physics of the liquid water (which at higher current densities increases the  
12 water content of the membrane electrolyte phase to be of the order of 20s rather than 10s and  
13 subsequently improves the ionic conductivity (Duan et al., 2012)) has not been captured in this  
14 single-phase model.

15 **[Figure 3]**

#### 16 **3.1. Anisotropic GDL versus isotropic GDLs**

17 Experimentally measured and realistic GDL anisotropic transport properties (gas permeability,  
18 gas diffusivity, thermal conductivity, and electrical conductivity) of the PEFC obtained from  
19 the literature, as shown in Table 2, are inputted into the PEFC model. We strived to ensure that  
20 for all the experimentally estimated transport properties to be of the same GDL material (i.e.,  
21 SGL 10BA) (Ismail et al., 2012; Alhazmi et al., 2013). However, for the gas diffusibility  
22 values, we used those of Kramer et al. (2008) and this was due to the unavailability of the  
23 corresponding values for SGL 10BA; nonetheless, this should not affect the general trends  
24 presented and the overall conclusions. The polarisation curve of the modelled PEFC with the

1 anisotropic GDL transport properties as well as the local distribution of key variables (the  
2 current density and oxygen mass fraction) within its cathode GDL are compared with those for  
3 the modelled PEFC model having isotropic GDL transport properties; see Figure 4. The  
4 isotropic transport properties are assumed to be the same as those of the through-plane direction  
5 for Case 2 and the same as those for the in-plane direction for Case 3; see Table 2.

6 **[Table 2]**

7 Figure 4a shows that the model over-predicts the fuel cell performance if the GDL transport  
8 properties are assumed to be isotropic and having the same values as those of the in-plane  
9 direction; for example, at 0.4 V, the current density is over-predicted by about 38%. On the  
10 other hand, the model under-predicts the fuel cell performance if the GDL transport properties  
11 are assumed to be isotropic and having the same values as those of the through-plane direction.  
12 However, the model is less sensitive the “isotropic through-plane” assumption (Case 2)  
13 compared to the “isotropic in-plane” assumption (Case 3). Namely, at 0.4 V, the current density  
14 is under-predicted by about 25% when switching from Case 1 to Case 2. Figure 4b compares  
15 the current density distribution at 0.55 V within the cathode GDL, halfway along the length of  
16 the channel of the PEFC, for both isotropic (through-plane and in-plane) and anisotropic cases.  
17 The local current density distribution in all cases have similar trends. For all three cases, the  
18 local current density is minimum at the section of the GDL which lies under the midpoint of  
19 the channel and increases steadily towards the interface between the collector rib and the gas  
20 channel where it peaks and then drops at the region beneath the current collector rib (this is  
21 more evident for Cases 1 and 3). This is attributed to the fact that the interface between the  
22 flow channel and the current collector is where the supply of oxygen and the transport of  
23 electrons are both optimised (the transport of oxygen to the catalyst layer is a minimum beneath  
24 the mid-point of the rib and the transport of **electrons** is a minimum beneath the mid-point of

1 the flow channel). The local current density is significantly higher in Case 3 compared to Cases  
2 1 and 2 and this evidently is due to the significantly higher in plane electrical conductivity  
3 which is assumed to be having the same value as the experimentally estimated in-plane  
4 conductivity shown in Table 2 (i.e., 4000 S/m). Case 2 shows that the current density saturates  
5 beneath the rib of the current collector, and this is due to lack of high in-plane conduction; this  
6 should be compared with Case 1 where the high in-plane conduction (4000 S/m) is responsible  
7 for “spreading” the current density more uniformly within the GDL. As expected, Fig. 4c shows  
8 that, for all cases, the concentration of oxygen (in the form of oxygen mass fraction) is  
9 maximum under the midpoint of the flow channel and minimum under the mid-point of the rib  
10 of the current collector. Note that Case 3 demonstrates lower oxygen concentration within the  
11 GDL, and this is due to the consumption of higher amount of oxygen at the cathode catalysts  
12 layer compared to Cases 1 and 2; this is induced by the higher overall electrical conduction of  
13 Case 3.

14 **[Figure 4]**

### 15 **3.2. Parametric study**

16 As this study is aimed at investigating the sensitivity of the PEFC performance to the  
17 anisotropic key transport properties of the GDL (the gas permeability, mass diffusivity, thermal  
18 conductivity, and electrical conductivity), a parametric study of the individual transport  
19 properties of the GDL was examined.

#### 20 **3.2.1. Anisotropic gas permeability**

21 Table 3 shows the 5 computational cases considered to investigate the impact of the gas  
22 permeability. Case 1 is the case in which the experimentally estimated gas permeability in  
23 through-plane and in-plane directions were fed into the model. In Cases 2 and 3, the  
24 experimentally measured through-plane gas permeability is kept constant and the

1 experimentally measured in-plane gas permeability is decreased and increased by an order of  
2 magnitude respectively. Likewise, in Cases 4 and 5, the experimentally measured in-plane gas  
3 permeability is kept constant and the experimentally measured through-plane gas permeability  
4 is decreased and increased by an order of magnitude. The results of the **simulated** cases are  
5 represented in Figure 5. Figure 5a shows that the linear profiles of the current density within  
6 the cathode GDL almost overlap each other; the same can be observed about the profiles of the  
7 oxygen concentration within the cathode GDL at 0.55 V. Further, the average current density  
8 at 0.55 V for all the cases shows a very minimal variation between the cases (the variation lies  
9 in the fourth decimal place). This signifies the very minimal impact of the GDL gas  
10 permeability on the performance of the fuel cell. As mentioned in prior works of Ismail et al.  
11 (2012); Zamel et al. (2012) observed that the main mode of transport within the GDL is  
12 diffusion, not convection.

13 **[Table 3 and Figure 5]**

### 14 **3.2.2. Anisotropic effective diffusivity**

15 The effective diffusivity within the GDL is often estimated using Bruggeman's correlation  
16 which is  $\varepsilon^{\tau}$  in Equation (4). The ratio between the effective diffusivity and the bulk diffusivity  
17 (which is Bruggeman's correlation in our case) is called the diffusibility. As with gas  
18 permeability, the experimentally estimated diffusibility in Case 1 has been realistically  
19 decreased and increased in through-plane and in-plane directions; see Table 4. This table shows  
20 that the average current density at 0.55 V changes very slightly with the changes in the in-plane  
21 diffusibility (compare Cases 1, 2 and 3). However, the average current density becomes more  
22 sensitive to changes in the through-plane diffusibility (compare Cases 1, 4 and 5); for example,  
23 the current density, for a given in-plane diffusibility of 0.5, increases by around 5% when the  
24 through-plane diffusibility increases from 0.1 to 0.5. Figure 6 shows the current density, and

1 the oxygen concentration profiles within the cathode GDL. As with the average current density,  
2 Figure 6a shows that, compared to the base case (Case 1), the local current density is more  
3 sensitive to the through-plane diffusibility (Cases 4 and 5) than the in-plane diffusibility (Cases  
4 2 and 3). This is since the through-plane direction is the direction through which the reactant  
5 gas (oxygen in this case) transport from the flow channel to the catalyst layer where it is  
6 consumed, thus completing the reaction, and generating the electrical current. For example, the  
7 mean local current density (averaged over the distance considered within the cathode GDL)  
8 increases by around 11% when the GDL diffusibility increases from 0.1 to 0.5.

9 Figure 6b shows that the oxygen mass fraction within the cathode under the flow channel is the  
10 lowest for Case 5 where the through-plane diffusibility is the largest, signifying higher amount  
11 of oxygen is consumed compared to other cases; this in line with the current density profiles  
12 shown in Figure 6a which demonstrates that the current density is in general the highest for  
13 Case 5. On the other hand, the oxygen concentration under the rib is the lowest for Case 2. This  
14 is because the in-plane diffusibility is the lowest for this case and as such the transport of  
15 oxygen from the regions below the flow channel to the regions below the rib is most hindered  
16 compared to other cases. On a related note, Cases 1, 2 and 3 do not show any remarkable  
17 difference in the distribution of oxygen in the region of the GDL below the channel. This shows  
18 that the in-plane diffusibility has no major impact on the oxygen distribution within this region.  
19 The in-plane diffusibility begins to dominate the distribution of oxygen as we approach the  
20 interface between the channel and the collector rib.

21 **[Table 4 and Figure 6]**

### 22 **3.2.3. Anisotropic thermal conductivity**

23 As with the GDL gas permeability and diffusibility, Table 5 shows five cases in which Case 1  
24 is the case with the experimentally estimated values for the through- and in-plane thermal

1 conductivity and the other 4 cases are the cases where the through-plane and the in-plane  
2 thermal conductivity values are realistically changed to investigate the sensitivity the fuel cell  
3 performance to the anisotropic GDL thermal conductivity. Overall, the impact of the GDL  
4 thermal conductivity on the fuel cell performance is, compared to electrical conductivity or  
5 even gas diffusivity, rather small; the difference in the average current density at 0.55 V  
6 between the best case (Case 4) and the worst case (Case 5) is just about 13.4 mA/cm<sup>2</sup>. The  
7 reason that Case 4 shows the best performance is that the significantly reduced through-plane  
8 thermal conductivity (i.e., 0.01 W/m□K) decreases heat dissipation rate, increases cell  
9 temperature, and subsequently increases the rate of reaction (as evidenced from the Butler-  
10 Volmer equation shown in Equations (14) and (15) and the membrane conductivity (as  
11 evidenced from the Springer's model shown in Equation (19)). In general, any decrease in either  
12 the in-plane thermal conductivity (compare Cases 1, 2 and 3) or the through-plane conductivity  
13 (compare Cases 1, 4 and 5) results in a slight improvement to the fuel performance. The  
14 distribution of current density within the cathode GDL (Figure 7a) are in line with the average  
15 current density results shown in Table 6; marginal gain are obtained with decreasing either the  
16 in-plane or the through-plane GDL thermal conductivities. Evidently, better cell performance  
17 means higher oxygen consumption rate and subsequently less oxygen concentration within the  
18 GDL and that is why Case 4 demonstrates the least oxygen mass fraction within the cathode  
19 GDL (Figure 7b).

20 [Table 5 and Figure 7]

#### 21 3.2.4. Anisotropic electrical conductivity

22 Table 6 shows 5 computation cases where the first case (Case 1) is the case with the  
23 experimentally estimated values for the through- and in-plane electrical conductivity and the  
24 other 4 cases are the cases where the through-plane and the in-plane electrical conductivity  
25 values are realistically changed to investigate the sensitivity the fuel cell performance to the

1 anisotropic GDL electrical conductivity. Further, Figure 8 displays the distribution of current  
2 density and oxygen concentration within the cathode GDL at 0.55 V. The first observation that  
3 could be extracted from Table 6 and Figure 8 is that the fuel cell performance and the  
4 distributions of current density and oxygen concentration are much more sensitive to the GDL  
5 electrical conductivity than the other transport properties. The reason behind this is that the  
6 electrical conductivity is associated with the ohmic losses which are the main potential losses  
7 for typically operating cell voltages (0.5 - 0.6 V). The second observation is that the fuel cell  
8 performance is significantly more sensitive to the through-plane electrical conductivity  
9 (compare Cases 1, 4 and 5) than to the in-plane electrical conductivity (compare Cases 1, 2 and  
10 3). To illustrate, the average current density at 0.55 V increases by more than 50% when  
11 increasing the through-plane GDL conductivity from 24 S/m (Case 4) to 96 S/m (Case 5). On  
12 the other hand, the average current density increases by less than 5% when increasing the in-  
13 plane GDL electrical conductivity from 2000 S/m (Case 2) to 8000 S/m (Case 3). This is mainly  
14 since the shortest (and the least resistive) pathway for the electrons to reach the catalyst layers  
15 (where they combine with oxygen and protons to produce water) is across the thickness of the  
16 GDL, not along the plane of the GDL.

17 Figure 8a shows that, for a given through-plane electrical conductivity, as the in-plane electrical  
18 conductivity increases (Cases 1, 2 and 3), the linear distribution of current density within the  
19 GDL expectedly becomes more uniform due to decreased in-plane electrical resistance.  
20 Further, in accordance with the average current density results at 0.5 V, it is evident that local  
21 current density is much more sensitive to the through-plane electrical conductivity (compare  
22 Cases 1, 4 and 5) than to the in-plane electrical conductivity (compare Cases 1, 2 and 3). This  
23 observation is also applicable to the distribution of oxygen distribution; the largest gap is  
24 between Case 4 and Case 5 where the through-plane electrical conductivity are 24 and 48 S/m

1 respectively. As expected, the lowest oxygen concentration within the GDL is demonstrated  
2 by Case 5 where the oxygen consumption rate is the maximum for this case.

3 [Table 6 and Figure 8]

## 4 5. Conclusions

5 A three-dimensional straight channel PEFC model has been developed. The main purpose of  
6 this study is to investigate the sensitivity of the fuel cell performance and the distributions of  
7 the key variables within the GDL (current density and oxygen concentration) to the anisotropy  
8 in the key transport properties of the GDL: **gas permeability, gas diffusivity, thermal  
9 conductivity, and electrical conductivity**. The key findings and observations are as follows:

- 10 • The anisotropic nature of the conventionally used GDLs need to be captured in the  
11 PEFC models. Overlooking this GDL's attribute leads to either significant  
12 overestimation (if the in-plane values of the transport properties are considered) or  
13 underestimation (if the through-plane values of the transport properties are considered)  
14 of the modelled fuel cell current density by up to 50% at typical cell voltages.
- 15 • The fuel cell performance and the distribution of current density and oxygen  
16 concentration within the GDL are, compared to other transport properties, highly  
17 sensitive to the electrical conductivity of the GDL, particularly in the through-plane  
18 direction. Quadrupling the through-plane GDL electrical conductivity increases the  
19 average current density of the fuel cell at 0.55 V by more than 50%.
- 20 • On the other hand, the fuel cell performance, and the distributions of the above key  
21 variables within the GDL are almost insensitive to the through-plane or in-plane gas  
22 permeability of the GDL as the main mode of transport within the GDL is diffusion.



- 1 • The fuel cell performance is moderately sensitive to both the gas diffusivity  
 2 (represented by the diffusibility in this study) and, to a lesser extent, the thermal  
 3 conductivity of the GDL. This observation is more evident with the through-plane  
 4 diffusibility and the thermal conductivity than with in-plane diffusibility or the thermal  
 5 conductivity of the GDL. This is mainly since the mass and heat transport to/from the  
 6 catalyst layer from/to the flow channel/rib is in the through-plane direction. Notably,  
 7 the fuel cell performance improves with decreasing the GDL through-plane thermal  
 8 conductivity as it lowers heats dissipation and increases the reaction rate at the cathode  
 9 catalyst layer.
- 10 • It is recommended that in the design and manufacture of the fibre GDLs, the carbon  
 11 fibre needs to be more oriented in the through-plane direction as against the  
 12 conventional in-plane direction as the GDL transport properties in that direction will  
 13 improve the performance of the PEFC.

14 Based on the findings of the study, it is recommended to design GDLs with superior through-  
 15 plane electrical conductivity and, to a lesser extent, through-plane diffusibility and thermal  
 16 conductivity. This could be achieved by having more carbon fibres oriented in the through-  
 17 plane direction.

## 18 Nomenclature

19	$a$	<i>Specific surface area, <math>m^{-1}</math></i>
20	$A_{ch}$	<i>Channel cross-sectional area, <math>m^2</math></i>
21	$c$	<i>Concentration, <math>mol/m^3</math></i>
22	$D$	<i>Diffusivity, <math>m^2/s</math></i>
23	$E_0$	<i>Reference potential, <math>V</math></i>
24	$E_r$	<i>Equilibrium potential, <math>V</math></i>
25	$F$	<i>Faraday constant, <math>C/mol</math></i>
26	$i$	<i>Current density, <math>A/m^2</math></i>
27	$i_0$	<i>Exchange current density, <math>A/m^2</math></i>

1			
2			
3	1	$i_{op}$	Operating current density, $A/m^2$
4			
5	2	$j$	Volumetric transfer current, $A/m^3$
6			
7	3	$K$	Permeability, $m^2$
8			
9	4	$M$	Molecular weight, $kg/mol$
10			
11	5	$P$	Pressure, $Pa$
12			
13	6	$R$	Universal gas constant, $J/mol \cdot K$
14			
15	7	$R_a$	Anode exchange current density
16			
17	8	$R_c$	Cathode exchange current density
18			
19	9	$S$	Source term in conservation equations
20			
21	10	$T$	Cell operating temperature, $K$
22			
23	11	$\vec{u}$	Velocity vector, $m/s$
24			
25	12	$Y$	Mass fraction
26			
27	13	$\Delta S$	Entropy
28			
29	14	<b>Greek symbols</b>	
30			
31	15	$\rho$	Density, $kg/m^3$
32			
33	16	$\mu$	Dynamic viscosity, $Pa \cdot s$
34			
35	17	$\sigma$	Electrical/ionic conductivity, $S/m$
36			
37	18	$\beta$	Inertial coefficient
38			
39	19	$\eta$	Over-potential, $V$
40			
41	20	$\varepsilon$	Porosity
42			
43	21	$\phi$	Potential, $V$
44			
45	22	$K$	Thermal conductivity, $W/m \cdot K$
46			
47	23	$\alpha$	Transfer coefficient
48			
49	24	$\xi$	Stoichiometric ratio
50			
51	25	<b>Subscripts</b>	
52			
53	26	$a$	Anode
54			
55	27	$act$	Activation
56			
57	28	$c$	Cathode
58			
59	29	$e$	Energy
60			
	30	$k,j$	Species
	31	$m$	Membrane phase
	32	$s$	Solid phase
	33	$sat$	Water saturation
	34	$v$	Water vapor
	35	$=$	In-plane
	36	$\perp$	Through-plane
	37	<b>Superscripts</b>	
	38	$eff$	Effective
	39	$ref$	Reference value

## 1 **Abbreviations**

2	3	4
5	2	<i>GDL</i> <i>Gas diffusion layer</i>
6	3	<i>MEA</i> <i>Membrane electrode assembly</i>
7	4	<i>PEFC</i> <i>Proton exchange membrane fuel cell</i>
8	5	<i>PTFE</i> <i>Polytetrafluoroethylene</i>

## 10 **Chemical symbols**

11	7	<i>H<sub>2</sub></i> <i>Hydrogen molecule</i>
12	8	<i>H<sub>2</sub>O</i> <i>Water molecule</i>
13	9	<i>O<sub>2</sub></i> <i>Oxygen molecule</i>

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**Table 1 Geometrical and physical properties for the base case of the PEFC model.**  
**Sources: Berning et al. (2002); Ismail et al. (2012); Zawodzinski et al. (1993).**

Property	Value
Channel length	$5 \times 10^{-2}$ m
Channel height	$1.0 \times 10^{-3}$ m
Channel width	$1.0 \times 10^{-3}$ m
Land area width	$1.0 \times 10^{-3}$ m
GDL thickness	$0.26 \times 10^{-3}$ m
Catalyst layer thickness	$1.0 \times 10^{-5}$ m
Membrane thickness	$0.23 \times 10^{-3}$ m
Operating temperature	353 K
Gauge pressure at anode	5 atm
Gauge pressure at cathode	3 atm
Relative humidity of inlet gases	100%
Oxygen/nitrogen molar ratio in air	0.21/0.79
Catalyst layer porosity	0.4
GDL porosity	0.7
GDL permeability	$4.97 \times 10^{-13}$ m <sup>2</sup>
Reference hydrogen concentration, $c_{H_2}^{ref}$	40 mol/m <sup>3</sup>
Reference oxygen concentration, $c_{O_2}^{ref}$	40 mol/m <sup>3</sup>
Electrical conductivity of solid phase	6000 S/m
Ionic conductivity of the membrane	0.6 S/m
Catalyst layer permeability	$1 \times 10^{-13}$ m <sup>2</sup>
Membrane permeability	$1.8 \times 10^{-18}$ m <sup>2</sup>
Thermal conductivity of GDLs	75 W/(m-K)
Thermal conductivity of catalyst layers	75 W/(m-K)
Thermal conductivity of Bipolar plates	75 W/(m-K)
Thermal conductivity of the membrane	0.67 W/(m-K)
Faraday's constant	96485 C/mol
Universal gas constant	8.314 J/(mol-K)
Active area	$11.56 \times 10^{-4}$ m <sup>2</sup>
Anode inlet mass fraction of hydrogen	0.37
Anode inlet mass fraction of water	0.63
Cathode inlet mass fraction of oxygen	0.21
Cathode inlet mass fraction of water	0.103
Cathode inlet mass fraction of nitrogen	0.69

Anode concentration exponents	0.5
Cathode concentration exponents	1
Anode reference exchange current density, $i_{0,a}^{ref}$	6000 A/m <sup>2</sup>
Cathode reference exchange current density, $i_{0,c}^{ref}$	0.0044 A/m <sup>2</sup>
Transfer coefficients for anode reaction	0.5
Transfer coefficients for cathode reaction	1
Anode specific surface area, $a_a$	$1.0 \times 10^7$ m <sup>-1</sup>
Cathode specific surface area, $a_c$	$1.0 \times 10^7$ m <sup>-1</sup>

**Table 2 Key GDL transport properties in through-plane and in-plane directions.**

	<b>Case 1</b>		<b>Case 2</b>	<b>Case 3</b>
<b>Transport properties</b>	<b>Through-plane</b>	<b>In-plane</b>	<b>Isotropic (Through-plane)</b>	<b>Isotropic (In-plane)</b>
<b>Permeability (m<sup>2</sup>)</b> <b>Source: Ismail et al. (2012)</b>	$4.97 \times 10^{-13}$	$1.87 \times 10^{-12}$	$4.97 \times 10^{-13}$	$1.87 \times 10^{-12}$
<b>Diffusibility (m<sup>2</sup>/s).</b> <b>Source: Kramer et al. (2008)</b>	0.3	0.5	0.3	0.5
<b>Thermal Conductivity (W/m-K)</b> <b>Source: Li et al. (2017)</b>	1.7	21	1.7	21
<b>Electrical Conductivity (S/m)</b> <b>Source: Ismail et al. (2012)</b>	48	4000	48	4000

**Table 3 Computation cases for the GDL gas permeability investigation. Source: Ismail et al. (2012).**

Case Number	Permeability (m <sup>2</sup> )		Average Current density (A/cm <sup>2</sup> ) at 0.55 V
	Through-plane, K <sub>⊥</sub>	In-plane, K <sub>∥</sub>	
1	$4.97 \times 10^{-13}$	$1.87 \times 10^{-12}$	0.5016
2	$4.97 \times 10^{-13}$	$1.87 \times 10^{-13}$	0.5015
3	$4.97 \times 10^{-13}$	$1.87 \times 10^{-11}$	0.5017
4	$4.97 \times 10^{-14}$	$1.87 \times 10^{-12}$	0.5016
5	$4.97 \times 10^{-12}$	$1.87 \times 10^{-12}$	0.5017

**Table 4 Computation cases for the GDL gas diffusivity investigation. Source: Kramer et al. (2008).**

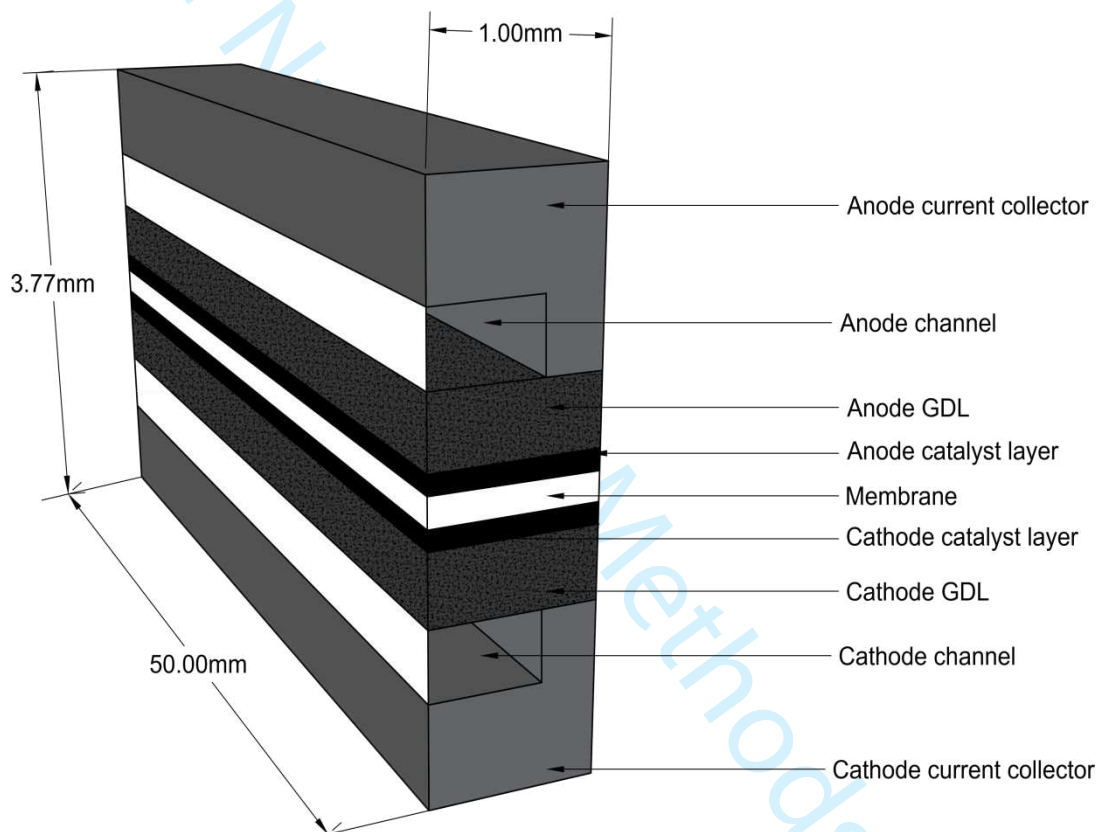
Case Number	Diffusibility		Average Current density (A/cm <sup>2</sup> ) at 0.55 V
	Through-plane, $f(\epsilon)_{\perp}$	In-plane, $f(\epsilon)_{\parallel}$	
1	0.3	0.5	0.5115
2	0.3	0.3	0.5109
3	0.3	0.7	0.5119
4	0.1	0.5	0.4932
5	0.5	0.5	0.5155

**Table 5 Computation cases for the GDL thermal conductivity investigation. Source: Alhazmi et al. (2013).**

Case Number	Thermal Conductivity (W/m.K)		Average Current density (A/cm <sup>2</sup> ) at 0.55 V
	Through-plane	In-plane	
1	0.1	10	0.5029
2	0.1	1	0.5054
3	0.1	100	0.5017
4	0.01	10	0.5089
5	1	10	0.4955

**Table 6 Computation cases for the GDL electrical conductivity investigation. Source: Ismail et al. (2012).**

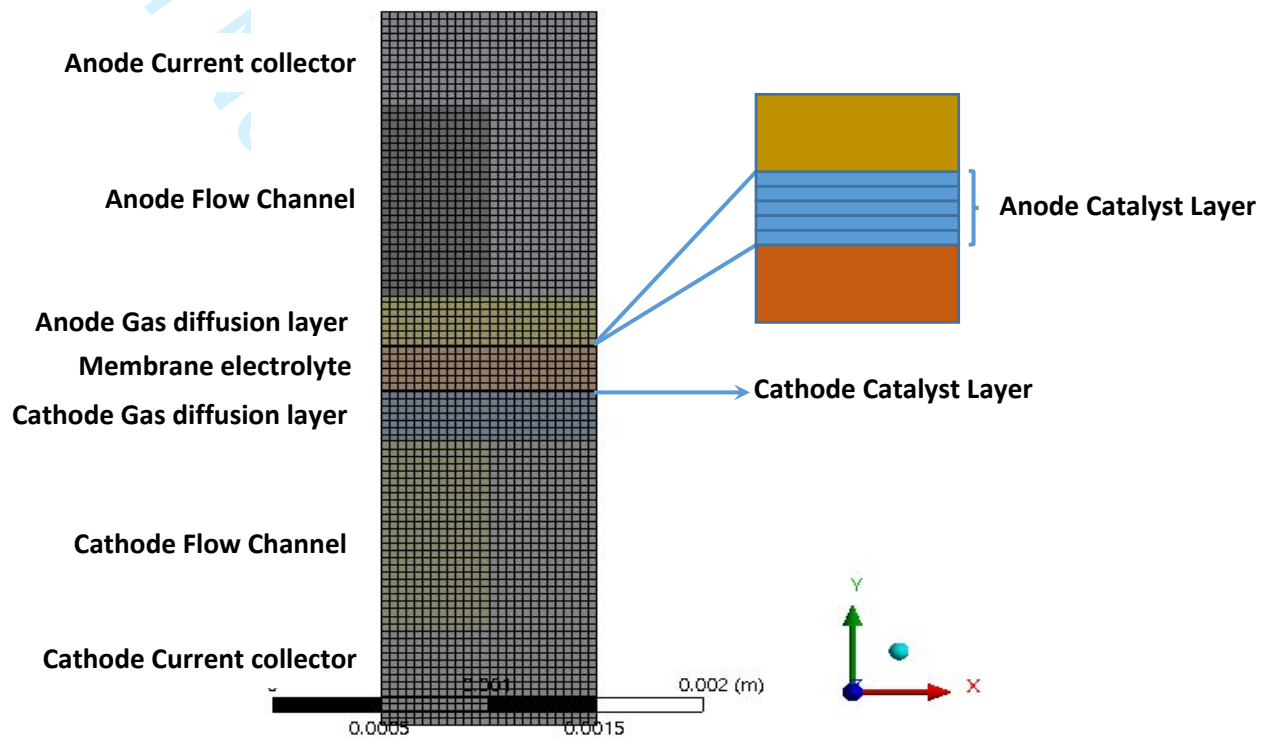
Case Number	Electrical Conductivity (S/m)		Average Current density (A/cm <sup>2</sup> ) at 0.55 V
	Through-plane	In-plane	
1	48	4000	0.493
2	48	2000	0.480
3	48	8000	0.503
4	24	4000	0.386
5	96	4000	0.580



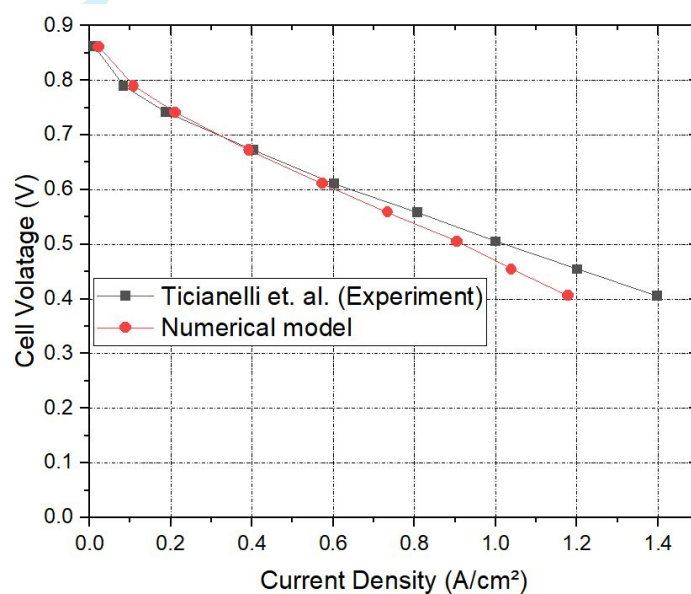
**Figure 1 A Schematic of the computational domain.**



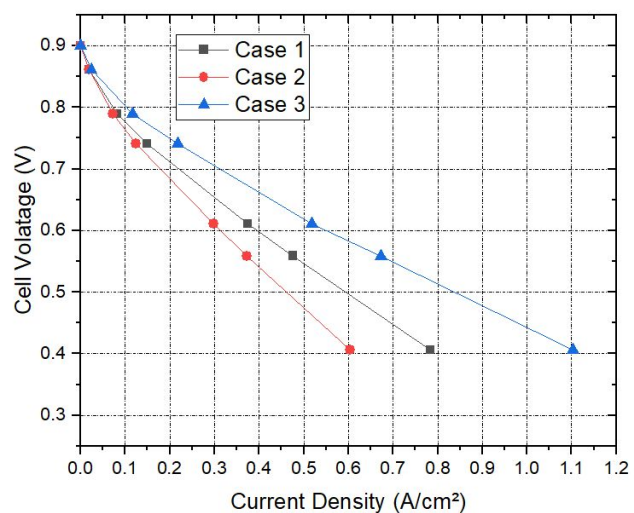
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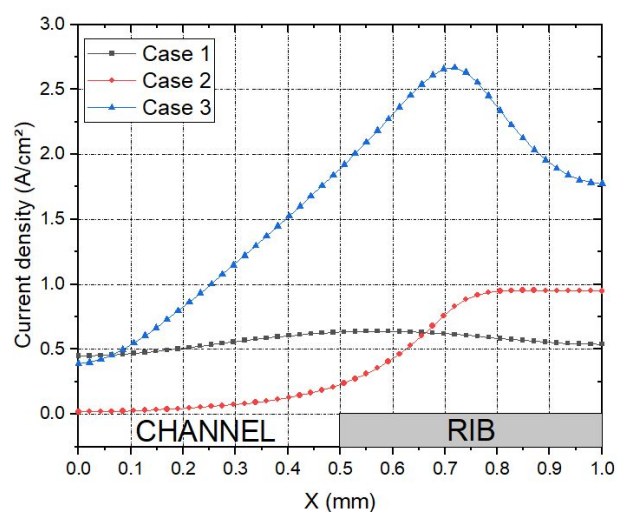
**Figure 2** The mesh profile of the front view of the geometry. Note that (i) the anode catalyst layer has been zoomed in to show the mesh across the catalyst layer and (ii) the number of elements in the z-direction is 350.



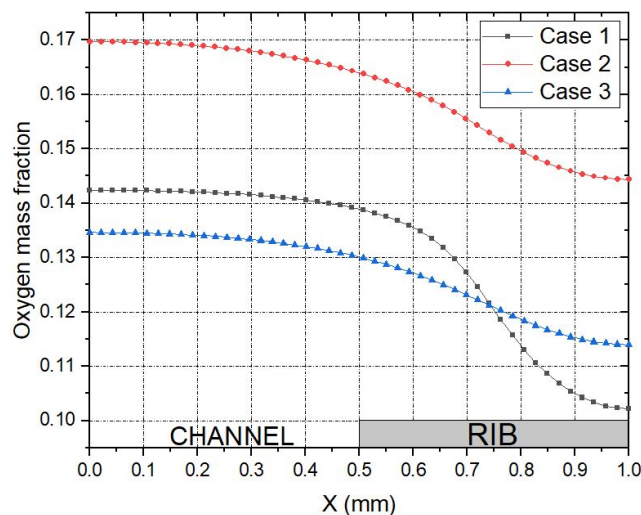
**Figure 3** The polarization curve generated from the numerical model as compared to the experimental polarization curve taken from Ticianelli et al. (1998).



(a)

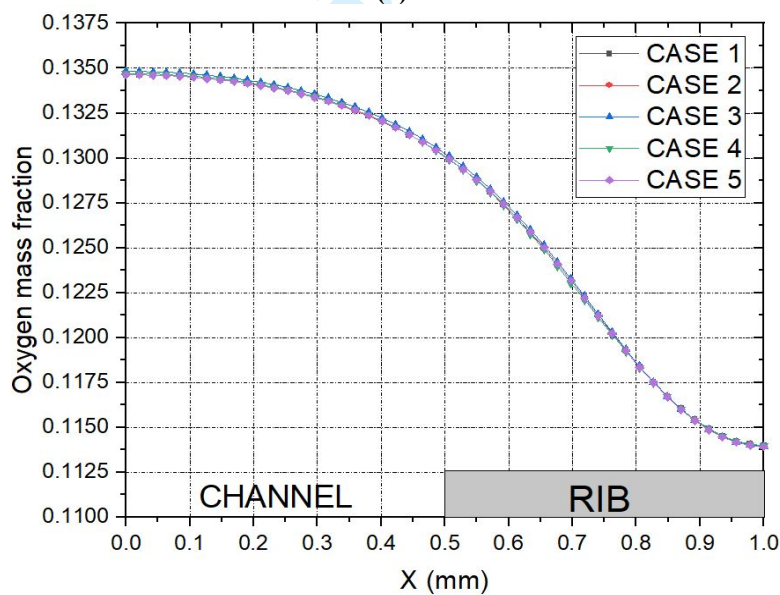
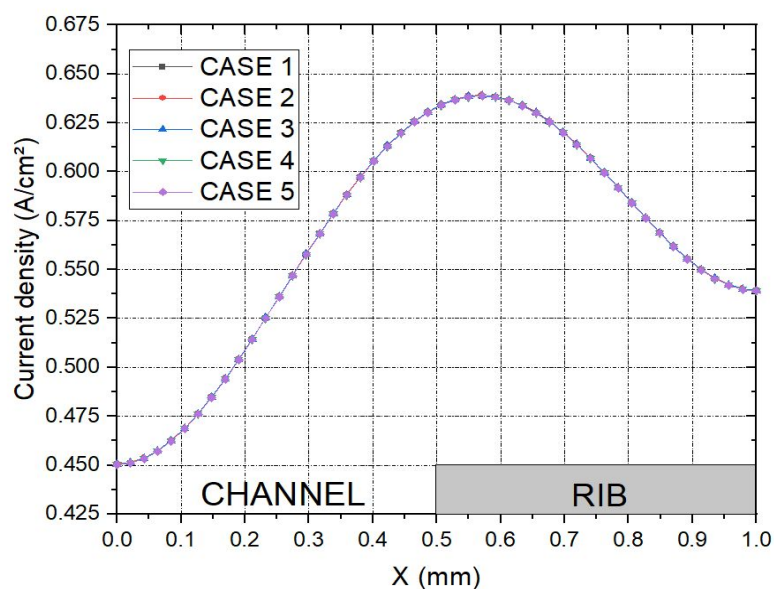


(b)



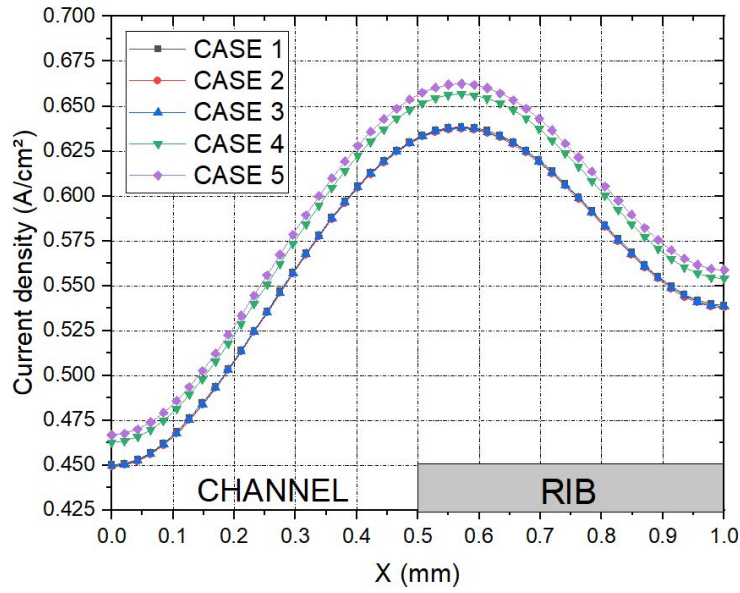
(c)

Figure 4 (a) The polarisation curves, (b) the distribution of current density within the cathode GDL at 0.55 V and (c) the distribution of oxygen mass fraction within the cathode GDL at 0.55 V for the investigated cases: Case 1 (where the GDL transport properties are anisotropic), Case 2 (where the GDL transport properties are isotropic and having the same values as those of the through-plane direction) and Case 3 (where the GDL transport properties are isotropic and having the same values as those of the in-plane direction).

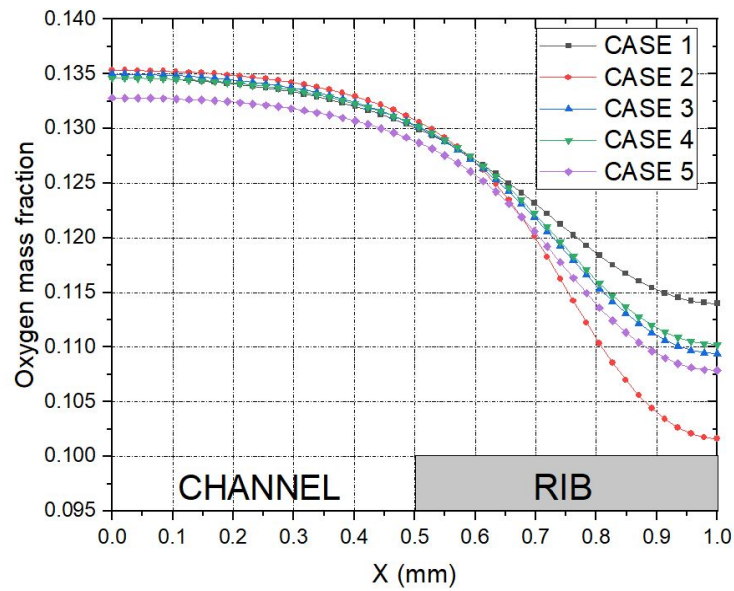


(b)

**Figure 5** The distribution of (a) current density and (b) oxygen mass fraction within the cathode GDL at 0.55 V for the GDL gas permeability computation cases shown in Table 3.

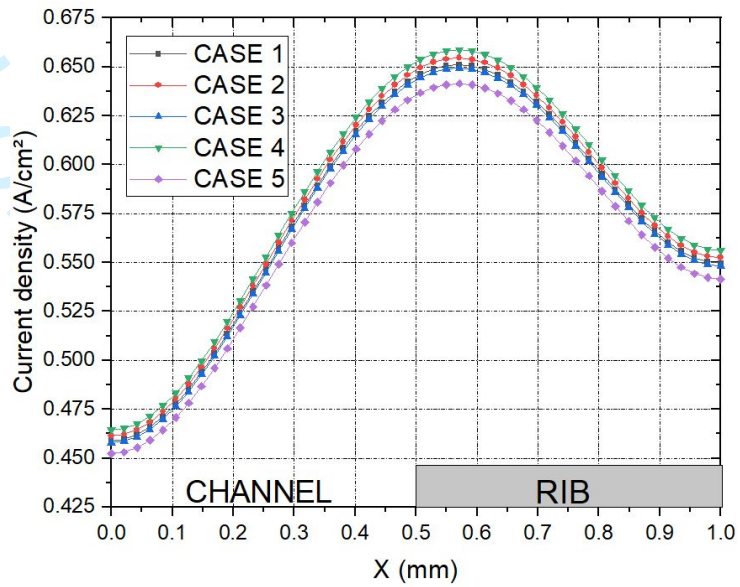


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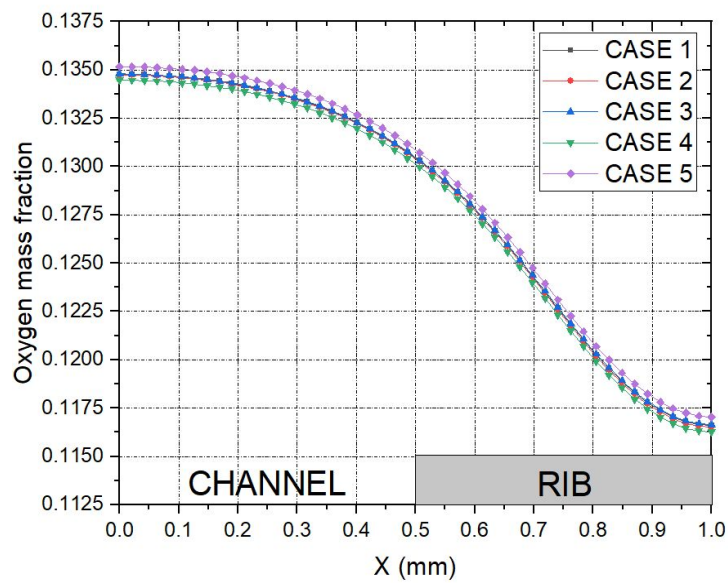


(b)

**Figure 6** The distribution of (a) current density and (b) oxygen mass fraction within the cathode GDL at 0.55 V for the GDL gas diffusivity computation cases shown in Table 4.



(a)



(b)

**Figure 7** The distribution of (a) current density and (b) oxygen mass fraction within the cathode GDL at 0.55 V for the GDL thermal conductivity computation cases shown in Table 5.

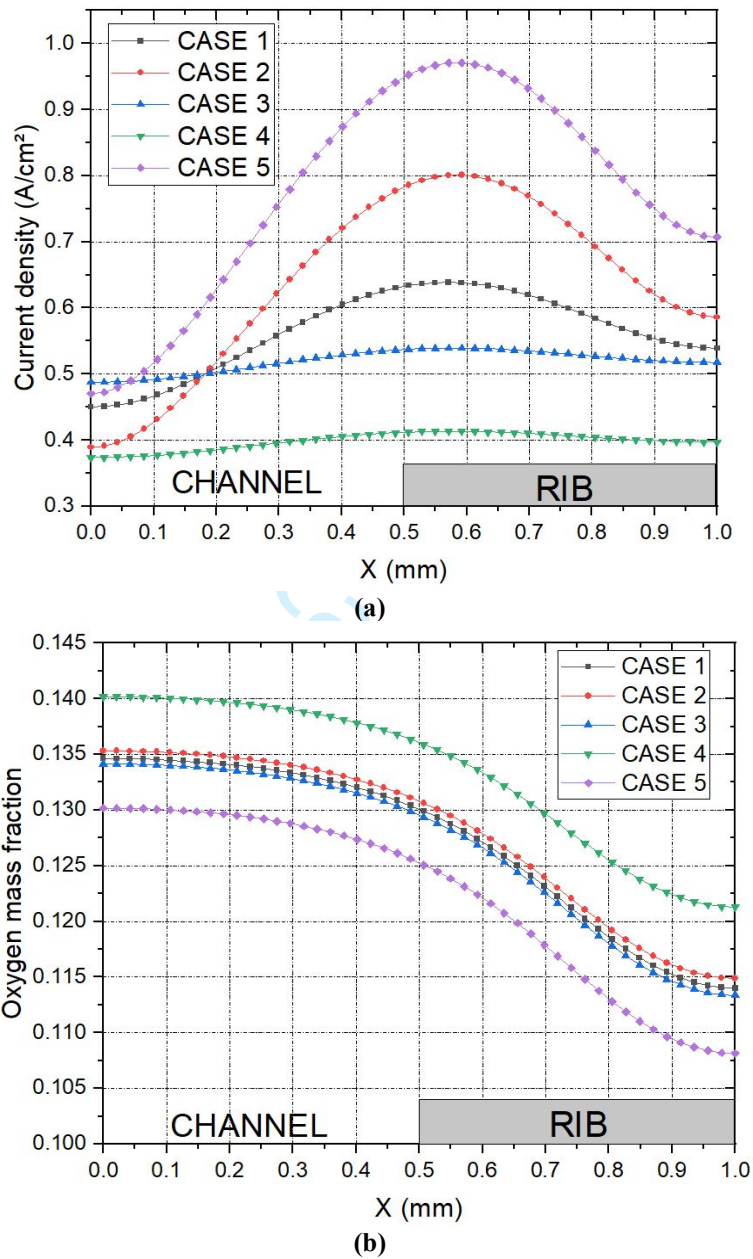


Figure 8 The distribution of (a) current density and (b) oxygen mass fraction within the cathode GDL at 0.55 V for the GDL electrical conductivity computation cases shown in Table 6.