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- Drone-mounted GPR surveying: flight-height considerations for diffraction-based velocity
 analysis
- 3

4 Abstract

5 Recent studies highlight the potential of the drone platform for ground penetrating 6 radar (GPR) surveying. Most guidance for optimising drone flight-heights is based on 7 maximising the image quality of target responses, but no study yet considers the impact on 8 diffraction travel-times. Strong GPR velocity contrasts across the air-ground interface introduce significant refraction effects that distort diffraction hyperbolae and introduce 9 10 errors into diffraction-based velocity analysis. The severity of these errors is explored with 11 synthetic GPR responses, using ray- and finite-difference approaches, and a field GPR dataset acquired over a sequence of diffracting features buried up to 1 m depth. 12 Throughout, GPR antennas with 1000 MHz centre frequency are raised from the ground to 13 14 heights < 0.9 m (i.e., 0-3 times the wavelength in air). Velocity estimates are within +10% of 15 modelled values (spanning from 0.07 m/ns to 0.13 m/ns) if the antenna height is within ½ 16 wavelength in air above the ground surface. Greater heights reduce diffraction curvature, 17 damaging velocity precision and masking diffractions against a background of subhorizontal reflectivity. Field data highlight further problems of the drone-based platform, with data 18 dominated by reverberations in the air-gap and reduced spatial resolution of wavelets at 19 20 target depth. We suggest that a drone-based platform is unsuitable for diffraction-based 21 velocity analysis, and any future drone surveys are benchmarked against ground-coupled datasets. 22

1 Introduction

2	Ground penetrating radar (GPR) is one of several geophysical systems to be
3	considered for deployment on a drone-based platform. GPR is an established near-surface
4	survey technique, using radio-wave energy to image a variety of geological, hydrological and
5	anthropogenic targets in the upper few metres of the subsurface (Annan, 2005). Most often,
6	the antennas of a GPR system remain closely coupled with the ground surface but the
7	growing availability and affordability of drone technology has prompted experimentation
8	with drone-based GPR deployments.
9	Drones offer logistical advantages for rugged, dangerous and/or inaccessible
10	terrains, e.g. over water courses (Lane Jr, 2019; Edemsky et al., 2021), at sites contaminated
11	with unexploded ordnance (Cerquera et al, 2017; García-Fernández et al., 2020; Šipoš and
12	Gleich, 2020) or over crevassed glacier fields (Mankoff et al., 2020). Even for practical
13	terrains, an autonomous drone following a pre-programmed flight path (Hammack et al.,
14	2020) improves efficiency by allowing surveyors to deploy other equipment simultaneously
15	(e.g., systems requiring manual installation, such as seismic and/or resistivity methods).
16	Although drone-based GPR surveys are subject to at least two sets of legislation that
17	regulates drone operations (e.g., Valentine, 2019) and GPR emissions (e.g., Ofcom, 2019),
18	several recent studies have demonstrated advantages of the acquisition platform (Cerquera
19	et al., 2017; Chandra and Tanzi, 2018; Garcia-Fernandez et al., 2020; Edemsky et al., 2021).
20	When benchmarking against conventional ground-coupled deployments, assessments of
21	drone-based GPR data typically consider the impact on recorded wavelet amplitudes. For

22 air-launched systems, the GPR energy entering the subsurface is diminished by reflectivity

- losses at the air-ground interface (García-Fernández et al., 2020) but other factors vary as a
 function of the drone flight-height, and these include:
- i) increased geometric spreading, with antennas positioned further from the target
 4 (García-Fernández et al., 2020);
- 5 ii) interference between reflections from the air-ground interface, and those from
- 6 within the subsurface (Diamanti and Annan, 2017; Edemsky et al., 2021), and
- 7 iii) poorer spatial resolution given the more rapid defocussing of the GPR beam as it
- 8 travels through air (Diamanti and Annan, 2013, 2017), and the vulnerability to
- 10 The experience of vehicle-mounted GPR surveys (e.g., Saarenketo and Scullion, 2000;

artefacts from above-surface scatterers.

11 Eriksen et al., 2004; Zan et al., 2016) can provide a foundation for height considerations, but

12 these often use horn antennas to maximise radiation in the target direction (usually

13 downwards). For any given centre frequency, horn antennas tend to be bulkier than bow-tie

systems (Pieraccini et al., 2017) hence, with accompanying batteries and control units, may

15 exceed the payload of the drone. Furthermore, most experiments with drone-based GPR

aim to mount an existing commercial system on the drone and most of these have a bow-tie

17 or dipole design. The issues listed above may therefore represent widespread design

18 considerations but recommendations for flight-height remain disparate, variously

19 suggesting any height between 0.5-1.5 times the dominant wavelength of the radar wavelet

- in air (e.g., Diamanti and Annan, 2017; García-Fernández et al., 2018, 2020; Šipoš and
- 21 Gleich, 2020). However, Smith (1984) suggests that antenna coupling is poor when antennas
- are elevated by more than 0.1 times the wavelength in air, indicating that these larger
- 23 conventions could be problematic.

9

Having noted these amplitude effects and the research effort to understand them, 1 2 this paper investigates the impact of flight-height on travel-time relationships expressed in 3 recorded data and how they impact diffraction-based velocity analysis. A starting assumption, when comparing to ground-based data, may be that reflections in drone-based 4 5 data are simply shifted late according to the additional travel-time through the air gap. This 6 may be reasonable for specular reflectivity, but refraction effects at the air-ground interface 7 can cause distortions to the appearance of diffraction hyperbolae (Causse, 2004). This is 8 especially problematic for engineering and archaeological applications where, for example, 9 targets are often detected using diffraction responses and, furthermore, their curvature is 10 used to determine subsurface velocities (e.g., for migration and time-to-depth conversion). Velocities may also be converted to dielectric permittivity, to inform hydrological and 11 engineering quantities such as water content and pavement density (Bradford et al., 2009; 12 13 St Clair and Holbrook, 2017; Diamanti et al, 2017). The limitations of hyperbolic velocity 14 analysis, and the equivalent issues in seismic reflection processing (e.g., Alkhalifah, 1997), will be familiar to many in the community but, to date, there has been no study to explore 15 16 the magnitude of velocity errors for a drone-based GPR system. It is therefore worth 17 exploring the feasibility of diffraction-based velocity analysis for this novel survey platform.

Using ray-based and finite-difference synthetic analyses, we show the severity of these distortions as the height of drone-mounted antennas is changed, and demonstrate the impact on diffraction-based velocity analysis. Our synthetics are complemented with field data, representing drone acquisition using antennas mounted on a height-adjustable frame. These data suggest that there would significant difficulty in even recognising diffraction hyperbolae in a drone-based dataset, potentially precluding efforts to improve

1 velocity characterisation. Finally, we advise on the situations in which 'fly low' or 'fly high'

- 2 scenarios may be preferable.
- 3

4 Diffraction travel-times and velocity relationships

5 The travel-time, $t(x-x_0)$, of a diffraction hyperbola from a point-source target is

6
$$t(x-x_0) = \sqrt{t_0^2 + \frac{4(x-x_0)^2}{v_{RMS}^2}}$$
 (1)

7 where *x* is the midpoint position between common-offset GPR antennas, x_0 is the surface 8 position vertically above the diffractor, t_0 is the two-way travel-time of diffracted arrivals at 9 x_0 , and v_{RMS} is root-mean-square velocity. These terms, and the hyperbolic t(x-x0) 10 relationship they describe, are shown schematically for the ground-based raypath model in 11 Figure 1. Assuming that drone-mounted antennas are flown at height *h* above a subsurface 12 with constant velocity v_{sub} , v_{RMS} is the travel-time weighted average between v_{sub} and the 13 velocity of the GPR wavelet through air (v_{air} , = 0.3 m/ns):

14
$$v_{RMS} = \sqrt{\frac{v_{sub}^2(t_0 - t_{air}) + v_{air}^2 t_{air}}{t_0}}$$
, (2)

where t_{air} is the two-way travel-time (= $2h/v_{air}$) through the air-gap at $x = x_0$. For a groundbased system, t_{air} is 0 and $v_{RMS} = v_{sub}$. These equations are strictly valid for monostatic systems, with zero transmitter-receiver offset, but nonetheless remain widely applied for finite-offset bistatic systems.

v_{RMS} can be evaluated using several analytic methods, including curve-fitting
 approaches and semblance-based velocity analysis (Booth and Pringle, 2016). With pairs of
 v_{RMS} and t₀ available, *v_{sub}* can be approximated using Dix's Equation (Dix, 1955):

1
$$v_{sub} \approx \sqrt{\frac{v_{RMS}^2 t_0 - v_{air}^2 t_{air}}{t_0 - t_{air}}}$$
, (3)

2 which can be used recursively to derive the vertical variation of v_{sub} if v_{RMS} : t_0 pairs are 3 available.

4	Equation (1) is exactly hyperbolic for ground-based systems and constant, isotropic,
5	v_{sub} . In layered velocity models, non-hyperbolic travel-time terms are introduced because
6	refraction across interfaces is neglected (i.e., straight rays are assumed). Since travel-times
7	deviate from those predicted by Equation (1), velocity estimates derived with it are
8	inaccurate with respect to the true v_{sub} . This is exacerbated where $ x-x_0 $ is large with
9	respect to the vertical distance between the antennas and the target (i.e., the sum of flight-
10	height and target depth). These errors can be circumvented using higher-order terms in
11	travel-time approximations (e.g., Causse, 2004; Causse and Sénéchal, 2006) or through full
12	waveform inversion (e.g., Jazayeri et al., 2018), but these are less widespread in practice
13	than assuming hyperbolic travel-times and accepting some velocity error. However, strong
14	refraction across the air-ground likely increases the severity of these errors.

15 Additionally, there are systematic velocity errors that should be considered for any practical velocity analysis. A diffracting target with a finite radius causes v_{sub} to be biased 16 17 fast (Shihab and Al-Nauimy, 2005; Ristic et al., 2009) and v_{sub} is exaggerated further if the intersection between the long-axis of an elongate diffractor (e.g., a pipe) and the profile 18 direction is not orthogonal. Conversely, many velocity analysis approaches (e.g., curve-19 20 matching and semblance) consider the travel-times of the highest amplitude cycles of the 21 GPR wavelet and therefore cause v_{sub} to be biased slow; velocity is expressed more accurately by first-break travel-times (Booth et al., 2010; Booth and Pringle, 2016). Although 22

- 1 the impact of these is appreciated, the relative significance of velocity errors from a drone-
- 2 based survey platform is currently unexplored.

3 Data Simulation

Two approaches were adopted to simulate drone-mounted GPR acquisitions using different flight heights and a range of *v*_{sub}. First, a simple ray-tracing approach was used to illustrate the distortion of diffracted raypaths and the origins of velocity errors. Second, finite-difference models were implemented in gprMax (Warren et al., 2016), to capture the near-field behaviour of a finite-frequency wavefield and a more realistic antenna radiation pattern.

10

11 Methods: Ray-based synthetics

12 Travel-times were computed for a point diffractor at 0.2 m depth in a homogeneous isotropic half-space. Transmitting and receiving antennas were offset at 0.02 m, which is 13 smaller than might be used in practice but used here to highlight the contribution to velocity 14 15 errors of refraction effects rather than non-zero offset. Antenna midpoint positions 16 extended to ±0.5 m either side of the diffractor, sampling every 0.02 m. Responses were 17 modelled with drone flight-height, h, ranging from 0 to 0.9 m. These heights correspond to 18 values up to 3-times the wavelength, λ , in air of a 1000 MHz wavelet; although wavelength 19 has no practical relevance in a ray-based simulation, we report h/λ ratios to compare with previous studies and for reference to observations from later finite-difference models. V_{sub} 20 was increased in 0.01 m/ns increments from 0.07 m/ns to 0.13 m/ns, and raypaths were 21 22 calculated by applying Snell's Law at the air-ground interface.

2	Figure 1 shows modelled raypaths for all <i>h</i> values and $v_{sub} = 0.09$ m/ns. The ground-based
3	model (Figure 1a) shows the straight-rays expected for constant <i>v_{sub}</i> . Low drone flight-
4	heights introduce significant ray-bending across the air-ground interface which gradually
5	decreases with increasing <i>h</i> . The corresponding travel-time curves (Figure 2a) highlight the
6	distortion from the diffraction hyperbola recorded by ground-based antennas. For models
7	with h > 0, the ground-going leg of the raypaths shows little variation from the vertical,
8	hence the corresponding diffractions are simply time-shifted variants of a hyperbola
9	originating at the air-ground interface. In all cases, the shift is \sim 4.4 ns, corresponding to the
10	vertical two-way travel time between the air-ground interface and the diffractor (Figure 2b)
11	This implies that refraction effects prevent v_{sub} from significantly influencing the curvature
12	of the diffraction response.

13

14 Results: Ray-based synthetics

15 V_{RMS} is estimated for each model using a linear regression to diffraction travel-times 16 within an aperture extending ±0.4 m either side of diffractor position, expressed in Figure 2c on t^2-x^2 axes. The reciprocal gradient of the best-fit straight-line (black dashed lines) defines 17 $\frac{1}{2}v_{RMS}^2$, and its intercept t_0^2 . Being exactly hyperbolic, travel-times for ground-based 18 19 antennas are fit perfectly, however non-hyperbolic terms for h > 0 introduce curved $t^2 - x^2$ 20 responses which are most evident for $h \le 0.3$ m. v_{sub} was estimated for each case by 21 substituting v_{RMS} :to into Dix's Equation, together with t_{air} (annotated in Figure 1) and v_{air} = 0.3 m/ns. Figure 3a shows v_{RMS} and the resulting v_{sub} , the latter expressed as a percentage 22 23 error in Figure 3b.

All v_{sub} estimates are biased fast but the largest errors are shown for the lowest h(e.g., >50% overestimate for h = 0.075 m, 10% for h = 0.9 m). Equivalent overestimates for all modelled v_{sub} (Figure 3c) suggest that velocity mismatch decreases with both increasing hand v_{sub} . For the fastest velocity case, overestimates are always < 40%, and are ~7% for the highest flight-heights. However, overestimates can approach 100% for cases of $v_{sub} \le 0.08$ m/ns and low flight-heights.

The analysis was repeated for diffractors placed at 0.6 m and 1.0 m depth (Figures 3d and e, respectively). For the 0.6 m depth case, *v*_{sub} overestimates are typically <10% for faster *v*_{sub} and/or greater flight-height. The overestimate seldom exceeds 6% for the 1 mdepth case, but targets here would not be widely considered suitable for imaging with 1000 MHz antennas. The errors in Figure 3b are therefore more illustrative of a typical best-case scenario for this antenna frequency.

13

14 Methods: Finite-difference Time-Domain (FDTD) synthetics

Ray-based modelling illustrates the challenges for diffraction-based velocity analysis 15 but neglects realistic aspects of GPR propagation. As ray-based synthetics are infinite-16 17 frequency models, they impose far-field conditions and thus plane-wave arrivals, yet 18 shallow targets could be present in the near-field (e.g., within a small number of 19 wavelengths; Warren and Giannopoulos, 2012) where wavefront curvature is significant. Furthermore, ray-based arrivals were weighted equally in the linear regression, whereas 20 amplitudes in real data are affected by geometrical spreading, attenuation losses and, in 21 22 particular, the anisotropic radiation pattern of GPR antennas. The lattermost is likely to be

particularly significant given the obliquity of the far-offset raypaths implied for low-*h* values
 in Figure 1.

3	FDTD synthetics were undertaken using gprMax (Warren, Giannapoulos and
4	Giannakis, 2016). A 3-D domain of dimensions $[x, y, z] = [1.0 \times 1.0 \times 1.2]$ m was established
5	and discretised into cells of dimensions [Δx , Δy , Δz] = 0.005 m. The modelled structure is
6	2.5D, continuous in the y-dimension and represents a horizontal pipe installed in a trench
7	(Figure 4). The pipe is a cylindrical perfect electrical conductor (pec), with diameter 0.1 m
8	and centred at $[x, z] = [0.5, 0.2]$ m. The horizontal floor of the trench is 0.5 m wide, 0.3 m
9	deep, and rises to 0.2 m at the edges of the domain. The overlying air-gap extends 0.7 m
10	above the ground surface, allowing antennas (red circles, Figure 4) to be placed at a range of
11	h from 0 to 0.6 m. This is up to 2 λ , for the 1000 MHz source wavelet centre frequency we
12	assumed.

All physical quantities are fixed, except for the relative dielectric permittivity, ε_r , of 13 the trench fill which is first set to 18.3 and then to 5.3, giving v_{sub} of 0.07 and 0.13 m/ns (the 14 extreme velocity cases considered in Section 3.1). The velocity through the lowermost layer 15 16 is fixed at 0.010 m/ns, such that the velocity contrast at the base of the trench is \pm 0.03 17 m/ns. Output radargrams were produced at y = 0.5 m, with antenna midpoints spanning from 0.05 to 0.95 m, in 0.02 m intervals. Once simulated, the time step in the synthetic 18 radargrams was downsampled via linear interpolation, from 0.0096 ns to 0.1 ns, to improve 19 20 the efficiency of later velocity analysis calculation. The radargrams were contaminated with 21 noise traces from a 1000 MHz field dataset (Section 4), scaled to give 15 dB signal-to-noise ratio at the diffraction apex. 22

23

1 Results: FDTD synthetics

2	Velocity analysis was undertaken for each model using semblance (e.g., Stucchi et
3	al., 2020), configured using the travel-time expression in Equation (1) (Booth and Pringle,
4	2016). The calculation spanned an aperture of 0.4 m either side of the apex and used an
5	analysis window with 0.1 ns duration. Figure 5 shows output radargrams and their
6	semblance responses; columns (a) and (b) relate to v_{sub} of 0.07 m/ns and 0.13 m/ns,
7	respectively, with rows (i) to (vii) showing flight-heights increased from 0 to 0.6 m. The
8	hyperbola on each radargram is the semblance-derived approximation to first-break travel-
9	times (ornament \oplus). These are based on semblance picks made at the strongest semblance
10	response, corresponding to the strongest half-cycle of the GPR wavelet (ornament \otimes) but
11	corrected for the ~0.53 ns lag from first break (Booth et al., 2010). The precision in v_{RMS} , and
12	in v_{sub} thereafter, is based on the width of the 90% semblance contour (Booth et al., 2011).
13	Diffraction responses in Figure 5 flatten progressively with increasing <i>h</i> above the
14	air/ground interface, becoming indistinct from the response from the trench floor.
15	Furthermore, consistent with observations in Figure 2b, they become time-shifted replicas
16	of each other: the travel-time moveout of the diffractions differs by just 0.8 ns between
17	panels aviii and bviii, despite the difference in the velocity models. Figure 6 shows that v_{RMS}
18	tends towards 0.3 m/ns as h increases (Figure 6a,c), with both v_{RMS} and v_{sub} becoming
19	increasingly imprecise. For expressing v_{sub} as a fractional error (Figure 6b,d), reference
20	values are increased respectively to 0.079 m/ns and 0.134 m/ns according the diffraction
21	travel-time given in Shihab and Al-Nuaimy (2005; Equation 3 therein) that incorporates the
22	finite-radius effect of our pipe geometry (specifically, with a radius-to-centre-depth ratio of

0.25. For comparison, Figures 6b and d also include the relative errors in v_{sub} from the ray based models in Figure 3c.

3	Although Figure 6 suggests that model v_{sub} will be overestimated for any h > 0, errors
4	are generally less than in ray-based models particularly for small h. For h = 0.075 m (0.25 λ),
5	simple ray-based models indicated that slow velocities could be overestimated by 100%, yet
6	Figure 6b suggests an overestimate no greater than \sim 5%. This is attributed to antenna
7	radiation effects. For ε_r > 12, Warren and Giannopolous (2012) indicate a reduction of > 20
8	dB in radiated amplitudes for take-off angles exceeding 60°. For our model geometry and h
9	= 0.075 m, this angle is reached when antennas are located \pm 0.16 m either side of the
10	diffractor. The effect is clear in Figure 5aii, in which diffracted amplitudes decrease rapidly
11	beyond positions \pm 0.2 m from the diffraction apex meaning that arrivals outside of this
12	aperture contribute less to the overall semblance response. This is why the semblance-
13	derived travel-time curve is a good match to the curvature of the diffraction around its apex
14	and diverges at its flanks. Indeed, in revisiting Figure 2c, the local gradient of the $h = 0.075$ m
15	curve is steepest in the $[0-0.2]^2$ m ² range of x^2 , and a linear regression using only this range
16	reduces the overestimate of v_{sub} from >70% to ~45%.

Guidance from finite-difference simulations is therefore opposite to ray-based
modelling, indicating that the accuracy *and* precision of velocity estimates is benefitted by a
low flight-height (Smith, 1984). Furthermore, given their flatness, the responses observed
with antennas > 0.3 m (1 λ) high are likely more vulnerable to noise and static shifts
resulting from velocity heterogeneity and or antenna mispositioning.

22

1 Field Data

2	The practical implications of the synthetic models were explored using GPR field
3	data, acquired with an adaptable frame to simulate drone-based acquisitions at varying
4	flight-heights (Figure 7a). The frame is made from a polystyrene cradle and carries
5	Sensors&Software (S&S) pulseEKKO PRO 1000 MHz antennas with 0.15 m offset between
6	antenna centres. Consistent with a drone platform, there is no material beneath the
7	antennas hence they radiate directly into the air. A carry handle from a S&S low-frequency
8	antenna is attached to the frame with its adjustable legs marked in 0.05 m intervals. With
9	the system carried at a constant level, the antennas can be elevated to different heights
10	above the ground surface. Along-profile distances were measured using a calibrated
11	odometer wheel, towed behind the frame.

12

13 Field Data Acquisition

Field data (Booth, 2021) were acquired in July 2020 on Canal Road (UK National Grid SE 22306 36370), a quiet side-street in the Rodley district of Leeds, UK (Figure 7b). Restrictions imposed during the UK's COVID-19 response limited the range of accessible field locations. Nonetheless, Canal Road is of archaeological interest given its 200-year history accessing an industrial wharf on the adjacent Leeds-Liverpool canal (Figure 7b): the modern road surface likely covers the original structure.

GPR profiles are 20 m long, although only their first 8 m are used in this paper, with
0.01 m trace interval and repeated with *h* increasing from 0 m to 0.35 m in increments of

1 0.05 m (= $\lambda/6$ for a 1000 MHz wavelet in air). The time sampling interval was 0.1 ns. Data

2 were processed in Sandmeier ReflexW[©] software (version 8.5), using the sequence:

- 3 i) dewow filter (window length 2 ns),
- 4 ii) Ormsby bandpass filter (corner frequencies at 200-400-1200-2400 MHz),
- 5 iii) time-variant 'energy decay' gain function, and
- 6 iv) spatial filtering; the mean trace from within successive 3 m windows is
- 7 calculated and subtracted from individual traces, thus preferentially
- 8 suppressing horizontal arrivals.

9 The noise traces with which the gprMax models (Figure 5) were contaminated are extracted
10 from 13 ns to 20 ns in the ground-based profiles.

Data from the ground-based acquisition (Figure 8a), processed using the sequence above, revealed a sequence of sub-horizontal interfaces and a series of diffractions with a regularly spacing of 0.5-0.6 m intervals, rising from ~8 ns to ~6 ns travel-time through the profile. Although their origin is unknown, presumed to related to the original road foundation, they nonetheless provide targets for diffraction-based velocity analysis. Had more time been available, the acquisition of a small grid would have been valuable for ensuring that our main profile crossed the diffractions orthogonally.

A wide-angle reflection/refraction (WARR) survey (Diamanti et al., 2018; Figure 8b) was acquired to provide velocity control: the transmitter was located 6.90 m along the profile, with the receiver position moved in 0.05 m increments from 7.05 to 8.65 m (0.15-1.85 m offset range). The semblance response to the WARR data suggests a three-layer velocity model (inset, Figure 8b). On substituting corrected semblance picks (ornament ⊕) into Dix's Equation and extrapolating the resulting velocity model across the profile, the

deepest clear diffraction (position 1.35 m along the x-axis, marked with the red arrow) is interpreted to originate from the base of a layer at 0.33 ± 0.05 m depth, 0.11 ± 0.05 m thick, with $v_{sub} = 0.087 \pm 0.008$ m/ns. This v_{sub} is used as the reference velocity, against which velocity errors are later compared, although it is acknowledged that ground truth velocities and diffractor geometries are unknown.

6

7 Field Data Results

8 Recorded profiles are shown in Figure 9, displayed before (9a) and after (9b) the 9 application of spatial filtering. For $h \ge 0.1$ m (2 $\lambda/6$; 9aiii-vii), data are dominated by 10 horizontal ringing, assumed to be reverberations between the ground surface (marked in Figure 8b) and the base of the antennas. Perturbations in the travel-time of the surface 11 12 reflection suggest some inconsistency in the antennas' height, but these are typically < 0.2ns (< 0.03 m) and are small compared to the depth of the target. In any case, they may 13 14 represent the stability of a real drone platform. The reverberations are suppressed with the application of spatial filtering, but the subsurface structure remains greatly obscured for $h \ge 1$ 15 16 0.1 m (2 λ /6). For $h \ge 0.1$ m (1 λ), some expression of the subhorizontal layering appears 17 (e.g., at ~10 ns in Figure 8bvi) but the diffractions remain obscured, and the image would be 18 difficult to interpret without also seeing the ground-based data.

19 With the sparsity of available diffraction responses in the field data, velocity analysis 20 was only performed for the diffraction at 1.35 m along the profile, for ground-based 21 antennas and h = 0.05 m (Figures 10a and b, respectively). Semblance is calculated in a 0.1 22 ns window and spans an aperture of 0.25 m either side of the diffraction apex. As 23 anticipated, the air gap increases v_{RMS} . The 13% increase (from v_{RMS} of 0.0917 m/ns, to 0.104

1	m/ns) is approximately half of that suggested in Figure 6c for representative flight heights
2	but the characteristics of the real data are otherwise consistent with the FDTD synthetics.
3	The accuracy of v_{sub} estimates is compared against the reference model at 1.35 m
4	(Figure 8). For the ground-based data, v_{RMS} and t_0 through the overburden are 0.099 m/ns
5	and 4.4 ns respectively. Combining these in Dix's Equation with the quantities derived in
6	Figure 10a, v_{sub} is estimated as 0.077 ± 0.003 m/ns, within 13% of the model v_{sub} . For $h =$
7	0.05 m, the overburden v_{RMS} must first be recalculated to allow for propagation through the
8	air-gap. Using Equation (2), and assuming $t_{air} = 0.33$ ns (= $2h/v_{air}$), the [v_{RMS} : t_0] pair at the
9	base of the first subsurface layer is [0.127 m/ns, 4.77 ns]. Here, Dix's Equation yields an
10	implausibly slow v_{sub} estimate of 0.036 m/ns, although this is highly sensitive to uncertainty
11	ranges: when v_{RMS} is increased by 0.009 m/ns to its upper uncertainty bound, the implied
12	v_{sub} is increased to 0.085 m/ns. Dix's Equation is vulnerable to uncertainties particularly
13	where travel-time differences in the denominator of the expression are small. However, this
14	is exacerbated for drone-based surveying, where the addition of an air-gap adds further
15	measurement uncertainty to the analysis.

17 Discussion

Drone platforms offer logistical benefits for GPR surveying, but the imaging and analysis of diffraction hyperbolae is vulnerable to errors related to strong refraction effects at the air-ground interface. Recommendations for optimising drone flight-height are contradictory when made using different approaches: ray-based models suggest a 'fly high' strategy to minimise refraction but the more realistic FDTD approach, using a full waveform simulation, indicates that 'flying low' benefits both the precision and accuracy of velocity

1	estimates. Field data also suggest that a low flight height is preferable, although our dataset
2	does little to recommend drone-based diffraction imaging overall. Although data quality in
3	our lowest flight-height (0.05 m, λ /6) compared well with that from a conventional ground-
4	based acquisition, the obscurity of diffractions in the majority of profiles suggests that the
5	accuracy of diffraction-based velocity analysis may be of secondary importance to the
6	question of whether diffractions can be recognised at all.
7	
8	Limited Visibility of Real Data Diffractions
9	Two considerations may explain the limited visibility of diffractions in the real data.
10	First, Figure 5 showed that characteristic diffraction responses will flatten rapidly with
11	increasing flight-height, to the point where they may become indistinct from subhorizontal
12	reflectivity and, potentially, the reflection from the air-ground interface (marked where
13	visible in Figure 5). With reduced curvature, the diffraction is more vulnerable to further
14	travel-time perturbations related to (e.g.) microtopography on the air-ground interface
15	and/or small-scale velocity anomalies in the overburden. A further feature of our real data
16	was the strong reverberations in the air gap: these were suppressed using consistent spatial
17	filters that preferentially attenuated horizontal trends, hence it is possible that diffraction
18	amplitudes were also attenuated in this step.
19	The second consideration is the spatial resolution of the wavelet, expressed by its

20 Fresnel diameter, F_d ,

21 $F_d = v_{RMS} (2t_0 \tau)^{\frac{1}{2}}$,

17

(4)

1	where τ is the half-period of the dominant frequency (Lindsey, 1989). For a wavelet of any
2	given frequency, propagating for a fixed travel-time, spatial resolution will be poorer (i.e., F_d
3	increases) for increased v_{RMS} . For the synthetic results in Figure 6a, assuming τ = 0.5 ns and
4	flight-height increased from 0 m to 0.6 m, v_{RMS} increases from ~0.08 m/ns to 0.21 m/ns, and
5	t_0 from 6 ns to 11 ns. This leads F_d to increase from 0.2 m to 0.7 m. The expression of
6	diffracting targets may fundamentally change for drone-based antennas compared to the
7	same targets' appearance in a ground-based system. For our field dataset, the sequence of
8	closely-spaced discrete diffractions in Figure 9 may become the specular surface seen in our
9	highest flight-height.
10	
11	Measures to Improve Velocity Accuracy
12	In situations where diffraction hyperbolae can be resolved, the accuracy of the
13	implied velocity models must still be addressed. If interpretations are to be made using the
14	hyperbolic travel-time definition in Equation 1, we advise using a narrow aperture to
15	mitigate non-hyperbolic travel-time terms. However, the resulting improvement in accuracy
16	will be a compromise with velocity precision, since precision is superior when a target event
17	expresses greater travel-time moveout (Booth et al., 2011). Furthermore, this may impact
18	the application of automated detection algorithms (e.g., Dou et al., 2017) that rely on
19	consistent expressions of hyperbolae to be successful.
20	The compromise between accuracy and precision can be avoided using higher-order
21	definitions (e.g., Alkhalifah, 1997; Causse, 2004) of travel-time moveout. A fourth-order

1
$$t(x-x_0) \approx \sqrt{t_0^2 + \frac{4(x-x_0)^2}{v_{RMS}^2} + C(x-x_0)^4},$$
 (5)

2 based on the definition of Alkhalifah (1997), accumulates all non-hyperbolic travel-time 3 terms into parameter C. When applied to Figure 5avii ($h = 2\lambda$), the residual travel-time between the observed diffraction moveout and that defined by Equation 5 is minimsed for 4 5 v_{RMS} = 0.2018 m/ns, ~3% lower than the value (0.2075 m/ns) implied by the hyperbolic 6 travel-time definition. However, on using this v_{RMS} in Dix's Equation, the implied v_{sub} is 0.1133 m/ns, an overestimate of 60% in the model value of 0.079 m/ns. This result implies 7 8 that the degree of non-hyperbolic moveout may even be too severe for a fourth-order 9 travel-time definition, without further restriction to the analysis aperture. 10 The most accurate approaches to velocity analysis may therefore involve full waveform inversion (Jazayeri et al., 2018), or a migration velocity analysis routine (St. Clair 11 and Holbrook, 2017) that seeks to best focus diffraction responses. Although these are 12 beyond the scope of this study, we caution that they intrinsically rely on being able to 13 recognise diffraction features to begin with and, as shown in our field dataset, this may not 14

16

15

17 <mark>Outlook</mark>

Drone-based GPR applications merit further investigation, but imaging and/or quantitative use of diffractions may be limited to cases in which flight height is as close to the ground as practically possible. In other settings, the drone platform may be more promising, for example when used for imaging subhorizontal specular reflectivity since the near-vertical propagation of reflected energy will minimise refraction effects at the air-

routinely be the case for all but the lowest drone flight heights.

ground interface. Low frequency airborne radar methods are already well-established in 1 2 glaciology, and the drone-based platform may be less problematic in this setting given the 3 small refractive index at the air-snow/ice interface (e.g., Tan, 2018; Mankoff et al., 2020). However, since the degree of refraction across the ground surface is a frequency-4 5 independent effect, we expect that low frequency applications in more conventional 6 terrestrial settings will still be impacted by similar velocity errors. We would therefore 7 advise that a drone acquisition is therefore performed with a low flight height, and is 8 accompanied if possible by a ground-based survey both to benchmark any loss of image 9 quality and provide more reliable velocity control. 10 Conclusions 11 Drone technology offers logistical benefits for several geophysical survey methods, 12 and numerous researchers have explored its applicability for GPR acquisition. Established 13 14 guidance suggests that the optimal flight height for the antennas is between 0.5-1.5 times the GPR wavelength in air, but no study has to date assessed this recommendation for its 15 16 impact on diffraction-based velocity analysis. This impact is potentially significant, owing to

17 strong refraction effects at the air-ground interface

FDTD simulations suggest that velocity analyses are both more accurate and precise if the drone is flown as close to the ground surface as possible. Although this geometry risks stronger ray-bending, the effect of non-hyperbolic terms is minimised by the anisotropic radiation pattern of the GPR antenna. Furthermore, higher flight heights produce flatter diffraction trajectories, risking diffraction responses being overlooked and/or

23 indistinguishable from nearby subhorizontal reflectivity.

1	A field dataset simulating a drone-based acquisition highlights the vulnerability of
2	diffractions being overlooked. Antennas are raised to over 1 wavelength (0.3 m) from the
3	ground surface, yet diffractions are only visible in the lowest-flying dataset (0.05 m off the
4	ground). A combination of reverberation in the air-gap and a decrease in the horizontal
5	resolution of the wavelet likely explains this poor performance. We conclude that the drone
6	platform merits further investigation for GPR applications, including measures to improve
7	velocity accuracy, but suggest that it is currently more suitable for imaging specular
8	reflectivity than it is the quantitative analysis of diffraction responses.
9	
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10	
11	FIGURE CAPTIONS
12	
13	Figure 1. Raypaths modelled for a point diffractor, placed at 0.2 m depth in a subsurface
14	with constant v_{sub} = 0.09 m/ns. Each panel shows antennas (red circles) raised to
15	successively increased height, from 0 m to 0.9 m, and the vertical travel-time, t_{air} , through
16	the air-gap. The additional annotation in the lower-right panel shows the vertical travel-
17	time, 4.4 ns, between the diffractor and ground surface. A schematic representation of
18	Equation (1) is inset in the upper-left panel, accurate for ground-based antennas and
19	constant v _{sub} .

Figure 2. Ray-based travel-time curves for models in Figure 1. a) Curves for ground-based
(blue; *h* = 0) and airborne (red; *h* > 0) antennas. b) End-member curves from (a), compared

- to diffraction hyperbolae (black dashed lines) from a diffracting target placed at the ground
 surface. Each pair of curves is simply shifted by ~4.4 ns. c) Expression of curves in (a) on t²-x²
 axes and best-fit straight-lines (black dashed lines) for each.
- 4

5 Figure 3. Measured velocities and errors with changing flight-height. a) v_{RMS} measured from 6 t^2-x^2 analysis (solid, blue), and the estimated v_{sub} (dashed, green) after substitution into Dix's 7 Equation. b) Percentage overestimate of v_{sub} , with respect to model value of 0.09 m/ns. c-e) 8 Overestimates of a range of v_{sub} values for point diffractors at 0.2 m, 0.6 m and 1.0 m depth 9 respectively. Contours are filled at 10% intervals, with white contours appearing at intervals 10 of 2% within the 0-10% range. The pink dashed line in (c) corresponds to the data in (b). Throughout, wavelength annotations are made to facilitate comparison with later FDTD 11 synthetics. 12

13

Figure 4. [x,z] cross-section through the gprMax model. A cylindrical perfect electric conductor (pec) is placed at 0.15 m depth in a subsurface with fixed electrical conductivity ($\sigma = 1 \text{ mS/m}$) but variable v_{sub} . Antennas (red circles) span a range of x from 0.05 m to 0.95 m, and are positioned at h up to 0.6 m (0-2 λ).

18

Figure 5. Synthetic radargrams and semblance responses for v_{sub} of a) 0.07 m/ns and b) 0.13
m/ns, and h increased (i to vii) from 0 m to 0.6 m. The hyperbola in each radargram
approximates first-break travel-times using semblance picks corrected (ornament ⊕) from
peak responses (ornament ⊗). Orange dashed line in models with h > 0.15 m shows the

- reflection from the air-ground interface. All radargram and semblance panels share the
 same colour scale and amplitude range.
- 3

Figure 6. Semblance-derived v_{RMS} and v_{sub} for the models in Figure 5. Coloured areas show
velocity estimates and their precision for (blue) v_{RMS} and (green) modified v_{sub} of (a,b) 0.079
m/ns and (c,d) 0.134 m/ns. Pink areas in b and d show the percentage overestimate in
model v_{sub}, with black lines showing the equivalent errors from ray-based models in Figure
3c.

9

Figure 7. Field data acquisition. a) 1000 MHz centre frequency antennas placed within a
polystyrene frame, to simulate drone-mounted GPR surveys. Inset, markers to simulate
different flight-heights. b) Survey location on Canal Road, Rodley, UK. Upper: view southeast along Canal Road and the position of 20 m-long profiles. Lower: Site map from UK
Ordnance Survey showing Canal Road and its proximity to the Leeds-Liverpool canal and a
defunct wharf. Viewpoint for upper panel is marked.

16

Figure 8. Ground-based GPR data from Canal Road surveys. a) First 10 m of ground-based GPR profile. A diffraction at 1.35 m position, at ~7 ns travel-time, beneath subhorizontal layering (depth ~0.33 m) is highlighted for later analysis. b) WARR data, spanning a midpoint range of 7.0 m to 7.8 m, and its semblance response. Reflection hyperbolae (red) are defined by [v_{RMS} : t_0] shown by ornament \oplus in the semblance panel. Inset: three-layer velocity:thickness model, accurate to ~ ±15%, based on the 90% semblance contour.

2	Figure 9. GPR Profiles from Canal Road survey, with <i>h</i> increased from (i) 0 m to (viii) 0.35 m
3	(= 7 λ /6). Data are shown (a) before and (b) after the application of spatial filtering. Red
4	boxes show the indication of subhorizontal layering for large h, and orange annotations
5	highlight the reflection from the ground surface at the heights that it could be resolved from
6	the direct air wave.

8	Figure 10. Semblance analysis of diffraction highlighted in Figure 8, for a) ground-based
9	antennas and b) antennas at $h = 0.05$ m. Diffraction hyperbolae (red) are defined by [v_{RMS} : t_0]
10	shown by ornament \oplus in the semblance panels, across the 0.25 m aperture either side of
11	the diffraction apex. Annotated velocity precision is based on the width of the 90%
12	semblance contour.