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# Partial Power Processing Multiport DC-DC Converter with Radial Module Connections 

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#### Abstract

The partial power processing (PPP) concept has been extensively employed in many two-port converters to achieve high efficiency and high power density by modifying one of the original converter ports to be connected in series between input and output. This is attractive but is confined to two-port applications, and how to extend it to multiport applications is not clear. Hence, this paper aims to explore a generalized PPP multiport scheme by arranging the connection of the module rather than the converter. For a PPP single-input(output)- N -outputs(inputs) converter, one terminal of all $\mathrm{N}+1$ modules is connected together to construct a radial structure, and another terminal is series/parallel connected with the input/output port. Each module only needs to process partial power caused by the voltage or current difference between input and output. Therefore, the required power rating of components is effectively reduced, contributing to low cost as well as low power loss. In this paper, a PPP single-input dual-output converter with active bridge modules is also taken as an example to be introduced in detail, designed and experimented upon, which validates that high efficiency and high power density can be achieved.


Index Terms- Partial power processing, multiport DC-DC, radial module connection, active bridge.

## I. Introduction

THE concept of partial power processing (PPP) has been proposed to improve the overall efficiency and power density of DC-DC converters and was firstly applied in photovoltaic (PV) power systems [1]. When transmitting power from the PV array to the battery bank, one port of the utilized two-port DC-DC converter is changed to be connected in series between them. Therefore, only the partial power caused by the voltage difference is processed through the converter, while the other power is transferred directly. Assuming that the efficiencies of the two-port DC-DC converter and the direct transmission are $\eta_{1}\left(\eta_{1}<100 \%\right)$ and $\eta_{2}\left(\eta_{2}=100 \%\right)$, respectively, the total efficiency of the conversion must be larger than $\eta_{1}$. Therefore, the global efficiency of PPP is successfully improved when compared with the traditional method of

[^0]processing the full power through the DC-DC converter. Moreover, because the DC-DC converter in the PPP system only processes a small part of the total power, its current and voltage stresses are correspondingly reduced, contributing to decreased cost and increased power density. Owing to these advantages, PPP two-port structures attract increasing attention, and they are already promoted to applications, such as space power systems [2, 3], wind turbines [4, 5], electric vehicles [6] and so on [7].

Two typical PPP two-port structures produced by changing the connection scheme of traditional isolated two-port DC-DC converters are proposed in [8], including the input-parallel-output-series structure and the input-series-output-parallel structure, which are named structure Type I and structure Type II, respectively [9], as shown in Fig. 1. From Fig. 1(a), node $a_{1}$ is connected to node $d_{1}$; therefore, port $c_{1} d_{1}$ is in series connection between the input port and output port, and port $a_{1} b_{1}$ is in parallel with input port $V_{i}$. Similarly, node $b_{2}$ is connected to node $c_{2}$ in Fig. 1(b), constructing the ISOP structure. In these structures, only the partial power generated by the voltage difference between $V_{i}$ and $V_{o}$ is processed by the DC-DC converter, while the other power is transmitted through the direct power delivery path. Accordingly, the ratio of the partial power $P_{p}$ to the total power $P_{t}$ is $\left(V_{o}-V_{i}\right) / V_{o}$ or $\left(V_{o}-V_{i}\right) / V_{i}$. In addition, the voltage and current stresses of the DC-DC converter in the PPP structure are relatively reduced when compared with the full power processing approach. The smaller the difference between port voltages $V_{i}$ and $V_{o}$, the higher the efficiency and the greater the power density. On the other hand, $V_{i}$ is smaller than $V_{o}$ in both Fig. 1(a) and Fig. 1(b) if the polarities of ports $c_{1} d_{1}$ and $a_{2} b_{2}$ are positive, while the stepdown voltage gain will be obtained if their polarities are reversed [10].

(a)

(b)

Fig. 1 Typical PPP two-port structures: (a) Type I and (b) Type II ${ }^{[9]}$.
Based on these two structures, a variety of PPP two-port converters have been explored by using different isolated DCDC converters, such as push-pull converters [11], phase-shifted full/half-bridge converters [12-15], flyback converters [16, 17], LLC converters [18], dual-active bridge (DAB) converter [19], and so on [20]. The topologies in [11-13] are able to realize
voltage step-down, while voltage step-up is achieved in [14-20]. Nevertheless, because the port voltage polarities of these isolated DC-DC converters are fixed, the derived PPP two-port topologies are unable to realize buck-boost voltage gain. To obtain a more flexible voltage relationship, two methods for realizing buck-boost are proposed in [21-24]. The first one adds additional switches in series with diodes such that both boost mode and buck mode can be obtained [21, 22]. The other one employs an H -bridge to change the output voltage polarity of the full power isolated DC-DC converter [23, 24]. However, the added switches increase the conduction loss as well as the cost.

In addition to two-port applications, two PPP three-port converters have also been proposed in [25, 26]. In [25], an isolated Sepic converter was activated to realize PPP from the supercapacitor to the output when the output load current exceeded the threshold value. In [26], a PPP three-port converter with a reduced number of components was employed to transfer power from the battery and PV modules to the output load. Nevertheless, a specific architecture and converter were used in [25, 26], which makes it difficult to help discover more possible solutions for multiport applications.

From the above, the existing PPP research mainly focuses on two-port applications, and two general structures have been presented. On the other hand, although two PPP three-port converters were proposed, the general architecture of the PPP multiport converter is still lacking. Therefore, this paper proposes a generalized PPP single-input(output)-Noutputs(inputs) DC-DC architecture with radial module connections to expand PPP from two ports to multiple ports. Rather than changing the connection scheme based on the original DC-DC converter, N outputs (inputs) are connected radially via respective series connected modules to a center point, which is also connected with the positive pole of the single input (output). An N+1 module is also parallelly connected with the single input (output). In this radial structure, only the partial power generated by voltage or current differences between input and output will be supplied and transmitted through modules, while the other power is directly delivered. Therefore, the high efficiency is achieved, and the power density is improved with reduced voltage and current stresses of the components. In addition, modules can be replaced by a variety of multiport DC-DC converters to achieve partial power conversion. The possible choices can be a threeport Flyback converter [27], a three-port bidirectional Cuk converter [28], a multi-active bridge converter [29] and other multi-winding transformer-based DC-DC converters [30]. Due to the characteristics above, in addition to the applications mentioned for PPP two-port structures, the proposed PPP multiport structure is also suitable for other high-power multiport applications, such as DC microgrid.

In the rest of the paper, the proposed PPP multiport DC-DC architecture with radial module connections is first introduced in section II. Subsequently, a detailed analysis of an example active bridge module-based PPP single-input dual-output (SIDO) DC-DC converter is conducted in section III. In section IV, the corresponding characteristic analysis and design consideration are illustrated, followed by the experimental
results of the prototype circuit in section V. Finally, the conclusions are drawn in section VI.

## II. The Proposed PPP Multiport DC-DC Architecture with Radial Module Connections

The proposed PPP multiport DC-DC architecture is shown in Fig. 2, including the single-input multi-output (SIMO) architecture in Fig. 2 (a) and the multi-input single-output (MISO) architecture in Fig. 2(b). N+1 magnetically linked modules are employed for $\mathrm{N}+1$ ports. From Fig. 2, one terminal of all modules $M_{1} \sim M_{\mathrm{N}+1}$ is connected to a center point, constructing a radial architecture. The other terminals of modules $M_{1} \sim M_{\mathrm{N}}$ are connected to the positive pole of outputs(inputs) $V_{o 1} \sim V_{o \mathrm{~N}}\left(V_{i 1} \sim V_{i \mathrm{~N}}\right)$. In addition, module $M_{\mathrm{N}+1}$ is in parallel with the single input(output) $V_{i 1}\left(V_{o 1}\right)$. All input and output share a common ground. In this radial structure, the number of outputs in Fig. 2(a) and inputs in Fig. 2(b) can be flexibly added or reduced, and the types of modules are diverse. Moreover, the output(input) voltage $V_{o(i) k}(k=1,2, \ldots, \mathrm{~N})$ can be designed to be greater or smaller than the single input(output) voltage $V_{i 1}\left(V_{o 1}\right)$ by adjusting the polarity of the module voltage $V_{k}(k=1,2, \ldots, \mathrm{~N})$. In addition, only a part of the system power is processed through modules, contributing to high efficiency and high power density.


Fig. 2 The proposed PPP DC-DC architecture with radial module connections: (a) SIMO and (b) MISO.

Take Fig. 2 (a) as an example to explain the favorable PPP merit of the proposed architecture. The currents of the modules,
output ports and input port are defined as $I_{1} \sim I_{\mathrm{N}+1}, I_{o 1} \sim I_{o \mathrm{~N}}$ and $I_{i 1}$, respectively. The power processed by module $M_{k}(k=1,2, \ldots, \mathrm{~N})$ is calculated in (1). When $V_{o k}<V_{i 1}, P_{k}$ flows out of the module. In contrast, $P_{k}$ flows into the module when $V_{o k}>V_{i 1}$. In addition, $P_{k}$ is decreased with the output voltage $V_{o k}$ approximating the input voltage $V_{i 1}$. Therefore, if the values of $V_{o k}$ and $V_{i 1}$ are similar, the required processing power of module $M_{k}$ is small, and under this condition, the sum of output currents $I_{o 1} \sim I_{o \mathrm{~N}}$ is also near the input current $I_{i 1}$ according to the power balance principle. Hence, the power processed by module $M_{\mathrm{N}+1}$ is also small, as shown in (1). With different load conditions, $P_{\mathrm{N}+1}$ is bidirectional. The ratio of the module power $P_{p}$ to the total system power $P_{t}$ is calculated in (2) by using absolute values. According to (2), the power ratio $P_{p} / P_{t}$ changing with output currents $I_{o 1}$ and $I_{o 2}$ is demonstrated in Fig. 3, where the per-unit current is set as 2.5 A with example system parameters $V_{i 1}=400 \mathrm{~V}, V_{o 1}=320 \mathrm{~V}$ and $V_{o 2}=480 \mathrm{~V}$. The maximum value 0.25 is achieved for $P_{p} / P_{t}$ when $I_{o 2}=0 \mathrm{~A}$, which is much smaller than 1. Moreover, a minimum value of 0.1 is obtained when ( $V_{i 1^{-}}$ $\left.V_{o 1}\right) \times I_{o 1}$ equals $\left(V_{o 2}-V_{i 1}\right) \times I_{o 2}$. Therefore, only a small part of the power needs to be processed by modules $M_{1} \sim M_{\mathrm{N}+1}$, especially when the difference between the input voltage and output voltage is small. Consequently, the voltage or current stresses of the components in these modules are successfully reduced, contributing to low cost and high power density.

$$
\begin{gather*}
\left\{\begin{array}{l}
P_{k}=V_{k} I_{k}=\left(V_{i 1}-V_{o k}\right) I_{o k}, k=1,2 \ldots, N \\
P_{N+1}=V_{N+1} I_{N+1}=V_{i 1}\left(I_{i 1}-\sum_{k=1}^{N} I_{o k}\right) \\
P_{t}
\end{array} \sum_{k=1}^{\sum_{k}^{N}\left|P_{k}\right|+\left|P_{N+1}\right|}=\frac{\sum_{k=1}^{N}\left|V_{i 1}-V_{o k}\right| I_{o k}+V_{i 1}\left|I_{i 1}-\sum_{k=1}^{N} I_{o k}\right|}{2 V_{i 1} I_{i 1}}\right. \tag{1}
\end{gather*}
$$

Fig. 3 The relationship among output currents $I_{o 1}, I_{o 2}$ and the power ratio $P_{p} / P_{t}$.
Due to the PPP ability, the efficiency of the proposed multiport architecture will also be high. Define the power transmission efficiency of the modules and the PPP converter as $\eta_{p}$ and $\eta_{t}$, respectively. Because only the partial power is processed by modules, while the other is delivered directly through wire with near $100 \%$ efficiency, the total efficiency $\eta_{t}$ are calculated in (3). From (3), $\eta_{t}$ is always larger than $\eta_{p}$ since $P_{p}$ is smaller than $P_{t}$. Moreover, the smaller the ratio $P_{p}$ to $P_{t}$ is, the higher the global efficiency $\eta_{t}$ that can be attained.

$$
\begin{equation*}
\eta_{t}=\frac{P_{p} \eta_{p}+P_{t}-P_{p}}{P_{t}}=\eta_{p}+\frac{\left(P_{t}-P_{p}\right)\left(1-\eta_{p}\right)}{P_{t}}>\eta_{p} \tag{3}
\end{equation*}
$$

## III. Operational Principle of an Example Active bridge MODULE-BASED PPP-SIDO DC-DC CONVERTER

To better understand the operation principle of the proposed PPP multiport DC-DC architecture with radial module connections in Fig. 2, a SIDO example with three active bridge modules $M_{1} \sim M_{3}$ as in Fig. 4 will be introduced in detail. It has an input port $V_{i 1}$, two output ports $V_{o 1} \sim V_{o 2}$, and it is assumed


Fig. 4 Circuit diagram of the proposed active bridge module-based PPP-SIDO DC-DC converter.
that $V_{o 1}<V_{i 1}<V_{o 2}$. Each module $M_{i}(i=1,2,3)$ consists of four switches $S_{i 1} \sim S_{i 4}(i=1,2,3)$, an inductor $L_{i}(i=1,2,3)$ and a winding of the transformer with turn numbers $N_{i}(i=1,2,3) . M_{1}$ and $M_{2}$ are connected in series, and $M_{3}$ is connected in parallel with $V_{i 1}$. In addition, the positive terminal of $M_{1}$ and the negative terminal of $M_{2}$ are connected to the positive terminal of $M_{3}$. Owing to this structure, only a small partial power $P_{1} \sim P_{3}$ is converted through modules $M_{1} \sim M_{3}$, while the other large part of the power is delivered directly from $V_{i 1}$ to $V_{o 1}$ and $V_{o 2}$.

From Fig. 4, the structure of the three-winding transformer with series inductors is depicted in Fig. 5(a). To conveniently calculate the inductor voltage $v_{L i}(i=1,2,3)$, the corresponding star-equivalent transformation is given in Fig. 5(b) [31], where $v^{\prime}{ }_{2}=v_{2} \times N_{1} / N_{2}, v^{\prime}=v_{3} \times N_{1} / N_{3}, L^{\prime}{ }_{2}=L_{2} \times N_{1}{ }^{2} / N_{2}{ }^{2}$ and $L_{3}^{\prime}=L_{3} \times N_{1}{ }^{2} / N_{3}{ }^{2}$, which represent the primary referred values of voltages $v_{2}$ and $v_{3}$, and the inductances $L_{2}$ and $L_{3}$, respectively. Based on Fig. 5(b) and the superposition theorem, the voltages $u_{i}(t)(i=1,2,3)$ are calculated in (4), where the voltage $v_{i}(t)(i=1,2,3)$ is decided by switch modes, as shown in (5). When switch $S_{i 1}$ is turned on, $v_{i}(t)=V_{i}$, while $v_{i}(t)=-V_{i}$ when $S_{i 1}$ is turned off. According to (4) and (5), the inductor voltages $v_{L i}(t)=v_{i}(t)$ $u_{i}(t)(i=1,2,3)$ are finally calculated in (6).

(a)

(b)

Fig. 5 The structure of a three-winding transformer with series inductors: (a) the re-depicted structure and (b) its star-equivalent model ${ }^{[31]}$.

$$
\begin{gather*}
{\left[\begin{array}{l}
u_{1}(t) \\
u_{2}(t) \\
u_{3}(t)
\end{array}\right]=\left[\begin{array}{ccc}
m_{1} & m_{2} N_{12} & m_{2} N_{13} \\
m_{1} N_{21} & m_{2} & m_{3} N_{23} \\
m_{1} N_{31} & m_{2} N_{32} & m_{3}
\end{array}\right]\left[\begin{array}{l}
v_{1}(t) \\
v_{2}(t) \\
v_{3}(t)
\end{array}\right]}  \tag{4}\\
\text { where } m_{1}=\frac{L_{2}^{\prime} L_{3}^{\prime} /\left(L_{2}^{\prime}+L_{3}^{\prime}\right)}{L_{1}+L_{2}^{\prime} L_{3}^{\prime} /\left(L_{2}^{\prime}+L_{3}^{\prime}\right)}, m_{2}=\frac{L_{1} L_{3}^{\prime} /\left(L_{1}+L_{3}^{\prime}\right)}{L_{2}+L_{1} L_{3}^{\prime} /\left(L_{1}+L_{3}^{\prime}\right)}, \\
m_{3}=\frac{L_{1} L_{2}^{\prime} /\left(L_{1}+L_{2}^{\prime}\right)}{L_{3}+L_{1} L_{2}^{\prime} /\left(L_{1}+L_{2}^{\prime}\right)} \text { and } N_{x y}=N_{x} / N_{y},(x, y=1,2,3) \\
\qquad\left\{\begin{array}{l}
v_{i}(t)=q_{i}(t) \times V_{i}, i=1,2,3 \\
q_{i}(t)=\left\{\begin{array}{c}
1, S_{i 1}=\text { on } \\
-1, S_{i 1}=o f f
\end{array}\right. \\
v_{L i}(t)=q_{i}(t) V_{i}-\sum_{k=1}^{3} \frac{N_{i}}{N_{k}} m_{k} q_{k}(t) V_{k},(i=1,2,3)
\end{array}\right. \tag{5}
\end{gather*}
$$

The key operation waveforms of the active bridge modulebased PPP-SIDO DC-DC converter are shown in Fig. 6. The drive signals of switches $S_{i 1} \sim S_{i 4}(i=1,2,3)$ are $v_{g s i 1} \sim v_{g s i 4}(i=1,2$, 3), respectively, as shown in Fig. 6. $S_{i 1}$ and $S_{i 2}$ are switched synchronously, as are $S_{i 3}$ and $S_{i 4}$. Moreover, $S_{i 1}$ and $S_{i 3}$ are activated in complementary fashion with a 0.5 duty cycle. The phase shift angles of $v_{g s 21}$ and $v_{g s 31}$ with respect to $v_{g s 11}$ are defined as $\varphi_{12}$ and $\varphi_{13}$, respectively. The phase shift angles $\varphi_{12}$ and $\varphi_{13}$ in radians are employed to regulate the power flows among the three modules $M_{1} \sim M_{3}$.


Fig. 6 Key operation waveforms of the proposed active bridge module-based PPP-SIDO DC-DC converter.

From Fig. 6, the half switching period $T_{s} / 2$ of $v_{g s 11}$ can be divided into six states $\left(t_{0} \sim t_{6}\right)$ with phase shift relationships $\pi / 2>\varphi_{12}>\varphi_{13}>0$. The corresponding values of $q_{i}(t)(i=1,2,3)$ in different states are given in TABLE I and the equivalent circuits of six states $\left(t_{0} \sim t_{6}\right)$ are also shown in Fig. 7. In addition, assume $N_{1}: N_{2}: N_{3}=V_{1}: V_{2}: V_{3}$ and $N_{1}{ }^{2}: N_{2}{ }^{2}: N_{3}{ }^{2}=L_{1}: L_{2}: L_{3}$ so that $m_{1} \sim m_{3}$ in (6) are all equal to $1 / 3$, which largely simplifies the calculation and analysis.

TABLE I


Fig. 7 The equivalent circuits of six states $t_{0}-t_{6}$.
State $1\left(t_{0} \sim t_{1}\right): S_{11}$ and $S_{12}$ are turned on at $t_{0}$. In addition, $S_{23}$, $S_{24,} S_{33}$ and $S_{34}$ also remain conducting in this state. According to (6) and TABLE I, the three inductor voltages are $v_{L 1}=4 \times V_{1} / 3$, $v_{L 2}=-2 \times V_{2} / 3$ and $v_{L 3}=-2 \times V_{3} / 3$. Hence, the inductor current $i_{L 1}$ increases, while $i_{L 2}$ and $i_{L 3}$ decrease linearly, as calculated in (7). Accordingly, $V_{i 1}$ charges $V_{o 1}, V_{o 2}$ and $L_{1}$ at the same time, while inductors $L_{2}$ and $L_{3}$ are discharged.

$$
\left\{\begin{array}{l}
i_{L 1}(t)=i_{L 1}\left(t_{0}\right)+\frac{4}{3} \cdot \frac{V_{1}}{L_{1}}\left(t-t_{0}\right)  \tag{7}\\
i_{L 2}(t)=i_{L 2}\left(t_{0}\right)-\frac{2}{3} \cdot \frac{V_{2}}{L_{2}}\left(t-t_{0}\right) \\
i_{L 3}(t)=i_{L 3}\left(t_{0}\right)-\frac{2}{3} \cdot \frac{V_{3}}{L_{3}}\left(t-t_{0}\right)
\end{array}\right.
$$

State $2\left(t_{1} \sim t_{2}\right): S_{33}$ and $S_{34}$ are turned off at $t_{1}$. Subsequently, the inductor $L_{3}$ starts to resonate with the parasitic capacitors $C_{s 31} \sim C_{s 34}$ of switches $S_{31} \sim S_{34}$, as illustrated in (8), where the drain-to-source voltages $v_{s 31}(t)$ and $v_{s 32}(t)$ are decreased.

$$
\left\{\begin{array}{l}
\left(C_{s 31}+C_{s 34}\right) \frac{d v_{s 31}(t)}{d t}=\left(C_{s 32}+C_{s 33}\right) \frac{d v_{s 32}(t)}{d t}=i_{L 3}(t)  \tag{8}\\
-L_{3} \frac{d i_{L 3}(t)}{d t}=v_{s 31}(t)+v_{s 32}(t)+u_{3}(t)-V_{3}
\end{array}\right.
$$

State $3\left(t_{2} \sim t_{3}\right)$ : After discharging of $C_{s 31}$ and $C_{s 32}$, the body diodes of switches $S_{31}$ and $S_{32}$ conduct; thereby, their drain-tosource voltages are clamped to zero. Switches $S_{31}$ and $S_{32}$ are turned on at $t_{2}$, which indicates that zero-voltage-switching (ZVS) turn-on is achieved. In this state, $v_{L 1}=2 \times V_{1} / 3, v_{L 2}=-$ $4 \times V_{2} / 3$ and $v_{L 3}=2 \times V_{3} / 3$. The corresponding inductor currents are given in (9). Therefore, $V_{o 1}, V_{o 2}, L_{1}$ and $L_{3}$ are charged by $V_{i 1}$, while $L_{2}$ is discharged.

$$
\left\{\begin{array}{l}
i_{L 1}(t)=i_{L 1}\left(t_{0}\right)+\frac{4}{3} \cdot \frac{V_{1}}{L_{1}} \cdot \frac{\varphi_{13}}{2 \pi} \cdot T_{s}+\frac{2}{3} \cdot \frac{V_{1}}{L_{1}}\left(t-t_{1}\right)  \tag{9}\\
i_{L 2}(t)=i_{L 2}\left(t_{0}\right)-\frac{2}{3} \cdot \frac{V_{2}}{L_{2}} \cdot \frac{\varphi_{13}}{2 \pi} \cdot T_{s}-\frac{4}{3} \cdot \frac{V_{2}}{L_{2}}\left(t-t_{1}\right) \\
i_{L 3}(t)=i_{L 3}\left(t_{0}\right)-\frac{2}{3} \cdot \frac{V_{3}}{L_{3}} \cdot \frac{\varphi_{13}}{2 \pi} \cdot T_{s}+\frac{2}{3} \cdot \frac{V_{3}}{L_{3}}\left(t-t_{1}\right)
\end{array}\right.
$$

State $4\left(t_{3} \sim t_{4}\right): S_{23}$ and $S_{24}$ are turned off at $t_{3}$, and the resonance among inductor $L_{2}$ and parasitic capacitors $C_{s 21} \sim C_{s 24}$ begins. The resonance formula is depicted in (10), where $C_{s 21}$ and $C_{s 22}$ are discharged, while $C_{s 23}$ and $C_{s 24}$ are charged.

$$
\left\{\begin{array}{l}
\left(C_{s 21}+C_{s 24}\right) \frac{d v_{s 21}(t)}{d t}=\left(C_{s 22}+C_{s 23}\right) \frac{d v_{s 22}(t)}{d t}=i_{L 2}(t)  \tag{10}\\
-L_{2} \frac{d i_{L 2}(t)}{d t}=v_{s 21}(t)+v_{s 22}(t)+u_{2}(t)-V_{2}
\end{array}\right.
$$

State $5\left(t_{4} \sim t_{5}\right)$ : When $v_{s 21}(t)$ and $v_{s 22}(t)$ drop to zero, the corresponding body diodes conduct; therefore, these two drain-to-source voltages are clamped to zero before $t_{4}$. ZVS turn-on of switches $S_{21}$ and $S_{22}$ is realized when they are turned on at $t_{4}$. Subsequently, the inductor voltages are all changed to zero such that their inductor currents are constant, as shown in (11). In this state, $V_{i 1}$ only charges $V_{o 1}$ and $V_{o 2}$.

$$
\left\{\begin{array}{l}
i_{L 1}(t)=i_{L 1}\left(t_{0}\right)+\frac{4}{3} \cdot \frac{V_{1}}{L_{1}} \cdot \frac{\varphi_{13}}{2 \pi} \cdot T_{s}+\frac{2}{3} \cdot \frac{V_{1}}{L_{1}} \frac{\left(\varphi_{12}-\varphi_{13}\right)}{2 \pi} \cdot T_{s}  \tag{11}\\
i_{L 2}(t)=i_{L 2}\left(t_{0}\right)-\frac{2}{3} \cdot \frac{V_{2}}{L_{2}} \cdot \frac{\varphi_{13}}{2 \pi} \cdot T_{s}-\frac{4}{3} \cdot \frac{V_{2}}{L_{2}} \frac{\left(\varphi_{12}-\varphi_{13}\right)}{2 \pi} \cdot T_{s} \\
i_{L 3}(t)=i_{L 3}\left(t_{0}\right)-\frac{2}{3} \cdot \frac{V_{3}}{L_{3}} \cdot \frac{\varphi_{13}}{2 \pi} \cdot T_{s}+\frac{2}{3} \cdot \frac{V_{3}}{L_{3}} \frac{\left(\varphi_{12}-\varphi_{13}\right)}{2 \pi} \cdot T_{s}
\end{array}\right.
$$

State $6\left(t_{5} \sim t_{6}\right): S_{11}$ and $S_{12}$ are turned off at $t_{5}$. Parasitic capacitors $C_{s 11}$ and $C_{s 12}$ are charged during resonance, as calculated in (12). Because $C_{s 11}$ and $C_{s 12}$ are charged, the drain-to-source voltages $v_{s 11}(t)$ and $v_{s 12}(t)$ are increased. When $v_{g s 13}$ and $v_{g s 14}$ turn positive at $t_{6}$, the half switching period ends.

$$
\left\{\begin{array}{l}
\left(C_{s 11}+C_{s 14}\right) \frac{d v_{s 13}(t)}{d t}=\left(C_{s 12}+C_{s 13}\right) \frac{d v_{s 14}(t)}{d t}=-i_{L 1}(t)  \tag{12}\\
L_{1} \frac{d i_{L 1}(t)}{d t}=v_{s 13}(t)+v_{s 14}(t)-u_{1}(t)-V_{1}
\end{array}\right.
$$

## IV. Characteristic Analysis and Design Consideration

Based on the operational principle of the proposed active bridge module-based PPP-SIDO DC-DC converter, the characteristics analysis and design considerations are introduced in this section with the system parameters in TABLE II. Part A calculates the active and non-active power flows

TABLE II
SYSTEM PARAMETERS

| Parameter | Value | Parameter | Value |
| :---: | :---: | :---: | :---: |
| Input Voltage $V_{i 1}$ | 400 V | Output Current $I_{o 1, \text { max }}$ | 2.5 A |
| Output Voltage $V_{o 1}$ | 320 V | Output Current $I_{o 2, \max }$ | 2.5 A |
| Output Voltage $V_{o 2}$ | 480 V | Turns Ratio $N_{1}: N_{2}: N_{3}$ | $1: 1: 5$ |
| Switching Period $T_{s}$ | $10 \mu \mathrm{~s}$ | Series Inductance | $1: 1: 25$ |

based on three active bridge modules. Part B concentrates on partial power flow analysis of the proposed structure. Subsequently, hardware design considerations will be given in Part C based on voltage and current stresses, working areas, and ZVS operation. In addition, small signal modeling and control design are depicted in Part D. Finally, the comparison is made in Part $E$ among the typical triple active bridge (TAB) converter [31, 32], an existing three-port PPP converter based on TAB [33] and the proposed example active bridge modulebased PPP-SIDO converter. The characteristics of the proposed converter are also summarized.

## A. Active and Non-active Power Flow Calculation

The three active bridge modules in the proposed example PPP-SIDO converter construct a TAB converter. From [31, 32], active power flows $P_{1}, P_{2}$ and $P_{3}$ of the three modules are calculated in (13), where $P_{12}, P_{13}$ and $P_{23}$ are virtual power flows according to the triangle-equivalent model, as shown in Fig. 8. Based on (13), (14) and the system parameters in TABLE II, phase shift angles $\phi_{12}$ and $\phi_{13}$ under different $I_{o 1}$ and $I_{o 2}$ are illustrated in Fig. 9, where $\phi_{12}$ and $\phi_{13}$ are the angles corresponding to radians $\varphi_{12}$ and $\varphi_{13}$. Therefore, the power flows of the proposed active bridge module-based PPP-SIDO DC-DC converter can be effectively controlled by phase shift angles $\varphi_{12}$ and $\varphi_{13}$.


Fig. 8 Triangle-equivalent model ${ }^{[31]} \overline{\text { of }}$ the three-winding transformer with series inductors in Fig. 5.

$$
\begin{align*}
& \left\{\begin{array}{l}
P_{1}=P_{12}+P_{13}=I_{o 1}\left(V_{i 1}-V_{o 1}\right) \\
P_{2}=P_{21}+P_{23}=I_{o 2}\left(V_{i 1}-V_{o 2}\right) \\
P_{3}=P_{31}+P_{32}=-P_{1}-P_{2}
\end{array}\right.  \tag{13}\\
& \left\{\begin{array}{l}
P_{12}=-P_{21}=\frac{V_{1} V_{2} N_{1}}{N_{2} \omega L_{12}} \varphi_{12}\left(1-\frac{\left|\varphi_{12}\right|}{\pi}\right) \\
P_{13}=-P_{31}=\frac{V_{1} V_{3} N_{1}}{N_{3} \omega L_{13}} \varphi_{13}\left(1-\frac{\left|\varphi_{13}\right|}{\pi}\right)
\end{array}\right.  \tag{14}\\
& P_{23}=-P_{32}=\frac{V_{2} V_{3} N_{1}^{2}}{N_{2} N_{3} \omega L_{23}}\left(\varphi_{13}-\varphi_{12}\right)\left(1-\frac{\left|\varphi_{13}-\varphi_{12}\right|}{\pi}\right) \\
& \text { where } \omega_{s}=2 \pi / T_{s} \text { and }\left\{\begin{array}{l}
L_{12}=L_{1}+L_{2}^{\prime}+L_{L} L_{2}^{\prime} / L_{3}^{\prime} \\
L_{13}=L_{1}+L_{3}^{\prime}+L_{1} L_{3}^{\prime} / L_{2}^{\prime} \\
L_{23}=L_{2}^{\prime}+L_{3}^{\prime}+L_{2}^{\prime} L_{3}^{\prime} / L_{L}
\end{array}\right. \text {. } \\
& L_{23}=L_{2}^{\prime}+\dot{L}_{3}^{\prime}+L_{2}^{\prime} L_{3}^{\prime} / L_{1}
\end{align*}
$$



Fig. 9 Graph showing the change of phase shift angles $\phi_{12}, \phi_{13}$ with loads $I_{o 1}, I_{o 2}$.
In addition to the active power $P_{1} \sim P_{3}$ calculated in (13), the non-active power is also considered. Owing to the square waveforms of $v_{1}(t), v_{2}^{\prime}(t)$ and $v^{\prime}{ }_{3}(t)$ in Fig. 8, they can be transformed universally based on a Fourier series [34], as shown in (15). Subsequently, we can obtain the equivalent inductor currents $i_{L 12}(t), i_{L 13}(t)$ and $i_{L 23}(t)$ in (16). Considering the symmetry of TAB in one switching cycle, the average current of the inductors over one switching period should be zero in the steady state, and we have formula (17). According to (15), (16) and (17), the Fourier series expression of the inductor currents is derived in (18). The expressions of the port currents $i_{1}(t), i_{2}(t)$ and $i_{3}(t)$ are given in (19). Afterward, the average power, i.e., the active power $P_{i}(i=1,2,3)$ of three

$$
\begin{align*}
& \left\{\begin{array}{l}
v_{1}(t)=\sum_{n=1,3,5 \ldots \ldots} \frac{4 V_{1}}{n \pi} \cdot \sin \left(n \omega_{s} t\right) \\
v_{2}^{\prime}(t)=\sum_{n=1,3,5 \ldots \ldots} \frac{4 V_{2}^{\prime}}{n \pi} \cdot \sin \left(n\left(\omega_{s} t-\varphi_{12}\right)\right) \\
v_{3}^{\prime}(t)=\sum_{n=1,3,5 \ldots . .} \frac{4 V_{3}^{\prime}}{n \pi} \cdot \sin \left(n\left(\omega_{s} t-\varphi_{13}\right)\right)
\end{array}\right.  \tag{15}\\
& \left\{\begin{array}{l}
i_{L 12}(t)-i_{L 12}(0)=\int_{0}^{t} \frac{v_{1}(t)-v_{2}^{\prime}(t)}{L_{12}} d t \\
i_{L 13}(t)-i_{L 13}(0)=\int_{0}^{t} \frac{v_{1}(t)-v_{3}^{\prime}(t)}{L_{13}} d t \\
i_{L 23}(t)-i_{L 23}(0)=\int_{0}^{t} \frac{v_{2}^{\prime}(t)-v_{3}^{\prime}(t)}{L_{23}} d t \\
i_{L x y}\left(\frac{\pi}{\omega_{s}}\right)=-i_{L x y}(0),(x, y=1,2,3)
\end{array}\right. \tag{16}
\end{align*}
$$

modules $M_{1} \sim M_{3}$ during one switching period is described in (20). Taking $P_{3}$ as an example, its expression is shown in (21). In addition, the product of the two sinusoids is shown in (22). According to the orthogonality of the trigonometric function, the second integral expression in (21) is equal to zero because $\mathrm{m} \neq \mathrm{n}$. The expression of the active power $P_{3}$ is derived in (23). Similarly, from (15), (19) and (20), the active powers $P_{i}(i=1,2,3)$ are finally derived in (24).

$$
\left\{\begin{align*}
& i_{L 12}(t)= \sum_{n=1,3,5, \ldots} \frac{4}{n^{2} \pi \omega_{s} L_{12}} \cdot\left[-V_{1} \cos \left(n \omega_{s} t\right)+V_{2}^{\prime} \cos \left(n \varphi_{12}\right) \cos \left(n \omega_{s} t\right)+V_{2}^{\prime} \sin \left(n \varphi_{12}\right) \sin \left(n \omega_{s} t\right)\right]  \tag{18}\\
& i_{L 13}(t)= \sum_{n=1,3,5, \ldots} \frac{4}{n^{2} \pi \omega_{s} L_{13}} \cdot\left[-V_{1} \cos \left(n \omega_{s} t\right)+V_{3}^{\prime} \cos \left(n \varphi_{13}\right) \cos \left(n \omega_{s} t\right)+V_{3}^{\prime} \sin \left(n \varphi_{13}\right) \sin \left(n \omega_{s} t\right)\right] \\
& i_{L 23}(t)= \sum_{n=1,3,5, \ldots} \frac{4 V_{2}^{\prime}}{n^{2} \pi \omega_{s} L_{23}} \cdot\left[-\cos \left(n \varphi_{12}\right) \cos \left(n \omega_{s} t\right)-\sin \left(n \varphi_{12}\right) \sin \left(n \omega_{s} t\right)-2 \cos \left(n \varphi_{12}\right)\right] \\
&+\sum_{n=1,3,5 . \ldots} \frac{4 V_{3}^{\prime}}{n^{2} \pi \omega_{s} L_{23}}\left[\cos \left(n \varphi_{13}\right) \cos \left(n \omega_{s} t\right)+\sin \left(n \varphi_{13}\right) \sin \left(n \omega_{s} t\right)+2 \cos \left(n \varphi_{13}\right)\right] \\
&\left\{\begin{array}{l}
i_{1}(t)=i_{L 12}(t)+i_{L 13}(t)=\sum_{n=1,3,5 \ldots \ldots} \frac{4}{n^{2} \pi \omega_{s}} \cdot \sqrt{A_{1}^{2}+B_{1}^{2}} \sin \left(n \omega_{s} t+\arctan \frac{A_{1}}{B_{1}}\right) \\
i_{2}^{\prime}(t)=-i_{L 12}(t)+i_{L 23}(t)=\sum_{n=1,3,5, \ldots} \frac{4}{n^{2} \pi \omega_{s}} \cdot\left(\sqrt{A_{2}^{2}+B_{2}^{2}} \sin \left(n \omega_{s} t+\arctan \frac{A_{2}}{B_{2}}\right)+C\right) \\
i_{3}^{\prime}(t)=-i_{L 13}(t)-i_{L 23}(t)=\sum_{n=1,3,5 \ldots . .} \frac{4}{n^{2} \pi \omega_{s}} \cdot\left(\sqrt{A_{3}^{2}+B_{3}^{2}} \sin \left(n \omega_{s} t+\arctan \frac{A_{3}}{B_{3}}\right)-C\right)
\end{array}\right.
\end{align*}\right.
$$

where

| $C=\frac{-2 V_{2}^{\prime} \cos \left(n \varphi_{12}\right)+2 V_{3}^{\prime} \cos \left(n \varphi_{13}\right)}{L_{23}}$ | $A_{1}=\frac{-V_{1}+V_{2}^{\prime} \cos \left(n \varphi_{12}\right)}{L_{12}}+\frac{-V_{1}+V_{3}^{\prime} \cos \left(n \varphi_{13}\right)}{L_{13}}$ |  |
| :---: | :---: | :---: |$\left.B_{1}=\frac{V_{2}^{\prime} \sin \left(n \varphi_{12}\right)}{L_{12}}+\frac{V_{3}^{\prime} \sin \left(n \varphi_{13}\right)}{L_{13}}\right)$

$$
\begin{gather*}
P_{i}=\frac{1}{T_{s}} \int_{0}^{T_{s}}\left(\sum_{n=1,3,5 \ldots} v_{i}(n t) i_{i}(n t)+\sum_{m \neq n} v_{i}(m t) i_{i}(n t)\right) d t  \tag{20}\\
P_{3}=\frac{1}{T_{s}} \int_{0}^{T_{s}}\left(\sum_{n=1,3,5 \ldots . .} \frac{16 V_{3}^{\prime}}{n^{3} \pi^{2} \omega_{s}} X_{3}(t)+\sum_{m \neq n} \frac{16 V_{3}^{\prime}}{m n^{2} \pi^{2} \omega_{s}} X_{3}(t)\right) d t \tag{21}
\end{gather*}
$$

where

$$
\begin{gather*}
X_{3}=\sin \left(m \omega_{s} t-m \varphi_{13}\right) \cdot\left(\sqrt{A_{3}^{2}+B_{3}^{2}} \cdot \sin \left(n \omega_{s} t+\arctan \frac{A_{3}}{B_{3}}\right)-C\right) . \\
\sin (a) \cdot \sin (b)=\frac{1}{2}(\cos (a-b)-\cos (a+b))  \tag{22}\\
P_{3}=\sum_{n=1,3,5 \ldots \ldots} \frac{8 V_{3}^{\prime} \sqrt{A_{3}^{2}+B_{3}^{2}}}{n^{3} \pi^{2} \omega_{s}} \cdot \cos \left(\arctan \frac{A_{3}}{B_{3}}+n \varphi_{13}\right)  \tag{23}\\
P_{1, m=n}=\sum_{n=1,3,5, \ldots} \frac{8 V_{1} \sqrt{A_{1}^{2}+B_{1}^{2}}}{n^{3} \pi^{2} \omega_{s}} \cdot \cos \left(\arctan \frac{A_{1}}{B_{1}}\right)  \tag{24}\\
P_{2, m=n}=\sum_{n=1,3,5 \ldots} \frac{8 V_{2}^{\prime} \sqrt{A_{2}^{2}+B_{2}^{2}}}{n^{3} \pi^{2} \omega_{s}} \cdot \cos \left(\arctan \frac{A_{2}}{B_{2}}+n \varphi_{12}\right) \\
P_{3, m=n}=\sum_{n=1,3,5 . \ldots} \frac{8 V_{3}^{\prime} \sqrt{A_{3}^{2}+B_{3}^{2}}}{n^{3} \pi^{2} \omega_{s}} \cdot \cos \left(\arctan \frac{A_{3}}{B_{3}}+n \varphi_{13}\right)
\end{gather*}
$$

If the active power for TAB is expressed by (25), then the power factor $\lambda=\cos (\phi)$ is used to indicate the phase differences between the voltage and current. The power factor $\lambda=\cos (\phi)$ can be divided into two situations: a) For the current and voltage with the same order harmonic component, the power factor $\lambda=\cos (\phi)$ is followed by (24). b) For the voltage and current with different order harmonic components, the active power is equal to 0 due to the orthogonality of the trigonometric function, which is $\cos (\phi)=0$.

$$
\left\{\begin{array}{l}
P=\sum_{n=1,3,5 \ldots} V(n) I(n) \cos (\phi)+\sum_{m \neq n} V(m) I(n) \cdot 0  \tag{25}\\
Q=\sum_{n=1,3,5 \ldots} V(n) I(n) \sin (\phi)+\sum_{m \neq n} V(m) I(n) \cdot 1
\end{array}\right.
$$

Similarly, the reactive power can also be classified into two categories: 1) the reactive power caused by the voltage and current components with the same frequency, and 2) the reactive power caused by the voltage and current components with different frequencies. Based on (24) and (25), the first category of the reactive power is derived as (26). When $m \neq n$, $\cos (\phi)=0$, while $\sin (\phi)=1$. The second category of the reactive power is shown in (27). Finally, the apparent power $S_{i}(i=1,2,3)$ of each active bridge module $M_{i}(i=1,2,3)$ is calculated in (28).

$$
\left\{\begin{array}{l}
Q_{1, m=n}=\sum_{n=1,3,5, \ldots} \frac{8 V_{1} \sqrt{A_{1}^{2}+B_{1}^{2}}}{n^{3} \pi^{2} \omega_{s}} \cdot \sin \left(\arctan \frac{A_{1}}{B_{1}}\right)  \tag{26}\\
Q_{2, m=n}=\sum_{n=1,3,5, \ldots} \frac{8 V_{2}^{\prime} \sqrt{A_{2}^{2}+B_{2}^{2}}}{n^{3} \pi^{2} \omega_{s}} \cdot \sin \left(\arctan \frac{A_{2}}{B_{2}}+n \varphi_{12}\right) \\
Q_{3, m=n}=\sum_{n=1,3,5, \ldots} \frac{8 V_{3}^{\prime} \sqrt{A_{3}^{2}+B_{1}^{2}}}{n^{3} \pi^{2} \omega_{s}} \cdot \sin \left(\arctan \frac{A_{3}}{B_{3}}+n \varphi_{13}\right)
\end{array}\right.
$$

$$
\begin{gather*}
\left\{\begin{array}{l}
Q_{1, m \neq n}=\sum_{m \neq n} \frac{8 V_{1} \sqrt{A_{1}^{2}+B_{1}^{2}}}{m n^{2} \pi^{2} \omega_{s}} \\
Q_{2, m \neq n}=\sum_{m \neq n} \frac{8 V_{2}^{\prime} \sqrt{A_{2}^{2}+B_{2}^{2}}}{m n^{2} \pi^{2} \omega_{s}} \\
Q_{3, m \neq n}=\sum_{m \neq n} \frac{8 V_{3}^{\prime} \sqrt{A_{3}^{2}+B_{3}^{2}}}{m n^{2} \pi^{2} \omega_{s}} \\
S_{i}=\sqrt{\sum_{m=n=1,3,5 \ldots} P_{i, m=n}^{2}+\sum_{m=n=1,3,5 \ldots} Q_{i, m=n}^{2}+\sum_{m \neq n=1,3,5 \ldots} Q_{i, m \neq n}^{2}}
\end{array}\right. \tag{27}
\end{gather*}
$$

## B. PPP-based Power Flow Analysis

According to (1) and the system parameters in TABLE II, the relationships among output currents $I_{o 1}$ and $I_{o 2}$ and module powers $P_{1} \sim P_{3}$, i.e., partial powers, are presented in Fig. 10(a), where the per-unit current and power are respectively 2.5 A and 2000W. From Fig. 10(a), $P_{1}$ is always positive, $P_{2}$ is negative, and $P_{3}$ is bidirectional, which is decided by load conditions. Their maximum absolute values are 200 W , which is much smaller than the maximum output power $P_{o 1}=800 \mathrm{~W}$, $P_{o 2}=1200 \mathrm{~W}$ and the maximum input power $P_{i 1}=2000 \mathrm{~W}$. In addition, Fig. 10(b) also demonstrates the partial power $P_{p}$ and the total power $P_{t}$ under different output currents $I_{o 1}$ and $I_{o 2}$ based on (2). Note that the partial power $P_{p}$ processed by modules is effectively reduced in comparison with the total power $P_{t}$ for any load condition.


Fig. 10 Relationships among $I_{o 1}, I_{o 2}$ and different power flows: (a) $P_{1} \sim P_{3}$ processed by modules $M_{1} \sim M_{3}$, and (b) partial power $P_{p}$ and total power $P_{t}$.

In addition, according to (24), (26) and (28), both the sum of the partial active-power $P_{p}=P_{1}+P_{2}+P_{3}$ and partial apparent power $S_{p}=S_{1}+S_{2}+S_{3}$ processed by three isolated modules $M_{1} \sim M_{3}$ can be calculated after letting $m$ and $n$ take the values 1,3 , and 5 , respectively. Subsequently, the curves of the partial power ratios $P_{p} / P_{t}$ and $S_{p} / P_{t}$ changing with the load currents $I_{o 1}$ and $I_{o 2}$
are shown as in Fig. 11. To verify the theoretical analysis above, simulation results from PSIM are also presented in Fig. 11, showing that the theoretical results are in good agreement with the simulated results. In addition, the results calculated by Fourier series in Fig. 11(a) also match Fig. 3. Comparing Fig. 11(a) and Fig. 11(b), the changing trends of the active-power ratio $P_{p} / P_{t}$ and apparent-power ratio $S_{p} / P_{t}$ are similar. Therefore, the design consideration is similar.


$$
\text { (b) } S_{p} / P_{t}
$$



Fig. 11 Theoretical and simulated results of the power ratios changing with the load currents $I_{o 1}$ and $I_{o 2}$ : (a) $P_{p} / P_{t}$ and (b) $S_{p} / P_{t}$.

## C. Hardware Design Considerations

First, the current and voltage stresses are calculated. Due to symmetry, the absolute values of inductor currents $i_{L i}(t)$ and $i_{L i}\left(t+T_{s} / 2\right)$ are equal, i.e., $i_{L i}\left(t_{0}\right)=-i_{L i}\left(t_{6}\right)$ in Fig. 6. According to (11), the inductor currents at $t_{0}$ are calculated in (29). Based on (29) and (7), the RMS currents $I_{s i 1, \text { rms }}$ of switches $S_{i 1}(i=1,2,3)$ are calculated in (30). In addition, the corresponding voltage stresses are depicted in (31). In each active bridge module $M_{i}(i=1,2,3)$, the current and voltage stresses of the four switches are equal. Accordingly, MOSFET IPW60R180P7 is chosen for switches $S_{i 1} \sim S_{i 4}$ in the prototype circuit.

$$
\begin{gather*}
\left\{\begin{array}{l}
i_{L 1}\left(t_{0}\right)=\left(-\frac{1}{3} \varphi_{12}-\frac{1}{3} \varphi_{13}\right) \cdot \frac{V_{1} T_{s}}{2 \pi L_{1}} \\
i_{L 2}\left(t_{0}\right)=\left(\frac{2}{3} \varphi_{12}-\frac{1}{3} \varphi_{13}\right) \cdot \frac{V_{2} T_{s}}{2 \pi L_{2}} \\
i_{L 3}\left(t_{0}\right)=\left(-\frac{1}{3} \varphi_{12}+\frac{2}{3} \varphi_{13}\right) \cdot \frac{V_{3} T_{s}}{2 \pi L_{3}}
\end{array}\right. \\
I_{s i 1, r m s}=\sqrt{\frac{3 \pi-2 \varphi_{12}}{6 \pi} i_{L i}^{2}\left(t_{0}\right)+\frac{\varphi_{12}}{6 \pi} i_{L i}^{2}\left(t_{1}\right)+\frac{2 \varphi_{13}-\varphi_{12}}{6 \pi} i_{L i}\left(t_{0}\right) i_{L i}\left(t_{1}\right)}  \tag{29}\\
\left\{\begin{array}{l}
V_{s 11}=V_{i 1}-V_{o 1} \\
V_{s 21}=V_{o 2}-V_{i 1} \\
V_{s 31}=V_{i 1}
\end{array}\right. \tag{30}
\end{gather*}
$$

The working areas and peak current are also considered. According to (13), (14) and the system parameters in TABLE II, the available ranges of power flows $\left(P_{1}, P_{2}\right)$ in terms of the series inductance $L_{1}$ are generated in Fig. 12, where $P_{1}$ is always positive, while $P_{2}$ is negative. From Fig. 12, the smaller the inductance $L_{1}$ is, the larger the power range. On the other hand, the maximum absolute inductor currents $i_{L 1, \text { max }} \sim i_{L 3, \text { max }}$ in terms of series inductance $L_{1}$ are also depicted in Fig. 13 according to (32) and (35). They are decreased with the decrement of $L_{1}$, which adversely affects the realization of the ZVS operation of switches. Therefore, the series inductance $L_{1}$ is finally designated as $20 \mu \mathrm{H}$ after a comprehensive consideration of both the power range and ZVS operation.


Fig. 12 The available range of power flow $\left(P_{1}, P_{2}\right)$ in terms of inductance $L_{1}$.


Fig. 13 The maximum absolute inductor currents $i_{L 1, \text { max }} \sim i_{L 3, \text { max }}$ in terms of series inductance $L_{1}$.

Finally, ZVS operation is designed. From the analysis in section III, switches $S_{11}, S_{12}, S_{23}, S_{24}, S_{33}$ and $S_{34}$ are turned on before $t_{1}$. The inductor current $i_{L 3}\left(t_{1}\right)$ is calculated in (32) based on (7) and (29), which is negative. When $S_{33}$ and $S_{34}$ are turned off at $t_{1}$, the inductor $L_{3}$ will resonate with the parasitic capacitors $C_{s 31} \sim C_{s 34}$, as shown in Fig. 14. The capacitors $C_{s 31} \sim C_{s 32}$ are discharged, while $C_{s 33} \sim C_{s 34}$ are charged. From Fig. 14 , the expression of $u_{3}(t)$ during $t_{1}$ to $t_{2}$ is calculated in (33) based on (4). Combining with (8), the drain-to-source voltage $v_{s 31}(t)$ is calculated in (34).


Fig. 14 Resonance process during $t_{1} \sim t_{2}$.

$$
\begin{gather*}
i_{L 3}\left(t_{1}\right)=-\frac{1}{3} \varphi_{12} \cdot \frac{V_{3} T_{s}}{2 \pi L_{3}}<0  \tag{32}\\
u_{3}(t)=\frac{N_{3}}{3}\left(V_{1}-\frac{V_{2}}{N_{2}}+\frac{-v_{s 31}(t)+V_{3}-v_{s 32}(t)}{N_{3}}\right)  \tag{33}\\
v_{s 31}(t)=A_{13} \cos \left(\omega_{3}\left(t-t_{1}\right)\right)+A_{23} \sin \left(\omega_{3}\left(t-t_{1}\right)\right)+A_{33} \tag{34}
\end{gather*}
$$

where $A_{13}=\frac{V_{3} / 3+\mathrm{N}_{3} V_{1} / 3}{C_{s} L_{3} \omega_{3}^{2}}, \quad A_{23}=\frac{i_{L 3}\left(t_{1}\right)}{\omega_{3} C_{s}}, A_{33}=V_{3}-A_{13}$, $\omega_{3}=\sqrt{4 /\left(3 C_{s} L_{3}\right)}$.

Similarly, the inductor currents $i_{L 2}\left(t_{3}\right)$ and $i_{L 1}\left(t_{5}\right)$ are calculated in (35) so that they are negative and positive, respectively. Therefore, resonances also occur in modules $M_{2}$ and $M_{1}$ during $t_{3} \sim t_{4}$ and $t_{5} \sim t_{6}$, respectively. During resonances,
the parasitic capacitors $C_{s 21}$ and $C_{s 13}$ are discharged, and the corresponding drain-to-source voltages $v_{s 21}(t)$ and $v_{s 13}(t)$ are also calculated in (36).

$$
\begin{gather*}
\left\{\begin{array}{l}
i_{L 2}\left(t_{3}\right)=\left(-\frac{2}{3} \varphi_{12}+\frac{1}{3} \varphi_{13}\right) \cdot \frac{V_{2} T_{s}}{2 \pi L_{2}}<0 \\
i_{L 1}\left(t_{5}\right)=\left(\frac{1}{3} \varphi_{12}+\frac{1}{3} \varphi_{13}\right) \cdot \frac{V_{1} T_{s}}{2 \pi L_{1}}>0
\end{array}\right.  \tag{35}\\
\left\{\begin{array}{l}
v_{s 21}(t)=A_{12} \cos \left(\omega_{2}\left(t-t_{3}\right)\right)+A_{22} \sin \left(\omega_{2}\left(t-t_{3}\right)\right)+A_{32} \\
v_{s 13}(t)=A_{11} \cos \left(\omega_{1}\left(t-t_{5}\right)\right)+A_{21} \sin \left(\omega_{1}\left(t-t_{5}\right)\right)+A_{31}
\end{array}\right. \tag{36}
\end{gather*}
$$

where $\quad A_{12}=\frac{V_{2} / 3+\mathrm{N}_{2} V_{1}}{C_{s} L_{2} \omega_{2}^{2}}, A_{22}=\frac{i_{L 2}\left(t_{3}\right)}{\omega_{2} C_{s}}, A_{32}=V_{2}-A_{12}$, $A_{11}=0, A_{21}=\frac{-i_{L 1}\left(t_{5}\right)}{\omega_{1} C_{s}}, A_{31}=V_{1}, \omega_{2}=\sqrt{\frac{4}{3 C_{s} L_{2}}}, \omega_{1}=\sqrt{\frac{4}{3 C_{s} L_{1}}}$.

According to (34), (36) and the system parameters in TABLE II, the drain-to-source voltages $v_{s 13}(t), v_{s 21}(t)$ and $v_{s 31}(t)$ are shown in Fig. 15. From Fig. 15, both $v_{s 13}(t)$ and $v_{s 21}(t)$ can drop to zero quickly. After they drop to zero, their body diodes will conduct; therefore, the ZVS turn-on of switches $S_{13}$ and $S_{21}$ is realized if their drive signals turn positive. Nevertheless, $v_{s 31}(t)$ decreases slowly and requires a large amount of time to reach zero, which is much larger than the practical dead time. To improve this, an inductor $L_{4}$ is added to connect with the drain terminals of switches $S_{32}$ and $S_{34}$. Accordingly, the resonance expression of $v_{s 31}(t)$ is changed from (34) to (37), where $i_{L 4}\left(t_{1}\right)<0$. Because $B_{1}>A_{13}$, while $B_{2}<A_{23}$, $v_{s 31}(t)$ drops faster after adding the parallel inductor $L_{4}$, which is also shown in Fig. 15. The ZVS turn-on of switch $S_{31}$ can also be obtained. With the decrease in $L_{4}$, the resonance time will be reduced, but the extra conduction losses will increase. Therefore, the inductance $L_{4}$ is finally designed as $300 \mu \mathrm{H}$ after establishing a trade-off between the ZVS realization and conduction loss.


Fig. 15 Resonance waveforms of drain-to-source voltages $v_{s 13}, v_{s 21}$ and $v_{s 31}$.

$$
\begin{equation*}
v_{s 31}(t)=B_{1} \cos \left(\omega_{3}\left(t-t_{1}\right)\right)+B_{2} \sin \left(\omega_{3}\left(t-t_{1}\right)\right)+B_{3} \tag{37}
\end{equation*}
$$

where $B_{1}=\left(N_{3} V_{1} / 3+\left(1 / 3+L_{3} / L_{4}\right) V_{3}\right) /\left(L_{3} C_{3} \omega_{3}^{2}\right), B_{3}=V_{3}-B_{1}$,

$$
B_{2}=\left(i_{L 3}\left(t_{1}\right)+i_{L 4}\left(t_{1}\right)\right) /\left(\omega_{3} C_{s}\right), i_{L 4}\left(t_{1}\right)=-V_{3} T_{s} /\left(4 L_{4}\right)
$$

$$
\left\{\begin{array}{l}
\left\langle i_{1}(t)\right\rangle_{T_{s}}=f_{1}\left(v_{o 2}, v_{i 1}, \phi_{12}, \phi_{13}\right)=\frac{\left\langle v_{o 2}(t)-v_{i 1}(t)\right\rangle_{T_{s}}}{N_{2} \omega_{s} L_{12}} \cdot \frac{\phi_{12}(t) \pi}{180^{\circ}} \cdot\left(1-\frac{\phi_{12}(t)}{180^{\circ}}\right)+\frac{\left\langle v_{i 1}(t)\right\rangle_{T_{s}}}{N_{3} \omega_{s} L_{13}} \cdot \frac{\phi_{13}(t) \pi}{180^{\circ}} \cdot\left(1-\frac{\phi_{13}(t)}{180^{\circ}}\right)  \tag{39}\\
\left\langle i_{2}(t)\right\rangle_{T_{s}}=f_{2}\left(v_{o 1}, v_{i 1}, \phi_{12}, \phi_{13}\right)=-\frac{\left\langle v_{i 1}(t)-v_{o 1}(t)\right\rangle_{T_{s}}}{N_{2} \omega_{s} L_{12}} \cdot \frac{\phi_{12}(t) \pi}{180^{\circ}} \cdot\left(1-\frac{\phi_{12}(t)}{180^{\circ}}\right)+\frac{\left\langle v_{i 1}(t)\right\rangle_{T_{s}} \pi}{N_{2} N_{3} \omega_{s} L_{23}} \cdot\left|\frac{\phi_{13}(t)}{180^{\circ}}-\frac{\phi_{12}(t)}{180^{\circ}}\right| \cdot\left(1-\left|\frac{\phi_{13}(t)}{180^{\circ}}-\frac{\phi_{12}(t)}{180^{\circ}}\right|\right)
\end{array}\right.
$$

$$
\begin{align*}
& \left\{\begin{array}{l}
C_{o 1} \frac{d \hat{v}_{o 1}(t)}{d t}+\frac{\hat{v}_{o 1}(t)}{R_{1}}=k_{1} \hat{v}_{o 2}(t)+k_{2} \hat{\phi}_{12}(t)+k_{3} \hat{\phi}_{13}(t) \\
C_{o 2} \frac{d \hat{v}_{o 2}(t)}{d t}+\frac{\hat{v}_{o 2}(t)}{R_{2}}=-m_{1} \hat{v}_{o 1}(t)-m_{2} \hat{\phi}_{12}(t)-m_{3} \hat{\phi}_{13}(t)
\end{array}\right.  \tag{40}\\
& \left\{k_{1}=\left.\frac{d f_{1}}{d v_{o_{2}}}\right|_{\nu_{2}=V_{o_{22}}}=\frac{\pi}{N_{2} \omega_{s} L_{12}} \cdot\left(\frac{\Phi_{12}}{180}-\frac{\Phi_{12}^{2}}{180^{2}}\right)=m_{1}\right. \\
& k_{2}=\left.\frac{d f_{1}}{d \phi_{12}}\right|_{\phi_{2}=\Phi_{12}}=\frac{\left(V_{o 2}-V_{i 1}\right) \pi}{N_{2} \omega_{s} L_{12}} \cdot\left(\frac{1}{180}-\frac{2 \Phi_{12}}{180^{2}}\right) \\
& \text { where }\left\{k_{3}=\left.\frac{d f_{1}}{d \phi_{1}}\right|_{\phi_{3}=\Phi_{13}}=\frac{V_{i 1} \pi}{N_{3} \omega_{s} L_{3}} \cdot\left(\frac{1}{180^{\circ}}-\frac{2 \Phi_{13}}{180^{2}}\right)\right. \\
& m_{2}=\left.\frac{d f_{2}}{d \phi_{12}}\right|_{\alpha_{2}=\Phi_{12}}=\frac{\left(V_{o 1}-V_{i 1}\right) \pi}{N_{2} \omega_{s} L_{12}} \cdot\left(\frac{1}{180^{-}}-\frac{2 \Phi_{12}}{180^{2}}\right)+m_{3} \\
& m_{3}=\left.\frac{d f_{2}}{d \phi_{13}}\right|_{\phi_{3}=\Phi_{13}}=\frac{V_{i 1} \pi}{N_{2} N_{3} \omega_{3} L_{23}} \cdot\left(\frac{1}{180^{-}}-\frac{2\left(\Phi_{13}-\Phi_{12}\right)}{180^{2}}\right) \\
& \left\{\begin{array}{l}
\hat{v}_{o 1}(s)=G_{v d 1} \hat{\phi}_{12}(s)+G_{v d 13} \hat{\phi}_{13}(s) \\
\hat{v}_{o 2}(s)=G_{v d 22} \hat{\phi}_{12}(s)+G_{v d 23} \hat{\phi}_{13}(s)
\end{array}\right.  \tag{41}\\
& \left\{G_{v d 12}=\hat{v}_{o 1}(s) / \hat{\phi}_{12}(s)=\frac{A_{1} B_{2}+A_{2} B_{0}}{A_{0} B_{0}-A_{1} B_{1}}\right. \\
& G_{v d 13}=\hat{\nu}_{o 1}(s) / \hat{\phi}_{13}(s)=\frac{A_{1} B_{3}+A_{3} B_{0}}{A_{0} B_{0}-A_{1} B_{1}}  \tag{42}\\
& G_{v d 22}=\hat{v}_{o 2}(s) / \hat{\phi}_{12}(s)=\frac{A_{2} B_{1}+A_{0} B_{2}}{A_{0} B_{0}-A_{1} B_{1}} \\
& G_{v d 23}=\hat{v}_{o 2}(s) / \hat{\phi}_{13}(s)=\frac{A_{3} B_{1}+A_{0} B_{3}}{A_{0} B_{0}-A_{1} B_{1}}
\end{align*}
$$

where $\quad A_{0}=s C_{o 1}+1 / R_{1}, \quad A_{i}=k_{i}(i=1,2,3), \quad B_{0}=s C_{o 1}+1 / R_{1}, \quad B_{i}=-$ $m_{i}(i=1,2,3)$.
The Bode plots of the control-to-output transfer functions are shown in Fig. 17(a) based on (42) and the system parameters in Table II. In addition, Fig. 17(b) also illustrates the Bode plots of the transfer functions from simulation software PSIM, which is basically consistent with the one obtained by the theoretical analysis in Fig. 17(a).


Fig. 17 Bode plots of the control-to-output transfer functions $G_{v d 12}, G_{v d 13}, G_{v d 22}$ and $G_{v d 23}$ obtained by (a) the theoretical analysis and (b) the simulation.
Subsequently, the control scheme is designed in Fig. 18, where constant voltage controls of $V_{o 1}$ and $V_{o 2}$ depend on $\phi_{12}$ and $\phi_{13}$, respectively, with separate compensators. Note that the phase of $G_{v d 23}$ is larger than $0^{\circ}$ from Fig. 17; therefore, the voltage error of the control system of output $V_{o 2}$ is designed as $v_{o 2}-V_{\text {ref } 2}$ rather than $V_{\text {ref } 2}-v_{o 2}$ to realize negative feedback closed loop control. According to the control-to-output transfer
functions in Fig. 17 and the control scheme in Fig. 18, the compensators $G_{c 1}$ and $G_{c 2}$ are designed in (43). The open-loop $G_{o p 1}=G_{v d 12} \times G_{c 1}$ and $-G_{o p 2}=-G_{v d 23} \times G_{c 2}$ are presented in Fig. 19. From Fig. 19, both the magnitude values of $G_{o p 1}$ and $G_{o p 2}$ at 0 Hz are large due to their $-20 \mathrm{~dB} / \mathrm{dec}$ slopes. This indicates the errors between the real and reference output voltages can be eliminated. Moreover, the phase margins of $G_{o p 1}$ and $G_{o p 2}$ are approximately $90^{\circ}$, ensuring the stability of the closed-loop system. In addition, their crossover frequencies are approximately 300 Hz , which contributes to quick responses. In other words, the closed-loop system obtains both good steadystate accuracy and dynamic performance after adding the compensators.


Fig. 18 The closed-loop control system with separate compensators.

(b)

Fig. 19 Bode plots: (a) $G_{v d 12}, G_{c 1}, G_{o p 1}$ and (b) $-G_{v d 23}, G_{c 2},-G_{o p 2}$.

## E. Comparison and Summary

A comparison is made among the typical TAB DC-DC converter [31, 32], the existing PPP three-port DC-DC converter based on TAB [33] and the proposed example active bridge module-based PPP-SIDO DC-DC converter. Their topologies are depicted in Fig. 20. In a conventional TAB converter, as shown in Fig. 20(a), this active bridge modules
need to process the full power of the respective ports. The active bridge modules in the proposed PPP-SIDO converter only need to convert the partial power caused by voltage or current differences, which is depicted in (1). This is because these modules are series/parallel connected with output/input ports in the proposed topology, as depicted in Fig. 20(c). Taking the parameters in TABLE II as an example, the power processed by each module in two topologies can be calculated in TABLE III. It is obvious that the voltage/current stresses of both the semiconductors and magnetic components in the three modules of the proposed topology (c) are successfully reduced, and the small power rating components can be chosen so that the volume and costs can be reduced. Moreover, the conduction losses are reduced, which contributes to a high efficiency. In addition, the proposed structure can be further expanded to multiport while maintaining PPP according to Fig. 2. In contrast, topology (a) must process full power, and topology (b) can only realize PPP between two ports. Finally, the overall comparison among the three topologies is summarized in Table IV.


Fig. 20 Active bridge module-based topologies: (a) typical $\mathrm{TAB}^{[31,32]}$, (b) the existing PPP three-port DC-DC converter based on TAB ${ }^{[33]}$, and (c) the proposed example active bridge module-based PPP-SIDO DC-DC converter. Table III
STRESS COMPARISON OF THE THREE MODULES BETWEEN TOPOLOGIES (A) AND (C) IN Fig. 20

| Module Stresses | Topology (a) | Topology (c) |
| :---: | :---: | :---: |
| Power (W) | $P_{1}=800$ | $P_{1}=200$ |
|  | $P_{2}=1200$ | $P_{2}=200$ |
|  | $P_{3}=2000$ | $P_{3}=0$ |
| Voltages(V) | $V_{1}=320$ | $V_{1}=80$ |
|  | $V_{2}=480$ | $V_{2}=80$ |
|  | $V_{3}=400$ | $V_{3}=400$ |
| Current (A) | $I_{1}=2.5$ | $I_{1}=2.5$ |
|  | $I_{2}=2.5$ | $I_{2}=2.5$ |
|  | $I_{3}=5$ | $I_{3}=0$ |

Table IV
COMPARISON OF ACTIVE BRIDGE MODULE-BASED TOPOLOGIES IN FIG. 20

| Topology | Ability to <br> Realize PPP | Module <br> Stress | Costs | Power <br> Density |
| :---: | :---: | :---: | :---: | :---: |
| (a) | No | Large | Large | Low |
| (b) | Only two-port | Medium | Medium | Medium |
| (c) | Multiport | Small | Small | High |

## V. EXPERIMENTAL VERIFICATION

Based on the system parameters and design in section IV, a prototype circuit is set up, as shown in Fig. 21. The experimental waveforms of port voltages $V_{i 1}, V_{o 1}, V_{o 2}$, and module voltages $V_{1} \sim V_{3}$ of $M_{1} \sim M_{3}$ are depicted in Fig. 22. From Fig. 22, the output voltages $V_{o 1}$ and $V_{o 2}$ are regulated to 320 V and 480 V , respectively. The module voltage $V_{3}$ of $M_{3}$ is equal


Fig. 21 Photograph of the prototype circuit.


Fig. 22 Experimental waveforms of port voltages $V_{i 1}, V_{o 1}, V_{o 2}$, and module voltages $V_{1} \sim V_{3}$.
to the input voltage $V_{i 1}=400 \mathrm{~V}$. The module voltages $V_{1,2}$ of $M_{1,2}$ are 80 V , which is the difference between the input and output voltages. Therefore, the voltage stresses of modules $M_{1,2}$ are effectively reduced in the proposed converter.

In addition, Fig. 23~Fig. 25 demonstrate key experimental waveforms and ZVS realization under three conditions of ( $I_{o 1}$, $I_{o 2}$ ), which are $(2.5 \mathrm{~A}, 2.5 \mathrm{~A}),(2.5 \mathrm{~A}, 0.5 \mathrm{~A})$ and $(0.5 \mathrm{~A}, 2.5 \mathrm{~A})$, respectively. According to Fig. 23(a)~Fig. 25(a), the phase shifts $\phi_{12}$ and $\phi_{13}$ are $\left(63.9^{\circ}, 31.95^{\circ}\right),\left(37^{\circ}, 54.7^{\circ}\right)$ and $\left(37^{\circ}\right.$, $17.6^{\circ}$ ), respectively, which coincide well with Fig. 9. Moreover, with the measured values of $I_{i 1}, I_{o 1}$, and $I_{o 2}$, the average current $I_{3}$ of module $M_{3}$, which is equal to $I_{i 1}-I_{o 1}-I_{o 2}$, is $0 \mathrm{~A},-0.4 \mathrm{~A}$ and 0.4 A under three load conditions. Therefore, the current stress of module $M_{3}$ is also reduced in the proposed converter when compared with the conventional TAB converter.

Moreover, from Fig. 23(b), the inductor current $i_{L 1}$ is negative before switch $S_{11}$ is turned on. Hence, the parasitic capacitor of switch $S_{11}$ will be discharged, and its drain-tosource voltage $v_{s 11}$ will be decreased after $S_{13}$ is turned off. When $v_{s 11}$ decreases to zero, the inductor current $i_{L 1}$ will flow through the source terminal to the drain terminal of switch $S_{11}$. Afterward, the ZVS operation of $S_{11}$ is achieved with its drive signal becoming positive. Similarly, from Fig. 23(c)~ Fig. 23(d), Fig. 24(b)~Fig. 24(d) and Fig. 25(b)~Fig. 25(d), all the switches can successfully achieve ZVS operation under these three load conditions. Comparing Fig. 23~Fig. 25, the maximum absolute value of the inductor currents $i_{L 1}$ is increased with the rising load currents $I_{o 1}$; therefore, the ZVS operation of switches in module $M_{1}$ is correspondingly easier. Module $M_{2}$ obtains a similar trend when $I_{o 2}$ increases. On the other hand, the ZVS


Fig. 23 Key experimental waveforms under load conditions $I_{o 1}=2.5 \mathrm{~A}, I_{o 2}=2.5 \mathrm{~A}$.


Fig. 24 Key experimental waveforms under load conditions $I_{o 1}=2.5 \mathrm{~A}, I_{o 2}=0.5 \mathrm{~A}$.


Fig. 25 Key experimental waveforms under load conditions $I_{o 1}=0.5 \mathrm{~A}, I_{o 2}=2.5 \mathrm{~A}$.
operation of switches in module $M_{3}$ is almost unaffected by load conditions because it is mainly influenced by the additional inductor current $i_{L 4}$ rather than $i_{L 3}$.

In addition, the dynamic response under the output resistance variation is presented in Fig. 26. From Fig. 26, as the output resistances change, the output voltages fluctuate at first and they will return to the rated values quickly.


Fig. 26 Dynamic response when output resistance $R_{1}$ is changed between $256 \Omega$ and $128 \Omega$, and $R_{2}$ is changed between $384 \Omega$ and $192 \Omega$, respectively.

According to the measured module voltages $V_{1 \sim 3}$ and average module current $I_{1 \sim 3}$, the corresponding powers $\left(P_{1}, P_{2}, P_{3}\right)$ being processed by three modules $M_{1} \sim M_{3}$ are equal to (200W, -200 W , $0 \mathrm{~W}),(200 \mathrm{~W},-40 \mathrm{~W},-160 \mathrm{~W})$ and (40W, $-200 \mathrm{~W}, 160 \mathrm{~W}$ ), respectively, under three load conditions $(2.5 \mathrm{~A}, 2.5 \mathrm{~A}),(2.5 \mathrm{~A}$, $0.5 \mathrm{~A})$ and $(0.5 \mathrm{~A}, 2.5 \mathrm{~A})$. They only account for $10 \%, 19.23 \%$ and $14.7 \%$ of the practical power of the input and output ports, and the remaining power is transferred from input to output directly. Therefore, their corresponding efficiencies are high at $98.87 \%, 98.40 \%$ and $98.86 \%$, respectively. In the prototype circuit, the power loss is mainly caused by conduction losses of both semiconductors and magnetic components, while switching loss and magnetic core loss can almost be ignored entirely due to the realization of ZVS and small magnetizing current. To justify the efficiencies, the detailed loss analysis of three load conditions $\left(I_{o 1}, I_{o 2}\right)=(2.5 \mathrm{~A}, 2.5 \mathrm{~A}) /(2.5 \mathrm{~A}, 0.5 \mathrm{~A}) /(0.5 \mathrm{~A}$, 2.5 A ) is conducted as follows:

According to Fig. 6, (30) and the system parameters in TABLE II, we can obtain the root mean square (RMS) current values of switches $I_{s i 1, \text { rms }}(i=1,2,3)$ under three load conditions in (44). The RMS values of the series and parallel connected inductor currents $I_{L i, \mathrm{rms}}(i=1,2,3)$ and $I_{L 4, \mathrm{rms}}$ can also be obtained in (45) and (46), respectively.

$$
\begin{gather*}
\left\{\begin{array}{c}
I_{s 11, m s}=2.21 A / 2.17 A / 0.62 A \\
I_{s 21, \text { mss }}
\end{array}=2.21 A / 0.62 A / 2.17 A\right.  \tag{44}\\
I_{s 31, m s}=0.12 A / 0.34 A / 0.34 A  \tag{45}\\
I_{L i, m s}=\sqrt{2} \cdot I_{s i l, m s}  \tag{46}\\
I_{L 4, r m s}=\frac{1}{\sqrt{3}} \cdot \frac{V_{3} T_{s}}{4 L_{4}}=1.92 A
\end{gather*}
$$

Based on the datasheet of MOSFET IPW60R180P7, the drain-to-source on-state resistance is $R_{d s}=0.18 \Omega$. Therefore, the conduction losses of switches under three load conditions are calculated in (47). In addition, because the three windings of the transformer are in series with inductors $L_{1} \sim L_{3}$, their sums of
resistances are $R_{m 1}=0.33 \Omega, R_{m 2}=0.31 \Omega$, and $R_{m 3}=6.98 \Omega$, respectively. The resistance of the parallel connected inductor $L_{4}$ is $R_{L 4}=0.74 \Omega$. The conduction losses of the magnetic components under three load conditions are obtained in (48). According to (47) and (48), the sum of the conduction losses is $P_{c, \text { loss }}=17.81 \mathrm{~W} / 13.42 \mathrm{~W} / 13.25 \mathrm{~W}$. We can thus obtain estimated efficiencies of $99.11 \% / 98.71 \% / 99.03 \%$. Compared with the measured efficiencies of $98.87 \% / 98.40 \% / 98.86 \%$, the estimated efficiencies are basically consistent with the measured efficiencies. Their small differences are caused by other losses and measurement errors.

$$
\begin{align*}
& P_{s, l o s s}=4 \cdot R_{d s} \cdot\left[I_{s 1, r m s}^{2}+I_{s 2, r m s}^{2}+\left(I_{s 3, r m s}+\frac{1}{\sqrt{2}} I_{L 4, r m s}\right)^{2}\right]  \tag{47}\\
&=8.62 \mathrm{~W} / 5.74 \mathrm{~W} / 5.74 \mathrm{~W} \\
& P_{L, l o s s}= \sum_{i=1}^{3} R_{m i} I_{L i, r m s}^{2}+R_{L 4} I_{L 4, r m s}^{2}  \tag{48}\\
&=9.19 \mathrm{~W} / 7.68 \mathrm{~W} / 7.51 \mathrm{~W}
\end{align*}
$$

In addition, the efficiencies over the full-load range are measured and presented in Fig. 27. Owing to the realization of partial power processing, power ratings over the whole load range are small; therefore, the losses are relatively small. As a result, the measured efficiencies are high over the whole load range, and the minimum efficiency reaches $98.13 \%$.


Fig. 27 Measured efficiencies of the proposed example active bridge modulebased PPP-SIDO DC-DC converter over the whole load range.

## VI. Conclusion

In this paper, a generalized PPP multiport DC-DC architecture with radial module connections is proposed for SIMO and MISO applications. This successfully expands PPP from two ports to multiple ports. In the proposed architecture, only the partial power generated by voltage or current differences between input and output will be processed by modules, while the other power will be transmitted directly. Therefore, a high power density and high global efficiency are obtained. Moreover, the magnetically linked modules can be implemented by using many various isolated converters. An example PPP-SIDO DC-DC converter with three active bridge modules $M_{1} \sim M_{3}$ is analyzed in detail in the paper, to gain a better understanding. The voltage stresses are effectively reduced in modules $M_{1} \sim M_{2}$, while the current stress is reduced in $M_{3}$. Therefore, a small power rating and high efficiency are obtained, which is effectively verified by the experimental results.

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